

The boundary condition $\phi = 0$ specifies ϕ

\Rightarrow Dirichlet boundary condition

$$3. \underline{E} = -\nabla\phi = -\left(\frac{\partial}{\partial x}\phi \hat{x} + \frac{\partial}{\partial y}\phi \hat{y} + \frac{\partial}{\partial z}\phi \hat{z}\right)$$

$$\text{where } \frac{\partial\phi}{\partial x} \approx \frac{\phi(i+1;n) - \phi(i-1;n)}{2\Delta x}$$

where x position is index of position i in x direction, at time-step n .

similar ~~eqns~~ for $\frac{\partial\phi}{\partial y}$ and $\frac{\partial\phi}{\partial z}$

$$4. \text{error} = \sum_{\substack{\text{lattice} \\ i,j,k}} |\phi(i,j,k;n+1) - \phi(i,j,k;n)| < \text{threshold}$$

CS ~~stop~~ When error $<$ threshold (usually 0.01 or 10^{-3})
we have reached steady state

$$\text{i.e. } \frac{\partial\phi}{\partial t} = 0 = \frac{\partial^2\phi}{\partial x^2} + \frac{\partial^2\phi}{\partial y^2} + \frac{\partial^2\phi}{\partial z^2} + \frac{\rho}{\epsilon}$$

7. Fds show agreement with Gauss' Law

8. Translational invariance along ~~the~~ infinite wire in z direction

$$\Rightarrow B_z = 0, \frac{\partial}{\partial z}A_x = 0, \frac{\partial}{\partial z}A_y = 0$$

$$\Rightarrow \underline{A} = \begin{pmatrix} 0 \\ 0 \\ A_z(x,y) \end{pmatrix} \quad \text{as } \underline{B} = \nabla \times \underline{A}$$

$A_z = 0$ at boundaries