

# CSE185

## Introduction to Computer Vision

### Lab 03: Spatial Filters

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# Overview

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- Median filter



Noisy input image



Median filter output

# Overview

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- Sobel filter



Input image



Sobel filter output

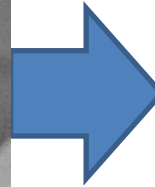
# Overviews

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- Gaussian filter



Input image



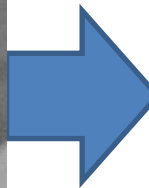
Gaussian filter output



# Sobel Filter

- Sobel filter is a simple edge detector

- $H = \begin{pmatrix} 1 & 2 & 1 \\ 0 & 0 & 0 \\ -1 & -2 & -1 \end{pmatrix}$  or  $H = \begin{pmatrix} 1 & 0 & -1 \\ 2 & 0 & -2 \\ 1 & 0 & -1 \end{pmatrix}$



Input image

Sobel filter output

# Sobel Filter

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- `sobel_filter.m`

```
function output = sobel_filter(img, kernel)
    % YOUR CODE HERE
end
```

- In `lab03.m`:

```
img = im2double(imread('lena.jpg'));

%% Sobel filter
H = [1, 2, 1; 0, 0, 0; -1, -2, -1]; % horizontal edge
%H = [1, 0, -1; 2, 0, -2; 1, 0, -1]; % vertical edge

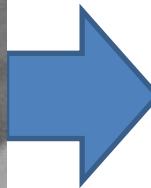
img_sobel = sobel_filter(img, H);
figure, imshow(img_sobel);
imwrite(img_sobel, 'sobel_h.jpg');
```

- Compare your result with `I = imfilter(img, H);`

# Gaussian Filter

- Gaussian filter is a low-pass/smoothing filter

$$g(\Delta x, \Delta y) = \frac{1}{Z} \exp \left( -\frac{\Delta x^2 + \Delta y^2}{2\sigma^2} \right)$$



Input image

Gaussian filter output

# Gaussian Filter

- Gaussian filter is a low-pass/smoothing filter

$$g(\Delta x, \Delta y) = \frac{1}{Z} \exp \left( -\frac{\Delta x^2 + \Delta y^2}{2\sigma^2} \right)$$

- $\Delta x, \Delta y$  are offsets from the kernel center, and  $Z$  is the normalized term to make the sum of all weights equal to 1
- In MATLAB:

0.0113	0.0149	0.0176	0.0186	0.0176	0.0149	0.0113
0.0149	0.0197	0.0233	0.0246	0.0233	0.0197	0.0149
0.0176	0.0233	0.0275	0.029	0.0275	0.0233	0.0176
0.0186	0.0246	0.029	0.0307	0.029	0.0246	0.0186
0.0176	0.0233	0.0275	0.029	0.0275	0.0233	0.0176
0.0149	0.0197	0.0233	0.0246	0.0233	0.0197	0.0149
0.0113	0.0149	0.0176	0.0186	0.0176	0.0149	0.0113

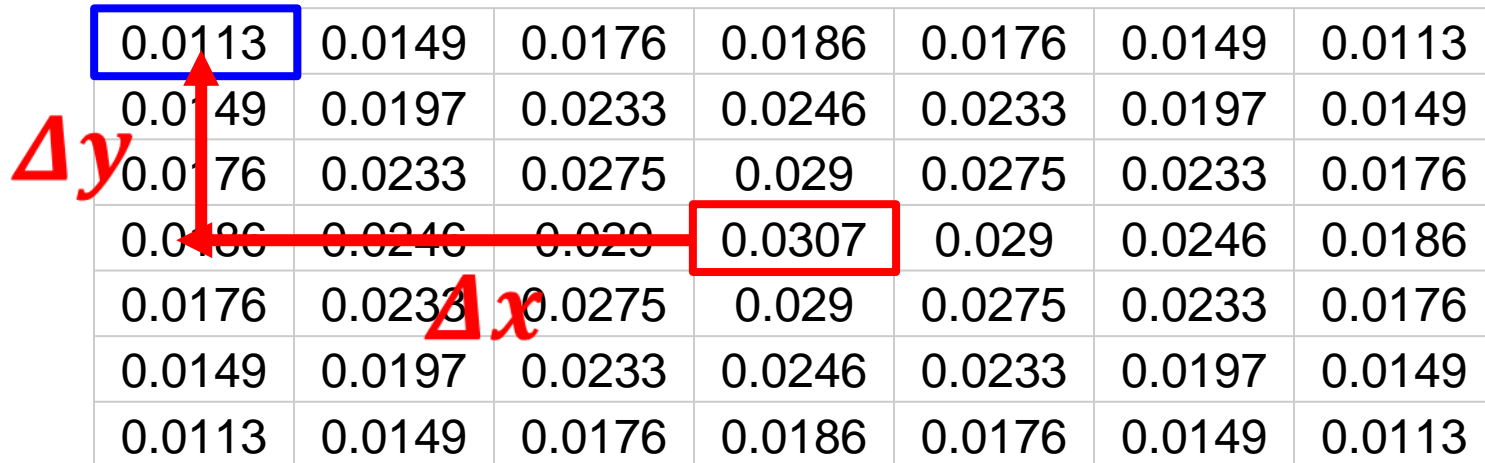


# Gaussian Filter

- Gaussian filter is a low-pass/smoothing filter

$$g(\Delta x, \Delta y) = \frac{1}{Z} \exp \left( -\frac{\Delta x^2 + \Delta y^2}{2\sigma^2} \right)$$

- $\Delta x, \Delta y$  are offsets from the kernel center, and  $Z$  is the normalized term to make the sum of all weights equal to 1
- In MATLAB:



0.0113	0.0149	0.0176	0.0186	0.0176	0.0149	0.0113
0.0149	0.0197	0.0233	0.0246	0.0233	0.0197	0.0149
0.0176	0.0233	0.0275	0.029	0.0275	0.0233	0.0176
0.0186	0.0246	0.029	0.0307	0.029	0.0246	0.0186
0.0176	0.0233	0.0275	0.029	0.0275	0.0233	0.0176
0.0149	0.0197	0.0233	0.0246	0.0233	0.0197	0.0149
0.0113	0.0149	0.0176	0.0186	0.0176	0.0149	0.0113

# Gaussian Filter

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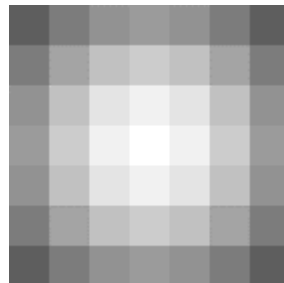
- You don't need to implement Gaussian kernel by yourself (this is bonus).

- Use `fspecial`:

```
H = fspecial('gaussian', hsize, sigma);
```

`hsize` is the size of the kernel, `sigma` =  $\sigma$

- Visualization of a Gaussian kernel:



# Gaussian Filter

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- `gaussian_filter.m`

```
function output = gaussian_filter(img, hsize, sigma)
    H = fspecial('gaussian', hsize, sigma);
    % YOUR CODE HERE
end
```

- In `lab03.m`:

```
%% Gaussian filter
hsize = 5; sigma = 2;
% hsize = 9; sigma = 4;

img_gaussian = gaussian_filter(img, hsize, sigma);
figure, imshow(img_gaussian);
imwrite(img_gaussian, 'gaussian_5.jpg');
```

- Compare your result with `I = imfilter(img, H);`

# Lab assignment 03

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1. Implement `sobel_filter.m`, use horizontal filter and save the image as `sobel_h.jpg`
2. Use vertical filter and save the image as `sobel_v.jpg`
3. Implement `gaussian_filter.m`, use `hsize = 5`, `sigma = 2`, and save the image as `gaussian_5.jpg`
4. Use `hsize = 9`, `sigma = 4`, and save the image as `gaussian_9.jpg`
5. Upload your output images and `lab03.m`, `sobel_filter.m`, and `gaussian_filter.m`

\* Use 'lena.jpg' as the input image for all questions.

# Bonus

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- Implement boundary padding
  - zero padding (pixels outside the image are zero)
  - replicated/repeated padding (pixels outside the image are the same as pixels on the boundaries)
- You can try built-in function `padarray` or `wextend`, but you need to implement by yourself to get bonus points
- Implement Gaussian kernel
  - compute a matrix based on  $g(\Delta x, \Delta y) = \exp\left(-\frac{\Delta x^2 + \Delta y^2}{2\sigma^2}\right)$
  - normalize the matrix to have sum equal to 1



# Reference

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- [Spatial Filtering](#)
- [Linear Algebra and MATLAB Tutorial](#)
- [Awesome Computer Vision](#)