Chapter 1

Demo problem: Solution of a Poisson problem in an "elastic" domain

Detailed documentation to be written. Here's a plot of the result and the already fairly well documented driver code...

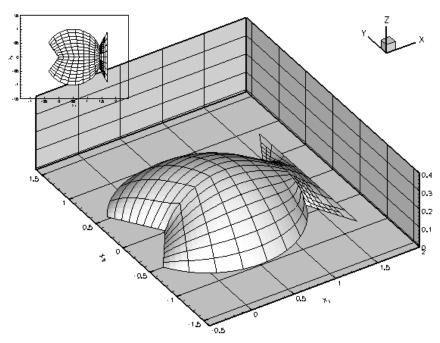


Figure 1.1 Adaptive solution of Poisson's equation in a fish-shaped domain for various `widths' of the domain. The update of the nodal positions in response to changes in the boundary shape is done by pseudo-elasticity.

```
//LIC// You should have received a copy of the GNU Lesser General Public
//LIC// License along with this library; if not, write to the Free Software
//LIC// Foundation, Inc., 51 Franklin Street, Fifth Floor, Boston, MA //LIC// 02110-1301 USA.
//LIC/
//LIC// The authors may be contacted at oomph-lib@maths.man.ac.uk.
//LIC//
// Solve Poisson equation in deformable fish-shaped domain.
// Mesh deformation is driven by pseudo-elasticity approach.
// Generic oomph-lib headers
#include "generic.h"
// Poisson equations
#include "poisson.h"
// Solid mechanics #include "solid.h"
// The fish mesh
#include "meshes/fish_mesh.h"
// Circle as generalised element:
#include "circle_as_generalised_element.h"
using namespace std;
using namespace oomph;
//-----
/// Namespace for const source term in Poisson equation
namespace ConstSourceForPoisson
 /// Strength of source function: default value 1.0
double Strength=1.0;
/// Const source function
 void get_source(const Vector<double>& x, double& source)
  source = -Strength;
 }
/// Refineable fish mesh upgraded to become a solid mesh
template<class ELEMENT>
class ElasticFishMesh : public virtual RefineableFishMesh<ELEMENT>,
                       public virtual SolidMesh
public:
 /// Constructor: Build underlying adaptive fish mesh and then
 /// set current Eulerian coordinates to be the Lagrangian ones.
 /// Pass pointer to geometric objects that specify the /// fish's back in the "current" and "undeformed" configurations,
 /// and pointer to timestepper (defaults to Static)
 // Note: FishMesh is virtual base and its constructor is automatically
 // called first! --> this is where we need to build the mesh;
 // the constructors of the derived meshes \operatorname{don'}\mathsf{t} call the
 // base constructor again and simply add the extra functionality.
ElasticFishMesh(GeomObject* back_pt, GeomObject* undeformed_back_pt,
                TimeStepper* time_stepper_pt=&Mesh::Default_TimeStepper) :
  FishMesh<ELEMENT>(back_pt,time_stepper_pt),
  RefineableFishMesh<ELEMENT>(back_pt,time_stepper_pt)
  // Mesh has been built, adaptivity etc has been set up -->
// assign the Lagrangian coordinates so that the current
// configuration becomes the stress-free initial configuration
  set_lagrangian_nodal_coordinates();
   // Build "undeformed" domain: This is a "deep" copy of the
   // Domain that we used to create set the Eulerian coordinates
   // in the initial mesh -- the original domain (accessible via
   // the private member data Domain_pt) will be used to update
  // the position of boundary nodes; the copy that we're
// creating here will be used to determine the Lagrangian coordinates
   // of any newly created SolidNodes during mesh refinement
  double xi_nose = this->Domain_pt->xi_nose();
double xi_tail = this->Domain_pt->xi_tail();
   Undeformed_domain_pt=new FishDomain(undeformed_back_pt,xi_nose,xi_tail);
   // Loop over all elements and set the undeformed macro element pointer
```

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unsigned n_element=this->nelement();
  for (unsigned e=0;e<n_element;e++)</pre>
    // Get pointer to full element type
    ELEMENT* el_pt=dynamic_cast<ELEMENT*>(this->element_pt(e));
    // Set pointer to macro element so the curvlinear boundaries
    // of the undeformed mesh/domain get picked up during adaptive
    // mesh refinement
    el_pt->set_undeformed_macro_elem_pt(
     Undeformed_domain_pt->macro_element_pt(e));
 /// Destructor: Kill "undeformed" Domain
virtual ~ElasticFishMesh()
  delete Undeformed_domain_pt;
private:
 /// Pointer to "undeformed" Domain -- used to determine the
/// Lagrangian coordinates of any newly created SolidNodes during
 /// Mesh refinement
Domain* Undeformed_domain_pt;
/// Global variables
//=====
namespace Global_Physical_Variables
 /// Pointer to constitutive law
ConstitutiveLaw* Constitutive_law_pt;
 /// Poisson's ratio
double Nu=0.3;
/// Solve Poisson equation on deforming fish-shaped domain.
/// Mesh update via pseudo-elasticity.
template<class ELEMENT>
class DeformableFishPoissonProblem : public Problem
public:
 /// Constructor:
DeformableFishPoissonProblem();
/// Run simulation
void run();
 /// Access function for the specific mesh
ElasticFishMesh<ELEMENT>* mesh_pt()
 {return dynamic_cast<ElasticFishMesh<ELEMENT>*>(Problem::mesh_pt());}
 /// Doc the solution
void doc_solution(DocInfo& doc_info);
 /// Update function (empty)
void actions_after_newton_solve() {}
    Update before solve: We're dealing with a static problem so
 /// the nodal positions before the next solve merely serve as
 /// initial conditions. For meshes that are very strongly refined
 /// near the boundary, the update of the displacement boundary
 /// conditions (which only moves the SolidNodes *on* the boundary),
 /// can lead to strongly distorted meshes. This can cause the /// Newton method to fail --> the overall method is actually more robust
 /// if we use the nodal positions as determined by the Domain/MacroElement-
/// based mesh update as initial guesses.
 void actions_before_newton_solve()
  bool update_all_solid_nodes=true;
  mesh_pt()->node_update(update_all_solid_nodes);
```

```
/// Update after adapt: Pin all redundant solid pressure nodes (if required)
 void actions_after_adapt()
  {
   // Pin the redundant solid pressures (if any)
   PVDEquationsBase<2>::pin_redundant_nodal_solid_pressures(
   mesh_pt()->element_pt());
private:
 /// Node at which the solution of the Poisson equation is documented
Node* Doc node pt:
 ofstream Trace_file;
 // Geometric object/generalised element that represents the deformable // fish back
ElasticallySupportedRingElement* Fish_back_pt;
};
//=----
template<class ELEMENT>
DeformableFishPoissonProblem<ELEMENT>::DeformableFishPoissonProblem()
 // Set coordinates and radius for the circle that will become the fish back
 double x_c=0.5;
 double y_c=0.0;
double r_back=1.0;
 // Build geometric object/generalised element that will become the
 // deformable fish back
 Fish_back_pt=new ElasticallySupportedRingElement(x_c,y_c,r_back);
 // Build geometric object/generalised that specifies the fish back in the
 // undeformed configuration (basically a deep copy of the previous one)
 GeomObject* undeformed_fish_back_pt=new
  {\tt ElasticallySupportedRingElement\,(x\_c,y\_c,r\_back);}
 // Build fish mesh with geometric object that specifies the deformable
 // and undeformed fish back
 Problem::mesh_pt()=new ElasticFishMesh<ELEMENT>(Fish_back_pt,
                                                  undeformed_fish_back_pt);
 // Choose a node at which the solution is documented: Choose
 // the central node that is shared by all four elements in
 // the base mesh because it exists at all refinement levels.
 // How many nodes does element 0 have?
 unsigned nnod=mesh_pt()->finite_element_pt(0)->nnode();
 // The central node is the last node in element 0:
\label{loc_node_pt=mesh_pt()-sinite_element_pt(0)->node_pt(nnod-1);} \\
 // Doc
 cout « std::endl « "Control node is located at: "
      « Doc_node_pt->x(0) « " " « Doc_node_pt->x(1) « std::endl « std::endl;
 // Set error estimator
 Z2ErrorEstimator* error_estimator_pt=new Z2ErrorEstimator;
mesh_pt()->spatial_error_estimator_pt()=error_estimator_pt;
 // Change/doc targets for mesh adaptation
 if (CommandLineArgs::Argc>1)
   mesh_pt()->max_permitted_error()=0.05;
   mesh_pt()->min_permitted_error()=0.005;
mesh_pt()->doc_adaptivity_targets(cout);
// Specify BC/source fct for Poisson problem:
 // Set the Poisson boundary conditions for this problem: All nodes are
 // free by default -- just pin the ones that have Dirichlet conditions
 // here.
 unsigned num_bound = mesh_pt()->nboundary();
 for (unsigned ibound=0; ibound<num_bound; ibound++)</pre>
   unsigned num_nod=mesh_pt()->nboundary_node(ibound);
   for (unsigned inod=0;inod<num_nod;inod++)</pre>
    {
    mesh_pt()->boundary_node_pt(ibound,inod)->pin(0);
    }
 // Set homogeneous boundary conditions for the Poisson equation
 // on all boundaries
 for (unsigned ibound=0; ibound<num_bound; ibound++)</pre>
   // Loop over the nodes on boundary
   unsigned num_nod=mesh_pt()->nboundary_node(ibound);
   for (unsigned inod=0;inod<num_nod;inod++)</pre>
     mesh_pt()->boundary_node_pt(ibound,inod)->set_value(0,0.0);
    }
```

```
/// Loop over elements and set pointers to source function
unsigned n_element = mesh_pt()->nelement();
 for (unsigned i=0;i<n_element;i++)</pre>
   // Upcast from FiniteElement to the present element
   ELEMENT *el_pt = dynamic_cast<ELEMENT*>(mesh_pt()->element_pt(i));
   //Set the source function pointer
   el_pt->source_fct_pt() = &ConstSourceForPoisson::get_source;
 // Specify BC/source fct etc for (pseudo-)Solid problem
 // Pin all nodal positions
 for(unsigned ibound=0;ibound<num_bound;ibound++)</pre>
   unsigned num_nod=mesh_pt()->nboundary_node(ibound);
for (unsigned inod=0;inod<num_nod;inod++)</pre>
     for (unsigned i=0;i<2;i++)</pre>
       mesh_pt()->boundary_node_pt(ibound,inod)->pin_position(i);
     }
    }
 //Loop over the elements in the mesh to set Solid parameters/function pointers
 for (unsigned i=0;i<n_element;i++)</pre>
   //Cast to a solid element
   ELEMENT *el_pt = dynamic_cast<ELEMENT*>(mesh_pt()->element_pt(i));
   // Set the constitutive law
   el_pt->constitutive_law_pt() =
    Global_Physical_Variables::Constitutive_law_pt;
 // Pin the redundant solid pressures (if any)
 PVDEquationsBase<2>::pin_redundant_nodal_solid_pressures(
 mesh_pt()->element_pt());
 //Attach the boundary conditions to the mesh
 cout « assign_eqn_numbers() « std::endl;
// Refine the problem uniformly (this automatically passes the // function pointers/parameters to the finer elements
refine_uniformly();
 // The non-pinned positions of the newly SolidNodes will have been
 // determined by interpolation. Update all solid nodes based on
 // the Mesh's Domain/MacroElement representation.
bool update_all_solid_nodes=true;
mesh_pt()->node_update(update_all_solid_nodes);
// Now set the Eulerian equal to the Lagrangian coordinates
mesh_pt()->set_lagrangian_nodal_coordinates();
/// Doc the solution
template<class ELEMENT>
void DeformableFishPoissonProblem<ELEMENT>::doc_solution(DocInfo& doc_info)
ofstream some_file;
char filename[100];
 // Number of plot points
unsigned npts = 5;
 // Call output function for all elements
 sprintf(filename, "%s/soln%i.dat", doc_info.directory().c_str(),
         doc_info.number());
some_file.open(filename);
mesh_pt()->output(some_file,npts);
some_file.close();
 // Write vertical position of the fish back, and solution at
 // control node to trace file
Trace_file
 « static_cast<Circle*>(mesh_pt()->fish_back_pt())->y_c()
« " " « Doc_node_pt->value(0) « std::endl;
/// Run the problem
template<class ELEMENT>
void DeformableFishPoissonProblem<ELEMENT>::run()
DocInfo doc_info;
 // Set output directory
doc_info.set_directory("RESLT");
// Step number
```

```
doc_info.number()=0;
 // Open trace file
char filename[100];
sprintf(filename, "%s/trace.dat", doc_info.directory().c_str());
Trace_file.open(filename);
Trace_file « "VARIABLES=\"y<sub>circle</sub>\",\"u<sub>control</sub>\""
              « std::endl;
  //Parameter incrementation
unsigned nstep=5;
for(unsigned i=0;i<nstep;i++)</pre>
   //Solve the problem with Newton's method, allowing for up to 2 //rounds of adaptation
   newton_solve(2);
    // Doc solution
   doc_solution(doc_info);
   doc_info.number()++;
   // Increment width of fish domain
   Fish_back_pt->y_c()+=0.03;
/// Driver for simple elastic problem.
/// If there are any command line arguments, we regard this as a
/// validation run and perform only a single step.
int main(int argc, char* argv[])
 // Store command line arguments
CommandLineArgs::setup(argc,argv);
//Set physical parameters
Global_Physical_Variables::Nu = 0.4;
 // Define a constitutive law (based on strain energy function)
Global_Physical_Variables::Constitutive_law_pt =
  new GeneralisedHookean(&Global_Physical_Variables::Nu);
  // Set up the problem: Choose a hybrid element that combines the
  // 3x3 node refineable quad Poisson element with a displacement-based
  // solid-mechanics element (for the pseudo-elastic mesh update in response
  // to changes in the boundary shape)
  DeformableFishPoissonProblem<
   {\tt RefineablePseudoSolidNodeUpdateElement < RefineableQPoissonElement < 2, 3>,}
   RefineableQPVDElement<2,3> >
  problem.run();
```

1.1 PDF file

A pdf version of this document is available.