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Holographic Declarative Memory and the Fan Effect: *A Test Case for a New Memory Module for ACT-R*

Presented by Terrence C. Stewart, U. Of Waterloo.

- Holographic Declarative Memory (**HDM**) is a new module for ACT-R, implemented for Python ACT-R (Stewart & West, 2006).
- HDM is an alternative to ACT-R's Declarative Memory (**DM**).
- HDM replaces DM's symbols with *holographic vectors* (Plate, 1995) and implements a holographic theory of memory based on **DSHM** (Rutledge-Taylor, Kelly, West, & Pyke, 2014) and **BEAGLE** (Jones & Mewhort, 2007).

Holographic Declarative Memory

- Holographic vectors retain the expressive power of symbols
 - Compactly store complicated, recursive relations between ideas
- Holographic vectors have a similarity metric, allowing for...
 - Shades of meaning and fuzzy matching
 - Loss compression for modeling forgetting
 - Fault tolerance
- HDM can enhance ACT-R's ability to:
 - Learn over the long term
 - Store large quantities of data/world knowledge
 - Learn associations

Why use holographic vectors?

- Holographic models of memory in the literature
- Case Study: The Fan Effect
 - What is the fan effect?
 - The ACT-R DM model of the fan effect
 - The HDM model of the fan effect
- Results: How does DM and HDM compare?
- Analysis: Why does HDM work?
- Conclusions / future work

In what follows ...

- Explain and predict a variety of human **memory** phenomena
 - **Fan effect** (Rutledge-Taylor et al., 2014)
 - **Serial recall** and **free recall** of lists (Franklin & Mewhort, 2015)
 - **Implicit** learning (Jamieson & Mewhort, 2011)
- **Analogical reasoning**
 - (Plate, 2000; Eliasmith & Thagard, 2001)
- Simple **problem-solving** tasks
 - (Eliasmith, 2013; Rutledge-Taylor et al., 2014)
- **SPAUN**, the world's largest functional **brain model**
 - (Eliasmith, 2013)
- **BEAGLE**, a model of learning **word meaning** from a corpus
 - (Jones & Mewhort, 2007)

Holographic memory in the literature

astronomy
physics
chemistry
biology
scientific
mathematics
technology
science
scientists

financial

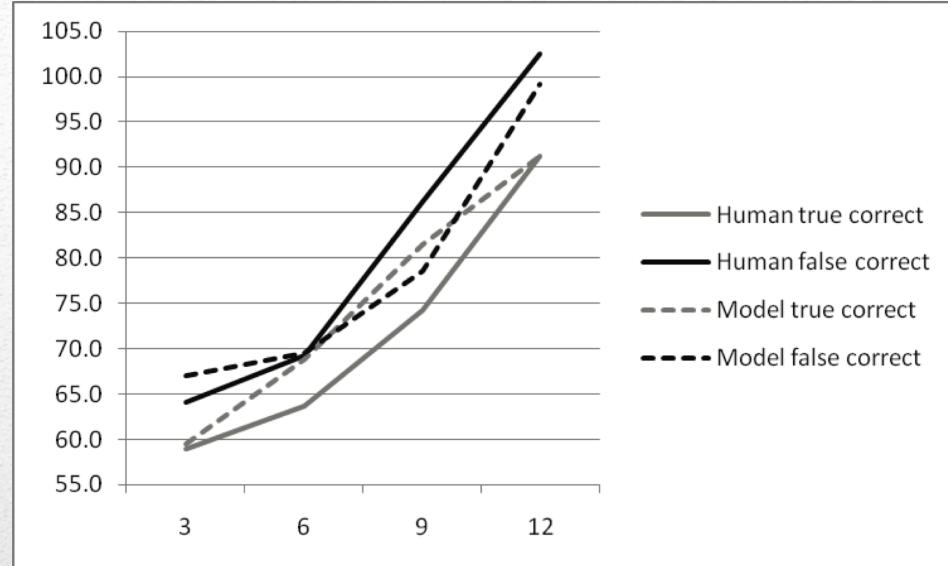
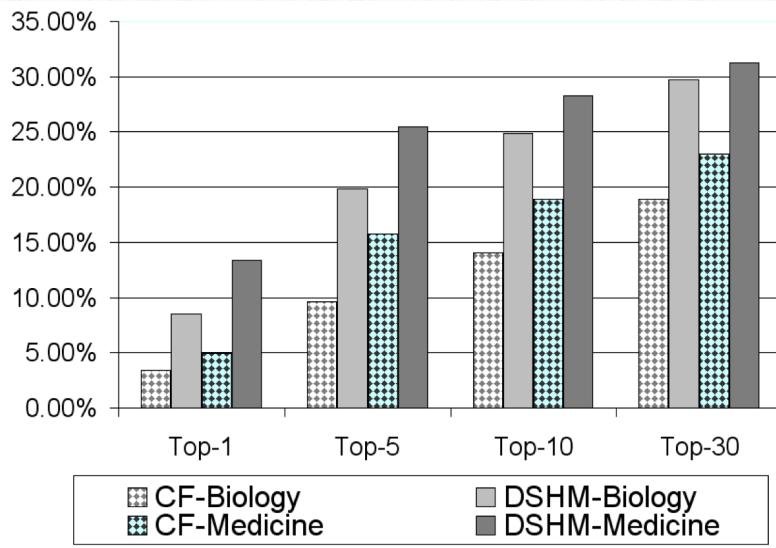
research

savings finance
invested pay
loaned borrow lend
invest bank
investments
spend save

- Takes a corpus as input
- Produces a set of vectors representing word meaning
- Similarities between vectors produce clusters of topic and part of speech
- Vector similarities predict semantic priming data

BEAGLE

(Jones & Mewhort, 2007)



- Applies BEAGLE to non-lingusitic stimuli
- Models two-term and three-term fan effect
- Models rock-paper-scissors play
- Effective recommender system for movies or research papers

DSHM

- “the **hippy** is in the **park**”

- “the **hippy** is in the **bank**”

$$\text{fan}(\textbf{hippy}) = 3$$

- “the **hippy** is in the **store**”

$$\text{fan}(\textbf{store}) = 2$$

- “the **officer** is in the **store**”

$$\text{fan}(\textbf{officer}) = 1$$

Fan Effect

- participants are **slower** to recognize or reject sentences that contain concepts that have a **higher fan**.

- **availability** of information in memory with respect to a cue is related to the **probability** of that piece of information conditional on the cue.

$$\text{fan}(\text{hippy}) = 3$$

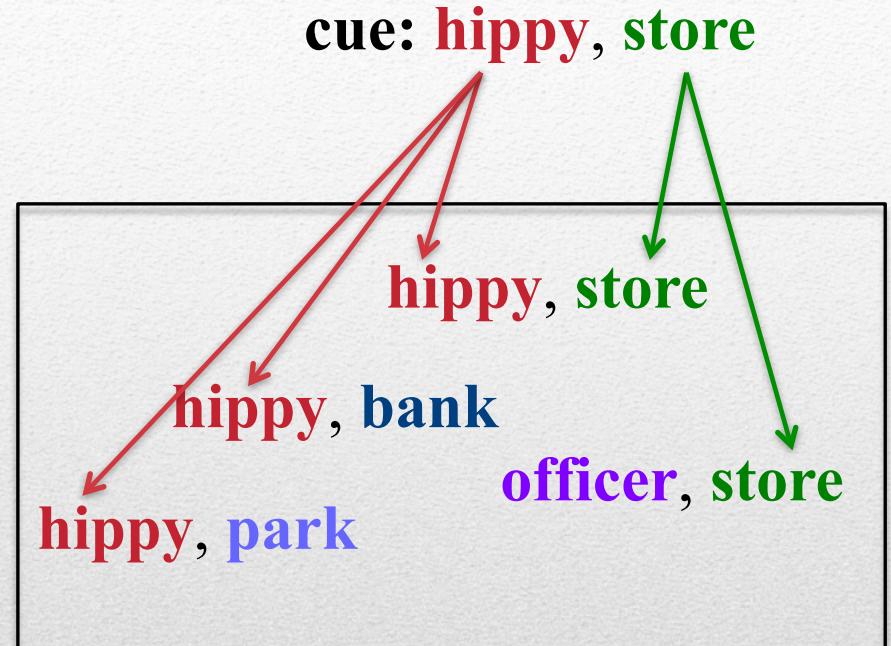
$$\text{fan}(\text{store}) = 2$$

$$\text{fan}(\text{officer}) = 1$$

Fan Effect

- sentences are represented as *person, location* **chunks** in DM

- when the model is cued, **activation** spreads to chunks that share concepts with the **cue**



Declarative Memory (DM)

ACT-R DM model

- Reaction time T is calculated as:

$$T = I + Fe^{-A_i}$$

- Activation A_i of chunk i is calculated as:

$$A_i = B_i + \sum_{j=1}^n W_j S_{ji}$$

- Association strength S_{ji} with concept j is:

$$S_{ji} = S + \ln(P(i|j))$$

- Where $P(i|j) = 1 / \text{fan of } j$

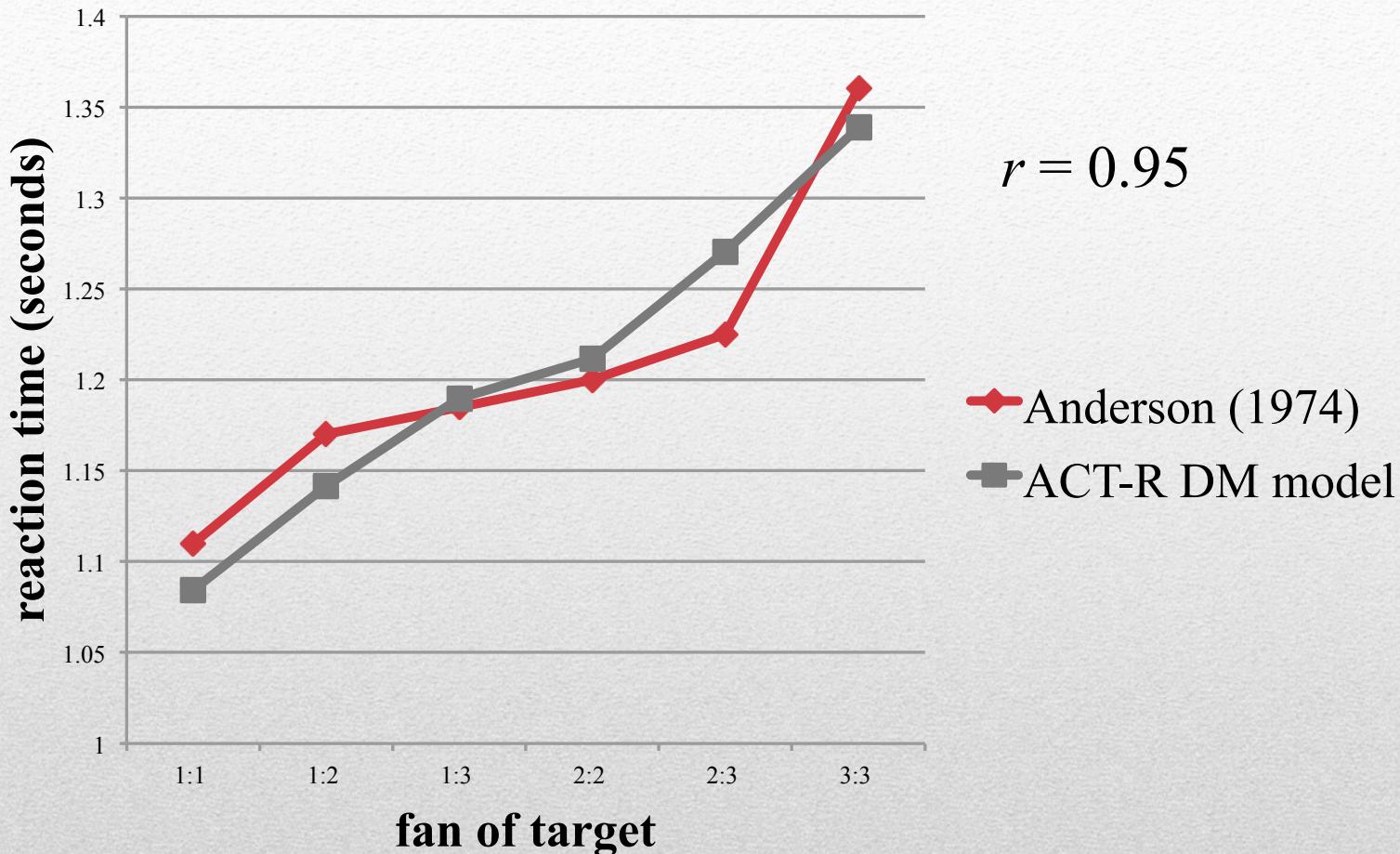
ACT-R DM model

- Anderson and Reder's (1999) model is, in milliseconds:

$$T = 239 f_{\text{person}}^{1/3} f_{\text{place}}^{1/3} + 845$$

- where f_{person} is the person's fan and f_{place} is the place's fan

ACT-R DM model



ACT-R DM vs. Human

For each task symbol (or concept) there are two vectors:

environmental vector

- a random vector that stands for what the symbol looks like

memory vector

- a continuously updated vector of the symbol's associations

Additionally, there is one special vector used in all associations:

placeholder vector Φ

- can be read as ?, i.e., the value that we want to retrieve.
- acts as a stand-in for the purposes of storage and retrieval.

HDM model

- * circular convolution is used to create associations between symbols in a sequence.
- + addition is used to add new associations to a memory vector

P_{before} is a permutation indicating that the permuted vector comes earlier in a sequence.

Holographic Reduced Representations (Plate, 1995)

“the **hippy** is in the **park**”

$$\mathbf{m}_{\text{hippy} \text{ (updated)}} = \mathbf{m}_{\text{hippy}} + (\mathbf{P}_{\text{before}} \Phi)^* \mathbf{e}_{\text{park}} \quad \text{“what came before park?”}$$

$$\mathbf{m}_{\text{park} \text{ (updated)}} = \mathbf{m}_{\text{park}} + (\mathbf{P}_{\text{before}} \mathbf{e}_{\text{hippy}})^* \Phi \quad \text{“what came after hippy?”}$$

To **encode** an association in HDM, memory vectors are updated with all **questions** to which the memory vector’s **concept** is an appropriate answer given HDM’s experiences.

Encoding associations

To test if “the **hippy** is in the **park**” is in memory, two cues are constructed:

$$\mathbf{q}_{\text{hippy?}} = (\mathbf{P}_{\text{before}} \mathbf{e}_{\text{hippy}})^* \Phi \quad \text{“what came after } \text{hippy}?”$$

$$\mathbf{q}_{?\text{park}} = (\mathbf{P}_{\text{before}} \Phi)^* \mathbf{e}_{\text{park}} \quad \text{“what came before } \text{park}?”$$

The memory vectors most **similar** to these cues are retrieved.

Similarity is measured as the **cosine** of the angle between vectors.

Retrieving associations

Activation is calculated as the **mean** of the **cosines** between each cue and the memory vector substituted out to create the cue:

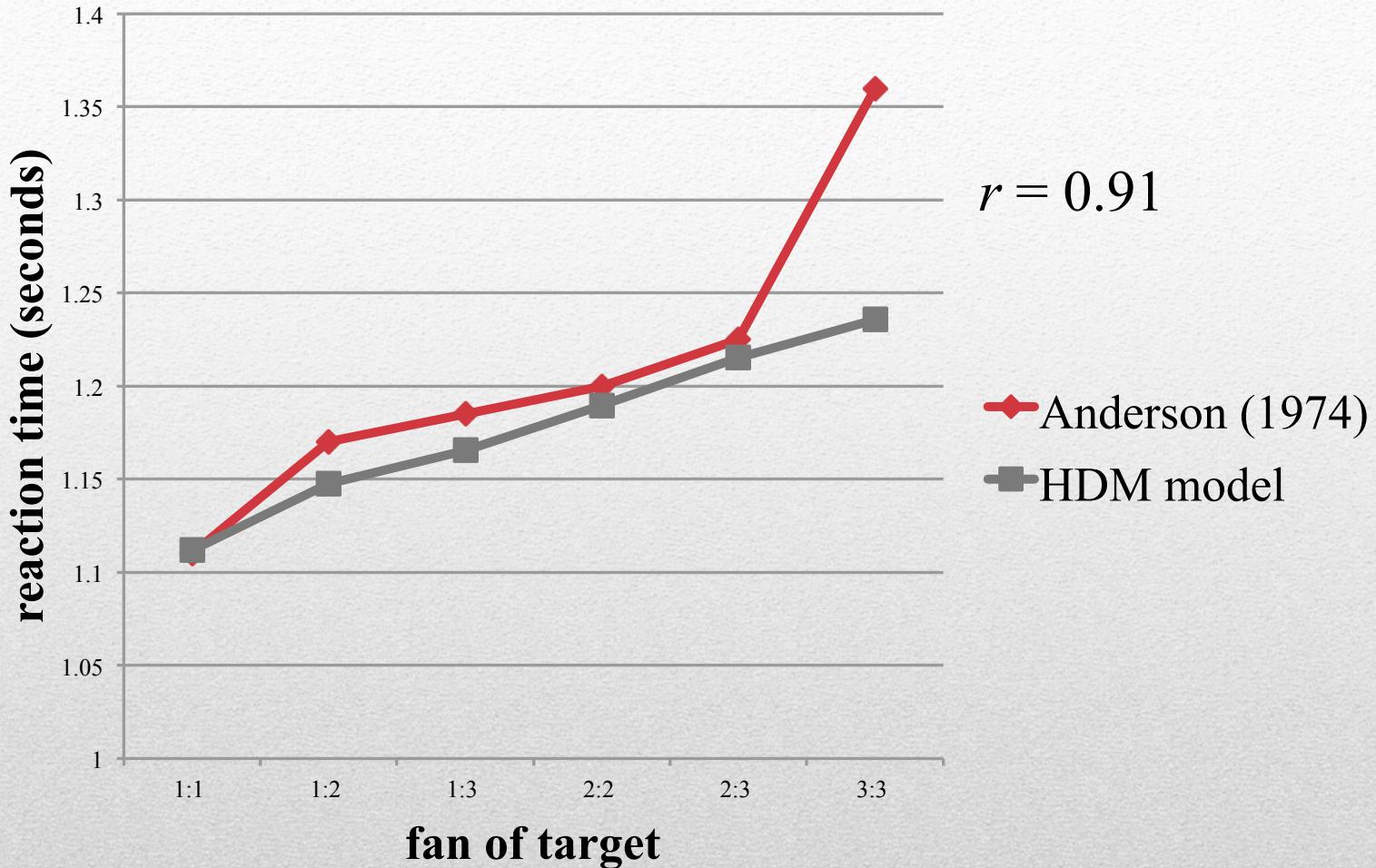
$$A = 0.5 \text{ cosine}(\mathbf{q}_{\text{hippy?}}, \mathbf{m}_{\text{park}}) + 0.5 \text{ cosine}(\mathbf{q}_{?\text{park}}, \mathbf{m}_{\text{hippy}})$$

Reaction **time** computed using **DM**'s reaction time equation:

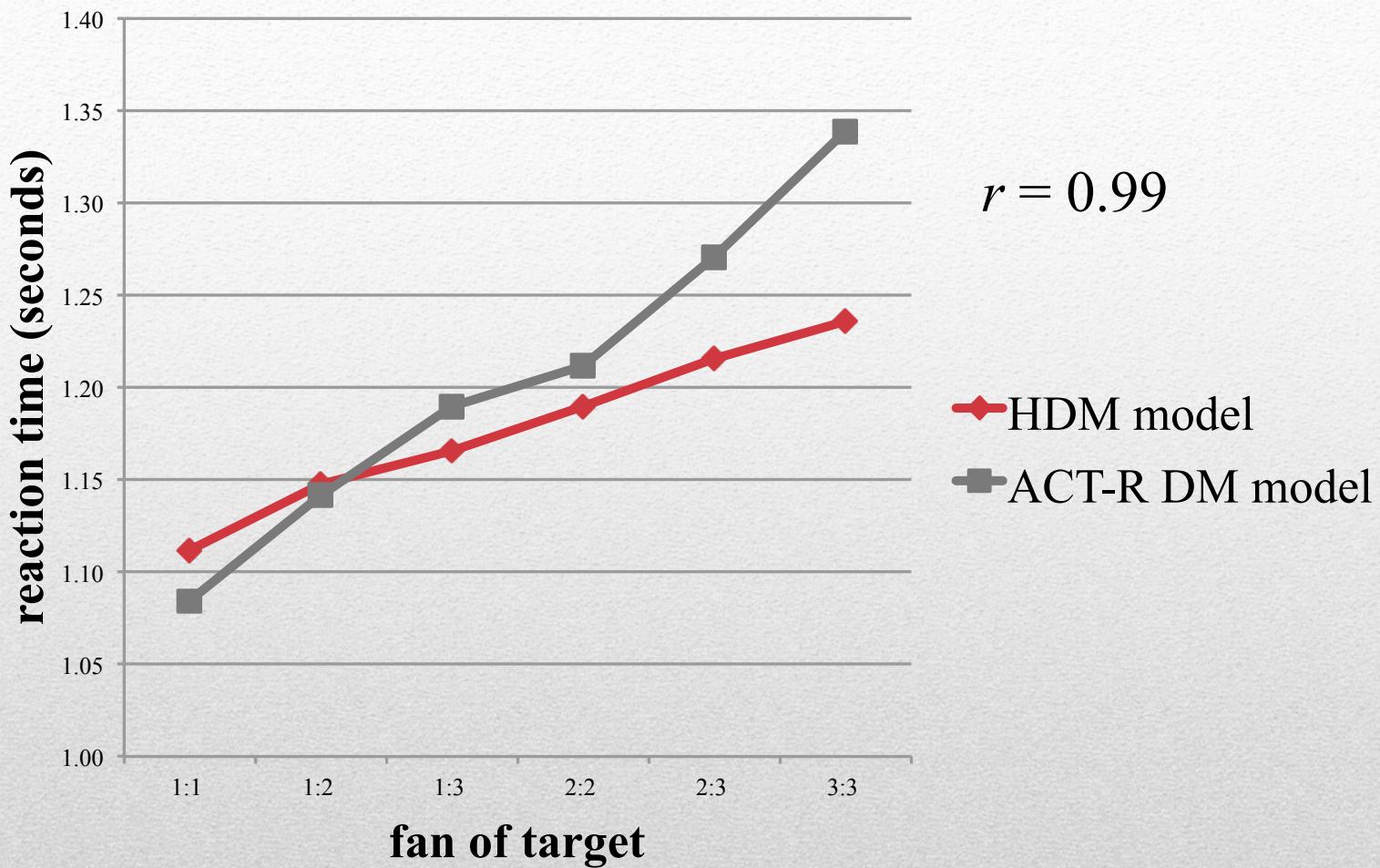
$$T = I + F e^{-Ai}$$

Parameters I and F set to the values used by Anderson and Reder's (1999) ACT-R DM model.

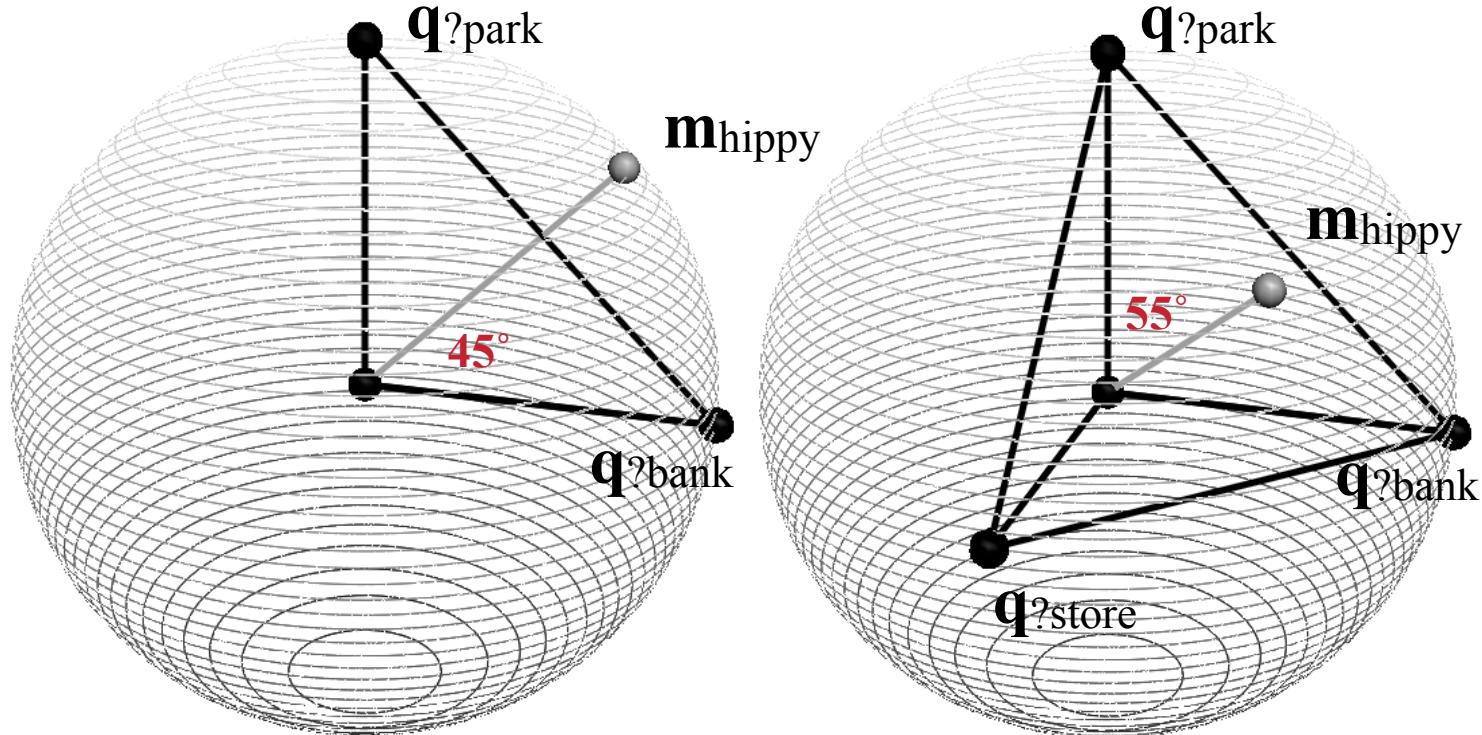
Activation & Reaction Time



HDM vs. Human



ACT-R DM vs. HDM



Fan in Vector Space

- Where f is the fan, the **cosine** between a **cue** and a **memory** vector is $f^{-1/2}$ if the vectors are perfectly orthogonal, or approximates $f^{-1/2}$ for the random vectors used by HDM.
- The cosine in HDM approximates the square-root of the probability only when the events are **equiprobable**.
- For n events with frequencies v_1 to v_n , cosine of event i is:

$$\text{cosine} = \frac{v_i}{\sqrt{v_1^2 + \dots + v_i^2 + \dots + v_n^2}}$$

Probability in Vector Space

We substitute **HDM** for **DM** in the ACT-R model of the fan effect and find that *without changing any parameters* HDM provides a good fit to the **fan effect**.

We present an **analysis** that allows us to specify the **mathematical** relationship between the **DM** and **HDM** models of the fan effect, and the relationship between HDM and the **conditional probability**.

Conclusions

HDM, by virtue of being a holographic model, has a number of capabilities for which DM is less suited:

- learning associations between concepts without having association strengths set by the modeler
- analogical or case-based reasoning
- performing tasks that require large amounts of knowledge

Future work

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