



Radar and Remote Sensing

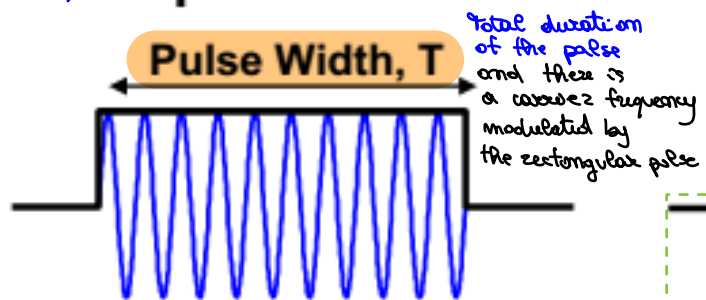
Range Doppler Radar

Range doppler is a technique that radar use to estimate Doppler.

→ How we see this technique that can be used with any waveform

Possible radar waveforms

1) Square Pulse



Bandwidth = $1/T$

Time \times Bandwidth = 1

→ We have a problem because τ and B are not independent in fact the time-bandwidth product is equal to 1

$$\Delta R = \frac{c}{2B}$$

$$R_{MAX} = \frac{c}{2f_2}$$

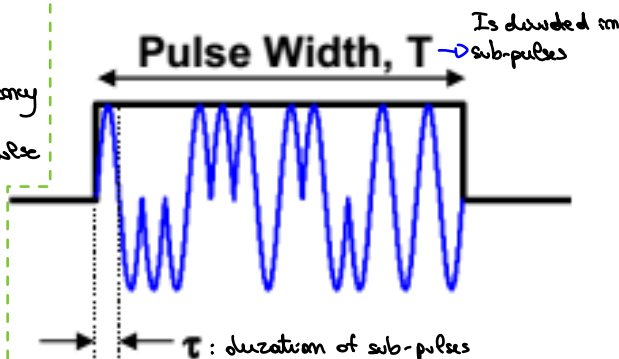
depends on the maximum unambiguous range

This type of waveform is very limited because one of the main issue to choose a waveform is the possibility to have a ΔR and the capability to detect target

But here if we want to increase ΔR we have to increase B a lot but reducing B we reducing time. And if we reduce τ we still want to maintain a certain energy of the signal a lot of power is needed

Digitally modulated waveform

Binary Phase Coded Waveform



τ can be set in the limit because the PRI is at the minimum that is $= T$,

Bandwidth = $1/\tau$

Time \times Bandwidth = T/τ

$$R_{MAX} = \frac{c}{2} \cdot \frac{1}{\max c}$$

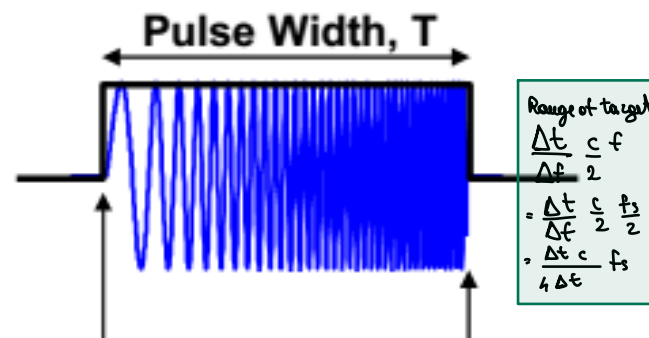
$$\Delta R = \frac{c}{2B}$$

→ The limit is give to our system to process data, because in the radar receive block diagram we don't convert the signal and convert the I/Q component and we do the correlation. So we have a buffer of data (W_1, \dots, W_N) The length of the buffer depend on the processing system to elaborate τ before to the mixer

Analog modulation → Linear frequency modulated waveform

- We have introduce a modulation in a Bandwidth $\Delta f = f_2 - f_1$
- Advantage: We can set independently Δf and T and so other advantages:
 - $\tau \cdot B$ is much bigger than 1 so the detectability (SNR) is much bigger than SNR to the match filter

Linear Frequency Modulated Waveform



$$\begin{aligned} \frac{\Delta t}{\Delta f} &= \frac{c}{2} \cdot \frac{f_2 - f_1}{2} \\ &= \frac{\Delta t}{\Delta f} \cdot \frac{c}{2} \cdot \frac{f_2 - f_1}{2} \\ &= \frac{\Delta t \cdot c}{4 \Delta f} \end{aligned}$$

Frequency F_1

Frequency F_2

Bandwidth = $\Delta F = F_2 - F_1$

Time \times Bandwidth = $T \Delta F$

$$R_{MAX} = \frac{\Delta t \cdot c}{4 \Delta f} \cdot f_s$$

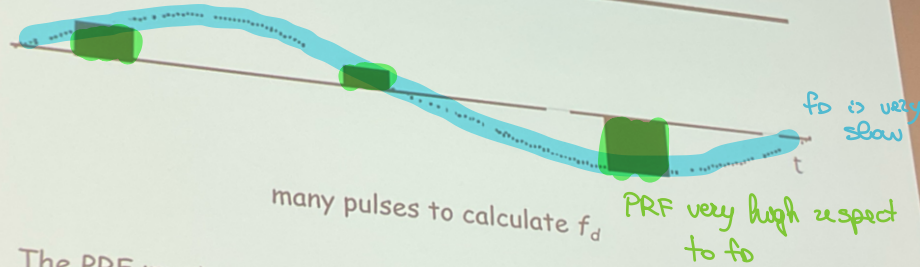
$$\Delta R = \frac{c}{2B}$$

Is different from the rectangular pulse, but it depend on f_s of beat frequency because we have to sampling the output of the mixer

2) ΔR → we can fix B to get a certain resolution and then we can fix the τ to have $B \cdot \tau > 1$

- We can have idle time between pulses so we can PRI and so in decrease the PAF → Problem for doppler

Doppler calculation



The PRF must sample at twice the highest Doppler frequency to avoid aliasing, i.e., avoid Doppler ambiguity

The PRF must sample the Doppler frequency with a number N of samples to achieve resolution

$$f_r > \frac{4v_{\max}}{\lambda}$$

$$\Delta f_d = \frac{1}{NT}$$

Range resolution

▷ Radar is called a four dimensional system because is capable to detect at the same time the range, azimuth, elevation and velocity of target

- The classical way to detect doppler is use many pulses to calculate f_0 because f_0 is much lower than PRF.

So we have pulses modulated pulse by the f_0

- PRF is a sampling frequency for the doppler and PRF must sample twice the highest f_0

Problem → PRF has a value according to the V_{\max} of target and so the largest is $V_{\max} \Rightarrow$ the largest PRF must be

If PRF is larger the PRI is smaller

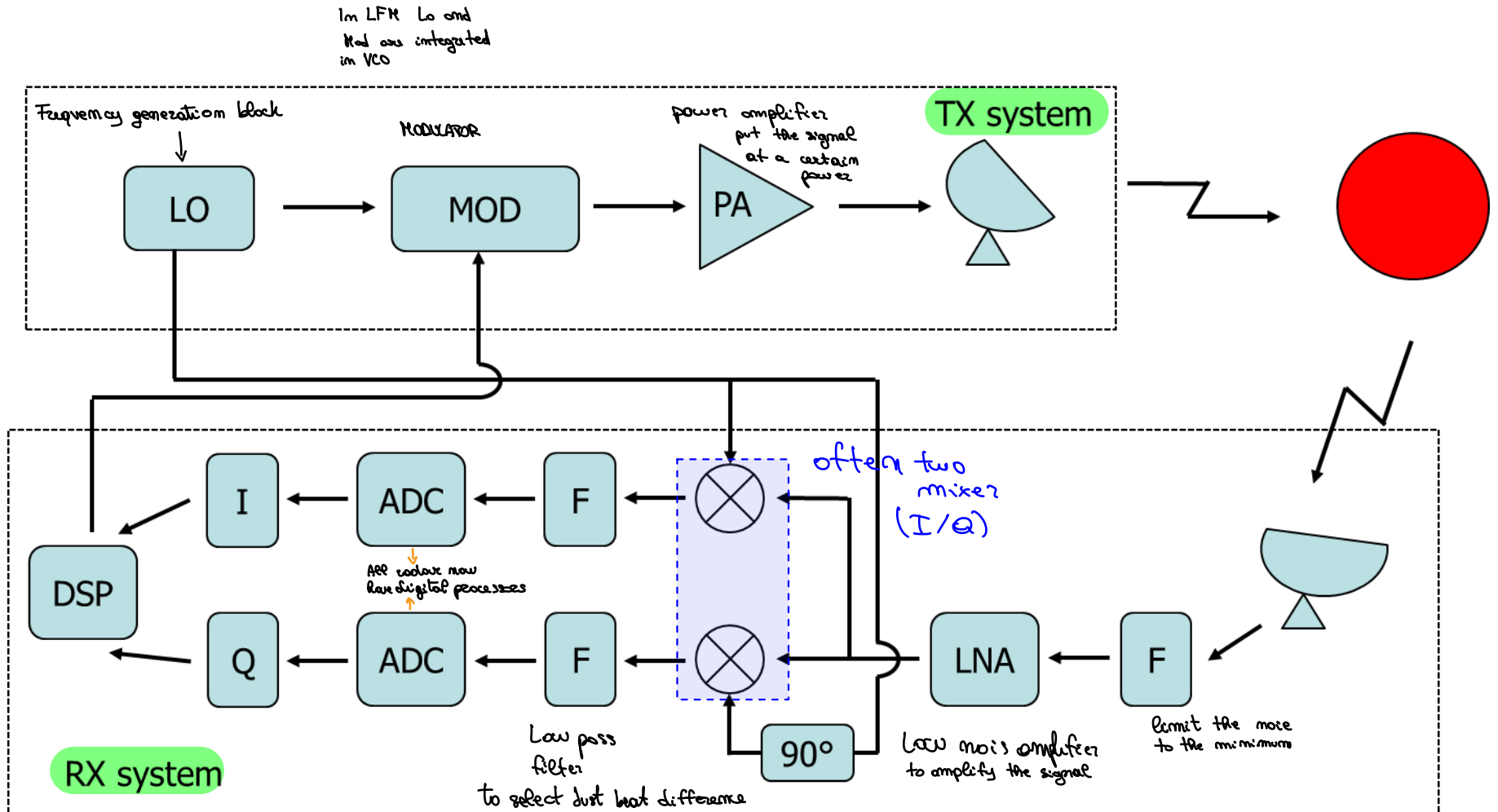
If we have large Bandwidth we want to have large duration of the signal to increase energy but we have a limit because if we want a very fast target we have to reduce the duration of the signal to improve PRF

▷ Every time we sample thanks to PRF the $f_0 \rightarrow$ Obviously: to estimate f_0 we have to do on FFT of the data

↳ Every time we do this we must sample the f_0 with a certain N # of sample that we collect to estimate f_0 to obtain a certain Doppler resolution.

From Δt we want $N \gg 1$ but if we collect a lot of data we delay the calculation so we limit the number of observation per second (for ex we have to sample 20 observation per second)

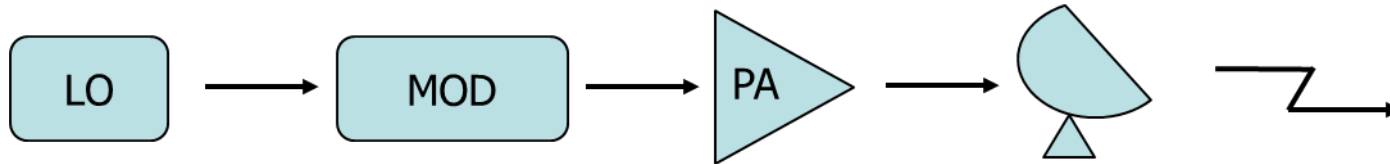
Range Doppler radar implementation



In this case we have a system available for mono/bi-static radar. In a monostatic we have to put the T/R module.

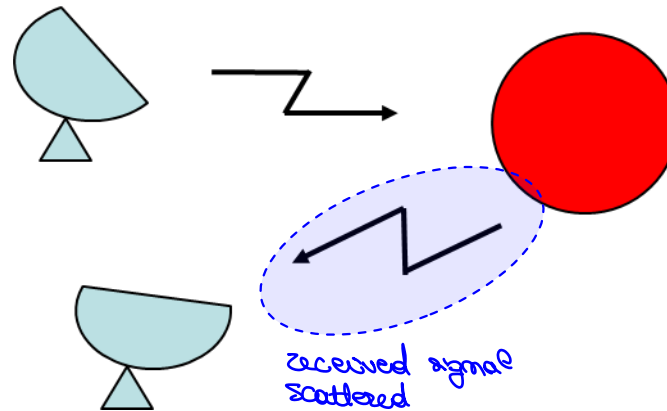
TX system

Usually we have a continuous transmission but we can have an *idle interval* between the pulses to get PRI that we've chosen



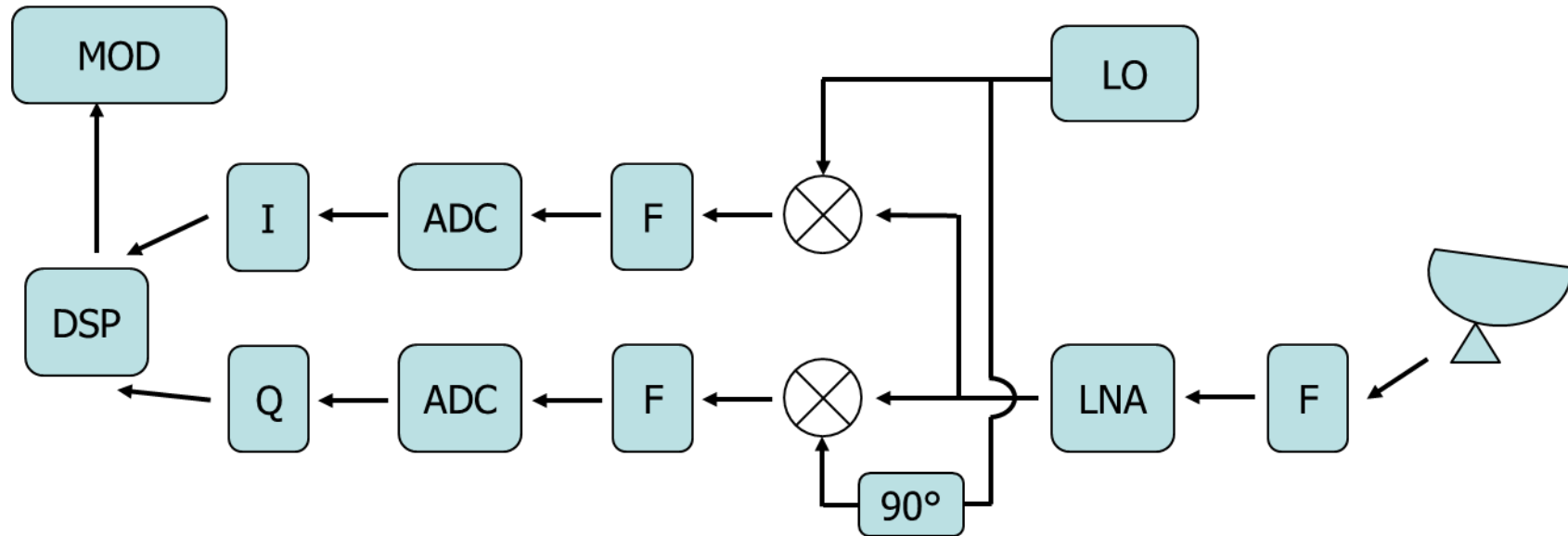
- ✓ A modulated signal is generated considering the given pulse length, the pulse repetition interval (PRI), the carrier frequency, and the bandwidth.
- ✓ The transmitted signal is made up of a modulated pulse and, if needed, a zero interval up to the required PRI. *Idle*
- ✓ Extra signals are also generated by the local oscillator to provide the input for the mixers at the coherent receiving stage.

Received signal



- ✓ The received signal can be approximated applying attenuation, delay, and frequency shift to the transmitted one, due to the target RCS, position and relative speed.
 $f_r \approx f_0$ ↓
scattered
- ✓ By means of the radar equation, the transmitted power, the antenna gain (TX and RX), the free space attenuation, the losses and the radar cross section of the target introduce an amplitude scaling factor.
- ✓ Additional white Gaussian noise is calculated to get to the received Signal to Noise Ratio (SNR).

RX system

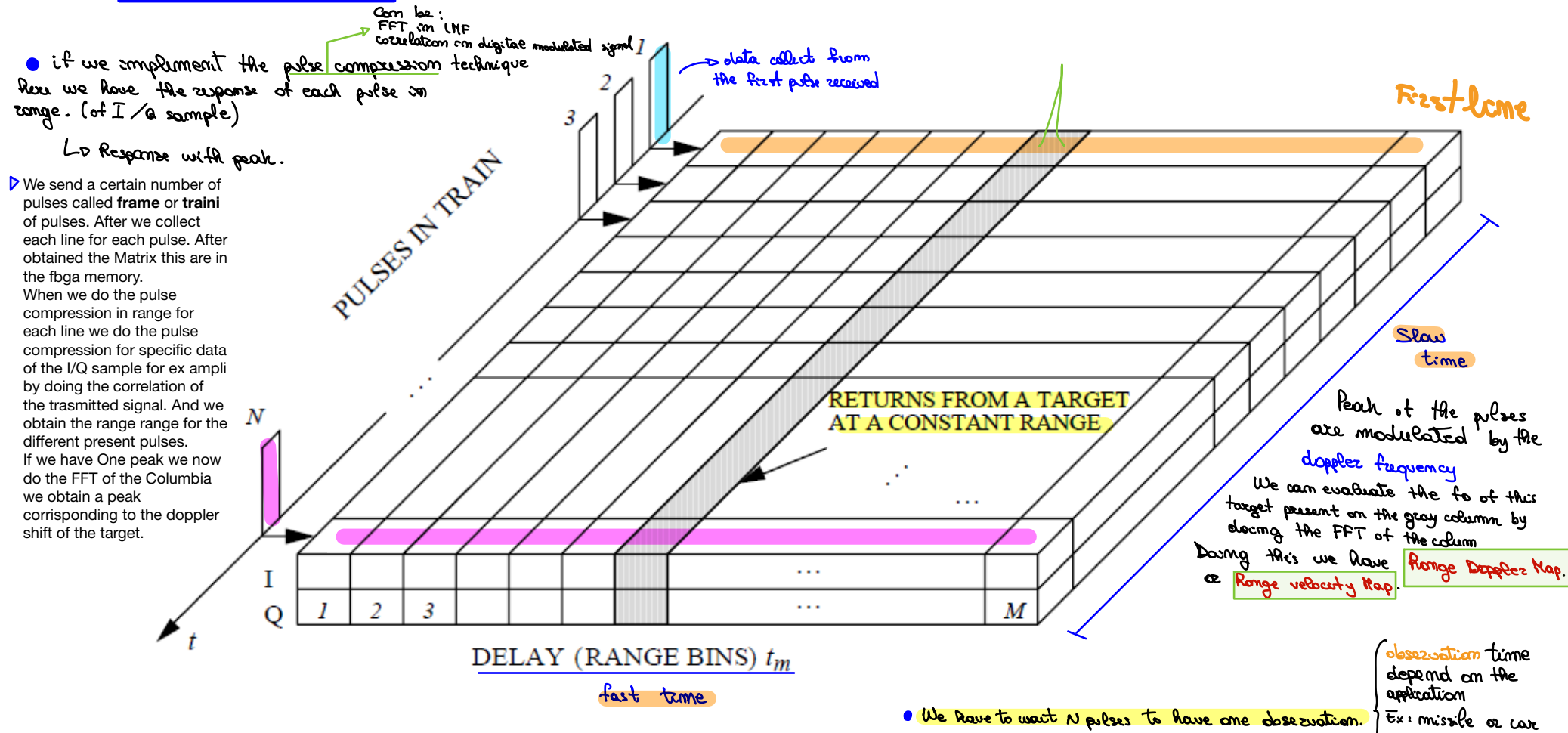


- ✓ The RX signal is filtered, amplified, splitted, and mixed with two replicas of the original signal coming out of the LO (with 90° phase difference between the two).
- ✓ The obtained signals are then sampled through the analog-to-digital converter to get the I and Q samples.

We have a vector of data every PRI and so we have to organize this vector \rightarrow We use a matrix which every line is a vector data. Then, after a certain number of vector we moving toward the following observation

Range Doppler radar implementation

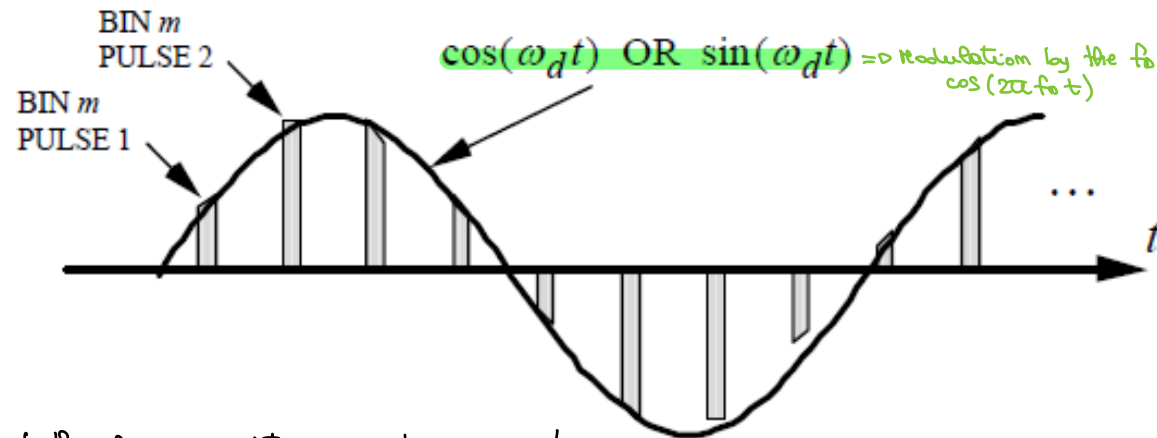
- ✓ Once I and Q are stored for a certain number of pulse repetition intervals (train or frame), the complex samples $I+jQ$ are organized into a matrix of data.



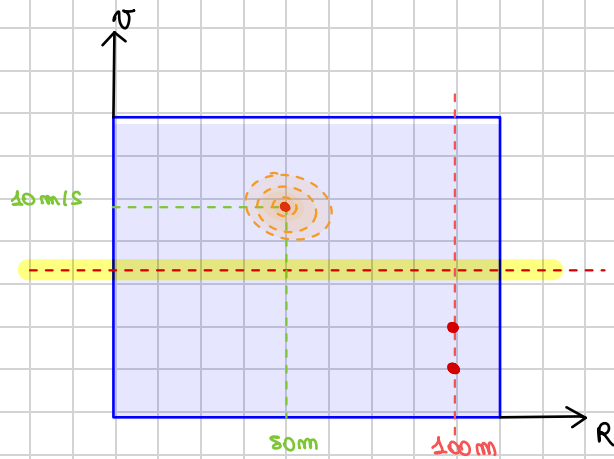
Range Doppler radar implementation

Here if we consider the gray column of the previous slide

Returns for a target that remains in a single range bin (for example, bin m)



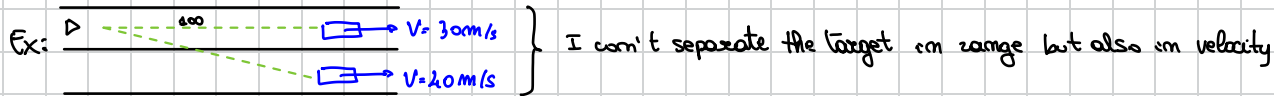
If we do the FFT of the column we obtain a peak corresponding to f_b that is proportional to the velocity of the target.



↳ "0-doppler" considered as region of clutter because usually radar want to detect moving target and so are away from this region
 In this case we have **echo radar** because our radar is not moving
 Otherwise, if the radar is moving this are the target at the velocity of the radar

↳ Just to see the response of the stationary target

- **Zero doppler cut** is an important plot where we cut the matrix at $v=0$ and plot what there are on the bottom or below.



▷ There are different waveforms and we can set the artificial intelligence to decide

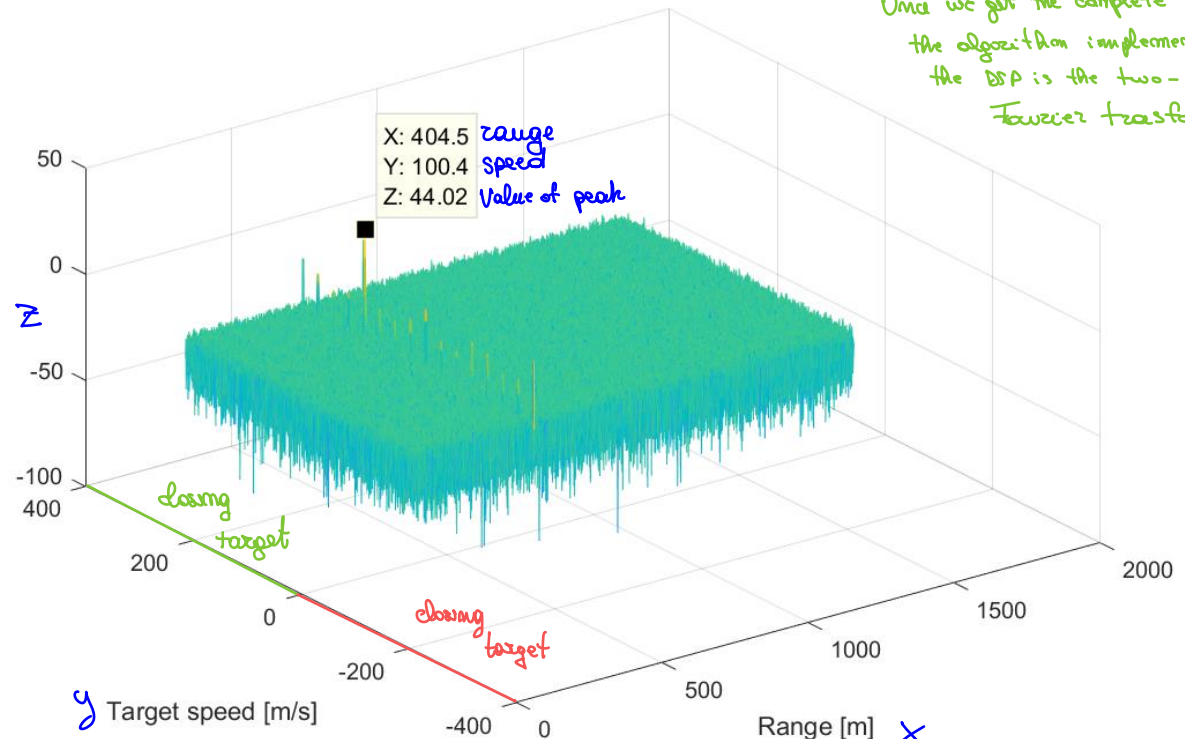
Ex: if I moving by fast circular e starts we will have a circular shape because i start from $v=0$ to $v=\max$ e viceversa.

Range Doppler radar implementation

- ✓ The time delay or range (represented along one dimension of the matrix called fast time) and Doppler frequency shift or speed (represented by means of a Fourier transform along the other dimension of the matrix called slow time) allow to derive the range and speed of the target. In case of FMCW a two-dimensional Fourier transform is performed.
- Handwritten notes:*
- "sampling is fast" with an arrow pointing to "fast time"
- "samples slower" with an arrow pointing to "slow time"

In this example the target is moving toward the radar at about 100m/s.

The position of the target with respect to the radar is approximately 400m range.



Once we get the complete matrix the algorithm implemented in the DSP is the two-dimensional Fourier transform.