

# CS 440: Introduction to Artificial Intelligence

## Lecture 9

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## Recap— Search

- ▶ Initial state
- ▶ Possible actions in each state
- ▶ Transition model:  
Takes state and action and gives new state
- ▶ Goal test  
Describes whether state is what you want
- ▶ Path cost  
Says how easy or hard action sequence is

## Recap— Breadth-first search

Simple regime for exploring

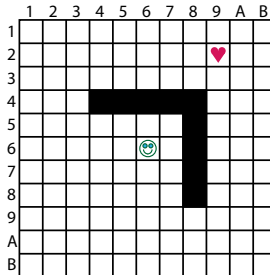
- ▶ Gradually “fan out” into the search space
- ▶ Explore level by level
- ▶ Consider all the nodes at level  $n$  first
- ▶ Then consider nodes at level  $n + 1$  (and so on)

## Recap—Depth-first search

- ▶ Implement frontier as a stack
- ▶ Small space requirements
- ▶ Efficient realization through function calls
- ▶ Not always shortest path first
- ▶ Related idea: “iterative deepening”

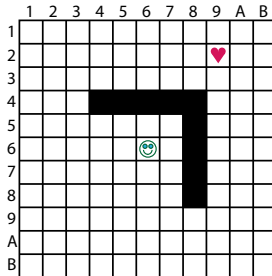
## Example

- ▶ planning paths in a tiled world
- ▶ can move one square n, s, e, w
- ▶ cannot move through obstacles
- ▶ must stay on board



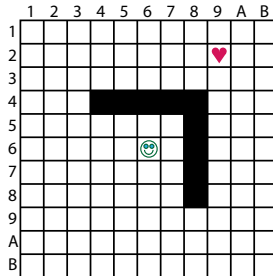
## Mr Happy wants to find love

- ▶ initial state?
- ▶ goal test?
- ▶ actions in (6,6)? in (7,6)? in (7,5)? in (7,3)?



## Mr Happy wants to find love

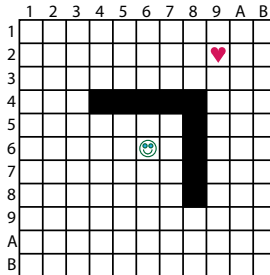
- ▶ initial state?
- ▶ goal test?
- ▶ actions in (6,6)? in (7,6)? in (7,5)? in (7,3)?



init:(6,6). goal(s):s=(9,2). (6,6):{n,s,e,w}. (7,6):{n,s,w}. (7,5):{s,w}. (7,3):{n,e,w}.

## Questions

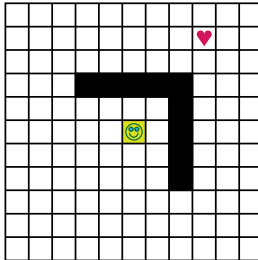
- ▶ BFS frontier after depth 0?
- ▶ After depth 1?
- ▶ After depth 2?
- ▶ After depth 3?





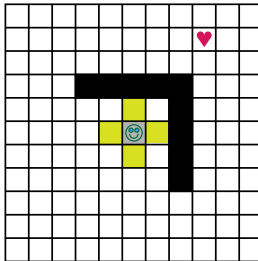
# Questions

- ▶ BFS frontier after depth 0?



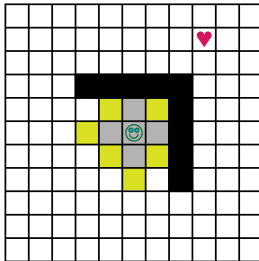
# Questions

- ▶ BFS frontier after depth 1?



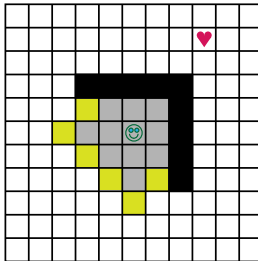
# Questions

- ▶ BFS frontier after depth 2?



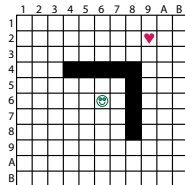
## Questions

- ▶ BFS frontier after depth 3?



## Questions about uninformed search

- ▶ Do you need frontier, explored list for DFS here?
- ▶ Why or why not?
- ▶ What does that say about DFS memory use?



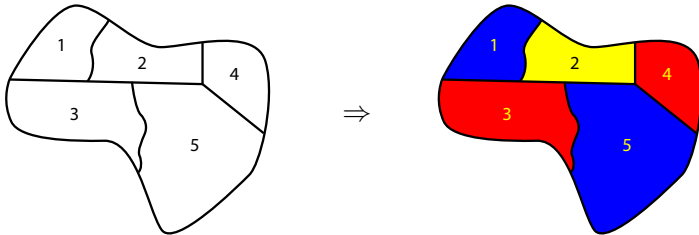
## Questions about uninformed search

- ▶ Do you need frontier, explored list for DFS here?
  - ▶ Yes, otherwise DFS will search many redundant paths
- ▶ What does that say about DFS memory use?
  - ▶ No way to use tree model of DFS search with cheap memory

# Map Coloring

- ▶ each “country” gets a color
- ▶ neighboring countries must get different colors
- ▶ use at most  $k$  colors  
interesting cases:  $k$  is 3 or 4

# Example





# Representation for DFS

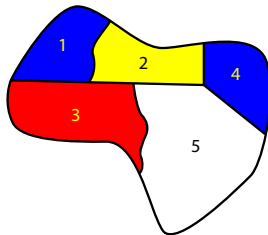
- ▶ Node is assignment of colors to first  $i$  countries
- ▶ Action is assign consistent color to country  $i + 1$
- ▶ Goal is all countries colored

Demo at <http://www.mathcove.net/petersen/lessons/get-lesson?les=14>

## Search example

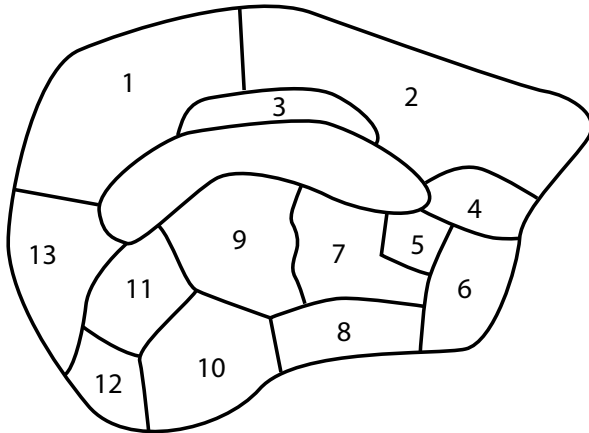
3 color our map

- ▶ Assign color 1 to country 1
- ▶ Assign color 2 to country 2
- ▶ Assign color 3 to country 3
- ▶ Assign color 1 to country 4
- ▶ Dead end: must backtrack



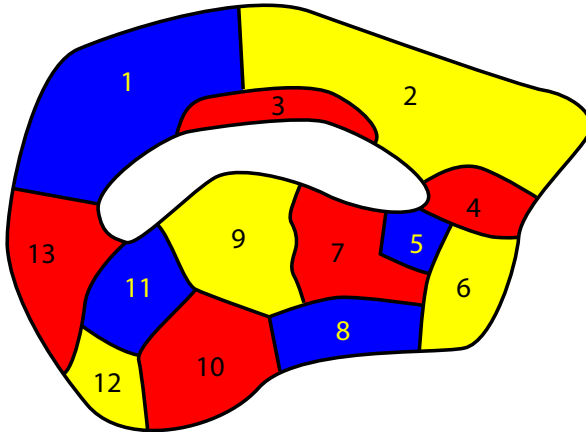
## Aside: making search plausible

3 color “donutland”



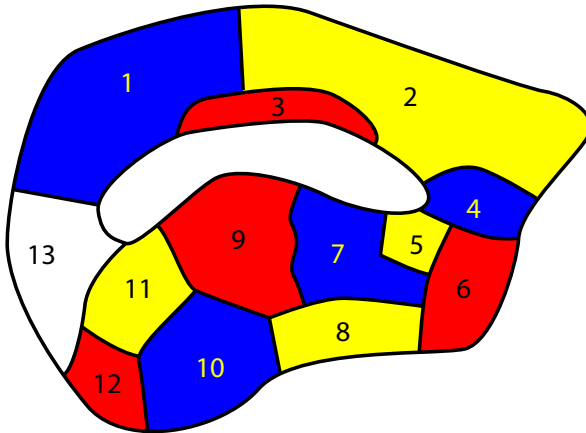
## Aside: making search plausible

Answer



## Aside: making search plausible

Serious dead end



# Properties of representation

- ▶ Solution lies at depth  $n$  for  $n$  countries
- ▶ Search space is a tree

## Alternative representation

- ▶ Node is assignment of colors to all  $n$  countries (not necessarily consistent)
- ▶ Action is change color of any country  $i$
- ▶ Goal is consistent coloring

# Properties of representation

- ▶ Solution may be very close to random initial point
- ▶ Search space is graph
- ▶ Many paths between any two states
- ▶ Suitable representation for local search (see next week)
  - ▶ hill climbing
  - ▶ simulated annealing
  - ▶ genetic search

Demo at <http://www.ff.iij4u.or.jp/~kanada/ccm/coloring/>