## **Chapter 1**

A simple fluid-structure interaction problem revisited: Finite Reynolds number flow, driven by an oscillating ring – mesh update done by AlgebraicElements.

We re-visit the simple fluid-structure interaction problem considered in the earlier example. This time we perform the update of the nodal positions with AlgebraicElements.

```
//LIC// This file forms part of oomph-lib, the object-oriented,
//LIC// multi-physics finite-element library, available
//LIC// at http://www.oomph-lib.org.
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//LIC//
// Driver for 2D Navier Stokes flow, driven by oscillating ring
// with pseudo-elasticity: The mean radius of ring is adjusted to
// allow conservation of volume (area).
// Oomph-lib includes
#include "generic.h"
#include "navier_stokes.h"
//{\tt Need \ to \ instantiate \ templated \ mesh}
#include "meshes/quarter_circle_sector_mesh.h"
//Include namespace containing Sarah's asymptotics
#include "osc_ring_sarah_asymptotics.h"
using namespace std;
using namespace oomph;
using namespace MathematicalConstants;
/// Namespace for physical parameters
```

```
namespace Global_Physical_Variables
 /// Reynolds number
double Re=100.0; // ADJUST_PRIORITY
 /// Reynolds x Strouhal number
 double ReSt=100.0; // ADJUST_PRIORITY
/// Driver for oscillating ring problem: Wall performs oscillations /// that resemble eigenmodes of freely oscillating ring and drives /// viscous fluid flow. Mean radius of wall is adjustable and
/// responds to a pressure value in the fluid to allow for
/// mass conservation.
template<class ELEMENT>
class OscRingNStProblem : public Problem
public:
 /// \ constructor: Pass timestep and function pointer to the
 /// solution that provides the initial conditions for the fluid
OscRingNStProblem(const double& dt,
                    FiniteElement::UnsteadyExactSolutionFctPt IC_fct_pt);
 /// Destructor (empty)
 ~OscRingNStProblem(){}
 /// Get pointer to wall as geometric object
GeomObject* wall_pt()
   return Wall_pt;
 /// Update after solve (empty)
void actions_after_newton_solve(){}
 /// \short Update the problem specs before solve (empty)
 void actions_before_newton_solve(){}
 /// \short Update the problem specs before checking Newton
 /// convergence: Update the fluid mesh and re-set velocity
 /// boundary conditions -- no slip velocity on the wall means /// that the velocity on the wall is dependent.
 void actions_before_newton_convergence_check()
  // Update the fluid mesh -- auxiliary update function for algebraic
  \ensuremath{//} nodes automatically updates no slip condition.
  fluid_mesh_pt()->node_update();
 /// \short Update the problem specs after adaptation:
 /// Set auxiliary update function that applies no slip on all
 /// boundary nodes and choose fluid pressure dof that drives
 /// the wall deformation
 void actions_after_adapt()
   // Ring boundary: No slip; this also implies that the velocity needs
   // to be updated in response to wall motion. This needs to be reset
   // every time the mesh is changed -- there's no mechanism by which
   // auxiliary update functions are copied to newly created nodes.
   // (that's because unlike boundary conditions, they don't
   // occur exclusively at boundaries)
   unsigned ibound=1;
    unsigned num_nod= fluid_mesh_pt()->nboundary_node(ibound);
    for (unsigned inod=0;inod<num_nod;inod++)</pre>
      fluid mesh pt()->boundary node pt(ibound, inod)->
       set_auxiliary_node_update_fct_pt(
        FSI_functions::apply_no_slip_on_moving_wall);
   // Set the reference pressure as the constant pressure in element 0
   dynamic_cast<PseudoBucklingRingElement*>(Wall_pt)
     ->set_reference_pressure_pt(fluid_mesh_pt()->element_pt(0)
                                  ->internal_data_pt(0));
 /// Run the time integration for ntsteps steps
```

```
void unsteady_run(const unsigned &ntsteps, const bool& restarted,
                   DocInfo& doc_info);
 /// \short Set initial condition (incl previous timesteps) according
 /// to specified function.
 void set_initial_condition();
 /// Doc the solution
void doc_solution(DocInfo& doc info):
 /// Access function for the fluid mesh
AlgebraicRefineableQuarterCircleSectorMesh<ELEMENT>* fluid_mesh_pt()
  return Fluid_mesh_pt;
 /// \short Dump problem data.
 void dump_it(ofstream& dump_file, DocInfo doc_info);
 /// \short Read problem data.
void restart(ifstream& restart_file);
private:
 /// Write header for trace file
void write_trace_file_header();
 /// Function pointer to set the intial condition
FiniteElement::UnsteadyExactSolutionFctPt IC_Fct_pt;
 /// Pointer to wall
GeomObject* Wall_pt;
 /// Pointer to fluid mesh
AlgebraicRefineableQuarterCircleSectorMesh<ELEMENT>* Fluid_mesh_pt;
 /// Pointer to wall mesh (contains only a single GeneralisedElement)
Mesh* Wall_mesh_pt;
 /// Trace file
ofstream Trace_file;
 /// Pointer to node on coarsest mesh on which velocity is traced
Node* Veloc_trace_node_pt;
 /// \ Pointer to node in symmetry plane on coarsest mesh at
 /// which velocity is traced
Node* Sarah_veloc_trace_node_pt;
/// Constructor: Pass (constant) timestep and function pointer to the solution
/// that provides the initial conditions for the fluid.
                     template<class ELEMENT>
OscRingNStProblem<ELEMENT>::OscRingNStProblem(const double& dt,
FiniteElement::UnsteadyExactSolutionFctPt IC_fct_pt) : IC_Fct_pt(IC_fct_pt)
 // Period of oscillation
double T=1.0;
 //Allocate the timestepper
add_time_stepper_pt(new BDF<4>);
   Initialise timestep -- also sets the weights for all timesteppers
 // in the problem.
 initialise_dt(dt);
// Parameters for pseudo-buckling ring
double eps_buckl=0.1; // ADJUST_PRIORITY
double ampl_ratio=-0.5; // ADJUST_PRIORIT
                          // ADJUST_PRIORITY
unsigned n_buckl=2; // ADJUST_PRIORITY
double r_0=1.0;
 // Build wall geometric element
Wall_pt=new PseudoBucklingRingElement(eps_buckl,ampl_ratio,n_buckl,r_0,T,
                                       time_stepper_pt());
 // Fluid mesh is suspended from wall between these two Lagrangian
 // coordinates:
 double xi_lo=0.0;
double xi_hi=2.0*atan(1.0);
 \ensuremath{//} Fractional position of dividing line for two outer blocks in fluid mesh
double fract mid=0.5;
 // Build fluid mesh
 Fluid_mesh_pt=new AlgebraicRefineableQuarterCircleSectorMesh<ELEMENT>(
 Wall_pt, xi_lo, fract_mid, xi_hi, time_stepper_pt());
 // Set error estimator
 Z2ErrorEstimator* error_estimator_pt=new Z2ErrorEstimator;
Fluid_mesh_pt->spatial_error_estimator_pt()=error_estimator_pt;
 // Fluid mesh is first sub-mesh
 add_sub_mesh(Fluid_mesh_pt);
```

```
// Build wall mesh
Wall_mesh_pt=new Mesh;
// Wall mesh is completely empty: Add Wall element in its GeneralisedElement
  incarnation
Wall_mesh_pt->add_element_pt(dynamic_cast<GeneralisedElement *>(Wall_pt));
// Wall mesh is second sub-mesh
add_sub_mesh(Wall_mesh_pt);
// Combine all submeshes into a single Mesh
build global mesh();
// Extract pointer to node at center of mesh (this node exists
// at all refinement levels and can be used to doc continuous timetrace
// of velocities)
unsigned nnode=fluid_mesh_pt()->finite_element_pt(0)->nnode();
Veloc_trace_node_pt=fluid_mesh_pt()->finite_element_pt(0)->node_pt(nnode-1);
\ensuremath{//} Extract pointer to node in symmetry plane (this node exists
// at all refinement levels and can be used to doc continuous timetrace
// of velocities)
unsigned nnode_1d=dynamic_cast<ELEMENT*>(
 fluid_mesh_pt()->finite_element_pt(0))->nnode_1d();
Sarah_veloc_trace_node_pt=fluid_mesh_pt()->
finite_element_pt(0)->node_pt(nnode_td-1);
// The "pseudo-elastic" wall element is "loaded" by a pressure.
// Use the "constant" pressure component in Crouzeix Raviart
// fluid element as that pressure.
dynamic_cast<PseudoBucklingRingElement*>(Wall_pt)
 ->set_reference_pressure_pt(fluid_mesh_pt()
                              ->element_pt(0)->internal_data_pt(0));
// Set the boundary conditions for this problem:
// All nodes are free by default -- just pin the ones that have
// Dirichlet conditions here.
// Bottom boundary:
unsigned ibound=0;
  unsigned num_nod= fluid_mesh_pt()->nboundary_node(ibound);
  for (unsigned inod=0;inod<num_nod;inod++)</pre>
    // Pin vertical velocity
      fluid_mesh_pt()->boundary_node_pt(ibound,inod)->pin(1);
// Ring boundary: No slip; this also implies that the velocity needs
// to be updated in response to wall motion
ibound=1;
  unsigned num_nod=fluid_mesh_pt()->nboundary_node(ibound);
  for (unsigned inod=0;inod<num_nod;inod++)</pre>
   {
    // Which node are we dealing with?
    Node* node_pt=fluid_mesh_pt()->boundary_node_pt(ibound,inod);
    // Set auxiliary update function pointer to apply no-slip condition
    // to velocities whenever nodal position is updated
    node_pt->set_auxiliary_node_update_fct_pt(
    FSI_functions::apply_no_slip_on_moving_wall);
// Pin both velocities
    for (unsigned i=0;i<2;i++)</pre>
      node_pt->pin(i);
     }
// Left boundary:
ibound=2;
  unsigned num_nod=fluid_mesh_pt()->nboundary_node(ibound);
  for (unsigned inod=0; inod<num nod; inod++)
   {
    // Pin horizontal velocity
      fluid_mesh_pt()->boundary_node_pt(ibound,inod)->pin(0);
   }
, ^{\prime} // Complete the build of all elements so they are fully functional
//Find number of elements in mesh
unsigned n_element = fluid_mesh_pt()->nelement();
// Loop over the elements to set up element-specific
// things that cannot be handled by constructor
for(unsigned i=0;i<n_element;i++)</pre>
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```
// Upcast from FiniteElement to the present element
  ELEMENT *el_pt = dynamic_cast<ELEMENT*>(fluid_mesh_pt()->element_pt(i));
   //Set the Reynolds number, etc
  el_pt->re_pt() = &Global_Physical_Variables::Re;
  el_pt->re_st_pt() = &Global_Physical_Variables::ReSt;
//Attach the boundary conditions to the mesh cout «"Number of equations: " « assign_eqn_numbers() « std::endl;
 // Set parameters for Sarah's asymptotic solution
 // Amplitude of the oscillation
 SarahBL::epsilon=static_cast<PseudoBucklingRingElement*>(Wall_pt)->
 eps_buckl();
 // Womersley number is the same as square root of Reynolds number
SarahBL::alpha=sqrt(Global_Physical_Variables::Re);
 // Amplitude ratio
 SarahBL::A=static_cast<PseudoBucklingRingElement*>(Wall_pt)->ampl_ratio();
 // Buckling wavenumber
 SarahBL::N=static_cast<PseudoBucklingRingElement*>(Wall_pt)->n_buckl_float();
 // Frequency of oscillation (period is one)
SarahBL::Omega=2.0*MathematicalConstants::Pi;
/// Set initial condition: Assign previous and current values
/// of the velocity from the velocity field specified via
/// the function pointer.
/// Values are assigned so that the velocities and accelerations
/// are correct for current time.
template<class ELEMENT>
void OscRingNStProblem<ELEMENT>::set_initial_condition()
 // Elastic wall: We're starting from a given initial state in which
 // the wall is undeformed. If set_initial_condition() is called again
 // after mesh refinement for first timestep, this needs to be reset.
dynamic_cast<PseudoBucklingRingElement*>(Wall_pt)->set_R_0(1.0);
 // Backup time in global timestepper
double backed_up_time=time_pt()->time();
 // Past history for velocities needs to be established for t=time0-deltat, \dots
 // Then provide current values (at t=time0) which will also form
 // the initial guess for first solve at t=time0+deltat
 // Vector of exact solution values (includes pressure)
 Vector<double> soln(3):
Vector<double> x(2);
 //Find number of nodes in mesh
 unsigned num_nod = fluid_mesh_pt()->nnode();
 // Get continuous times at previous timesteps
 int nprev_steps=time_stepper_pt()->nprev_values();
Vector<double> prev_time(nprev_steps+1);
 for (int itime=nprev_steps;itime>=0;itime-
  prev_time[itime] = time_pt() -> time(unsigned(itime));
 // Loop over current & previous timesteps (in outer loop because
 // the mesh might also move)
 for (int itime=nprev_steps;itime>=0;itime--)
  double time=prev_time[itime];
   // Set global time (because this is how the geometric object refers
   // to continous time
  time pt()->time()=time;
   cout « "setting IC at time =" « time « std::endl;
   // Update the fluid mesh for this value of the continuous time
   // (The wall object reads the continous time from the same
   // global time object)
   fluid mesh pt()->node update();
   // Loop over the nodes to set initial guess everywhere
   for (unsigned jnod=0; jnod<num_nod; jnod++)</pre>
     // Get nodal coordinates
     x[0]=fluid_mesh_pt()->node_pt(jnod)->x(0);
     x[1]=fluid_mesh_pt()->node_pt(jnod)->x(1);
     // Get intial solution
     (*IC_Fct_pt) (time, x, soln);
     // Loop over velocity directions (velocities are in soln[0] and soln[1]).
     for (unsigned i=0;i<2;i++)</pre>
       fluid_mesh_pt()->node_pt(jnod)->set_value(itime,i,soln[i]);
```

```
// Loop over coordinate directions
    for (unsigned i=0;i<2;i++)</pre>
      fluid_mesh_pt()->node_pt(jnod)->x(itime,i)=x[i];
     }
 // Reset backed up time for global timestepper
time_pt()->time()=backed_up_time;
/// Doc the solution
//----
template<class ELEMENT>
void OscRingNStProblem<ELEMENT>::doc_solution(DocInfo& doc_info)
ofstream some_file;
char filename[100];
// Number of plot points
 unsigned npts;
npts=5;
// Output solution on fluid mesh
sprintf(filename, "%s/soln%i.dat", doc_info.directory().c_str(),
        doc_info.number());
 //some_file.precision(20);
 some_file.open(filename);
unsigned nelem=fluid_mesh_pt()->nelement();
 for (unsigned ielem=0;ielem<nelem;ielem++)</pre>
  dynamic_cast<ELEMENT*>(fluid_mesh_pt()->element_pt(ielem))->
   full_output(some_file,npts);
 some_file.close();
 // Plot wall posn
sprintf(filename, "%s/Wall%i.dat", doc_info.directory().c_str(),
        doc_info.number());
 some_file.open(filename);
unsigned nplot=100;
 Vector<double > xi_wall(1);
 Vector<double > r_wall(2);
 for (unsigned iplot=0;iplot<nplot;iplot++)</pre>
   xi_wall[0]=0.5*Pi*double(iplot)/double(nplot-1);
   wall_pt->position(xi_wall,r_wall);
some_file « r_wall[0] « " " « r_wall[1] « std::endl;
 some_file.close();
 // Doc Sarah's asymptotic solution
sprintf(filename, "%s/exact_soln%i.dat", doc_info.directory().c_str(),
        doc info.number());
 some_file.open(filename);
fluid_mesh_pt()->output_fct(some_file,npts,
                      time_stepper_pt()->time_pt()->time(),
                      SarahBL::full_exact_soln);
some file.close();
 // Get position of control point
Vector<double> r(2);
Vector<double> xi(1);
xi[0] = MathematicalConstants::Pi/2.0;
wall_pt()->position(xi,r);
// Get total volume (area) of computational domain, energies and average
 // pressure
 double area=0.0;
double press_int=0.0;
 double diss=0.0;
double kin_en=0.0;
 nelem=fluid_mesh_pt()->nelement();
 for (unsigned ielem=0;ielem<nelem;ielem++)</pre>
  area+=fluid_mesh_pt()->finite_element_pt(ielem)->size();
  press_int+=dynamic_cast<ELEMENT*>(fluid_mesh_pt()->element_pt(ielem))
    ->pressure integral();
  diss+=dynamic_cast<ELEMENT*>(fluid_mesh_pt()->element_pt(ielem))->
   dissipation();
```

```
kin_en+=dynamic_cast<ELEMENT*>(fluid_mesh_pt()->element_pt(ielem))->
   kin_energy();
// Total kinetic energy in entire domain
double global_kin=4.0*kin_en;
// Max/min refinement level
unsigned min_level;
unsigned max level;
fluid_mesh_pt()->get_refinement_levels(min_level, max_level);
// Total dissipation for quarter domain
double time=time_pt()->time();
double diss_asympt=SarahBL::Total_Diss_sarah(time)/4.0;
// Asymptotic predictions for velocities at control point
Vector<double> x_sarah(2);
Vector<double> soln_sarah(3);
x_sarah[0]=Sarah_veloc_trace_node_pt->x(0);
x_sarah[1]=Sarah_veloc_trace_node_pt->x(1);
SarahBL::exact_soln(time, x_sarah, soln_sarah);
// Doc
« " " « r[1]
« " " « global_kin
            « " " « SarahBL::Kin_energy_sarah(time_pt()->time())
            « " " « static_cast<PseudoBucklingRingElement*>(Wall_pt)->r_0()
            « " " « press_int/area
            « " " « diss
            « " " « diss asympt
              " " « Veloc_trace_node_pt->x(0)
            « " " « Veloc_trace_node_pt->x(1)
            « " " « Veloc_trace_node_pt->value(0)
            « " " « Veloc_trace_node_pt->value(1)
            " " « fluid_mesh_pt() ->nelement()
              " " « ndof()
            « " " « min_level
              " " « max_level
            " " « fluid_mesh_pt()->nrefinement_overruled()
            " " « fluid_mesh_pt()->max_error()
            " " « fluid_mesh_pt()->min_error()
            " " « fluid_mesh_pt()->max_permitted_error()
              " " « fluid_mesh_pt()->min_permitted_error()
            « " " « fluid_mesh_pt() ->max_keep_unrefined()
              " " « doc_info.number()
            « " " « Sarah_veloc_trace_node_pt->x(0)
            " " « Sarah_veloc_trace_node_pt->x(1)
            « " " « Sarah_veloc_trace_node_pt->value(0)
            « " " « Sarah_veloc_trace_node_pt->value(1)
              " " « x_sarah[0]
            « " " « x_sarah[1]
            « " " « soln_sarah[0]
            « " " « soln_sarah[1]
            « static cast<PseudoBucklingRingElement*>(Wall pt)->r 0()-1.0
            « std::endl;
// Output fluid solution on coarse-ish mesh
// Extract all elements from quadtree representation
Vector<Tree*> all_element_pt;
fluid_mesh_pt()->forest_pt()->
 stick_all_tree_nodes_into_vector(all_element_pt);
// Build a coarse mesh
Mesh* coarse_mesh_pt = new Mesh();
//Loop over all elements and check if their refinement level is
//equal to the mesh's minimum refinement level
nelem=all_element_pt.size();
for (unsigned ielem=0;ielem<nelem;ielem++)</pre>
  Tree* el_pt=all_element_pt[ielem];
  if (el_pt->level() ==min_level)
    coarse_mesh_pt->add_element_pt(el_pt->object_pt());
   }
// Output fluid solution on coarse mesh
sprintf(filename, "%s/coarse_soln%i.dat", doc_info.directory().c_str(),
        doc_info.number());
some_file.open(filename);
nelem=coarse_mesh_pt->nelement();
for (unsigned ielem=0;ielem<nelem;ielem++)</pre>
  dynamic_cast<ELEMENT*>(coarse_mesh_pt->element_pt(ielem))->
   full_output(some_file,npts);
some file.close();
// Write restart file
sprintf(filename, "%s/restart%i.dat", doc_info.directory().c_str(),
        doc_info.number());
```

```
some_file.open(filename);
dump_it(some_file,doc_info);
some file.close();
/// Dump the solution
                    -----
template < class ELEMENT>
void OscRingNStProblem<ELEMENT>::dump_it(ofstream& dump_file,DocInfo doc_info)
 // Dump refinement status of mesh
//fluid_mesh_pt()->dump_refinement(dump_file);
 // Call generic dump()
Problem::dump(dump_file);
/// Read solution from disk
template<class ELEMENT>
void OscRingNStProblem<ELEMENT>::restart(ifstream& restart_file)
 // Refine fluid mesh according to the instructions in restart file
//fluid_mesh_pt()->refine(restart_file);
 // Rebuild the global mesh
 //rebuild_global_mesh();
 // Read generic problem data
Problem::read(restart_file);
// // Complete build of all elements so they are fully functional
// finish_problem_setup();
 //Assign equation numbers
 « std::endl« std::endl;
/// Driver for timestepping the problem: Fixed timestep but
/// guaranteed spatial accuracy. Beautiful, innit?
//----
template<class ELEMENT>
void OscRingNStProblem<ELEMENT>::unsteady_run(const unsigned& ntsteps,
                                           const bool& restarted,
                                           DocInfo& doc_info)
// Open trace file
char filename[100];
sprintf(filename, "%s/trace.dat", doc_info.directory().c_str());
Trace_file.open(filename);
 // Max. number of adaptations per solve
unsigned max_adapt;
 // Max. number of adaptations per solve
 if (restarted)
  max_adapt=0;
else
  max_adapt=1;
 // Max. and min. error for adaptive refinement/unrefinement
fluid_mesh_pt()->max_permitted_error()= 0.5e-2;
fluid_mesh_pt()->min_permitted_error()= 0.5e-3;
 // Don't allow refinement to drop under given level
 fluid_mesh_pt()->min_refinement_level()=2;
 // Don't allow refinement beyond given level
 fluid_mesh_pt()->max_refinement_level()=6;
 // Don't bother adapting the mesh if no refinement is required
 // and if less than ... elements are to be merged.
fluid_mesh_pt()->max_keep_unrefined()=20;
// Get max/min refinement levels in mesh
unsigned min_refinement_level;
 unsigned max_refinement_level;
 fluid_mesh_pt()->get_refinement_levels(min_refinement_level,
                                      max_refinement_level);
// Doc refinement targets
 fluid_mesh_pt()->doc_adaptivity_targets(cout);
 // Write header for trace file
 write_trace_file_header();
 // Doc initial condition
doc_solution(doc_info);
doc info.number()++;
 // Switch off doc during solve
doc_info.disable_doc();
```

```
// If we set first to true, then initial guess will be re-assigned
 // after mesh adaptation. Don't want this if we've done a restart.
bool first;
bool shift;
 if (restarted)
   first=false;
   shift=false;
   // Move time back by dt to make sure we're re-solving the read-in solution time_pt()->time()-=time_pt()->dt();
   first=true;
   shift=true;
 //Take the first fixed timestep with specified tolerance for Newton solver
 double dt=time_pt()->dt();
 unsteady_newton_solve(dt,max_adapt,first,shift);
 // Switch doc back on
doc_info.enable_doc();
 // Doc initial solution
 doc_solution(doc_info);
 doc_info.number()++;
 // Now do normal run; allow for one mesh adaptation per timestep
max_adapt=1;
 //Loop over the remaining timesteps
 for (unsigned t=2;t<=ntsteps;t++)</pre>
   // Switch off doc during solve
   doc_info.disable_doc();
   //Take fixed timestep
   first=false;
   unsteady newton solve(dt.max adapt.first);
   // Switch doc back on
   doc_info.enable_doc();
   // Doc solution
   //if (icount%10==0)
      doc solution (doc info);
      doc_info.number()++;
 // Close trace file
 Trace_file.close();
/// Write trace file header
template<class ELEMENT>
void OscRingNStProblem<ELEMENT>::write_trace_file_header()
 // Doc parameters in trace file
Trace_file « "# err_max " « fluid_mesh_pt()->max_permitted_error() « std::endl;
Trace_file « "# err_min " « fluid_mesh_pt()->min_permitted_error() « std::endl;
Trace_file « "# Re " « Global_Physical_Variables::Re « std::endl;
Trace_file « "# St " « Global_Physical_Variables::ReSt/
« fluid_mesh_pt()->min_refinement_level() « std::endl;
Trace_file « "# max_refinement_level "
Trace_file « ",\"min. refinement level\"";
Trace_file « ",\"# of elements whose refinement was over-ruled\"";
Trace_file « ",\"max. error\"";
Trace_file « ",\"min. error\"";
Trace_file « ",\"max. permitted error\"";
Trace_file « ",\"max. permitted error\"";
Trace_file « ",\"min. permitted error\"";
Trace_file « ",\"max. permitted # of unrefined elements\"";
Trace_file « ",\"doc number\"";
Trace_file « ",\"x<sub>1</sub><sup>(track2 FE)</sup>\\"";
Trace_file « ",\"x<sub>2</sub><sup>(track2 FE)</sup>\\"";
Trace_file « ",\"u<sub>1</sub><sup>(track2 FE)</sup>\\"";
```

```
Trace_file « ",\"u<sub>2</sub><sup>(track2 FE)</sup>\"";
Trace_file « ",\"x<sub>1</sub><sup>(track2 Sarah)</sup>\"";
Trace_file « ",\"x<sub>2</sub><sup>(track2 Sarah)</sup>\"";
Trace_file « ",\"u<sub>1</sub><sup>(track2 Sarah)</sup>\"";
Trace_file « ",\"u<sub>2</sub><sup>(track2 Sarah)</sup>\"";
Trace_file « ",\"u<sub>2</sub><sup>(track2 Sarah)</sup>\"";
Trace_file « ",\"u<sub>0</sub>-1\"";
Trace_file « std::endl;
/// Demonstrate how to solve OscRingNSt problem in deformable domain
/// with mesh adaptation
int main(int argc, char* argv[])
 // Store command line arguments
CommandLineArgs::setup(argc,argv);
//Do a certain number of timesteps per period
unsigned nstep_per_period=40; // 80; // ADJUST_PRIORITY
unsigned nperiod=3;
 // Work out total number of steps and timestep
unsigned nstep=nstep\_per\_period*nperiod;
double dt=1.0/double(nstep_per_period);
// Set up the problem: Pass timestep and Sarah's asymptotic solution for // generation of initial condition
OscRingNStProblem<AlgebraicElement<RefineableQCrouzeixRaviartElement<2> > >
 problem(dt,&SarahBL::full_exact_soln);
 // Restart?
 //----
bool restarted=false;
 // Pointer to restart file
 ifstream* restart_file_pt=0;
 if (CommandLineArgs::Argc!=2)
  cout « "No restart" « std::endl;
   restarted=false;
   // Refine uniformly
   problem.refine_uniformly();
   problem.refine_uniformly();
   problem.refine_uniformly();
   // Set initial condition on uniformly refined domain (if this isn't done
   // then the mesh contains the interpolation of the initial guess
   // on the original coarse mesh -- if the nodal values were zero in
   // the interior and nonzero on the boundary, then the the waviness of
   \ensuremath{//} of the interpolated i.g. between the nodes on the coarse mesh
   \ensuremath{//} gets transferred onto the fine mesh where we can do better
   problem.set_initial_condition();
 // Restart
else if (CommandLineArgs::Argc==2)
   restarted=true;
   // Open restart file
   restart_file_pt=new ifstream(CommandLineArgs::Argv[1],ios_base::in);
   if (restart_file_pt!=0)
     cout « "Have opened " « CommandLineArgs::Argv[1] «
      " for restart. " « std::endl;
   else
     std::ostringstream error_stream;
     error_stream \ll "ERROR while trying to open "
                   « CommandLineArgs::Argv[2]
« " for restart." « std::endl;
     throw OomphLibError(error_stream.str(),
                            OOMPH_CURRENT_FUNCTION,
                            OOMPH_EXCEPTION_LOCATION);
   // Do the actual restart
   problem.restart(*restart_file_pt);
 // Two command line arguments: do validation run
    (CommandLineArgs::Argc==3)
    nstep=3;
    cout « "Only doing nstep steps for validation: " « nstep « std::endl;
 // Setup labels for output
```

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```
DocInfo doc_info;
// Output directory
doc_info.set_directory("RESLT");
// Do unsteady run of the problem for nstep steps
problem.unsteady_run(nstep,restarted,doc_info);
// Validate the restart procedure
if (CommandLineArgs::Argc==3)
 // Build problem and restart
  // Set up the problem: Pass timestep and Sarah's asymptotic solution for
  // generation of initial condition
 OscRingNStProblem<AlgebraicElement<RefineableQCrouzeixRaviartElement<2> > >
  restarted_problem(dt,&SarahBL::full_exact_soln);
  \ensuremath{//} Setup labels for output
 DocInfo restarted_doc_info;
  // Output directory
  restarted_doc_info.set_directory("RESLT_restarted");
  // Step number
  restarted\_doc\_info.number()=0;
  // Copy by performing a restart from old problem
  restart_file_pt=new ifstream("RESLT/restart2.dat");
  // Do the actual restart
  restarted\_problem.restart(\star restart\_file\_pt);
  // Do unsteady run of the problem for one step
  unsigned nstep=2;
  bool restarted=true;
```

## 1.1 PDF file

A pdf version of this document is available.