



# Adaptive and Autonomous Aerospace Systems

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Part 3: Autonomous systems

Lab experience 3: Trajectory generation for quadrotors with obstacles



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AEROSPACE SYSTEMS & CONTROL LABORATORY

# Outline

- This laboratory shows how to plan a minimum snap trajectory (minimum control effort) for a multirotor unmanned aerial vehicle (UAV) from a start pose to a goal pose on a 3D map by using the optimized rapidly exploring random tree (RRT\*) path planner.
- The first step is to set up a 3D map of a given environment, provide a start pose and goal pose.
- Then, to plan a path with RRT\* using 3D straight line connections.
- Finally, to fit a minimum snap trajectory through the obtained waypoints.

**TASK:** implement in MATLAB the code reported in the next slides and try tuning the RRT\* algorithm to achieve **fast** but also **smooth** trajectories.

```
addpath map_tools
```

```
%Configure the random number generator for repeatable result.
```

```
rng("default")
```

```
%% Map geometry and grid resolution
```

```
r = 0.2; % drone radius: parameter to be used in inflate map routine
```

```
% Mapsize
```

```
mapsize.x = 10; %[m]
```

```
length_ground = mapsize.x;
```

```
mapsize.y = 4; %[m]
```

```
width_ground = mapsize.y;
```

```
% Map resolution
```

```
res = 0.2; %[m]
```

```
grid_size = res;
```

```
height_ground = res;
```

```
%% Create map
```

```
map3D = occupancyMap3D(1/res); %1/res cells per meter
```

```
map3D.FreeThreshold = map3D.OccupiedThreshold; % set to 0.65; unknown spaces (occupancy 0.5) considered as free
```

```
% Define Ground Plane
```

```
for x = -length_ground/2+res/2:res:length_ground/2-res/2
```

```
for y = -width_ground/2+res/2:res:width_ground/2-res/2
```

```
for z = -height_ground
```

```
xyz = [x y z];
```

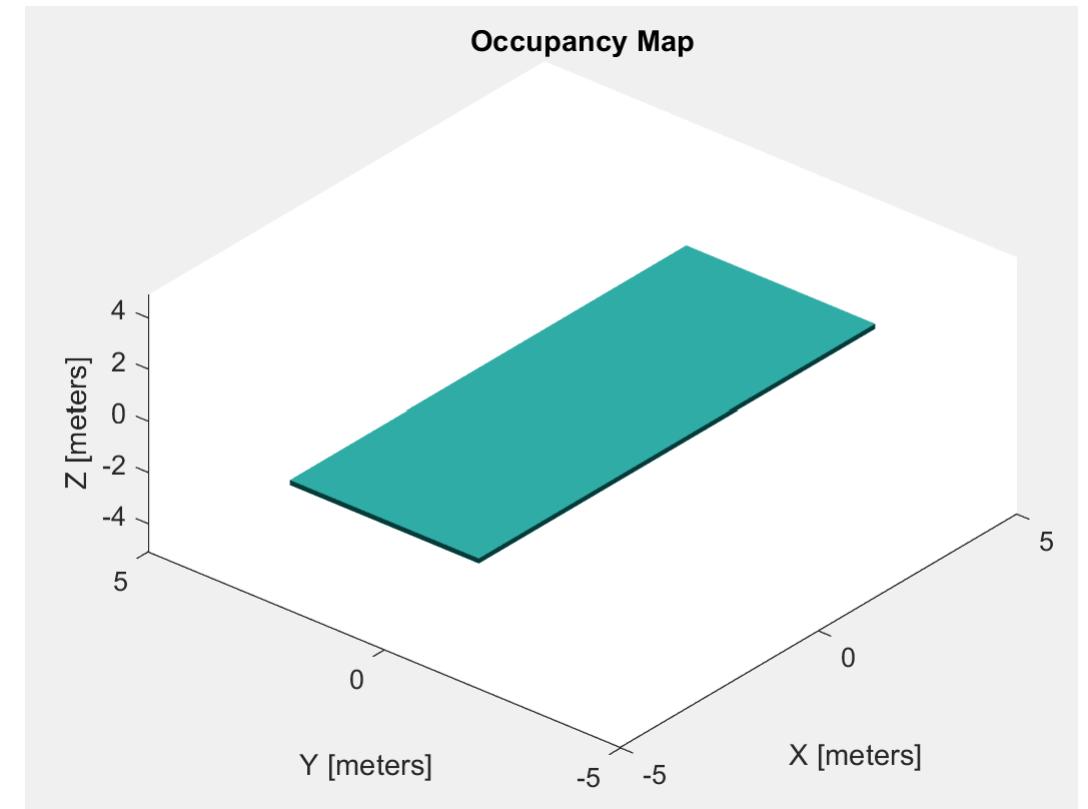
```
setOccupancy(map3D, xyz, 1)
```

```
end
```

```
end
```

```
end
```

```
show(map3D)
```



```

% Define Ground Plane
for x = -length_ground/2+res/2:length_ground/2-res/2
    for y = -width_ground/2+res/2:res:width_ground/2-res/2
        for z = -height_ground
            xyz = [x y z];
            setOccupancy(map3D, xyz, 1)
        end
    end
end

show(map3D)

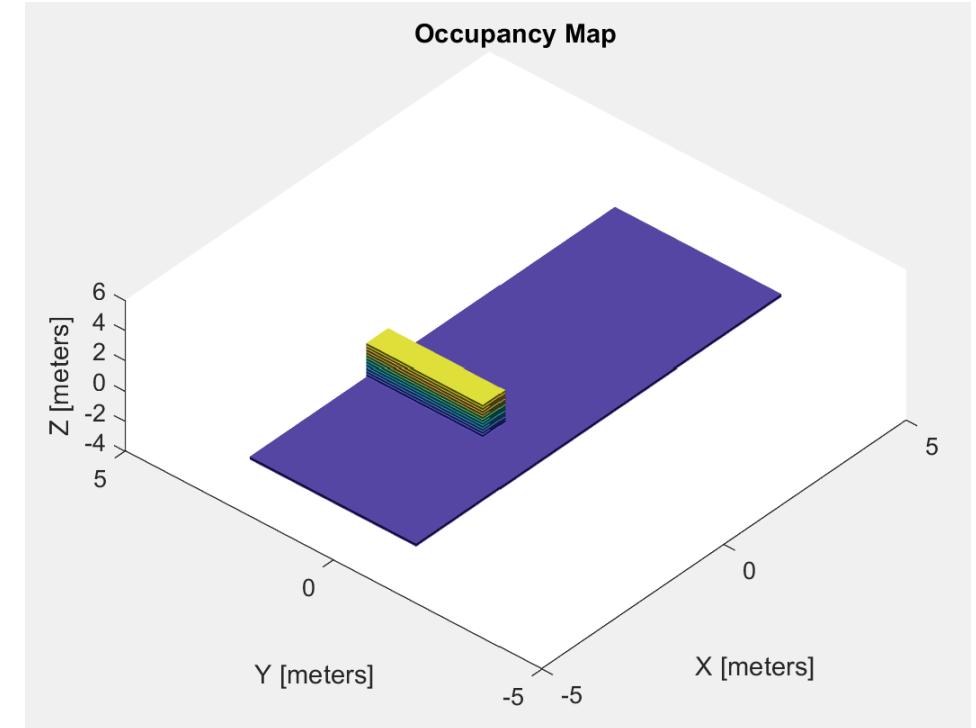
%% Insert boxes
length_box = 0.4; % use multiple of the cell dimensions
width_box = 2.4;
height_box = 2;

% Box 1
pos_x1 = -1.6; % use multiple of the cell dimensions
pos_y1 = 0.4;
pos_z1 = 1;

create_box(res, pos_x1, pos_y1, pos_z1, length_box, width_box, height_box, map3D)

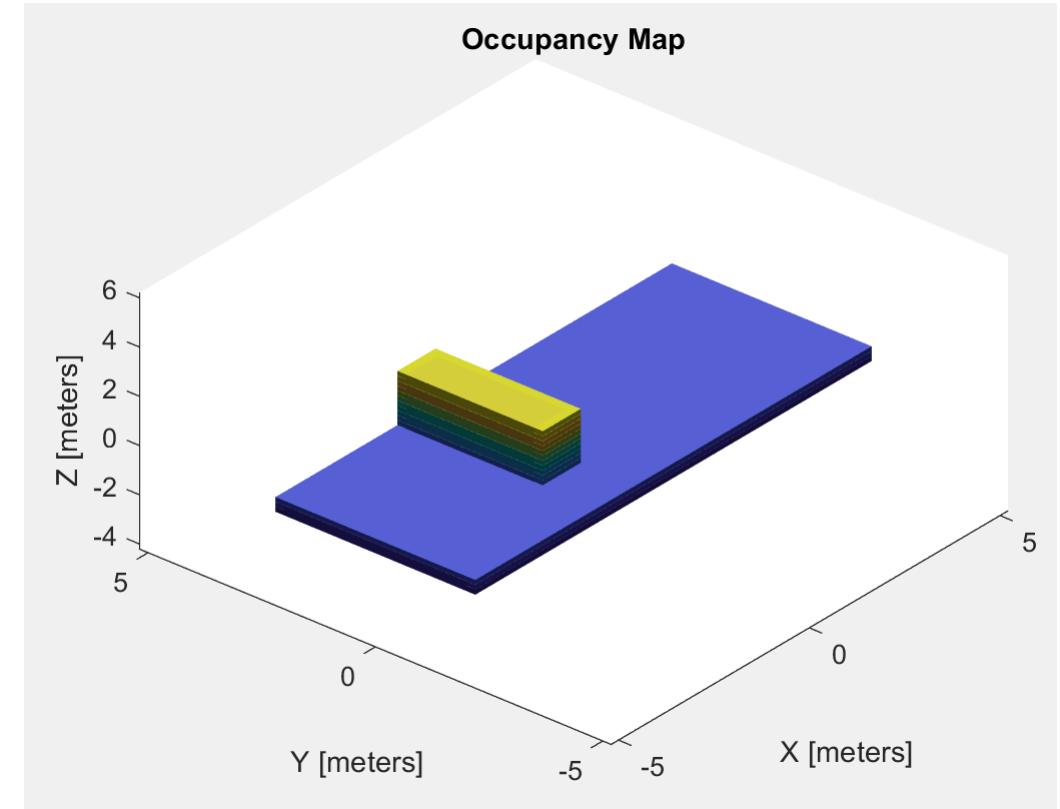
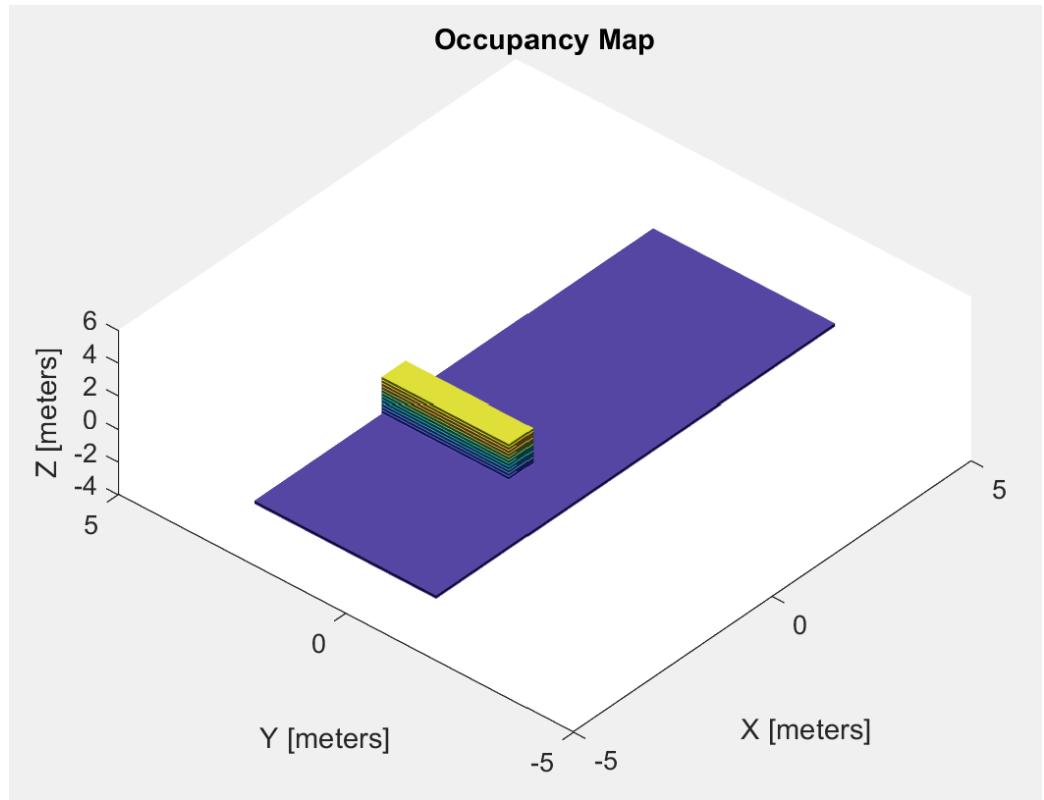
show(map3D)

```



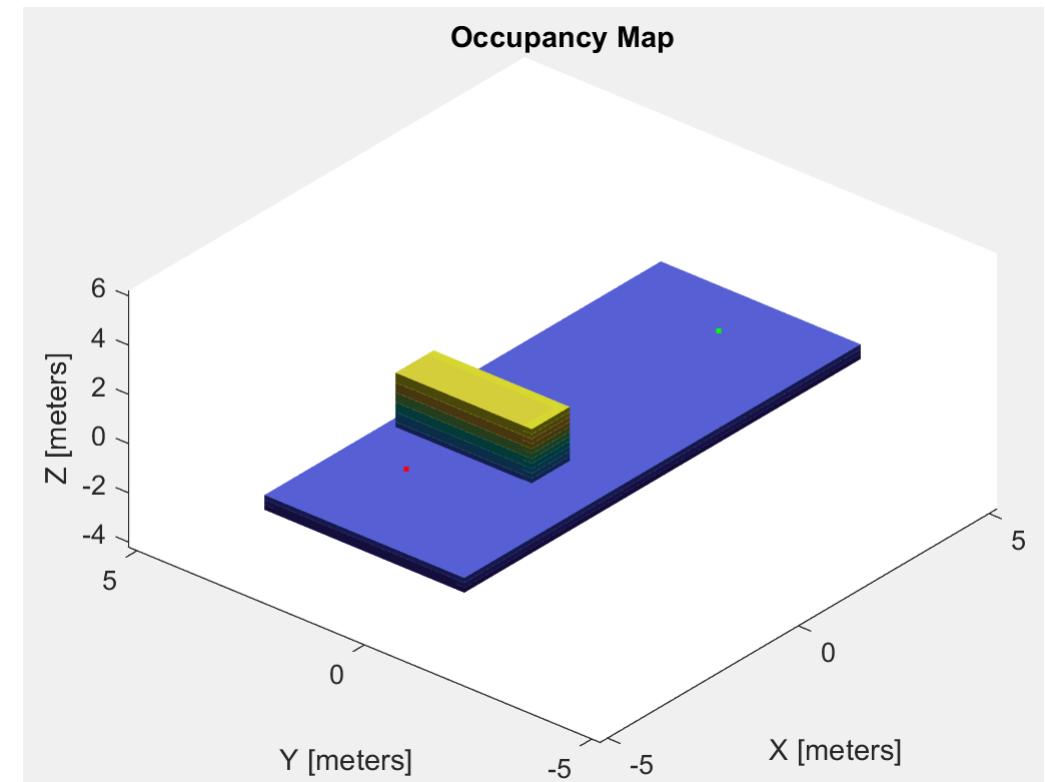
%% inflate the map with the drone radius

```
inflate(map3D,r)  
show(map3D)
```



```
%% Starting position  
startState = [-3.5, 0.5, 1];  
  
% Target position  
goalState = [3.5, -0.5, 1];
```

```
% Plot map, start pose, and goal pose  
show(map3D)  
hold on  
scatter3(startState(1),startState(2),startState(3),30,".r")  
scatter3(goalState(1),goalState(2),goalState(3),30,".g")
```



%% Define state space

```
xmax = mapsize.x/2;  
ymax = mapsize.y/2;  
zmax = 2;  
ss = E3space([-xmax xmax;-ymax ymax;0 zmax]);
```

% Define validator occupancy object

```
sv = validatorOccupancyMap3D(ss);  
sv.ValidationDistance = res;  
sv.Map = map3D;
```

## %% Plan the path

```
planner = plannerRRTStar(ss,sv);

%tunable parameters
planner.ContinueAfterGoalReached = true;
planner.MaxConnectionDistance = TO BE SET;
planner.GoalBias = TO BE SET; %between 0 and 1
planner.MaxIterations = TO BE SET;
planner.MaxNumTreeNodes = TO BE SET;
%planner.BallRadiusConstant = 100 ; % (default) read the documentation

[pthObj,solnInfo] = plan(planner, startState, goalState);

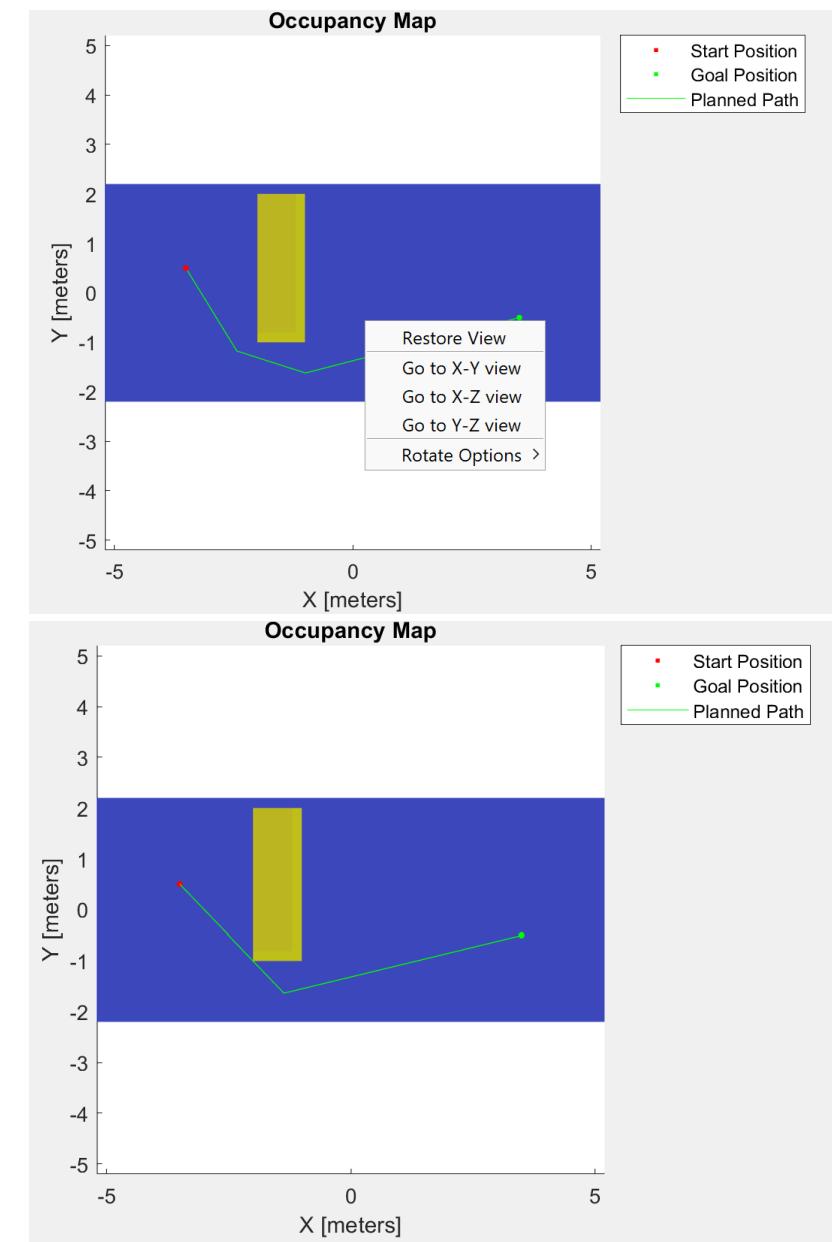
if (~solnInfo.IsPathFound)
    disp("No Path Found by the RRT, terminating example")
    return
end
```

% Plot the waypoints

```
plot3(pthObj.States(:,1),pthObj.States(:,2),pthObj.States(:,3),"-g")
```

```
view([-31 63])
```

```
legend("", "Start Position", "Goal Position", "Planned Path")
```



## %% Generate trajectory

```
waypoints = pthObj.States(:,1:3);  
nWayPoints = pthObj.NumStates;
```

```
% Calculate the distance between waypoints
```

```
distance = zeros(1,nWayPoints);  
for i = 2:nWayPoints  
    distance(i) = norm(waypoints(i,1:3) - waypoints(i-1,1:3));  
end
```

```
% Assume a UAV speed of 1 m/s and calculate time taken to reach each waypoint
```

```
UAVspeed = 1;  
timepoints = cumsum(distance/UAVspeed);  
nSamples = 100;
```

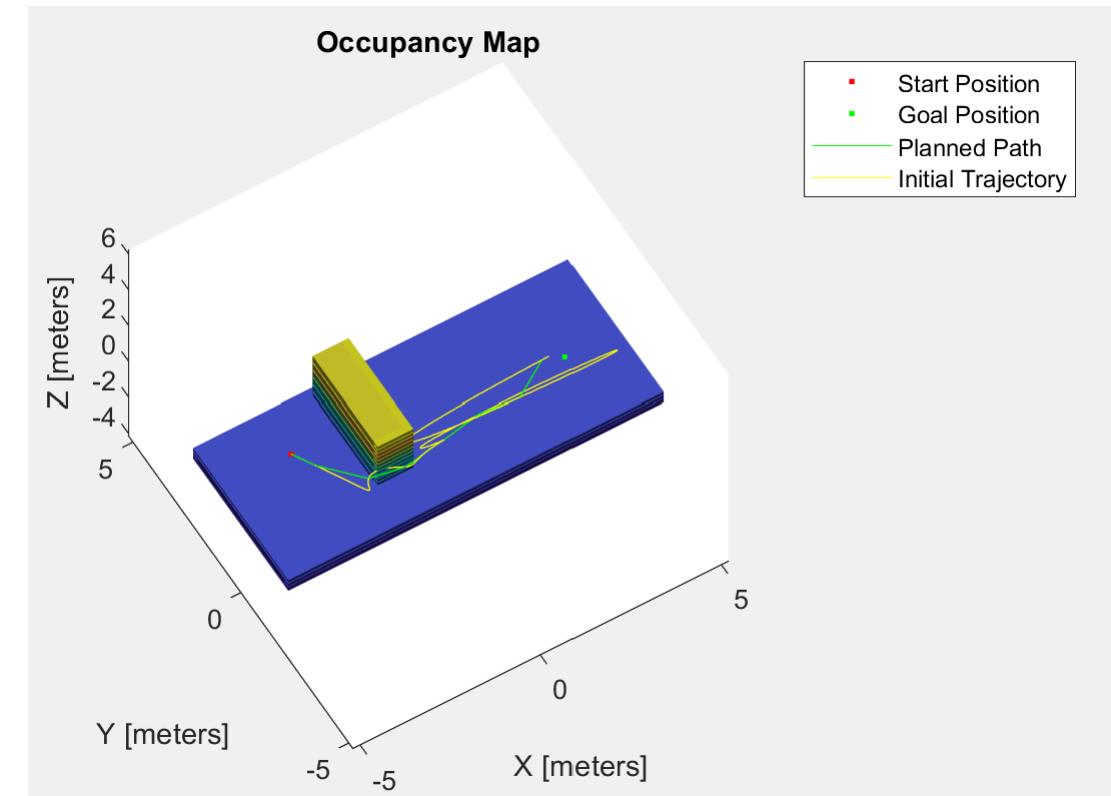
```
% Compute states along the trajectory (minsnappytraj )
```

```
[y,yd,ydd,yddd,ydddd,pp,tPoints,tSamples] = minsnappytraj(waypoints',timepoints,nSamples);
```

```
initialStates = y';
```

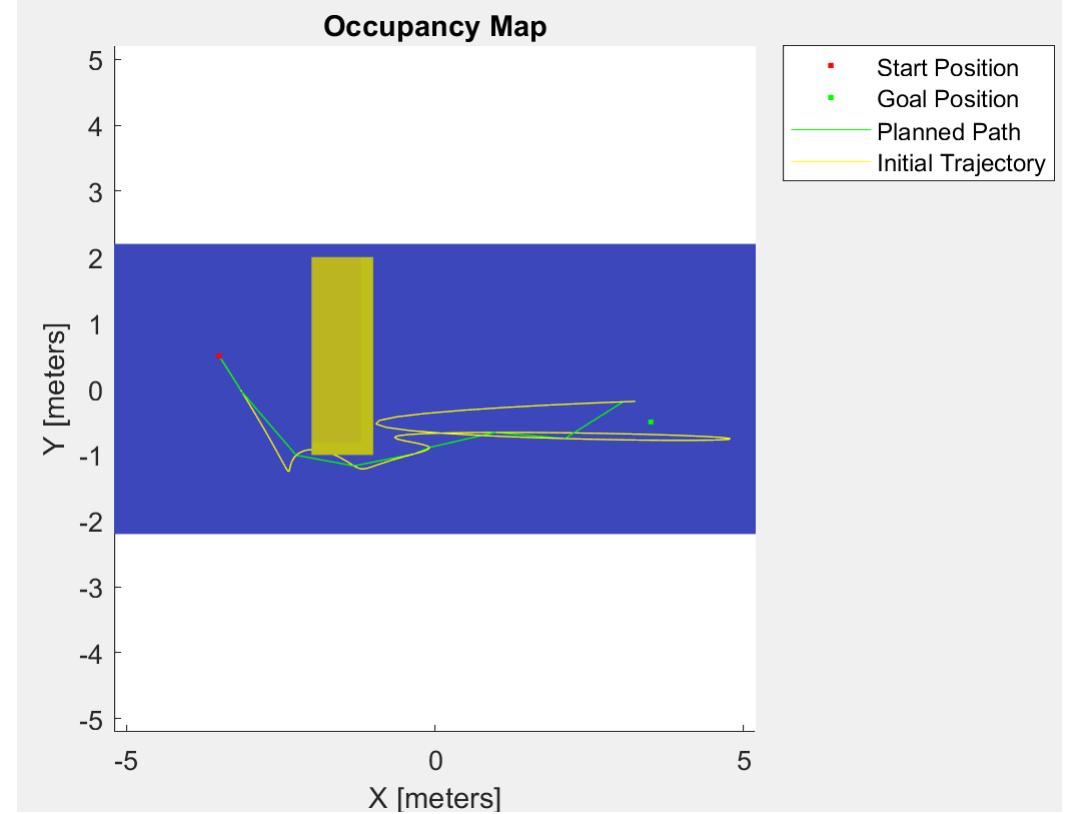
```
% Plot the minimum snap trajectory
```

```
plot3(initialStates(:,1),initialStates(:,2),initialStates(:,3),"y")  
legend("", "Start Position", "Goal Position", "Planned Path", "Initial Trajectory")
```



% check that the trajectory does not hit the obstacles

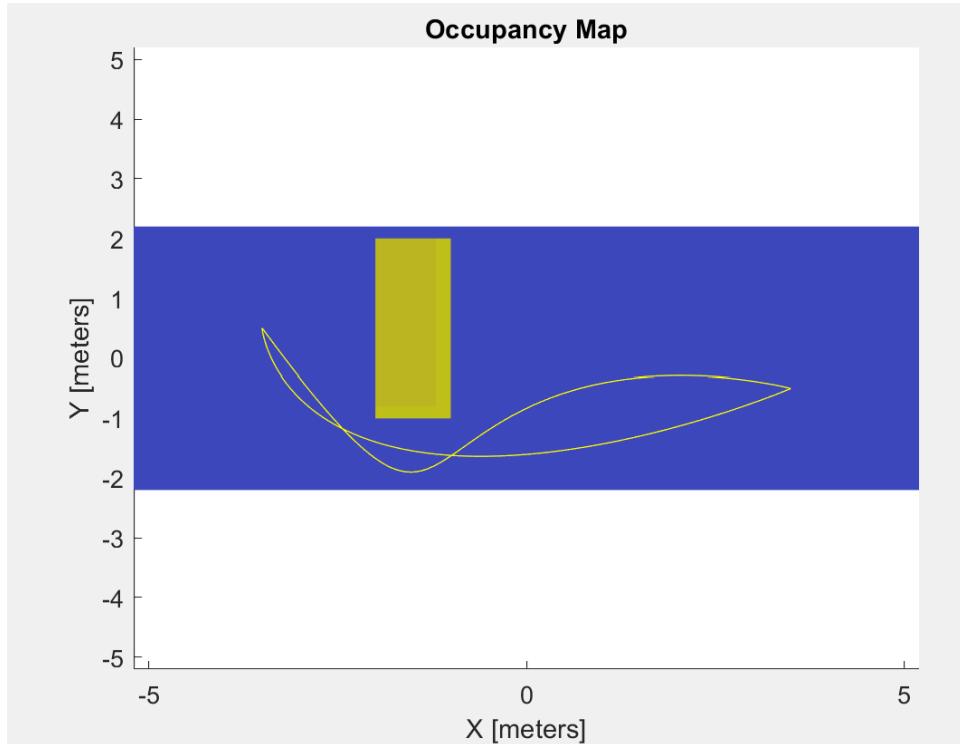
```
states = y';  
valid = all(isStateValid(sv,states));  
  
if (~valid)  
    disp("Trajectory not feasible, adding intermediate waypoints")  
end
```



## %% Generate trajectory: Alternative solution using time weight

```
% Compute states along the trajectory (minsnappolytraj with time weight)
```

```
[y,yd,ydd,yddd,ydddd,pp,tPoints,tSamples] =  
minsnappolytraj(waypoints',timepoints,nSamples,MinSegmentTime=0.1,MaxSegmentTime=20,TimeAllocation=true,TimeWeight=1);
```



## % Generate feasible minimum snap trajectory by adding intermediate waypoints

```
while(~valid)
% Check the validity of the states
validity = isStateValid(sv,states);

% Map the states to the corresponding waypoint segments
segmentIndices = MapStatesToPathSegments(waypoints,states);

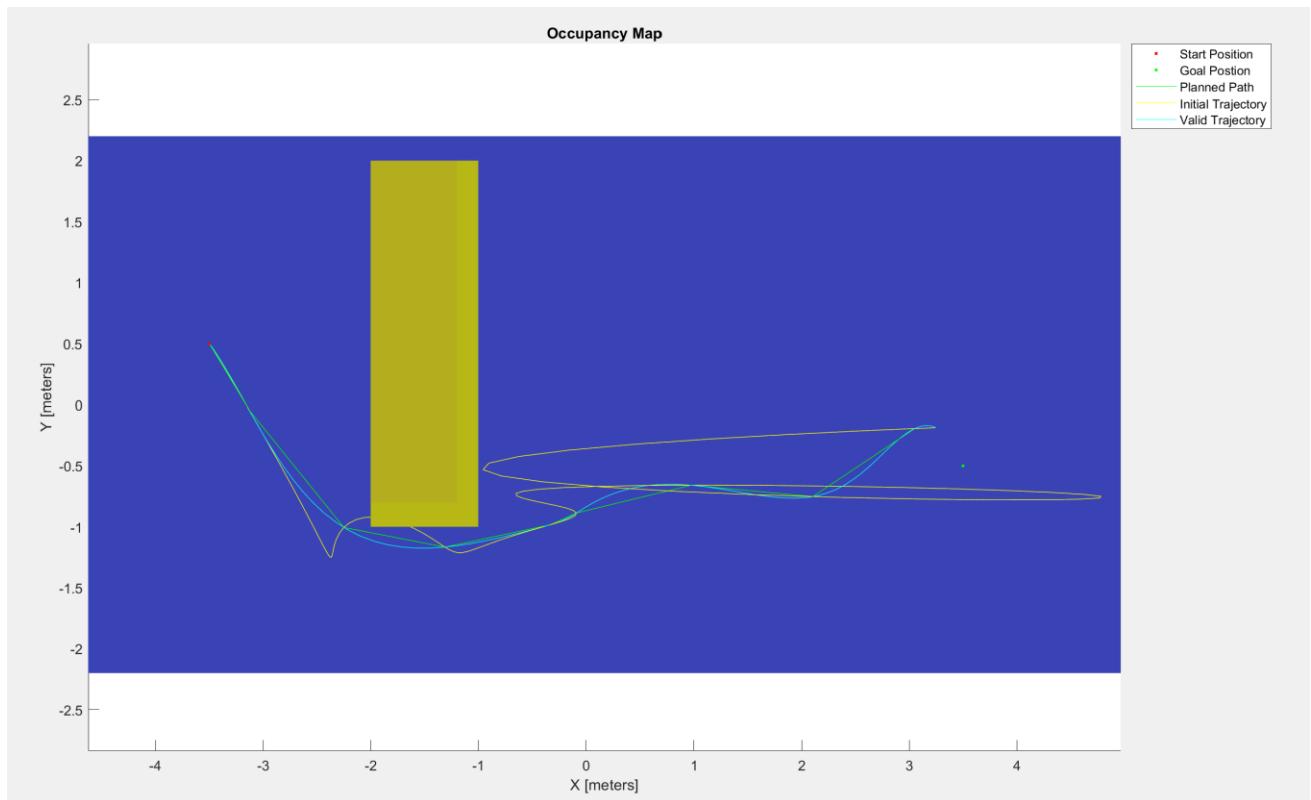
% Get the segments for the invalid states
% Use unique, because multiple states in the same segment might be invalid
invalidSegments = unique(segmentIndices(~validity));

% Add intermediate waypoints on the invalid segments
for i = 1:numel(invalidSegments)
segment = invalidSegments(i);
% Take the midpoint of the position to get the intermediate position
midpoint = (waypoints(segment,:) + waypoints(segment+1,:))/2;
end

nWayPoints = size(waypoints,1);
distance = zeros(1,nWayPoints);
for i = 2:nWayPoints
distance(i) = norm(waypoints(i,1:3) - waypoints(i-1,1:3));
end

% Calculate the time taken to reach each waypoint
timepoints = cumsum(distance/UAVspeed);
nSamples = 100;
[y,yd,ydd,yddd,pp,tPoints,tSamples] = minsnappolytraj(waypoints',timepoints,nSamples,MinSegmentTime=0.1,MaxSegmentTime=20,TimeAllocation=true,TimeWeight=1);
states = y';
% Check if the new trajectory is valid
valid = all(isStateValid(sv,states));

end
```



```

save('poly_coeff','pp')

% Plot the final valid trajectory

plot3(states(:,1),states(:,2),states(:,3),"c")
view([-31 63])
legend("", "Start Position", "Goal Postion", "Planned Path", "Initial Trajectory", "Valid Trajectory")
hold off

%% plot velocity and acceleration to check dynamic feasibility

figure
plot(tSamples,yd)
grid on
xlabel('Time [s]')
ylabel("Velocity [m/s]")

figure
plot(tSamples,ydd)
grid on
xlabel('Time [s]')
ylabel("Acceleration [m/s2]")

```

