

CS 440: Introduction to Artificial Intelligence

Lecture 10

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Recap— Search

- ▶ Initial state
- ▶ Possible actions in each state
- ▶ Transition model:
Takes state and action and gives new state
- ▶ Goal test
Describes whether state is what you want
- ▶ Path cost
Says how easy or hard action sequence is

Recap— Search

Many ways to formalize any problem: Want

- ▶ few actions at each point
- ▶ short paths to solutions
- ▶ match with search algorithm

Example

Interpreting Minesweeper Boards

		1	1		
		2	2		
	1	2		2	1
	2	3	2	1	0
			1	1	1
			1	1	

Example

Interpreting Minesweeper Boards

		1	1	X	X
	X	2	2		X
	1	2	X	2	1
	2	3	2	1	0
	X	X	1	1	1
			1	1	X

Formalizing Minesweeper

State:

- ▶ board with unexplained counts

Action:

- ▶ hypothesize a mine at (x, y)
- ▶ nuances to avoid duplication

Transition

- ▶ decrement counts adjacent to newly-placed mine

Goal

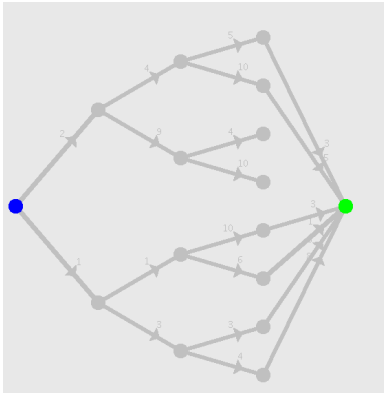
- ▶ unexplained counts are 0

Today's Focus: Path Cost

Generalize from steps of cost 1 to steps with positive cost

- ▶ Number of steps measures complexity of *constructing* solution
- ▶ Path cost measures complexity of *using* solution
- ▶ Key insight: These are not necessarily the same

Example



File is bfg.xml

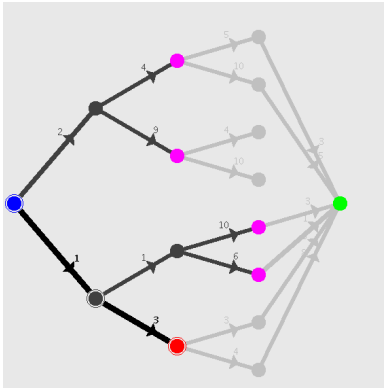
Costs more visible
in upcoming slides

Natural first step

Best-first search

- ▶ Generalization of breadth-first search
- ▶ Sort frontier based on path cost rather than number of steps

Snapshot

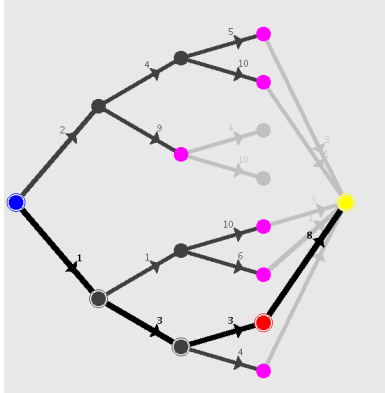


Here we've expanded all nodes of cost 2.

Move to next node, with cost 4.

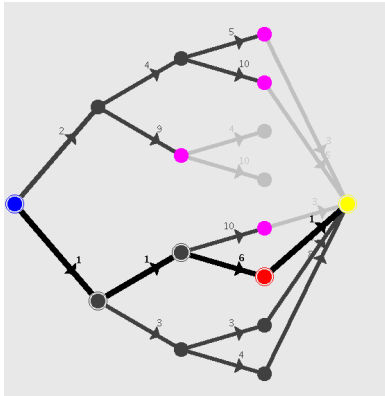
Complication

Solution as first added to frontier...



Complication

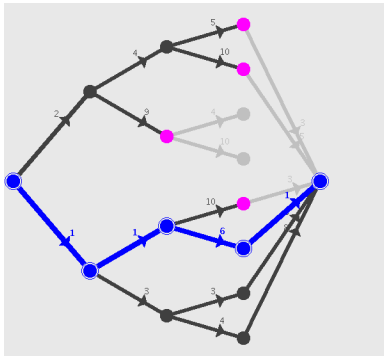
...may not have least-cost path.



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Want to make sure

- ▶ search reports least-cost solution
- ▶ frontier associates states with least-cost path



Pseudocode - Variables

- ▶ *node*: current node being visited
- ▶ *frontier*: priority queue of nodes still to visit ordered by heuristic cost
- ▶ *explored*: set of nodes already visited

Pseudocode - Initialization

- ▶ *node* : initial state of problem, heuristic cost
- ▶ *frontier* : queue with *node* as only element
- ▶ *explored* : empty set

Pseudocode - Now repeat

- ▶ if frontier is empty return failure
- ▶ set *node* to result of popping best from *frontier*
- ▶ if *node* is a goal, return *node*
- ▶ add *node* to explored list
- ▶ process *node*'s children

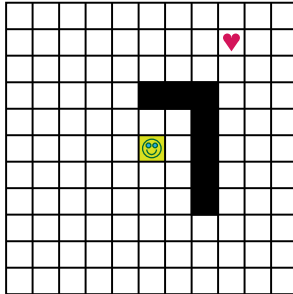
Process node's children

For each possible *action* from *node*

- ▶ construct *child* by applying *action* to *node*
- ▶ if *child* state is not in *explored* or *frontier*
insert *child* on *frontier*
- ▶ if *child* state is on *frontier* with higher cost
remove old node and add *child* to *frontier*

Path planning in games

- ▶ Position, destination, $\{ n, s, e, w \}$



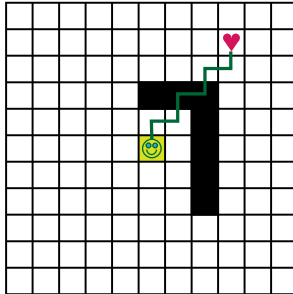
Breadth-first search

- Search by cost so far

10	9	8	7	6	7	8	9	10	11	12
9	8	7	6	5	6	7	8	♥	10	11
8	7	6	5	4	5	6	7	8	9	10
7	6	5	4	3				9	10	11
6	5	4	3	2	1	2		10	11	12
5	4	3	2	1	😊	1		9	10	11
6	5	4	3	2	1	2		8	9	10
7	6	5	4	3	2	3		7	8	9
8	7	6	5	4	3	4	5	6	7	8
9	8	7	6	5	4	5	6	7	8	9
10	9	8	7	6	5	6	7	8	9	10

Heuristics and lookahead

- Can make a rough guess at work remaining



Shape of heuristic function

- Optimistic but useful

9	8	7	6	5	4	3	2	1	2	3		
8	7	6	5	4	3	2	1	♥	1	2		
9	8	7	6	5	4	3	2	1	2	3		
10	9	8	7	6				2	3	4		
11	10	9	8	7				6	5	3	4	5
12	11	10	9	8				😊	6	4	5	6
13	12	11	10	9				8	7	5	6	7
14	13	12	11	10	9	8			6	7	8	
15	14	13	12	11	10	9			8	7	8	9
16	15	14	13	12	11	10			9	8	9	10
17	16	15	14	13	12	11			10	9	10	11

Combine cost and heuristic

► Measures

19	17	15	13	11	11	11	11	11	13	15
17	15	13	11	9	9	9	9	♥	11	13
17	15	13	11	9	9	9	9		11	13
17	15	13	11	9					11	13
17	15	13	11	9	7	7			13	15
17	15	13	11	9	😊	7			13	15
19	17	15	13	11	9	9			13	15
21	19	17	15	13	11	11			13	15
23	21	19	17	15	13	13	13	13	15	17
25	23	21	19	17	15	15	15	15	17	19
27	25	23	21	19	17	17	17	17	19	21

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10	9	8	7	6	7	8	9	10	11	12
9	8	7	6	5	6	7	8	♥	10	11
8	7	6	5	4	5	6	7	8	9	10
7	6	5	4	3				9	10	11
6	5	4	3	2	1	2		10	11	12
5	4	3	2	1	😊	1		9	10	11
6	5	4	3	2	1	2		8	9	10
7	6	5	4	3	2	3		7	8	9
8	7	6	5	4	3	4	5	6	7	8
9	8	7	6	5	4	5	6	7	8	9
10	9	8	7	6	5	6	7	8	9	10

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9	8	7	6	5	4	3	2	1	2	3
8	7	6	5	4	3	2	1	♥	1	2
9	8	7	6	5	4	3	2	1	2	3
10	9	8	7	6					2	3
11	10	9	8	7	6	5			3	4
12	11	10	9	8	😊	6			4	5
13	12	11	10	9	8	7			5	6
14	13	12	11	10	9	8			6	7
15	14	13	12	11	10	9	8	7	8	9
16	15	14	13	12	11	10	9	8	9	10
17	16	15	14	13	12	11	10	9	10	11

A* Search

Practical variant of heuristic search

- ▶ Go-to-method for informed search
- ▶ Assumes you have a good way to measure progress

Basic idea: Explore the search node that looks most promising

- ▶ Measure progress by actual cost already incurred
- ▶ *plus* estimate of cost remaining

Demonstration

`http:
//www.vision.ee.ethz.ch/~cvcourse/astar/AStar.html`

Observations about A* Search

- ▶ Finds optimal solutions
- ▶ Minimal search if you can find a solution without detours
Just explore zone of optimal solutions
- ▶ Search can be exponential in size of smallest detour needed