

Econ 204B

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UCSB

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Getting to know you

On notecard please write:

- ▶ Name: Matthew Fitzgerad
- ▶ Preferred First Name: Matt
- ▶ Hometown: Riverside, CA
- ▶ Programming language with most experience: R
 - ▶ Level: beginner/intermediate/advanced

General Information

Contact:

- ▶ Email: mfitzgerald00@ucsb.edu
- ▶ Office: North Hall 2048
- ▶ Office Hours: Wednesdays 11:00am -1:00pm

Problem Sets:

- ▶ Typically will have both written and programming components
- ▶ Grades will be on a 10 point scale
- ▶ Need to be done in \LaTeX

Materials

- ▶ There are lots of online materials and books
- ▶ One very useful resource are the lectures from [QuantEcon](#)
 - ▶ Material on topics
 - ▶ Material on Julia
- ▶ For Julia specifically:
 - ▶ [Julia documentation page](#)
 - ▶ [Learn Julia the Hard Way](#)

General Cont.

- ▶ I will be using Julia with Atom as my text editor
- ▶ You can use any language that you'd like, however there are benefits to using Julia
 - ▶ You have resources to help you learn (Professor Rupert and me)
 - ▶ You get experience early in an up and coming language
 - ▶ Even if you know other languages, it's always good to be familiar with as many as possible
- ▶ For the first assignment you will need to use Julia, and later I will create Julia scripts for you to complete
- ▶ If you had trouble installing, let me know and we can get you set up

Overview

- ▶ This quarter we will learn a new tool: **dynamic programming**
- ▶ Allows us to take into consideration the dynamics of economic decision making
 - ▶ In simple static optimization problems individuals consider how much of each good they'd like to consume
 - ▶ In dynamic optimization we take into account that consumption today comes at the expense of savings, and thus consumption tomorrow
 - ▶ Can also take into account uncertainty in the future which influences decisions today

Examples of Dynamic Problems

Dynamic optimization important for many problems in both micro and macro economics:

- ▶ General consumption problems
 - ▶ How much to consume vs. save tomorrow (can add shocks to future income stream)
 - ▶ Decision to invest in human capital (take lower wage in the present to attain a higher wage in the future)
- ▶ Resource Extraction problems (water, fish, timber harvest, etc.)
- ▶ Firm entry (or exit) decision
- ▶ Job search

Dynamic Programming Intuition

Recall the definition of indirect utility

$$V(\mathbf{p}, M) = \max_{\mathbf{x}} u(\mathbf{x})$$
$$\text{s.t. } \mathbf{p}'\mathbf{x} = M$$

First order conditions:

$$\frac{u_i(\mathbf{x})}{p_i} = \lambda \quad \text{for } i = 1, 2, \dots, l$$

Dynamic Programming Intuition Cont.

What is the interpretation of $V(\mathbf{p}, M)$?

- ▶ Maximized level of utility given current state (\mathbf{p}, M)
- ▶ Given (\mathbf{p}, M) consumer will have $V(\mathbf{p}, M)$ level of utility

What is the interpretation of λ ?

$$\begin{aligned}\lambda &= V_M(\mathbf{p}, M) \\ \implies \frac{u_i(\mathbf{x})}{p_i} &= V_M(\mathbf{p}, M) \text{ for } i = 1, 2, \dots, I\end{aligned}$$

If we knew $V(\mathbf{p}, M)$ at every (\mathbf{p}, M) , don't need to know how consumer will allocate M just need to know she's acting optimally

Multi-Period Problems

- ▶ While this was a static optimization problem, when we look at dynamic optimization problems the intuition will be similar
- ▶ Consider the optimization problem faced by an infinitely-lived agent with an endowment stream $\{e_t\}_{t=0}^{\infty}$ (assume complete markets). Agent maximizes present discounted value of lifetime utility:

$$\begin{aligned} \max_{\{c_t\}_{t=0}^{\infty}} \quad & \sum_{t=0}^{\infty} \beta^t u(c_t) \\ \text{s.t.} \quad & \sum_{t=0}^{\infty} c_t \leq \sum_{t=0}^{\infty} e_t \end{aligned}$$

Multi-Period Problems Cont.

- ▶ Solution to this problem is sequence of consumption decisions $\{c_t\}_{t=0}^{\infty}$
- ▶ If we add uncertainty we would need an optimal sequence for every possible sequence of states
- ▶ Instead we can write the problem recursively, making the assumption that the agent will make optimal decisions in the future:

$$V(a) = \max_c \{u(c) + \beta V(a')\}$$
$$\text{s.t. } c + a' = (1+r)a + e$$

- ▶ Solution will be a value function V , or equivalently a policy function that maps states to outcomes

Where we're going

- ▶ Next week we'll talk more about solving these dynamic problems
- ▶ We'll also talk more about recursive formulation of the problem
- ▶ These types of problems are often difficult or impossible to solve analytically, and thus we need to learn computational methods to find solution
- ▶ The recursive formulation of these types of problems makes them easy to set up on the computer

Latex in Atom

- ▶ Install the following packages:
 - ▶ language-latex
 - ▶ latex
 - ▶ latex-completions
 - ▶ latex-plus
- ▶ Potential issue with keyboard shortcut to compile
 - ▶ One solution is to go into settings in latex package and check the box for “Build on Save”
 - ▶ This will compile pdf every time you save, thus `cmd+s/cntrl+s` will compile and save

Homework 1

- ▶ Homework 1 will be posted after section today
 - ▶ Four questions: Variable assignment, Functions, Loops, and Plotting
 - ▶ Once you know how to do these 4 things in a language, you're 'conversational' (i.e. you now know enough to Google questions)
- ▶ First try to do the problems on your own, but certainly feel free to ask me questions
- ▶ Learning a new language can be daunting but once you get the basics down it becomes much easier!

Let's take a look at Atom!