

Rapport projekt X

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■ Uppgift 1: Visualisera data

Sammanfattning

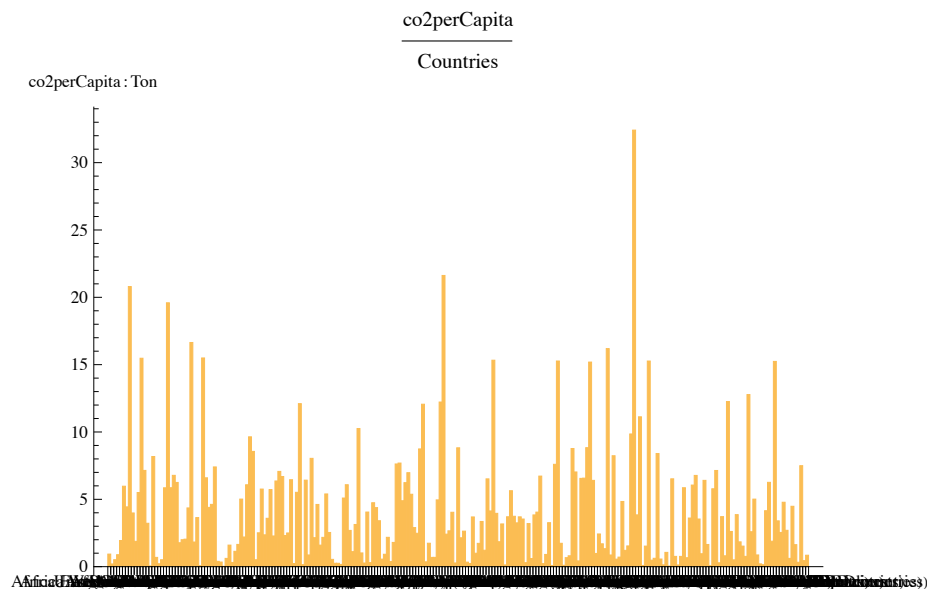
Uppgift

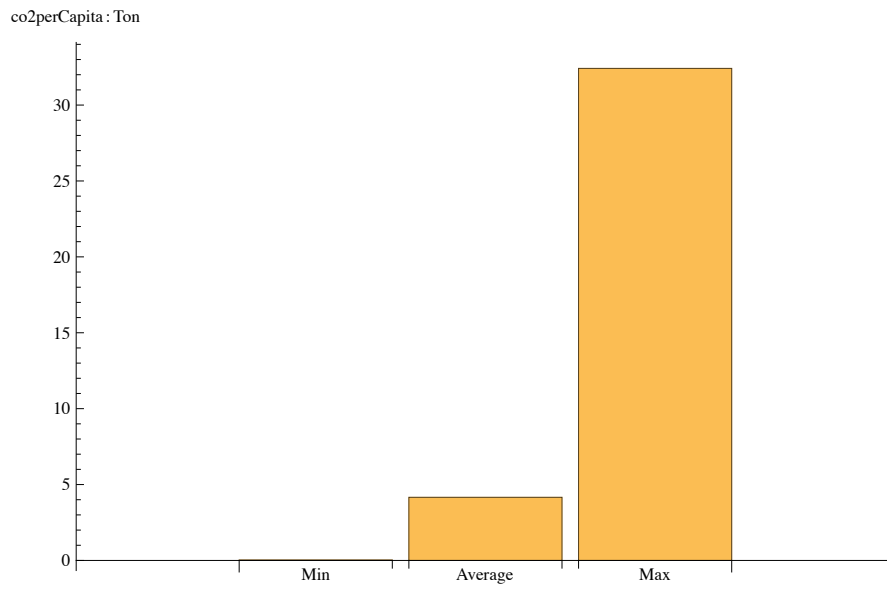
Nedan finns data för länders total territoriella CO₂-utsläpp och CO₂ per capita. Första listan innehåller länderna. Kombinera länder med data (de är i samma ordning) och visualisera detta med lämpliga grafer som visar utsläpp totalt för de länder som släpper ut mest jämfört med resten av världen. På samma sätt för per capita data. Varje graf skall ha följande:

1. Axelbeckningar
2. Enheter
3. Figurtext som kortfattat förklarar figuren

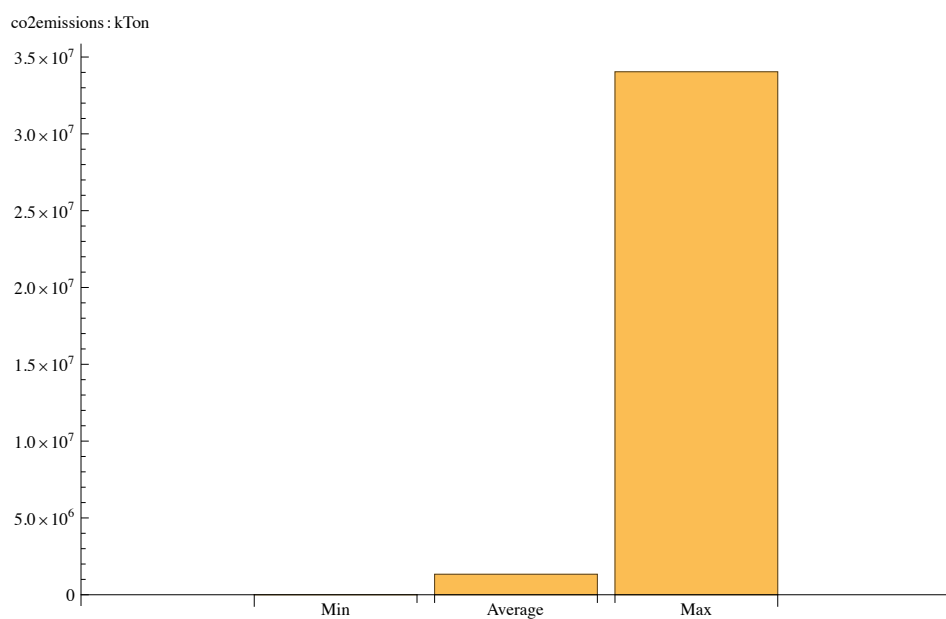
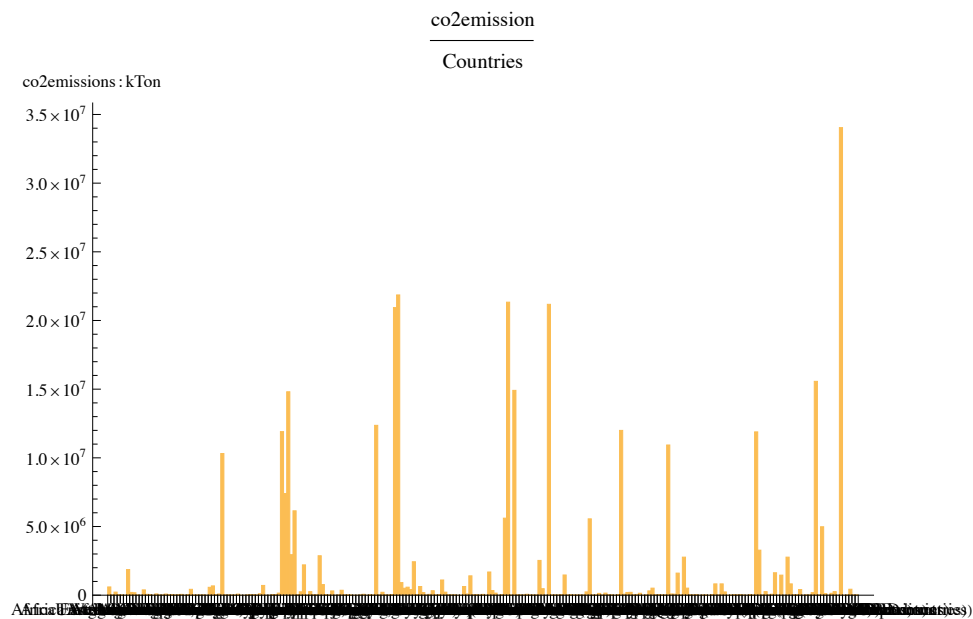
Resultat

1, a)





1, b)



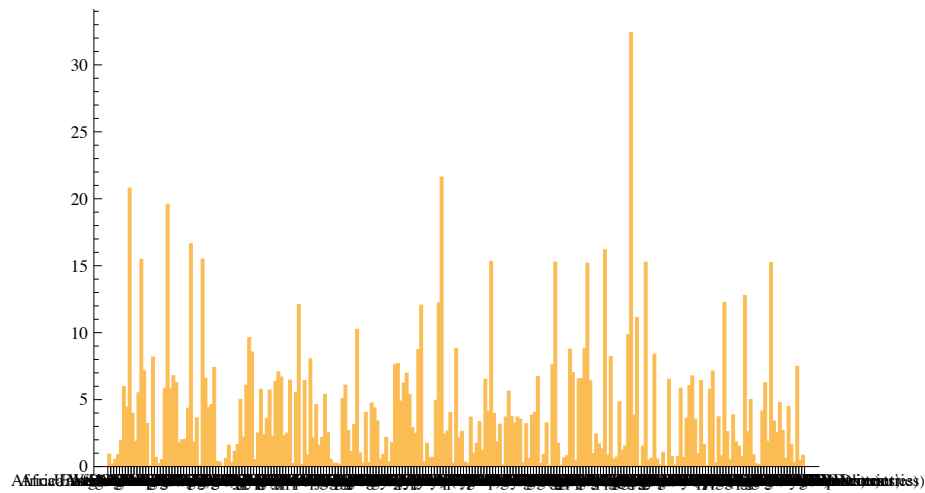
Kod

1, a)

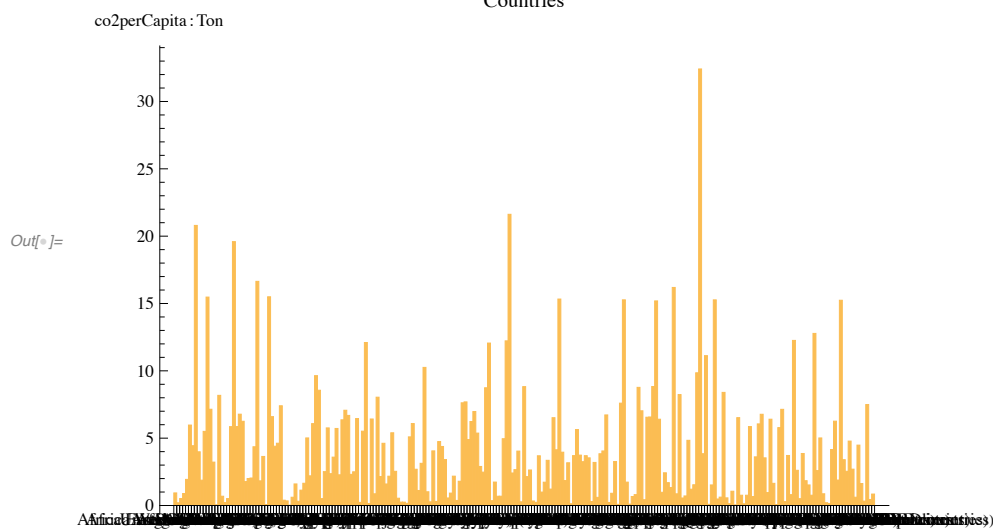
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 "Croatia", "Haiti", "Hungary", "IBRD only", "IDA & IBRD total",
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Max[co2perCapita]
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Out[ ]:= 32.4156
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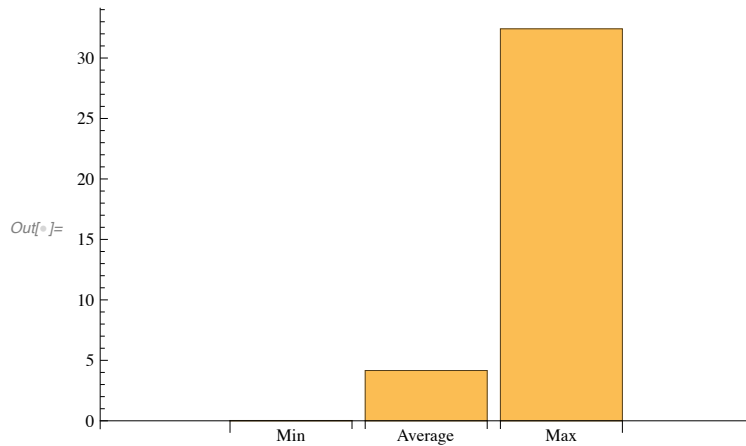
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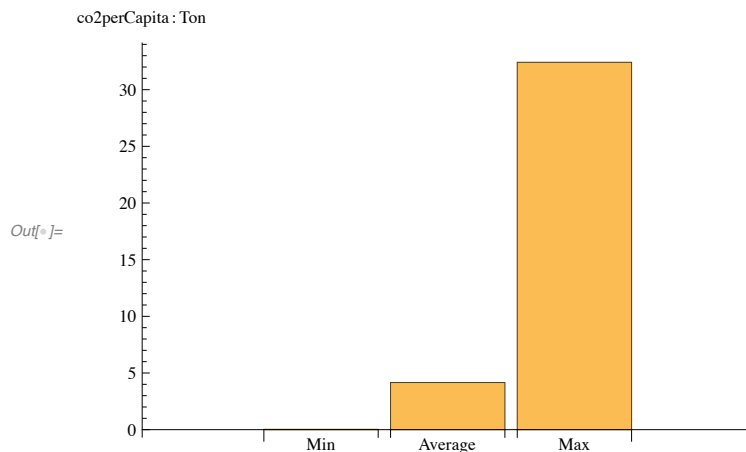
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Out[ ]:= 0.0261693
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In[ ]:= Show[%27, AxesLabel → {HoldForm[X : Extreme values], HoldForm[co2perCapita : Ton]},
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1, b)

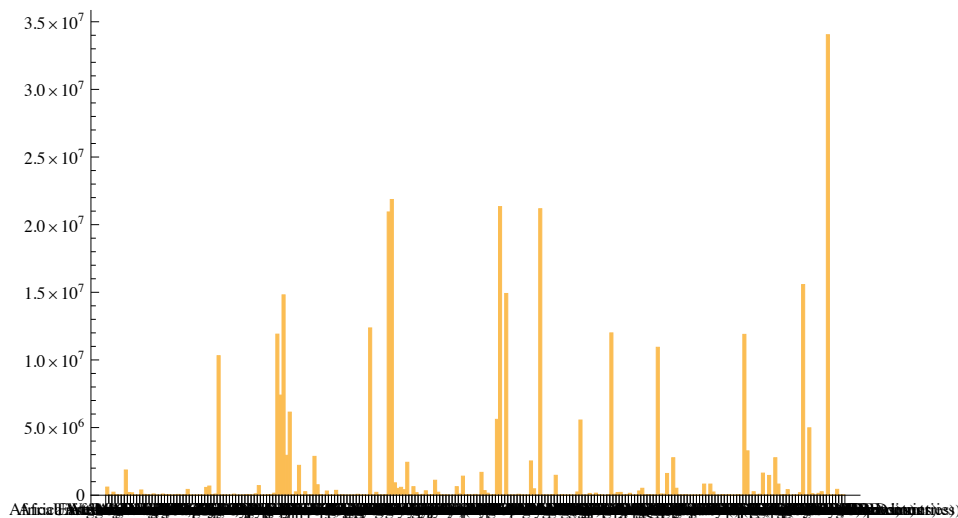
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"Paraguay", "Pacific island small states", "Post-demographic dividend",
"Qatar", "Romania", "Russian Federation", "Rwanda", "South Asia",
"Saudi Arabia", "Sudan", "Senegal", "Singapore", "Solomon Islands",
"Sierra Leone", "El Salvador", "Somalia", "Serbia",
"Sub-Saharan Africa (excluding high income)", "South Sudan",
"Sub-Saharan Africa", "Small states", "Sao Tome and Principe", "Suriname",
"Slovak Republic", "Slovenia", "Sweden", "Eswatini", "Seychelles",
"Syrian Arab Republic", "Chad", "East Asia & Pacific (IDA & IBRD countries)",
"Europe & Central Asia (IDA & IBRD countries)",
"Togo", "Thailand", "Tajikistan", "Turkmenistan",
"Latin America & the Caribbean (IDA & IBRD countries)", "Timor-Leste",
"Middle East & North Africa (IDA & IBRD countries)", "Tonga",
"South Asia (IDA & IBRD)", "Sub-Saharan Africa (IDA & IBRD countries)",
"Trinidad and Tobago", "Tunisia", "Turkey", "Tuvalu", "Tanzania", "Uganda",
"Ukraine", "Upper middle income", "Uruguay", "United States", "Uzbekistan",
"St. Vincent and the Grenadines", "Venezuela, RB", "Vietnam", "Vanuatu",
"World", "Samoa", "Yemen, Rep.", "South Africa", "Zambia", "Zimbabwe"}]

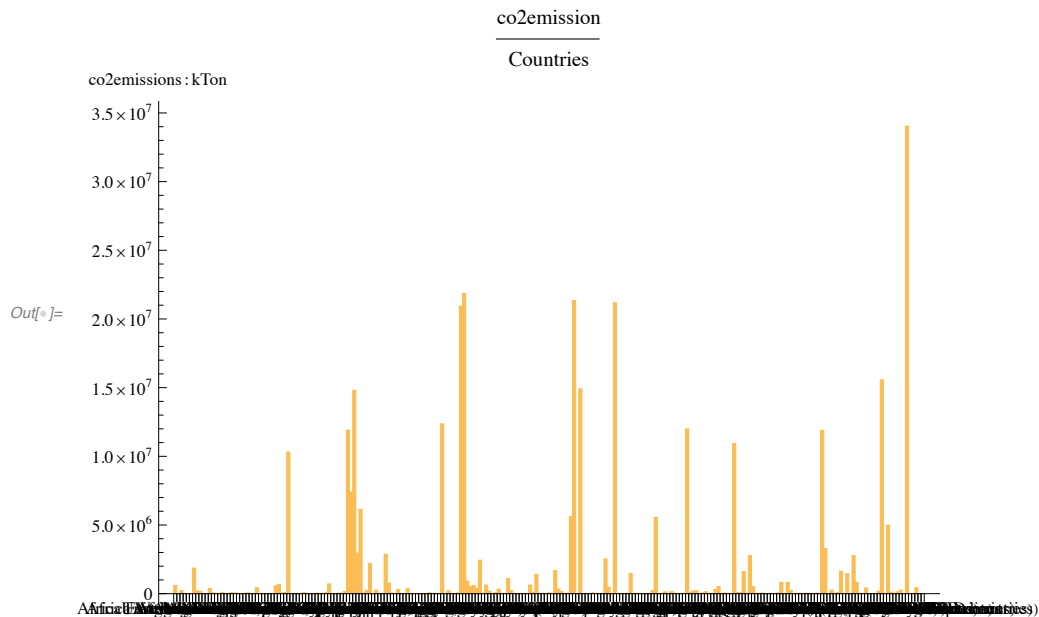
```



```

In[ ]:= Show[%35, AxesLabel -> {HoldForm[Countries], HoldForm[co2emissions : kTon]},
PlotLabel -> HoldForm[ $\frac{\text{co2emission}}{\text{Countries}}$ ], LabelStyle -> {GrayLevel[0]}]

```



```

In[*]:= co2emissions = {600351.1333, 7440, 224380, 27340, 5560, 460, 1863603.727, 200300,
177410, 5550, 530, 386620, 63180, 32020, 590, 93470, 7910, 4270, 82760,
41130, 30750, 2260, 22540, 59310, 680, 22710, 427710, 1250, 7140, 1380,
8210, 330, 574400, 676470, 37480, 86620, 10313460, 9910, 8620, 2200,
3220, 79490, 260, 620, 8260, 36920, 24970, 7230, 102480, 709540, 490,
180, 33380, 25120, 151670, 11907866.46, 7400359.524, 14810056.87,
2949087.39, 6142069.263, 39530, 246260, 2207420, 800, 258340, 16000,
16280, 2871000, 771602.9297, 44360, 1900, 309960, 180, 4610, 358800,
9460, 16110, 3120, 570, 310, 6670, 65290, 300, 18210, 2440, 12366368.33,
9770, 211980, 16580, 3330, 46390, 20938730, 21860535.52, 915178.5696,
505410, 583110, 407199.3144, 2434520, 37110, 629290, 188140, 2200,
61970, 324850, 8510, 24700, 1106150, 220450, 18400, 11000, 11160, 80,
260, 630870, 89460, 1408370, 18790, 27710, 1320, 58940, 390, 1689187.436,
338640.0291, 149413.7119, 140, 21630, 5608350.968, 21334207.73, 2570,
14912796.92, 11590, 9320, 7630, 66680, 8590, 3370, 1910, 2531611.759,
472140, 190, 21177938.67, 7370, 5620, 1550, 32520, 1470946.392, 2520,
21320, 6640, 4000, 4130, 1570, 239620, 5558099.304, 4250, 2290, 130670,
5210, 151170, 37350, 12030, 70, 32210, 11998460, 73370, 197072.5527,
208370, 10140, 54280, 142240, 290, 7460, 312740, 513004.5719, 18120,
49780, 8420, 3780, 10935463.93, 90170, 74880, 1607550, 1080, 2770040,
514600, 20200, 9860, 47360, 370, 1020, 6810, 690, 45540, 822805.4476,
1380, 823424.7218, 237761.658, 140, 2080, 33000, 14050, 36000, 1090,
620, 27910, 1070, 11889820, 3278021.798, 2260, 257860, 7330, 71730,
1633250, 640, 1461080, 190, 2770040, 823424.7218, 17760, 29980,
412970, 10, 11580, 6130, 185370, 15569855.45, 6520, 4981300, 112090,
280, 138160, 257860, 180, 34041045.97, 320, 9310, 433250, 7740, 12270};

```

```

Max[co2emissions]

```

```

Out[*]:= 3.4041 x 10^7

```

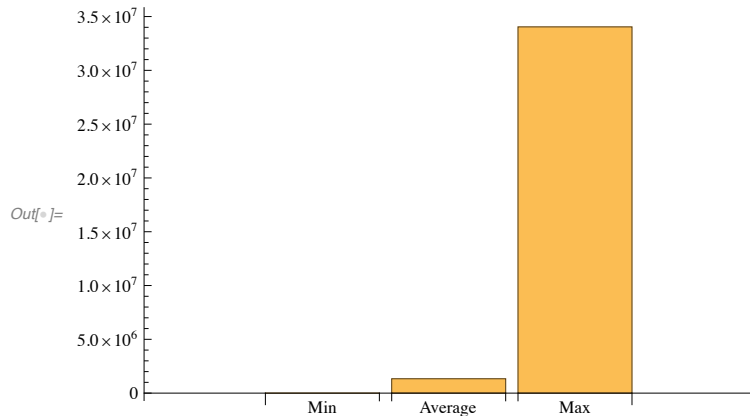
```
In[ ]:= Mean[co2emissions]
```

```
Out[ ]:= 1.33554 × 106
```

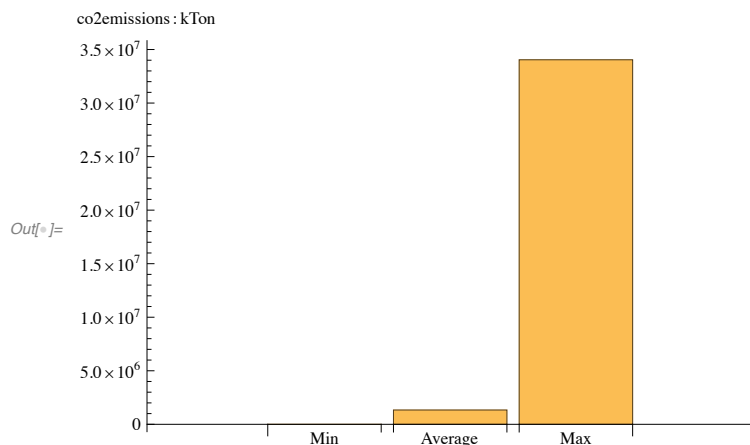
```
In[ ]:= Min[co2emissions]
```

```
Out[ ]:= 10
```

```
In[ ]:= BarChart[{10, 1.3355376685054393`*^6, 3.404104597`*^7},  
ChartLabels → {"Min", "Average", "Max"}]
```



```
In[ ]:= Show[%41, AxesLabel → {None, HoldForm[co2emissions : kTon]}],  
PlotLabel → None, LabelStyle → {GrayLevel[0]}]
```



■ Uppgift 2: Analysera data

Sammanfattning

Uppgift

Nedan finns data för världens energikonsumtion i TWh/år för olika energislag och för världens totala energikonsumtion. Anpassa lämpliga modeller (exponentialmodell, linjär modell, etc) till givet data nedan så att du kan förutsäga världens framtida energiandvändning. Använd funktionen FindFit för att hitta lämpliga koefficienter till modellerna. Tips : Förskjut tidsskalan med $t \rightarrow t - 1990$ för att göra det enklare att hitta parametrarna i FindFit för icke – linjära anpassningar. Varje graf skall ha följande :

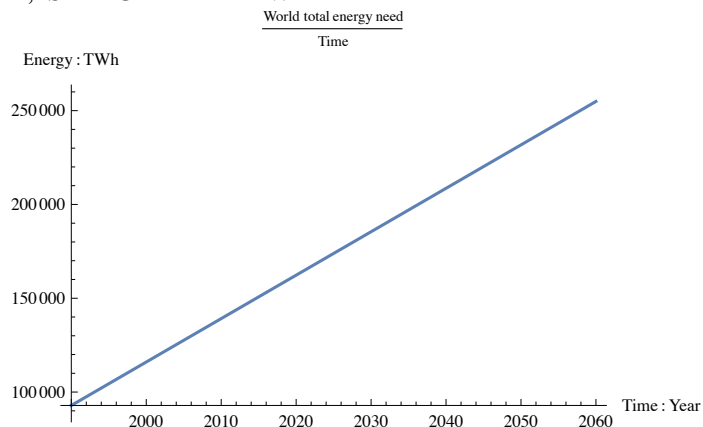
1. Axelbeckningar
2. Enheter
3. Figurtext som kortfattat förklarar figuren

Svara på följande frågor :

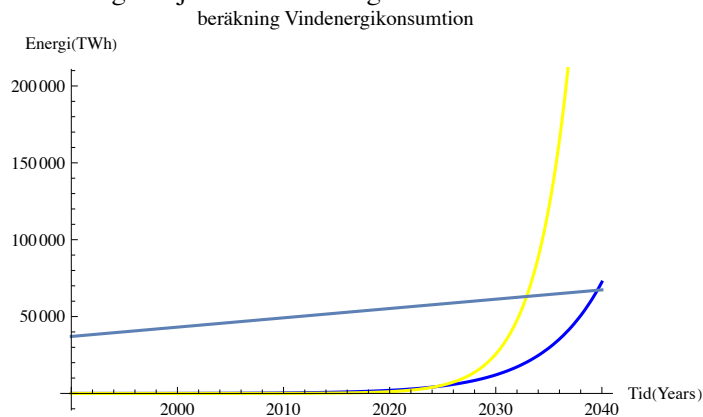
1. Uppskatta världens energikonsumtion år 2050!
2. Uppskatta när olja som energikälla kan ersättas av förnybara energikällor!
3. Uppskatta om/när världens energikonsumtion är CO₂ fri!
4. Vilket förnybart energislag uppskattas vara viktigast år 2050?
5. Vad har val av modell för betydelse?
6. Är ovanstående förutsägelser rimliga?
7. Vilka felkällor finns?

Resultat

1, Svar: Ca:232000 TWh



2, Svar: Solenergi kommer kunna ersätta Olja vid år ca: 2031 och tätt där efter år ca: 2036 passerar vindenergin oljan. Visualisering:



3, Svar: Ca: år 2036 kommer förnybar energi kunna försörja världens energibehov enligt informationen från föregående år.

totaltfunktion[2036]

199 339.

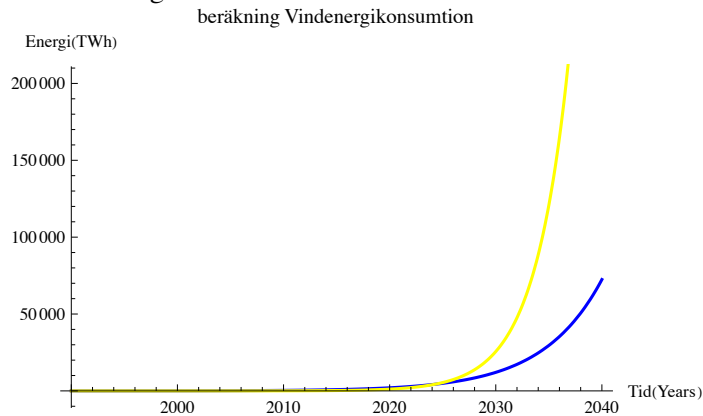
**vattenfunktion[2036] + vindfunktion[2036] +
solfunktion[2036] + karnkraftfunktion[2036]**

208 512.

(*TWh*)

4, Svar: Vi kan se att solen och därefter vinden är dom viktigaste förnybara energikällorna 2050. dessa förnybara energikällor domderar TWh/År och därmed ritas ej resterande förnybara energikällor ut.

Visualisering:



5, Svar: Beroende på vilken modell du väljer, tex linjär, exponentiell eller polynomekvation kommer tillväxten respektive minskningen variera då derivatan ändras på olika sätt. Om man försöker plotta en exponentialekvation kommer i detta fall ökningarna representeras mycket snabbare än vad tillexempel det skulle i en linjär ekvation.

6, Svar: ovanstående förutsägelser är rimliga då det baseras på föregående års fakta och därefter representerar en modell för framtiden. Man kan argumentera att förändringarna kan ske snabbare då det finns ett större politiskt stöd för co2 fritt i dagsläget än vad det eventuellt gjorde innan 2017.

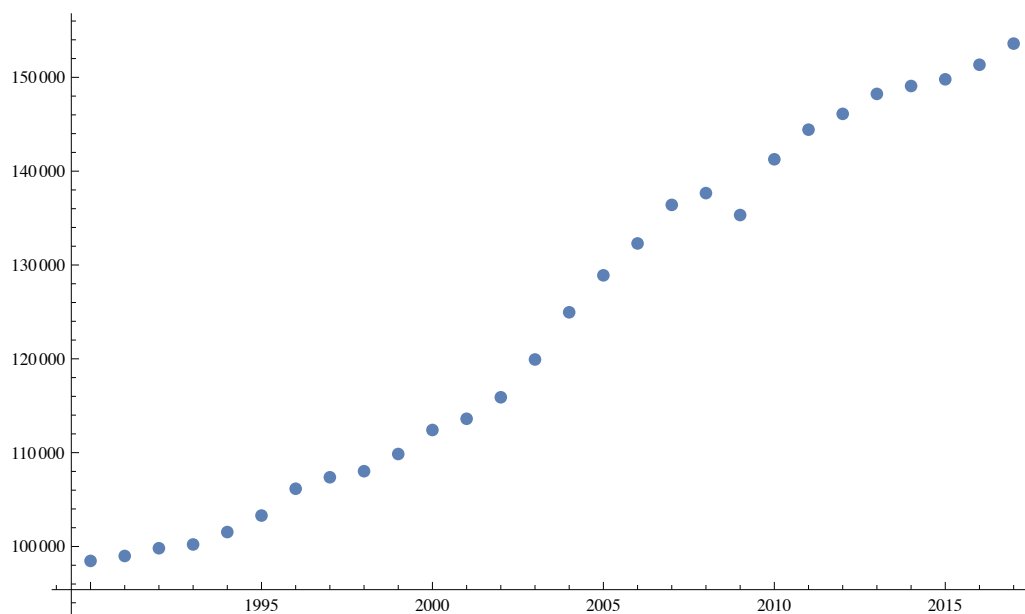
Sen är tillexempel solutvecklingen svår att fortsätta växa exponentiellt då byggdelarna till solpaneler blir svåråtkomliga. Co2 fri energi till 2030 är dock en orimlig förutsägelse då det inte finns drivkraft eller finansiellt initiativ för det över hela världen.

7, Svar: Exempel på felkällor är att utvecklingarna inte kommer att ske enligt representationerna då det exempelvis kan komma nya forskning och teknik som ändrar uppfattningen om vad som är bra investeringar för klimatsmart el. En annan felkälla är att man kan använda fel lineregen och därmed representerar punkterna på ett felaktigt sätt. Tillsist så skulle en felkälla vara att vi bara har fått information till 2017 vilket gör estimationerna mer osäkra.

Kod

```
In[108]:= 1, total = {{1990., 98462.371847116}, {1991., 98987.38143285},
{1992., 99813.54908523199}, {1993., 100216.423316547},
{1994., 101537.18489717401}, {1995., 103296.25934793001},
{1996., 106154.70010584098}, {1997., 107376.31135546902},
{1998., 108022.57284627101}, {1999., 109856.69807370701},
{2000., 112416.258116246}, {2001., 113610.635952175},
{2002., 115901.223848704}, {2003., 119930.15013616001},
{2004., 124960.08846344402}, {2005., 128897.75152416898},
{2006., 132297.06634468702}, {2007., 136405.679742778},
{2008., 137662.43593741}, {2009., 135324.15543267998},
{2010., 141265.10288404}, {2011., 144422.53459229},
{2012., 146106.05926769998}, {2013., 148234.8407671},
{2014., 149077.14748530003}, {2015., 149790.2224058},
{2016., 151341.68784990002}, {2017., 153595.6630277}};
```

```
ListPlot[total, AxesLabel → HoldForm[Time : Year]]
```



```

In[ ]:= total = {{1990., 98462.371847116}, {1991., 98987.38143285},
  {1992., 99813.54908523199}, {1993., 100216.423316547},
  {1994., 101537.18489717401}, {1995., 103296.25934793001},
  {1996., 106154.70010584098}, {1997., 107376.31135546902},
  {1998., 108022.57284627101}, {1999., 109856.69807370701},
  {2000., 112416.258116246}, {2001., 113610.635952175},
  {2002., 115901.223848704}, {2003., 119930.15013616001},
  {2004., 124960.08846344402}, {2005., 128897.75152416898},
  {2006., 132297.06634468702}, {2007., 136405.679742778},
  {2008., 137662.43593741}, {2009., 135324.15543267998},
  {2010., 141265.10288404}, {2011., 144422.53459229},
  {2012., 146106.05926769998}, {2013., 148234.8407671},
  {2014., 149077.14748530003}, {2015., 149790.2224058},
  {2016., 151341.68784990002}, {2017., 153595.6630277}};
model = LinearModelFit[total, x, x]

```

```

Out[ ]:= FittedModel[
$$-4.51374 \times 10^6 + 2314.87 x$$
]

```

```

In[ ]:= model["RSquared"]

```

```

Out[ ]:= 0.978342

```

```

In[ ]:= lineEquation = model[x]

```

```

In[ ]:= 
$$-4.51373668000478 \times 10^6 + 234.870212774434 x$$

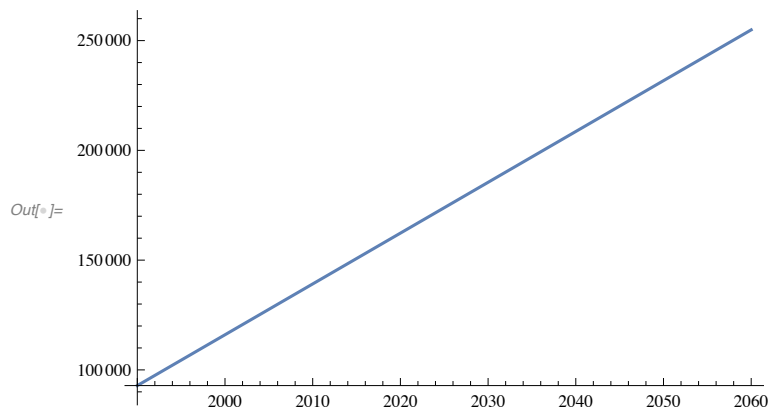
bestFit = Plot[lineEquation, {x, 1990, 2060}]

```

```

Out[ ]:= 
$$-4.51374 \times 10^6 + 234.87 x$$

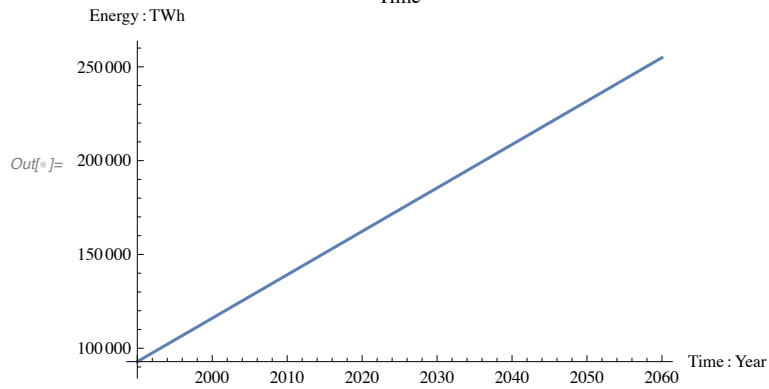

```




```

In[ ]:= Show[bestFit, AxesLabel → {HoldForm[Time : Year], HoldForm[Energy : TWh]},
  PlotLabel → HoldForm[ $\frac{\text{World total energy need}}{\text{Time}}$ ], LabelStyle → {GrayLevel[0]}]

```



```

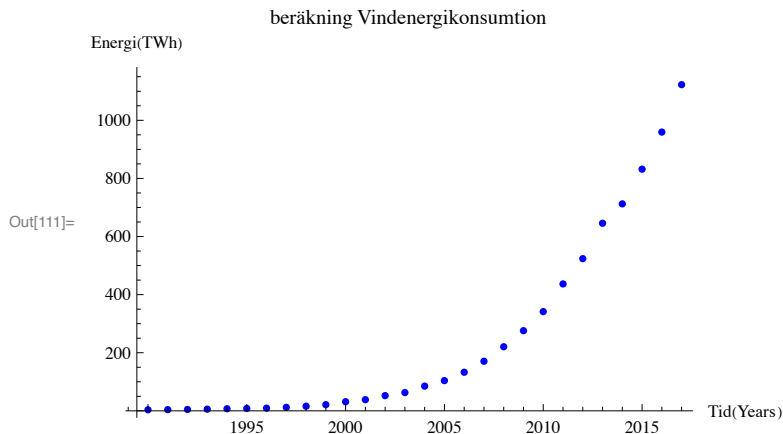
In[ ]:= model[2050]
231747.5618280936`
(*Svar: Ca:232000 TWh*)

2,

```

```
In[110]:= vind = {{1990., 3.632470516}, {1991., 4.086706675},
  {1992., 4.733212019}, {1993., 5.697568819},
  {1994., 7.122929844}, {1995., 8.261923444}, {1996., 9.204610762},
  {1997., 12.01757667}, {1998., 15.91490057}, {1999., 21.21534431},
  {2000., 31.41996387}, {2001., 38.39098735}, {2002., 52.33180737},
  {2003., 62.91691456}, {2004., 85.11605376}, {2005., 104.0868359},
  {2006., 132.8592792}, {2007., 170.6860872}, {2008., 220.5696719},
  {2009., 275.9292658}, {2010., 341.5652412}, {2011., 436.8034429},
  {2012., 523.8148612}, {2013., 645.7219776}, {2014., 712.4070431},
  {2015., 831.8262454}, {2016., 959.4687163}, {2017., 1122.74585}}
ListPlot[vind, AxesLabel -> {"Tid(Years)", "Energi(TWh)"},
  PlotStyle -> {Blue}, PlotLabel -> Vindenergikonsumtion beräkning ]
```

```
Out[110]= {{1990., 3.63247}, {1991., 4.08671}, {1992., 4.73321}, {1993., 5.69757},
  {1994., 7.12293}, {1995., 8.26192}, {1996., 9.20461}, {1997., 12.0176},
  {1998., 15.9149}, {1999., 21.2153}, {2000., 31.42}, {2001., 38.391},
  {2002., 52.3318}, {2003., 62.9169}, {2004., 85.1161}, {2005., 104.087},
  {2006., 132.859}, {2007., 170.686}, {2008., 220.57}, {2009., 275.929},
  {2010., 341.565}, {2011., 436.803}, {2012., 523.815}, {2013., 645.722},
  {2014., 712.407}, {2015., 831.826}, {2016., 959.469}, {2017., 1122.75}}
```

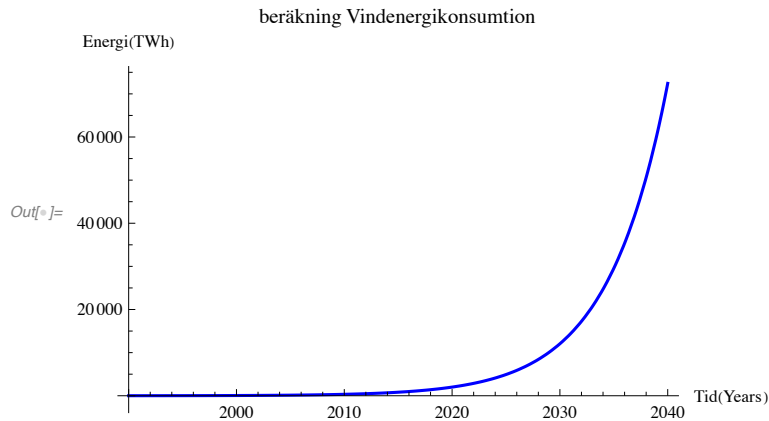


```
In[ ]:= {avind, bvind} = {a, b} /. FindFit[vind, {a Exp[b (t - 1990)]}, {a, b}, t]
```

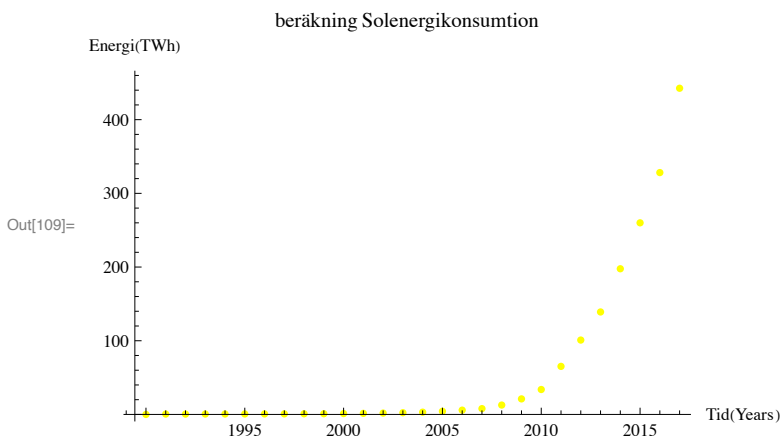
```
Out[ ]:= {9.25548, 0.179304}
```

```
vindfunktion[t_] := avind Exp[bvind (t - 1990)]
```

```
In[ ]:= beraknavind = Plot[vindfunktion[t], {t, 1990, 2040},
  PlotRange → All, AxesLabel → {"Tid (Years)", "Energi (TWh)"},
  PlotStyle → {Blue}, PlotLabel → Vindenergikonsumtion beräkning]
```



```
In[108]:= sol = {{1990., 0.}, {1991., 0.505223075},
  {1992., 0.468615413}, {1993., 0.556737928}, {1994., 0.60006443},
  {1995., 0.640874386}, {1996., 0.705278679}, {1997., 0.756655499},
  {1998., 0.880289501}, {1999., 0.965823997}, {2000., 1.177935576},
  {2001., 1.463956125}, {2002., 1.831247734}, {2003., 2.3293707},
  {2004., 3.054656084}, {2005., 4.249617769}, {2006., 5.818328387},
  {2007., 7.864870878}, {2008., 12.72162081}, {2009., 21.09259048},
  {2010., 33.82948514}, {2011., 65.21188479}, {2012., 100.9252749},
  {2013., 139.0442186}, {2014., 197.6716635}, {2015., 260.0058008},
  {2016., 328.1826964}, {2017., 442.6183606}};
ListPlot[sol, PlotRange → All, AxesLabel → {"Tid (Years)", "Energi (TWh)"},
  PlotStyle → {Yellow}, PlotLabel → Solenergikonsumtion beräkning]
```

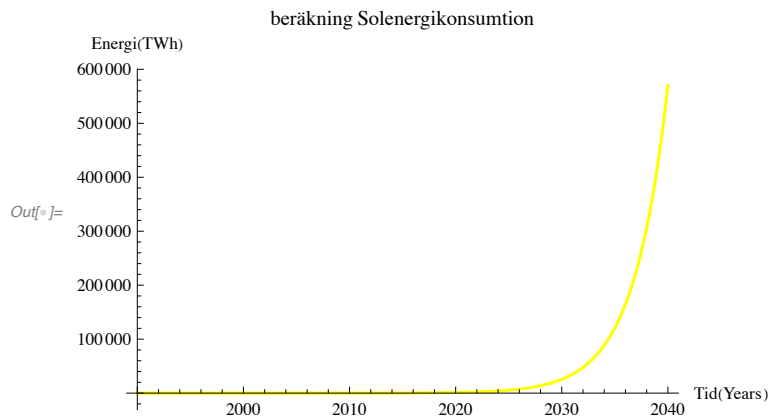


```
In[ ]:= {asol, bsol} = {a, b} /. FindFit[sol, {a Exp[b (t - 1990)]}, {a, b}, t]
```

```
Out[ ]:= {0.104136, 0.310299}
```

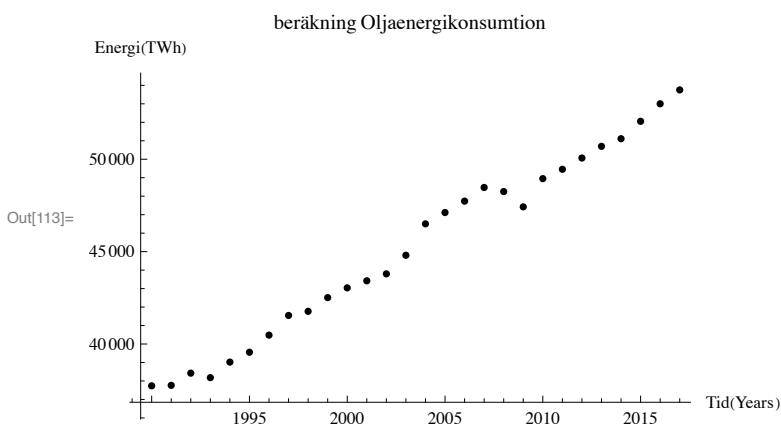
```
In[ ]:= solfunktion[t_] := asol Exp[bsol (t - 1990)]
```

```
In[ ]:= beraknasol = Plot[solfunktion[t], {t, 1990, 2040},
  PlotRange → All, AxesLabel → {"Tid(Years)", "Energi (TWh)"},
  PlotStyle → {Yellow}, PlotLabel → Solenergikonsumtion beräkning]
```



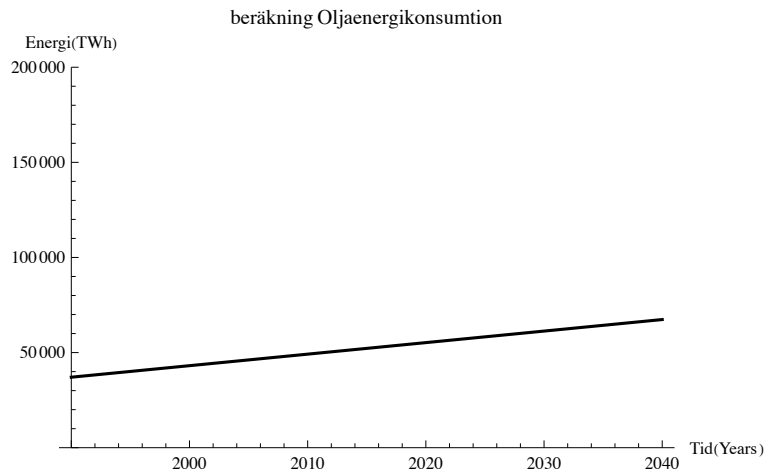
```
In[112]:= olja = {{1990., 37736.94729}, {1991., 37763.14824},
  {1992., 38422.53103}, {1993., 38179.42324}, {1994., 39021.80173},
  {1995., 39555.43054}, {1996., 40480.1731}, {1997., 41544.67299},
  {1998., 41768.48384}, {1999., 42510.09274}, {2000., 43038.62001},
  {2001., 43421.10755}, {2002., 43796.55068}, {2003., 44803.21017},
  {2004., 46503.96733}, {2005., 47115.72728}, {2006., 47732.19992},
  {2007., 48471.73162}, {2008., 48250.64229}, {2009., 47422.36853},
  {2010., 48949.72046}, {2011., 49455.27172}, {2012., 50065.86499},
  {2013., 50698.38455}, {2014., 51109.97172}, {2015., 52053.27008},
  {2016., 53001.86598}, {2017., 53752.27638}}
ListPlot[olja, AxesLabel → {"Tid(Years)", "Energi (TWh)"},
  PlotStyle → {Black}, PlotLabel → Oljaenergikonsumtion beräkning]
```

```
Out[112]= {{1990., 37 736.9}, {1991., 37 763.1}, {1992., 38 422.5}, {1993., 38 179.4},
  {1994., 39 021.8}, {1995., 39 555.4}, {1996., 40 480.2}, {1997., 41 544.7},
  {1998., 41 768.5}, {1999., 42 510.1}, {2000., 43 038.6}, {2001., 43 421.1},
  {2002., 43 796.6}, {2003., 44 803.2}, {2004., 46 504.}, {2005., 47 115.7},
  {2006., 47 732.2}, {2007., 48 471.7}, {2008., 48 250.6}, {2009., 47 422.4},
  {2010., 48 949.7}, {2011., 49 455.3}, {2012., 50 065.9}, {2013., 50 698.4},
  {2014., 51 110.}, {2015., 52 053.3}, {2016., 53 001.9}, {2017., 53 752.3}}
```



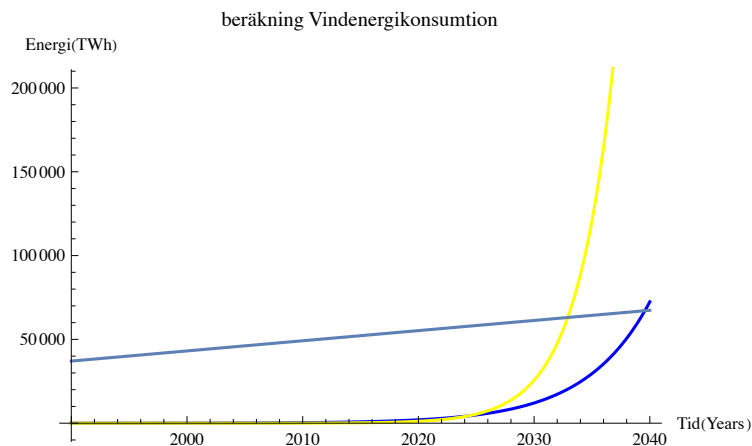
```
model = FindFit[olja, a x + b, {a, b}, x]
```

```
beraknaolja = Plot[a x + b /. model, {x, 1990, 2040},
  PlotRange → {200 000, 0}, AxesLabel → {"Tid (Years)", "Energi (TWh)"},
  PlotStyle → {Black}, PlotLabel → Oljaenergikonsumtion beräkning]
```



```
Show[beraknavind, beraknasol, beraknaolja, PlotRange → {200 000, 0}]
```

```
Out[118]= {a → 606.174, b → -1.16923 × 106}
```



3,

Kol (TWh)

```
kol = {{1990., 25845.88485}, {1991., 25561.41954},
  {1992., 25478.81089}, {1993., 25580.92144}, {1994., 25729.64169},
  {1995., 25867.8533}, {1996., 26516.28457}, {1997., 26549.71899},
  {1998., 26351.79429}, {1999., 26492.77461}, {2000., 27403.94562},
  {2001., 27851.05371}, {2002., 28936.6423}, {2003., 31475.58334},
  {2004., 33656.31109}, {2005., 36118.94545}, {2006., 37979.81684},
  {2007., 40143.91171}, {2008., 40712.5427}, {2009., 40088.33994},
  {2010., 41932.74507}, {2011., 43948.96889}, {2012., 44129.62497},
  {2013., 44953.01385}, {2014., 44916.83781}, {2015., 43786.8458},
```

```
{2016.` , 43101.23216`}, {2017.` , 43397.13549`}};
```

Olja (TWh)

```
olja = {{1990.` , 37736.94729`}, {1991.` , 37763.14824`},
{1992.` , 38422.53103`}, {1993.` , 38179.42324`}, {1994.` , 39021.80173`},
{1995.` , 39555.43054`}, {1996.` , 40480.1731`}, {1997.` , 41544.67299`},
{1998.` , 41768.48384`}, {1999.` , 42510.09274`}, {2000.` , 43038.62001`},
{2001.` , 43421.10755`}, {2002.` , 43796.55068`}, {2003.` , 44803.21017`},
{2004.` , 46503.96733`}, {2005.` , 47115.72728`}, {2006.` , 47732.19992`},
{2007.` , 48471.73162`}, {2008.` , 48250.64229`}, {2009.` , 47422.36853`},
{2010.` , 48949.72046`}, {2011.` , 49455.27172`}, {2012.` , 50065.86499`},
{2013.` , 50698.38455`}, {2014.` , 51109.97172`}, {2015.` , 52053.27008`},
{2016.` , 53001.86598`}, {2017.` , 53752.27638`}};
```

Naturgas (TWh)

```
naturgas = {{1990.` , 19486.64542`}, {1991.` , 19984.58677`},
{1992.` , 20076.92098`}, {1993.` , 20275.09431`}, {1994.` , 20405.36342`},
{1995.` , 21121.78818`}, {1996.` , 22143.41796`}, {1997.` , 22082.05319`},
{1998.` , 22485.93806`}, {1999.` , 23107.57158`}, {2000.` , 24019.89227`},
{2001.` , 24367.11133`}, {2002.` , 25108.12839`}, {2003.` , 25769.17552`},
{2004.` , 26752.16794`}, {2005.` , 27537.09099`}, {2006.` , 28347.57835`},
{2007.` , 29580.25097`}, {2008.` , 30321.37836`}, {2009.` , 29477.9263`},
{2010.` , 31759.12422`}, {2011.` , 32410.44868`}, {2012.` , 33270.53388`},
{2013.` , 33714.94785`}, {2014.` , 33986.84723`}, {2015.` , 34741.88349`},
{2016.` , 35741.82987`}, {2017.` , 36703.96587`}};
```

Kärnkraft (TWh)

```
karnkraft = {{1990.` , 2000.642591`}, {1991.` , 2096.356868`},
{1992.` , 2112.277946`}, {1993.` , 2185.016841`}, {1994.` , 2226.050783`},
{1995.` , 2322.592422`}, {1996.` , 2407.002623`}, {1997.` , 2390.480054`},
{1998.` , 2431.571247`}, {1999.` , 2524.546817`}, {2000.` , 2580.976669`},
{2001.` , 2653.821898`}, {2002.` , 2696.204132`}, {2003.` , 2641.599256`},
{2004.` , 2757.124087`}, {2005.` , 2769.046942`}, {2006.` , 2803.605088`},
{2007.` , 2746.479825`}, {2008.` , 2737.860822`}, {2009.` , 2699.245242`},
{2010.` , 2767.507814`}, {2011.` , 2651.771616`}, {2012.` , 2472.44864`},
{2013.` , 2491.705601`}, {2014.` , 2541.027341`}, {2015.` , 2575.664304`},
{2016.` , 2612.83283`}, {2017.` , 2635.561104`}};
```

Bio - bränslen (TWh)

```
biobransle = {{1990.` , 11111.11111`}, {1991.` , 11242.7549`},
{1992.` , 11375.95839`}, {1993.` , 11510.74008`}, {1994.` , 11647.11865`},
{1995.` , 11785.11302`}, {1996.` , 11924.74234`}, {1997.` , 12066.02598`},
{1998.` , 12208.98355`}, {1999.` , 12414.05573`}, {2000.` , 12500.`},
{2001.` , 12500.`}, {2002.` , 12470.`}, {2003.` , 12328.70237`},
{2004.` , 12159.75217`}, {2005.` , 12076.14729`}, {2006.` , 11993.11724`},
{2007.` , 11910.65806`}, {2008.` , 11828.76583`}, {2009.` , 11747.43666`},
{2010.` , 11666.66667`}, {2011.` , 11553.3766`}, {2012.` , 11441.18663`},
{2013.` , 11330.0861`}, {2014.` , 11220.06442`}, {2015.` , 11111.11111`},
{2016.` , 11003.2158`}, {2017.` , 10895.32049`}};
```

Andra Förnybara Energikällor (TWh)

```
andrafornybara = {{1990.` , 116.4628246`},
```

```
{1991.` , 121.4122701`}, {1992.` , 130.3448548`}, {1993.` , 134.7069628`},
{1994.` , 139.8004029`}, {1995.` , 145.5958811`}, {1996.` , 149.6884804`},
{1997.` , 160.9528063`}, {1998.` , 168.4548712`}, {1999.` , 177.1371664`},
{2000.` , 185.2722028`}, {2001.` , 191.0179267`}, {2002.` , 205.6996386`},
{2003.` , 217.2027959`}, {2004.` , 234.3682046`}, {2005.` , 254.3922875`},
{2006.` , 271.7633551`}, {2007.` , 294.2977297`}, {2008.` , 314.3656167`},
{2009.` , 338.2157334`}, {2010.` , 378.0383427`}, {2011.` , 397.4546676`},
{2012.` , 430.3624386`}, {2013.` , 463.9825019`}, {2014.` , 504.3899227`},
{2015.` , 538.2067786`}, {2016.` , 556.9861292`}, {2017.` , 586.1710901`}};
```

Vattenkraft (TWh)

```
vatten = {{1990.` , 2161.045291`}, {1991.` , 2213.110915`},
{1992.` , 2211.503167`}, {1993.` , 2344.266136`}, {1994.` , 2359.685227`},
{1995.` , 2488.983207`}, {1996.` , 2523.481143`}, {1997.` , 2569.633113`},
{1998.` , 2590.551798`}, {1999.` , 2608.338262`}, {2000.` , 2654.953445`},
{2001.` , 2586.668594`}, {2002.` , 2633.835653`}, {2003.` , 2629.430399`},
{2004.` , 2808.226932`}, {2005.` , 2918.064831`}, {2006.` , 3030.307944`},
{2007.` , 3079.79887`}, {2008.` , 3263.589026`}, {2009.` , 3253.601171`},
{2010.` , 3435.905581`}, {2011.` , 3503.227091`}, {2012.` , 3671.297583`},
{2013.` , 3797.954118`}, {2014.` , 3887.930335`}, {2015.` , 3891.408797`},
{2016.` , 4036.073668`}, {2017.` , 4059.868393`}};
```

Vindkraft (TWh)

```
vind = {{1990.` , 3.632470516`}, {1991.` , 4.086706675`},
{1992.` , 4.733212019`}, {1993.` , 5.697568819`}, {1994.` , 7.122929844`},
{1995.` , 8.261923444`}, {1996.` , 9.204610762`}, {1997.` , 12.01757667`},
{1998.` , 15.91490057`}, {1999.` , 21.21534431`}, {2000.` , 31.41996387`},
{2001.` , 38.39098735`}, {2002.` , 52.33180737`}, {2003.` , 62.91691456`},
{2004.` , 85.11605376`}, {2005.` , 104.0868359`}, {2006.` , 132.8592792`},
{2007.` , 170.6860872`}, {2008.` , 220.5696719`}, {2009.` , 275.9292658`},
{2010.` , 341.5652412`}, {2011.` , 436.8034429`}, {2012.` , 523.8148612`},
{2013.` , 645.7219776`}, {2014.` , 712.4070431`}, {2015.` , 831.8262454`},
{2016.` , 959.4687163`}, {2017.` , 1122.74585`}};
```

Solenergi (TWh)

```
sol = {{1990.` , 0.`}, {1991.` , 0.505223075`},
{1992.` , 0.468615413`}, {1993.` , 0.556737928`}, {1994.` , 0.60006443`},
{1995.` , 0.640874386`}, {1996.` , 0.705278679`}, {1997.` , 0.756655499`},
{1998.` , 0.880289501`}, {1999.` , 0.965823997`}, {2000.` , 1.177935576`},
{2001.` , 1.463956125`}, {2002.` , 1.831247734`}, {2003.` , 2.3293707`},
{2004.` , 3.054656084`}, {2005.` , 4.249617769`}, {2006.` , 5.818328387`},
{2007.` , 7.864870878`}, {2008.` , 12.72162081`}, {2009.` , 21.09259048`},
{2010.` , 33.82948514`}, {2011.` , 65.21188479`}, {2012.` , 100.9252749`},
{2013.` , 139.0442186`}, {2014.` , 197.6716635`}, {2015.` , 260.0058008`},
{2016.` , 328.1826964`}, {2017.` , 442.6183606`}};
```

Världens total energikonsumtion (TWh)

```
totalt = {{1990.` , 98462.371847116`}, {1991.` , 98987.38143285`},
{1992.` , 99813.54908523199`}, {1993.` , 100216.423316547`},
{1994.` , 101537.18489717401`}, {1995.` , 103296.25934793001`},
{1996.` , 106154.70010584098`}, {1997.` , 107376.31135546902`},
```

```

{1998., 108022.57284627101}, {1999., 109856.69807370701},
{2000., 112416.258116246}, {2001., 113610.635952175},
{2002., 115901.223848704}, {2003., 119930.15013616001},
{2004., 124960.08846344402}, {2005., 128897.75152416898},
{2006., 132297.06634468702}, {2007., 136405.679742778},
{2008., 137662.43593741}, {2009., 135324.15543267998},
{2010., 141265.10288404}, {2011., 144422.53459229},
{2012., 146106.05926769998}, {2013., 148234.8407671},
{2014., 149077.14748530003}, {2015., 149790.2224058},
{2016., 151341.68784990002}, {2017., 153595.6630277}};

{ctotalt, dtotalt} = {c, d} /. FindFit[totalt, {c (x - 1990) + d}, {c, d}, x]
{2314.87, 92 × 855.}
totaltfunktion[x_] := ctotalt (x - 1990) + dtotalt
totaltgenomsnitt = Plot[totaltfunktion[x], {x, 1990, 2050},
AxesLabel → {"År", "Energi [TWh]"}, PlotStyle → {Magenta},
PlotLabel → "total konsumtion Genomsnittlig "]

{colja, dolja} = {c, d} /. FindFit[olja, {c (x - 1990) + d}, {c, d}, x]
{606.174, 37 × 053.3}
oljafunktion[x_] := colja (x - 1990) + dolja
oljaberaknad = Plot[oljafunktion[x], {x, 1990, 2050},
AxesLabel → {"År", "Energi [TWh]"}, PlotStyle → {Black},
PlotLabel → "konsumtion av energi från olja Beräknad"]

{cvatten, dvatten} = {c, d} /. FindFit[vatten, {c (x - 1990) + d}, {c, d}, x]
{71.3453, 2008.72}
vattenfunktion[x_] := cvatten (x - 1990) + dvatten
vattenberaknad = Plot[vattenfunktion[x], {x, 1990, 2050},
AxesLabel → {"År", "Energi [TWh]"}, PlotStyle → {Grey},
PlotLabel → "konsumtion av energi från vatten Beräknad"]

{cvind, dvind} = {c, d} /. FindFit[vind, {c Exp[d (x - 1990)]}, {c, d}, x]
{9.25548, 0.179304}
vindfunktion[x_] := cvind Exp[bvind (x - 1990)]
vindberaknad = Plot[vindfunktion[x], {x, 1990, 2050},
AxesLabel → {"År", "Energi [TWh]"}, PlotStyle → {Red},
PlotLabel → "konsumtion av energi från vindkraft Beräknad"]

{csol, dsol} = {c, d} /. FindFit[sol, {c Exp[d (x - 1990)]}, {c, d}, x]
{0.104136, 0.310299}
solfunktion[x_] := csol Exp[dsol (x - 1990)]
solberaknad = Plot[solfunktion[x], {1990, 2050},
AxesLabel → {"År", "Energi [TWh]"}, PlotStyle → {Green},
PlotLabel → "konsumtion av solenergi Beräknad"]

```



```

{candrafornybara, dandrafornybara} =
  {c, d} /. FindFit[andrafornybara, {c (x - 1990) + d}, {c, d}, x]
  {17.1558, 47.2089}
andrafornybarafunktion[x_] := candrafornybara (x - 1990) + dandrafornybara
andrafornybaraberaknad = Plot[andrafornybarafunktion[x],
  {x, 1990, 2050}, AxesLabel → {"År", "Energi [TWh]"}, PlotStyle → {Cyan},
  PlotLabel → "konsumtion av energi andra förnybara källor Beräknad" ]

{ckol, dkol} = {c, d} /. FindFit[kol, {c (x - 1990) + d}, {c, c}, x]
{908.405, 21 × 826.1}
kolfunktion[x_] := ckol (x - 1990) + dkol
kolberaknad = Plot[kolfunktion[x], {x, 1990, 2050},
  AxesLabel → {"År", "Energi [TWh]"}, PlotStyle → {Brown},
  PlotLabel → "konsumtion av energi från kol Beräknad" ]

{cnaturgas, dnaturgas} =
  {c, d} /. FindFit[naturgas, {c Exp[d (x - 1990)]}, {c, d}, x]
  {18 × 874.3, 0.0249077}
naturgasfunktion[x_] := cnaturgasExp[dnaturgas (x - 1990)]
naturgasberaknad = Plot[naturgasfunktion[x], {x, 1990, 2050},
  AxesLabel → {"År", "Energi [TWh]"}, PlotStyle → {Purple},
  PlotLabel → "konsumtion av energi från naturgaskraft Beräknad" ]

{cbiobransle, dbiobransle} =
  {c, d} /. FindFit[biobransle, {c (x - 1990) + d}, {c, d}, x]
  {-17.7882, 11 × 990.9}
biobranslefunktion[x_] := cbiobransle (x - 1990) + dbiobransle
biobransleberaknad = Plot[biobranslefunktion[x], {x, 1990, 2050},
  AxesLabel → {"År", "Energi [TWh]"}, PlotStyle → {LightBlue},
  PlotLabel → "konsumtion av energi från biobransle Beräknad" ]

{ckarnkraft, dkarnkraft} =
  {c, d} /. FindFit[karnkraft, {c Exp[d (x - 1990)]}, {c, d}, x]
  {2276., 0.00738811}
karnkraftfunktion[x_] := ckarnkraftExp[dkarnkraft (x - 1990)]
karnkraftberaknad = Plot[karnkraftfunktion[x], {x, 1990, 2050},
  AxesLabel → {"År", "Energi [TWh]"}, PlotStyle → {Yellow},
  PlotLabel → "konsumtion av energi från karnkraftkraft Beräknad" ]

```

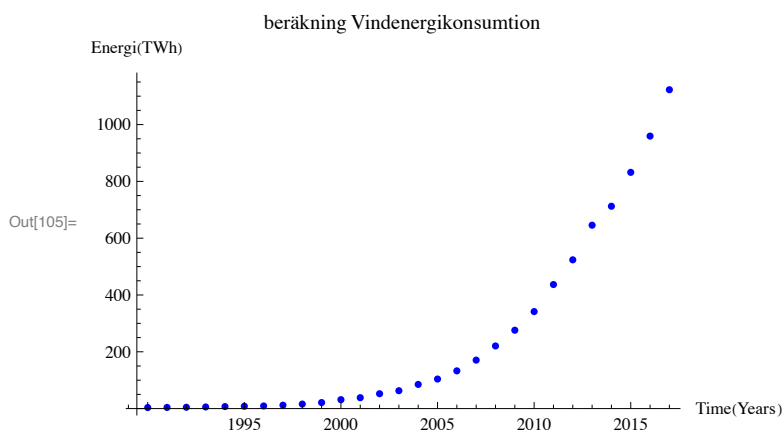
```
totaltfunktion[2036]
199 339.
```

```
vattenfunktion[2036] + vindfunktion[2036] +
  solfunktion[2036] + karnkraftfunktion[2036]
208 512.
```

```
4,
```

```
In[104]:= vind = {{1990., 3.632470516}, {1991., 4.086706675},
  {1992., 4.733212019}, {1993., 5.697568819},
  {1994., 7.122929844}, {1995., 8.261923444}, {1996., 9.204610762},
  {1997., 12.01757667}, {1998., 15.91490057}, {1999., 21.21534431},
  {2000., 31.41996387}, {2001., 38.39098735}, {2002., 52.33180737},
  {2003., 62.91691456}, {2004., 85.11605376}, {2005., 104.0868359},
  {2006., 132.8592792}, {2007., 170.6860872}, {2008., 220.5696719},
  {2009., 275.9292658}, {2010., 341.5652412}, {2011., 436.8034429},
  {2012., 523.8148612}, {2013., 645.7219776}, {2014., 712.4070431},
  {2015., 831.8262454}, {2016., 959.4687163}, {2017., 1122.74585}}
ListPlot[vind, PlotRange -> All, AxesLabel -> {"Time(Years)", "Energi(TWh)"},
  PlotStyle -> {Blue}, PlotLabel -> Vindenergikonsumtion beräkning]
```

```
Out[104]= {{1990., 3.63247}, {1991., 4.08671}, {1992., 4.73321}, {1993., 5.69757},
  {1994., 7.12293}, {1995., 8.26192}, {1996., 9.20461}, {1997., 12.0176},
  {1998., 15.9149}, {1999., 21.2153}, {2000., 31.42}, {2001., 38.391},
  {2002., 52.3318}, {2003., 62.9169}, {2004., 85.1161}, {2005., 104.087},
  {2006., 132.859}, {2007., 170.686}, {2008., 220.57}, {2009., 275.929},
  {2010., 341.565}, {2011., 436.803}, {2012., 523.815}, {2013., 645.722},
  {2014., 712.407}, {2015., 831.826}, {2016., 959.469}, {2017., 1122.75}}
```

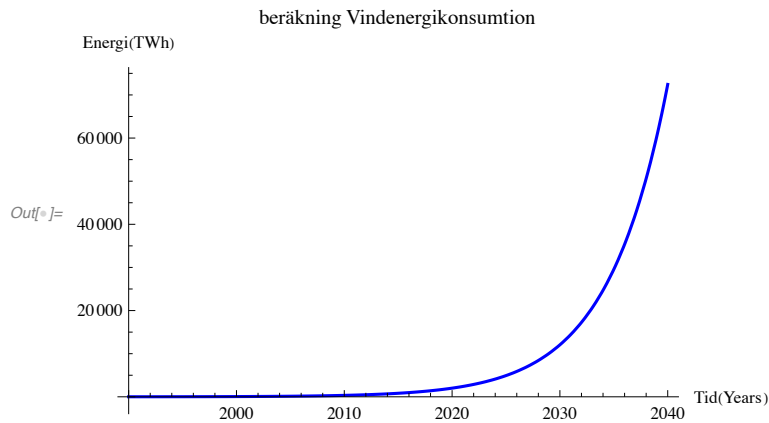


```
In[ ]:= {avind, bvind} = {a, b} /. FindFit[vind, {a Exp[b (t - 1990)]}, {a, b}, t]
```

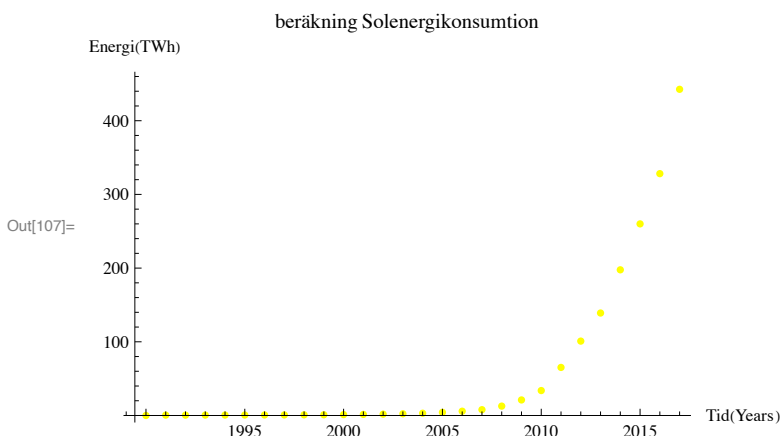
```
Out[ ]:= {9.25548, 0.179304}
```

```
vindfunktion[t_] := avind Exp[bvind (t - 1990)]
```

```
In[8]:= beraknavind = Plot[vindfunktion[t], {t, 1990, 2040},
  PlotRange -> All, AxesLabel -> {"Tid (Years)", "Energi (TWh)"},
  PlotStyle -> {Blue}, PlotLabel -> Vindenergikonsumtion beräkning]
```



```
In[106]:= sol = {{1990., 0.}, {1991., 0.505223075},
  {1992., 0.468615413}, {1993., 0.556737928}, {1994., 0.60006443},
  {1995., 0.640874386}, {1996., 0.705278679}, {1997., 0.756655499},
  {1998., 0.880289501}, {1999., 0.965823997}, {2000., 1.177935576},
  {2001., 1.463956125}, {2002., 1.831247734}, {2003., 2.3293707},
  {2004., 3.054656084}, {2005., 4.249617769}, {2006., 5.818328387},
  {2007., 7.864870878}, {2008., 12.72162081}, {2009., 21.09259048},
  {2010., 33.82948514}, {2011., 65.21188479}, {2012., 100.9252749},
  {2013., 139.0442186}, {2014., 197.6716635}, {2015., 260.0058008},
  {2016., 328.1826964}, {2017., 442.6183606}};
ListPlot[sol, AxesLabel -> {"Tid (Years)", "Energi (TWh)"},
  PlotStyle -> {Yellow}, PlotLabel -> Solenergikonsumtion beräkning]
```

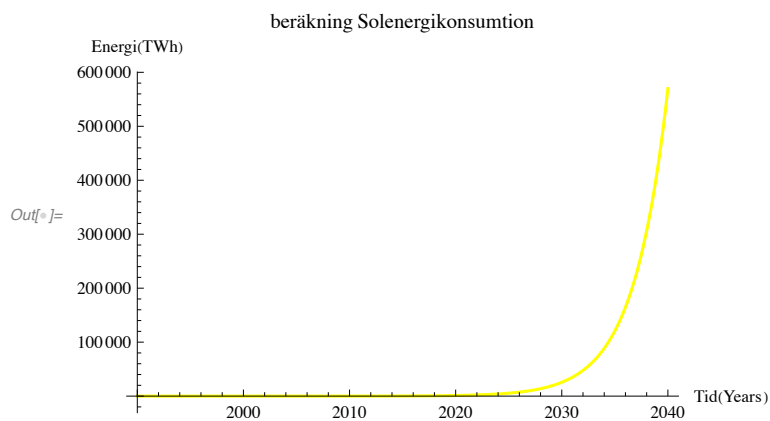


```
In[9]:= {asol, bsol} = {a, b} /. FindFit[sol, {a Exp[b (t - 1990)]}, {a, b}, t]
```

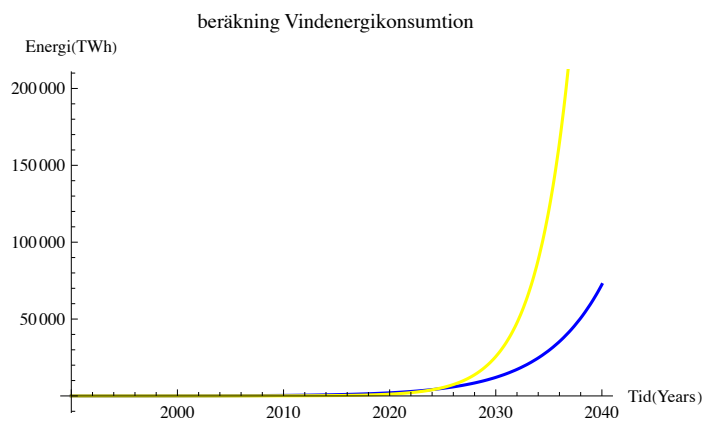
```
Out[9]= {0.104136, 0.310299}
```

```
In[9]:= solfunktion[t_] := asol Exp[bsol (t - 1990)]
```

```
In[ ]:= beraknasol = Plot[solfunktion[t], {t, 1990, 2040},
  PlotRange -> All, AxesLabel -> {"Tid (Years)", "Energi (TWh)"},
  PlotStyle -> {Yellow}, PlotLabel -> Solenergikonsumtion beräkning]
```



```
Show[beraknavind, beraknasol, PlotRange -> {200 000, 0}]
```



5, (*Ingen kod träsvs*)

6, (*Ingen kod krävs*)

7, (*Ingen kod krävs*)