# ragni-cas - A Pure Ruby Automatic Differentiation Library for Fast Prototyping of Interfaces

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#### Abstract

Ca. 100 words

Keywords: CAS, code-generation, Ruby

### 1. Motivation and significance

- Ruby is a purely object-oriented scripting language that allows to express
- several programming paradigms. It was designed in the mid-1990s by Yuki-
- 4 hiro Matsumoto (also known as *Matz*), and it is internationally standardized
- 5 since 2012 as ISO/IEC 30170.
- With the advent of the *Internet of Things*, a written from scratch version
- of the Ruby interpreter called mRuby (eMbedded Ruby) has been published
- 8 on GitHub by Matsumoto in 2014. The new interpreter is a lightweight
- 9 implementation aimed at both low power devices and personal computer
- that complies with the standard. mRuby has a completely new API, and
- it is designed to be embedded in a complex project as a front-end interface
- e.g. a numerical optimization suite may use mRuby to get problem input
- 13 definitions.
- The Ruby code-base exposes a a large set of utilities in core and standard
- library. This set of tool can be furthermore expanded through libraries, also

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- known as *gems*. Even the high number of gems deployed and available, there is no complete library that implements a **symbolic automatic differenti-**ation (AD) engine that also handles some basic computer algebra routines that is cross compatible with all the different *Ruby* interpreter.
- Ruby has matured its fame as a web oriented language because of its capabilities web templete system and in general for processing complex content. This characteristic allows to efficiently generate code in other languages, and
- 23 given such a gem, it is really easy to develop rapidly a specific code genera-24 tor for well known software — e.g. IPOPT.
- The library that is described in this work, is a gem implemented in pure Ruby code and thus compatible with all interpreter that complies with the standard, that is able to perform symbolic AD and some simple computer algebra operations. In particular the library aims at:
  - be an instrument for rapid development of prototype interface for numerical algorithms including the mRuby engine or exporting generated code that can be in different languages;

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- the library allows to rapidly test workaround for numerical issues particular to certain problems, by changing on request how the code is exported, and how basic functions are formulated;
- long term impact, quite ambitious, of creating a complete open-source

  CAS system for the *Ruby* language, that must be compatible with all

  the interpreters that comply with the standard.
- This is not the first gem that is able to perform AD. The available computer algebra library for Ruby are:
- *Rucas* gem at early stage and with discontinued developing status; it implements basic simplification routines. There is no AD method, but it

is one of the milestones.

Symengine is a wrapper for the C++ library symengine. The back-end library is very complete, but it is compatible only with the mainstream Ruby interpreter. At the moment, the SciRuby project reports the gem as broken, and removed it from its codebase. From a direct test, when performing AD of a function, the engine returns always nil.

Datamelt probably the most complete choice, is a Java library and compatible with one particular Ruby virtual machine, called JRuby.

### 50 2. Software description

51 2.1. Software Architecture

ragni-cas is an object oriented AD gem that supports some simple computer algebra routines such as simplifications and substitutions. When gem is required, automatically overloads some methods of the Fixnum and Float classes, to make them compatible whit symbolic objects.

Each symbolic function is an object modeled by a class. The class inherits from a common virtual ancestor: CAS::Op(operation). An operation encapsulates sub-operations recursively, building a linked list, that can be considered as the mathematical equivalent of function composition:

$$(f \circ g) \tag{1}$$

When a new operation is created, it is appended to the linked list, creating a graph that can have an arbitrary number of branches. The number of branches are determined by the parent container class of the current symbolic function. There are three possible containers. Single argument functions — e.g.  $\sin(\cdot)$  — have as closest parent the CAS::Op class, that links to one

sub-graph. Functions with two arguments — e.g. difference or exponential function — inherit from CAS::BinaryOp, that links to two subgraphs. Functions with arbitrary number of arguments — e.g. sum and product — have as parent the CAS::NaryOp<sup>1</sup>, that links to an arbitrary number of subgraph. The different kind of containers allows to introduce some properties like as-69 sociativity and commutativity. Each container allows to access the subgraphs through instance properties. Containers structure is shown in fgure 2.1 71 Terminal leaf of the graph are the two classes CAS::Constant and CAS::Va-72 riable. The first is a node for a simple numerical value, while the latter 73 represents an independent variable, that can be used to perform derivatives and evaluations. As for now, those nodes are only scalar numbers, with the 75 plan to define also the vector and matrix extensions in the next major release. 76 Automatic differentiation (CAS::Op#diff) crosses the graph until reaches 77 the ending node. The terminal node is the starting point for derivatives accumulation, the mathematical equivalent of the chain rule:

$$(f \circ g)' = (f' \circ g) g' \tag{2}$$

The recursiveness is used also for simplifications (CAS::Op#simplify), substitutions (CAS::Op#subs) and evaluations (CAS::Op#call).

#### 2.2. Software Functionalities

The main functionality of the library is the **AD**, that can be performed against an independent variable or a symbolic expression. The function that performs the differentiation is a method of the CAS::Op container. Argument of the function is again a CAS::Op or a CAS::Variable.

87 x = CAS::vars 'x' # creates a variable

<sup>&</sup>lt;sup>1</sup>Please note that this container is still at experimental stage

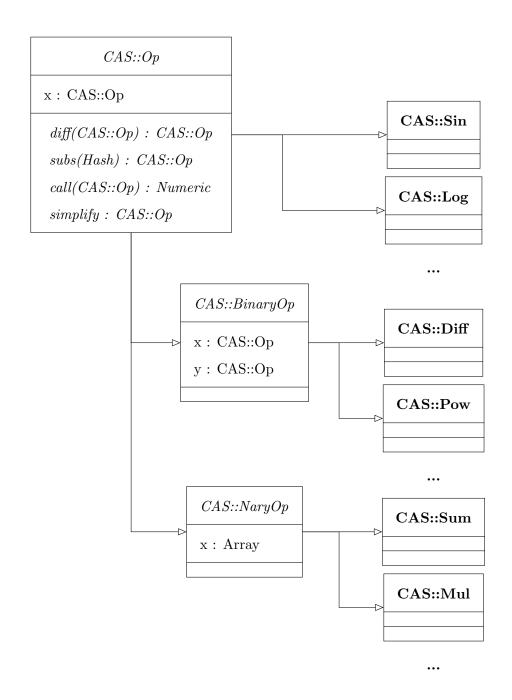


Figure 1: Simplified version of classes interface and inheritance

```
88 f = x ** 2 + 1 # define a symbolic expression

89 f.diff(x) # derivative w.r.t. x

90 # => 2 * x ^ (2 - 1) + 0
```

Resulting graph still contains a zero, since **simplifications** are not executed automatically. Each node of the graph contains some rules for simplify itself, that means simplification engine can see only one node ahead in the graph. Simplification are called recursively inside the graph, exactly like AD, bringing the strong limitation of not handling simplifications that come from *heuristic expansion* of sub-graphs — e.g. simplification through the use of trigonometric identities. Those simplification must be achieved manually using **substitutions**.

```
99 x, y = CAS::vars 'x', 'y' # creates two variables
100 f = CAS::log( CAS::sin( y ) ) # symbolic expression
101 f.subs({ y=> CAS::asin(CAS::exp(x)) }) # perform substitution
102 f.simplify # simplify expression
103 # => x
```

The graph can be **evaluated** substituting defining some values for the independent variable in a feed dictionary. The graph is recursively reduced to a single numeric value:

Symbolic functions can be used also to create expressions — e.g.  $f(\cdot) \ge g(\cdot)$  — or piecewise functions — e.g.  $\max(f(\cdot),g(\cdot))$ :

```
113  x = CAS::vars 'x'
114  f = x ** 2
115  g = 2 * x + 1
116  f.greater_equal g
117  # => ((x)^(3) ((2 * x) + 1))
118  CAS::max f, g
119  # => (((x)^(3) ((2 * x) + 1)) ? (x)^(3) : ((2 * x) + 1))
```

Expression are stored in a special container class, called CAS::Condition.

The library is developed to be used for **code generation**, and in some case also **metaprogramming**. Expressions, once manipulated, can be easily exported as source code (in a defined language —i.e. the following example in standard *Ruby* code):

```
125 x = CAS::vars 'x'  # creates a variable
126 f = CAS::log(CAS::sin(x))  # define a symbolic function
127 # => Math::log(Math::sin(x))
```

the same function can be also used to create directly a callable lambda already parsed by the interpreter:

Must be noted that parsing the graph creates a snapshot, and any further modification to the expression will not update the callable object. This draw-back is balanced by faster execution time of the *lambda*: when a graph needs only to be evaluated in a iterative algorithm, and not to be manipulated, transforming it in a *lambda* reduces the execution time per loop.

Other functionalities — e.g. displaying drivers — are not reported in the current work for a sake of brevity. Please refer to gem documentation for more insight.

## 3. Illustrative Examples

# 142 **4. Impact**

### 5. Conclusions

## 144 Acknowledgements

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### 147 Current code version

Nr.	Code metadata description	Please fill in this column
C1	Current code version	0.0.0
C2	Permanent link to code/repository	github.com/MatteoRagni/cas-rb &
	used for this code version	rubygems.org/gems/ragni-cas
С3	Legal Code License	MIT
C4	Code versioning system used	git (GitHub)
C5	Software code languages, tools, and	Ruby
	services used	
C6	Compilation requirements, operat-	$Ruby \ge 2.x$ , $pry$ for testing console
	ing environments	(optional)
C7	If available Link to developer docu-	rubydoc.info/gems/ragni-cas
	mentation/manual	
C8	Support email for questions	info@ragni.me

Table 1: Code metadata (mandatory)