# Capitolo 1

# Implementazione di procedure di decisione per frammenti Binding in Vampire

L'algoritmo di decisione, la classificazione, Il preprocessing

# 1.1 Preprocessing

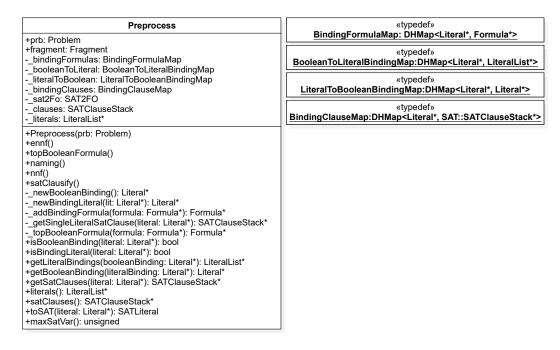


Figura 1.1: Struttura del Preprocessing

## 1.1.1 Boolean Top Formula

#### 1.1.2 Forall-And

#### 1.1.3 SAT-Clausification

## 1.2 Procedura di Decisione

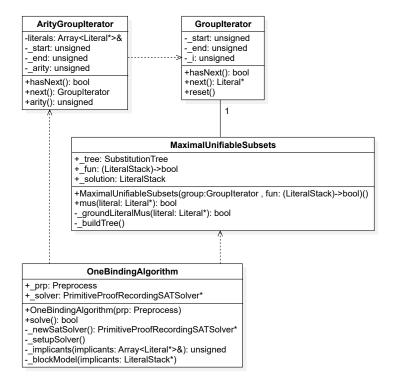


Figura 1.2: Struttura dell'algoritmo di decisione

# 1.2.1 Implicants Sorting

#### 1.2.2 Maximal Unifiable Subsets

# Algorithm 1: Maximal Unifiable Subsets

```
Firma: \operatorname{mus}(literal)
Input: literal un puntatore ad un letterale
Output: \top o \bot
GlobalData: S una mappa da letterali a bool
if S[literal] then

| return \top;
end
if literal is ground then

| return groundLiteralMus(literal);
end
S[literal] = \top;
res := mus(literal, \emptyset);
S[literal] = \bot;
return res;
```

#### Algorithm 2: Maximal Unifiable Subsets

```
Firma: mus(literal, FtoFree)
Input: literal un puntatore ad un letterale, FtoFree un puntatore ad una lista di letterali
Output: \top o \bot
GlobalData: S una mappa da letterali a interi, fun una funzione da lista di letterali a bool,
 tree un SubstitutionTree
isMax := \top;
uIt = tree.getUnifications(query: literal, retrieveSubstitutions: true);
toFree := \emptyset;
while uIt.hasNext() do
    (u,\sigma) := uIt.next();
   if S[u] = 0 then
       S[u] = 1;
       l := literal^{\sigma};
       if l = literal then
           u' := u^{\sigma};
           if u' = u then
              FtoFree := FtoFree \cup \{u\};
           end
           else
              toFree := toFree \cup \{u\};
           end
       end
       else
           isMax = \bot;
           if \neg mus(l, toFree) then
            return \perp;
           \mathbf{end}
           S[u] = -1;
           toFree := toFree \cup \{u\};
       \mathbf{end}
   \quad \mathbf{end} \quad
end
if isMax then
   if \neg fun(\{x \mid S[x] = 1\}) then
    return \perp;
   end
end
while toFree \neq \emptyset do
   S[toFree.pop()] = 0;
end
return \top;
```

#### Algorithm 3: Maximal Unifiable Subsets Ground

```
Firma: groundMus(literal)
Input: literal un puntatore ad un letterale ground
Output: \top o \bot
GlobalData: S una mappa da letterali a interi, fun una funzione da lista di letterali a bool,
tree un SubstitutionTree
if S[literal] \neq 0 then
 return \top;
\quad \text{end} \quad
uIt = tree.getUnifications(query: literal, retrieveSubstitutions: true);
solution := \emptyset;
while uIt.hasNext() do
   (u, \sigma) := uIt.next();
   if S[u] = 0 then
       if u is ground then
        S[u] = -1;
       end
       solution := solution \cup \{u\};
   \quad \mathbf{end} \quad
end
return fun(solution);
```

#### 1.2.3 Algoritmo Finale

#### Algorithm 4: Algoritmo di decisione

```
Firma: solve(prp)
Input: prp il problema pre-processato
Output: \top o \bot
satSolver := newSatSolver();
satSolver.addClauses(prp.clauses);
while satSolver.solve() = SATISFIABLE do
   res := \top;
   implicants := getImplicants(satSolver, prp);
   implicants := sortImplicants(implicants);
   if implicants contains only ground Literals then
      return \top;
   end
   agIt := ArityGroupIterator(implicants);
   while res And agIt.hasNext() do
      maximalUnifiableSubsets := SetupMus(group, internalSat);
      foreach lit \in group do
          if \neg maximalUnifiableSubsets.mus(lit) then
             res := \bot;
             blockModel(maximalUnifiableSubsets.getSolution());
             Break;
          end
      end
      if res = \top then
         return \top;
      end
   end
end
\mathbf{return}\ \bot;
```

#### Algorithm 5: Sat interna

```
Firma: internalSat(literals)
Input: literals una lista di letterali
Output: \top o \bot
if literals.length = 1 And getSatClauses(literals.top()).length = 1 then
| return \top;
end
satSolver := newSatSolver();
foreach l \in literals do
| satSolver.addClause(getSatClauses(l));
end
return satSolver.solve() = SATISFIABLE;
```

#### Algorithm 6: getImplicants **Firma:** getImplicants(solver, prp) Input: solver un sat solver, prp il problema pre-processato Output: Una lista letterali $implicants := \emptyset;$ foreach $l \in prp.literals()$ do satL := prp.toSat(l); ${\bf if}\ solver.trueInAssignment(satL)\ {\bf then}$ if prp.isBooleanBinding(l) then $implicants := implicants \cup prp.getLiteralBindings(l);$ end else $implicants := implicants \cup \{l\};$ end end end ${\bf return}\ implicants;$

# 1.3 Algoritmo di Classificazione

(Input formula rettificata senza true e false)

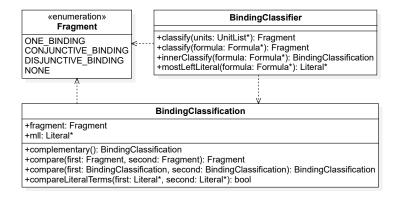


Figura 1.3: Classificatore

#### Algorithm 7: Classificatore esterno

```
Firma: classify(\varphi) Input: \varphi Una formula rettificata
Output: Un elemento dell'enumerazione Fragment
switch \varphi do
    \mathbf{case}\ \mathit{Literal}\ \mathbf{do}
       return ONE_BINDING;
    end
    case A[\wedge, \vee]B do
       return compare(classify(A), classify(B));
    end
    case \neg A do
       return classify(A).complementary();
    end
    case [\forall,\exists]A do
        sub := \varphi;
        connective := connective of \varphi;
        repeat
            sub := subformula of sub;
            connective := connective of sub;
        until connective \notin \{ \forall, \exists \};
        (fragment, \_) := innerClassify(sub);
        return fragment;
    \quad \text{end} \quad
    case A \Leftrightarrow B do
       return compare(classify(A \Rightarrow B), classify(B \Rightarrow A));
    end
    case A \oplus B do
       return classify(A \Leftrightarrow B).complementary();
    case A \Rightarrow B do
        return compare(classify(\neg A), classify(B));
    end
end
```

#### Algorithm 8: Classificatore interno

```
Firma: innerClassify(\varphi) Input: \varphi Una formula rettificata
Output: Una coppia (Fragment, Literal)
switch \varphi do
   case Literal\ l\ do
       return (ONE\_BINDING, l);
   end
   case A[\land,\lor]B do
       return innerCompare(innerClassify(A), innerClassify(B), connective of <math>\varphi);
   end
     return innerClassify(A).complementary();
   end
   case A[\Rightarrow, \Leftrightarrow, \oplus]B do
    return innerCompare(innerClassify(A), innerClassify(B), connective of \varphi);
   end
   else
       return (None, null);
   end
end
```

#### Algorithm 9: Compare esterno

```
Firma: compare(A, B) Input: A, B due elementi dell'enumerazione Fragment

Output: Un elemento dell'enumerazione Fragment

if A = B then

| return A;

end

if One\_Binding \notin \{A, B\} then

| return None;

end

return max(A, B);
```

#### Algorithm 10: Compare interno

```
Firma: innerCompare(A, B, con) Input: A, B due coppie (Fragment, Literal), con un connectivo
Output: Una coppia (Fragment, Literal)
switch A.first, B.first, con do
    \mathbf{case}\ \mathit{One\_Binding},\ \mathit{One\_Binding},\ \_\_\mathbf{do}
       if A.second has same terms of B.second then
           return A;
        end
       else if conn = \wedge then
            return (Conjunctive_Binding, null);
       end
       else if conn = \vee then
         return (Disjunctive_Binding, null);
       end
    \mathbf{case} \ [\mathit{One\_Binding}, \ \mathit{Conjunctive\_Binding} \ | \ \mathit{Conjunctive\_Binding}, \ \mathit{One\_Binding}], \land \mathbf{do}
       return (Conjunctive_Binding, null);
    \quad \text{end} \quad
    case [One_Binding, Disjunctive_Binding | Disjunctive_Binding, One_Binding], ∨ do
       return (Disjunctive_Binding, null);
    \quad \text{end} \quad
    case Conjunctive_Binding, Conjunctive_Binding, ∧ do
       return (Conjunctive_Binding, null);
    end
    case Disjunctive\_Binding, Disjunctive\_Binding, \lor do
       return (Disjunctive_Binding, null);
    end
end
return (None, null);
```