

Initial Code CIND 820

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```
#loading in packages, and Libraries
```

```
#install.packages("tidyverse")  
#install.packages("tseries")  
#install.packages("forecast")  
#install.packages("fpp2")  
#install.packages("tinytex")  
#tinytex::install_tinytex()
```

```
library(tidyverse)
```

```
## Warning: package 'tidyverse' was built under R version 4.2.2
```

```
## Warning in Sys.timezone(): unable to identify current timezone 'C':  
## please set environment variable 'TZ'
```

```
## -- Attaching packages ----- tidyverse 1.3.2 --  
## v ggplot2 3.4.0      v purrr   0.3.5  
## v tibble  3.1.8      v dplyr  1.0.10  
## v tidyr   1.2.1      v stringr 1.4.1  
## v readr   2.1.3      v forcats 0.5.2
```

```
## Warning: package 'ggplot2' was built under R version 4.2.2
```

```
## Warning: package 'tibble' was built under R version 4.2.2
```

```
## Warning: package 'tidyr' was built under R version 4.2.2
```

```
## Warning: package 'readr' was built under R version 4.2.2
```

```
## Warning: package 'purrr' was built under R version 4.2.2
```

```
## Warning: package 'dplyr' was built under R version 4.2.2
```

```
## Warning: package 'stringr' was built under R version 4.2.2
```

```
## Warning: package 'forcats' was built under R version 4.2.2
```

```
## -- Conflicts ----- tidyverse_conflicts() --  
## x dplyr::filter() masks stats::filter()  
## x dplyr::lag()     masks stats::lag()
```

```
library(forecast)
```

```
## Warning: package 'forecast' was built under R version 4.2.2
```

```
## Registered S3 method overwritten by 'quantmod':
```

```
##   method      from
```

```
## as.zoo.data.frame zoo
```

```
library(tseries)
```

```
## Warning: package 'tseries' was built under R version 4.2.2
```

```
library(lubridate)
```

```
## Warning: package 'lubridate' was built under R version 4.2.2
```

```
## Loading required package: timechange
```

```
## Warning: package 'timechange' was built under R version 4.2.2
```

```
##
```

```
## Attaching package: 'lubridate'
```

```
##
```

```
## The following objects are masked from 'package:base':
```

```
##
```

```
##   date, intersect, setdiff, union
```

```
library(dplyr)
```

```
library(ggplot2)
```

```
#Importing Dataset
```

```
salesdata <- read.csv(file.choose())
```

```
head(salesdata)
```

```
##   ORDERNUMBER QUANTITYORDERED PRICEEACH ORDERLINENUMBER  SALES    ORDERDATE
## 1      10107             30      95.70           2 2871.00 2/24/2003 0:00
## 2      10121             34      81.35           5 2765.90 5/7/2003 0:00
## 3      10134             41      94.74           2 3884.34 7/1/2003 0:00
## 4      10145             45      83.26           6 3746.70 8/25/2003 0:00
## 5      10159             49     100.00          14 5205.27 10/10/2003 0:00
## 6      10168             36      96.66           1 3479.76 10/28/2003 0:00
##   STATUS QTR_ID MONTH_ID YEAR_ID PRODUCTLINE MSRP PRODUCTCODE
## 1 Shipped     1         2     2003 Motorcycles  95   S10_1678
## 2 Shipped     2         5     2003 Motorcycles  95   S10_1678
## 3 Shipped     3         7     2003 Motorcycles  95   S10_1678
## 4 Shipped     3         8     2003 Motorcycles  95   S10_1678
## 5 Shipped     4        10     2003 Motorcycles  95   S10_1678
## 6 Shipped     4        10     2003 Motorcycles  95   S10_1678
##                CUSTOMERNAME                PHONE                ADDRESSLINE1
```

```
## 1      Land of Toys Inc.      2125557818      897 Long Airport Avenue
## 2      Reims Collectables      26.47.1555      59 rue de l'Abbaye
## 3      Lyon Souvenirs +33 1 46 62 7555 27 rue du Colonel Pierre Avia
## 4      Toys4GrownUps.com      6265557265      78934 Hillside Dr.
## 5 Corporate Gift Ideas Co.      6505551386      7734 Strong St.
## 6      Technics Stores Inc.      6505556809      9408 Furth Circle
## ADDRESSLINE2      CITY STATE POSTALCODE COUNTRY TERRITORY CONTACTLASTNAME
## 1      NYC      NY      10022      USA      <NA>      Yu
## 2      Reims      51100      France      EMEA      Henriot
## 3      Paris      75508      France      EMEA      Da Cunha
## 4      Pasadena      CA      90003      USA      <NA>      Young
## 5      San Francisco      CA      94217      USA      <NA>      Brown
## 6      Burlingame      CA      94217      USA      <NA>      Hirano
## CONTACTFIRSTNAME DEALSIZE
## 1      Kwai      Small
## 2      Paul      Small
## 3      Daniel      Medium
## 4      Julie      Medium
## 5      Julie      Medium
## 6      Juri      Medium
```

#Unique Countries

```
unique(salesdata$COUNTRY)
```

```
## [1] "USA"      "France"    "Norway"    "Australia" "Finland"
## [6] "Austria"  "UK"        "Spain"     "Sweden"    "Singapore"
## [11] "Canada"   "Japan"     "Italy"     "Denmark"   "Belgium"
## [16] "Philippines" "Germany"   "Switzerland" "Ireland"
```

#Unique Toys

```
unique(salesdata$PRODUCTLINE)
```

```
## [1] "Motorcycles"      "Classic Cars"      "Trucks and Buses" "Vintage Cars"
## [5] "Planes"           "Ships"              "Trains"
```

#creating backup dataset

```
salesdata2 <- salesdata
```

#Cleaning Data

#Removing timestamps from orderdate column

```
salesdata2$ORDERDATE <- gsub(" .*", "", salesdata2$ORDERDATE)
```

#Changing OrderDate Class to "Date"

```
salesdata2$ORDERDATE <- mdy(salesdata2$ORDERDATE)
```

```
class(salesdata2$ORDERDATE)
```

```
## [1] "Date"
```

```
#Re-ordering the Orderdate in ascending order
salesdata2 <- salesdata2[order(salesdata2$ORDERDATE),]
```

```
#Checking to see the total sales per country
salesdata2 %>%
  group_by(COUNTRY)%>%
  summarise(sum_country = sum(SALES, na.rm = TRUE ))
```

```
## # A tibble: 19 x 2
##   COUNTRY      sum_country
##   <chr>         <dbl>
## 1 Australia    630623.
## 2 Austria      202063.
## 3 Belgium      108413.
## 4 Canada       224079.
## 5 Denmark      245637.
## 6 Finland      329582.
## 7 France       1110917.
## 8 Germany       220472.
## 9 Ireland       57756.
## 10 Italy        374674.
## 11 Japan        188168.
## 12 Norway       307464.
## 13 Philippines   94016.
## 14 Singapore    288488.
## 15 Spain        1215687.
## 16 Sweden        210014.
## 17 Switzerland  117714.
## 18 UK           478880.
## 19 USA          3627983.
```

```
#Checking to see the total sales per Toy
```

```
salesdata2 %>%
  group_by(PRODUCTLINE)%>%
  summarise(sum_country = sum(SALES, na.rm = TRUE ))
```

```
## # A tibble: 7 x 2
##   PRODUCTLINE      sum_country
##   <chr>         <dbl>
## 1 Classic Cars    3919616.
## 2 Motorcycles     1166388.
## 3 Planes          975004.
## 4 Ships           714437.
## 5 Trains          226243.
## 6 Trucks and Buses 1127790.
## 7 Vintage Cars    1903151.
```

```
#Forecast 1, Part 1: Forecast test without variables
```

```
#Creating Time Series
```

```
sale <- ts(salesdata2[,5], start = c(2003,1), end = c(2005,5), frequency = 12)
sale
```

```
##           Jan      Feb      Mar      Apr      May      Jun      Jul      Aug      Sep
## 2003 5151.00 3390.00 1903.22 1689.03 3782.00 3773.38 1404.00 2472.96 4808.31
## 2004 3394.98 3920.00 1189.98 2242.89 2011.10 2539.50 4791.82 4228.20 1938.89
## 2005 3403.35 4460.82 5958.50 4615.78 3457.92
##           Oct      Nov      Dec
## 2003 2055.74 5404.62 5398.26
## 2004 3680.28 2873.00 3224.31
## 2005
```

```
#Building Arima Model
```

```
Test_Model <- auto.arima(sale)
```

```
#Print Model Summary
```

```
print(summary(Test_Model))
```

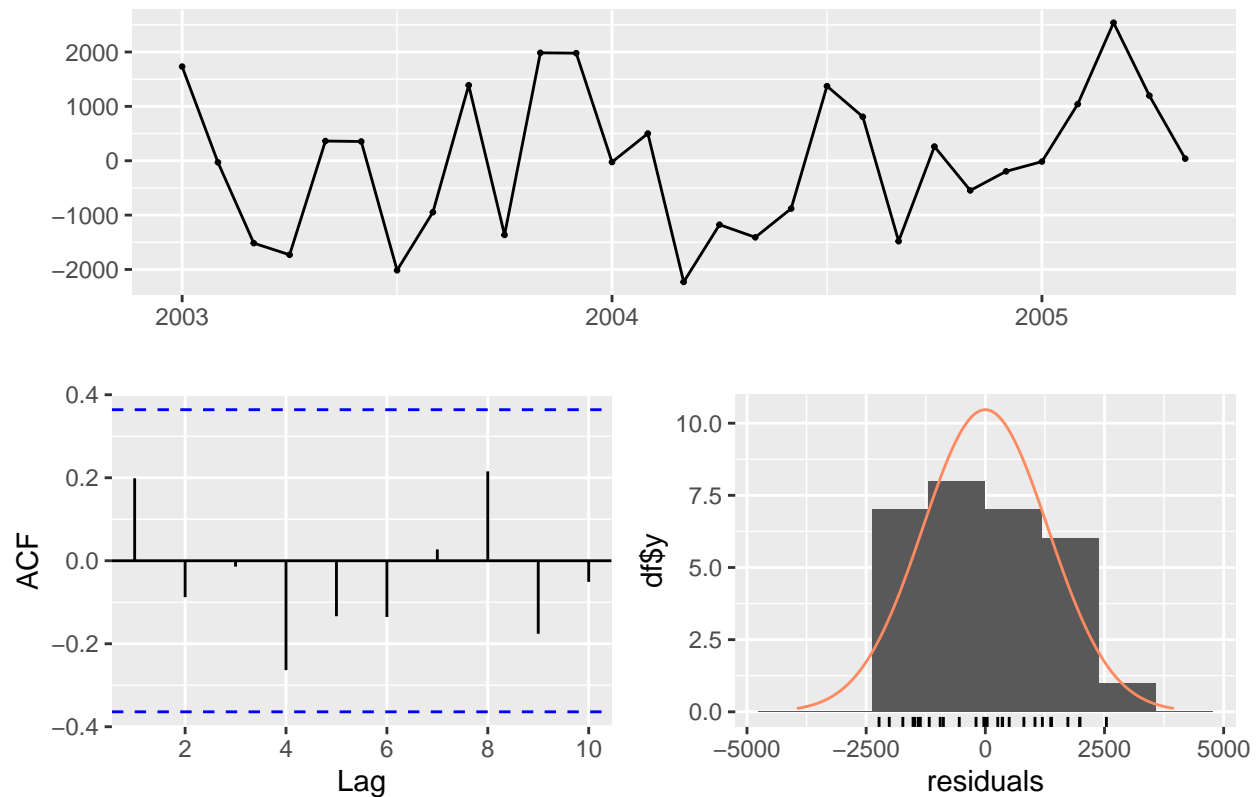
```
## Series: sale
## ARIMA(0,0,0) with non-zero mean
##
## Coefficients:
##           mean
##      3419.4428
## s.e.    240.4282
##
## sigma^2 = 1736229: log likelihood = -248.97
## AIC=501.93   AICc=502.39   BIC=504.66
##
## Training set error measures:
##           ME      RMSE      MAE      MPE      MAPE      MASE
## Training set 2.901512e-13 1294.743 1073.013 -19.40661 41.16299 0.6072734
##           ACF1
## Training set 0.1988037
```

```
#Note: ARIMA(0,0,0) means that the data is white noise
```

```
#Checking residual values of Model
```

```
checkresiduals(Test_Model)
```

Residuals from ARIMA(0,0,0) with non-zero mean

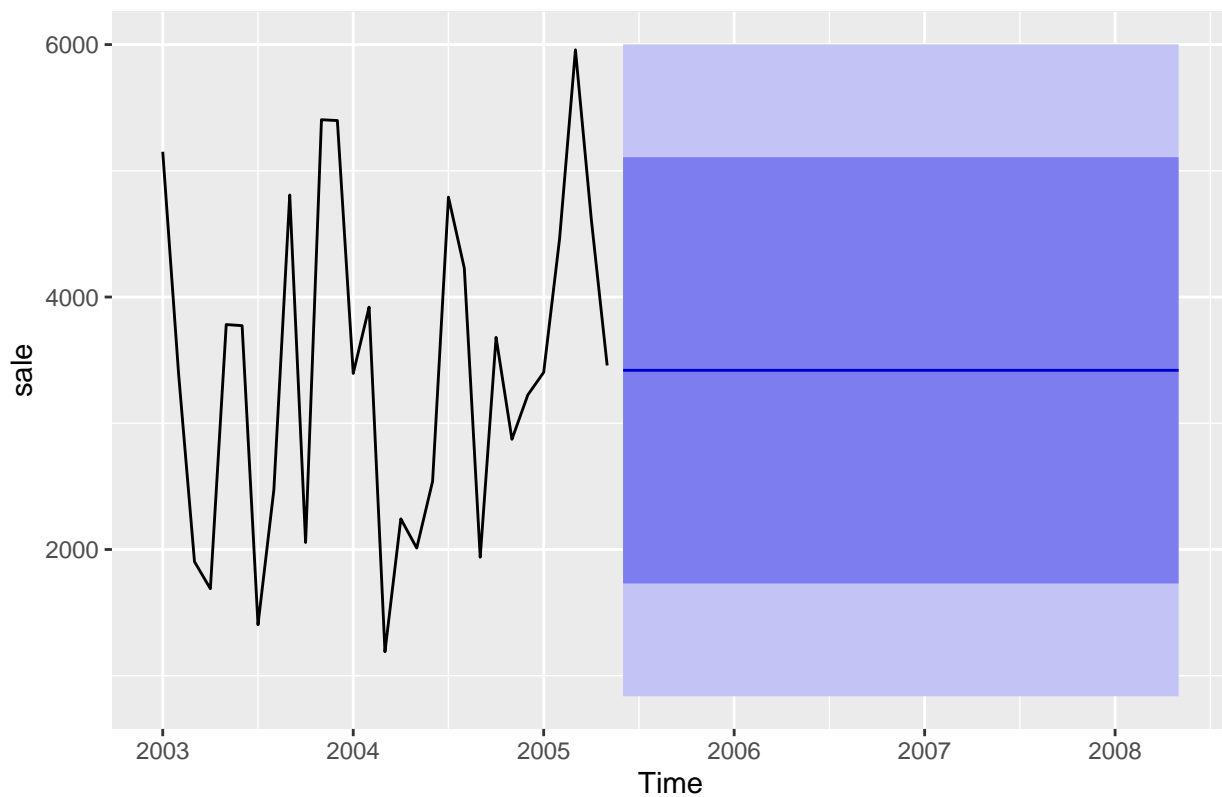


```
##
##  Ljung-Box test
##
## data:  Residuals from ARIMA(0,0,0) with non-zero mean
## Q* = 5.415, df = 6, p-value = 0.4918
##
## Model df: 0.   Total lags used: 6
```

```
#Create Forecast of Model
#Forecast for the next two years
Test_Forecast <- forecast(Test_Model, h=36)
```

```
#Plot Forecast Results
#Showing the last 5 years
autoplot(Test_Forecast, include = 60)
```

Forecasts from ARIMA(0,0,0) with non-zero mean



```
#Print Summary of Forecast Results
print(summary(Test_Forecast))
```

```
##
## Forecast method: ARIMA(0,0,0) with non-zero mean
##
## Model Information:
## Series: sale
## ARIMA(0,0,0) with non-zero mean
##
## Coefficients:
##          mean
##      3419.4428
## s.e.   240.4282
##
## sigma^2 = 1736229:  log likelihood = -248.97
## AIC=501.93   AICc=502.39   BIC=504.66
##
## Error measures:
##              ME      RMSE      MAE      MPE      MAPE      MASE
## Training set  2.901512e-13 1294.743 1073.013 -19.40661 41.16299 0.6072734
##              ACF1
## Training set  0.1988037
##
## Forecasts:
##      Point Forecast    Lo 80    Hi 80    Lo 95    Hi 95
```

```
## Jun 2005      3419.443 1730.793 5108.093 836.8755 6002.01
## Jul 2005      3419.443 1730.793 5108.093 836.8755 6002.01
## Aug 2005      3419.443 1730.793 5108.093 836.8755 6002.01
## Sep 2005      3419.443 1730.793 5108.093 836.8755 6002.01
## Oct 2005      3419.443 1730.793 5108.093 836.8755 6002.01
## Nov 2005      3419.443 1730.793 5108.093 836.8755 6002.01
## Dec 2005      3419.443 1730.793 5108.093 836.8755 6002.01
## Jan 2006      3419.443 1730.793 5108.093 836.8755 6002.01
## Feb 2006      3419.443 1730.793 5108.093 836.8755 6002.01
## Mar 2006      3419.443 1730.793 5108.093 836.8755 6002.01
## Apr 2006      3419.443 1730.793 5108.093 836.8755 6002.01
## May 2006      3419.443 1730.793 5108.093 836.8755 6002.01
## Jun 2006      3419.443 1730.793 5108.093 836.8755 6002.01
## Jul 2006      3419.443 1730.793 5108.093 836.8755 6002.01
## Aug 2006      3419.443 1730.793 5108.093 836.8755 6002.01
## Sep 2006      3419.443 1730.793 5108.093 836.8755 6002.01
## Oct 2006      3419.443 1730.793 5108.093 836.8755 6002.01
## Nov 2006      3419.443 1730.793 5108.093 836.8755 6002.01
## Dec 2006      3419.443 1730.793 5108.093 836.8755 6002.01
## Jan 2007      3419.443 1730.793 5108.093 836.8755 6002.01
## Feb 2007      3419.443 1730.793 5108.093 836.8755 6002.01
## Mar 2007      3419.443 1730.793 5108.093 836.8755 6002.01
## Apr 2007      3419.443 1730.793 5108.093 836.8755 6002.01
## May 2007      3419.443 1730.793 5108.093 836.8755 6002.01
## Jun 2007      3419.443 1730.793 5108.093 836.8755 6002.01
## Jul 2007      3419.443 1730.793 5108.093 836.8755 6002.01
## Aug 2007      3419.443 1730.793 5108.093 836.8755 6002.01
## Sep 2007      3419.443 1730.793 5108.093 836.8755 6002.01
## Oct 2007      3419.443 1730.793 5108.093 836.8755 6002.01
## Nov 2007      3419.443 1730.793 5108.093 836.8755 6002.01
## Dec 2007      3419.443 1730.793 5108.093 836.8755 6002.01
## Jan 2008      3419.443 1730.793 5108.093 836.8755 6002.01
## Feb 2008      3419.443 1730.793 5108.093 836.8755 6002.01
## Mar 2008      3419.443 1730.793 5108.093 836.8755 6002.01
## Apr 2008      3419.443 1730.793 5108.093 836.8755 6002.01
## May 2008      3419.443 1730.793 5108.093 836.8755 6002.01
```

```
#Forecast 1, Part 2: Testing Forecast with manual ARIMA variables
```

```
#Building second test model
```

```
test2_model <-arima(sale,order = c(1,1,2), seasonal = list(order = c(1,1,1)))
```

```
#Print Manual Arima Model Summary
```

```
print(summary(test2_model))
```

```
##
```

```
## Call:
```

```
## arima(x = sale, order = c(1, 1, 2), seasonal = list(order = c(1, 1, 1)))
```

```
##
```

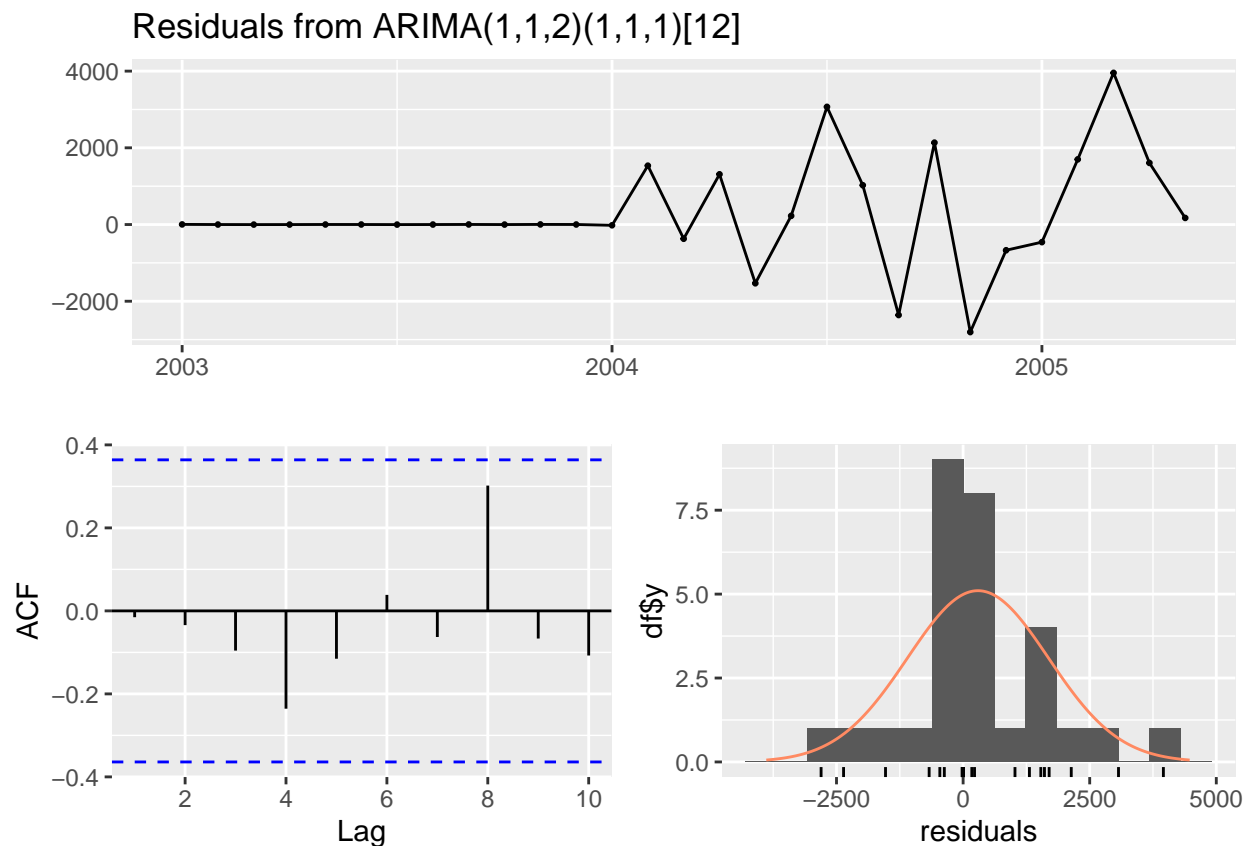
```
## Coefficients:
```

```
## Warning in sqrt(diag(x$var.coef)): NaNs produced
```



```
##          ar1      ma1      ma2      sar1      sma1
##      -0.5240 -0.2090 -0.7909 -0.2296 -0.263
## s.e.   0.4451  0.5139  0.4627      NaN      NaN
##
## sigma^2 estimated as 3554617:  log likelihood = -146.26,  aic = 304.51
##
## Training set error measures:
##              ME      RMSE      MAE      MPE      MAPE      MASE      ACF1
## Training set 293.7786 1400.422 860.8828 1.217806 26.17624 0.638426 -0.01521605
```

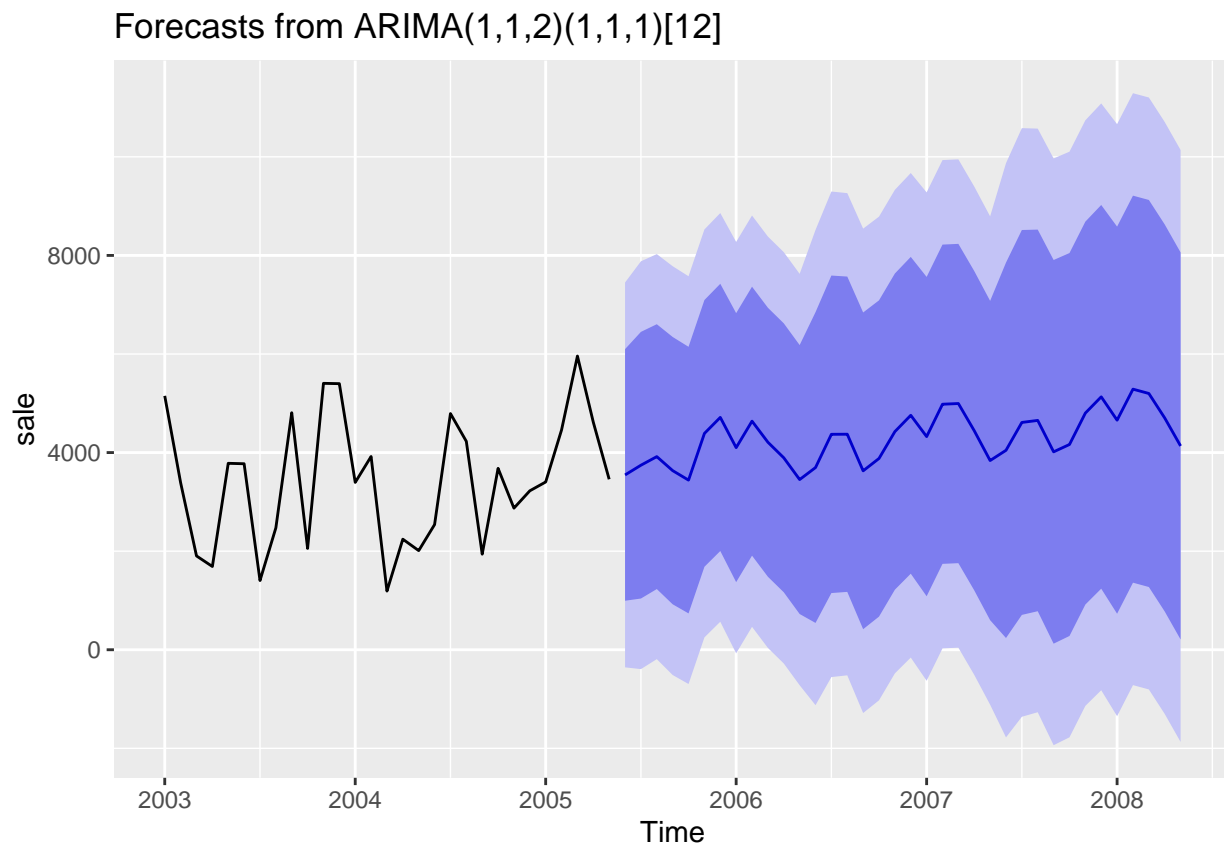
```
#Checking residual values of Manual Arima Model
checkresiduals(test2_model)
```



```
##
## Ljung-Box test
##
## data: Residuals from ARIMA(1,1,2)(1,1,1)[12]
## Q* = 6.9817, df = 3, p-value = 0.07248
##
## Model df: 5. Total lags used: 8
```

```
#Create Forecast for Manual ARIMA Model
#Forecast for the next two years
Test2_Forecast <- forecast(test2_model, h=36)
```

```
#Plot Forecast Results
#Showing the last 5 years
autoplot(Test2_Forecast, include = 60)
```



```
#Print Summary Forecast Results
print(summary(Test2_Forecast))
```

```
##
## Forecast method: ARIMA(1,1,2)(1,1,1)[12]
##
## Model Information:
##
## Call:
## arima(x = sale, order = c(1, 1, 2), seasonal = list(order = c(1, 1, 1)))
##
## Coefficients:

## Warning in sqrt(diag(x$var.coef)): NaNs produced

##          ar1      ma1      ma2      sar1      sma1
##      -0.5240 -0.2090 -0.7909 -0.2296 -0.263
## s.e.   0.4451  0.5139  0.4627      NaN      NaN
##
## sigma^2 estimated as 3554617:  log likelihood = -146.26,  aic = 304.51
```

```
##
## Error measures:
##           ME      RMSE      MAE      MPE      MAPE      MASE      ACF1
## Training set 293.7786 1400.422 860.8828 1.217806 26.17624 0.4872179 -0.01521605
##
## Forecasts:
##           Point Forecast      Lo 80      Hi 80      Lo 95      Hi 95
## Jun 2005      3546.564    994.1562 6098.971   -357.00658  7450.134
## Jul 2005      3744.003   1039.2497 6448.756   -392.56005  7880.565
## Aug 2005      3917.844   1231.4215 6604.266   -190.68463  8026.373
## Sep 2005      3633.973    922.6706 6345.275   -512.60609  7780.552
## Oct 2005      3441.519    737.1683 6145.869   -694.42833  7577.466
## Nov 2005      4388.843   1683.1593 7094.527    250.85673  8526.830
## Dec 2005      4713.941   2003.5513 7424.331    568.75772  8859.124
## Jan 2006      4100.020   1371.2775 6828.762    -73.23145  8273.271
## Feb 2006      4637.255   1909.3836 7365.126    465.33589  8809.174
## Mar 2006      4209.310   1480.9810 6937.639     36.69079  8381.929
## Apr 2006      3893.838   1165.7374 6621.939   -278.43207  8066.109
## May 2006      3452.943    724.7416 6181.145   -719.48123  7625.368
## Jun 2006      3696.173    544.2984 6848.048  -1124.20319  8516.549
## Jul 2006      4370.846   1150.2564 7591.436   -554.62097  9296.314
## Aug 2006      4372.514   1174.2059 7570.822   -518.87617  9263.904
## Sep 2006      3629.726    417.1071 6842.344  -1283.55044  8543.002
## Oct 2006      3880.466    672.6117 7088.320  -1025.52381  8786.456
## Nov 2006      4425.372   1218.3127 7632.432   -479.40223  9330.147
## Dec 2006      4756.272   1542.7633 7969.781   -158.36556  9670.910
## Jan 2007      4324.516   1085.3996 7563.632   -629.28486  9278.316
## Feb 2007      4981.129   1742.5890 8219.670     28.20932  9934.049
## Mar 2007      4995.310   1756.4713 8234.148     41.93390  9948.685
## Apr 2007      4443.981   1205.2886 7682.674   -509.17169  9397.134
## May 2007      3838.491    599.7408 7077.241  -1114.74991  8791.731
## Jun 2007      4046.225    237.9480 7854.503  -1778.03224  9870.483
## Jul 2007      4611.335    707.1005 8515.570  -1359.67661  10582.347
## Aug 2007      4652.530    781.6329 8523.427  -1267.49628  10572.557
## Sep 2007      4015.103    123.5276 7906.678  -1936.54775  9966.753
## Oct 2007      4164.092    279.9070 8048.277  -1776.25644  10104.441
## Nov 2007      4801.388    917.4656 8685.310  -1138.55863  10741.334
## Dec 2007      5130.955   1239.0692 9022.841   -821.17087  11083.081
## Jan 2008      4657.377    730.8464 8583.907  -1347.73317  10662.487
## Feb 2008      5286.583   1360.8770 9212.289   -717.26613  11290.432
## Mar 2008      5199.258   1273.1249 9125.391   -805.24448  11203.761
## Apr 2008      4702.079    776.1564 8628.001  -1302.10132  10706.259
## May 2008      4134.377    208.3678 8060.386  -1869.93587  10138.689
```

```
#Forecast 2: Forecast with Variables
```

```
#Creating Time Series
```

```
sale <- ts(salesdata2[,5], start = c(2003,1), end = c(2005,5), frequency = 12)
sale
```

```
##           Jan      Feb      Mar      Apr      May      Jun      Jul      Aug      Sep
## 2003 5151.00 3390.00 1903.22 1689.03 3782.00 3773.38 1404.00 2472.96 4808.31
## 2004 3394.98 3920.00 1189.98 2242.89 2011.10 2539.50 4791.82 4228.20 1938.89
## 2005 3403.35 4460.82 5958.50 4615.78 3457.92
```

```
##           Oct       Nov       Dec
## 2003 2055.74 5404.62 5398.26
## 2004 3680.28 2873.00 3224.31
## 2005
```

```
#Built Fit Arima Model
```

```
#Taking first difference of the data
```

```
#Getting rid of seasonality by taking first seasonal difference
```

```
AR_Model <- auto.arima(sale, d=1, D=1, stepwise = FALSE, approximation = FALSE, trace = TRUE)
```

```
##
## ARIMA(0,1,0)(0,1,0)[12] : 301.8345
## ARIMA(0,1,1)(0,1,0)[12] : 298.6723
## ARIMA(0,1,2)(0,1,0)[12] : 301.4452
## ARIMA(0,1,3)(0,1,0)[12] : 305.0502
## ARIMA(0,1,4)(0,1,0)[12] : Inf
## ARIMA(0,1,5)(0,1,0)[12] : Inf
## ARIMA(1,1,0)(0,1,0)[12] : 301.691
## ARIMA(1,1,1)(0,1,0)[12] : 301.4556
## ARIMA(1,1,2)(0,1,0)[12] : 304.5768
## ARIMA(1,1,3)(0,1,0)[12] : 308.9399
## ARIMA(1,1,4)(0,1,0)[12] : 313.8526
## ARIMA(2,1,0)(0,1,0)[12] : 302.386
## ARIMA(2,1,1)(0,1,0)[12] : 305.0913
## ARIMA(2,1,2)(0,1,0)[12] : 308.9395
## ARIMA(2,1,3)(0,1,0)[12] : 314.2561
## ARIMA(3,1,0)(0,1,0)[12] : 305.9916
## ARIMA(3,1,1)(0,1,0)[12] : 309.3616
## ARIMA(3,1,2)(0,1,0)[12] : 313.8845
## ARIMA(4,1,0)(0,1,0)[12] : 308.8125
## ARIMA(4,1,1)(0,1,0)[12] : 312.9575
## ARIMA(5,1,0)(0,1,0)[12] : 314.1303
##
##
##
## Best model: ARIMA(0,1,1)(0,1,0)[12]
```

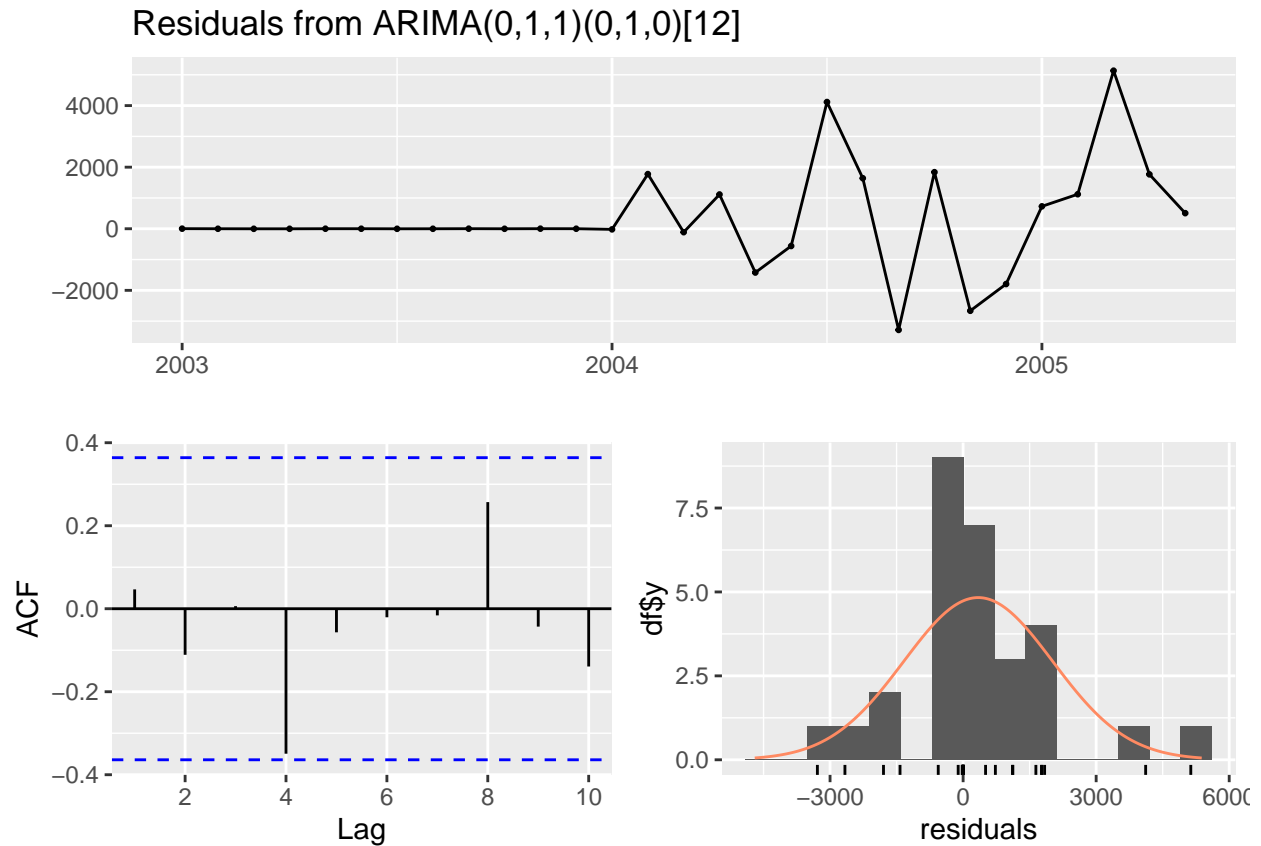
```
#Printing AR Model Summary
```

```
print(summary(AR_Model))
```

```
## Series: sale
## ARIMA(0,1,1)(0,1,0)[12]
##
## Coefficients:
##          ma1
##        -0.8112
## s.e.    0.2503
##
## sigma^2 = 5492903: log likelihood = -146.87
## AIC=297.75 AICc=298.67 BIC=299.29
##
## Training set error measures:
```

```
##
## Training set 340.9011 1685.573 1021.186 1.189803 30.21683 0.5779418 0.04659647
```

```
#Checking Residuals of AR_Model
checkresiduals(AR_Model)
```

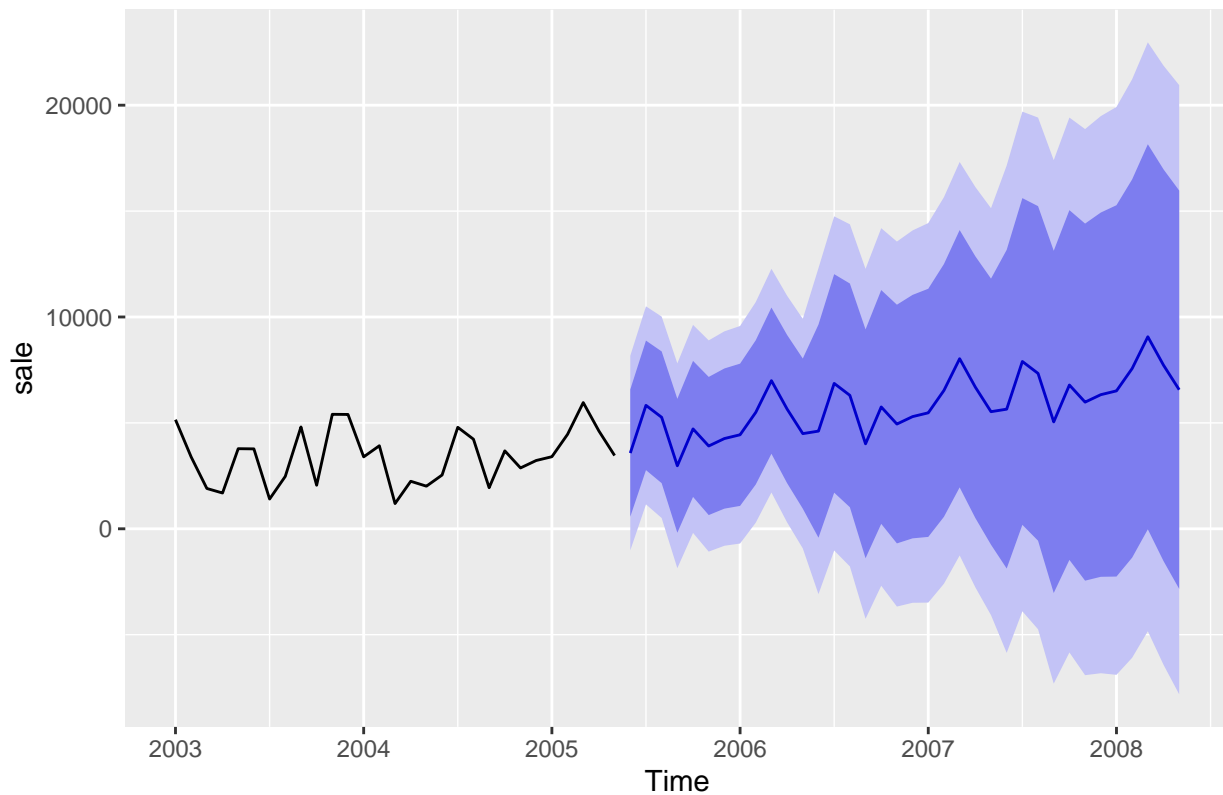


```
##
## Ljung-Box test
##
## data: Residuals from ARIMA(0,1,1)(0,1,0)[12]
## Q* = 5.0074, df = 5, p-value = 0.415
##
## Model df: 1. Total lags used: 6
```

```
#Forecasting ARIMA Model
#forecast two years ahead
AR_Model_Forecast <- forecast(AR_Model, h=36)
```

```
#Plotting AR Model Forecast
#including the last 5 years
autoplot(AR_Model_Forecast, include = 60)
```

Forecasts from ARIMA(0,1,1)(0,1,0)[12]



```
#Print Summary of AR Model Forecast
print(summary(AR_Model_Forecast))
```

```
##
## Forecast method: ARIMA(0,1,1)(0,1,0)[12]
##
## Model Information:
## Series: sale
## ARIMA(0,1,1)(0,1,0)[12]
##
## Coefficients:
##      ma1
##      -0.8112
## s.e.    0.2503
##
## sigma^2 = 5492903:  log likelihood = -146.87
## AIC=297.75   AICc=298.67   BIC=299.29
##
## Error measures:
##           ME      RMSE      MAE      MPE      MAPE      MASE      ACF1
## Training set 340.9011 1685.573 1021.186 1.189803 30.21683 0.5779418 0.04659647
##
## Forecasts:
##           Point Forecast      Lo 80      Hi 80      Lo 95      Hi 95
## Jun 2005      3575.410    571.4262  6579.393 -1018.7867  8169.606
## Jul 2005      5827.730   2770.7051  8884.754  1152.4140 10503.045
```

```
## Aug 2005      5264.110  2154.9487  8373.271   509.0583 10019.161
## Sep 2005      2974.800 -185.6377  6135.237 -1858.6721  7808.272
## Oct 2005      4716.190 1505.2947  7927.085 -194.4504  9626.830
## Nov 2005      3908.910   648.3378  7169.482 -1077.7047  8895.524
## Dec 2005      4260.220   950.7165  7569.723 -801.2287  9321.668
## Jan 2006      4439.260 1081.5382  7796.981 -695.9322  9574.452
## Feb 2006      5496.730 2091.4726  8901.987   288.8383 10704.621
## Mar 2006      6994.410 3542.2714 10446.548 1714.8198 12274.000
## Apr 2006      5651.690 2153.2985  9150.081   301.3621 11002.017
## May 2006      4493.830   949.7892  8037.870 -926.3126  9913.972
## Jun 2006      4611.319 -420.2468  9642.886 -3083.7971 12306.436
## Jul 2006      6863.639 1705.8697 12021.409 -1024.4886 14751.767
## Aug 2006      6300.019 1019.0614 11580.977 -1776.5089 14376.548
## Sep 2006      4010.709 -1390.6281  9412.047 -4249.9235 12271.342
## Oct 2006      5752.099   233.0074 11271.191 -2688.6234 14192.822
## Nov 2006      4944.819 -689.5667 10579.205 -3672.2305 13561.869
## Dec 2006      5296.129 -451.2383 11043.497 -3493.7110 14085.970
## Jan 2007      5475.169 -383.0014 11333.340 -3484.1297 14434.468
## Feb 2007      6532.639   565.7227 12499.556 -2592.9722 15658.251
## Mar 2007      8030.319 1956.6035 14104.035 -1258.6274 17319.266
## Apr 2007      6687.599   508.9301 12866.269 -2761.8598 16137.059
## May 2007      5529.739 -752.1300 11811.609 -4077.5508 15137.030
## Jun 2007      5647.229 -1875.6561 13170.114 -5858.0309 17152.489
## Jul 2007      7899.549   186.7582 15612.340 -3896.1466 19695.245
## Aug 2007      7335.929 -562.2026 15234.061 -4743.2209 19415.079
## Sep 2007      5046.619 -3032.6027 13125.841 -7309.4844 17402.723
## Oct 2007      6788.009 -1468.3319 15044.350 -5838.9748 19414.993
## Nov 2007      5980.729 -2449.0104 14410.469 -6911.4450 18872.903
## Dec 2007      6332.039 -2267.6033 14931.681 -6819.9790 19484.057
## Jan 2008      6511.079 -2255.1739 15277.332 -6895.7479 19917.906
## Feb 2008      7568.549 -1361.2064 16498.305 -6088.3334 21225.431
## Mar 2008      9066.229  -24.0885 18156.547 -4836.2119 22968.670
## Apr 2008      7723.509 -1524.5834 16971.602 -6420.2279 21867.246
## May 2008      6565.649 -2837.5715 15968.870 -7815.3357 20946.634
```

#Forecast 3, Part 1: Forecasting with focus on USA data

#Sub-setting the data to only show sales in USA

```
USA_Sales <- subset(salesdata2, COUNTRY == "USA")
head(USA_Sales)
```

```
##      ORDERNUMBER QUANTITYORDERED PRICEEACH ORDERLINENUMBER  SALES  ORDERDATE
## 579          10100             30     100.00              3 5151.00 2003-01-06
## 681          10100             50      67.80              2 3390.00 2003-01-06
## 1268         10100             22      86.51              4 1903.22 2003-01-06
## 2025         10100             49      34.47              1 1689.03 2003-01-06
## 476          10102             39     100.00              2 4808.31 2003-01-10
## 502          10102             41      50.14              1 2055.74 2003-01-10
##      STATUS QTR_ID MONTH_ID YEAR_ID  PRODUCTLINE MSRP PRODUCTCODE
## 579 Shipped     1         1     2003 Vintage Cars  170   S18_1749
## 681 Shipped     1         1     2003 Vintage Cars   60   S18_2248
## 1268 Shipped     1         1     2003 Vintage Cars   92   S18_4409
## 2025 Shipped     1         1     2003 Vintage Cars   41   S24_3969
## 476 Shipped     1         1     2003 Vintage Cars  102   S18_1342
```

```

## 502 Shipped      1      1      2003 Vintage Cars      53      S18_1367
##                                CUSTOMERNAME      PHONE      ADDRESSLINE1
## 579 Online Diecast Creations Co. 6035558647 2304 Long Airport Avenue
## 681 Online Diecast Creations Co. 6035558647 2304 Long Airport Avenue
## 1268 Online Diecast Creations Co. 6035558647 2304 Long Airport Avenue
## 2025 Online Diecast Creations Co. 6035558647 2304 Long Airport Avenue
## 476      Vitachrome Inc. 2125551500      2678 Kingston Rd.
## 502      Vitachrome Inc. 2125551500      2678 Kingston Rd.
##      ADDRESSLINE2      CITY STATE POSTALCODE COUNTRY TERRITORY CONTACTLASTNAME
## 579      Nashua      NH      62005      USA      <NA>      Young
## 681      Nashua      NH      62005      USA      <NA>      Young
## 1268      Nashua      NH      62005      USA      <NA>      Young
## 2025      Nashua      NH      62005      USA      <NA>      Young
## 476      Suite 101      NYC      NY      10022      USA      <NA>      Frick
## 502      Suite 101      NYC      NY      10022      USA      <NA>      Frick
##      CONTACTFIRSTNAME DEALSIZE
## 579      Valarie      Medium
## 681      Valarie      Medium
## 1268      Valarie      Small
## 2025      Valarie      Small
## 476      Michael      Medium
## 502      Michael      Small

```

#Creating Time Series

```

US_sales <- ts(USA_Sales[,5], start = c(2003,1), end = c(2005,5), frequency = 12)
US_sales

```

```

##      Jan      Feb      Mar      Apr      May      Jun      Jul      Aug      Sep
## 2003 5151.00 3390.00 1903.22 1689.03 4808.31 2055.74 2871.00 3896.49 6065.55
## 2004 3155.14 1858.00 4379.18 4432.70 3157.44 8257.00 6241.60 930.90 3288.78
## 2005 4178.85 2253.68 3415.44 4916.66 2490.50
##      Oct      Nov      Dec
## 2003 3036.60 2055.23 2845.75
## 2004 2354.88 1801.24 4818.15
## 2005

```

#Build Fit Arima Model

#Taking first difference of the data

#Getting rid of seasonality by taking first seasonal difference

```

US_AR_Model <- auto.arima(US_sales, d=1, D=1, stepwise = FALSE, approximation = FALSE, trace = TRUE)

```

```

##
## ARIMA(0,1,0)(0,1,0)[12]      : 305.7411
## ARIMA(0,1,1)(0,1,0)[12]      : Inf
## ARIMA(0,1,2)(0,1,0)[12]      : Inf
## ARIMA(0,1,3)(0,1,0)[12]      : Inf
## ARIMA(0,1,4)(0,1,0)[12]      : Inf
## ARIMA(0,1,5)(0,1,0)[12]      : Inf
## ARIMA(1,1,0)(0,1,0)[12]      : 307.4029
## ARIMA(1,1,1)(0,1,0)[12]      : Inf
## ARIMA(1,1,2)(0,1,0)[12]      : Inf
## ARIMA(1,1,3)(0,1,0)[12]      : Inf

```

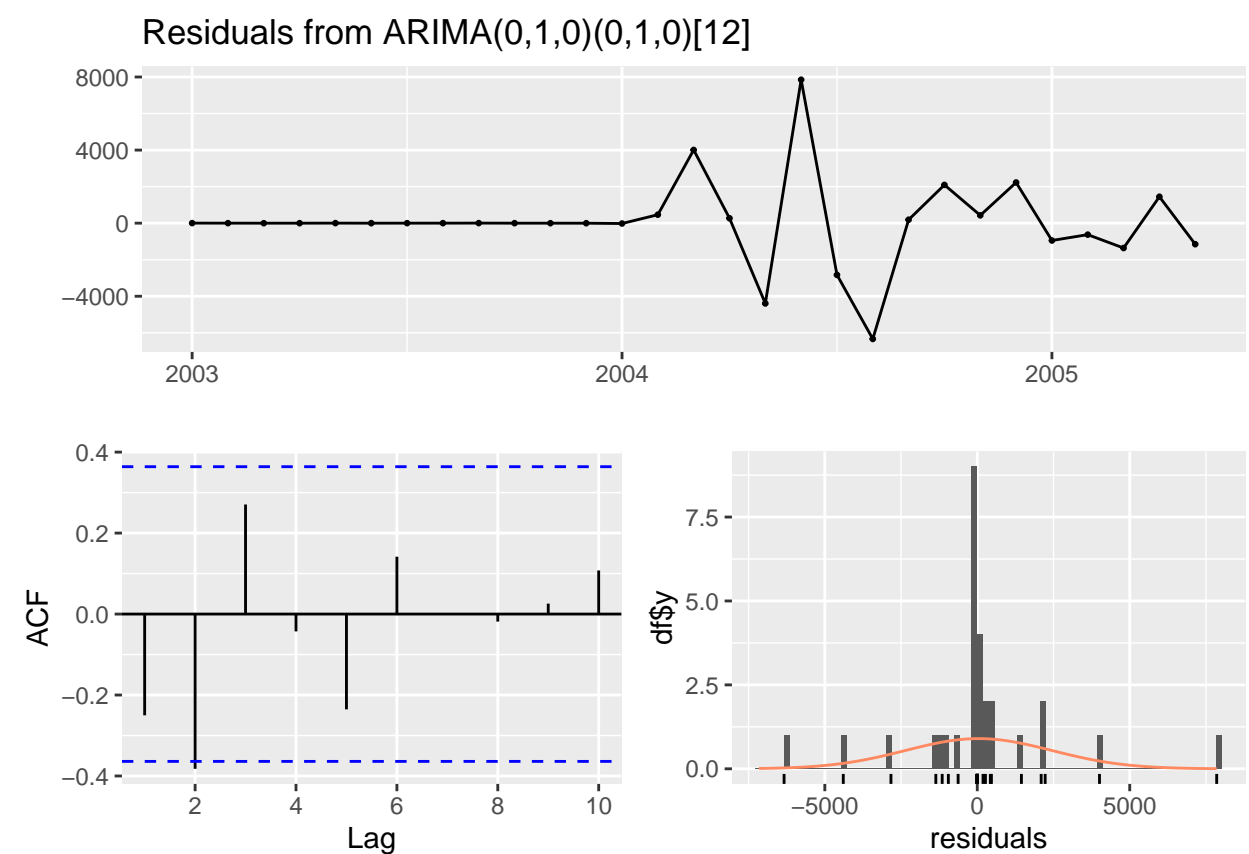


```
## ARIMA(1,1,4)(0,1,0)[12] : Inf
## ARIMA(2,1,0)(0,1,0)[12] : 306.299
## ARIMA(2,1,1)(0,1,0)[12] : Inf
## ARIMA(2,1,2)(0,1,0)[12] : Inf
## ARIMA(2,1,3)(0,1,0)[12] : Inf
## ARIMA(3,1,0)(0,1,0)[12] : 309.9308
## ARIMA(3,1,1)(0,1,0)[12] : Inf
## ARIMA(3,1,2)(0,1,0)[12] : Inf
## ARIMA(4,1,0)(0,1,0)[12] : 313.9995
## ARIMA(4,1,1)(0,1,0)[12] : Inf
## ARIMA(5,1,0)(0,1,0)[12] : 315.5938
##
##
##
## Best model: ARIMA(0,1,0)(0,1,0)[12]
```

```
#Printing AR Model Summary
print(summary(US_AR_Model))
```

```
## Series: US_sales
## ARIMA(0,1,0)(0,1,0)[12]
##
## sigma^2 = 10100398: log likelihood = -151.73
## AIC=305.46 AICc=305.74 BIC=306.23
##
## Training set error measures:
##           ME      RMSE      MAE      MPE      MAPE      MASE      ACF1
## Training set 45.20457 2360.643 1264.177 -20.37292 48.77984 0.6683622 -0.250164
```

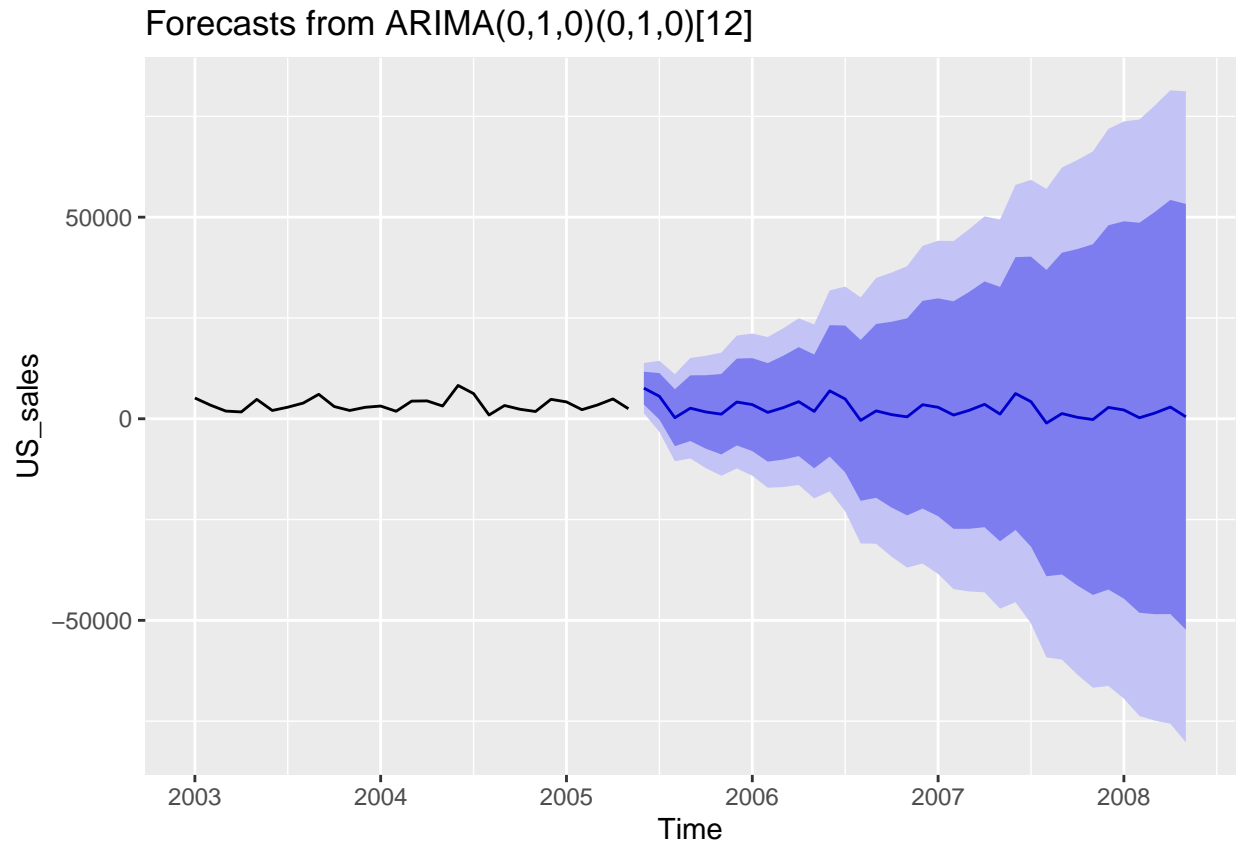
```
#Checking Residuals of AR_Model
checkresiduals(US_AR_Model)
```



```
##
##  Ljung-Box test
##
## data:  Residuals from ARIMA(0,1,0)(0,1,0)[12]
## Q* = 12.335, df = 6, p-value = 0.05491
##
## Model df: 0.   Total lags used: 6
```

```
#Forecasting ARIMA Model
#forecast two years ahead
US_AR_Model_Forecast <- forecast(US_AR_Model, h=36)
```

```
#Plotting AR Model Forecast
#including the last 5 years
autoplot(US_AR_Model_Forecast, include = 60)
```



```
#Print Summary of AR Model Forecast
print(summary(US_AR_Model_Forecast))
```

```
##
## Forecast method: ARIMA(0,1,0)(0,1,0)[12]
##
## Model Information:
## Series: US_sales
## ARIMA(0,1,0)(0,1,0)[12]
##
## sigma^2 = 10100398: log likelihood = -151.73
## AIC=305.46 AICc=305.74 BIC=306.23
##
## Error measures:
##           ME      RMSE      MAE      MPE      MAPE      MASE      ACF1
## Training set 45.20457 2360.643 1264.177 -20.37292 48.77984 0.6683622 -0.250164
##
## Forecasts:
##           Point Forecast      Lo 80      Hi 80      Lo 95      Hi 95
## Jun 2005          7590.06   3517.1452 11662.975   1361.074 13819.05
## Jul 2005          5574.66  -185.3114 11334.631  -3234.456 14383.78
## Aug 2005           263.96 -6790.5354  7318.455 -10524.960 11052.88
## Sep 2005          2621.84 -5523.9897 10767.670  -9836.131 15079.81
## Oct 2005          1687.94 -7419.3744 10795.254 -12240.495 15616.38
## Nov 2005          1134.30 -8842.2631 11110.863 -14123.537 16392.14
## Dec 2005           4151.21 -6624.7098 14927.130 -12329.137 20631.56
```

```
## Jan 2006      3511.91  -8008.0328 15031.853 -14106.322 21130.14
## Feb 2006      1586.74 -10632.0045 13805.485 -17100.217 20273.70
## Mar 2006      2748.50 -10131.1876 15628.188 -16949.282 22446.28
## Apr 2006      4249.72 -9258.6103 17758.050 -16409.488 24908.93
## May 2006      1823.56 -12285.4309 15932.551 -19754.279 23401.40
## Jun 2006      6923.12 -9368.5394 23214.779 -17992.823 31839.06
## Jul 2006      4907.72 -13306.9089 23122.349 -22949.151 32764.59
## Aug 2006      -402.98 -20356.1062 19550.146 -30918.653 30112.69
## Sep 2006      1954.90 -19596.9395 23506.740 -31005.794 34915.59
## Oct 2006      1021.00 -22018.8856 24060.886 -34215.464 36257.46
## Nov 2006       467.36 -23970.1290 24904.849 -36906.554 37841.27
## Dec 2006      3484.27 -22275.1052 29243.645 -35911.295 42879.83
## Jan 2007      2844.97 -24171.6906 29861.631 -38473.447 44163.39
## Feb 2007       919.80 -27298.1817 29137.782 -42235.879 44075.48
## Mar 2007      2081.56 -27288.6466 31451.767 -42836.295 46999.41
## Apr 2007      3582.78 -26896.1238 34061.684 -43030.681 50196.24
## May 2007      1156.62 -30392.0427 32705.283 -47092.896 49406.14
## Jun 2007      6256.18 -27575.9916 40088.352 -45485.661 57998.02
## Jul 2007      4240.78 -31730.2299 40211.790 -50772.132 59253.69
## Aug 2007     -1069.92 -39059.5405 36919.701 -59170.031 57030.19
## Sep 2007      1287.96 -38618.2925 41194.212 -59743.386 62319.31
## Oct 2007       354.06 -41380.8978 42089.018 -63474.050 64182.17
## Nov 2007     -199.58 -43686.4104 43287.250 -66706.948 66307.79
## Dec 2007      2817.33 -42353.4807 47988.141 -66265.463 71900.12
## Jan 2008      2178.03 -44616.1989 48972.259 -69387.567 73743.63
## Feb 2008       252.86 -48110.3241 48616.044 -73712.247 74217.97
## Mar 2008      1414.62 -48468.1956 51297.436 -74874.563 77703.80
## Apr 2008      2915.84 -48441.6620 54273.342 -75628.681 81460.36
## May 2008       489.68 -52301.3299 53280.690 -80247.202 81226.56
```

```
#Forecast 3, Part 2: Testing USA Sales Forecast with manual ARIMA variables
```

```
#Building second USA model
```

```
US2_model <-arima(US_sales,order = c(1,1,2), seasonal = list(order = c(1,1,1)))
```

```
#Print Manual Arima Model Summary
```

```
print(summary(US2_model))
```

```
##
```

```
## Call:
```

```
## arima(x = US_sales, order = c(1, 1, 2), seasonal = list(order = c(1, 1, 1)))
```

```
##
```

```
## Coefficients:
```

```
## Warning in sqrt(diag(x$var.coef)): NaNs produced
```

```
##          ar1          ma1          ma2          sar1          sma1
```

```
##      -0.2617  -0.3827  -0.6172   0.2606   0.2604
```

```
## s.e.   0.3915   0.2986   0.2804      NaN      NaN
```

```
##
```

```
## sigma^2 estimated as 4519107: log likelihood = -147.9, aic = 307.81
```

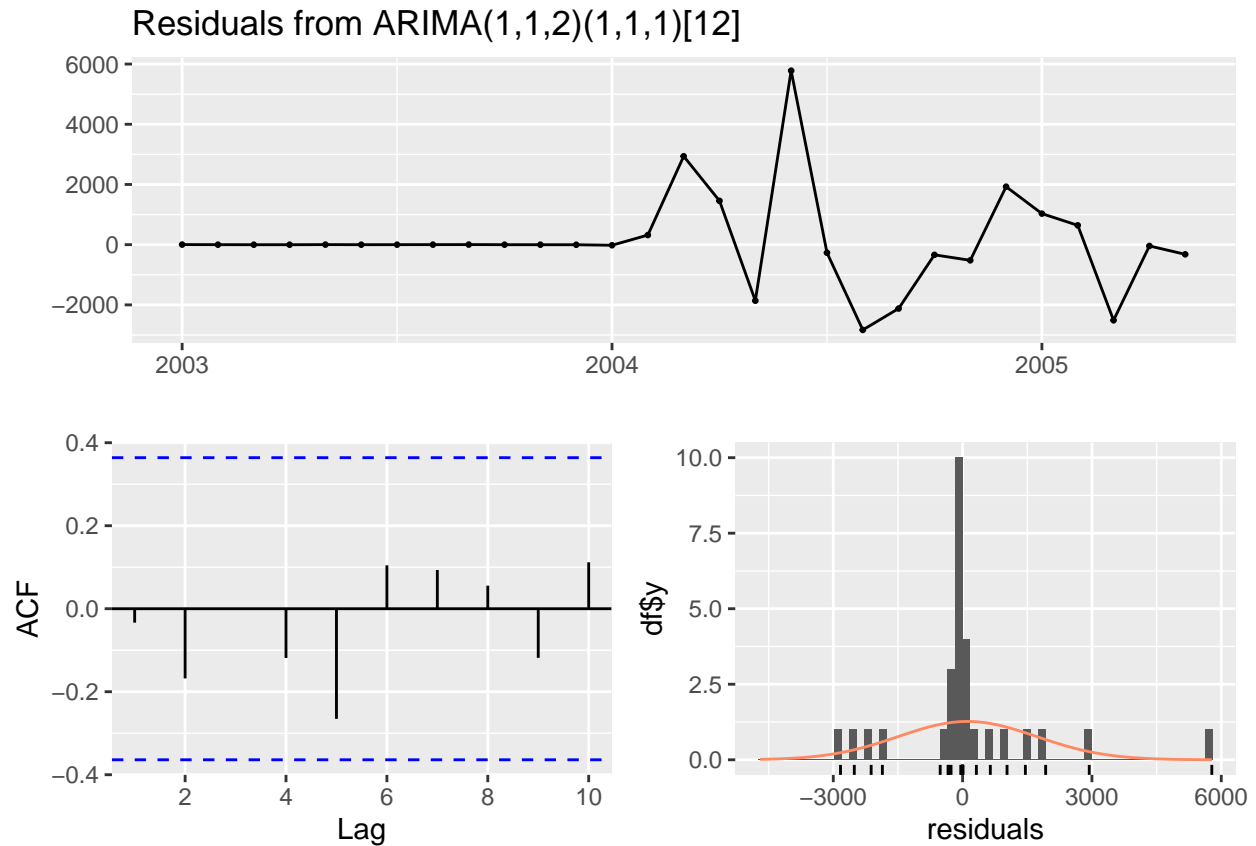
```
##
```

```
## Training set error measures:
```

```
##
## Training set 112.4188 1579.023 860.1448 -9.75588 29.09879 0.4765104 -0.03351387
```

```
#Checking residual values of Manual Arima Model
```

```
checkresiduals(US2_model)
```



```
##
## Ljung-Box test
##
## data: Residuals from ARIMA(1,1,2)(1,1,1)[12]
## Q* = 5.0344, df = 3, p-value = 0.1693
##
## Model df: 5. Total lags used: 8
```

```
#Create Forecast for Manual ARIMA Model
```

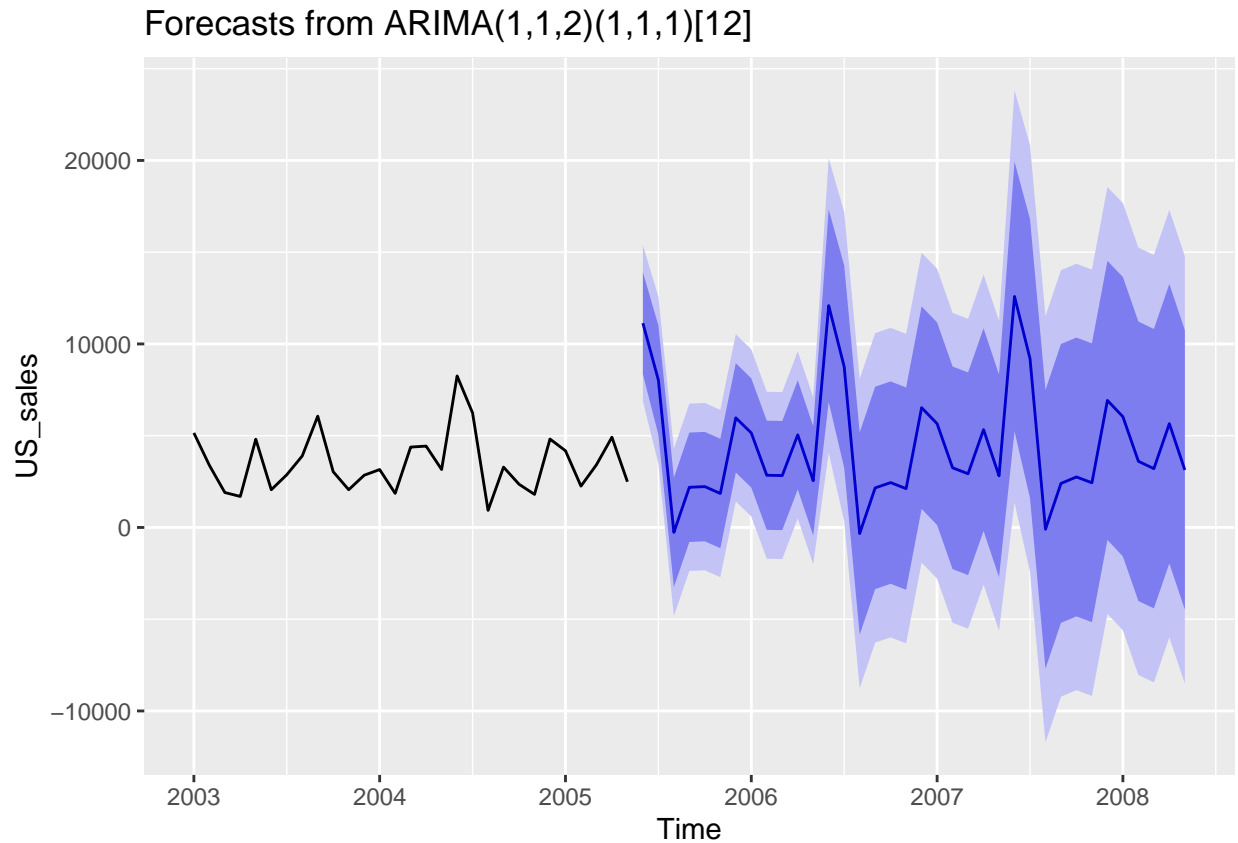
```
#Forecast for the next two years
```

```
US2_Forecast <- forecast(US2_model, h=36)
```

```
#Plot Forecast Results
```

```
#Showing the last 5 years
```

```
autoplot(US2_Forecast, include = 60)
```



```
#Print Summary Forecast Results
print(summary(US2_Forecast))
```

```
##
## Forecast method: ARIMA(1,1,2)(1,1,1)[12]
##
## Model Information:
##
## Call:
## arima(x = US_sales, order = c(1, 1, 2), seasonal = list(order = c(1, 1, 1)))
##
## Coefficients:

## Warning in sqrt(diag(x$var.coef)): NaNs produced

##          ar1          ma1          ma2          sar1          sma1
##        -0.2617   -0.3827   -0.6172    0.2606    0.2604
## s.e.    0.3915    0.2986    0.2804         NaN         NaN
##
## sigma^2 estimated as 4519107:  log likelihood = -147.9,  aic = 307.81
##
## Error measures:
##              ME      RMSE      MAE      MPE      MAPE      MASE      ACF1
## Training set 112.4188 1579.023 860.1448 -9.75588 29.09879 0.4547532 -0.03351387
##
```

```
## Forecasts:
##      Point Forecast      Lo 80      Hi 80      Lo 95      Hi 95
## Jun 2005      11132.10177  8350.3957 13913.808   6877.8494 15386.354
## Jul 2005       8027.96667  5052.8175 11003.116   3477.8687 12578.065
## Aug 2005      -268.74013 -3246.9283  2709.448  -4823.4859  4286.006
## Sep 2005       2190.08259  -790.8085  5170.974  -2368.7969  6748.962
## Oct 2005       2225.98132  -754.6596  5206.622  -2332.5156  6784.478
## Nov 2005       1850.75490 -1128.9582  4830.468  -2706.3231  6407.833
## Dec 2005       5974.21082  2993.2330  8955.189   1415.1987 10533.223
## Jan 2006       5149.27704  2175.1449  8123.409    600.7345  9697.820
## Feb 2006       2844.37886  -129.7505  5818.508  -1704.1595  7392.917
## Mar 2006       2828.10734  -146.0228  5802.237  -1720.4321  7376.647
## Apr 2006       5046.10801  2071.9781  8020.238    497.5689  9594.647
## May 2006       2545.87832  -428.2517  5520.008  -2002.6611  7094.418
## Jun 2006      12087.95238  6841.7430 17334.162   4064.5675 20111.337
## Jul 2006       8756.50736  3244.2386 14268.776    326.2197 17186.795
## Aug 2006      -332.99963 -5841.9433  5175.944  -8758.2019  8092.203
## Sep 2006       2155.98648 -3358.1465  7670.119  -6277.1522 10589.125
## Oct 2006       2443.56935 -3069.9022  7957.041  -5988.5578 10875.696
## Nov 2006       2115.09556 -3396.9004  7627.092  -6314.7748 10544.966
## Dec 2006       6526.80837  1010.4846 12043.132  -1909.6808 14963.298
## Jan 2007       5653.52321   133.5193 11173.527  -2788.5942 14095.641
## Feb 2007       3249.67677 -2270.3215  8769.675  -5192.4321 11691.786
## Mar 2007       2926.45382 -2593.5459  8446.454  -5515.6573 11368.565
## Apr 2007       5331.22145  -188.7779 10851.221  -3110.8891 13773.332
## May 2007       2811.69194 -2708.3077  8331.692  -5630.4190 11253.803
## Jun 2007      12588.39670  5244.1353 19932.658   1356.3182 23820.475
## Jul 2007       9197.72289  1595.8557 16799.590  -2428.3297 20823.776
## Aug 2007       -98.35935 -7689.5092  7492.791 -11708.0212 11511.303
## Sep 2007       2398.48627 -5199.1405  9996.113  -9221.0811 14018.054
## Oct 2007       2751.64897 -4845.0546 10348.353  -8866.5065 14369.804
## Nov 2007       2435.35725 -5159.5199 10030.234  -9180.0051 14050.720
## Dec 2007       6922.17943  -679.1801 14523.539  -4703.0968 18547.456
## Jan 2008       6036.29564 -1576.8372 13649.429  -5606.9864 17679.578
## Feb 2008       3606.66685 -4006.4587 11219.792  -8036.6040 15249.938
## Mar 2008       3203.46338 -4409.6642 10816.591  -8439.8104 14846.737
## Apr 2008       5656.89577 -1956.2312 13270.023  -5986.3772 17300.169
## May 2008       3132.33742 -4480.7899 10745.465  -8510.9361 14775.611
```

```
#Forecast 4, Part 1: Forecasting with Focus on Spain Data
```

```
#Sub-setting the data to only show sales in Spain
```

```
Spain_Sales <- subset(salesdata2, COUNTRY == "Spain")
head(Spain_Sales)
```

```
##      ORDERNUMBER QUANTITYORDERED PRICEEACH ORDERLINENUMBER  SALES  ORDERDATE
## 267          10104             34         100              1 5958.50 2003-01-31
## 368          10104             41         100              9 4615.78 2003-01-31
## 654          10104             24         100              8 3457.92 2003-01-31
## 703          10104             29         100             12 3772.61 2003-01-31
## 1014         10104             23         100             13 4556.99 2003-01-31
## 1242         10104             38         100              3 5348.50 2003-01-31
##      STATUS QTR_ID MONTH_ID YEAR_ID  PRODUCTLINE MSRP PRODUCTCODE
## 267  Shipped      1         1     2003   Classic Cars 151    S12_3148
```

```

## 368 Shipped      1      1    2003 Trucks and Buses 118    S12_4473
## 654 Shipped      1      1    2003      Classic Cars 163    S18_2238
## 703 Shipped      1      1    2003 Trucks and Buses 122    S18_2319
## 1014 Shipped     1      1    2003      Classic Cars 169    S18_3232
## 1242 Shipped     1      1    2003      Classic Cars 143    S18_4027
##              CUSTOMERNAME              PHONE              ADDRESSLINE1 ADDRESSLINE2
## 267 Euro Shopping Channel (91) 555 94 44 C/ Moralarzarzal, 86
## 368 Euro Shopping Channel (91) 555 94 44 C/ Moralarzarzal, 86
## 654 Euro Shopping Channel (91) 555 94 44 C/ Moralarzarzal, 86
## 703 Euro Shopping Channel (91) 555 94 44 C/ Moralarzarzal, 86
## 1014 Euro Shopping Channel (91) 555 94 44 C/ Moralarzarzal, 86
## 1242 Euro Shopping Channel (91) 555 94 44 C/ Moralarzarzal, 86
##              CITY STATE POSTALCODE COUNTRY TERRITORY CONTACTLASTNAME CONTACTFIRSTNAME
## 267 Madrid                28034    Spain      EMEA          Freyre          Diego
## 368 Madrid                28034    Spain      EMEA          Freyre          Diego
## 654 Madrid                28034    Spain      EMEA          Freyre          Diego
## 703 Madrid                28034    Spain      EMEA          Freyre          Diego
## 1014 Madrid               28034    Spain      EMEA          Freyre          Diego
## 1242 Madrid               28034    Spain      EMEA          Freyre          Diego
##              DEALSIZE
## 267      Medium
## 368      Medium
## 654      Medium
## 703      Medium
## 1014     Medium
## 1242     Medium

```

```

#Creating Time Series
Spain_sales <- ts(Spain_Sales[,5], start = c(2003,1), end = c(2005,5), frequency = 12)
Spain_sales

```

```

##              Jan      Feb      Mar      Apr      May      Jun      Jul      Aug      Sep
## 2003 5958.50 4615.78 3457.92 3772.61 4556.99 5348.50 1942.15 1742.40 2921.62
## 2004 1705.92 4219.20 7329.06 3347.74 2439.57 3857.00 2309.58 2795.86 2795.27
## 2005 7083.00 2314.69 3415.77 3576.12 4141.33
##              Oct      Nov      Dec
## 2003 1666.70 3227.63 3705.24
## 2004 3390.20 2921.70 3128.92
## 2005

```

```

#Build Fit Arima Model
#Taking first difference of the data
#Getting rid of seasonality by taking first seasonal difference

Spain_AR_Model <- auto.arima(Spain_sales, d=1, D=1, stepwise = FALSE, approximation = FALSE, trace = TRUE)

##
## ARIMA(0,1,0)(0,1,0)[12] : 307.4258
## ARIMA(0,1,1)(0,1,0)[12] : Inf
## ARIMA(0,1,2)(0,1,0)[12] : Inf
## ARIMA(0,1,3)(0,1,0)[12] : 302.8597
## ARIMA(0,1,4)(0,1,0)[12] : Inf
## ARIMA(0,1,5)(0,1,0)[12] : Inf

```



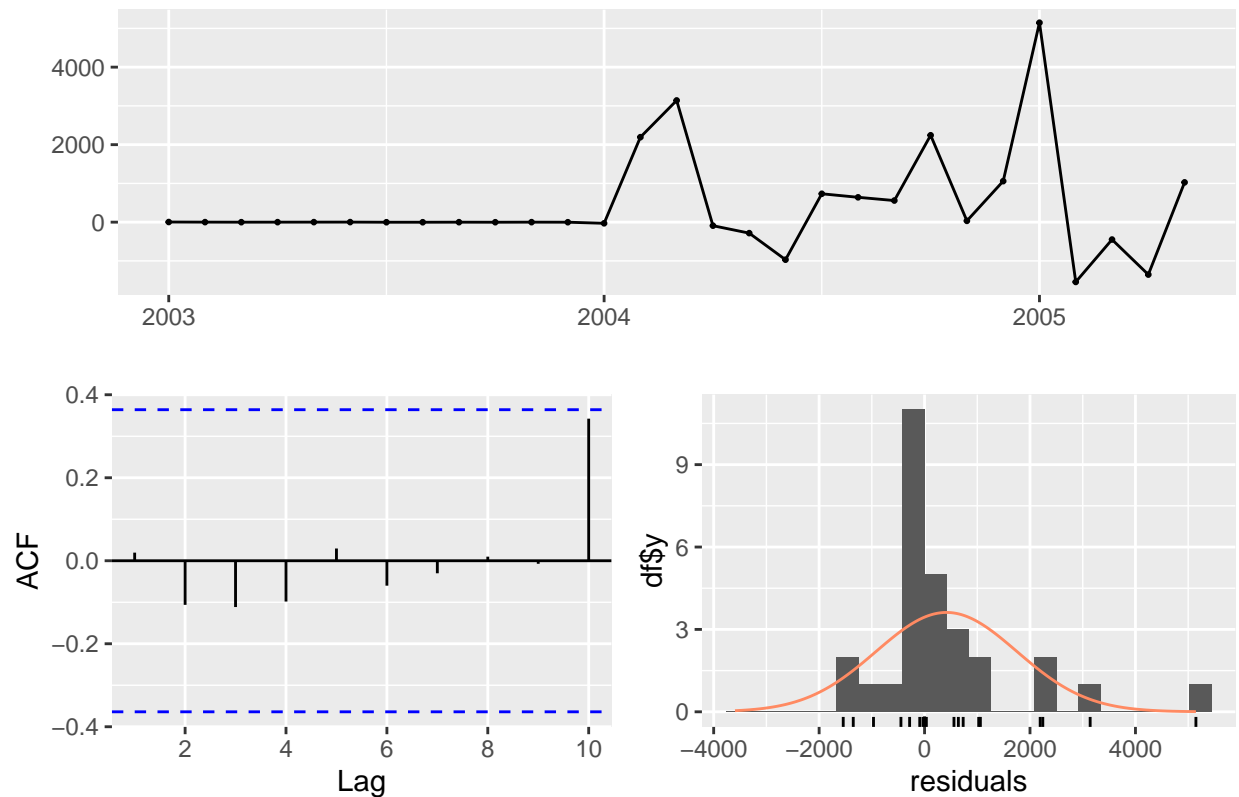
```
## ARIMA(1,1,0)(0,1,0)[12] : 309.5293
## ARIMA(1,1,1)(0,1,0)[12] : Inf
## ARIMA(1,1,2)(0,1,0)[12] : Inf
## ARIMA(1,1,3)(0,1,0)[12] : 307.1979
## ARIMA(1,1,4)(0,1,0)[12] : Inf
## ARIMA(2,1,0)(0,1,0)[12] : 304.3293
## ARIMA(2,1,1)(0,1,0)[12] : Inf
## ARIMA(2,1,2)(0,1,0)[12] : Inf
## ARIMA(2,1,3)(0,1,0)[12] : Inf
## ARIMA(3,1,0)(0,1,0)[12] : 306.4106
## ARIMA(3,1,1)(0,1,0)[12] : Inf
## ARIMA(3,1,2)(0,1,0)[12] : Inf
## ARIMA(4,1,0)(0,1,0)[12] : 307.4779
## ARIMA(4,1,1)(0,1,0)[12] : Inf
## ARIMA(5,1,0)(0,1,0)[12] : 312.7335
##
##
##
## Best model: ARIMA(0,1,3)(0,1,0)[12]
```

```
#Printing AR Model Summary
print(summary(Spain_AR_Model))
```

```
## Series: Spain_sales
## ARIMA(0,1,3)(0,1,0)[12]
##
## Coefficients:
##          ma1      ma2      ma3
##      -0.9670  -0.7277  0.7913
## s.e.   0.4764   0.3612  0.5304
##
## sigma^2 = 4236114: log likelihood = -145.61
## AIC=299.22 AICc=302.86 BIC=302.31
##
## Training set error measures:
##              ME      RMSE      MAE      MPE      MAPE      MASE      ACF1
## Training set 415.5884 1378.023 741.585 7.201743 18.18483 0.4225967 0.01957441
```

```
#Checking Residuals of AR_Model
checkresiduals(Spain_AR_Model)
```

Residuals from ARIMA(0,1,3)(0,1,0)[12]

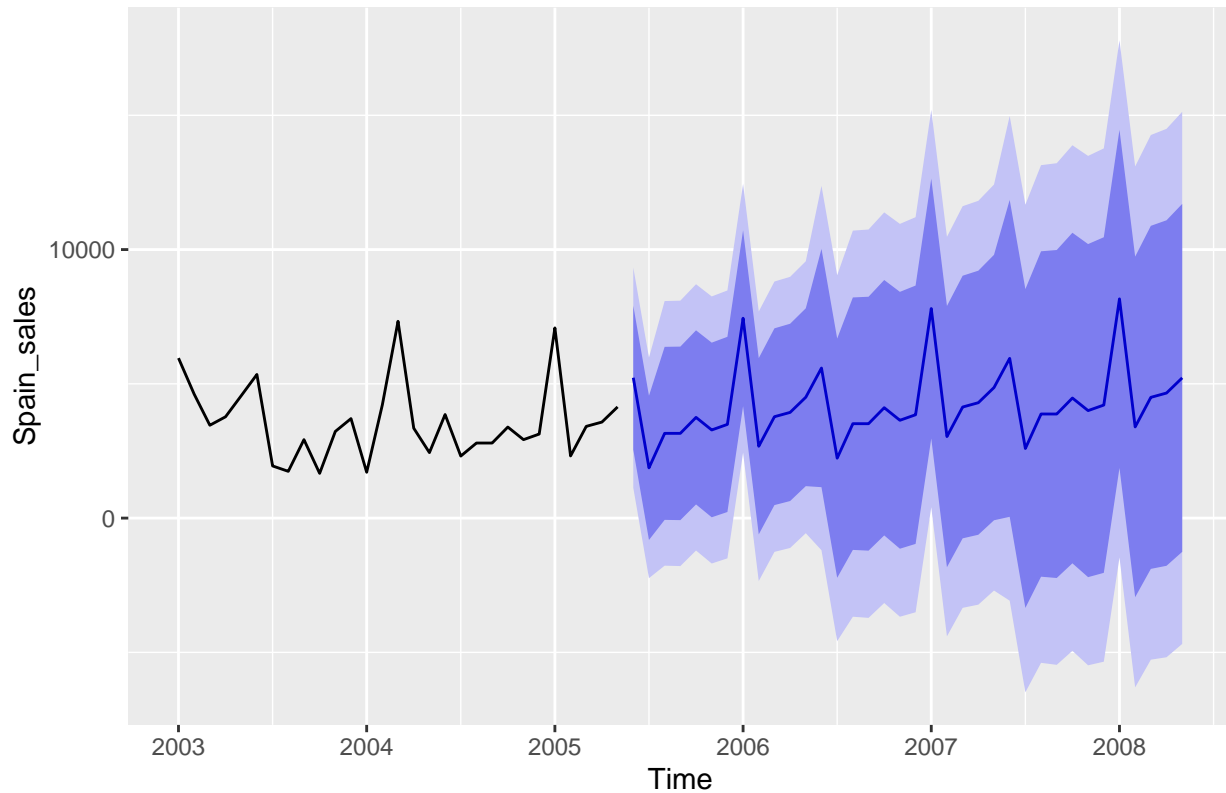


```
##
##  Ljung-Box test
##
## data:  Residuals from ARIMA(0,1,3)(0,1,0)[12]
## Q* = 1.3391, df = 3, p-value = 0.7199
##
## Model df: 3.   Total lags used: 6
```

```
#Forecasting ARIMA Model
#forecast two years ahead
Spain_AR_Model_Forecast <- forecast(Spain_AR_Model, h=36)
```

```
#Plotting AR Model Forecast
#including the last 5 years
autoplot(Spain_AR_Model_Forecast, include = 60)
```

Forecasts from ARIMA(0,1,3)(0,1,0)[12]



```
#Print Summary of AR Model Forecast
print(summary(Spain_AR_Model_Forecast))
```

```
##
## Forecast method: ARIMA(0,1,3)(0,1,0)[12]
##
## Model Information:
## Series: Spain_sales
## ARIMA(0,1,3)(0,1,0)[12]
##
## Coefficients:
##          ma1      ma2      ma3
##      -0.9670  -0.7277  0.7913
## s.e.   0.4764   0.3612  0.5304
##
## sigma^2 = 4236114:  log likelihood = -145.61
## AIC=299.22   AICc=302.86   BIC=302.31
##
## Error measures:
##              ME      RMSE      MAE      MPE      MAPE      MASE      ACF1
## Training set 415.5884 1378.023 741.585 7.201743 18.18483 0.4225967 0.01957441
##
## Forecasts:
##      Point Forecast      Lo 80      Hi 80      Lo 95      Hi 95
## Jun 2005      5227.953 2547.17935 7908.727 1128.0633 9327.843
## Jul 2005      1870.941 -813.73515 4555.616 -2234.9166 5976.798
```

```
## Aug 2005      3156.232   -64.96746  6377.431 -1770.1673  8082.631
## Sep 2005      3155.642   -75.62026  6386.904 -1786.1470  8097.430
## Oct 2005      3750.572   509.27817  6991.865 -1206.5590  8707.702
## Nov 2005      3282.072    30.77755  6533.366 -1690.3536  8254.497
## Dec 2005      3489.292   228.02760  6750.556 -1498.3813  8476.965
## Jan 2006      7443.372  4172.16804 10714.575  2440.4974 12446.246
## Feb 2006      2675.062  -606.05141  5956.175 -2342.9678  7693.091
## Mar 2006      3776.142   485.14897  7067.134 -1256.9974  8809.281
## Apr 2006      3936.492   635.64893  7237.335 -1111.7117  8984.695
## May 2006      4501.702  1191.03819  7812.365  -561.5212  9564.925
## Jun 2006      5588.325  1152.33733 10024.313 -1195.9327 12372.583
## Jul 2006      2231.312 -2222.70864  6685.333 -4580.5249  9043.150
## Aug 2006      3516.603 -1183.69195  8216.899 -3671.8780 10705.085
## Sep 2006      3516.013 -1211.82923  8243.856 -3714.5980 10746.625
## Oct 2006      4110.943  -644.28692  8866.174 -3161.5538 11383.441
## Nov 2006      3642.443 -1140.01778  8424.905 -3671.6998 10956.587
## Dec 2006      3849.663  -959.87446  8659.201 -3505.8900 11205.217
## Jan 2007      7803.743  2967.28044 12640.206   407.0116 15200.475
## Feb 2007      3035.433 -1827.80558  7898.672 -4402.2488 10473.116
## Mar 2007      4136.513  -753.35500  9026.382 -3341.8950 11614.922
## Apr 2007      4296.863  -619.49017  9213.217 -3222.0506 11815.777
## May 2007      4862.073  -80.62343  9804.770 -2697.1291 12421.276
## Jun 2007      5948.697   48.81958 11848.574 -3074.3867 14971.780
## Jul 2007      2591.684 -3344.48538  8527.853 -6486.9036 11670.272
## Aug 2007      3876.975 -2181.76027  9935.711 -5389.0611 13143.011
## Sep 2007      3876.385 -2230.38517  9983.156 -5463.1141 13215.884
## Oct 2007      4471.315 -1683.11517 10625.746 -4941.0738 13883.704
## Nov 2007      4002.815 -2198.90892 10204.539 -5481.9034 13487.534
## Dec 2007      4210.035 -2038.62474 10458.695 -5346.4655 13766.536
## Jan 2008      8164.115  1868.86938 14459.361 -1463.6324 17791.863
## Feb 2008      3395.805 -2945.68428  9737.295 -6302.6660 13094.276
## Mar 2008      4496.885 -1890.51315 10884.283 -5271.7976 14265.568
## Apr 2008      4657.235 -1775.74440 11090.215 -5181.1581 14495.628
## May 2008      5222.445 -1255.79495 11700.685 -4685.1681 15130.058
```

```
#Forecast 4, Part 2: Testing Spain Sales Forecast with manual ARIMA variables
```

```
#Building second Spain model
```

```
Spain2_model <-arima(Spain_sales,order = c(1,1,2), seasonal = list(order = c(1,1,1)))
```

```
#Print Manual Arima Model Summary
```

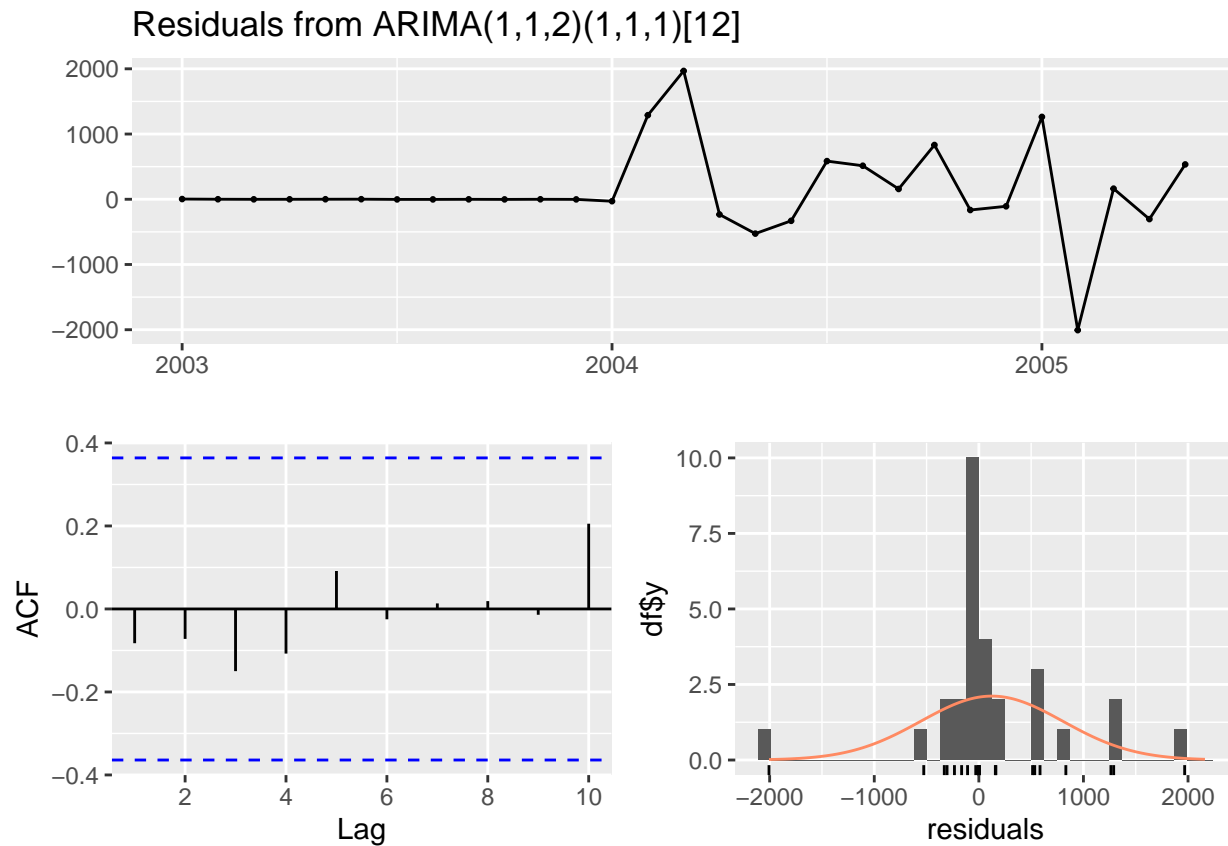
```
print(summary(Spain2_model))
```

```
##
## Call:
## arima(x = Spain_sales, order = c(1, 1, 2), seasonal = list(order = c(1, 1, 1)))
##
## Coefficients:
##          ar1          ma1          ma2          sar1          sma1
##      -0.6549  -0.0103  -0.9896  -0.5987  -0.8971
## s.e.   0.2738   2.1122   2.1118   0.3323   6.2131
##
## sigma^2 estimated as 835194:  log likelihood = -144.03,  aic = 300.06
```

```
##
## Training set error measures:
##           ME      RMSE      MAE      MPE      MAPE      MASE      ACF1
## Training set 124.1344 678.843 380.1319 0.8057485 10.70574 0.264418 -0.08251263
```

```
#Checking residual values of Manual Arima Model
```

```
checkresiduals(Spain2_model)
```



```
##
## Ljung-Box test
##
## data: Residuals from ARIMA(1,1,2)(1,1,1)[12]
## Q* = 1.9439, df = 3, p-value = 0.5841
##
## Model df: 5. Total lags used: 8
```

```
#Create Forecast for Manual ARIMA Model
```

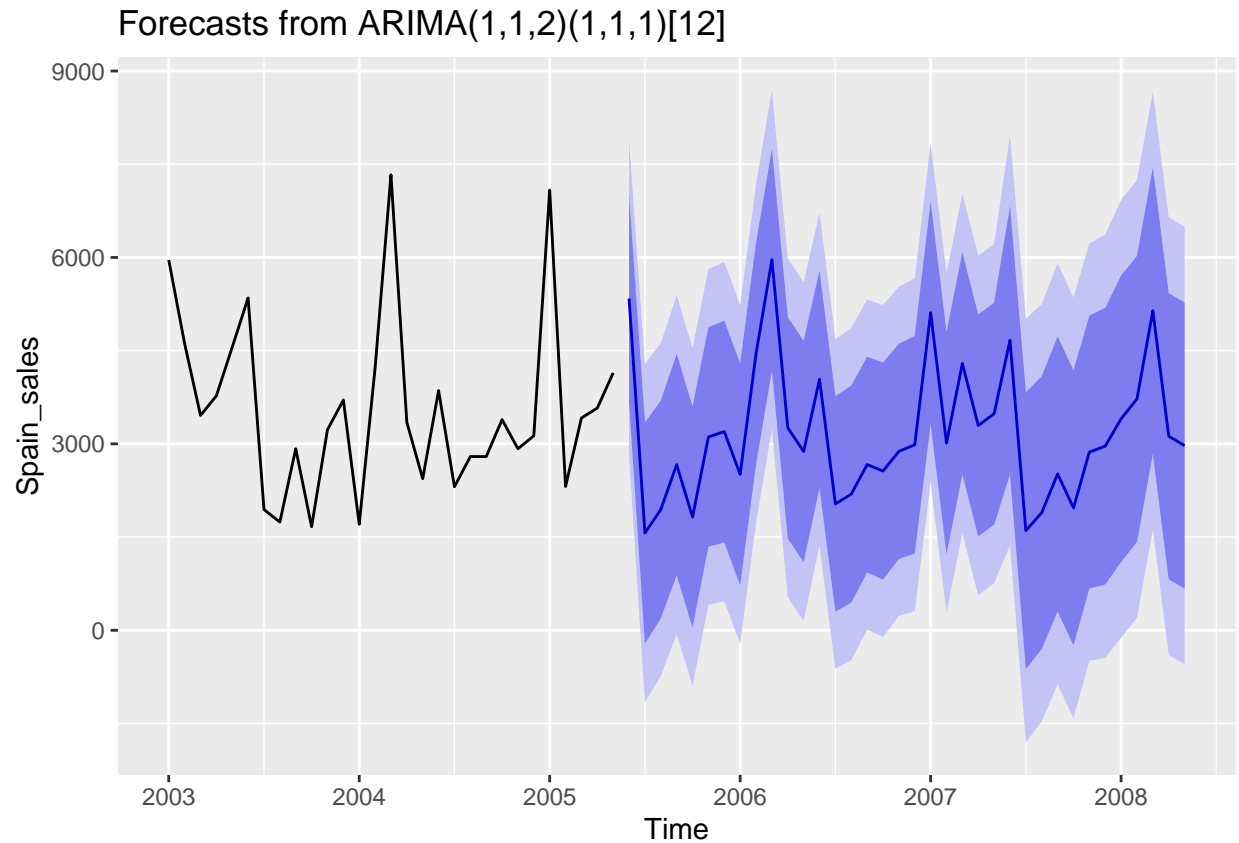
```
#Forecast for the next two years
```

```
Spain2_Forecast <- forecast(Spain2_model, h=36)
```

```
#Plot Forecast Results
```

```
#Showing the last 5 years
```

```
autoplot(Spain2_Forecast, include = 60)
```



```
#Print Summary Forecast Results
print(summary(Spain2_Forecast))
```

```
##
## Forecast method: ARIMA(1,1,2)(1,1,1)[12]
##
## Model Information:
##
## Call:
## arima(x = Spain_sales, order = c(1, 1, 2), seasonal = list(order = c(1, 1, 1)))
##
## Coefficients:
##          ar1          ma1          ma2          sar1          sma1
##       -0.6549   -0.0103   -0.9896   -0.5987   -0.8971
## s.e.    0.2738    2.1122    2.1118    0.3323    6.2131
##
## sigma^2 estimated as 835194:  log likelihood = -144.03,  aic = 300.06
##
## Error measures:
##              ME      RMSE      MAE      MPE      MAPE      MASE      ACF1
## Training set 124.1344 678.843 380.1319 0.8057485 10.70574 0.2166204 -0.08251263
##
## Forecasts:
##           Point Forecast      Lo 80      Hi 80      Lo 95      Hi 95
## Jun 2005          5338.919 3674.85873 7002.979 2793.95839 7883.880
## Jul 2005          1564.634 -214.99233 3344.260 -1157.06947 4286.337
```

```
## Aug 2005      1943.854  192.27678 3695.432 -734.95244 4622.661
## Sep 2005      2666.011  884.15183 4447.871  -59.10757 5391.130
## Oct 2005      1821.639   45.14929 3598.129 -895.26760 4538.546
## Nov 2005      3110.397 1344.05220 4876.741  409.00593 5811.787
## Dec 2005      3197.668 1413.49694 4981.838  469.01402 5926.321
## Jan 2006      2508.932  725.34851 4292.516 -218.82362 5236.688
## Feb 2006      4448.932 2669.50873 6228.355 1727.53906 7170.325
## Mar 2006      5963.929 4182.05186 7745.807 3238.78293 8689.076
## Apr 2006      3258.450 1477.62709 5039.272  534.91660 5981.983
## May 2006      2877.406 1096.68763 4658.125  154.03208 5600.781
## Jun 2006      4039.347 2290.23803 5788.457 1364.31550 6714.379
## Jul 2006      2032.702  299.75711 3765.646 -617.60828 4683.011
## Aug 2006      2191.510  445.21175 3937.809 -479.22292 4862.244
## Sep 2006      2667.292  932.36688 4402.217   13.95308 5320.631
## Oct 2006      2562.598  815.92799 4309.268 -108.70326 5233.899
## Nov 2006      2879.205 1147.61169 4610.797  230.96181 5527.447
## Dec 2006      2985.940 1235.74299 4736.137  309.24470 5662.635
## Jan 2007      5111.173 3326.52440 6895.823 2381.78825 7840.559
## Feb 2007      3012.410 1226.29044 4798.530  280.77566 5744.045
## Mar 2007      4294.300 2509.27789 6079.322 1564.34423 7024.256
## Apr 2007      3294.978 1509.02153 5080.935  563.59317 6026.363
## May 2007      3486.771 1701.75323 5271.790  756.82167 6216.721
## Jun 2007      4665.923 2510.08957 6821.757 1368.86013 7962.986
## Jul 2007      1603.687 -623.55629 3830.930 -1802.58754 5009.961
## Aug 2007      1892.685 -302.22306 4087.593 -1464.13731 5249.508
## Sep 2007      2517.134  303.86557 4730.402 -867.76792 5902.036
## Oct 2007      1968.830 -243.66760 4181.327 -1414.89295 5352.552
## Nov 2007      2867.967  671.83296 5064.101 -490.73025 6226.665
## Dec 2007      2962.723  736.21051 5189.235 -442.43399 6367.880
## Jan 2008      3403.429 1099.60116 5707.257 -119.97169 6926.830
## Feb 2008      3722.559 1421.14733 6023.970  202.85369 7242.264
## Mar 2008      5144.103 2841.42391 7446.782 1622.45912 8665.747
## Apr 2008      3123.234  820.88040 5425.587 -397.91194 6644.380
## May 2008      2972.106  670.30390 5273.907 -548.19635 6492.408
```

```
#Forecast 5, Part 1: Forecasting with focus on Classic Cars
```

```
#Sub-setting the data to only show sales in
```

```
Class_Car_Sales <- subset(salesdata2, PRODUCTLINE == "Classic Cars")
head(Class_Car_Sales)
```

```
##      ORDERNUMBER QUANTITYORDERED PRICEEACH ORDERLINENUMBER  SALES  ORDERDATE
## 27             10103              26         100             11 5404.62 2003-01-29
## 134            10103              42         100              4 5398.26 2003-01-29
## 2615           10103              42         100              6 4460.82 2003-01-29
## 267            10104              34         100              1 5958.50 2003-01-31
## 654            10104              24         100              8 3457.92 2003-01-31
## 1014           10104              23         100             13 4556.99 2003-01-31
##      STATUS QTR_ID MONTH_ID YEAR_ID  PRODUCTLINE MSRP PRODUCTCODE
## 27  Shipped     1         1     2003 Classic Cars  214   S10_1949
## 134 Shipped     1         1     2003 Classic Cars  147   S10_4962
## 2615 Shipped     1         1     2003 Classic Cars  101   S700_2824
## 267  Shipped     1         1     2003 Classic Cars  151   S12_3148
## 654  Shipped     1         1     2003 Classic Cars  163   S18_2238
```

```
## 1014 Shipped      1      1      2003 Classic Cars  169      S18_3232
##              CUSTOMERNAME              PHONE              ADDRESSLINE1 ADDRESSLINE2
## 27      Baane Mini Imports      07-98 9555 Erling Skakkes gate 78
## 134     Baane Mini Imports      07-98 9555 Erling Skakkes gate 78
## 2615    Baane Mini Imports      07-98 9555 Erling Skakkes gate 78
## 267     Euro Shopping Channel (91) 555 94 44      C/ Moralarzal, 86
## 654     Euro Shopping Channel (91) 555 94 44      C/ Moralarzal, 86
## 1014    Euro Shopping Channel (91) 555 94 44      C/ Moralarzal, 86
##              CITY STATE POSTALCODE COUNTRY TERRITORY CONTACTLASTNAME
## 27      Stavern      4110 Norway      EMEA      Bergulfsen
## 134     Stavern      4110 Norway      EMEA      Bergulfsen
## 2615    Stavern      4110 Norway      EMEA      Bergulfsen
## 267     Madrid      28034 Spain      EMEA      Freyre
## 654     Madrid      28034 Spain      EMEA      Freyre
## 1014    Madrid      28034 Spain      EMEA      Freyre
##              CONTACTFIRSTNAME DEALSIZE
## 27      Jonas      Medium
## 134     Jonas      Medium
## 2615    Jonas      Medium
## 267     Diego      Medium
## 654     Diego      Medium
## 1014    Diego      Medium
```

#Creating Time Series

```
Class_Car_sales <- ts(Class_Car_Sales[,5], start = c(2003,1), end = c(2005,5), frequency = 12)
Class_Car_sales
```

```
##              Jan      Feb      Mar      Apr      May      Jun      Jul      Aug      Sep
## 2003 5404.62 5398.26 4460.82 5958.50 3457.92 4556.99 5348.50 1942.15 1742.40
## 2004 4566.05 5265.15 6130.35 3485.82 3731.04 3130.82 1777.10 4049.56 5565.12
## 2005 4379.18 4432.70 3157.44 8257.00 6241.60
##              Oct      Nov      Dec
## 2003 2921.62 7208.00 8690.36
## 2004 1892.10 5448.80 2130.01
## 2005
```

#Build Fit Arima Model

#Taking first differnce of the data

#Getting rid of seasonality by taking first seasonal difference

```
CC_AR_Model <- auto.arima(Class_Car_sales, d=1, D=1, stepwise = FALSE, approximation = FALSE, trace = T)
```

```
##
## ARIMA(0,1,0)(0,1,0)[12] : 311.3148
## ARIMA(0,1,1)(0,1,0)[12] : Inf
## ARIMA(0,1,2)(0,1,0)[12] : Inf
## ARIMA(0,1,3)(0,1,0)[12] : Inf
## ARIMA(0,1,4)(0,1,0)[12] : Inf
## ARIMA(0,1,5)(0,1,0)[12] : Inf
## ARIMA(1,1,0)(0,1,0)[12] : 311.3759
## ARIMA(1,1,1)(0,1,0)[12] : Inf
## ARIMA(1,1,2)(0,1,0)[12] : Inf
## ARIMA(1,1,3)(0,1,0)[12] : Inf
```



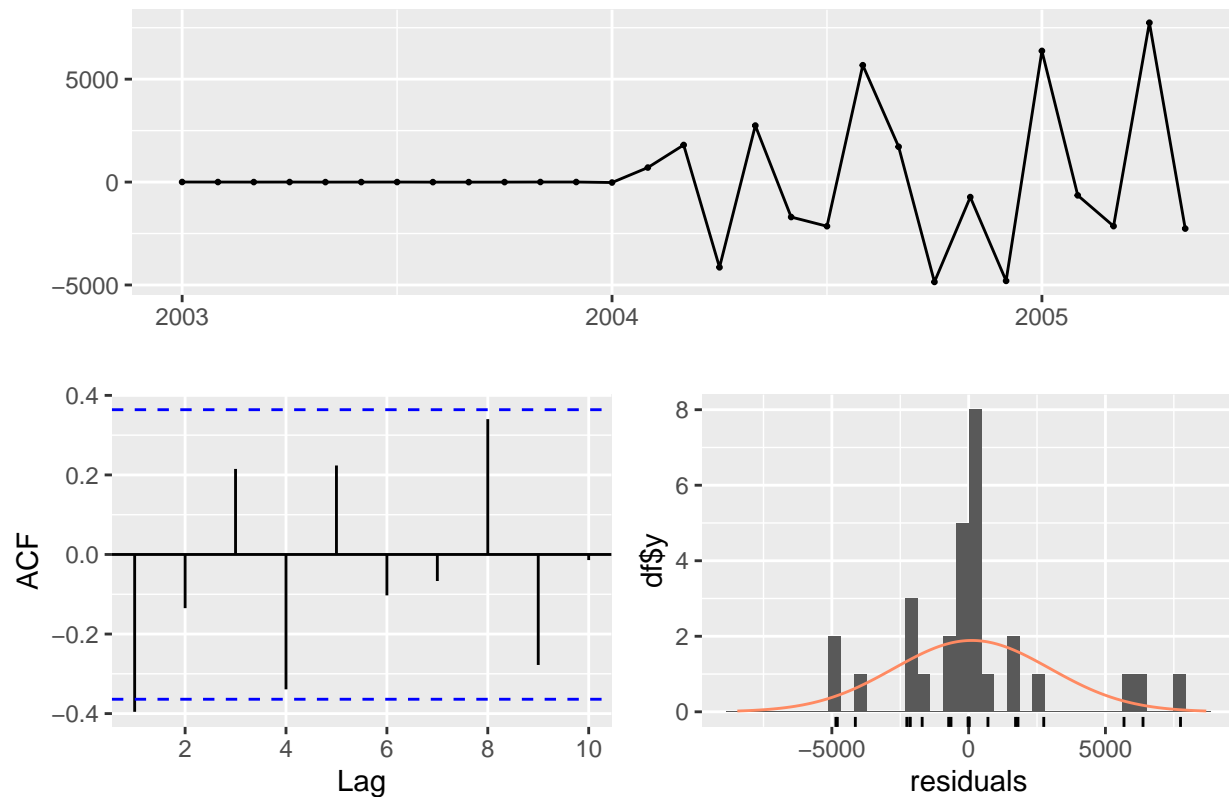
```
## ARIMA(1,1,4)(0,1,0)[12] : Inf
## ARIMA(2,1,0)(0,1,0)[12] : 312.4
## ARIMA(2,1,1)(0,1,0)[12] : Inf
## ARIMA(2,1,2)(0,1,0)[12] : Inf
## ARIMA(2,1,3)(0,1,0)[12] : Inf
## ARIMA(3,1,0)(0,1,0)[12] : 315.9898
## ARIMA(3,1,1)(0,1,0)[12] : Inf
## ARIMA(3,1,2)(0,1,0)[12] : Inf
## ARIMA(4,1,0)(0,1,0)[12] : 317.3993
## ARIMA(4,1,1)(0,1,0)[12] : Inf
## ARIMA(5,1,0)(0,1,0)[12] : 322.7064
##
##
##
## Best model: ARIMA(0,1,0)(0,1,0)[12]
```

```
#Printing AR Model Summary
print(summary(CC_AR_Model))
```

```
## Series: Class_Car_sales
## ARIMA(0,1,0)(0,1,0)[12]
##
## sigma^2 = 14309652: log likelihood = -154.51
## AIC=311.03 AICc=311.31 BIC=311.8
##
## Training set error measures:
##           ME      RMSE      MAE      MPE      MAPE      MASE      ACF1
## Training set 114.9285 2809.801 1731.863 -13.15426 49.49796 0.7970617 -0.3954847
```

```
#Checking Residuals of AR_Model
checkresiduals(CC_AR_Model)
```

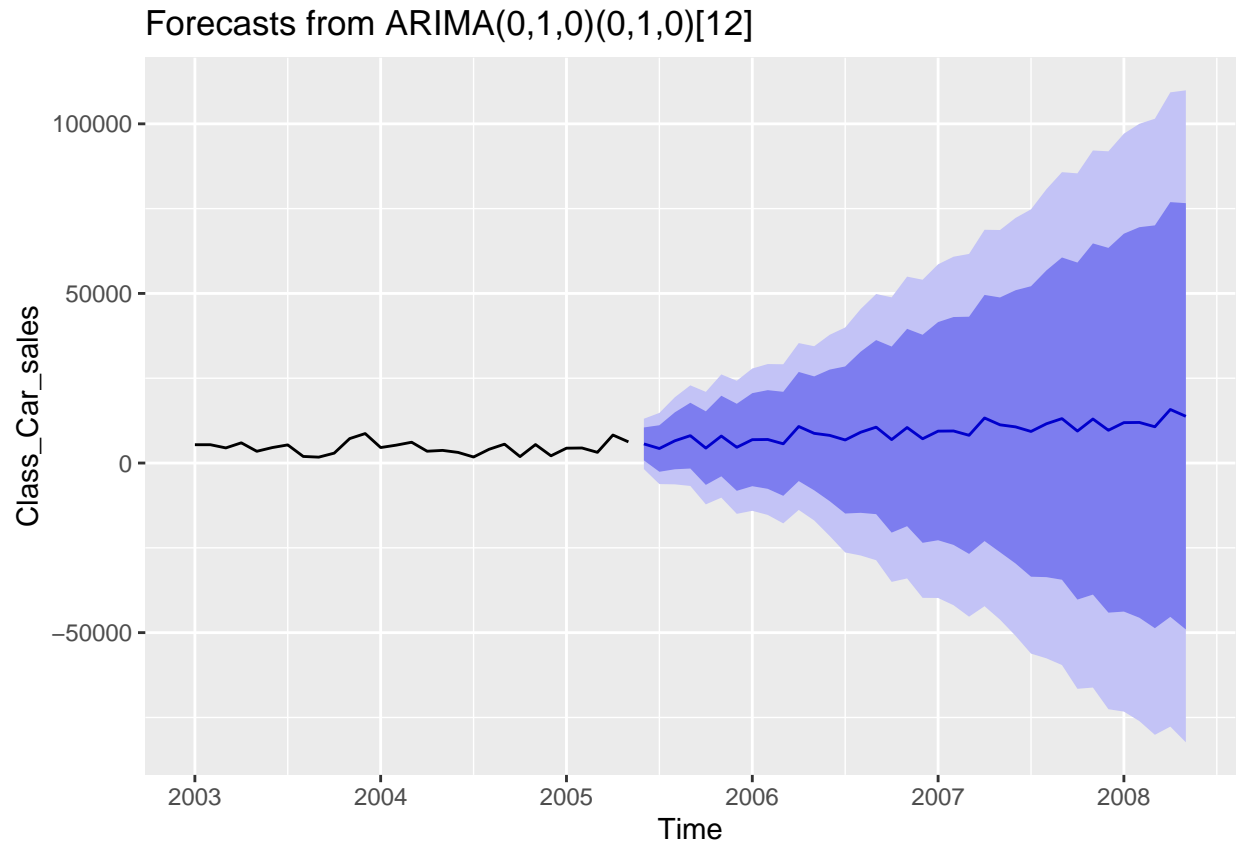
Residuals from ARIMA(0,1,0)(0,1,0)[12]



```
##
##  Ljung-Box test
##
## data:  Residuals from ARIMA(0,1,0)(0,1,0)[12]
## Q* = 13.648, df = 6, p-value = 0.03382
##
## Model df: 0.   Total lags used: 6
```

```
#Forecasting ARIMA Model
#forecast two years ahead
CC_AR_Model_Forecast <- forecast(CC_AR_Model, h=36)
```

```
#Plotting AR Model Forecast
#including the last 5 years
autoplot(CC_AR_Model_Forecast, include = 60)
```



```
#Print Summary of AR Model Forecast
print(summary(CC_AR_Model_Forecast))
```

```
##
## Forecast method: ARIMA(0,1,0)(0,1,0)[12]
##
## Model Information:
## Series: Class_Car_sales
## ARIMA(0,1,0)(0,1,0)[12]
##
## sigma^2 = 14309652: log likelihood = -154.51
## AIC=311.03 AICc=311.31 BIC=311.8
##
## Error measures:
##           ME      RMSE      MAE      MPE      MAPE      MASE      ACF1
## Training set 114.9285 2809.801 1731.863 -13.15426 49.49796 0.7970617 -0.3954847
##
## Forecasts:
##           Point Forecast      Lo 80      Hi 80      Lo 95      Hi 95
## Jun 2005          5641.38    793.5138 10489.25 -1772.792 13055.55
## Jul 2005          4287.66 -2568.2581 11143.58 -6197.562 14772.88
## Aug 2005          6560.12 -1836.6306 14956.87 -6281.602 19401.84
## Sep 2005          8075.68 -1620.0524 17771.41 -6752.663 22904.02
## Oct 2005          4402.66 -6437.4984 15242.82 -12175.932 20981.25
## Nov 2005          7959.36 -3915.4385 19834.16 -10201.577 26120.30
## Dec 2005          4640.57 -8185.6783 17466.82 -14975.484 24256.62
```

```
## Jan 2006      6889.74 -6822.0962 20601.58 -14080.704 27860.18
## Feb 2006      6943.26 -7600.3386 21486.86 -15299.255 29185.77
## Mar 2006      5668.00 -9662.2990 20998.30 -17777.669 29113.67
## Apr 2006     10767.56 -5310.9932 26846.11 -13822.465 35357.59
## May 2006      8752.16 -8041.3411 25545.66 -16931.284 34435.60
## Jun 2006      8151.94 -11239.5248 27543.40 -21504.746 37808.63
## Jul 2006      6798.22 -14882.0967 28478.54 -26358.963 39955.40
## Aug 2006      9070.68 -14678.9170 32820.28 -27251.194 45392.55
## Sep 2006     10586.24 -15066.2567 36238.74 -28645.868 49818.35
## Oct 2006      6913.22 -20510.4525 34336.89 -35027.668 48854.11
## Nov 2006     10469.92 -18617.2772 39557.12 -34015.109 54954.95
## Dec 2006      7151.13 -23509.4679 37811.73 -39740.208 54042.47
## Jan 2007      9400.30 -22756.8064 41557.41 -39779.750 58580.35
## Feb 2007      9453.82 -24133.1822 43040.82 -41913.067 60820.71
## Mar 2007      8178.56 -26779.9003 43137.02 -45285.791 61642.91
## Apr 2007     13278.12 -22999.9887 49556.23 -42204.459 68760.70
## May 2007     11262.72 -26288.6901 48814.13 -46167.206 68692.65
## Jun 2007     10662.50 -29606.9010 50931.90 -50924.234 72249.23
## Jul 2007      9308.78 -33506.4150 52123.97 -56171.410 74788.97
## Aug 2007     11581.24 -33636.6456 56799.13 -57573.548 80736.03
## Sep 2007     13096.80 -34402.3941 60595.99 -59546.949 85740.55
## Oct 2007      9423.78 -40252.0662 59099.63 -66548.871 85396.43
## Nov 2007     12980.48 -38780.5667 64741.53 -66181.210 92142.17
## Dec 2007      9661.69 -44103.7470 63427.13 -72565.450 91888.83
## Jan 2008     11910.86 -43786.8821 67608.60 -73271.486 97093.21
## Feb 2008     11964.38 -45600.8416 69529.60 -76074.029 100002.79
## Mar 2008     10689.12 -48684.8726 70063.11 -80115.566 101493.81
## Apr 2008     15788.68 -45340.5868 76917.95 -77700.466 109277.83
## May 2008     13773.28 -49062.2475 76608.81 -82325.367 109871.93
```

```
#Forecast 5, Part 2: Testing Classic Cars Sales Forecast with manual ARIMA variables
```

```
#Building second Classic Cars model
```

```
CC2_model <-arima(Class_Car_sales,order = c(1,1,2), seasonal = list(order = c(1,1,1)))
```

```
#Print Manual Arima Model Summary
```

```
print(summary(CC2_model))
```

```
##
```

```
## Call:
```

```
## arima(x = Class_Car_sales, order = c(1, 1, 2), seasonal = list(order = c(1,
##      1, 1)))
```

```
##
```

```
## Coefficients:
```

```
## Warning in sqrt(diag(x$var.coef)): NaNs produced
```

```
##          ar1      ma1      ma2      sar1      sma1
```

```
##      -0.5019  0.0000 -0.9999 -0.6247 -0.6696
```

```
## s.e.   0.2367  0.5865  0.5864      NaN      NaN
```

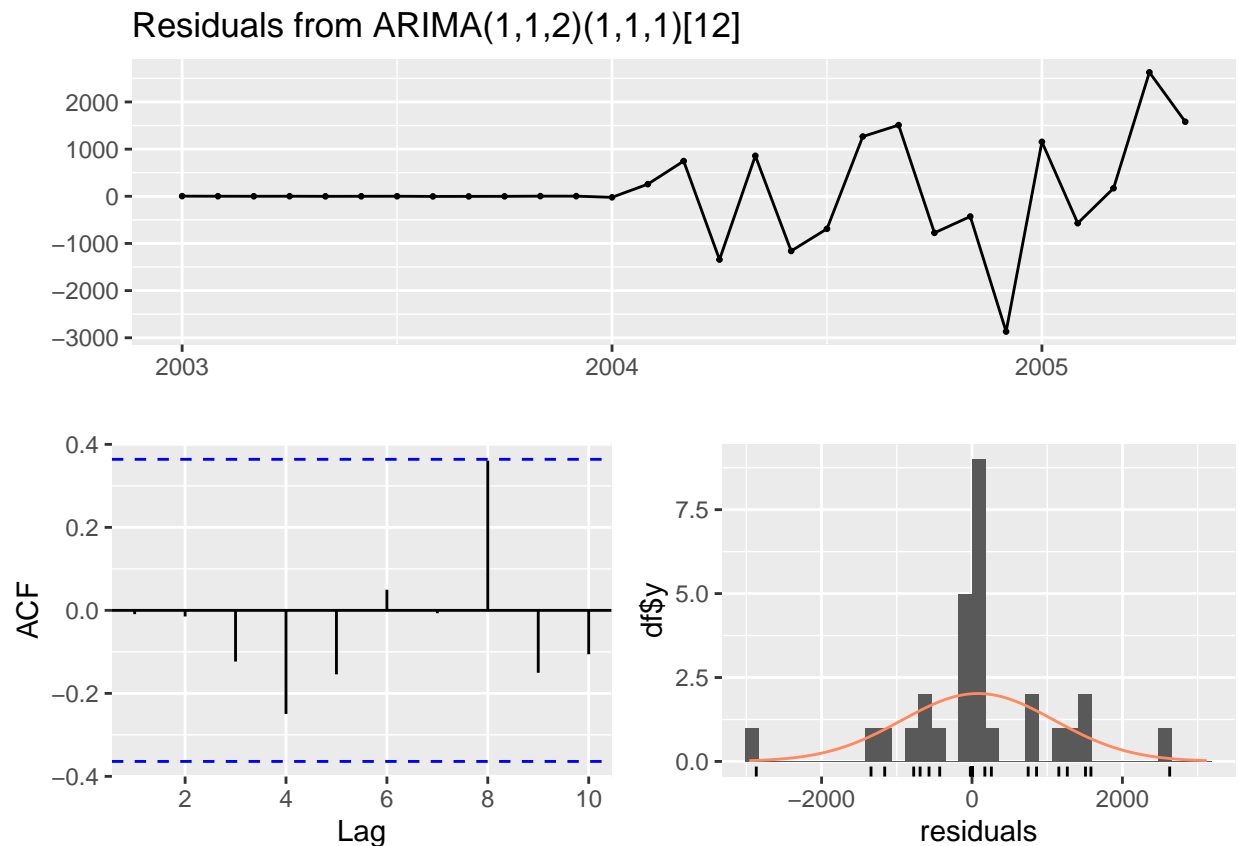
```
##
```

```
## sigma^2 estimated as 1811390: log likelihood = -148.88, aic = 309.76
```

```
##
```

```
## Training set error measures:
##           ME      RMSE      MAE      MPE      MAPE      MASE
## Training set 80.06016 999.7029 622.5583 -4.275056 17.21661 0.329219
##           ACF1
## Training set -0.009113655
```

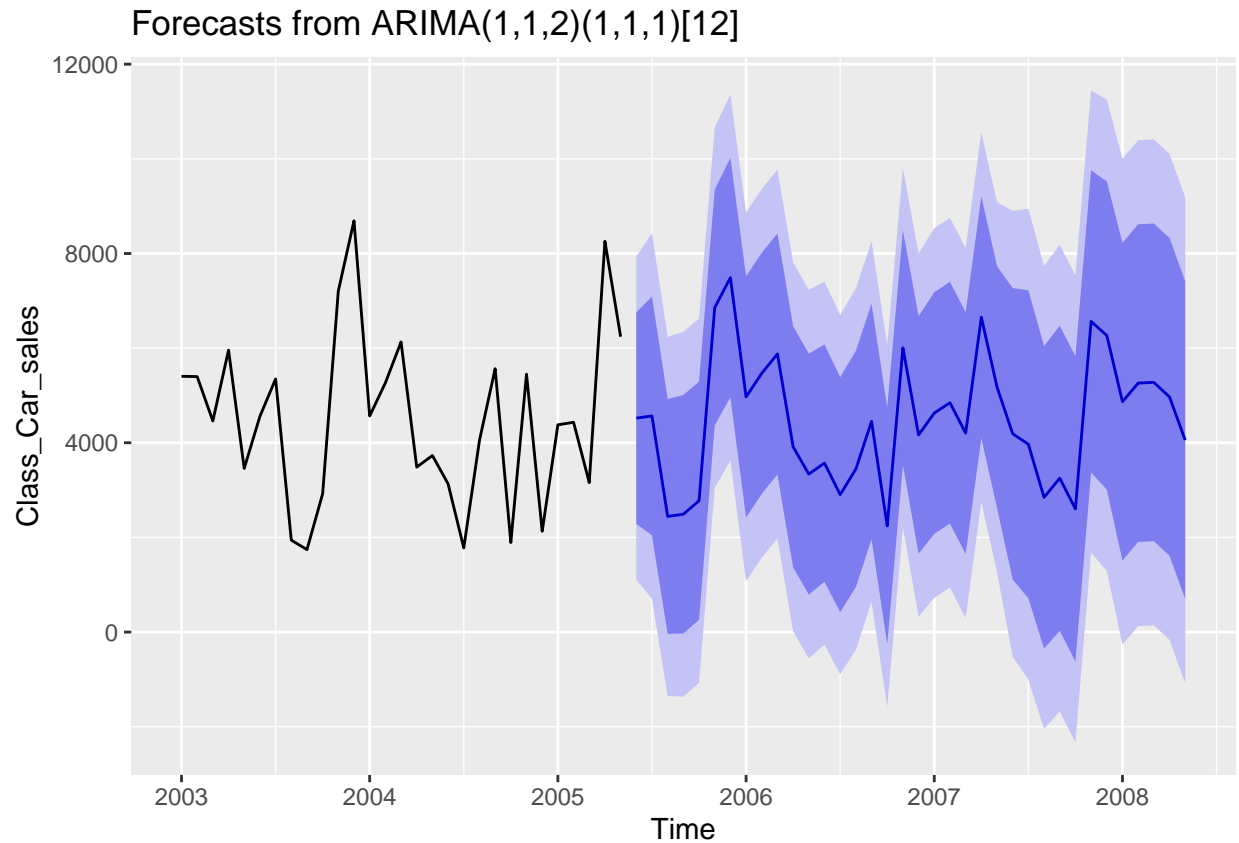
```
#Checking residual values of Manual Arima Model
checkresiduals(CC2_model)
```



```
##
## Ljung-Box test
##
## data: Residuals from ARIMA(1,1,2)(1,1,1)[12]
## Q* = 9.3368, df = 3, p-value = 0.02513
##
## Model df: 5. Total lags used: 8
```

```
#Create Forecast for Manual ARIMA Model
#Forecast for the next two years
CC2_Forecast <- forecast(CC2_model, h=36)
```

```
#Plot Forecast Results
#Showing the last 5 years
autoplot(CC2_Forecast, include = 60)
```



```
#Print Summary Forecast Results
print(summary(CC2_Forecast))
```

```
##
## Forecast method: ARIMA(1,1,2)(1,1,1)[12]
##
## Model Information:
##
## Call:
## arima(x = Class_Car_sales, order = c(1, 1, 2), seasonal = list(order = c(1,
##     1, 1)))
##
## Coefficients:

## Warning in sqrt(diag(x$var.coef)): NaNs produced

##          ar1      ma1      ma2      sar1      sma1
##       -0.5019  0.0000 -0.9999 -0.6247 -0.6696
## s.e.   0.2367  0.5865  0.5864      NaN      NaN
##
## sigma^2 estimated as 1811390:  log likelihood = -148.88,  aic = 309.76
##
## Error measures:
##              ME      RMSE      MAE      MPE      MAPE      MASE
## Training set 80.06016 999.7029 622.5583 -4.275056 17.21661 0.2865224
```

```
##                      ACF1
## Training set -0.009113655
##
## Forecasts:
##      Point Forecast      Lo 80      Hi 80      Lo 95      Hi 95
## Jun 2005      4520.653 2288.40668 6752.899 1106.72686 7934.579
## Jul 2005      4566.197 2041.61055 7090.783  705.17545 8427.218
## Aug 2005      2443.141 -37.32573 4923.608 -1350.40557 6236.688
## Sep 2005      2489.158 -30.37715 5008.692 -1364.13826 6342.453
## Oct 2005      2775.914 259.51880 5292.309 -1072.58035 6624.408
## Nov 2005      6856.534 4366.68813 9346.379 3048.64348 10664.424
## Dec 2005      7488.499 4960.03856 10016.960 3621.55230 11355.446
## Jan 2006      4969.094 2421.63814 7516.549 1073.09662 8865.091
## Feb 2006      5467.812 2921.76279 8013.862 1573.96553 9361.659
## Mar 2006      5877.323 3330.63057 8424.015 1982.49304 9772.153
## Apr 2006      3914.539 1368.03488 6461.043  19.99696 7809.081
## May 2006      3338.242  791.90916 5884.575 -556.03794 7232.522
## Jun 2006      3570.923 1064.60923 6077.236 -262.15302 7403.999
## Jul 2006      2904.338 422.84221 5385.835 -890.78252 6699.459
## Aug 2006      3445.724 948.77463 5942.673 -373.03044 7264.478
## Sep 2006      4450.499 1963.86164 6937.137  647.51516 8253.483
## Oct 2006      2243.259 -254.22094 4740.739 -1576.30699 6062.825
## Nov 2006      6006.880 3527.15261 8486.607 2214.46431 9799.295
## Dec 2006      4165.799 1657.47003 6674.128  329.64097 8001.957
## Jan 2007      4627.733 2074.48869 7180.977  722.88276 8532.583
## Feb 2007      4847.054 2293.45673 7400.651  941.66405 8752.444
## Mar 2007      4204.803 1651.40791 6758.198  299.72234 8109.883
## Apr 2007      6653.275 4099.72824 9206.823 2747.96201 10558.589
## May 2007      5178.188 2624.81886 7731.558 1273.14669 9083.230
## Jun 2007      4190.428 1110.27143 7270.585 -520.26504 8901.121
## Jul 2007      3968.725  715.23581 7222.214 -1007.05732 8944.507
## Aug 2007      2845.712 -349.71774 6041.143 -2041.27632 7732.701
## Sep 2007      3251.597  28.23774 6474.957 -1678.10570 8181.300
## Oct 2007      2602.259 -622.30298 5826.821 -2329.28286 7533.800
## Nov 2007      6563.900 3370.79067 9757.009 1680.46087 11447.338
## Dec 2007      6267.638 3012.25946 9523.016 1288.96637 11246.309
## Jan 2008      4867.240 1510.09257 8224.388 -267.07409 10001.555
## Feb 2008      5261.090 1904.87998 8617.301  128.20956 10393.971
## Mar 2008      5275.836 1919.21814 8632.453  142.33210 10409.339
## Apr 2008      4968.760 1612.21926 8325.301 -164.62628 10102.147
## May 2008      4055.114  698.78893 7411.439 -1077.94218 9188.170
```

```
#Forecast 6, Part 1: Forecasting with focus on Vintage Cars
```

```
#Sub-setting the data to only show sales in
```

```
Vintage_Car_Sales <- subset(salesdata2, PRODUCTLINE == "Vintage Cars")
head(Vintage_Car_Sales)
```

```
##      ORDERNUMBER QUANTITYORDERED PRICEEACH ORDERLINENUMBER  SALES  ORDERDATE
## 579          10100             30    100.00             3 5151.00 2003-01-06
## 681          10100             50     67.80             2 3390.00 2003-01-06
## 1268         10100             22     86.51             4 1903.22 2003-01-06
## 2025         10100             49     34.47             1 1689.03 2003-01-06
## 729          10101             25    100.00             4 3782.00 2003-01-09
```

```

## 831      10101      26      100.00      1 3773.38 2003-01-09
##      STATUS QTR_ID MONTH_ID YEAR_ID  PRODUCTLINE MSRP PRODUCTCODE
## 579 Shipped      1          1    2003 Vintage Cars   170    S18_1749
## 681 Shipped      1          1    2003 Vintage Cars    60    S18_2248
## 1268 Shipped     1          1    2003 Vintage Cars    92    S18_4409
## 2025 Shipped     1          1    2003 Vintage Cars    41    S24_3969
## 729 Shipped      1          1    2003 Vintage Cars   127    S18_2325
## 831 Shipped      1          1    2003 Vintage Cars   168    S18_2795
##
##      CUSTOMERNAME      PHONE      ADDRESSLINE1
## 579 Online Diecast Creations Co.      6035558647 2304 Long Airport Avenue
## 681 Online Diecast Creations Co.      6035558647 2304 Long Airport Avenue
## 1268 Online Diecast Creations Co.      6035558647 2304 Long Airport Avenue
## 2025 Online Diecast Creations Co.      6035558647 2304 Long Airport Avenue
## 729      Blauer See Auto, Co. +49 69 66 90 2555      Lyonerstr. 34
## 831      Blauer See Auto, Co. +49 69 66 90 2555      Lyonerstr. 34
##      ADDRESSLINE2      CITY STATE POSTALCODE COUNTRY TERRITORY CONTACTLASTNAME
## 579      Nashua      NH      62005      USA      <NA>      Young
## 681      Nashua      NH      62005      USA      <NA>      Young
## 1268      Nashua      NH      62005      USA      <NA>      Young
## 2025      Nashua      NH      62005      USA      <NA>      Young
## 729      Frankfurt      60528 Germany      EMEA      Keitel
## 831      Frankfurt      60528 Germany      EMEA      Keitel
##      CONTACTFIRSTNAME DEALSIZE
## 579      Valarie      Medium
## 681      Valarie      Medium
## 1268      Valarie      Small
## 2025      Valarie      Small
## 729      Roland      Medium
## 831      Roland      Medium

```

#Creating Time Series

```

Vintage_Car_sales <- ts(Vintage_Car_Sales[,5], start = c(2003,1), end = c(2005,5), frequency = 12)
Vintage_Car_sales

```

```

##      Jan      Feb      Mar      Apr      May      Jun      Jul      Aug      Sep
## 2003 5151.00 3390.00 1903.22 1689.03 3782.00 3773.38 1404.00 2472.96 4808.31
## 2004 2539.50 4791.82 1938.89 2873.00 3065.04 3382.50 3193.52 3983.50 4774.86
## 2005 6069.00 1608.00 3859.68 5074.39 2499.56
##      Oct      Nov      Dec
## 2003 2055.74 2242.89 2011.10
## 2004 1630.60 2406.36 1565.85
## 2005

```

#Build Fit Arima Model

#Taking first differnce of the data

#Getting rid of seasonality by taking first seasonal difference

```

Vintage_AR_Model <- auto.arima(Vintage_Car_sales, d=1, D=1, stepwise = FALSE, approximation = FALSE, tr

```

```

##
## ARIMA(0,1,0)(0,1,0)[12]      : 301.7281
## ARIMA(0,1,1)(0,1,0)[12]      : Inf
## ARIMA(0,1,2)(0,1,0)[12]      : Inf

```



```
## ARIMA(0,1,3)(0,1,0)[12] : Inf
## ARIMA(0,1,4)(0,1,0)[12] : Inf
## ARIMA(0,1,5)(0,1,0)[12] : Inf
## ARIMA(1,1,0)(0,1,0)[12] : 296.6916
## ARIMA(1,1,1)(0,1,0)[12] : Inf
## ARIMA(1,1,2)(0,1,0)[12] : Inf
## ARIMA(1,1,3)(0,1,0)[12] : Inf
## ARIMA(1,1,4)(0,1,0)[12] : Inf
## ARIMA(2,1,0)(0,1,0)[12] : 294.7644
## ARIMA(2,1,1)(0,1,0)[12] : Inf
## ARIMA(2,1,2)(0,1,0)[12] : Inf
## ARIMA(2,1,3)(0,1,0)[12] : Inf
## ARIMA(3,1,0)(0,1,0)[12] : 296.068
## ARIMA(3,1,1)(0,1,0)[12] : Inf
## ARIMA(3,1,2)(0,1,0)[12] : Inf
## ARIMA(4,1,0)(0,1,0)[12] : 295.9752
## ARIMA(4,1,1)(0,1,0)[12] : 299.8898
## ARIMA(5,1,0)(0,1,0)[12] : 300.1159
##
##
##
## Best model: ARIMA(2,1,0)(0,1,0)[12]
```

#Printing AR Model Summary

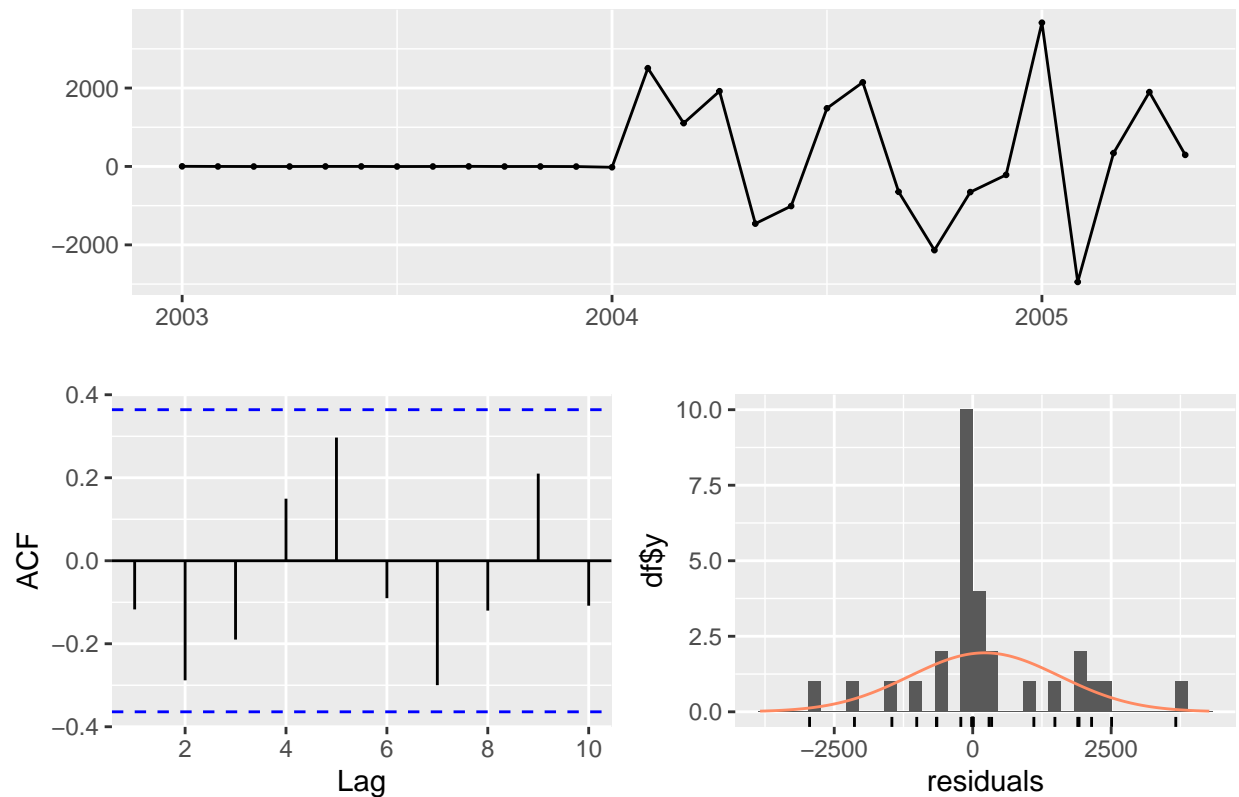
```
print(summary(Vintage_AR_Model))
```

```
## Series: Vintage_Car_sales
## ARIMA(2,1,0)(0,1,0)[12]
##
## Coefficients:
##          ar1      ar2
##      -1.0311  -0.5432
## s.e.   0.2239   0.2110
##
## sigma^2 = 3751904: log likelihood = -143.38
## AIC=292.76  AICc=294.76  BIC=295.08
##
## Training set error measures:
##              ME      RMSE      MAE      MPE      MAPE      MASE      ACF1
## Training set 216.3675 1345.832 843.5712 -1.800827 29.04654 0.6486324 -0.117224
```

#Checking Residuals of AR_Model

```
checkresiduals(Vintage_AR_Model)
```

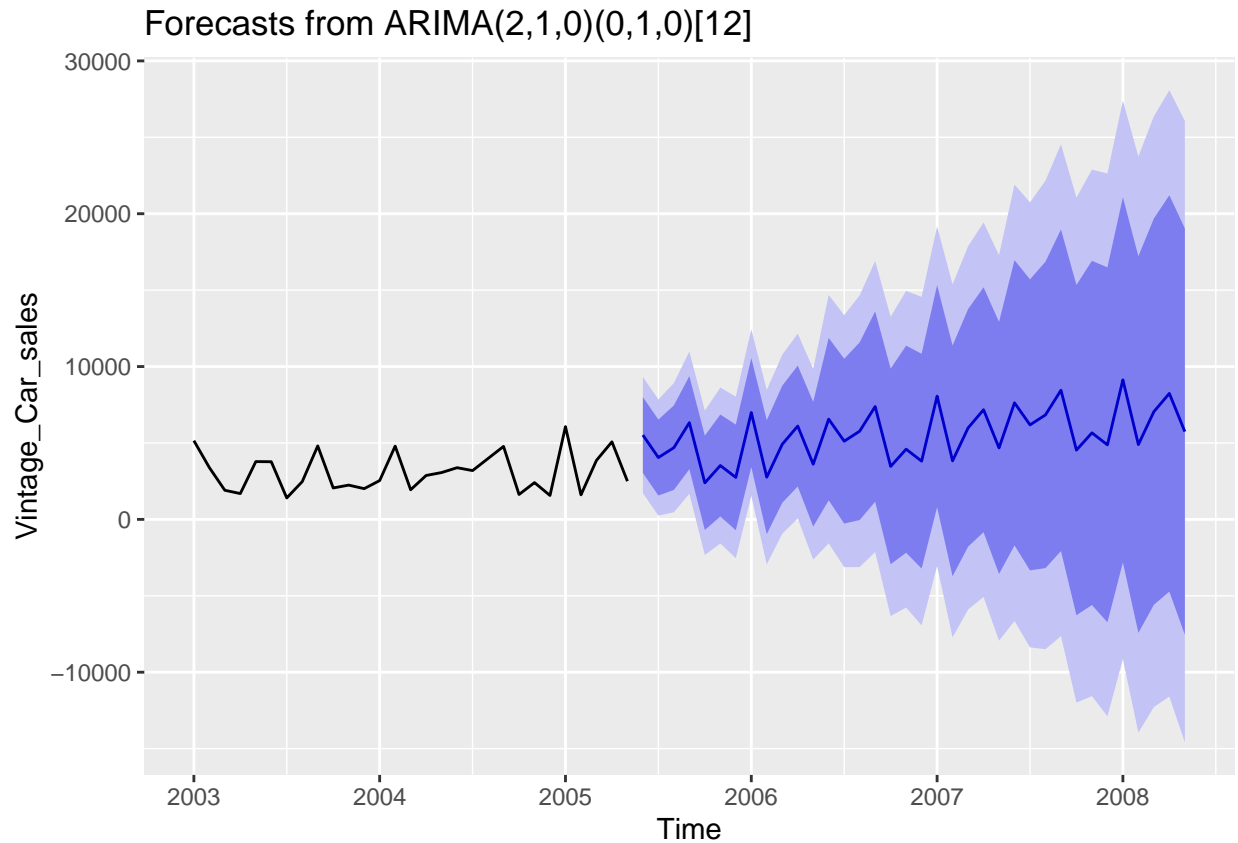
Residuals from ARIMA(2,1,0)(0,1,0)[12]



```
##
##  Ljung-Box test
##
## data:  Residuals from ARIMA(2,1,0)(0,1,0)[12]
## Q* = 8.8744, df = 4, p-value = 0.06432
##
## Model df: 2.   Total lags used: 6

#Forecasting ARIMA Model
#forecast two years ahead
VC_AR_Model_Forecast <- forecast(Vintage_AR_Model, h=36)

#Plotting AR Model Forecast
#including the last 5 years
autoplot(VC_AR_Model_Forecast, include = 60)
```



```
#Print Summary of AR Model Forecast
print(summary(VC_AR_Model_Forecast))
```

```
##
## Forecast method: ARIMA(2,1,0)(0,1,0)[12]
##
## Model Information:
## Series: Vintage_Car_sales
## ARIMA(2,1,0)(0,1,0)[12]
##
## Coefficients:
##          ar1      ar2
##       -1.0311  -0.5432
## s.e.    0.2239   0.2110
##
## sigma^2 = 3751904:  log likelihood = -143.38
## AIC=292.76   AICc=294.76   BIC=295.08
##
## Error measures:
##              ME      RMSE      MAE      MPE      MAPE      MASE      ACF1
## Training set 216.3675 1345.832 843.5712 -1.800827 29.04654 0.6486324 -0.117224
##
## Forecasts:
##      Point Forecast      Lo 80      Hi 80      Lo 95      Hi 95
## Jun 2005      5517.533  3035.18915  7999.877  1721.11564  9313.951
## Jul 2005      4046.962  1563.41799  6530.507   248.70899  7845.216
```

## Aug 2005	4691.521	1927.32338	7455.718	464.04573	8918.996
## Sep 2005	6328.965	3285.74520	9372.185	1674.76203	10983.168
## Oct 2005	2391.295	-694.46251	5477.052	-2327.96379	7110.554
## Nov 2005	3525.564	190.80022	6860.327	-1574.51698	8625.645
## Dec 2005	2746.361	-708.04143	6200.764	-2536.69177	8029.414
## Jan 2006	6991.561	3430.19992	10552.921	1544.92943	12438.192
## Feb 2006	2763.233	-964.02038	6490.487	-2937.10930	8463.576
## Mar 2006	4915.118	1085.84800	8744.388	-941.24522	10771.482
## Apr 2006	6106.343	2153.72290	10058.964	61.33204	12151.355
## May 2006	3609.936	-466.04868	7685.920	-2623.74452	9843.616
## Jun 2006	6559.804	1247.85290	11871.755	-1564.12404	14683.732
## Jul 2006	5116.859	-272.78180	10506.499	-3125.88514	13359.603
## Aug 2006	5769.926	-41.74889	11581.600	-3118.26355	14658.115
## Sep 2006	7383.591	1159.64732	13607.534	-2135.10930	16902.291
## Oct 2006	3465.818	-2933.26090	9864.896	-6320.72850	13252.364
## Nov 2006	4592.487	-2181.27311	11366.248	-5767.08523	14952.060
## Dec 2006	3810.313	-3215.85261	10836.478	-6935.27990	14555.905
## Jan 2007	8062.704	801.23441	15324.174	-3042.75561	19168.164
## Feb 2007	3828.575	-3719.53293	11376.684	-7715.26012	15372.411
## Mar 2007	5982.536	-1787.62509	13752.697	-5900.89975	17865.971
## Apr 2007	7174.772	-834.85029	15184.395	-5074.88832	19424.433
## May 2007	4676.194	-3569.40945	12921.798	-7934.36851	17286.757
## Jun 2007	7627.751	-1705.07038	16960.572	-6645.56749	21901.069
## Jul 2007	6184.244	-3335.16481	15703.652	-8374.43529	20742.923
## Aug 2007	6836.973	-3186.48051	16860.427	-8492.57633	22166.523
## Sep 2007	8451.292	-2068.17528	18970.758	-7636.84462	24539.428
## Oct 2007	4533.028	-6268.16327	15334.220	-11985.96864	21052.025
## Nov 2007	5659.848	-5601.44788	16921.145	-11562.81801	22882.515
## Dec 2007	4877.785	-6733.81057	16489.380	-12880.61791	22636.188
## Jan 2008	9129.980	-2813.91294	21073.873	-9136.62808	27396.589
## Feb 2008	4895.993	-7424.94315	17216.930	-13947.25296	23739.240
## Mar 2008	7049.914	-5587.07116	19686.899	-12276.68689	26376.514
## Apr 2008	8242.114	-4725.18182	21209.410	-11589.65370	28073.882
## May 2008	5743.595	-7549.03063	19036.221	-14585.72176	26072.912

```
#Forecast 6, Part 2: Testing Vintage Cars Sales Forecast with manual ARIMA variables
```

```
#Building second Vintage Cars model
```

```
Vintage2_model <-arima(Vintage_Car_sales,order = c(1,1,2), seasonal = list(order = c(1,1,1)))
```

```
#Print Manual Arima Model Summary
```

```
print(summary(Vintage2_model))
```

```
##
```

```
## Call:
```

```
## arima(x = Vintage_Car_sales, order = c(1, 1, 2), seasonal = list(order = c(1,  
##      1, 1)))
```

```
##
```

```
## Coefficients:
```

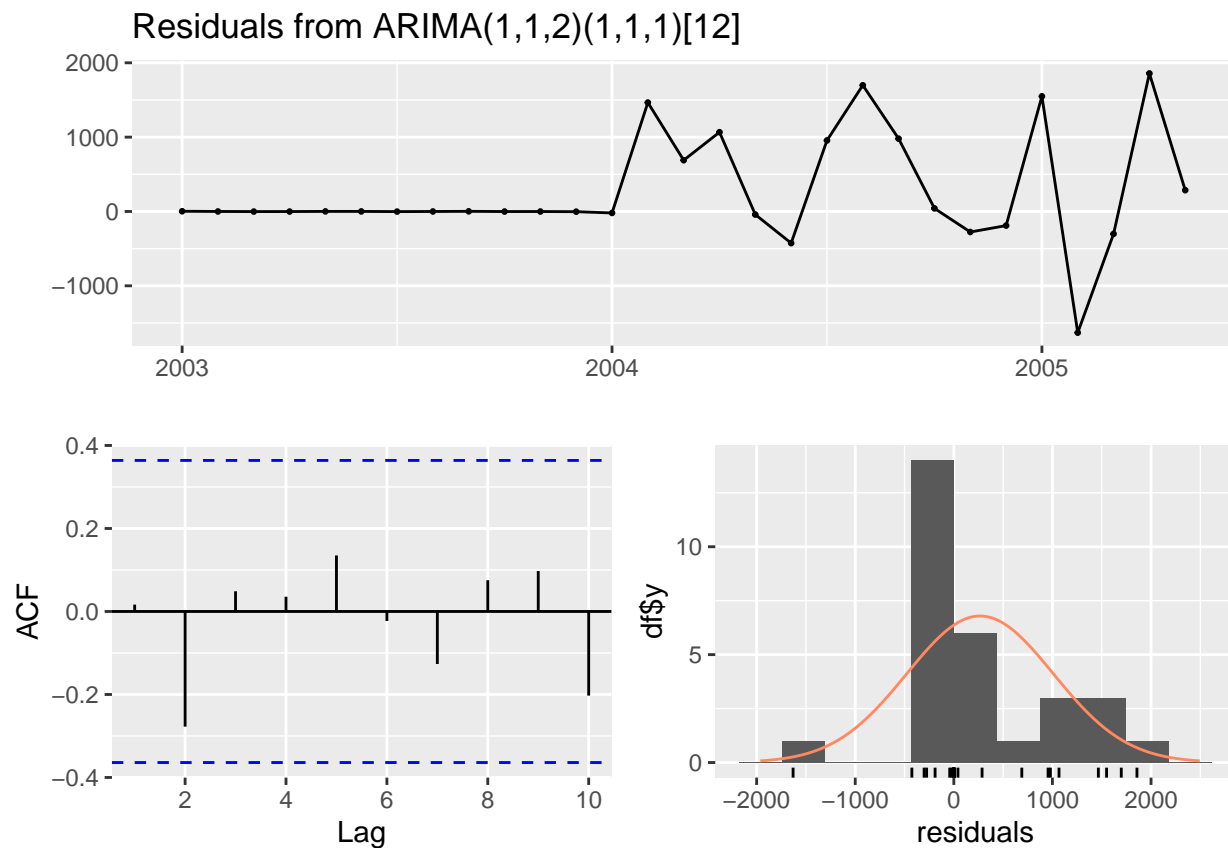
```
## Warning in sqrt(diag(x$var.coef)): NaNs produced
```

```
##          ar1          ma1          ma2          sar1          sma1
```

```
##      -0.0308  -1.9180  1.0000  -0.2229  -0.2796
## s.e.   0.2637   0.2237  0.2277      NaN      NaN
##
## sigma^2 estimated as 1093447:  log likelihood = -138.47,  aic = 288.95
##
## Training set error measures:
##              ME      RMSE      MAE      MPE      MAPE      MASE      ACF1
## Training set 265.599 776.7214 465.1846 4.297413 14.50478 0.3020522 0.01653682
```

```
#Checking residual values of Manual Arima Model
```

```
checkresiduals(Vintage2_model)
```



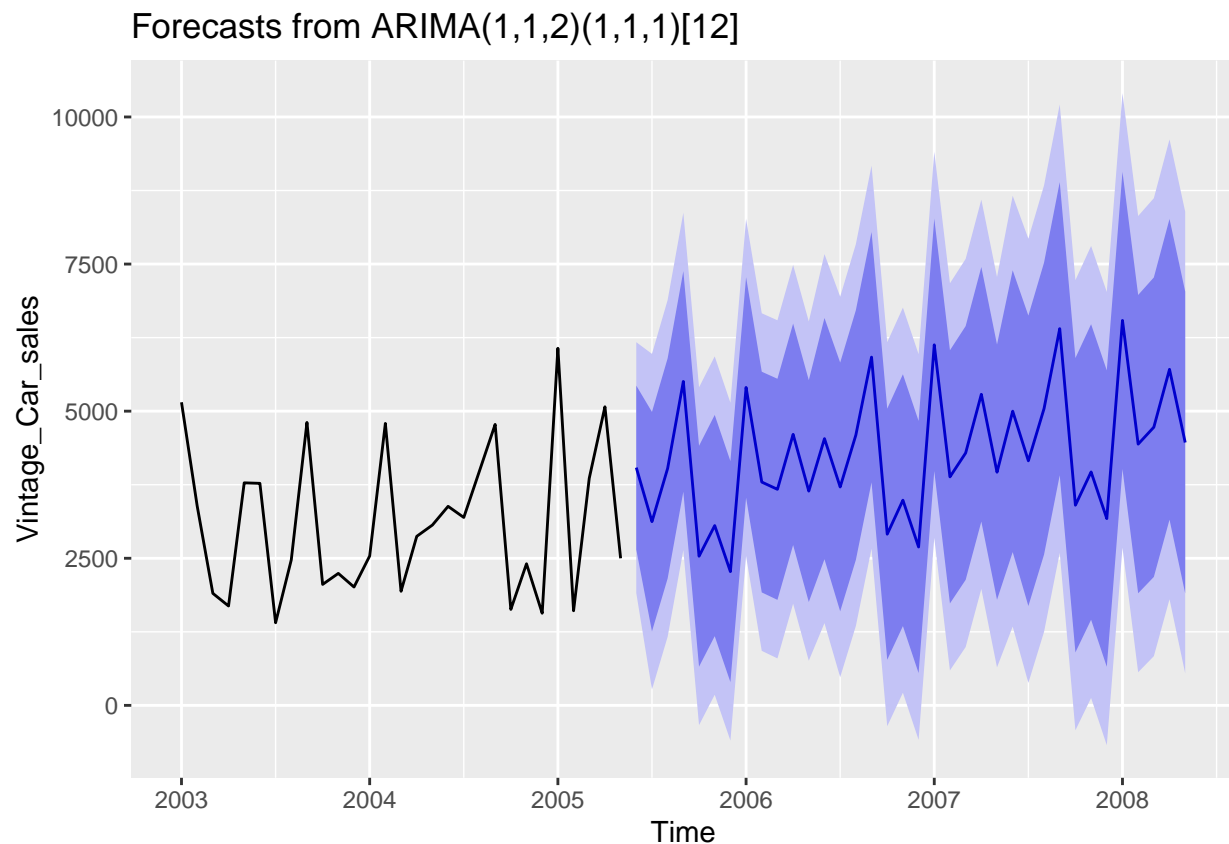
```
##
## Ljung-Box test
##
## data: Residuals from ARIMA(1,1,2)(1,1,1)[12]
## Q* = 4.2998, df = 3, p-value = 0.2309
##
## Model df: 5. Total lags used: 8
```

```
#Create Forecast for Manual ARIMA Model
```

```
#Forecast for the next two years
```

```
Vintage2_Forecast <- forecast(Vintage2_model, h=36)
```

```
#Plot Forecast Results
#Showing the last 5 years
autoplot(Vintage2_Forecast, include = 60)
```



```
#Print Summary Forecast Results
print(summary(Vintage2_Forecast))
```

```
##
## Forecast method: ARIMA(1,1,2)(1,1,1)[12]
##
## Model Information:
##
## Call:
## arima(x = Vintage_Car_sales, order = c(1, 1, 2), seasonal = list(order = c(1,
##     1, 1)))
##
## Coefficients:

## Warning in sqrt(diag(x$var.coef)): NaNs produced

##      ar1      ma1      ma2      sar1      sma1
##    -0.0308 -1.9180  1.0000 -0.2229 -0.2796
## s.e.  0.2637  0.2237  0.2277      NaN      NaN
##
```

```
## sigma^2 estimated as 1093447: log likelihood = -138.47, aic = 288.95
##
## Error measures:
##           ME      RMSE      MAE      MPE      MAPE      MASE      ACF1
## Training set 265.599 776.7214 465.1846 4.297413 14.50478 0.3576862 0.01653682
##
## Forecasts:
##           Point Forecast      Lo 80      Hi 80      Lo 95      Hi 95
## Jun 2005      4040.939 2647.5298 5434.349 1909.9034 6171.975
## Jul 2005      3121.903 1257.3036 4986.502  270.2443 5973.562
## Aug 2005      4028.379 2157.8169 5898.941 1167.6011 6889.157
## Sep 2005      5505.162 3631.5922 7378.732 2639.7842 8370.540
## Oct 2005      2534.520  657.8699 4411.170 -335.5687 5404.608
## Nov 2005      3055.589 1175.9191 4935.259  180.8820 5930.296
## Dec 2005      2273.210  396.2169 4150.202 -597.4031 5143.822
## Jan 2006      5403.052 3530.5707 7275.533 2539.3389 8266.765
## Feb 2006      3795.064 1919.5501 5670.577  926.7131 6663.414
## Mar 2006      3671.656 1793.1150 5550.197  798.6754 6544.637
## Apr 2006      4606.469 2724.9055 6488.033 1728.8658 7484.073
## May 2006      3641.452 1756.8707 5526.034  759.2334 6523.671
## Jun 2006      4533.574 2483.7992 6583.349 1398.7139 7668.434
## Jul 2006      3711.913 1598.3579 5825.467  479.5096 6944.315
## Aug 2006      4594.434 2473.0855 6715.782 1350.1116 7838.756
## Sep 2006      5918.383 3790.9975 8045.769 2664.8275 9171.939
## Oct 2006      2909.046  775.5891 5042.503 -353.7946 6171.886
## Nov 2006      3486.882 1347.3989 5626.365  214.8250 6758.939
## Dec 2006      2691.546  549.1418 4833.951 -584.9786 5968.071
## Jan 2007      6127.481 3982.8059 8272.155 2847.4838 9407.477
## Feb 2007      3883.594 1732.9855 6034.202  594.5222 7172.666
## Mar 2007      4289.562 2133.0361 6446.088  991.4403 7587.683
## Apr 2007      5286.760 3124.3333 7449.187 1979.6136 8593.907
## May 2007      3962.937 1794.6251 6131.249  646.7900 7279.085
## Jun 2007      4999.770 2606.0896 7393.450 1338.9518 8660.588
## Jul 2007      4156.405 1688.7065 6624.103  382.3858 7930.424
## Aug 2007      5044.265 2563.7901 7524.741 1250.7058 8837.825
## Sep 2007      6402.279 3911.6019 8892.957 2593.1169 10211.442
## Oct 2007      3401.567  900.6551 5902.478 -423.2475 7226.381
## Nov 2007      3966.750 1455.6719 6477.828  126.3873 7807.113
## Dec 2007      3174.302  656.1203 5692.484 -676.9246 7025.529
## Jan 2008      6542.013 4017.1643 9066.861 2680.5903 10403.435
## Feb 2008      4439.859 1905.0404 6974.678  563.1883 8316.530
## Mar 2008      4727.837 2183.0861 7272.587  835.9766 8619.696
## Apr 2008      5711.130 3156.4868 8265.773 1804.1403 9618.120
## May 2008      4467.280 1902.7822 7031.778  545.2189 8389.341
```

```
#Forecast 7, Part 1: Forecasting with focus on Ireland
```

```
#Sub-setting the data to only show sales in Ireland
```

```
Ireland_Sales <- subset(salesdata2, COUNTRY == "Ireland")
head(Ireland_Sales)
```

```
##           ORDERNUMBER QUANTITYORDERED PRICEEACH ORDERLINENUMBER  SALES  ORDERDATE
## 197           10220           32      100.00           2 7181.44 2004-02-12
## 277           10220           30      100.00           3 4713.60 2004-02-12
```

```

## 327      10220      27      100.00      1 5045.22 2004-02-12
## 1252     10220      50      100.00      5 8258.00 2004-02-12
## 1449     10220      26       56.07      8 1457.82 2004-02-12
## 2057     10220      37      100.00      7 5032.74 2004-02-12
##      STATUS QTR_ID MONTH_ID YEAR_ID  PRODUCTLINE MSRP PRODUCTCODE
## 197  Shipped      1        2    2004 Classic Cars  207    S12_1108
## 277  Shipped      1        2    2004 Classic Cars  151    S12_3148
## 327  Shipped      1        2    2004 Classic Cars  173    S12_3891
## 1252 Shipped      1        2    2004 Classic Cars  143    S18_4027
## 1449 Shipped      1        2    2004 Classic Cars   57    S24_1444
## 2057 Shipped      1        2    2004 Classic Cars  118    S24_4048
##      CUSTOMERNAME      PHONE  ADDRESSLINE1 ADDRESSLINE2  CITY
## 197  Clover Collections, Co. +353 1862 1555 25 Maiden Lane  Floor No. 4 Dublin
## 277  Clover Collections, Co. +353 1862 1555 25 Maiden Lane  Floor No. 4 Dublin
## 327  Clover Collections, Co. +353 1862 1555 25 Maiden Lane  Floor No. 4 Dublin
## 1252 Clover Collections, Co. +353 1862 1555 25 Maiden Lane  Floor No. 4 Dublin
## 1449 Clover Collections, Co. +353 1862 1555 25 Maiden Lane  Floor No. 4 Dublin
## 2057 Clover Collections, Co. +353 1862 1555 25 Maiden Lane  Floor No. 4 Dublin
##      STATE POSTALCODE COUNTRY TERRITORY CONTACTLASTNAME CONTACTFIRSTNAME
## 197      2 Ireland      EMEA      Cassidy      Dean
## 277      2 Ireland      EMEA      Cassidy      Dean
## 327      2 Ireland      EMEA      Cassidy      Dean
## 1252     2 Ireland      EMEA      Cassidy      Dean
## 1449     2 Ireland      EMEA      Cassidy      Dean
## 2057     2 Ireland      EMEA      Cassidy      Dean
##      DEALSIZE
## 197      Large
## 277      Medium
## 327      Medium
## 1252     Large
## 1449     Small
## 2057     Medium

```

```

#Creating Time Series
Ireland_sales <- ts(Ireland_Sales[,5], start = c(2003,1), end = c(2005,5), frequency = 12)
Ireland_sales

```

```

##      Jan      Feb      Mar      Apr      May      Jun      Jul      Aug      Sep
## 2003 7181.44 4713.60 5045.22 8258.00 1457.82 5032.74 1056.40 3983.05 2056.20
## 2004 1666.35 2856.88 2234.40 3986.50 7181.44 4713.60 5045.22 8258.00 1457.82
## 2005 2056.20 2069.75 4061.76 2096.32 1666.35
##      Oct      Nov      Dec
## 2003 2069.75 4061.76 2096.32
## 2004 5032.74 1056.40 3983.05
## 2005

```

```

#Build Fit Arima Model
#Taking first differnce of the data
#Getting rid of seasonality by taking first seasonal difference

Ireland_AR_Model <- auto.arima(Ireland_sales, d=1, D=1, stepwise = FALSE, approximation = FALSE, trace = FALSE)

##

```



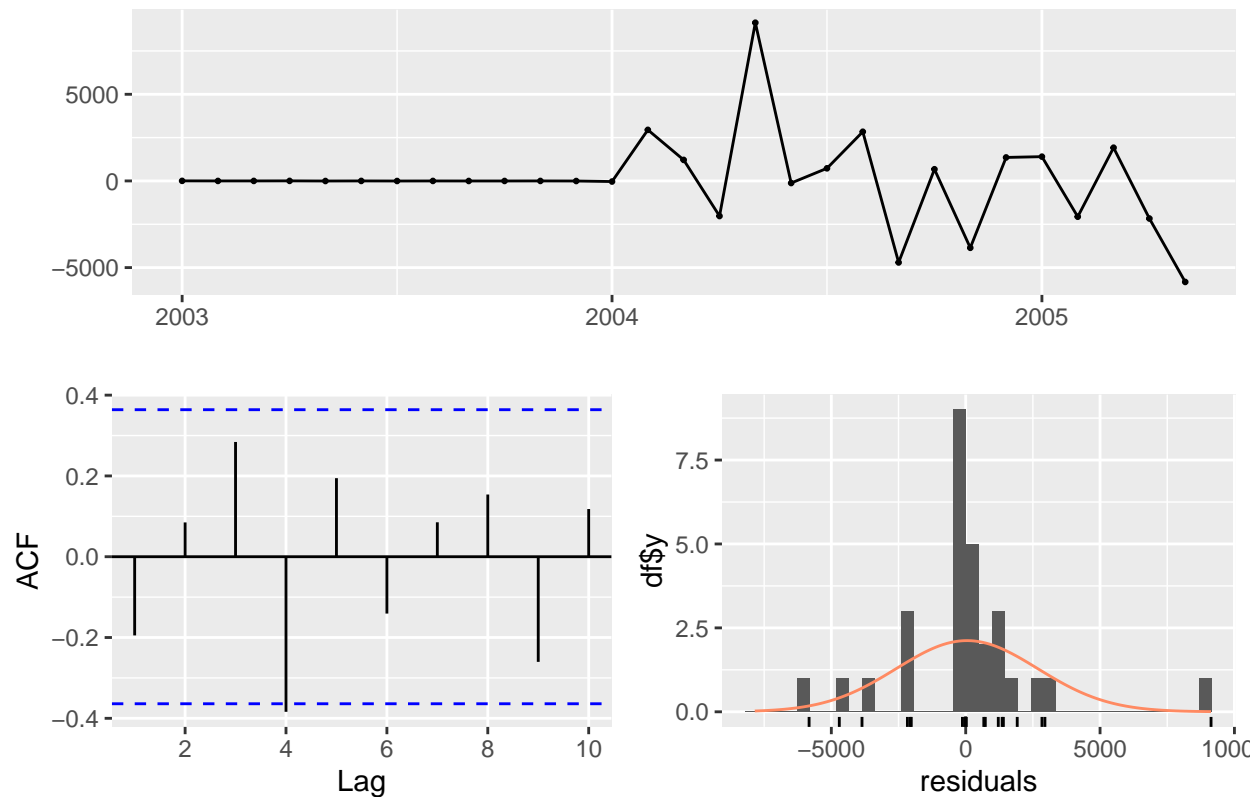
```
## ARIMA(0,1,0)(0,1,0)[12] : 315.8979
## ARIMA(0,1,1)(0,1,0)[12] : 312.4617
## ARIMA(0,1,2)(0,1,0)[12] : Inf
## ARIMA(0,1,3)(0,1,0)[12] : Inf
## ARIMA(0,1,4)(0,1,0)[12] : Inf
## ARIMA(0,1,5)(0,1,0)[12] : Inf
## ARIMA(1,1,0)(0,1,0)[12] : 311.7407
## ARIMA(1,1,1)(0,1,0)[12] : 314.0416
## ARIMA(1,1,2)(0,1,0)[12] : Inf
## ARIMA(1,1,3)(0,1,0)[12] : Inf
## ARIMA(1,1,4)(0,1,0)[12] : Inf
## ARIMA(2,1,0)(0,1,0)[12] : 312.798
## ARIMA(2,1,1)(0,1,0)[12] : 313.0919
## ARIMA(2,1,2)(0,1,0)[12] : Inf
## ARIMA(2,1,3)(0,1,0)[12] : Inf
## ARIMA(3,1,0)(0,1,0)[12] : 312.7271
## ARIMA(3,1,1)(0,1,0)[12] : 316.2446
## ARIMA(3,1,2)(0,1,0)[12] : Inf
## ARIMA(4,1,0)(0,1,0)[12] : 315.0883
## ARIMA(4,1,1)(0,1,0)[12] : 319.7976
## ARIMA(5,1,0)(0,1,0)[12] : 319.5299
##
##
## Best model: ARIMA(1,1,0)(0,1,0)[12]
```

```
#Printing AR Model Summary
print(summary(Ireland_AR_Model))
```

```
## Series: Ireland_sales
## ARIMA(1,1,0)(0,1,0)[12]
##
## Coefficients:
##          ar1
##        -0.5924
## s.e.    0.1960
##
## sigma^2 = 12938952: log likelihood = -153.41
## AIC=310.82 AICc=311.74 BIC=312.36
##
## Training set error measures:
##              ME      RMSE      MAE      MPE      MAPE      MASE      ACF1
## Training set 48.03123 2586.999 1483.938 -27.62018 61.84773 0.5297139 -0.1947669
```

```
#Checking Residuals of AR_Model
checkresiduals(Ireland_AR_Model)
```

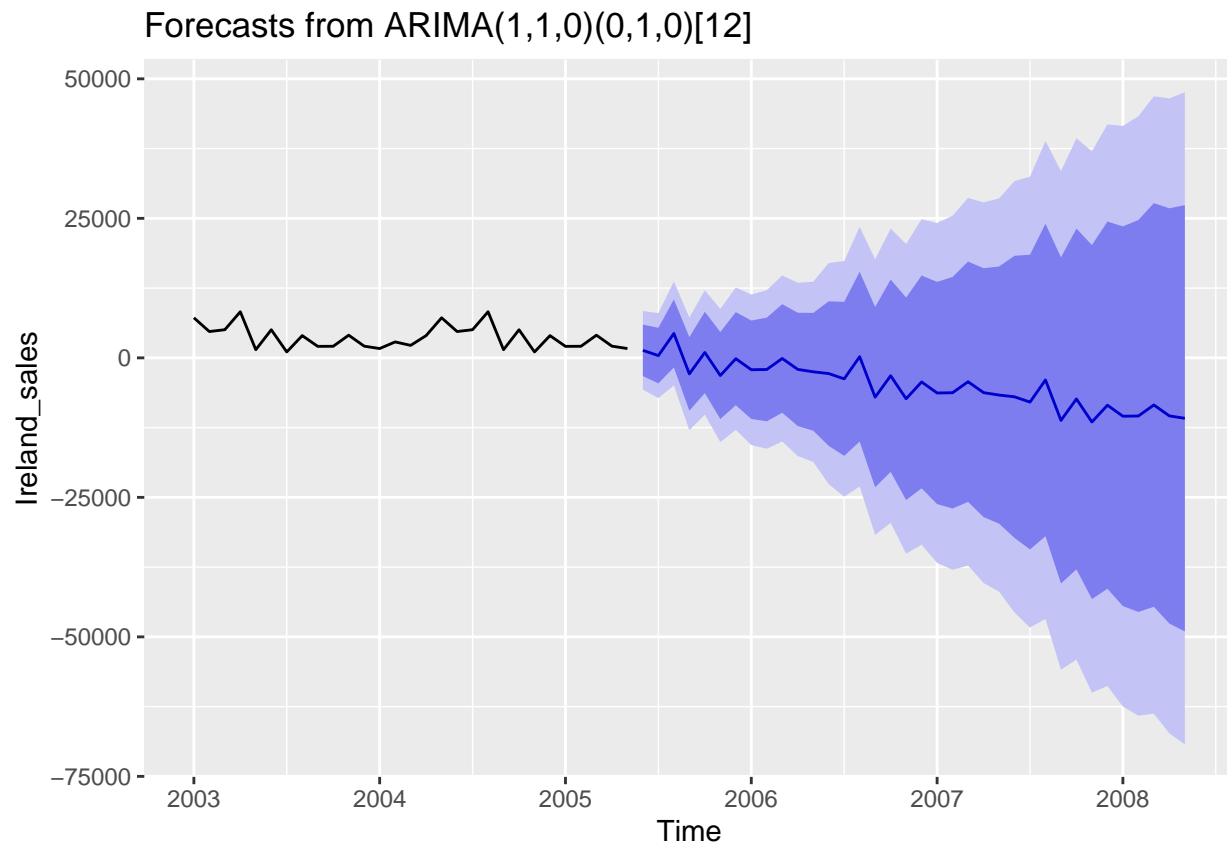
Residuals from ARIMA(1,1,0)(0,1,0)[12]



```
##
##  Ljung-Box test
##
## data:  Residuals from ARIMA(1,1,0)(0,1,0)[12]
## Q* = 11.739, df = 5, p-value = 0.03855
##
## Model df: 1.   Total lags used: 6
```

```
#Forecasting ARIMA Model
#forecast two years ahead
IR_AR_Model_Forecast <- forecast(Ireland_AR_Model, h=36)
```

```
#Plotting AR Model Forecast
#including the last 5 years
autoplot(IR_AR_Model_Forecast, include = 60)
```



```
#Print Summary of AR Model Forecast
print(summary(IR_AR_Model_Forecast))
```

```
##
## Forecast method: ARIMA(1,1,0)(0,1,0)[12]
##
## Model Information:
## Series: Ireland_sales
## ARIMA(1,1,0)(0,1,0)[12]
##
## Coefficients:
##      ar1
##      -0.5924
## s.e.    0.1960
##
## sigma^2 = 12938952:  log likelihood = -153.41
## AIC=310.82   AICc=311.74   BIC=312.36
##
## Error measures:
##              ME      RMSE      MAE      MPE      MAPE      MASE      ACF1
## Training set 48.03123 2586.999 1483.938 -27.62018 61.84773 0.5297139 -0.1947669
##
## Forecasts:
##      Point Forecast      Lo 80      Hi 80      Lo 95      Hi 95
## Jun 2005      1345.9355 -3263.902  5955.773 -5704.203  8396.074
## Jul 2005       405.4036 -4572.648  5383.455 -7207.869  8018.676
```

```
## Aug 2005      4371.8164 -1711.620 10455.253 -4931.997 13675.630
## Sep 2005     -2874.8217 -9466.587  3716.944 -12956.057  7206.414
## Oct 2005       964.5837 -6322.340  8251.508 -10179.805 12108.972
## Nov 2005     -3168.4395 -10964.003  4627.124 -15090.725  8753.846
## Dec 2005      -148.9692 -8490.782  8192.844 -12906.671 12608.733
## Jan 2006     -2130.8067 -10946.354  6684.741 -15613.024 11351.410
## Feb 2006     -2084.6816 -11371.529  7202.166 -16287.689 12118.326
## Mar 2006      -111.9694 -9834.978  9611.040 -14982.029 14758.090
## Apr 2006     -2065.9772 -12213.401  8081.446 -17585.123 13453.168
## May 2006     -2502.7197 -13053.515  8048.076 -18638.769 13633.329
## Jun 2006     -2819.1222 -15768.572 10130.327 -22623.596 16985.352
## Jul 2006     -3762.0309 -17562.736 10038.674 -24868.388 17344.326
## Aug 2006       205.7900 -15003.639 15415.220 -23055.025 23466.605
## Sep 2006     -7041.6822 -23192.207  9108.842 -31741.778 17658.413
## Oct 2006     -3201.7827 -20431.294 14027.728 -29552.046 23148.481
## Nov 2006     -7335.0987 -25471.845 10801.648 -35072.859 20402.661
## Dec 2006     -4315.4549 -23376.632 14745.722 -33467.010 24836.100
## Jan 2007     -6297.3951 -26205.745 13610.955 -36744.589 24149.799
## Feb 2007     -6251.2092 -26991.660 14489.242 -37970.992 25468.574
## Mar 2007     -4278.5330 -25807.797 17250.731 -37204.701 28647.635
## Apr 2007     -6232.5195 -28529.081 16064.042 -40332.167 27867.128
## May 2007     -6669.2746 -29703.930 16365.381 -41897.740 28559.191
## Jun 2007     -6985.6696 -32260.439 18289.100 -45640.094 31668.755
## Jul 2007     -7928.5827 -34340.584 18483.419 -48322.253 32465.088
## Aug 2007     -3960.7592 -31958.153 24036.635 -46779.078 38857.560
## Sep 2007    -11208.2330 -40417.826 18001.360 -55880.451 33463.985
## Oct 2007     -7368.3326 -37902.641 23165.976 -54066.527 39329.862
## Nov 2007    -11501.6491 -43212.932 20209.634 -59999.871 36996.573
## Dec 2007     -8482.0050 -41380.700 24416.690 -58796.217 41832.208
## Jan 2008    -10463.9454 -44478.430 23550.539 -62484.610 41556.719
## Feb 2008    -10417.7594 -45529.890 24694.372 -64117.130 43281.611
## Mar 2008     -8445.0832 -44611.601 27721.435 -63757.000 46866.833
## Apr 2008    -10399.0697 -47595.833 26797.694 -67286.610 46488.471
## May 2008    -10835.8249 -49031.746 27360.096 -69251.445 47579.795
```

```
#Forecast 7, Part 2: Testing Ireland Sales Forecast with manual ARIMA variables
```

```
#Building second Ireland model
```

```
Ireland2_model <-arima(Ireland_sales,order = c(1,1,2), seasonal = list(order = c(1,1,1)))
```

```
#Print Manual Arima Model Summary
```

```
print(summary(Ireland2_model))
```

```
##
```

```
## Call:
```

```
## arima(x = Ireland_sales, order = c(1, 1, 2), seasonal = list(order = c(1, 1, 1)))
```

```
##
```

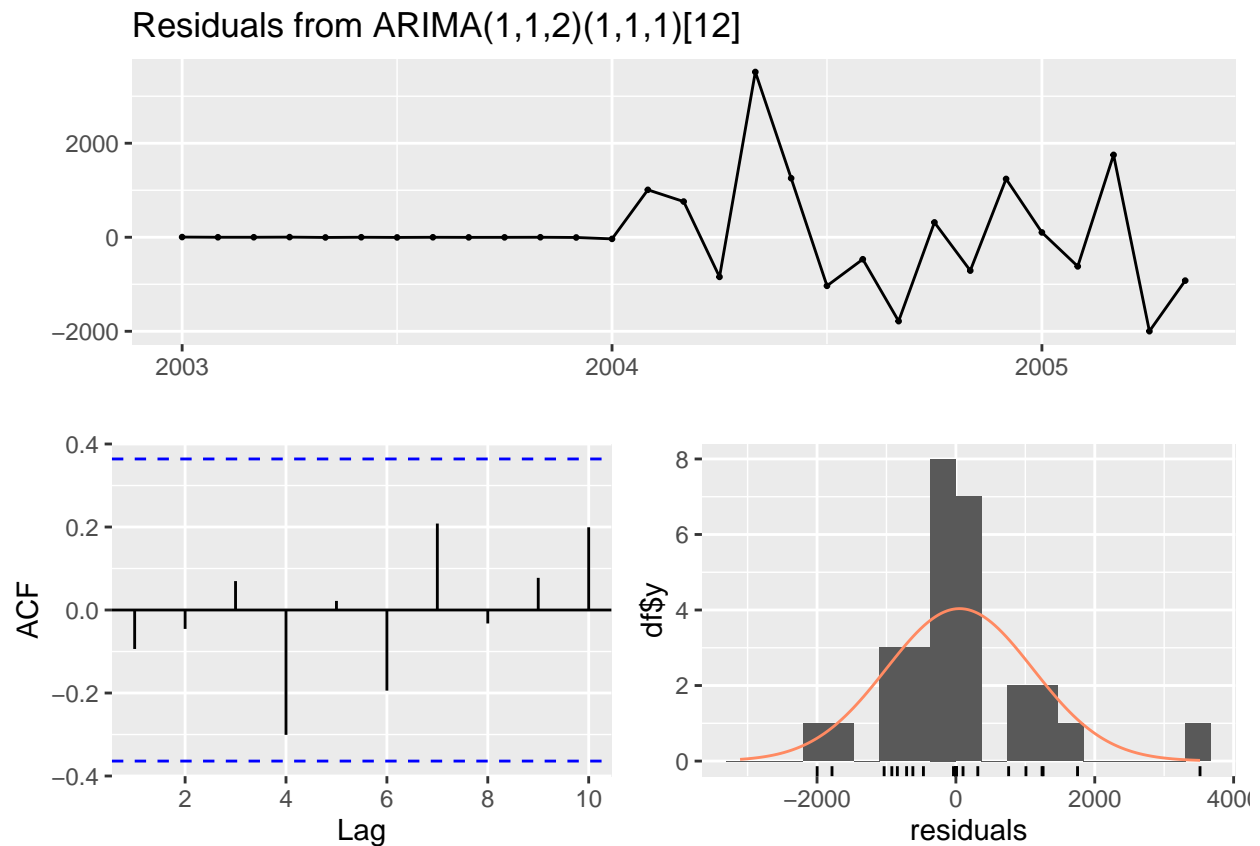
```
## Coefficients:
```

```
## Warning in sqrt(diag(x$var.coef)): NaNs produced
```

```
##          ar1          ma1          ma2          sar1          sma1
```

```
##      -0.3965  -0.5348  1.0000  -0.5585  -0.6755
## s.e.   0.2392   0.1295  0.1486      NaN      NaN
##
## sigma^2 estimated as 1947937:  log likelihood = -147.51,  aic = 307.03
##
## Training set error measures:
##              ME      RMSE      MAE      MPE      MAPE      MASE      ACF1
## Training set 52.73706 1036.711 634.1176 -6.55304 22.45482 0.2690344 -0.09384108
```

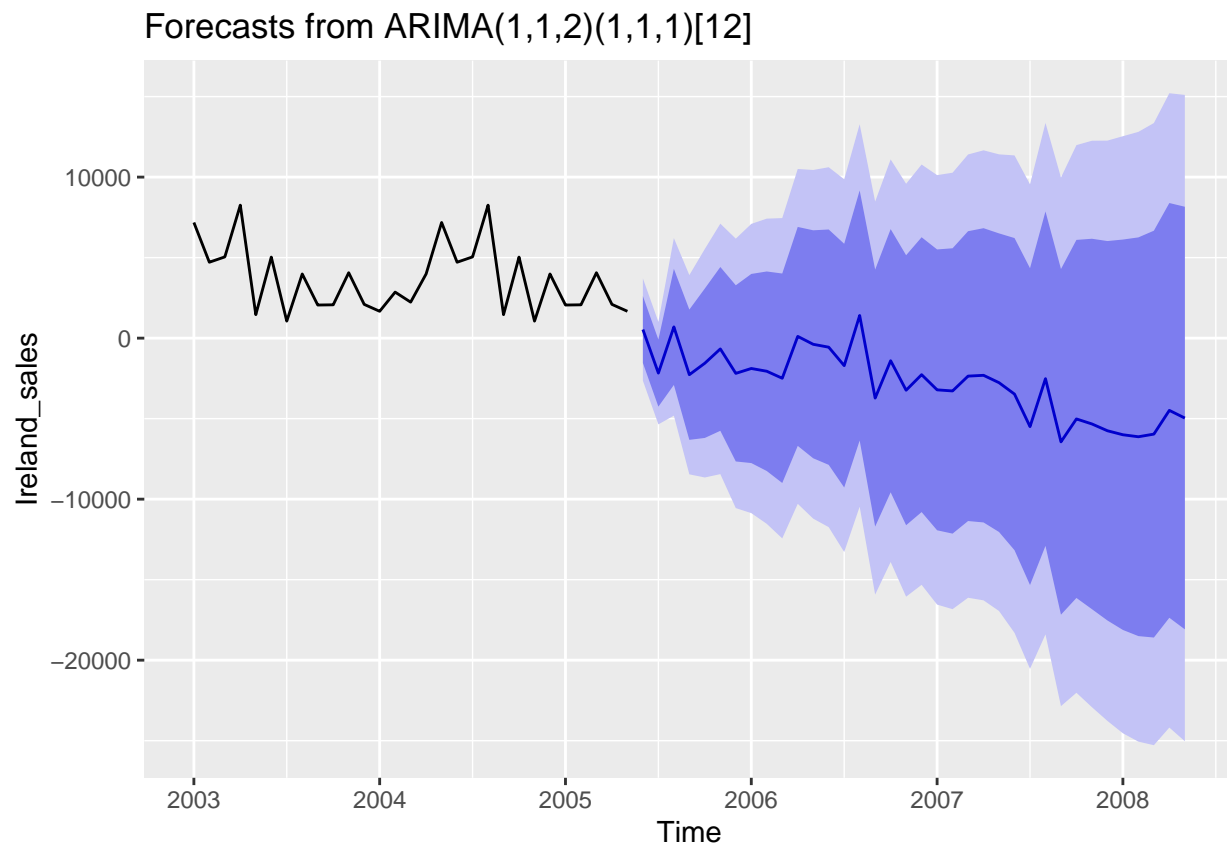
```
#Checking residual values of Manual Arima Model
checkresiduals(Ireland2_model)
```



```
##
## Ljung-Box test
##
## data: Residuals from ARIMA(1,1,2)(1,1,1)[12]
## Q* = 7.085, df = 3, p-value = 0.06924
##
## Model df: 5. Total lags used: 8
```

```
#Create Forecast for Manual ARIMA Model
#Forecast for the next two years
Ireland2_Forecast <- forecast(Ireland2_model, h=36)
```

```
#Plot Forecast Results
#Showing the last 5 years
autoplot(Ireland2_Forecast, include = 60)
```



```
#Print Summary Forecast Results
print(summary(Ireland2_Forecast))
```

```
##
## Forecast method: ARIMA(1,1,2)(1,1,1)[12]
##
## Model Information:
##
## Call:
## arima(x = Ireland_sales, order = c(1, 1, 2), seasonal = list(order = c(1, 1,
##    1)))
##
## Coefficients:

## Warning in sqrt(diag(x$var.coef)): NaNs produced

##          ar1      ma1      ma2      sar1      sma1
##      -0.3965 -0.5348  1.0000 -0.5585 -0.6755
## s.e.   0.2392   0.1295  0.1486      NaN      NaN
##
```

```
## sigma^2 estimated as 1947937: log likelihood = -147.51, aic = 307.03
##
## Error measures:
##           ME      RMSE      MAE      MPE      MAPE      MASE      ACF1
## Training set 52.73706 1036.711 634.1176 -6.55304 22.45482 0.2263577 -0.09384108
##
## Forecasts:
##           Point Forecast      Lo 80      Hi 80      Lo 95      Hi 95
## Jun 2005      534.6773 -1539.913 2609.26753 -2638.135 3707.489
## Jul 2005     -2172.6543 -4253.070 -92.23849 -5354.376 1009.067
## Aug 2005      697.8528 -2905.843 4301.54849 -4813.524 6209.230
## Sep 2005     -2271.5631 -6316.660 1773.53412 -8458.005 3914.879
## Oct 2005     -1558.2059 -6197.535 3081.12292 -8653.447 5537.035
## Nov 2005      -669.3083 -5753.882 4415.26565 -8445.493 7106.876
## Dec 2005     -2188.1167 -7658.321 3282.08777 -10554.072 6177.839
## Jan 2006     -1885.9198 -7757.415 3985.57566 -10865.597 7093.758
## Feb 2006     -2055.8738 -8251.979 4140.23111 -11531.998 7420.251
## Mar 2006     -2490.6806 -8994.032 4012.67040 -12436.698 7455.336
## Apr 2006      107.7577 -6689.375 6904.89081 -10287.560 10503.076
## May 2006     -383.0467 -7461.712 6695.61859 -11208.931 10442.838
## Jun 2006     -561.5982 -7868.453 6745.25701 -11736.469 10613.272
## Jul 2006     -1708.3126 -9275.023 5858.39753 -13280.597 9863.972
## Aug 2006      1407.5839 -6356.008 9171.17565 -10465.805 13280.973
## Sep 2006     -3722.9566 -11701.749 4255.83607 -15925.467 8479.554
## Oct 2006     -1402.7842 -9575.123 6769.55443 -13901.298 11095.729
## Nov 2006     -3234.6887 -11617.990 5148.61243 -16055.841 9586.464
## Dec 2006     -2269.1969 -10802.180 6263.78647 -15319.269 10780.875
## Jan 2007     -3212.5401 -11932.216 5507.13594 -16548.134 10123.054
## Feb 2007     -3279.7895 -12140.465 5580.88651 -16831.024 10271.445
## Mar 2007     -2359.2085 -11358.818 6640.40141 -16122.924 11404.507
## Apr 2007     -2309.8400 -11446.198 6826.51768 -16282.693 11663.013
## May 2007     -2766.6792 -12037.840 6504.48117 -16945.695 11412.337
## Jun 2007     -3477.5806 -13170.334 6215.17266 -18301.367 11346.206
## Jul 2007     -5495.9623 -15332.736 4340.81170 -20540.010 9548.085
## Aug 2007     -2517.1245 -12899.643 7865.39411 -18395.816 13361.567
## Sep 2007     -6440.5934 -17172.024 4290.83740 -22852.901 9971.714
## Oct 2007     -5017.8895 -16136.440 6100.66114 -22022.245 11986.466
## Nov 2007     -5330.1206 -16831.233 6170.99156 -22919.554 12259.313
## Dec 2007     -5752.2067 -17533.254 6028.84051 -23769.764 12265.350
## Jan 2008     -5999.8675 -18122.097 6122.36216 -24539.218 12539.483
## Feb 2008     -6124.4814 -18504.365 6255.40225 -25057.880 12808.917
## Mar 2008     -5960.9370 -18592.799 6670.92479 -25279.703 13357.829
## Apr 2008     -4487.8142 -17366.856 8391.22769 -24184.609 15208.981
## May 2008     -4963.6244 -18085.219 8157.97001 -25031.371 15104.122
```

```
#Forecast 8, Part 1: Forecasting with focus on Trains
```

```
#Sub-setting the data to only show sales of Trains
```

```
Trains_Sales <- subset(salesdata2, PRODUCTLINE == "Trains")
head(Trains_Sales)
```

```
##      ORDERNUMBER QUANTITYORDERED PRICEEACH ORDERLINENUMBER  SALES  ORDERDATE
## 2251      10104           49      65.87           4 3227.63 2003-01-31
## 2407      10104           32      53.31           2 1705.92 2003-01-31
```

```

## 1066      10105      38      100.00      13 4330.10 2003-02-11
## 2252      10116      27       63.38      1 1711.26 2003-04-11
## 1067      10117      21       95.80      7 2011.80 2003-04-16
## 2408      10117      21       49.21     11 1033.41 2003-04-16
##      STATUS QTR_ID MONTH_ID YEAR_ID PRODUCTLINE MSRP PRODUCTCODE
## 2251 Shipped      1          1     2003      Trains    62      S32_3207
## 2407 Shipped      1          1     2003      Trains    58      S50_1514
## 1066 Shipped      1          2     2003      Trains   100      S18_3259
## 2252 Shipped      2          4     2003      Trains    62      S32_3207
## 1067 Shipped      2          4     2003      Trains   100      S18_3259
## 2408 Shipped      2          4     2003      Trains    58      S50_1514
##      CUSTOMERNAME      PHONE
## 2251      Euro Shopping Channel      (91) 555 94 44
## 2407      Euro Shopping Channel      (91) 555 94 44
## 1066      Danish Wholesale Imports      31 12 3555
## 2252      Royale Belge (071) 23 67 2555
## 1067      Dragon Souveniers, Ltd.      +65 221 7555
## 2408      Dragon Souveniers, Ltd.      +65 221 7555
##      ADDRESSLINE1 ADDRESSLINE2      CITY STATE
## 2251      C/ Moralarzarzal, 86      Madrid
## 2407      C/ Moralarzarzal, 86      Madrid
## 1066      Vinb'ltet 34      Kobenhavn
## 2252      Boulevard Tirou, 255      Charleroi
## 1067      Bronz Sok., Bronz Apt. 3/6 Tesvikiye      Singapore
## 2408      Bronz Sok., Bronz Apt. 3/6 Tesvikiye      Singapore
##      POSTALCODE      COUNTRY TERRITORY CONTACTLASTNAME CONTACTFIRSTNAME DEALSIZE
## 2251      28034      Spain      EMEA      Freyre      Diego      Medium
## 2407      28034      Spain      EMEA      Freyre      Diego      Small
## 1066      1734      Denmark      EMEA      Petersen      Jytte      Medium
## 2252      B-6000      Belgium      EMEA      Cartrain      Pascale      Small
## 1067      79903      Singapore      Japan      Natividad      Eric      Small
## 2408      79903      Singapore      Japan      Natividad      Eric      Small

```

```

#Creating Time Series
Trains_sales <- ts(Trains_Sales[,5], start = c(2003,1), end = c(2005,5), frequency = 12)
Trains_sales

```

```

##      Jan      Feb      Mar      Apr      May      Jun      Jul      Aug      Sep
## 2003 3227.63 1705.92 4330.10 1711.26 2011.80 1033.41 2054.36 3179.52 4837.18
## 2004 1681.35 2573.46 1779.71 5344.50 2351.36 2537.64 1408.00 2448.72 3070.52
## 2005 1804.44 3564.75 2856.14 2544.75 5614.56
##      Oct      Nov      Dec
## 2003 2151.82 3131.94 2091.18
## 2004 3952.83 2445.60 972.40
## 2005

```

```

#Build Fit Arima Model
#Taking first differnce of the data
#Getting rid of seasonality by taking first seasonal difference

```

```

Trains_AR_Model <- auto.arima(Trains_sales, d=1, D=1, stepwise = FALSE, approximation = FALSE, trace = T)

```

```

##

```



```

## ARIMA(0,1,0)(0,1,0)[12] : 304.2086
## ARIMA(0,1,1)(0,1,0)[12] : Inf
## ARIMA(0,1,2)(0,1,0)[12] : Inf
## ARIMA(0,1,3)(0,1,0)[12] : Inf
## ARIMA(0,1,4)(0,1,0)[12] : Inf
## ARIMA(0,1,5)(0,1,0)[12] : Inf
## ARIMA(1,1,0)(0,1,0)[12] : 295.7086
## ARIMA(1,1,1)(0,1,0)[12] : Inf
## ARIMA(1,1,2)(0,1,0)[12] : Inf
## ARIMA(1,1,3)(0,1,0)[12] : Inf
## ARIMA(1,1,4)(0,1,0)[12] : Inf
## ARIMA(2,1,0)(0,1,0)[12] : 297.7131
## ARIMA(2,1,1)(0,1,0)[12] : Inf
## ARIMA(2,1,2)(0,1,0)[12] : Inf
## ARIMA(2,1,3)(0,1,0)[12] : Inf
## ARIMA(3,1,0)(0,1,0)[12] : 298.4716
## ARIMA(3,1,1)(0,1,0)[12] : Inf
## ARIMA(3,1,2)(0,1,0)[12] : Inf
## ARIMA(4,1,0)(0,1,0)[12] : 302.1822
## ARIMA(4,1,1)(0,1,0)[12] : Inf
## ARIMA(5,1,0)(0,1,0)[12] : 307.3804
##
##
## Best model: ARIMA(1,1,0)(0,1,0)[12]

```

```

#Printing AR Model Summary
print(summary(Trains_AR_Model))

```

```

## Series: Trains_sales
## ARIMA(1,1,0)(0,1,0)[12]
##
## Coefficients:
##          ar1
##        -0.7842
## s.e.    0.1702
##
## sigma^2 = 4597944: log likelihood = -145.39
## AIC=294.79  AICc=295.71  BIC=296.33
##
## Training set error measures:
##              ME      RMSE      MAE      MPE      MAPE      MASE      ACF1
## Training set 99.93263 1542.157 1014.844 -9.612831 40.98315 0.6780262 -0.2175376

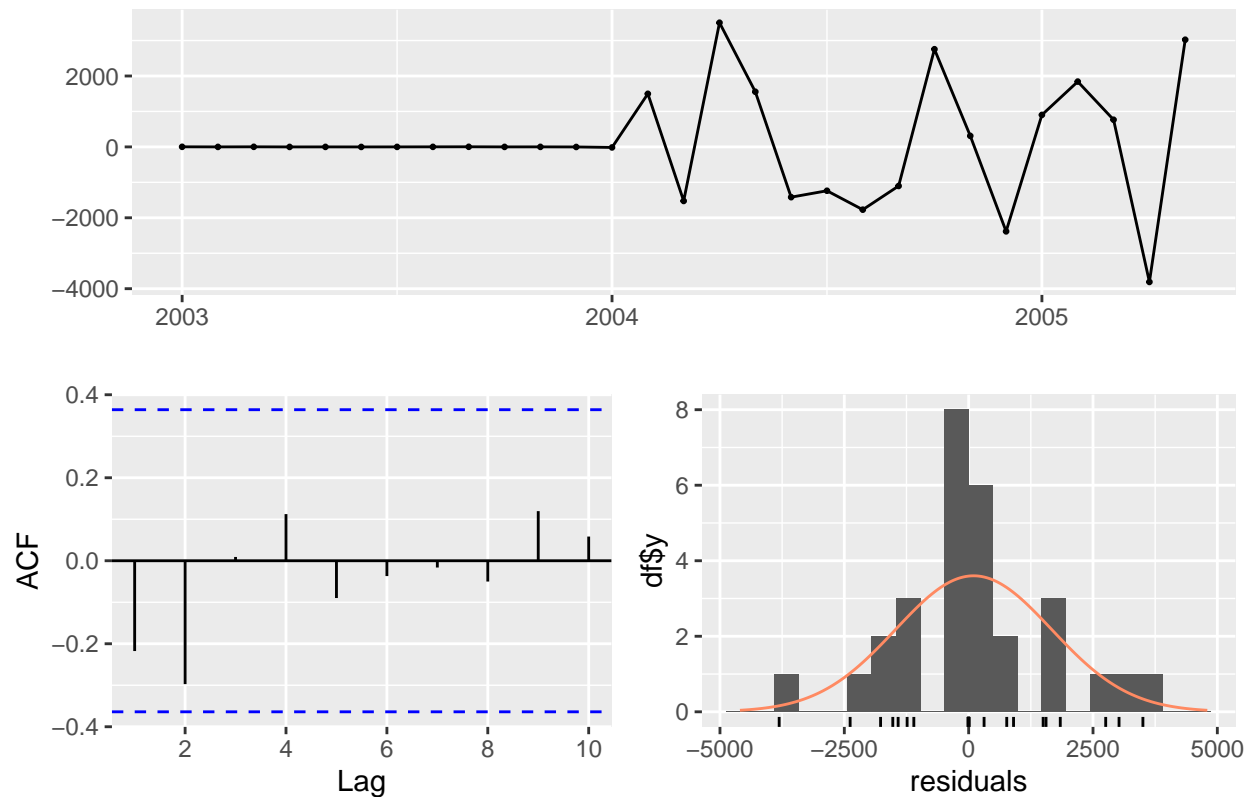
```

```

#Checking Residuals of AR_Model
checkresiduals(Trains_AR_Model)

```

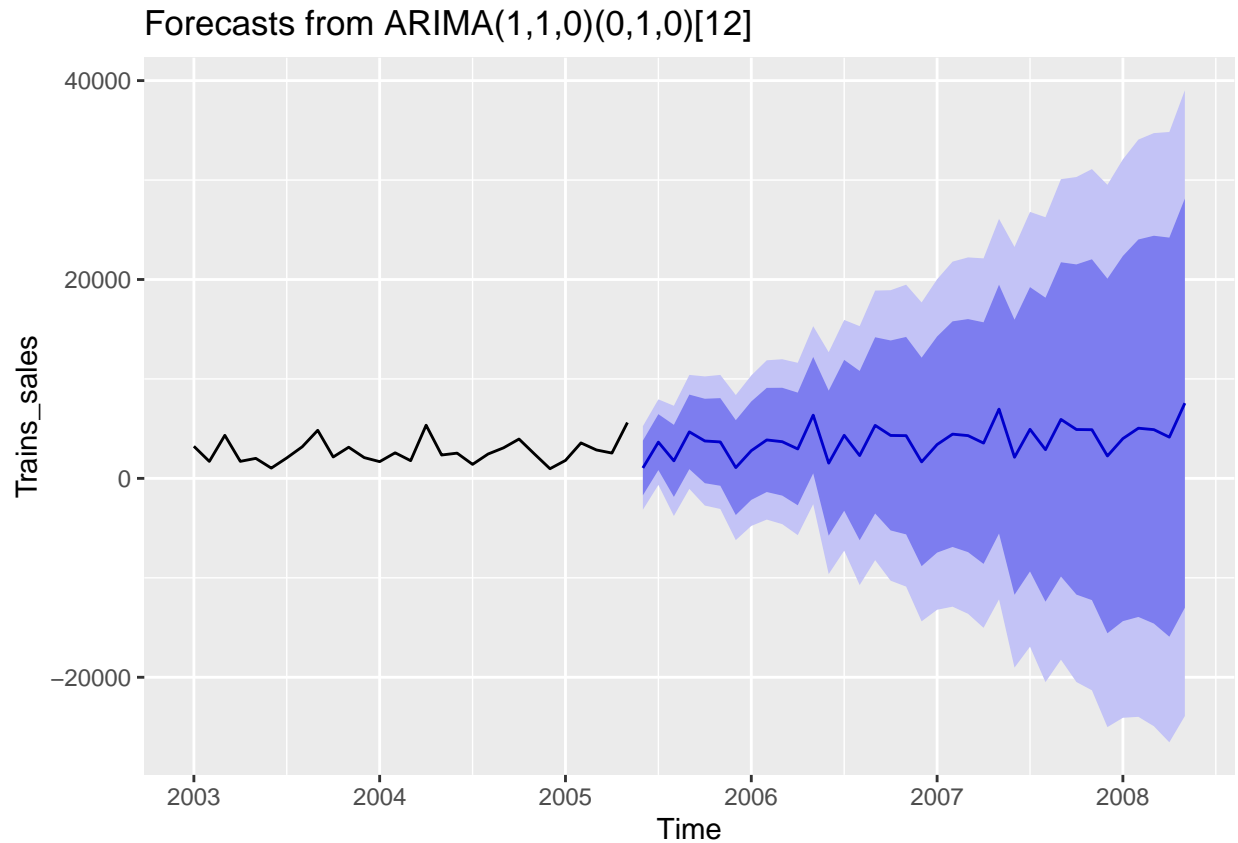
Residuals from ARIMA(1,1,0)(0,1,0)[12]



```
##
##  Ljung-Box test
##
## data:  Residuals from ARIMA(1,1,0)(0,1,0)[12]
## Q* = 5.2742, df = 5, p-value = 0.3833
##
## Model df: 1.   Total lags used: 6
```

```
#Forecasting ARIMA Model
#forecast two years ahead
Trains_AR_Model_Forecast <- forecast(Trains_AR_Model, h=36)
```

```
#Plotting AR Model Forecast
#including the last 5 years
autoplot(Trains_AR_Model_Forecast, include = 60)
```



```
#Print Summary of AR Model Forecast
print(summary(Trains_AR_Model_Forecast))
```

```
##
## Forecast method: ARIMA(1,1,0)(0,1,0)[12]
##
## Model Information:
## Series: Trains_sales
## ARIMA(1,1,0)(0,1,0)[12]
##
## Coefficients:
##      ar1
##      -0.7842
## s.e.    0.1702
##
## sigma^2 = 4597944:  log likelihood = -145.39
## AIC=294.79   AICc=295.71   BIC=296.33
##
## Error measures:
##              ME      RMSE      MAE      MPE      MAPE      MASE      ACF1
## Training set 99.93263 1542.157 1014.844 -9.612831 40.98315 0.6780262 -0.2175376
##
## Forecasts:
##      Point Forecast      Lo 80      Hi 80      Lo 95      Hi 95
## Jun 2005      1046.495 -1701.5130 3794.502 -3156.2204 5249.210
## Jul 2005      3645.040   833.7523 6456.327  -654.4533 7944.533
```

```
## Aug 2005      1762.252 -1859.2102  5383.715 -3776.2967  7300.801
## Sep 2005      4676.561   930.5707  8422.551 -1052.4367 10405.558
## Oct 2005      3761.169  -483.8376  8006.175 -2731.0082 10253.346
## Nov 2005      3663.631  -742.8924  8070.155 -3075.5653 10402.828
## Dec 2005      1085.002 -3682.9803  5852.983 -6206.9974  8377.001
## Jan 2006      2783.880 -2163.4512  7731.210 -4782.4099 10350.169
## Feb 2006      3864.447 -1371.0205  9099.914 -4142.5094 11871.403
## Mar 2006      3688.866 -1731.7989  9109.532 -4601.3258 11979.059
## Apr 2006      2959.494 -2705.6860  8624.674 -5704.6511 11623.639
## May 2006      6357.071   507.5420 12206.599 -2589.0113 15303.153
## Jun 2006      1531.982 -5759.8038  8823.769 -9619.8423 12683.807
## Jul 2006      4332.075 -3251.1597 11915.311 -7265.4819 15929.633
## Aug 2006      2291.241 -6219.3613 10801.844 -10724.6023 15307.085
## Sep 2006      5329.484 -3531.3479 14190.316 -8221.9891 18880.958
## Oct 2006      4316.907 -5233.0082 13866.823 -10288.4282 18922.243
## Nov 2006      4295.579 -5629.4864 14220.644 -10883.4986 19474.657
## Dec 2006      1657.189 -8826.4799 12140.858 -14376.1989 17690.577
## Jan 2007      3402.929 -7460.7856 14266.643 -13211.6885 20017.546
## Feb 2007      4446.748 -6896.2638 15789.761 -12900.8918 21794.389
## Mar 2007      4299.984 -7417.2718 16017.240 -13620.0124 22219.981
## Apr 2007      3548.015 -8596.3372 15692.368 -15025.1690 22121.199
## May 2007      6963.311 -5544.3428 19470.965 -12165.4949 26092.117
## Jun 2007      2124.328 -11703.8768 15952.533 -19024.0864 23272.743
## Jul 2007      4935.317 -9358.7627 19229.397 -16925.5915 26796.226
## Aug 2007      2885.939 -12396.1411 18168.019 -20485.9855 26257.863
## Sep 2007      5930.882 -9867.3063 21729.070 -18230.3618 30092.125
## Oct 2007      4913.051 -11688.9719 21515.074 -20477.5520 30303.654
## Nov 2007      4895.842 -12239.5869 22031.272 -21310.5353 31102.220
## Dec 2007      2254.222 -15572.8542 20081.298 -25009.9381 29518.381
## Jan 2008      4002.495 -14356.6543 22361.644 -24075.4009 32080.391
## Feb 2008      5044.328 -13932.7358 24021.392 -23978.5865 34067.243
## Mar 2008      4899.121 -14599.0145 24397.257 -24920.7042 34718.947
## Apr 2008      4145.931 -15918.4066 24210.269 -26539.8253 34831.687
## May 2008      7562.185 -13007.7593 28132.129 -23896.8300 39021.200
```

```
#Forecast 8, Part 2: Testing Train Sales Forecast with manual ARIMA variables
```

```
#Building second Train model
```

```
Train2_model <-arima(Trains_sales,order = c(1,1,2), seasonal = list(order = c(1,1,1)))
```

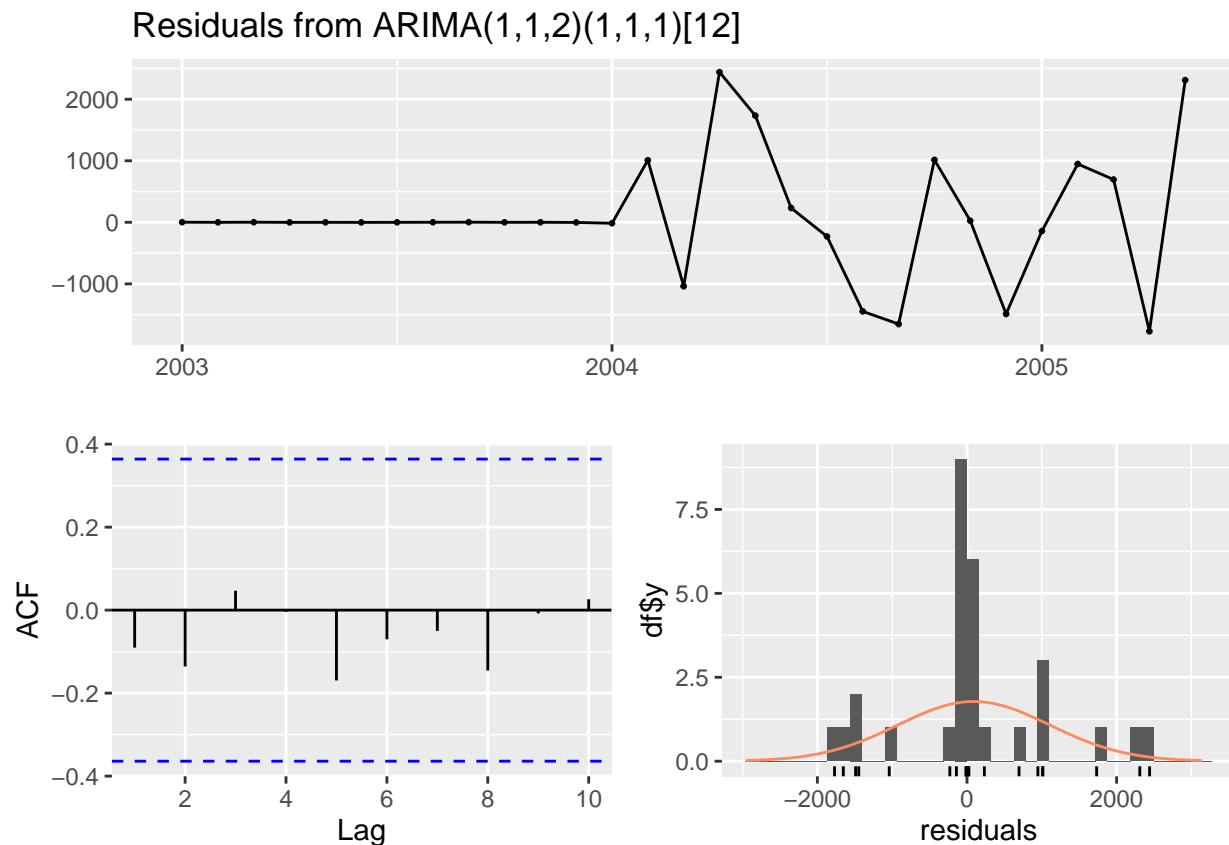
```
#Print Manual Arima Model Summary
```

```
print(summary(Train2_model))
```

```
##
## Call:
## arima(x = Trains_sales, order = c(1, 1, 2), seasonal = list(order = c(1, 1,
##      1)))
##
## Coefficients:
##      ar1      ma1      ma2      sar1      sma1
##    -0.8463  -0.5232  -0.4768   0.4759  -0.9962
## s.e.   0.3544   0.5575   0.5298   0.7112   1.7424
##
```

```
## sigma^2 estimated as 1819965: log likelihood = -142.16, aic = 296.32
##
## Training set error measures:
##           ME      RMSE      MAE      MPE      MAPE      MASE
## Training set 90.54335 1002.062 627.9016 -4.576541 24.35332 0.4539364
##           ACF1
## Training set -0.09034899
```

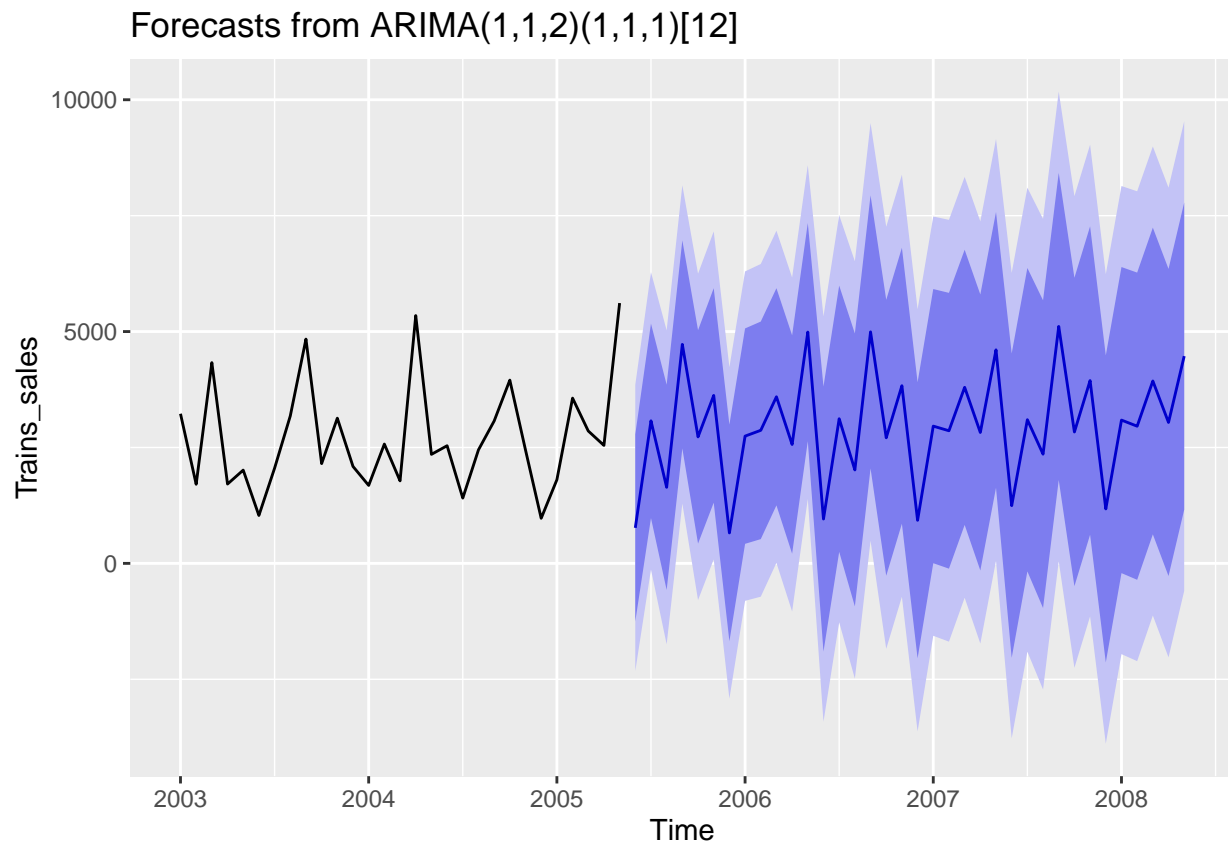
```
#Checking residual values of Manual Arima Model
checkresiduals(Train2_model)
```



```
##
## Ljung-Box test
##
## data: Residuals from ARIMA(1,1,2)(1,1,1)[12]
## Q* = 3.2308, df = 3, p-value = 0.3574
##
## Model df: 5. Total lags used: 8
```

```
#Create Forecast for Manual ARIMA Model
#Forecast for the next two years
Train2_Forecast <- forecast(Train2_model, h=36)
```

```
#Plot Forecast Results
#Showing the last 5 years
autoplot(Train2_Forecast, include = 60)
```



```
#Print Summary Forecast Results
print(summary(Train2_Forecast))
```

```
##
## Forecast method: ARIMA(1,1,2)(1,1,1)[12]
##
## Model Information:
##
## Call:
## arima(x = Trains_sales, order = c(1, 1, 2), seasonal = list(order = c(1, 1,
##      1)))
##
## Coefficients:
##      ar1      ma1      ma2     sar1     sma1
##    -0.8463 -0.5232 -0.4768  0.4759 -0.9962
## s.e.   0.3544   0.5575   0.5298  0.7112   1.7424
##
## sigma^2 estimated as 1819965:  log likelihood = -142.16,  aic = 296.32
##
## Error measures:
##           ME      RMSE      MAE      MPE      MAPE      MASE
```

```

## Training set 90.54335 1002.062 627.9016 -4.576541 24.35332 0.4195067
##           ACF1
## Training set -0.09034899
##
## Forecasts:
##           Point Forecast           Lo 80           Hi 80           Lo 95           Hi 95
## Jun 2005           766.3201 -1251.092538 2783.733 -2319.04630 3851.687
## Jul 2005          3075.1172  978.787489 5171.447  -130.94243 6281.177
## Aug 2005          1640.8463 -572.208552 3853.901 -1743.72904 5025.422
## Sep 2005          4723.2414 2479.617464 6966.865 1291.91471 8154.568
## Oct 2005          2728.3066  427.272963 5029.340  -790.82067 6247.434
## Nov 2005          3622.6099 1310.494863 5934.725   86.53511 7158.685
## Dec 2005           656.7795 -1678.732416 2992.291 -2915.07775 4228.637
## Jan 2006          2744.8201  421.977394 5067.663  -807.66125 6297.301
## Feb 2006          2869.4706  523.704315 5215.237  -718.06933 6457.010
## Mar 2006          3593.2305 1251.615199 5934.846   12.03893 7174.422
## Apr 2006          2564.1171  209.486260 4918.748 -1036.98001 6165.214
## May 2006          4988.8220 2637.325402 7340.319 1392.51831 8585.126
## Jun 2006           956.4992 -1901.223272 3814.222 -3414.01018 5327.009
## Jul 2006          3119.9629  249.327422 5990.598 -1270.29522 7510.221
## Aug 2006          2015.5980 -926.944994 4958.141 -2484.63316 6515.829
## Sep 2006          4993.0164 2048.936955 7937.096  490.43545 9495.597
## Oct 2006          2708.6478 -266.809508 5684.105 -1841.92147 7259.217
## Nov 2006          3832.0078  856.929483 6807.086  -717.98182 8381.997
## Dec 2006           929.1522 -2047.068042 3905.373 -3622.58389 5480.888
## Jan 2007          2960.4937   3.936854 5917.051 -1561.16979 7482.157
## Feb 2007          2860.5806 -113.565381 5834.727 -1687.98315 7409.144
## Mar 2007          3797.3031  830.146941 6764.459  -740.57064 8335.177
## Apr 2007          2823.2472 -152.703028 5799.197 -1728.07590 7374.570
## May 2007          4605.3590 1632.416423 7578.302   58.63569 9152.082
## Jun 2007          1245.3138 -2035.793967 4526.422 -3772.70750 6263.335
## Jul 2007          3099.2636 -172.286784 6370.814 -1904.14097 8102.668
## Aug 2007          2355.2903 -962.801448 5673.382 -2719.29310 7429.874
## Sep 2007          5110.6212 1798.729939 8422.512   45.52061 10175.722
## Oct 2007          2834.1954 -491.055556 6159.446 -2251.33708 7919.728
## Nov 2007          3943.2769  617.699978 7268.854 -1142.75411 9029.308
## Dec 2007          1174.7118 -2134.668694 4484.092 -3886.54891 6235.973
## Jan 2008          3090.7876 -209.806768 6391.382 -1957.03587 8138.611
## Feb 2008          2958.7278 -354.304423 6271.760 -2108.11773 8025.573
## Mar 2008          3933.5626  626.279319 7240.846 -1124.49071 8991.616
## Apr 2008          3039.2122 -272.439059 6350.864 -2025.52136 8103.946
## May 2008          4470.2640 1159.099220 7781.429  -593.72553 9534.254

```