## Quantifying the Risk of Being Diagnosed with Diabetes Using Generalized Linear Mixed Effect Models

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**Final Project** 

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### **Background**

Diabetes is a common disease affecting 1 in 10 Americans. Diabetes can be dangerous because it is known to harm nerves and blood vessels, leading to serious health complications, such as strokes, heart disease, and blindness. It is known that diabetes affects cohorts of age, gender, and race differently. However, there are other individual factors that can increase the risk of diabetes, such as obesity.

Diabetes is more common among non-Hispanic blacks than whites and Asian Americans.

(ADA) It is also known that obesity, BMI, HDL cholesterol, gender, waist-to-hip ratio, and height can all be determinants of diabetes, as well. These are all simple and cheap measures that could be used to determine the risk that an individual has for getting diabetes. The development of a linear model could help to quantify the risk associated with these factors and being diagnosed with diabetes.

## **Problem Description**

Using publicly available data, a generalized mixed effect model will be built to help assess the risk of being diagnosed with diabetes.

#### Methods

#### **Data Description**

The data was retrieved from the Biostatistics Department at Vanderbilt and was originally collected by Dr. John Schorling of the University of Virginia School of Medicine for a

study on church-based smoking cessation interventions for rural African Americans.

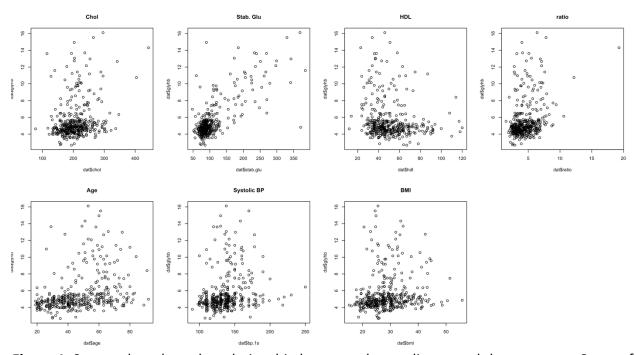
(SCHORLING, 1997). Data was collected from the African American populations from two different counties in Virginia in the 1990s. There were 19 variables and 403 individuals studied; Table 1 describes the variables measured.

VARIABLE	DESCRIPTION			
ID	Subject ID			
CHOL	Total cholesterol			
STAB.GLU	Stabilized glucose conc. In blood			
HDL	High density lipoprotein			
RATIO	Ratio of cholesterol to HDL			
GLYHB	Glycosylated hemoglobin			
LOCATION	County observation resides in;			
	either Buckingham or Louisa			
AGE	Age of participant in years			
GENDER	Gender of participant			
HEIGHT	Height of participant in inches			
WEIGHT	Weight of participant in pounds			
FRAME	Description of body frame as small,			
	medium, or large			
BP.1S	First systolic blood pressure reading			
BP.1D	First diastolic blood pressure reading			
BP.2S	Second systolic blood pressure reading			
BP.2D	Second diastolic blood pressure reading			
WAIST	Measure of waist circumference in inches			
HIP	Measure of hip circumference in inches			
TIME.PPN	Post-prandial time between when labs			
	were drawn recorded in minutes			

**Table 1:** Description of variables in dataset.

Figure 1 below shows scatterplots of the response (as a continuous variable) and some of the continuous predictors. There are clear linear relationships between some (Stabilized Glucose) and there are weak relationships between others (total cholesterol to HDL ratio). The

scatterplots also suggest that the data might be skewed for some of the predictors, such as age and BMI.



**Figure 1:** Scatterplots show the relationship between the predictors and the response. Some of the data appears to be skewed and there is some linear relationship.

#### Missing Values and Imputation

There are a substantial number of missing values in this data set. There are 575 NA values and 524 of those belong to two variables: the second readings of systolic and diastolic blood pressure (262 missing values each). That means that approximately 65% of the measurements for these two variables are missing. For this reason, these variables were omitted from the analysis. The other variables had at most 3.2% missingness. The amount of missing variables are illustrated in Figure 2 below. Upon examination of missing values, it is assumed that they are missing completely at random (MCAR). The missing data values were imputed using the "mice" package in R. There were a total of 5 imputed datasets using a

predictive mean matching imputation method. Figure 3 shows a density plot of the imputed values overlayed with the density of the original values. This figure shows that the imputed values (colored magenta) are similar to the original.

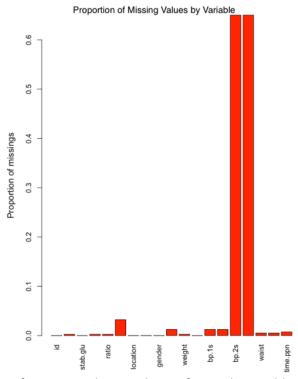
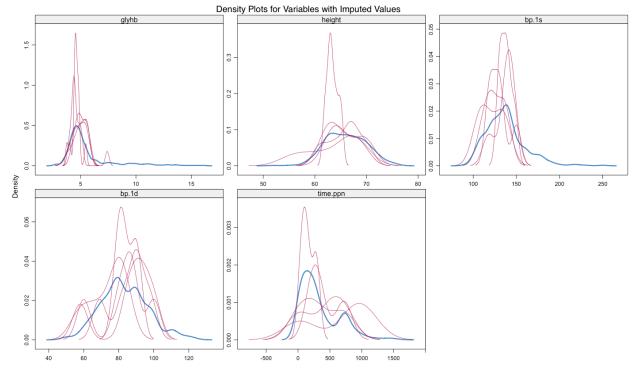


Figure 2: The proportion of missing values is shown for each variable. For data imputation, it is advised that no more than 5% of the data be missing.



**Figure 3:** Density plots are shown for the variables with imputed missing values. The blue distributions represent original data and the magenta distributions (for the 5 imputed datasets) represent imputed values. It is desirable to see peaks in the imputed data near the peaks of the original data, suggesting that the imputed data is similar to the original data.

#### Introduction of New Variables

The original variables were manipulated from the original. A new variable of BMI (Body Mass Index) was calculated for each observation. The formula below in Equation 1 shows how to calculate BMI from weight and height using pounds and inches. It has been observed that BMI is positively associated with having diabetes mellitus. (Bays et al, 2007) For this reason, BMI was included in the analysis.

$$BMI = 703 \frac{weight}{(height)^2} \tag{1}$$

The response variable, glycosylated hemoglobin, is a recorded as continuous variable and is used to diagnose diabetes. A positive diagnosis of diabetes is given for values greater than 7.0. A new categorical variable was created to represent a positive diagnosis of diabetes (glyhb > 7.0).

#### **Preliminary Data Exploration**

A preliminary analysis of the linear relationship between continuous predictor variables and response variable (glyhb) was performed using ANOVA and restricted cubic splines (utilizing 3 knots). The ANOVA uses a Chi-Square test to determine the significance of a non-linear relationship between the predictor and response. Figure 4 shows the output for the Chi-Square test. Since the p-value is greater than 0.05, the non-linear term is not significant and a linear relationship exists. This analysis was performed for the remaining continuous variables and the results are summarized in Table 2. Terms determined to have significant non-linear relationships with diabetes used restricted cubic splines in the regression model discussed later.

	Wald Statistics			Response:	glyhb
Factor	Chi-Square	d.f.	Р		
chol	14.17	2	0.0008		
Nonlinear	0.01	1	0.9129		
TOTAL	14.17	2	0.0008		

**Figure 4:** The results of fitting a restricted cubic splines model of cholesterol onto glycosylated hemoglobin. The p-value of the Chi-Square test suggests that a linear relation will suffice in predicting the response.

VARIABLE	$\chi^2$ STATISTIC	DF	P-VALUE	RELATIONSHIP TO RESPONSE
CHOLESTEROL	0.01	1	0.913	Linear
STABILIZED GLUCOSE	10.20	1	0.001	Non-linear
HDL	3.83	1	0.050	Linear
RATIO CHOL/HDL	0.32	1	0.570	Linear
AGE	5.74	1	0.0167	Non-Linear
HEIGHT	0.00	1	0.947	Linear
WEIGHT	2.57	1	0.109	Linear
SYSTOLIC B.P.	5.58	1	0.018	Non-Linear
DIASTOLIC B.P.	0.35	1	0.556	Linear
WAIST	1.96	1	0.161	Linear
HIP	2.97	1	0.085	Linear
POST-PRANDIAL TIME	0.00	1	0.968	Linear
BMI	3.27	1	0.071	Linear

**Table 2:** The results of a Chi-Square test are shown; the results describe the linearity of the relationship between the continuous predictors and the response.

## **Model Building**

#### **Model Selection**

A generalized linear mixed model (GLMM) and multiple logistic regression model (Generalized Linear Model) were chosen to model the data. A comparison of these models' fit is explored. The data was collected from a group of African Americans in a congregated region of Virginia and those who interacted regularly at the same churches. It is suspected that the data may be clustered for this reason. The incorporation of a random variable in the GLMM helps to model the possible correlation of the observations. GLMMs make several assumptions: 1) normality, 2) the logit link function is appropriate, and 3) there is constant variance among residual errors and random effects. GLMMs use Gauss-Hermite Quadrature to calculate maximum likelihood estimates of the parameters. A random intercept model was chosen because longitudinal data was not considered. If longitudinal data was considered, it

may have been desirable to include a random slope term to model the random aspect to the change in blood pressure measurements for each individual. However, since the only data considered is the data that the participants show up with, a random intercept model was chosen because the intercept represents the participants' baseline measurements and no change is measured. Multiple logistic regression models are easier to interpret and work with in R, therefore a likelihood ratio test was used to compare the fits of the GLMM and multiple logistic regression models. Multiple logistic regression utilizes maximum likelihood estimation to approximate the model parameters.

A full GLMM model was fit and then backwards selection was used to reduce the model. A random intercept was incorporated based on participant location. For the sake of interpretability, a multiple logistic regression model was fit and a likelihood ratio test was used to compare the two models. The test is used to determine of the difference in log-likelihoods of the two models is statistically significant (the reduced models were used in the comparison after confirming that both the reduced models were adequate compared to their respective full models using likelihood ratio tests). The result was a p-value of 0.990, suggesting that the two models are not significantly different. Therefore, a multiple logistic regression model was used and those results are presented. The R output for the full and reduced GLMM models are shown in Figures 5 and 6, respectively. The R output for the full model is shown below in Figure 7. There are some drawbacks to using backwards elimination, including that some predictors that are important may be eliminated based on p-value. Another hazard of backwards selection is that variables may become insignificant after other variables are removed and then may become significant again. (Chowdhury & Turin, 2020) For this reason, outside research

was used to double-check the validity of the findings of backwards selection. Some variables were kept solely due to the findings of other researchers. These variables include BMI, waist-to-hip ratio, HDL, obesity (measured with BMI in our case), and height. (Schmidt et al, 1992; Bays et al, 2007; Farbstein & Levy, 2012; WILLER; Schulze et al 1970) For this reason, BMI and the waist-to-hip ratio were kept in the model even though their coefficients were insignificant. The final reduced model is shown in Figure 8. A significance level of 0.15 was used for variables that weren't suggested as having a relationship with diabetes in other research.

```
| Generalized linear mixed model fit by maximum likelihood (Adaptive Gauss-Hermite Quadrature, nAGQ = 10) [glmerMod] | Family binomial ( logit ) | 1500.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 | 1700.00 |
```

Figure 5: A full GLMM model was fit and the results are shown.

Figure 6: A reduced GLMM model was fit. A summary of the fit is shown.

```
glm(formula = glyhb.cat ~ chol + stab.glu + hdl + ratio + age + height + weight + bp.1s + bp.1d + waist * hip + gender *
    bmi, data = dat)
Deviance Residuals:
Min 1Q Median 3Q Max
-1.23397 -0.11029 -0.03622 0.03830 1.11588
Coefficients:
               Estimate Std. Error t value Pr(>|t|)
-1.261e-02 1.367e+00 -0.009 0.993
(Intercept)
chol
                 3.797e-04 5.631e-04 0.674
                                                     0.501
                                                    <2e-16 ***
stab.glu
                 4.301e-03 2.635e-04 16.323
                                         -0.004
                -6.457e-06 1.758e-03
ratio
                1.183e-02 1.960e-02
                                           0.603
                                                     0.547
                 1.382e-03 1.016e-03
heiaht
                -3.208e-04 2.050e-02 -0.016
                                                     0.988
                -7.739e-06 3.775e-03
                                                     0.998
                                          -0.002
weight
bp.1s
                 7.611e-04 8.254e-04
                                           0.922
                                                     0.357
                -1.967e-04 1.264e-03
bp.1d
                                         -0.156
                                                     0.876
waist
                -9.012e-03 1.540e-02
                                         -0.585
                                                     0.559
                -1.991e-02 1.493e-02
hip
                                          -1.334
                                                     0.183
                 9.711e-02 1.767e-01
bmi
                 2.904e-03 2.144e-02
                                         0.135
                                                     0.892
                  3.462e-04 3.361e-04
                                          1.030
gendermale:bmi -5.260e-03 6.227e-03 -0.845
                                                     0.399
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
(Dispersion parameter for gaussian family taken to be 0.06532482)
Null deviance: 51.067 on 402 degrees of freedom
Residual deviance: 25.281 on 387 degrees of freedom
AIC: 61.8
Number of Fisher Scoring iterations: 2
```

Figure 7: A full multiple logistic regression model was fit using most of the original variables.

```
glm(formula = glyhb.cat ~ chol + stab.glu + rcs(stab.glu, 3) + hdl + age + bp.1s + gender * bmi + w.h.ratio, family = binomial(), data = dat)
Deviance Residuals:

Min 1Q Median 3Q Max
-2.8046 -0.2787 -0.1431 -0.0596 3.9586
 Coefficients: (1 not defined because of singularities)
                                -21.503234
0.007525
(Intercept)
 stab.glu
                                                          3.693 0.000222 ***
                                 0.112142
                                              0.030368
rcs(stab.glu, 3)stab.glu NA rcs(stab.glu, 3)stab.glu' -0.202352
                                                         NA NA
-2.627 0.008619 **
                                              0.077033
                                -0.015832
                                              0.013843
                                 0.025209
0.012514
                                              0.015811
age
bp.1s
                                              0.009540
                                                          1.312 0.189598
gendermale
bmi
                                 2.242253
                                              2.159681
                                                          1.038 0.299161
                                 0.043515
3.431615
                                              0.035698
3.139357
                                                           1.219 0.222863
w.h.ratio
gendermale:bmi
                                -0.098068
                                              0.074321 -1.320 0.186996
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for binomial family taken to be 1)
     Null deviance: 339.14 on 402 degrees of freedom
Residual deviance: 155.28 on 392 degrees of freedom AIC: 177.28
Number of Fisher Scoring iterations: 7
```

**Figure 8:** After backwards elimination, a reduced model was determined. Not all of the predictors are significant, but some were kept because of significance determined in other studies.

Table 3 summarizes the results of the multiple logistic regression. The confidence intervals suggest that some of the parameters are not useful in the explanation of the response and can be removed since the interval contains 0. The coefficients were kept because other research suggests that these are significant in explaining diabetes. Based on the confidence intervals, only one of the variables had a significant relationship with predicting diabetes: stabilized glucose levels (zero is not in the 95% confidence interval)l. The estimated odds of contracting diabetes increases by  $e^{0.112} = 1.119$  times (an 11.9% increase) higher for each unit increase in stabilized glucose.

COEFFICIENT	<b>ESTIMATE</b>	STANDARD ERROR	CONFIDENCE INTERVAL
INTERCEPT	-21.503	4.639	(-31.286, -12.962)
CHOL	0.008	0.005	(-0.002, 0.018)
STAB.GLU	0.112	0.030	(0.0564, 0.176)
RCS(STAB.GLU, 3)STAB.GLU'	-0.202	0.077	(-0.361, -0.057)
HDL	-0.016	-0.015	(-0.044, -0.011)
AGE	0.025	0.016	(-0.006, 0.057)
BP.1S	0.013	0.010	(-0.007, 0.031)
<b>GENDER: MALE</b>	2.242	2.242	(-2.047, 6.482)
ВМІ	0.044	0.036	(-0.028, 0.114)
<b>WAIST-TO-HIP RATIO</b>	3.432	3.139	(-2.729, 9.647)
GENDER:MALE*BMI	-0.098	-0.098	(-0.245, 0.048)

**Table 3:** This table shows the same results as Figure 7. Parameter estimates are given with standard error for the reduced model.

#### **Model Validation**

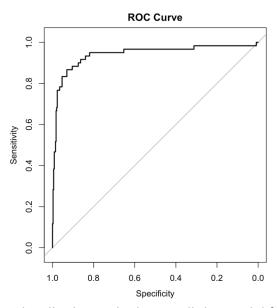
A likelihood ratio test was used to compare the utility of the full and reduced models. A p-value of 0.999 suggests that the reduced model is adequate in explaining the variance in the response variable.

Singularity was an issue encountered with modeling the GLMM. Singularity in GLMMs occurs when the model may be overfit and the variance of the effects is close to zero. There is no consensus on how to handle singularity in this context. This may have impacted the fit and decision to use a Generalized Linear Model.

There were 5 data sets with different imputed values. It is customary to perform the regression on all of the datasets and then pool the results. All of the regressions produced equivalent values for the parameter estimates.

A Receiver Operating Characteristic (ROC) curve is useful in determining the overall measure of fit of the model and how well it discriminates between outcomes. Figure 9 shows the ROC curve for the multiple linear regression model. The area under the curve (AUC) is a

measure of the fit of the model. A value of 0.5 implies a 50/50 guess, therefore a high AUC is desirable because it implies a higher prediction accuracy. The multiple logistic model has an AUC value of 0.942, which suggests high predictive accuracy for the data used to build it. Such a high value for AUC raises concern for overfitting.



**Figure 9:** A ROC curve graphically shows the how well the model fits the data used to build it. The model estimates the data far better than a simple 50/50 guess.

The dispersion of the data was measured using a Chi-Square Test with a Pearson ratio test statistic. This test had a p-value of 0, suggesting the measure of overdispersion is significantly different from zero. The presence of overdispersion may have impacted the results of fit and may impact the predictive ability of the model on new data, considering the GLM has such a high AUC (the model may be overfit).

#### **Model Assumption Check**

According to SCHIELZETH (2020), GLMMs are robust to "objective" failures of the normality assumption, therefore, there is not much concern about this violation.

The constant variance assumption was evaluated by testing for the existence of overdispersion. A Chi-Square test using the Pearson statistic was performed and a p-value of 0.999 was calculated, suggesting there is no significant difference between the amount of overdispersion and 0. The constant variance assumption is presumed to be satisfied. There may be under dispersion, and this should also be tested for.

#### **Discussion**

There was a degree of relaxation when the predictors were being selected to build the model. A high significance level of 15% was used to capture more variability in the model.

Also, features were chosen based on the importance discovered by the work of other researchers, even if their statistical significance did not mee the 15% threshold.

The data was collected from two small, rural counties and from African Americans who attended the same churches. Correlation between observations requires the use of a generalized mixed model. Since the data used to build the model was collected over 20 years ago, the prediction should not be relied upon for current patients. A new model should be developed based on recent data and can use the techniques employed in this paper. If new data is to be collected to explore the risk factors of diabetes, a larger dataset representing people from other areas of the country would be an improvement to help get rid of the cluster effect. The original data used in this paper was intended to solve a different research question

about church-going African Americans in rural locations and smoking programs, as it pertains to coronary disease.

Some of the assumptions of GLMMs were violated. Solutions to this issue include retrieving new data or using a different model. It has been shown by SCHIELZETH (2020) that GLMMs are robust in their parameter estimation when the normality and variance assumptions were not met. Other researchers have shown that different models, such as Artificial Neural Networks, Random Forests, and K-means clustering, are all suitable methods for predicting diabetes. (ALAM, 2019) Due to time constraints, the model was not evaluated in terms of under dispersion. Referring to the scatterplots in Figure 1, visually, it can be seen there is a possibility of under dispersion.

One issue encountered in building the model was that of singularity. A singular mixed model means that the parameters are on a boundary of the parameter space and that the variances of the effects are close to zero. The existence of singularity suggests that the model may be overfit. Singularity is a common issue encountered when using the GLMMs with large data sets. There is no clear method of handling singularity in this case, but several options have been suggested. Reducing the complexity of the model may allow the variance-covariance matrix of the GLMM to be estimated. (Matuschek et al, 2017) Other solutions involve model selection: 1) use a selection method that considers predictive accuracy and overfitting (Bates et al 2015, Matuschek et al 2017) and 2) use backwards selection prioritizing singularity rather than significance of terms. (Barr et al, 2013) Even with these suggestions, there is no consensus on how to deal with singularity in GLMMs.

All of the imputed datasets were used with the model and yielded similar results, even though they are not shown in the report (shown in the R code in Appendix I). Only the first imputed data set was used to build the regression model. Since so few data points were missing (other than the two variables that were dropped), there was very little difference in the model parameter estimates.

A multiple logistic regression model was successfully developed and shown to be a viable replacement to the GLMM in modeling the data. Further model calibration and validation is needed to assess the fit of the model and to determine the extent of multicollinearity.

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- Hannes Matuschek, Reinhold Kliegl, Shravan Vasishth, Harald Baayen, and Douglas Bates (2017). Balancing type I error and power in linear mixed models. *Journal of Memory and Language* **94**, 305–315.

## Appendix I: R Code and Output

```
> #Matthew Brigham
> #STA 531
> #Final Project
> # Diabetes With Generalized Linear Mixed Models and Multiple Logistic Regression.
> # MICE missing value imputation was used and one data set was used to beuild the models.
> # At the end of the code, the final regression model was used on the remaining imputed data sets
> # and it is shown that all of the coefficients are similar.
>#
> # Note: glyhb > 7 is diagnosed diabetes
>#
> # fit_08 is reduced GLM model
> ############ Import Data ###########
> orig_dat = read.csv("diabetes.csv")
> head(orig_dat)
 id chol stab.glu hdl ratio glyhb location age gender height weight frame bp.1s bp.1d bp.2s bp.2d waist hip
          82 56 3.6 4.31 Buckingham 46 female 62 121 medium 118 59 NA NA 29 38
          97 24 6.9 4.44 Buckingham 29 female 64 218 large 112 68 NA NA 46 48
2 1001 165
3 1002 228 92 37 6.2 4.64 Buckingham 58 female 61 256 large 190 92 185 92 49 57
4 1003 78 93 12 6.5 4.63 Buckingham 67 male 67 119 large 110 50 NA NA 33 38
5 1005 249 90 28 8.9 7.72 Buckingham 64 male 68 183 medium 138 80 NA NA 44 41
time.ppn
   720
2
   360
3
   180
   480
   300
5
   195
6
> dat0 = orig dat
> ######## Data Manipulations ########
> # Identify and Impute Missing Values
  library(mice)
  library(VIM)
  # Look for Pattern of Missingness
  md.pattern(dat0) #tells us number of observations with that missing data structure
 id stab.glu location age gender frame chol hdl ratio weight waist hip time.ppn height bp.1s bp.1d glyhb bp.2s
136 1 1 1 1 1 1 1 1 1 1 1 1
                                     1 1 1 1 1 1
239 1
     1 11 1 1 1 1 1 1 1 1
                                      1 1 1 1 1 0
3 1
      1
         1 1 1 1 1 1 1 1 1 1
                                     1 1 1 1 0 1
               1 1 1 1 1
                            1 1 1
                                     1
                                        1 1 1
          1 1
               1
                  1 1 1 1
                            1
                               1 1
                                     1
                                           Ω
4 1
          1 1
               1 1 1 1 1
                            1 1 1
                                        Ω
      1
                                     1
         1 1
               1 1 1 1 1
                                        0 0
1 1
      1
                            1 1 1
                                     1
1 1
      1
         1 1
              1 1 1 1 1 1 1 1
                                     0
                                        1 1 1
1 1
      1
         1 1 1 1 1 1 1 1 1 1
                                     0 1 1 1
                                     0 1 0 0 1 0
1 1
      1
          1 1 1 1 1 1 1 1 1 1
      1
          1 1 1 1 1 1 1
                               0 0
                                     1 1 1 1
1 1
                                                 1
               1 1 1 1 1 1 0 0
```

```
1 1
             1 1 1 1 1 1 0 1 1
      1
                                               1 1 1 1 1 0
            1 1 1 1 0 0 0 1 1 1
                                               1 1 1 1 1 0
  0
       0
            0 0 0 0 1 1 1 1 2 2
                                               3 5 5 5 13 262
  bp.2d
136 1 0
239 0 2
3
   1 1
10
    0 3
3
    0 4
    0.3
    0 5
    0 3
1
    0 5
    1 2
1
    0 4
    0 3
1
   agg_plot = aggr(dat0, combined = F) #histogram showing proportion of missing data by variable
   # Impute NA values
   dat1=dat0
   dat1 = dat0[,-c(15, 16)] #remove categorical variables and 2nd measurements of BP
   imp = mice(dat1, maxit = 0) # 0 iterations
Warning message:
Number of logged events: 3
   pred_mat = imp$predictorMatrix #get predictor matrix
>
   method = imp$method #get methods, mostly pmm: predictive mean matching
   imp2 = mice(dat1, m=5, maxit = 50, predictorMatrix = pred_mat, method = method, seed = 500, print = F) #creates 5 datasets of imputed
values
   # Analyze the distribution with and without imputed values for each of 5 imputed datasets
   newdat_imp_1 = complete(imp2,1)
   newdat_imp_2 = complete(imp2,2)
   newdat_imp_3 = complete(imp2,3)
   newdat_imp_4 = complete(imp2,4)
   newdat_imp_5 = complete(imp2,5)
   #Density Plot of Imputed Data
   par(mfrow=c(2,7))
>
   densityplot(imp2)
> #Add new variables
   dat = newdat imp 1
   # Rescale and square nonlinear terms (determined later)
   dat$stab.glu.2 = ((dat$stab.glu - median(dat$stab.glu))/sd(dat$stab.glu))^2 #center before squaring
   dat$age.2 = ((dat$age - median(dat$age))/sd(dat$age))^2
   dat$bp.1s.2 = ((dat$bp.1s - median(dat$bp.1s))/sd(dat$bp.1s))^2
   # Change glyhb to categorical: glyhb>7 = 1, glyhb<7 = 0
   for (i in 1:length(dat$glyhb)){
    if (dat | glyhb[i] >= 7){
     dat$glyhb.cat[i] = 1
    } else if (dat$glyhb[i] < 7){
     dat$glyhb.cat[i] = 0
    }
   }
```

```
#calculate waist to hip ratio
   dat$w.h.ratio = (dat$waist)/dat$hip
   #Add new variable BMI
   dat$bmi = dat$weight/((dat$height)^2)*703
   # Change "frame" to a factor small, medium, large
   dat$frame = factor(dat$frame, levels = c("small", "medium", "large"))
> ####### Data Exploration #####
dat = newdat_imp_1 #first imputed data set
> #summary statistics of original and imputed data sets
  summary(dat) #contains imputed values and new values
           chol
                   stab.glu
                              hdl
                                       ratio
                                                 glyhb
Min.: 1000 Min.: 78.0 Min.: 48.0 Min.: 12.00 Min.: 1.50 Min.: 2.680
1st Qu.: 4792 1st Qu.:179.0 1st Qu.: 81.0 1st Qu.: 38.00 1st Qu.: 3.20 1st Qu.: 4.385
Median: 15766 Median: 204.0 Median: 89.0 Median: 46.00 Median: 4.20 Median: 4.840
Mean :15978 Mean :207.7 Mean :106.7 Mean :50.43 Mean :4.52 Mean :5.567
3rd Qu.:20336 3rd Qu.:230.0 3rd Qu.:106.0 3rd Qu.: 59.00 3rd Qu.: 5.40 3rd Qu.: 5.600
Max. :41756 Max. :443.0 Max. :385.0 Max. :120.00 Max. :19.30 Max. :16.110
 location
                       gender
                                    height
                                              weight
                                                      frame
               age
              Min. :19.00 Length:403
                                        Min. :52.00 Min. :99.0 Length:403
Length:403
Class:character 1st Qu.:34.00 Class:character 1st Qu.:63.00 1st Qu.:150.5 Class:character
Mode :character Median :45.00 Mode :character Median :66.00 Median :172.0 Mode :character
         Mean :46.85
                               Mean :66.02 Mean :177.5
         3rd Qu.:60.00
                               3rd Qu.:69.00 3rd Qu.:200.0
                               Max. :76.00 Max. :325.0
         Max. :92.00
            bp.1d
                      waist
                                hip
                                        time.ppn
Min.: 90.0 Min.: 48.00 Min.: 26.00 Min.: 30.00 Min.: 5.0
1st Qu.:121.5 1st Qu.: 75.00 1st Qu.:33.00 1st Qu.:39.00 1st Qu.: 90.0
Median: 136.0 Median: 82.00 Median: 37.00 Median: 42.00 Median: 240.0
Mean :136.9 Mean :83.34 Mean :37.88 Mean :43.02 Mean :341.3
3rd Qu.:146.0 3rd Qu.: 90.00 3rd Qu.:41.00 3rd Qu.:46.00 3rd Qu.: 525.0
Max. :250.0 Max. :124.00 Max. :56.00 Max. :64.00 Max. :1560.0
> summary(dat0) #contains NA values
   id
           chol
                   stab.glu
                              hdl
                                       ratio
                                                 glyhb
Min.: 1000 Min.: 78.0 Min.: 48.0 Min.: 12.00 Min.: 1.500 Min.: 2.68
1st Qu.: 4792 1st Qu.:179.0 1st Qu.: 81.0 1st Qu.: 38.00 1st Qu.: 3.200 1st Qu.: 4.38
Median: 15766 Median: 204.0 Median: 89.0 Median: 46.00 Median: 4.200 Median: 4.84
Mean :15978 Mean :207.8 Mean :106.7 Mean :50.45 Mean :4.522 Mean :5.59
3rd Qu.:20336 3rd Qu.:230.0 3rd Qu.:106.0 3rd Qu.: 59.00 3rd Qu.: 5.400 3rd Qu.: 5.60
Max. :41756 Max. :443.0 Max. :385.0 Max. :120.00 Max. :19.300 Max. :16.11
        NA's :1
                         NA's :1
                                   NA's :1 NA's :13
                       gender
                                    height
                                              weight
              Min. :19.00 Length:403
                                        Min. :52.00 Min. :99.0 Length:403
Length:403
Class :character 1st Qu.:34.00 Class :character 1st Qu.:63.00 1st Qu.:151.0 Class :character
Mode :character Median :45.00 Mode :character Median :66.00 Median :172.5 Mode :character
         Mean :46.85
                               Mean :66.02 Mean :177.6
         3rd Qu.:60.00
                               3rd Qu.:69.00 3rd Qu.:200.0
         Max. :92.00
                               Max. :76.00 Max. :325.0
                          NA's :5 NA's :1
                                bp.2d
  bp.1s
            bp.1d
                      bp.2s
                                           waist
                                                     did
                                                             time.ppn
Min.: 90.0 Min.: 48.00 Min.: 110.0 Min.: 60.00 Min.: 26.0 Min.: 30.00 Min.: 5.0
1st Qu.:121.2 1st Qu.: 75.00 1st Qu.:138.0 1st Qu.: 84.00 1st Qu.:33.0 1st Qu.:39.00 1st Qu.: 90.0
Median:136.0 Median:82.00 Median:149.0 Median:92.00 Median:37.0 Median:42.00 Median:240.0
Mean :136.9 Mean :83.32 Mean :152.4 Mean :92.52 Mean :37.9 Mean :43.04 Mean :341.2
3rd Qu.:146.8 3rd Qu.: 90.00 3rd Qu.:161.0 3rd Qu.:100.00 3rd Qu.:41.0 3rd Qu.:46.00 3rd Qu.: 517.5
Max. :250.0 Max. :124.00 Max. :238.0 Max. :124.00 Max. :56.0 Max. :64.00 Max. :1560.0
                    NA's :262 NA's :262 NA's :2 NA's :3
NA's :5
         NA's :5
> #Linearity - restricted cubic splines for continuous variables.
```

```
> fit chol = lrm(glyhb.cat ~ rcs(chol,3), x=T, y=T, data =dat)
Error in eval(predvars, data, callenv): object 'glyhb.cat' not found
> anova(fit chol) #linear p-value = 0.9129
Error in anova(fit chol): object 'fit chol' not found
   plot(dat$chol,dat$glyhb, main = "Chol")
Error in plot.new(): figure margins too large
   fit stab.glu = Irm(glyhb.cat ~ rcs(stab.glu,3), x=T, y=T, data =dat)
Error in eval(predvars, data, callenv): object 'glyhb.cat' not found
> anova(fit_stab.glu) #NONLINEAR p-value = 0.0014
Error in anova(fit stab.glu): object 'fit stab.glu' not found
   plot(dat$stab.glu,dat$glyhb, main = "Stab. Glu")
Error in plot.new(): figure margins too large
> fit_hdl = lrm(glyhb.cat ~ rcs(hdl,3), x=T, y=T, data =dat)
Error in eval(predvars, data, callenv): object 'glyhb.cat' not found
> anova(fit hdl) #LINEAR or NONLINEAR p-value = 0.0502
Error in anova(fit_hdl): object 'fit_hdl' not found
   plot(dat$hdl,dat$glyhb, main = "HDL")
Error in plot.new(): figure margins too large
   fit_ratio = lrm(glyhb.cat ~ rcs(ratio,3), x=T, y=T, data =dat)
Error in eval(predvars, data, callenv): object 'glyhb.cat' not found
> anova(fit ratio) #LINEAR p-value = 0.5695
Error in anova(fit_ratio): object 'fit_ratio' not found
   plot(dat$ratio,dat$glyhb, main = "ratio")
Error in plot.new(): figure margins too large
> fit_age = lrm(glyhb.cat ~ rcs(age,3), x=T, y=T, data =dat)
Error in eval(predvars, data, callenv): object 'glyhb.cat' not found
> anova(fit_age) #NONLINEAR p-value = 0.0166
Error in anova(fit_age) : object 'fit_age' not found
> plot(dat$age,dat$glyhb, main = "Age")
Error in plot.new(): figure margins too large
   fit_height = Irm(glyhb.cat ~ rcs(height,3), x=T, y=T, data =dat)
Error in eval(predvars, data, callenv): object 'glyhb.cat' not found
> anova(fit_height) #LINEAR p-value = 0.9470
Error in anova(fit height): object 'fit height' not found
   plot(dat$height,dat$glyhb, main = "Height")
Error in plot.new(): figure margins too large
   fit_weight = lrm(glyhb.cat ~ rcs(weight,3), x=T, y=T, data =dat)
Error in eval(predvars, data, callenv): object 'glyhb.cat' not found
   anova(fit weight) #LINEAR or NONLINEAR p-value = 0.1086
Error in anova(fit_weight) : object 'fit_weight' not found
   plot(dat$weight.dat$glvhb, main = "Weight")
Error in plot.new(): figure margins too large
   fit bp.1s = lrm(glyhb.cat ~ rcs(bp.1s,3), x=T, y=T, data =dat)
Error in eval(predvars, data, callenv): object 'glyhb.cat' not found
> anova(fit bp.1s) #NONLINEAR p-value = 0.0182
Error in anova(fit_bp.1s): object 'fit_bp.1s' not found
> plot(dat$bp.1s,dat$glyhb, main = "Systolic BP")
Error in plot.new(): figure margins too large
   fit_bp.1d = lrm(glyhb.cat ~ rcs(bp.1d,3), x=T, y=T, data =dat)
Error in eval(predvars, data, callenv): object 'glyhb.cat' not found
> anova(fit_bp.1d) #LINEAR p-value = 0.5562
Error in anova(fit bp.1d): object 'fit bp.1d' not found
   plot(dat$bp.1d,dat$glyhb, main = "Diastolic BP")
Error in plot.new(): figure margins too large
   fit_waist = lrm(glyhb.cat ~ rcs(waist,3), x=T, y=T, data =dat)
Error in eval(predvars, data, callenv): object 'glyhb.cat' not found
```

```
> anova(fit_waist) #LINEAR p-value = 0.1611
Error in anova(fit waist): object 'fit waist' not found
> plot(dat$waist,dat$glyhb, mian = "Waist")
Error in plot.new(): figure margins too large
   fit_hip = lrm(glyhb.cat ~ rcs(hip,3), x=T, y=T, data =dat)
Error in eval(predvars, data, callenv): object 'glyhb.cat' not found
> anova(fit hip) #LINEAR or NONLINEAR p-value = 0.0846
Error in anova(fit hip): object 'fit hip' not found
> plot(dat$hip,dat$glyhb, main = "Hip")
Error in plot.new(): figure margins too large
   fit_time.ppn = lrm(glyhb ~ rcs(time.ppn,3), x=T, y=T, data =dat)
   anova(fit_time.ppn) #LINEAR p-value = 0.9678
        Wald Statistics
                           Response: glyhb
Factor Chi-Square d.f. P
time.ppn 0.52 2 0.7729
 Nonlinear 0.51
                 1 0.4772
TOTAL 0.52 2 0.7729
> plot(dat$time.ppn,dat$glyhb, main = "Time.ppn")
Error in plot.new(): figure margins too large
> fit_bmi = lrm(glyhb ~ rcs(bmi,3), x=T, y=T, data =dat)
Error in rcs(bmi, 3): object 'bmi' not found
> anova(fit_bmi) #LINEAR or NONLINEAR p-value = 0.0706
Error in anova(fit_bmi) : object 'fit_bmi' not found
> plot(dat$bmi,dat$glyhb, main = "BMI")
Error in xy.coords(x, y, xlabel, ylabel, log):
 'x' and 'y' lengths differ
> #Scatterplots
   x1 = dat[,c("glyhb", "chol", "stab.glu", "stab.glu.2", "hdl", "ratio", "age",
         "bp.1s", "bmi", "age.2", "w.h.ratio" )]
Error in `[.data.frame`(dat,,c("glyhb", "chol", "stab.glu", "stab.glu.2",:
undefined columns selected
   pairs(x1)
Error in pairs(x1): object 'x1' not found
   par(mfrow = c(2,4))
   plot(dat$chol,dat$glyhb, main = "Chol")
   plot(dat$stab.glu,dat$glyhb, main = "Stab. Glu")
   plot(dat$hdl,dat$glyhb, main = "HDL")
   plot(dat$ratio,dat$glyhb, main = "ratio")
   plot(dat$age,dat$glyhb, main = "Age")
   plot(dat$bp.1s,dat$glyhb, main = "Systolic BP")
   plot(dat$bmi,dat$glyhb, main = "BMI")
Error in xy.coords(x, y, xlabel, ylabel, log):
'x' and 'y' lengths differ
> ####### GLMM W/ and W/O Random Location and Restr. Cubic Splines
> #Fit glmer with random effect location
   #Full Model
   fit_1 = glmer(glyhb.cat ~ chol + stab.glu + rcs(stab.glu, 3) + hdl + ratio + age + rcs(age, 3) + height
           + weight + frame + bp.1s + rcs(bp.1s, 3) + bp.1d + waist*hip + gender*bmi + w.h.ratio
           + (1 | location), data = dat, family = binomial,
           control = glmerControl(optimizer = "bobyga"),
           nAGQ = 10)
Error in eval(predvars, data, env): object 'glyhb.cat' not found
> sumfit_1 = summary(fit_1);
   sumfit_1
```

```
Generalized linear mixed model fit by maximum likelihood (Adaptive Gauss-Hermite Quadrature, nAGQ = 10) [glmerMod]
Family: binomial (logit)
Formula: glyhb.cat ~ chol + stab.glu + rcs(stab.glu, 3) + hdl + ratio +
 age + rcs(age, 3) + height + weight + frame + bp.1s + rcs(bp.1s,
  3) + bp.1d + waist * hip + gender * bmi + w.h.ratio + (1 | location)
 Data: dat
Control: glmerControl(optimizer = "bobyqa")
  AIC BIC logLik deviance df.resid
 193.8 285.1 -73.9 147.8 368
Scaled residuals:
 Min 1Q Median 3Q Max
-12.766 -0.186 -0.095 -0.030 55.409
Random effects:
Groups Name
                 Variance Std.Dev.
location (Intercept) 0
Number of obs: 391, groups: location, 2
Fixed effects:
              Estimate Std. Error z value Pr(>|z|)
(Intercept)
                 17.378312 34.788031 0.500 0.6174
chol
               0.013604 \ 0.009213 \ 1.477 \ 0.1398
stab.glu
                 0.112609 0.031808 3.540 0.0004 ***
hdl
               -0.274750 0.298238 -0.921 0.3569
ratio
               0.085484 0.060292 1.418 0.1562
age
rcs(age, 3)age'
                  -0.066389 0.063936 -1.038 0.2991
height
                -0.353933  0.396287 -0.893  0.3718
weight
                 0.052933 0.066866 0.792 0.4286
framemedium
                     -0.411135  0.651062  -0.631  0.5277
framelarge
                  -0.835901 0.815884 -1.025 0.3056
                0.041050 0.035885 1.144 0.2526
bp.1s
rcs(bp.1s, 3)bp.1s'
                    -0.028929 0.031843 -0.908 0.3636
                0.002631 0.022976 0.115 0.9088
bp.1d
               0.678614 0.665461 1.020 0.3078
waist
hip
              -0.486744 0.577057 -0.843 0.3990
                   5.497504 3.646371 1.508 0.1316
gendermale
               -0.241231 0.373216 -0.646 0.5180
bmi
                -23.487465 28.590671 -0.822 0.4114
w.h.ratio
waist:hip
                 -0.001260 0.003418 -0.369 0.7124
gendermale:bmi
                     -0.194605 0.122699 -1.586 0.1127
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 '' 1
Correlation matrix not shown by default, as p = 22 > 12.
Use print(x, correlation=TRUE) or
 vcov(x)
           if you need it
fit warnings:
fixed-effect model matrix is rank deficient so dropping 3 columns / coefficients
Some predictor variables are on very different scales: consider rescaling
convergence code: 0
boundary (singular) fit: see ?isSingular
   #remove bp.1d
   fit_2 = glmer(glyhb.cat ~ chol + stab.glu + rcs(stab.glu, 3) + hdl + ratio + age + rcs(age, 3) + height
          + weight + frame + bp.1s + rcs(bp.1s, 3) + waist*hip + gender*bmi + w.h.ratio
          + (1 | location), data = dat, family = binomial,
          control = glmerControl(optimizer = "bobyqa"),
          nAGQ = 10)
Error in eval(predvars, data, env): object 'glyhb.cat' not found
```

sumfit\_2 = summary(fit\_2);

```
Error in h(simpleError(msg, call)) :
error in evaluating the argument 'object' in selecting a method for function 'summary': object 'fit 2' not found
> sumfit 2
Error: object 'sumfit 2' not found
    #remove frame
   fit_3 = glmer(glyhb.cat \sim chol + stab.glu + rcs(stab.glu, 3) + hdl + ratio + age + rcs(age, 3) + height
            + weight + bp.1s + rcs(bp.1s, 3) + waist*hip + gender*bmi + w.h.ratio
            + (1 | location), data = dat, family = binomial,
           control = glmerControl(optimizer = "bobyqa"),
            nAGQ = 10)
Error in eval(predvars, data, env): object 'glyhb.cat' not found
> sumfit_3 = summary(fit_3);
Error in h(simpleError(msg, call)) :
error in evaluating the argument 'object' in selecting a method for function 'summary': object 'fit 3' not found
> sumfit 3
Error: object 'sumfit_3' not found
    #remove waist*hip
   fit_4 = glmer(glyhb.cat ~ chol + stab.glu + rcs(stab.glu, 3) + hdl + ratio + age + rcs(age, 3) + height
            + weight + bp.1s + rcs(bp.1s, 3) + gender*bmi + w.h.ratio
            + (1 | location), data = dat, family = binomial,
            control = glmerControl(optimizer = "bobyqa"),
            nAGQ = 10)
Error in eval(predvars, data, env): object 'glyhb.cat' not found
   sumfit_4 = summary(fit_4);
Error in h(simpleError(msg, call)):
error in evaluating the argument 'object' in selecting a method for function 'summary': object 'fit_4' not found
> sumfit 4
Error: object 'sumfit_4' not found
   #remove waist*hip
   fit_4 = glmer(glyhb.cat ~ chol + stab.glu + rcs(stab.glu, 3) + hdl + ratio + age + rcs(age, 3) + height
            + weight + bp.1s + rcs(bp.1s, 3) + gender*bmi + w.h.ratio
            + (1 | location), data = dat, family = binomial,
            control = glmerControl(optimizer = "bobyqa"),
            nAGQ = 10)
Error in eval(predvars, data, env): object 'glyhb.cat' not found
   sumfit_4 = summary(fit_4);
Error in h(simpleError(msg, call)) :
error in evaluating the argument 'object' in selecting a method for function 'summary': object 'fit_4' not found
Error: object 'sumfit_4' not found
   #remove weight
   fit_5 = glmer(glyhb.cat ~ chol + stab.glu + rcs(stab.glu, 3) + hdl + ratio + age + rcs(age, 3) + height
            + bp.1s + rcs(bp.1s, 3) + gender*bmi + w.h.ratio
            + (1 | location), data = dat. family = binomial.
           control = glmerControl(optimizer = "bobyqa"),
           nAGQ = 10)
Error in eval(predvars, data, env): object 'glyhb.cat' not found
  sumfit 5 = summary(fit 5);
Error in h(simpleError(msg, call)):
error in evaluating the argument 'object' in selecting a method for function 'summary': object 'fit_5' not found
Error: object 'sumfit_5' not found
   #remove ratio
   fit_6 = glmer(glyhb.cat ~ chol + stab.glu + rcs(stab.glu, 3) + hdl + age + rcs(age, 3) + height
            + bp.1s + rcs(bp.1s, 3) + gender*bmi + w.h.ratio
            + (1 | location), data = dat, family = binomial,
           control = glmerControl(optimizer = "bobyga"),
            nAGQ = 10)
Error in eval(predvars, data, env): object 'glyhb.cat' not found
> sumfit 6 = summary(fit 6);
Error in h(simpleError(msg, call)):
```

```
error in evaluating the argument 'object' in selecting a method for function 'summary': object 'fit_6' not found
Error: object 'sumfit_6' not found
   #remove rcs(bp.1s, 3)
   fit_7 = glmer(glyhb.cat ~ chol + stab.glu + rcs(stab.glu, 3) + hdl + age + rcs(age, 3) + height
          + bp.1s + gender*bmi + w.h.ratio
          + (1 | location), data = dat, family = binomial.
          control = glmerControl(optimizer = "bobyqa"),
          nAGQ = 10)
Error in eval(predvars, data, env): object 'glyhb.cat' not found
> sumfit 7 = summary(fit 7);
Error in h(simpleError(msg, call)):
error in evaluating the argument 'object' in selecting a method for function 'summary': object 'fit_7' not found
Error: object 'sumfit_7' not found
   #remove rcs(age, 3)
   fit_8 = glmer(glyhb.cat ~ chol + stab.glu + rcs(stab.glu, 3) + hdl + age + height
          + bp.1s + gender*bmi + w.h.ratio
          + (1 | location), data = dat, family = binomial,
          control = glmerControl(optimizer = "bobyga"),
          nAGQ = 10)
Error in eval(predvars, data, env): object 'glyhb.cat' not found
   sumfit_8 = summary(fit_8);
   sumfit 8
Generalized linear mixed model fit by maximum likelihood (Adaptive Gauss-Hermite Quadrature, nAGQ = 10) [glmerMod]
Family: binomial (logit)
Formula: glyhb.cat ~ chol + stab.glu + rcs(stab.glu, 3) + hdl + age +
  height + bp.1s + gender * bmi + w.h.ratio + (1 | location)
 Data: dat
Control: glmerControl(optimizer = "bobyqa")
  AIC BIC logLik deviance df.resid
 181.3 233.2 -77.6 155.3 390
Scaled residuals:
 Min 1Q Median 3Q Max
-7.308 -0.200 -0.102 -0.043 49.821
Random effects:
                 Variance Std.Dev.
Groups Name
location (Intercept) 0
Number of obs: 403, groups: location, 2
Fixed effects:
              Estimate Std. Error z value Pr(>|z|)
                 -20.682689 7.486508 -2.763 0.005733 **
(Intercent)
chol
                0.007519 0.005134 1.465 0.143041
                 stab.glu
-0.016004 0.013897 -1.152 0.249503
               0.024570 0.016441 1.494 0.135070
age
                height
                0.012636 0.009569 1.321 0.186632
bp.1s
gendermale
                    2.308531 2.212538 1.043 0.296770
bmi
                0.042620 0.036265 1.175 0.239899
                 3.498648 3.177621 1.101 0.270885
w.h.ratio
gendermale:bmi
                     -0.098308 0.074387 -1.322 0.186307
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Correlation of Fixed Effects:
      (Intr) chol stb.gl r(.,3) hdl age height bp.1s gndrml bmi w.h.rt
       -0.109
chol
stab.glu -0.533 0.010
```

```
rcs(s.,3).' 0.541 0.009 -0.988
      -0.135 -0.165 0.023 -0.027
      -0.178 -0.103 -0.074 0.054 -0.089
height -0.785 0.005 0.131-0.164 0.089 0.278
bp.1s
      -0.103 -0.039 0.129 -0.096 -0.049 -0.362 -0.092
gendermale -0.007 0.049 -0.009 0.047 -0.036 -0.088 -0.214 0.129
      -0.275 -0.034 -0.065 0.068 0.148 0.242 0.178 -0.079 0.457
w.h.ratio -0.249 -0.031 0.073 -0.067 -0.035 -0.175 -0.154 -0.013 0.188 -0.043
genderml:bm 0.176 -0.031 -0.037 0.000 0.097 0.048 0.023 -0.120 -0.952 -0.430 -0.248
fit warnings:
fixed-effect model matrix is rank deficient so dropping 1 column / coefficient
convergence code: 0
boundary (singular) fit: see ?isSingular
>
   #likelihood ratio test for full and reduced GLMM data sets
> res_dev_glmm_loc_reduced = 155.3
  res_dev_glmm_full =
   df_glmm_loc_reduced = 390
   df_glmm_loc_full =
  AIC glmm loc reduced = 181.3
   AIC glmm loc full =
   lower.tail = F) #p-value is 0.990 - therefore can use either
> ####### Multiple Logistic Regression Assessment
> #Compare to glmm random location with likelihood ratio test
> #Restricted cubic splines were used to model terms identified as non-linear
   md.pattern(dat) #tells us number of observations with that missing data structure
{ `---' }
{00}
==> V <== No need for mice. This data set is completely observed.
 id chol stab.glu hdl ratio glyhb location age gender height weight frame bp.1s bp.1d waist hip time.ppn
> agg_plot = aggr(dat, combined = F) #histogram showing proportion of missing data by variable
   #full model - removed frame, rcs(bp.1s, 3), rcs(stab.glu, 3), rcs(age, 3), w.h.ratio
   fit_01 = glm(glyhb.cat ~ chol + stab.glu + hdl + ratio + age + height
         + weight + bp.1s + bp.1d + waist*hip + gender*bmi,
         data = dat)
Error in eval(predvars, data, env): object 'glyhb.cat' not found
> sumfit_01 = summary(fit_01)
> sumfit 01
glm(formula = glyhb.cat ~ chol + stab.glu + hdl + ratio + age +
 height + weight + bp.1s + bp.1d + waist * hip + gender *
 bmi, data = dat)
Deviance Residuals:
       1Q Median
                       3Q Max
-1.23397 -0.11029 -0.03622 0.03830 1.11588
Coefficients:
       Estimate Std. Error t value Pr(>|t|)
(Intercept) -1.261e-02 1.367e+00 -0.009 0.993
chol
         3.797e-04 5.631e-04 0.674 0.501
         4.301e-03 2.635e-04 16.323 <2e-16 ***
```

```
-6.457e-06 1.758e-03 -0.004 0.997
hdl
          1.183e-02 1.960e-02 0.603 0.547
ratio
          1.382e-03 1.016e-03 1.360 0.175
age
          -3.208e-04 2.050e-02 -0.016 0.988
height
           -7.739e-06 3.775e-03 -0.002 0.998
weight
bp.1s
           7.611e-04 8.254e-04 0.922 0.357
          -1.967e-04 1.264e-03 -0.156 0.876
bp.1d
          -9.012e-03 1.540e-02 -0.585 0.559
waist
         -1.991e-02 1.493e-02 -1.334 0.183
gendermale 9.711e-02 1.767e-01 0.549 0.583
          2.904e-03 2.144e-02 0.135 0.892
bmi
waist:hip 3.462e-04 3.361e-04 1.030 0.304
gendermale:bmi -5.260e-03 6.227e-03 -0.845 0.399
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 '' 1
(Dispersion parameter for gaussian family taken to be 0.06532482)
  Null deviance: 51.067 on 402 degrees of freedom
Residual deviance: 25.281 on 387 degrees of freedom
AIC: 61.8
Number of Fisher Scoring iterations: 2
   #remove bp.1d
   fit_02 = glm(glyhb.cat ~ chol + stab.glu + rcs(stab.glu, 3) + hdl + ratio + age + rcs(age, 3) + height
           + weight + frame + bp.1s + rcs(bp.1s, 3) + waist*hip + gender*bmi + w.h.ratio,
           data = dat, family = binomial())
Error in eval(predvars, data, env): object 'glyhb.cat' not found
> sumfit 02 = summary(fit 02)
Error in h(simpleError(msg, call)) :
error in evaluating the argument 'object' in selecting a method for function 'summary': object 'fit_02' not found
> sumfit 02
Error: object 'sumfit_02' not found
   #remove waist*hip
   fit_02 = glm(glyhb.cat ~ chol + stab.glu + rcs(stab.glu, 3) + hdl + ratio + age + rcs(age, 3) + height
           + weight + frame + bp.1s + rcs(bp.1s, 3) + gender*bmi + w.h.ratio,
           data = dat, family = binomial())
Error in eval(predvars, data, env): object 'glyhb.cat' not found
> sumfit 02 = summary(fit 02)
Error in h(simpleError(msg, call)) :
error in evaluating the argument 'object' in selecting a method for function 'summary': object 'fit_02' not found
> sumfit 02
Error: object 'sumfit_02' not found
   #remove rcs(bp.1s, 3)
   fit 03 = glm(glyhb.cat ~ chol + stab.glu + rcs(stab.glu, 3) + hdl + ratio + age + rcs(age, 3) + height
           + weight + frame + bp.1s + gender*bmi + w.h.ratio,
           data = dat, family = binomial())
Error in eval(predvars, data, env): object 'glyhb.cat' not found
> sumfit 03 = summary(fit 03)
Error in h(simpleError(msg, call)) :
error in evaluating the argument 'object' in selecting a method for function 'summary': object 'fit 03' not found
> sumfit 03
Error: object 'sumfit 03' not found
    #remove frame
   fit_04 = glm(glyhb.cat ~ chol + stab.glu + rcs(stab.glu, 3) + hdl + ratio + age + rcs(age, 3) + height
           + weight + bp.1s + gender*bmi + w.h.ratio,
           data = dat, family = binomial())
Error in eval(predvars, data, env): object 'glyhb.cat' not found
> sumfit_04 = summary(fit_04)
Error in h(simpleError(msg, call)):
 error in evaluating the argument 'object' in selecting a method for function 'summary': object 'fit_04' not found
```

```
> sumfit 04
Error: object 'sumfit 04' not found
   #remove weight
   fit_05 = glm(glyhb.cat ~ chol + stab.glu + rcs(stab.glu, 3) + hdl + ratio + age + rcs(age, 3) + height
           + bp.1s + gender*bmi + w.h.ratio,
           data = dat, family = binomial())
Error in eval(predvars, data, env): object 'glyhb.cat' not found
> sumfit 05 = summary(fit 05)
Error in h(simpleError(msg, call)):
error in evaluating the argument 'object' in selecting a method for function 'summary': object 'fit_05' not found
> sumfit 05
Error: object 'sumfit_05' not found
   #remove ratio
   fit_06 = glm(glyhb.cat ~ chol + stab.glu + rcs(stab.glu, 3) + hdl + age + rcs(age, 3) + height
          + bp.1s + gender*bmi + w.h.ratio,
          data = dat, family = binomial())
Error in eval(predvars, data, env): object 'glyhb.cat' not found
   sumfit_06 = summary(fit_06)
Error in h(simpleError(msg, call)) :
error in evaluating the argument 'object' in selecting a method for function 'summary': object 'fit_06' not found
> sumfit_06
Error: object 'sumfit_06' not found
   #remove rcs(age, 3)
   fit_07 = glm(glyhb.cat ~ chol + stab.glu + rcs(stab.glu, 3) + hdl + age + height
          + bp.1s + gender*bmi + w.h.ratio,
          data = dat, family = binomial())
Error in eval(predvars, data, env): object 'glyhb.cat' not found
> sumfit 07 = summary(fit 07)
Error in h(simpleError(msg, call)) :
 error in evaluating the argument 'object' in selecting a method for function 'summary': object 'fit_07' not found
> sumfit 07
Error: object 'sumfit 07' not found
   #looks good, try removing height (other research says height is important)
   #remove height
   fit_08 = glm(glyhb.cat ~ chol + stab.glu + rcs(stab.glu, 3) + hdl + age
          + bp.1s + gender*bmi + w.h.ratio,
          data = dat, family = binomial())
Error in eval(predvars, data, env): object 'glyhb.cat' not found
   sumfit_08 = summary(fit_08)
   sumfit 08
glm(formula = glyhb.cat ~ chol + stab.glu + rcs(stab.glu, 3) +
 hdl + age + bp.1s + gender * bmi + w.h.ratio, family = binomial(),
  data = dat)
Deviance Residuals:
        1Q Median 3Q Max
-2.8046 -0.2787 -0.1431 -0.0596 3.9586
Coefficients: (1 not defined because of singularities)
              Estimate Std. Error z value Pr(>|z|)
(Intercept)
                -21.503234 4.638557 -4.636 3.56e-06 ***
                0.007525 0.005134 1.466 0.142771
                 stab.glu
                         NA
                               NA NA NA
rcs(stab.glu, 3)stab.glu
hdl
               0.025209 0.015811 1.594 0.110842
age
                0.012514 0.009540 1.312 0.189598
bp.1s
gendermale
                    2.242253 2.159681 1.038 0.299161
```

```
0.043515 0.035698 1.219 0.222863
hmi
                 3.431615 3.139357 1.093 0.274352
w.h.ratio
gendermale:bmi
                    -0.098068 0.074321 -1.320 0.186996
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 '' 1
(Dispersion parameter for binomial family taken to be 1)
  Null deviance: 339.14 on 402 degrees of freedom
Residual deviance: 155.28 on 392 degrees of freedom
AIC: 177.28
Number of Fisher Scoring iterations: 7
  confint(fit_08)
Waiting for profiling to be done...
                2.5 %
                       97.5 %
                -31.285765012 -12.96193827
(Intercept)
               -0.001990458 0.01814252
chol
stab.glu
                0.056363399 0.17618307
rcs(stab.glu, 3)stab.glu
                         NA
rcs(stab.glu, 3)stab.glu' -0.360606016 -0.05666169
              -0.043772938  0.01059884
hdl
              -0.005540259 0.05684134
age
bp.1s
               -0.006800703  0.03093685
gendermale
                  -2.047247704 6.48225930
               -0.027951454 0.11366166
bmi
w.h.ratio
                -2.728663414 9.64719862
gendermale:bmi
                    -0.245265050 0.04803552
   #likelihood ratio test to compare GLM full and reduced Mult Log Regression
   res_dev_log_full = 147.84
   res_dev_log_red = 155.28
   df log full = 369
   df_log_red = 392
   AIC_log_full = 191.84
   AIC_log_red = 177.28
   pchisq(res_dev_log_red - res_dev_log_full, df_log_red - df_log_full,
      lower.tail = F) #p-value is 0.999 - therefore can use reduced
[1] 0.9990926
   #likelihood ratio test for GLMM random location and Mult Log. Regression
   res dev glmm loc = 155.3
   res_dev_logistic = 155.28
   df_glmm_loc = 390
  df logistic = 392
   AIC glmm loc = 181.3
   AIC_logistic = 177.28
   pchisq(res_dev_glmm_loc - res_dev_logistic, df_glmm_loc - df_logistic,
       lower.tail = F) #p-value is 0.990 - therefore can use either
[1] NaN
Warning message:
In pchisq(res_dev_glmm_loc - res_dev_logistic, df_glmm_loc - df_logistic, :
NaNs produced
> ######## Assessment of Reduced Multiple Logistic Regression Model #####
#fit a logistic regression model using terms from glm (which gave me p values)
   require(rms)
   dd = datadist(dat)
   options(datadist = 'dd')
```

```
Irm.reduced = Irm(glyhb.cat ~ chol + stab.glu + hdl + age
             + bp.1s + gender*bmi, data = dat)
Error in eval(predvars, data, callenv): object 'glyhb.cat' not found
   #Calibration using bootstraps and Calibration Plot - DOES NOT WORK (can't use glm)
   cal_log = calibrate(lrm.reduced, B=100) #does not work with glm or lrm models
Error in (function (classes, fdef, mtable):
unable to find an inherited method for function 'calibrate' for signature "Irm"
   boot_strap = boot(dat,
             predict(fit_08),
             R = 1000,
             cor.type = 's')
Error in statistic(data, original, ...) :
could not find function "statistic"
> boots = bootstrap(dat, 100)
   probs = predict(fit_08, newdata = dat[boots[1,],])
Error in xj[i]: invalid subscript type 'list'
   predict_matrix = data.matrix(dat[,])
   #discrimination - ROC Curve
   library(pROC)
   pred = predict(fit_08, type = c("response"))
   roccurve = roc(dat$glyhb.cat ~ pred)
Error in model.frame.default(formula = dat$glyhb.cat ~ pred, na.action = "na.pass"):
invalid type (NULL) for variable 'dat$glyhb.cat'
   plot(roccurve, main = "ROC Curve")
   auc(roccurve) #Area Under Curve = 0.9419 - good discrimination
Area under the curve: 0.9419
   #validation
>
   library(purrr) #for map()
   validate(Irm.reduced, method = "boot", B= 1000, data = dat, x = TRUE, y = TRUE)
Error in validate.lrm(lrm.reduced, method = "boot", B = 1000, data = dat, :
fit did not use x=TRUE,y=TRUE
   require(Ime4)
   require(languageR)
   somers.mer(fit_08)
Error in somers.mer(fit_08): could not find function "somers.mer"
   x = bootstrap(dat, 100)
   map(x, lrm.reduced)
Error: Can't convert a `lrm/rms/glm` object to function
Run `rlang::last_error()` to see where the error occurred.
   somers2()
Error in somers2(): argument "y" is missing, with no default
>
> ########### Assess Model GLM ###########
#Residuals
   res = residuals(fit_08, "pearson")
   hist(res)
   plot(res) #resid vs index
   min(res)
[1] -7.075276
   max(res)
[1] 50.27119
> which(res>25) #observation 334 has extremely large residual comparatively
334
334
   #try removing observation 334 - Does not improve fit
```

```
fit_09 = glm(glyhb.cat ~ chol + stab.glu + rcs(stab.glu, 3) + hdl + age
          + bp.1s + gender*bmi + w.h.ratio,
          data = dat[-334,], family = binomial())
Error in eval(predvars, data, env): object 'glyhb.cat' not found
   sumfit_09 = summary(fit_09)
   sumfit_09
Call:
glm(formula = glyhb.cat ~ chol + stab.glu + rcs(stab.glu, 3) +
 hdl + age + bp.1s + gender * bmi + w.h.ratio, family = binomial(),
  data = dat[-334, ])
Deviance Residuals:
  Min
       1Q Median 3Q Max
-2.5075 -0.2291 -0.0902 -0.0305 3.5245
Coefficients: (1 not defined because of singularities)
              Estimate Std. Error z value Pr(>|z|)
                -26.657327 5.515142 -4.833 1.34e-06 ***
(Intercept)
               0.007229 0.005375 1.345 0.178605
chol
stab.glu
                rcs(stab.glu, 3)stab.glu
                         NA
                              NA NA NA
rcs(stab.glu, 3)stab.glu' -0.306901 0.090449 -3.393 0.000691 ***
hdl
              \hbox{-0.021562} \quad 0.015111 \ \hbox{-1.427} \ 0.153600
               0.032681 0.016989 1.924 0.054393 .
age
bp.1s
                0.013644 0.010363 1.317 0.187973
                   1.580012 2.285483 0.691 0.489361
gendermale
               0.043526 0.036946 1.178 0.238761
bmi
                 4.159627 3.345645 1.243 0.213759
w.h.ratio
gendermale:bmi
                     -0.084494 0.078259 -1.080 0.280293
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 '' 1
(Dispersion parameter for binomial family taken to be 1)
  Null deviance: 335.31 on 401 degrees of freedom
Residual deviance: 137.40 on 391 degrees of freedom
AIC: 159.4
Number of Fisher Scoring iterations: 7
   plot(fit 09)
   #Overdispersion - no consensus on how to calc, cite source bookmarked
>
   r df = df.residual(fit 08)
   r_pearson = residuals(fit_08, "pearson")
   test_stat_over = sum(r_pearson^2)
   pearson ratio = test stat over/r df #indicates possibility of underdispersion. usually
   p = pchisq(test stat over, df = r df, lower.tail = F)
   p #p=0 reject null, dispersion is significantly different from zero
[1] 0
> ########## Fit Remaining Imputed Data Sets ###########
> #All models were ran on first imputed data set.
> #Show that imputed data sets are not significantly different due to small
> #percentage of missing values.
   #Final Fit for remaining imputed data sets
   #assume same final features as calculated from 1st imputed data set
   dat2 = complete(imp2,2)
   dat3 = complete(imp2,3)
   dat4 = complete(imp2,4)
```

```
dat5 = complete(imp2,5)
> #Add new variables to data sets
   dat2$stab.glu.2 = ((dat2$stab.glu - median(dat2$stab.glu))/sd(dat2$stab.glu))^2
   dat2$age.2 = ((dat2$age - median(dat2$age))/sd(dat2$age))^2
   dat2$bp.1s.2 = ((dat2$bp.1s - median(dat2$bp.1s))/sd(dat2$bp.1s))^2
   for (i in 1:length(dat2$glyhb)){ # Change glyhb to categorical: glyhb>7 = 1, glyhb<7 = 0
    if (dat2\$glyhb[i] >= 7){
     dat2$glyhb.cat[i] = 1
     } else if (dat$glyhb[i] < 7){
      dat2$glyhb.cat[i] = 0
   }
   dat2$w.h.ratio = (dat2$waist)/dat2$hip #waist-hip ratio
   dat2$bmi = dat2$weight/((dat2$height)^2)*703 #Add new variable BMI
   dat2$frame = factor(dat2$frame, levels = c("small", "medium", "large")) # Change "frame" to a factor small, medium, large
   dat3$stab.glu.2 = ((dat3$stab.glu - median(dat3$stab.glu))/sd(dat3$stab.glu))^2
   dat3$age.2 = ((dat3$age - median(dat3$age))/sd(dat3$age))^2
   dat3$bp.1s.2 = ((dat3$bp.1s - median(dat3$bp.1s))/sd(dat3$bp.1s))^2
   for (i in 1:length(dat3$glyhb)){ # Change glyhb to categorical: glyhb>7 = 1 , glyhb<7 = 0
    if (dat3\$glyhb[i] >= 7){
     dat3$glyhb.cat[i] = 1
     } else if (dat$glyhb[i] < 7){
      dat3$glyhb.cat[i] = 0
    }
   }
   dat3$w.h.ratio = (dat3$waist)/dat3$hip #waist-hip ratio
   dat3$bmi = dat3$weight/((dat3$height)^2)*703 #Add new variable BMI
    dat3$frame = factor(dat3$frame, levels = c("small", "medium", "large")) # Change "frame" to a factor small, medium, large
   dat4$stab.glu.2 = ((dat4$stab.glu - median(dat4$stab.glu))/sd(dat4$stab.glu))^2
   dat4$age.2 = ((dat4$age - median(dat4$age))/sd(dat4$age))^2
   dat4\$bp.1s.2 = ((dat4\$bp.1s - median(dat4\$bp.1s))/sd(dat4\$bp.1s))^2
   for (i in 1:length(dat4\$glyhb)){ # Change glyhb to categorical: glyhb>7 = 1, glyhb<7 = 0
    if (dat4\$glyhb[i] >= 7){
     dat4$glyhb.cat[i] = 1
     } else if (dat$glyhb[i] < 7){
     dat4$glyhb.cat[i] = 0
    }
   dat4$w.h.ratio = (dat4$waist)/dat4$hip #waist-hip ratio
    dat4$bmi = dat4$weight/((dat4$height)^2)*703 #Add new variable BMI
   dat4$frame = factor(dat4$frame, levels = c("small", "medium", "large")) # Change "frame" to a factor small, medium, large
   dat5$stab.glu.2 = ((dat5$stab.glu - median(dat5$stab.glu))/sd(dat5$stab.glu))^2
   dat5$age.2 = ((dat5$age - median(dat5$age))/sd(dat5$age))^2
    dat5$bp.1s.2 = ((dat5$bp.1s - median(dat5$bp.1s))/sd(dat5$bp.1s))^2
   for (i in 1:length(dat5$glyhb)){  # Change glyhb to categorical: glyhb>7 = 1 , glyhb<7 = 0
    if (dat5\$glyhb[i] >= 7){
     dat5$glyhb.cat[i] = 1
     } else if (dat$glyhb[i] < 7){
      dat5$glyhb.cat[i] = 0
    }
   dat5$w.h.ratio = (dat5$waist)/dat5$hip #waist-hip ratio
   dat5$bmi = dat5$weight/((dat5$height)^2)*703 #Add new variable BMI
   dat5$frame = factor(dat5$frame, levels = c("small", "medium", "large")) # Change "frame" to a factor small, medium, large
   fitimp2.2 = glm(glyhb.cat ~ chol + stab.glu + rcs(stab.glu, 3) + hdl + age
             + bp.1s + gender*bmi + w.h.ratio,
```

```
data = dat2, family = binomial())
   sumfitimp2.2 = summary(fitimp2.2);
   sumfitimp2.2
Call:
glm(formula = glyhb.cat ~ chol + stab.glu + rcs(stab.glu, 3) +
 hdl + age + bp.1s + gender * bmi + w.h.ratio, family = binomial(),
 data = dat2)
Deviance Residuals:
 Min 1Q Median
                      3Q Max
-2.7980 -0.2793 -0.1425 -0.0595 3.9583
Coefficients: (1 not defined because of singularities)
             Estimate Std. Error z value Pr(>|z|)
(Intercept)
                -21.562380 4.655701 -4.631 3.63e-06 ***
               0.007597 \ \ 0.005147 \ \ 1.476 \ 0.139973
chol
stab.glu
               0.112539 0.030406 3.701 0.000215 ***
                        NA
                              NA NA
rcs(stab.glu, 3)stab.glu
                                          NA
hdl
              -0.015976 0.013841 -1.154 0.248414
               0.024863 0.015823 1.571 0.116119
age
bp.1s
               0.012679 \ 0.009528 \ 1.331 \ 0.183303
gendermale
                   2.269839 2.130793 1.065 0.286760
bmi
               0.042398 0.035890 1.181 0.237474
w.h.ratio
                3.484139 3.145612 1.108 0.268026
gendermale:bmi
                    Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 '' 1
(Dispersion parameter for binomial family taken to be 1)
 Null deviance: 339.14 on 402 degrees of freedom
Residual deviance: 155.24 on 392 degrees of freedom
AIC: 177.24
Number of Fisher Scoring iterations: 7
   plot(fitimp2.2)
   fitimp2.3 = glm(glyhb.cat ~ chol + stab.glu + rcs(stab.glu, 3) + hdl + age
           + bp.1s + gender*bmi + w.h.ratio,
           data = dat3, family = binomial())
   sumfitimp2.3 = summary(fitimp2.3);
   sumfitimp2.3
glm(formula = glyhb.cat ~ chol + stab.glu + rcs(stab.glu, 3) +
 hdl + age + bp.1s + gender * bmi + w.h.ratio, family = binomial(),
 data = dat3)
Deviance Residuals:
  Min
       1Q Median 3Q Max
-2.7999 -0.2785 -0.1429 -0.0596 3.9582
Coefficients: (1 not defined because of singularities)
             Estimate Std. Error z value Pr(>|z|)
               -21.561625 4.647818 -4.639 3.5e-06 ***
(Intercept)
               0.007547 \ 0.005141 \ 1.468 \ 0.142111
               0.112500 0.030382 3.703 0.000213 ***
stab.glu
                             NA NA NA
rcs(stab.glu, 3)stab.glu
                       NA
hdl
              -0.015953 0.013840 -1.153 0.249050
              0.024870 0.015820 1.572 0.115922
age
               0.012780 0.009495 1.346 0.178314
bp.1s
gendermale
                   2.263816 2.144153 1.056 0.291055
```

```
0.042798 0.035818 1.195 0.232145
hmi
                 3.465085 3.141939 1.103 0.270093
w.h.ratio
gendermale:bmi
                    -0.099010 0.073771 -1.342 0.179553
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 '' 1
(Dispersion parameter for binomial family taken to be 1)
 Null deviance: 339.14 on 402 degrees of freedom
Residual deviance: 155.20 on 392 degrees of freedom
AIC: 177.2
Number of Fisher Scoring iterations: 7
   plot(fitimp2.3)
   fitimp2.4 = glm(glyhb.cat ~ chol + stab.glu + rcs(stab.glu, 3) + hdl + age
           + bp.1s + gender*bmi + w.h.ratio,
           data = dat4, family = binomial())
   sumfitimp2.4 = summary(fitimp2.4);
   sumfitimp2.4
glm(formula = glyhb.cat ~ chol + stab.glu + rcs(stab.glu, 3) +
 hdl + age + bp.1s + gender * bmi + w.h.ratio, family = binomial(),
  data = dat4)
Deviance Residuals:
      1Q Median 3Q Max
-2.8041 -0.2796 -0.1430 -0.0597 3.9606
Coefficients: (1 not defined because of singularities)
             Estimate Std. Error z value Pr(>|z|)
(Intercept)
                -21.487366 4.640000 -4.631 3.64e-06 ***
               0.007517 0.005132 1.465 0.142984
chol
stab.glu
                rcs(stab.glu, 3)stab.glu
                        NA
                             NA NA NA
hdl
              -0.015892 0.013834 -1.149 0.250652
               0.025093 0.015806 1.588 0.112379
bp.1s
               0.012588 0.009535 1.320 0.186764
                   2.212110 2.161305 1.024 0.306068
gendermale
bmi
               0.042472 0.035890 1.183 0.236650
                 3.420605 3.137245 1.090 0.275572
w.h.ratio
gendermale:bmi
                    Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 '' 1
(Dispersion parameter for binomial family taken to be 1)
 Null deviance: 339.14 on 402 degrees of freedom
Residual deviance: 155.35 on 392 degrees of freedom
AIC: 177.35
Number of Fisher Scoring iterations: 7
   plot(fitimp2.4)
   fitimp2.5 = glm(glyhb.cat ~ chol + stab.glu + rcs(stab.glu, 3) + hdl + age
           + bp.1s + gender*bmi + w.h.ratio,
           data = dat5, family = binomial())
   sumfitimp2.5 = summary(fitimp2.5);
   sumfitimp2.5
```

Call:

```
glm(formula = glyhb.cat ~ chol + stab.glu + rcs(stab.glu, 3) +
 hdl + age + bp.1s + gender * bmi + w.h.ratio, family = binomial(),
 data = dat5)
Deviance Residuals:
 Min
        1Q Median
                       3Q Max
-2.8881 -0.3016 -0.1605 -0.0748 3.8649
Coefficients: (1 not defined because of singularities)
              Estimate Std. Error z value Pr(>|z|)
                 -19.740987 4.370964 -4.516 6.29e-06 ***
(Intercept)
                0.005693 0.004816 1.182 0.237119
chol
                 0.100647  0.028404  3.543  0.000395 ***
stab.glu
rcs(stab.glu, 3)stab.glu
                         NA
                               NA NA NA
-0.010000 \quad 0.013349 \quad -0.749 \quad 0.453772
                0.031693 0.015410 2.057 0.039719 *
age
bp.1s
                0.007145  0.009452  0.756  0.449665
                    2.099593 2.106941 0.997 0.319001
gendermale
bmi
                0.054356  0.034580  1.572  0.115975
w.h.ratio
                 3.007525 3.078233 0.977 0.328555
gendermale:bmi
                     -0.091468 0.072412 -1.263 0.206529
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for binomial family taken to be 1)
 Null deviance: 342.61 on 402 degrees of freedom
Residual deviance: 162.86 on 392 degrees of freedom
AIC: 184.86
Number of Fisher Scoring iterations: 7
   plot(fitimp2.5)
   #Pool Paramters for 5 datasets
   paramdat1 = fit_08$coefficients
   paramdat2 = fitimp2.2$coefficients
   paramdat3 = fitimp2.3$coefficients
   paramdat4 = fitimp2.4$coefficients
   paramdat5 = fitimp2.5$coefficients
   paramdat1
       (Intercept)
                            chol
                                         stab.glu rcs(stab.glu, 3)stab.glu
      -21.503234392
                           0.007524847
                                               0.112141876
                                                                       NA
rcs(stab.glu, 3)stab.glu'
                                hdl
                                               age
                                                             bp.1s
                                              0.025209309
                                                                  0.012514372
      -0.202352186
                          -0.015832158
       gendermale
                              hmi
                                          w.h.ratio
                                                         gendermale:bmi
       2.242253263
                           0.043514522
                                              3.431615007
                                                                  -0.098067885
   paramdat2
       (Intercept)
                            chol
                                         stab.glu rcs(stab.glu, 3)stab.glu
      -21.562380046
                           0.007596636
                                               0.112539367
rcs(stab.glu, 3)stab.glu'
                                hdl
                                               age
                                                             bp.1s
                                              0.024862979
                                                                  0.012678948
      -0.203365804
                          -0.015975674
       gendermale
                              bmi
                                          w.h.ratio
                                                         gendermale:bmi
       2.269839073
                           0.042397759
                                              3.484138667
                                                                 -0.099523453
   paramdat3
       (Intercept)
                                         stab.glu rcs(stab.glu, 3)stab.glu
                            chol
      -21.561624893
                           0.007547253
                                               0.112500436
rcs(stab.glu, 3)stab.glu'
                                hdl
                                               age
                                                             bp.1s
      -0.203275914
                          -0.015953009
                                              0.024870192
                                                                  0.012780495
       gendermale
                              bmi
                                          w.h.ratio
                                                         gendermale:bmi
                          0.042797623
       2.263816324
                                              3.465085189
                                                                  -0.099010288
   paramdat4
       (Intercept)
                            chol
                                         stab.glu rcs(stab.glu, 3)stab.glu
```

-21.487365803

0.007517253

0.112437770

```
rcs(stab.glu, 3)stab.glu'
                               hdl
                                              age
                                                           bp.1s
      -0.203051336
                         -0.015891909
                                             0.025093377
                                                                0.012587716
       gendermale
                             bmi
                                         w.h.ratio
                                                       gendermale:bmi
       2.212110402
                         0.042471793
                                             3.420605167
                                                               -0.097177911
   paramdat5
      (Intercept)
                           chol
                                        stab.glu rcs(stab.glu, 3)stab.glu
                          0.005693271
                                             0.100646727
      -19.740987442
                                                                     NA
rcs(stab.glu, 3)stab.glu'
                               hdl
                                             age
                                                           bp.1s
                                             0.031692786
                                                                0.007145219
      -0.175901856
                          -0.010000192
       gendermale
                                         w.h.ratio
                                                       gendermale:bmi
                             bmi
       2.099593258
                         0.054355909
                                             3.007524505
                                                               -0.091468255
```

> all.equal(paramdat5, paramdat4, paramdat3, paramdat2, paramdat1) #returns TRUE, all equal

Error in all.equal.numeric(paramdat5, paramdat4, paramdat3, paramdat2, :

all(scale > 0) is not TRUE

In addition: Warning messages:

1: In if (countEQ) {:

the condition has length > 1 and only the first element will be used

2: In if (!countEQ) N <- length(target):

the condition has length > 1 and only the first element will be used