

### 3 $M$ -fold Cross-validation

Implement and perform  $M$ -fold cross validation for LVQ1 training, using the data set of assignment 1.

First, shuffle the two-class data set randomly once, then split the data into  $M = 5$  disjoint subsets, each containing 20% of the data. Take care that the correct labels are still assigned to the data points.

In an individual training run, use 4 of the  $M = 5$  subsets for training and 1 subset for validation. Perform LVQ1 training as in assignment 1 with  $K$  prototypes per class for up to 100 *epochs*. Initialize each prototype in a randomly selected point of its class.

Determine the *training error* (performance on the 4/5 of data used for training) and the *validation error* (performance on 1/5 of the data) **at the end of each training process**. Repeat this for the 5 possible splits into training and validation set to obtain 5 individual results.

Compute the average training and validation errors (i.e. the fraction of misclassified data points) and their standard deviations over the  $M = 5$  results. Plot the results as a function of  $K$ , the number of LVQ prototypes per class.<sup>2</sup>

You should hand in a structured report comprising:

- **(2 point)** A brief introduction and description of your experiments.
- **(4 points)** Figures displaying both the final training and validation error as a function of  $K = 1, 2, \dots, 5$  as obtained in 5-fold cross-validation (averages and standard deviation, see above). Of course you may obtain and present results for even greater values of  $K$ .
- **(4 points)** A discussion of your results. What is your conclusion with respect to the choice of the number  $K$  of prototypes?

### Bonus (suggestions)

1 point max. in total:

- Consider also 10-fold cross validation ( $M = 10$ ) and compare with the results for  $M = 5$ .
- Repeat the cross-validation experiments for  $K = 1$ , now for different constant learning rates  $\eta$ . Can you determine a *best* value?
- Perform  $M$ -fold cross validation for the regression problem (and data set) of assignment 2.

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<sup>2</sup>A useful matlab command for displaying the standard deviations is `errorbar(...)`.