# Supply response at the field-level: disentangling area and yield effects

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#### **Abstract**

Agricultural price supply response is thought to occur mainly through changes in acreage rather than through yield increase. Many studies find that yields respond weakly to prices, leading to the counter-intuitive idea that yields are insensitive to prices. In this paper, I argue that this result is likely due to the use of aggregated data: county- or state-level yields are averages, whose composition itself is affected by price changes. When area expansion is done by cultivating less fertile fields or by foregoing rotation, this composition effect reduces average yields, even if yields increase on each individual field.

To disentangle the effect of the intensive and composition effect on county-level yields, I run an analysis at the field level. Taking advantage of the availability of remotely-sensed crop choice and yield data for close to one million fields in the US Midwest, I to analyse response effects separately for fields in mono-culture and in rotation, and obtain estimates of the intensive versus rotational effects on yields. Using this measure, I will reconstruct county-level yields, and investigate the offsetting effects of intensive and rotational margin on aggregate yields.

# 1 Introduction

In his 1809 opus *On the Principles of Political Economy and Taxation*, Ricardo discussed the situation in which land of decreasing quality was set into production to respond to the demand of an increasing population. Although Ricardo's discussion focused on the impact of the price increase on land rents, it is interesting to note the implications concerning yields. If soil productivity differs importantly among the field classes, it is possible that average yields actually decrease after the price increase, despite a positive response of all fields. This *ecological fallacy*, where a relationship at the aggregate level needs not be representative for the relationship at the individual level<sup>1</sup>, stems from the fact that the aggregate yield variable is an average, whose composition itself changes. This makes interpretation

<sup>&</sup>lt;sup>1</sup>Ecological fallacy is the term used mainly in political science, see King (1997) for a classical treatment.

of the results ambiguous: when observing yield changes at the aggregate level only, it is not possible to infer whether these changes are due to changes in individual yields, or whether they are due to a composition effect of the average yield.

The lack of interpretability of aggregated data has been acknowledged in many studies such as Roberts et al. (2013), Beddow and Pardey (2015) or Miao et al. (2016), but remains so far unaddressed. As a typical example, Miao et al. (2016) find that the yield response to prices for soybeans is close to zero statistically, conceding however that this result "could also be indicative of the intensive [yield] and extensive margin [area] effects offsetting each other". As a result, it is difficult to draw policy-relevant implications from supply response analysis, for a same estimate could be obtained under very different scenarios.

In this study, I focus on the case of maize and soybeans in the US Midwest. While Ricardo's stylised fact of yields decreasing due to use of less fertile soils does not really hold in this case (the total surface devoted to corn and soybeans is pretty stable over time in the Midwest), yields decreases can happen here when expanding a crop by foregoing rotation. Rotation of corn and soybeans has been found to lead to a 2% to 10% increase in yields, and close to 5% savings in fertiliser application (Farmaha et al., 2016b). As acreage response to corn prices is rather high (Hendricks et al., 2014 find an elasticity of 0.4), this suggests the possibility of a decrease in county-level average yields.

To investigate this, I use field-level data derived from satellite observation, spanning the period 2000-2015. Using the crop data layer from USDA (Boryan et al., 2011), pixel-level yields estimates from Lobell and Azzari (2017) and fields boundaries, I obtain the yield and crop history for close to one million fields situated in the Corn Belt. This allows me to measure supply response at the field level, and to understand the composition effect in aggregate data.

# 2 Literature review

Methods to estimate supply response can be divided in two broad groups, structural approaches and empirical ones. In the structural approach, one seeks to estimate parameters of production or profit functions, and derive the elasticity based on theoretical relationships. On the other side, the empirical approach directly regress production, acreage or yield on a price variable. Choice of the method is often dictated by the type of available data: the structural approach is rather used with farm-level data, while the empirical approach relies more often on aggregate data. As a consequence,

the structural approach is found more often in studies in developing countries, where official data is rare and farm surveys are often undertaken by researchers. On the other side, most studies in the US for example rely on the empirical approach.

The structural approach is based on modelling the producer optimisation problem. This can be done either by estimating the production functions (primal approach) or profit functions (dual approach). It relies heavily on the choice of a specific functional form. A second important choice concerns whether one consider the farmer to be unconstrained regarding access to inputs and outputs. If the farmer is considered unconstrained, as is done for most studies in developed countries, standard theory from the firm applies. On the other side, studies focusing on developing countries introduce various constraints such as marketing, credit or labour limitations, leading to the so-called farm-household model (Singh et al., 1986). Endogeneity issues arise in the structural approach due to the so-called transmission problem and to unobserved productivity characteristics, so that instrumental variables are required.

The empirical approach is based on the work of Nerlove (1956), which investigates the response of expected output to expected prices:

$$A_t^{\star} = \beta_0 + \beta_1 \hat{P}_{t|t-1} + \epsilon_t \tag{1}$$

Where  $A_t^*$  refers to desired planted area, and  $\hat{P}_{t|t-1}$  refers to expectation at time t-1 of harvest price at time t. As neither expected area nor expected prices are observed, these need to be specified by the analyst. Effective area is usually specified as a distributed-lag adjustment between planned area  $A_t^*$  and past area  $A_{t-1}$ :

$$A_t = A_{t-1} + \gamma (A_t^* - A_{t-1}) \tag{2}$$

For the expected price, various assumptions have been used, ranging from extrapolative, adaptive, (quasi) rational, or the use of futures markets (see Nerlove and Bessler, 2001 for an extensive review). Nerlove initial specification was an adaptive expectation:

$$\hat{P}_{t|t-1} = \hat{P}_{t-1|t-2} + \delta(P_{t-1} - \hat{P}_{t-1|t-2})$$
(3)

Once the two processes specified, the Nerlove model leads to an estimable reduced-form where actual output depends on lags of actual output and lags of prices. The structural elasticity parameter

is then derived as a ratio of the reduced-form parameters.

In the original work of Nerlove (1956), only one of the two adjustments was assumed, and, by setting the other expected variable to its observed value (i.e. setting either  $A_t^* = A_t$  or  $\hat{P}_{t|t-1} = P_{t-1}$ ), this leads to the reduced form:

$$A_t = \alpha_0 + \alpha_1 P_{t-1} + \alpha_2 A_{t-1} + \nu_t \tag{4}$$

The short–run supply response parameter is simply  $\alpha_1$ , while the long-run parameter is  $\alpha_1/(1-\alpha_2)$ . Interestingly, the latter corresponds also to the structural supply response parameter  $\beta_1$  in the initial structural equation (1). An issue with the reduced-form (4) is that two different structural interpretations (adaptive expectation for prices and distributed lag adjustment for expected area) lead to the same reduced-form.<sup>2</sup> This implies that the two theories are *observationally equivalent*, rendering a structural interpretation of the parameters difficult. In his following book Nerlove (1958) considered the case where both expected variables were used (i.e. (2) and (3) are set into (1)), leading to an augmented reduced-form:

$$A_t = \alpha_0' + \alpha_1' P_{t-1} + \alpha_2' A_{t-1} + \alpha_3' A_{t-2} + \nu_t'$$
(5)

The long-run supply response parameter becomes now  $\alpha'_1/(1-\alpha'_2-\alpha'_3)$ . Although this version of the Nerlove model has the advantage of leading to a clearer interpretation of the structural parameters, the simpler version with only one lag of the dependent variable has been mostly used.

Subsequent changes of the model have focused mainly on specifying the price expectation process (3). Eckstein (1984, 1985) shows that a rational expectation model leads to the same reduced-form representation as in the simple Nerlove reduced-form (4). Gardner (1976) suggested using futures prices as proxy for the expected prices. Under this approach, the price equation does induce a lag of acreage in the reduced-form, although the lag may be introduced assuming a partial adjustment process for acreage.

Statistical estimation of the reduced-form faces several issues. Nerlove (1958) pointed out that residuals were serially correlated, and suggested several approaches to deal with this. Brandow (1958) criticised the fact that the simple Nerlove model did not include exogenous controls, which can introduce omitted variable bias. Another concern, raised by Braulke (1982), is the potential multi-

<sup>&</sup>lt;sup>2</sup>Note however that the dynamic properties of the  $v_t$  term differ depending on the structural model, which could inform a test to discriminate between the two theories.

collinearity between  $A_{t-1}$  and  $P_{t-1}$ . Diebold and Lamb (1997) discuss the fact that the long-term parameter is a ratio of coefficients, which causes the estimator to have infinite moments and be bimodal. Addition of a lagged dependent variable also introduces bias in the estimation, leading even to inconsistent estimates in the panel case (Nickell, 1981). While the issue is usually ignored in the standard case, it has been addressed in the panel case using Arellano and Bond (1991) GMM estimator (Haile et al., 2016; de Menezes and Piketty, 2012). The GMM approach consists in using the second lag of the dependent variable as instrument, which is highly problematic in this context since some formulations of the Nerlove model imply the presence of the second lag as explanatory variable, condradicting the exclusion restriction.

Concerns about the endogeneity of the price and error term have received more recent attention (Choi and Helmberger, 1993; Roberts and Schlenker, 2013; Hendricks et al., 2015). Roberts and Schlenker (2013) focused on aggregate total supply  $Q_t$ , and argued that yield shocks can be correlated to prices. To summarise and simplify the argument, let  $Q_t = A_t \cdot Y_t$  (where  $A_t$  and  $Y_t$  are respectively acreage and yield), and taking logs:  $q_t = a_t + y_t$ , where lower case letters denote variable in logs. Yield is decomposed into a long term  $(y_t^{LT})$  and short term deviation  $(y_t^{ST})$  component, also interpreted as yield shock. The latter can be further decomposed into a predictable and an unpredictable component,  $y_t^{ST} \equiv \hat{y}_{t|t-1}^{ST} + \hat{y}_t^{ST}$ . Assuming that yield deviations are exogenous to prices, and using futures prices as in Gardner (1976), leads to following model:

$$q_t = \alpha + \beta p_{t|t-1} + y_t^{LT} + \hat{y}_{t|t-1}^{ST} + \tilde{y}_t^{ST} + \nu_t = \alpha + \beta p_{t|t-1} + \tilde{\nu}_t$$
 (6)

Endogeneity arises if the futures price adjusts to yield trends or predictable yield deviations, i.e. if  $p_{t|t-1} = f(y_t^{LT}, \hat{y}_{t|t-1}^{ST})$ . If this is the case, estimation of production on price alone will suffer from the omitted asymptotic variable issue. As prices are likely negatively correlated with yield shocks, this will lead to under-estimation of the true parameter.

Roberts and Schlenker (2013) suggested adding  $y_t^{ST}$  in the main equation,<sup>3</sup> and using  $y_{t-1}^{ST}$  as instrumental variable, arguing that the storage model ensures that past yield shocks affect current production only through prices (due to carry-over from the previous year). This is possible under the assumption that past yield shocks do not influence present shocks.

<sup>&</sup>lt;sup>3</sup>The term  $y_t^{LT}$  is also implicitly taken into account by using a time spline in the main equation.

Rotation The benefits of rotating maize and soybeans are multiple, and subject to some discussion in the agronomy literature (Farmaha et al., 2016a). Rotation mechanisms operate mainly through a reduction in pests and fixation of nitrogen by soybeans. The effects of rotation are a boost in yields, as well as reduced need of nitrogen. Estimates of the yield boost vary among studies. Porter et al. (1997) study a small sample of experimental plots in Minnesota and Wisconsin, and report a 15% increase in maize yields when previously cropped with soybeans, with some heterogeneity where lower-yielding fields see a higher increase, close to 25%. Similar numbers were obtained for soybeans. Another set of experimental data, used by Hennessy (2006) and Livingston et al. (2015), suggests rotation effects increasing yields for both crops by 25%. Farmaha et al. (2016a) on the other side use observational data from high-productivity irrigated fields in the western U.S. Corn Belt. They find lower rotation effects, from 2%-5% for maize and 6% to soybeans. Data on fertiliser use indicated that producers were reducing the amount of nitrogen by 6%. All these papers note that maize shows a one-year memory, i.e. there will be no difference between a  $\langle SSM \rangle$  and  $\langle MSM \rangle$  sequence. On the other side, soybeans is usually found to exhibit a two-years memory, fields with two previous years of maize  $(\langle MMS \rangle)$  giving higher yields than fields with one year of maize and soybeans previously  $(\langle SMS \rangle)$ .

### 3 Model

### 3.1 Individual supply in presence of rotation effects

Rotation effects in production functions have been modelled in various ways, with the main differences being in the way the rotation effects are taken into account, and in the way dynamics are introduced. An early strand of literature used mathematical programming to derive optimal rules in a static framework, see El-Nazer and McCarl (1986) or Musser et al. (1985). Dynamic programming methods based on Bellman equations have been used, see Thomas (2003) on the crop choice in presence of nitrogen carry-over, or Livingston et al. (2015); MacEwan and Howitt (2011) specifically on rotations.

Rotation effects on yields at the individual level are not always modelled explicitly in the literature, with examples like Livingston et al. (2015) using vague *adjustment factors* coefficients in the revenue equation. Hennessy (2006) on the other side provides a clear modelling framework of rotation effects, which I will use from now on.

Hennessy (2006) considers two effects of rotation, the *input saving* effect  $\alpha$  and the *yield boost* effect

 $\beta$ . The input saving effect arises from nutrient carry-over from the previous period(s), and is assumed to be perfectly substitutable with chemical fertiliser. This implies that the total amount of nutrient  $n_t$  for crop is equal to the sum of chemical fertiliser  $F_t$  and the input-saving effect  $\alpha$ ,  $n_t = F_t + \alpha$ . Further, this input-saving effect depends on the type of crop succession, which we will write as  $\alpha^i_j$ , i.e. when crop i follows crop j, leading to  $n^i_t = F^i_t + \alpha^i_j$ . The second effect of crop rotation is the yield *boost effect*  $\beta^i_j$  (for crop i following crop j), which is assumed to enter additively. These two elements lead to the following yield production function:

$$Y(F, i, j) = y^{i}(F_t^{i} + \alpha_j^{i}) + \beta_j^{i}$$

Given that crop j was planted at previous period t-1, crop  $i^*$  is chosen for period t if  $\pi^{i^*}(p,w,i^*,j) > \pi^i(p,w,i,j) \forall i \neq i^*$ , where  $\pi^i$  is the profit function for crop i depending on the output price p and fertiliser price p. Hennessy (2006) makes the critical assumption that both the input-saving  $\alpha^i_j$  and yield boost  $\beta^i_j$  effects do not depend on previous level of nutrient  $n_{t-1}$  or on actual level of fertiliser p. While this restrictive assumption departs from the nitrogen carry-over literature, it has the advantage of alleviating the need for dynamic programming tools. Furthermore, it allows us to focus on our question of interest, yield supply response in the short term, for a given crop choice.

An important implication of the perfect substitutability assumption between input saving  $\alpha$  and chemical fertiliser is that the optimal nutrient level  $n_t^*$  does not depend on the previous crop status.<sup>5</sup> This in turn implies that the difference in yield for crop i between rotation  $\langle ji \rangle$  or rotation  $\langle ki \rangle$  is equal to the difference in respective yield boosts, i.e.  $\tilde{Y}(p,w,i,j) - \tilde{Y}(p,w,i,k) = \beta_j^i - \beta_k^i$ . A further consequence of the previous result is that yield response to prices will be the same, irrespective of the rotation status.

It is important to note under which conditions this result was obtained. Firstly, the implicit assumption here is that there are no credit or liquidity constraint, so that a farm-firm model can be used, instead of a farm-household one. Consequences of relaxing this assumption are outside the scope of this paper, but seem promising for a developing country case, testing for example the implication of credit or fertiliser subsidy programs on rotation patterns.

<sup>&</sup>lt;sup>4</sup>Thomas (2003) uses for example a specification similar to  $\alpha_i^i = m^j(n_{t-1})$ .

<sup>&</sup>lt;sup>5</sup>To see this, note that, for two different previous crops j or k, first order conditions  $y'(F_j^{*i} + \alpha_j^i) = w/p$  and  $y'(F_k^{*i} + \alpha_k^i) = w/p$  will both lead to the same available nutrient  $n_t^* = F_j^{*i} + \alpha_j^i = F_k^{*i} + \alpha_j^k$ .

# 3.2 Aggregate supply: a simple Ricardian model

Moving on now to aggregate supply, I analyse now a model with farm heterogeneity, and its impact on aggregate supply. To get intuition for the composition effect, I describe here the simple *Ricardian* case, where land of lower quality gradually enters production. The yield function is  $y(p,\theta)$ , and depends on prices p and land quality  $\theta$ . Land quality is assumed to be increasing in  $\theta$ , so that yields increase with  $\theta$ , i.e.  $\partial y(p,\theta)/\partial \theta>0$ . Yields respond positively to prices, assuming a standard positive intensive margin response. Let  $\theta^*(p)$  be the level at which cultivating is non-negative, i.e.  $\pi(\theta^*,p)=0$ . Fields with higher land quality  $\theta\geq\theta^*$  enter production, while fields with lower quality  $(\theta<\theta^*)$  do not produce. An increase in prices reduces the minimum quality threshold  $(\frac{d\theta^*(p)}{p}<0)$ , inducing more fields to enter production. Let further  $f(\theta)$  be the density of  $\theta$ , and  $F(\theta)$  its cumulative distribution function. Normalizing the land quality over the [0,1] interval, the average yield is given by:

$$\bar{y}(\theta^{\star}(p), p) = \int_{\theta^{\star}(p)}^{1} f(\theta) y(p, \theta) d\theta / (1 - F(\theta^{\star}(p)))$$

Figure 1 gives a simple illustration of the Ricardian model. In the first panel, the distribution of the land quality  $\theta$  is shown. The minimum land-quality  $\theta^*(p)$  is set at the value of 0.6: all fields with  $\theta > \theta^*$  produce (i.e.  $1 - F(\theta^*(p))$  fields produce). The second panel shows the yield function and average yield  $\bar{y}(\theta^*(p), p)$ .

The derivative of average yields with respect to prices is (see appendix A.1 for the full derivation):

$$\frac{\partial \bar{f}(p)}{\partial p} = \frac{\int_{\theta^{\star}}^{1} f(\theta) \frac{\partial y(p,\theta^{\star})}{\partial p} d\theta (1 - F(\theta^{\star})) + f(\theta^{\star}(p)) \frac{d\theta^{\star}(p)}{dp} \left[ \int_{\theta^{\star}}^{1} f(\theta) [y(p,\theta^{\star}) - y(p,\theta)] d\theta \right]}{(1 - F(\theta^{\star}))^{2}}$$
(7)

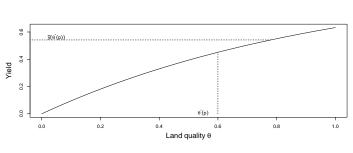
The first term in the numerator represents the intensive margin response, and corresponds to the average response of fields already producing. Under the standard assumption of positive individual supply response  $\frac{\partial y(p,\theta)}{\partial p}>0$ , this term is positive. The second term corresponds to the composition effect of the extensive margin. It is composed of the (weighted) acreage response term  $\frac{d\theta^{\star}(p)}{dp}$  multiplied by the average yield difference among producers  $\int_0^{\theta^{\star}} f(\theta)[y(p,\theta^{\star})-y(p,\theta)]d\theta$ . With the assumption of yields increasing in  $\theta$  ( $\frac{\partial y(p,\theta)}{\partial \theta}<0$ ), and of entry of lower quality land ( $\frac{d\theta^{\star}(p)}{p}<0$ ), we have that

So Not-Maize Maize

Land quality θ

0.8

Figure 1: Ricardan model: continuous version  $\mbox{(a) Distribution of } \theta$ 



(b) Productivity and average yield at  $\bar{p}$ 

 $y(p, \theta^*) < y(p, \theta) \quad \forall \theta < \theta^*$ , so that the second term is negative.

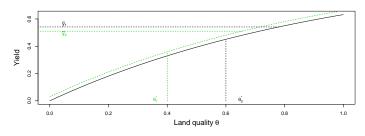
This formula formalises the decomposition of the aggregate response into the average positive response of *incumbent* producers, and the composition effect due to the entry of new producers. As these new producers have lower yields, the composition effect reduces the aggregate response.

Whether the overall impact of the price increase will be negative or positive depends on the respective strength of the intensive and extensive margins. Figure 2 illustrates two possible cases. The first panel shows a case where there is a strong intensive margin (displacement of the curve) and small extensive one (new point  $\theta^*(p')$ ). The resulting average yield is higher than before. The second panel depicts the opposite situation, wherea weak intensive and strong extensive margin responses lead to a decrease in the average yield.

Extension of the theoretical model to the case where land expansion comes from rotation instead of a Ricardian marginal land can be made following the same idea. Hendricks et al. (2014) assume that rotation cases are naturally ordered over a *corn-propensity* index  $\theta$ . Fields with lowest propensity  $\theta < \theta^1$  are cultivated to soybeans in monoculture ( $\langle S \rangle$ ), fields with intermediate propensity  $\theta^1 \leq \theta < \theta^2$ 

Figure 2: Effect of a price increase

(a) Large intensive margin, low extensive



(b) Low intensive margin, high extensive

 $\theta^2$  are cultivated in rotation ( $\langle SM \rangle$ ), while fields with high propensity  $\theta^2 \leq \theta$  are cultivated to corn in monoculture ( $\langle M \rangle$ ). See Figure 7 on Page 28 for an illustration. The assumption here is that there is no direct switching from  $\langle S \rangle$  fields to  $\langle M \rangle$  fields. This assumption seems constraining, but in practice it does not appear to be very restrictive, as few fields are found to follow such transition. In such a scenario, an increase in corn prices will lower the two thresholds  $\theta^1$  and  $\theta^2$ , increasing the share of corn-monoculture fields  $\langle M \rangle$ , and decreasing the share of soy-monoculture fields  $\langle S \rangle$ . The effect on the share of rotating fields  $\langle SM \rangle$  on the other side is ambiguous, and depends on the (weighted) changes in  $\theta^1$  and  $\theta^2$ .

Turning now to the assumption on the productivity along the corn-propensity  $\theta$  dimension, I assume now that it follows the production function discussed in Sectio 3.1. That is, rotating fields will benefit from the yield boost  $\beta$  and fertiliser-saving  $\alpha$ . In that case, a price increase will increase the share of fields without rotation effects (due to the change from  $\langle SM \rangle$  to  $\langle M \rangle$ ). However, the loss in  $\langle SM \rangle$  will be partially compensated by the gain in  $\langle SM \rangle$  due to a decrease in  $\langle S \rangle$  fields. That is, contrary to the Ricardian case, in the rotation case, the composition effect itself is not necessarily negative. It is worth coming back to the model's restriction that  $\langle S \rangle$  fields can only transition to  $\langle SM \rangle$ , and not to  $\langle M \rangle$ . This restriction turns out to affect only effects at long term, which I have not discussed

so far. Indeed, whether a  $\langle S \rangle$  turns in period 2 into the  $\langle SM \rangle$  or  $\langle M \rangle$  type will not change the share of M fields in period 2, nor will change the amount of fields with rotation benefits at period 2. It is only considering a longer horizont that the distinction will matter.

# 3.3 Comparing individual and aggregate response: a decomposition

Estimating a benchmark aggregate model as discussed in 5.2.1 will set the basis for comparing the yield response at the aggregate (macro) and individual (micro) level, and test my research hypothesis that the macro intensive margin under-estimates the micro intensive margin due to a micro extensive margin response. Intuitively, the difference between micro and macro estimate should correspond to the acreage response, as suggested by the decomposition (7) in Section (3.2). Such a raw decomposition suffers however from the fact that there are other reasons why the macro estimator differs from the micro one: aggregation bias due to heterogeneity of the coefficients (Hendricks et al., 2014), aggregation bias due to mis-specification of the functional form<sup>6</sup>, endogeneity bias and simple sampling variation all suggest that these estimators should differ.

To allow for a more precise comparison of the estimates, I decompose here the aggregate intensive margin response into its individual intensive and extensive components. This provides a way to obtain macro response based on the micro parameters only. These micro-based macro estimates will then be compared to the ones obtained from the benchmark model, testing the hypothesis that these estimates are equal. Obtaining similar estimates form the two methods would prove useful, as it could justify using the decomposition at a more disaggregated level, investigating for example the presence of spatial heterogeneity in the intensive and extensive margin.

Rewrite the crop choice variable  $c_{it}$ , attributing value of 1 for maize, and 0 for soybeans. Denote field area by  $a_i$ , and total maize acreage by  $A_t^M = \sum_i a_i c_{it}$ ,  $A_t^S = \sum_i a_i (1 - c_{it})$ . The short term response is given by:<sup>7</sup>

$$\partial A_t^M / \partial p_t^M = \sum_i a_i (c_{i,t-1} \beta_{MM}^A + (1 - c_{i,t-1}) \beta_{SM}^A) = A_{t-1}^M \beta_{MM}^A + A_{t-1}^S \beta_{SM}^A$$

The average maize yield  $\bar{y}_t^M$  is decomposed into average yield from rotations  $\langle M \rangle$  and from sequences  $\langle S \to M \rangle$ ,  $\bar{y}_t^M = \alpha_t^{MM} \bar{y}_t^{MM} + \alpha_t^{SM} \bar{y}_t^{SM}$ .  $\alpha_t^{SM}$  is the share of the area devoted to  $\langle S \to M \rangle$ 

<sup>&</sup>lt;sup>6</sup>Remember that the specification of the benchmark model is obtained under the assumption of equal response between rotating and non-rotating fields.

<sup>&</sup>lt;sup>7</sup>See Hendricks et al., 2014, page 1479.

sequences over total area cultivated to maize, i.e.  $\alpha_t^{SM} \equiv \frac{A_t^{SM}}{A_t^{MM} + A_t^{SM}} = \frac{A_t^{SM}}{A_t^{M}}$ . Differentiating this average yield with respect to prices gives:

$$\begin{array}{ll} \frac{\partial \bar{y}_{t}^{M}}{\partial p_{t}^{M}} &= \alpha_{MM} \frac{\partial \bar{y}_{t}^{MM}}{\partial p_{t}} &+ \alpha_{SM} \frac{\partial \bar{y}_{t}^{SM}}{\partial p_{t}^{M}} + \frac{\left[\partial A_{t}^{SM}/\partial p_{t} \cdot A_{t}^{MM} - \partial A_{t}^{MM}/\partial p_{t} \cdot A_{t}^{SM}\right] \bar{y}_{t}^{SM}}{(A_{t}^{M})^{2}} \\ &+ \frac{\left[\partial A_{t}^{MM}/\partial p_{t} \cdot A_{t}^{SM} - \partial A_{t}^{SM}/\partial p_{t} \cdot A_{t}^{MM}\right] \bar{y}_{t}^{MM}}{(A_{t}^{M})^{2}} \end{array}$$

Given the linearity assumptions made in the crop choice and yields equations (9) and (10), one gets (see Appendix A.2):

$$\frac{\partial \bar{y}_{t}^{M}}{\partial p_{t}^{M}} = \beta_{M}^{\gamma} + \alpha_{SM}\gamma + \frac{\alpha_{SM}A_{t-1}^{M}\beta_{MM}^{A} - \alpha_{MM}A_{t-1}^{S}\beta_{SM}^{A}}{A_{M}} \cdot (\bar{y}_{MM} - \bar{y}_{SM}) \tag{8}$$

The first two terms represent the individual intensive margin response, allowing for a possibly different response from  $\langle S \to M \rangle$  fields compared to  $\langle S \to M \rangle$  ones. The last term represents the *composition* effect, and is composed of the yield differential  $\bar{y}_{MM} - \bar{y}_{SM}$  and area response. The yield differential  $\bar{y}_{MM} - \bar{y}_{SM}$  corresponds to the average yield boost loss. The area response is a function of the actual share of each type and their supply response. This decomposition illustrates the claim that aggregate intensive response encompasses both the individual intensive and extensive margins.

# 4 Crop and yield data

To conduct an analysis at the field-level, I assemble data from three main sources: a crop classification at the pixel level, a yield map for the corresponding corn ans soybeans pixels, and a field boundary dataset. Figure 3 illustrates the three datasets combined. The first panel shows the CDL classification, together with the field boundaries. The second panel shows the yield predictions for the pixels for which the CDL predicts maize. The third panel shows the soybeans yield predictions.

# 4.1 Crop classification

The crop data comes from the USDA Crop Data Layer (CDL) dataset (Boryan et al., 2011). The CDL classifies Landsat pixels of  $30m \times 30m$  into a large number of classes. The accuracy of the classification

Malze Yields
Soy Yields

Figure 3: Illustration of the CDL, yield and boundary data

for maize and soybeans in the Corn Belt is very high, in general above 95%. Corn and soybeans appear in multiple distinct classes, including categories such as corn and soybeans only, but also double-crop categories such as "Winter Wheat and Corn" or "Soybeans and Cotton". Due to the small share of the alternative classes, I focus on the main corn and soybeans categories.

# 4.2 Yield data

The yield predictions are based on the scalable satellite-based crop yield (SCYM) method of Lobell et al. (2015). The underlying idea of the method is to use an agronomic crop model to obtain predictions of yield and a vegetation index. The vegetation index chosen is a variant of the NDVI, called the Green Chlorophyll Vegetation index (GCVI), which can also be observed with a satellite. Predictions from the agronomic model serve as variables in a regression of yields on GCVI and weather variables. The regression coefficients are then used to obtain out-of-sample yield predictions based on the remotely sensed GCVI and the local weather variables.

The advantage of this method is that it does not make use of ground data for calibration purpose. When ground data is available, it can be used as validation, leading to out-of-sample (i.e. test) measure of fit, instead of in-sample measures (training). Lobell et al. (2015) test the accuracy of their maize and soybeans predictions in Illinois, Iowa and Indiana using data for ~10'000 fields obtained

<sup>&</sup>lt;sup>8</sup>See https://www.nass.usda.gov/Research\_and\_Science/Cropland/metadata/meta.php

 $<sup>^9</sup>$ As such, the comparisons of  $R^2$  between SCYM and direct calibrated regression in Lobell et al. (2015); Burke and Lobell (2017) are not valid as they compare training and tests  $R^2$ .

from the USDA Risk Management Agency. They find prediction  $R^2$  between 0.14 and 0.58 for the state-year maize pairs, while the  $R^2$  on the full sample is 0.35. Predictions for soybeans are less accurate, ranging between 0.03 and 0.5. Prediction bias in  $Y^{True} = \alpha + \beta \hat{Y} + \epsilon$  arises both in the intercept and slope, although there is no clear tendency in over- or under-estimation of the values. Disaggregation of the bias suggests that it is commodity, year and state specific. Farmaha et al. (2016c) use the SCYM method in Nebraska in a study on yield gap, and obtain predictions  $R^2$  ranging from 0.12 to 0.34, with a tendency to over-estimate yield. Lobell and Azzari (2017) use also the SCYM method to study yield heterogeneity at the county level. They predict field-level yield for maize and soybeans in Illinois, Iowa and Indiana, from 2000 to 2015. Averaging their yield prediction at the county level, they find  $R^2$  of 0.67 and 0.74 for maize and soybeans respectively when comparing these with USDA county estimates. The SCYM is found to over-estimate yields, with larger bias at higher yields. The authors use then the USDA county averages to calibrate their data.

### 4.3 Field boundaries

An issue with the CDL data is that the analysis is done at the pixel-level, while we are interested in field-level analysis. There exists however a dataset of fields boundary, the USDA Common Land Unit (CLU).<sup>10</sup> Unfortunately, the actual dataset is not publicly available, so that only a copy of the 2009 version can be used.

Two issues arise when using this dataset. Firstly, as the data is from 2009, fields boundaries may have changed. Drastic changes are unlikely, but cultivation of two different crops in the same field is possible. The second issue is that given that the CDL analysis is at the pixel level, instead of being at the field level, pixels in a field can contain multiple crop classes. Preliminary investigations showed clear cases of border contamination, where pixels at the edge of the field were attributed other classes (in particular classes corresponding to bush/forest elements).

These two issues call for specific rules for the attribution of a crop to a given field. Hendricks et al. (2014) used a *centroid-offset* rule, where the field's class is attributed according to the class of the pixel that lies at a certain distance of the field's centroid. This procedure suffers from two issues: firstly, it is not guaranteed that the centroid offset falls within the field itself. Second, if there are really two crops cultivated in one field, the method will attribute only one class. Arguably, the arbitrariness of the offset rule should guarantee that there is no bias in which class will be chosen.

 $<sup>^{10}</sup> https://www.fsa.usda.gov/programs-and-services/aerial-photography/imagery-products/common-land-unit-clu/index$ 

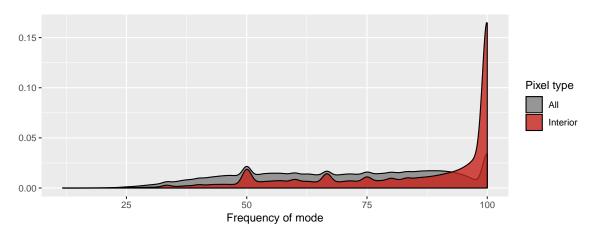


Figure 4: Agreement of pixel classification, over all fields, 2015 data

Another method is followed by Stevens (2015), who selects the mode of the classes found within a field. This method does not suffer from the issue of the centroid falling outside the field, yet also can attribute one class whenever there are actually two. To avoid this issue, I focus on fields with a relatively high classification agreement, i.e. I set a minimum threshold on the frequency of the mode. Further, I only take into account for this calculation interior pixels, i.e. pixels that do not touch the border of the field. This avoids to consider mixed-pixels, that are potentially contaminated by elements outside of the field.

Figure 4 shows the frequency of the mode, with either all pixels taken into account, or only the interior ones. This is made for all plots in the nine states, using CDL classification for 2015. It is interesting to see that although the field boundaries were made in 2009, there is still a relatively good agreement for the year 2015. One can see that taking only interior pixels instead of all pixels leads to a much better result: a much larger proportion of the fields have 90% or more of the pixels showing the same value. One see furthermore a few bumps around the value of 50%, 66% and 75%. This suggests that the field was planted to two distinct crops (or more), using either a 1/2, 1/3 or 1/4 proportion.

To retain only fields with a good classification accuracy, the threshold was set at a minimum of 85% over all years considered (2008-2015). This is arguably a rather strict value, but it ensures that the data considered is how high quality. This is particularly important for the yield data, for which we want to make sure that we are not averaging over contamined pixels, which can have a drastic effect on the final yield estimate. In fact, using the high-classification quality fields only, the correlation between NASS county yields and averages from the SCYM dataset is improved.

#### 4.4 Weather data

Weather variables are introduced as control variables to avoid omitted variable bia. While it is reasonable to think that weather is not influenced by prices, it is still the case that prices might anticipate weather events later in the season. To prevent this, I include a large set of weather controls from the DAYMET dataset (Thornton et al., 2017), which is at a resolution of  $1000m \times 1000m$ . The dataset includes precipitation, minimum and maximum temperatures, as well as partial pressure of water vapor. These daily measures are averaged per month, and squared terms are included. Growing degree days (GDD) will be included later on, following the work of Schlenker and Roberts (2006, 2009).

### 4.5 Price variables

Price variable  $p_{it}^M$  and  $p_{it}^S$  are futures quotations for post-harvest delivery (December for maize and November for soybeans), quoted pre- and in-season. The pre-planting period is defined to be the month of February and March. This is chosen earlier than actual planting times which are Mid April to May for maize, and May to June for soybeans. Given that the choice of crop is almost only between maize and soybeans, the planting period relevant to maize is also the one relevant for soybeans. Finally, this is also the period chosen by Hendricks et al. (2014). The pre-planting price is also relevant for the yield equation, as farmers can influence yields by choosing specific types of hybrids or the sowing densities. Later on, I shall include as well a post-planting price, which shall be defined as the May-June period. This is intended to reflect within season adjustments, such as fertiliser application. Given the sunk costs already supported, it is expected that post-planting price changes will have a smaller effect compared to pre-planting ones in the yield equations.

Futures prices are adjusted for the local basis, which is taken as the difference between the closest delivery futures price and the local spot price at neighbouring elevator. The basis is measured at the same period that the price is defined, i.e. for pre-planting prices, I use an average of February-March futures (for the December maturity) and an average of the basis at the same period.

The cash prices were obtained from elevator data found in Bloomberg<sup>11</sup>. I end up with a dataset of close to 2000 elevators points. Data at the field level is obtained by spatial interpolation from neighbouring elevators. I use inverse distance weighting; interpolation parameters are obtained by cross-validation. It might be objected that possible transportation costs should be considered, taking

<sup>&</sup>lt;sup>11</sup>Bloomberg disseminates data originally collected by Data Transmission Network and Geograin. Data was geo-located, and databases were consolidated, averaging quotations over close vicinities.

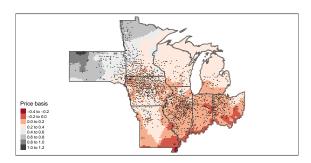


Figure 5: Location of elevators and basis interpolation (corn, March 2014)

for example at distance to the elevator. However, given that I use a fixed-effects strategy at the field-level, there is no need for such an adjustment, as it will get absorbed by the fixed-effects.

Figure 5 shows the location of the grain elevators and a smooth representation of the local basis. The location of the elevators follows closely where corn and soybneans are planted, compare with Figure 6 on Page 27.

On ethanol refineries There is an extensive literature (see Motamed et al., 2016 for references) finding that ethanol refineries have an impact on local maize acreage response. Motamed et al. (2016) for example find that the elasticity of maize acreage with respect to local refining capacity is about 1.5. As local refineries are likely related to the price variable, this suggests that one should add a refinery vicinity variable to avoid omitted variable bias. This however raises the concern that we are adding a so-called *bad control* (see Angrist and Pischke, 2008 section 3.2.3). Bad control happens when the control variable is itself endogenous to the outcome variable. This is unfortunately likely to be the case here, where location of refineries itself depends on acreage response. This is at least the argument made by Motamed et al. (2016), motivating their search for IV variables. Besides this, effects of the refinery location are likely to translate into changes in the local basis (as found by McNew and Griffith, 2005). This implies that the yield response I am measuring is also including the effect of refineries. This only changes the interpretation of the response coefficients: they include not only year-to-year variations, but also more longer-term variations.

# 5 Estimation

The main objective of the empirical analysis is to obtain reliable estimates of the supply response at the field level. Although yield response is the main interest, acreage response will also be investigated. The second objective is to compare the field level estimates with estimates based on aggregate data. The research hypothesis is that yield response at the aggregated level is under-estimating micro response, due to the composition effect of acreage response in average yields.

To do so, I present the model specification for the field-level analysis in Section 5.1, and for the aggregate analysis in Section 5.2.

# 5.1 Supply response at the individual level

### 5.1.1 Model specification

I will estimate both the extensive and intensive margin at the field-level. For crop choice  $c_{it}$  (i.e. crop planted on field i at time t), I will mainly follow the specification from Hendricks et al. (2014), estimating first-order transition probabilities  $Pr(c_{it}|c_{it-1})$ . For yields, denoted by  $y_{it}^M$ , I estimate a similar equation, with the main difference that rotation-specific parameters are introduced. The equations for maize are:

$$Pr(c_{it} = M | c_{it-1} = S) = \alpha_i + \beta_{SM,M}^A p_{it}^M + \beta_{SM,S}^A p_{it}^S + \gamma_{SM}^A x_{it} + \epsilon_{it}$$

$$Pr(c_{it} = M | c_{it-1} = M) = \alpha_i + \beta_{MM,M}^A p_{it}^M + \beta_{MM,S}^A p_{it}^S + \gamma_{MM}^A x_{it} + \epsilon_{it}$$

$$y_{it+1}^M = \alpha_i + \beta_{MM,M}^Y p_{it}^M + \beta_{MM,S}^Y p_{it}^S + \gamma_{MM}^Y x_{it} + \delta \mathbb{1}^R + \mathbb{1}^R (\beta_{SM,M}^Y p_{it}^M + \beta_{SM,S}^Y p_{it}^S + \gamma_{SM}^Y x_{it}) + (16)$$

Where price coefficients are denoted by  $\beta^A$  for crop choice,  $\beta^Y$  for yield.  $\mathbb{1}^R$  is the indicator function taking value of 1 if there was a rotation.  $x_{it}$  is a vector of control variables, including mainly weather variables.  $\delta$  represents the yield boost due to rotation.  $p_{it}^M$  is a vector of futures prices for post-harvest delivery adjusted for basis.

Analysis by Hendricks et al. (2014) suggested important heterogeneity in the supply responses. Given the very large sample size (close to one million fields), heterogeneity can be easily introduced by estimating separate models on different sub-samples. I intend to follow the method of Hendricks et al. (2014), who use the Major Land Resource Areas classification to define 24 distinct zones. To get further insights into the spatial heterogeneity, local spatially-weighted panel data models could be used, as in Cai et al. (2014).

#### 5.1.2 Choice of variables for the field-level analysis

**Time trends** A final issue to discuss is how to take into account time trends in the data. This seems particularly relevant for the yield equations, given that yields increase over time due to technological progress, albeit at a slower rate recently. It would be tempting to add years fixed effects, but given that our price variable  $p_{it}$  is composed of a spatially invariant futures prices  $p_t$  and a spatially-variant basis  $b_{it}$ , this would amount to remove the futures price from the analysis. To accommodate for this, quadratic or splines variable could be used to capture the trend, similar to the work of Roberts and Schlenker (2013).

### 5.1.3 Identification strategy for micro response

For the field-level analysis, several points deserve scrutiny to guarantee consistency of the estimates: a) choice of estimator, b) the issue of endogeneity, c) consequences of measurement error, and finally d) presence of spatial correlation.

Choice of estimator Regarding the choice of estimator, it should be noted that the crop choice Equation 9 is of the binary type, while the yield Equations 10 are observed conditionally on the crop choice equation. In other terms, we are facing here a sample selection/endogenous switching model within a fixed-effects panel. As we are primarily interested here in realised yields  $E[y_{it}^M|c_{it}=1]$  rather than in counterfactual yields  $E[y_{it}^M]$ , use of complex sample selection models does not appear necessary at this point, suggesting to use a standard linear FE for the yield equation. Similarly, for the crop choice equation, given the complexity of binary panel models, I intend to use a linear probability model, as is also done by Hendricks et al. (2014).

**Endogeneity** Endogeneity between the futures prices and crop acreage and yield represents a potential issue for estimation. Remembering that prices are composed of the Chicago futures price  $p_t$  and the local basis  $b_{it}$ , we need to ask whether each of these components is exogenous to a field's yield or acreage. Regarding the first component, the futures price, it seems reasonable to assume that an individual field's yield or acreage does not influence the futures price in Chicago. A counter-argument to this claim is that the Chicago price is likely to react to changes in aggregate production. It seems difficult to reconcile these two observations, which suggest a complex situation where simultaneity

<sup>&</sup>lt;sup>12</sup>Indeed, note that  $\tilde{p}_t \equiv \bar{p}_t - p_{it} = \bar{p}_t + \bar{b}_t - (p_t + b_{it}) = \tilde{b}_{it}$  as  $\bar{p}_t = p_t$ 

arises with aggregation of data. I was not able to find relevant literature addressing this, finding only a scare literature investigating the opposite phenomenon, when endogeneity at the individual level disappears at the aggregate level (Shin, 1987). For the second component, the local basis, it seems difficult to claim even at the micro level that it is exogenous to acreage or yields.

The possibility of endogeneity calls for further investigations on how to address the issue. The standard solution will be to search for instrumental variable, or for good control variables (as Hendricks et al. 2015 show that controls are as useful as IVs). The instruments in Roberts and Schlenker (2013) seem however difficult to use, given that they rely indirectly on the assumption of the absence of yield response. An alternative solution I envision is to use a *placebo test*, estimating the effect of a post-planting and post-fertilisation price. As one expects this price to have no effect, this could serve as an endogeneity test, and, should the test be rejected, eventually could serve to correct the endogeneity. Theoretical justification for this approach remain yet to be investigated.

# 5.2 Comparison with supply response estimates at the aggregate level

The second objective of this research is to compare individual (micro) supply estimates to those obtained based on data aggregated at the county level (macro). This is done in two steps. I first specify a *benchmark* aggregate model, in Section 5.2.1, which will serve as a raw comparison. I refine later on the comparison, by establishing a theoretical decomposition of the macro intensive margin into its micro intensive and extensive counterparts, see Section 3.3.

### 5.2.1 Benchmark model for aggregate supply

Estimating a model on data aggregated at the county level will help compare estimates of the intensive margin at the micro and macro level. As such, there is a tension in specifying this *benchmark* model between following as closely the micro specification chosen here, or following instead specifications found elsewhere in the literature. I intend to resolve this trade-off by estimating two sets of specifications, which I shall call the *benchmark* and *replication* specifications. The *benchmark* specification will follow as closely as possible the field-level specification, and serve as basis for the micro-macro comparison. The set of *replication* models will follow specifications used in the literature. The replication models will be compared against my macro benchmark model, not against the micro specification. Rationale for this comparison is to make sure that my results are robust to various specifications, allowing to compare my results with those in the broader literature.

**Benchmark aggregate model** The benchmark aggregate model will closely follow the field-level specification (see (9) and (10)). Using now  $C_{jt}$  for county j total acreage of a commodity (commodity subscripts are omitted for clarity) and  $Y_{jt}$  for county-average yield, the model at the county-level is:

$$C_{jt} = \alpha_j + \beta^C p_{jt} + \gamma^C x_{jt} + \delta^C C_{jt-1} + \epsilon_{jt}^C$$
(11)

$$Y_{jt+1} = \alpha_j + \beta^Y p_{jt} + \gamma^Y x_{jt} + \delta^Y C_{jt} + \epsilon_{jt}^Y$$
(12)

Aggregation brings in two main differences compared with the micro equations. Firstly, the field-level crop choice variable  $c_{itj}$  becomes a continuous variable, county acreage,  $C_{jt}$ . We no longer can condition on previous field history, but condition on previous county acreage  $C_{jt-1}$ . Interestingly, this results into a Nerlovian model, although its justification is based on rotation effects, not on partial adjustment. The second difference with the micro model is that the yield equation does contain also the previous county acreage variable.

It is important to note that the actual specification is based on rather heuristic than formal arguments. I shall investigate more formally conditions under which aggregation of the micro equations (9) and (10) leads to this specification. Intuition so far suggests that it is obtained by assuming equality of response coefficients among SM and MM sequences,  $^{13}$  and that relaxing this assumption would lead to  $C_{jt-1}$  interacting with the price and control variables.

New difficulties arise for the estimation of the macro model. For one, the acreage equation contains now a lagged dependent variable, which will require a GMM correction à la Arellano and Bond (1991). Also, as I argued above (see 5.1.3), endogeneity might arise at the aggregate level. Using a post-planting and post-fertilisation placebo price variable might prove helpful, but heterogeneity in planting and fertiliser dates at the county level might render it less effective. Endogeneity can also arise given that  $C_{jt}$  appears in both equations, making it a simultaneous equation system. As this system is however of the triangular form, this should not represent a main issue.

<sup>&</sup>lt;sup>13</sup>More precisely, assuming  $\beta_{lm,m}^k = \beta_{mm,m}^k$  and  $\gamma_{lm,m}^k = \gamma_{mm,m}^k$  with  $k \in \{\text{yield, area}\}\$ and  $l, m \in M, S$  in equations 9 and 10 results into this aggregation.

# 6 Conclusion

# **A** Derivations

# A.1 Derivation of equation 7

Note that notation here differs slightly from the notation in the main text. Yield function g has to be sibstituted for f, density and cumulative functions f() and F() become g() and G(). Finally, the main text describes the case where land above  $\theta^*$  produces, while the proof below is for the case where fields below  $\theta^*$  do produce.

We want the derivative of  $\bar{f}(p) = \int_0^{\theta^*(p)} g(\theta) f(p,\theta) d\theta / G(\theta^*(p))$  with respect to prices. Using Leibniz rule for the integral, together with the ratio rule, leads to:

$$\frac{\partial \bar{f}(p)}{\partial p} = \frac{\left[g(\theta^{\star}(p)) f(p, \theta^{\star}(p)) \frac{d\theta^{\star}(p)}{dp} + \int_{0}^{\theta^{\star}} g(\theta) \frac{\partial f(p, \theta)}{\partial p} d\theta\right] \cdot G(\theta^{\star}) + \int_{0}^{\theta^{\star}} g(\theta) f(p, \theta) d\theta \cdot g(\theta^{\star}) \frac{d\theta^{\star}(p)}{dp}}{G(\theta^{\star})^{2}}$$

The first and third terms in the numerator can be combined into (omitting the dependency of  $\theta^*$  on p):

$$g(\theta^{\star}) \frac{d\theta^{\star}(p)}{dp} \left[ f(p, \theta^{\star}) G(\theta^{\star}) - \int_{0}^{\theta^{\star}} g(\theta) f(p, \theta) d\theta \right] =$$

$$g(\theta^{\star}) \frac{d\theta^{\star}(p)}{dp} \left[ \int_{0}^{\theta^{\star}} g(\theta) f(p, \theta^{\star}) d\theta - \int_{0}^{\theta^{\star}} g(\theta) f(p, \theta) d\theta \right] =$$

$$g(\theta^{\star}) \frac{d\theta^{\star}(p)}{dp} \left[ \int_{0}^{\theta^{\star}} g(\theta) [f(p, \theta^{\star}) - f(p, \theta)] d\theta \right]$$

Bringing this term back into the main equation leads to:

$$\frac{\partial \bar{f}(p)}{\partial p} = \frac{\int_{0}^{\theta^{\star}} g(\theta) \frac{\partial f(p,\theta)}{\partial p} d\theta G(\theta^{\star}) + g(\theta^{\star}(p)) \frac{d\theta^{\star}(p)}{dp} \left[ \int_{0}^{\theta^{\star}} g(\theta) [f(p,\theta^{\star}) - f(p,\theta)] d\theta \right]}{G(\theta^{\star})^{2}}$$

### A.2 Derivation of empirical response

The short term expected yield is decomposed into yields of  $\langle M \to M \rangle$  and  $\langle S \to M \rangle$  fields:

$$E[y_{it}^{M}|x_{it},c_{it-1}] \equiv E[y_{it}^{M}|c_{it}=1,x_{it}] = E[y_{it}^{M}|c_{it}=1,c_{it-1}=1,x_{it}]P(c_{it}=1|c_{it-1}=1) + E[y_{it}^{M}|c_{it}=1,c_{it-1}=1,x_{it}]P(c_{it}=1|c_{it-1}=1) + E[y_{it}^{M}|c_{it}=1,c_{it-1}=1,x_{it}]P(c_{it}=1|c_{it-1}=1) + E[y_{it}^{M}|c_{it}=1,c_{it-1}=1,x_{it}]P(c_{it}=1|c_{it-1}=1) + E[y_{it}^{M}|c_{it}=1,x_{it}]P(c_{it}=1|c_{it-1}=1) + E[y_{it}^{M}|c_{it}=1,x_{it}]P(c_{it}=1|c_{it-$$

The derivative of the expected yield is given by:

$$\frac{\partial E[y_{it}^{M}|x_{it}]}{\partial x_{it}} = \frac{\partial E[y_{it}^{M}|c_{it}=1,c_{it-1}=1,x_{it}]}{\partial x_{it}}P(c_{it}=1|c_{it-1}=1) + \frac{\partial E[y_{it}^{M}|c_{it}=1,c_{it-1}=0,x_{it}]}{\partial x_{it}}P(c_{it}=1|c_{it-1}=0) + \frac{\partial P(c_{it}=1|c_{it-1}=1)}{\partial x_{it}}E[y_{it}^{M}|c_{it}=1,c_{it-1}=1,x_{it}] + \frac{\partial P(c_{it}=1|c_{it-1}=0)}{\partial x_{it}}E[y_{it}^{M}|c_{it}=1,c_{it-1}=0,x_{it}]$$

Note that as  $c_{it}$  takes values of 0 or 1, we have  $P(c_{it} = 1 | c_{it-1} = 1) = E(c_{it} | c_{it-1} = 1)$ . The last line simplifies then to:

$$\frac{\partial E[c_{it}=1|c_{it-1}=1]}{\partial x_{it}}E[y_{it}^{M}|c_{it}=1,c_{it-1}=1,x_{it}]+\frac{\partial E[c_{it}=1|c_{it-1}=0]}{\partial x_{it}}E[y_{it}^{M}|c_{it}=1,c_{it-1}=0,x_{it}].$$

# A.3 Figures

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Figure 6: Corn and soybeans location

# % area cultivated for each crop

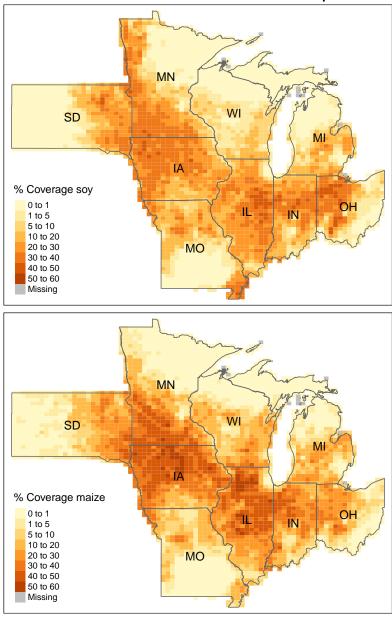


Figure 7: Corn-propensity model

