

$$P := P_2 \cdot x^2 + P_1 \cdot x + P_0$$

$$P := P_2 x^2 + P_1 x + P_0 \quad (1)$$

$$Q_1 := Q_{11} \cdot x + Q_{10}$$

$$Q_1 := Q_{11} x + Q_{10} \quad (2)$$

$$Q_2 := Q_{21} \cdot x + Q_{20}$$

$$Q_2 := Q_{21} x + Q_{20} \quad (3)$$

$$Q := \text{collect}(Q_1 \cdot Q_2, x)$$

$$Q := Q_{11} Q_{21} x^2 + (Q_{10} Q_{21} + Q_{11} Q_{20}) x + Q_{10} Q_{20} \quad (4)$$

$$R := R_2 \cdot x^2 + R_1 \cdot x + R_0$$

$$R := R_2 x^2 + R_1 x + R_0 \quad (5)$$

$$g := \text{collect}(P \cdot Q_1, x)$$

$$g := P_2 Q_{11} x^3 + (P_1 Q_{11} + P_2 Q_{10}) x^2 + (P_0 Q_{11} + P_1 Q_{10}) x + P_0 Q_{10} \quad (6)$$

$$g := P_2 Q_{11} x^3 + (P_1 Q_{11} + P_2 Q_{10}) x^2 + (P_0 Q_{11} + P_1 Q_{10}) x + P_0 Q_{10} \quad (7)$$

$$h := \text{collect}\left(\frac{Q_2 \cdot R}{4 \cdot \Delta}, x\right)$$

$$h := \frac{Q_{21} R_2 x^3}{4 \Delta} + \frac{(Q_{20} R_2 + Q_{21} R_1) x^2}{4 \Delta} + \frac{(Q_{20} R_1 + Q_{21} R_0) x}{4 \Delta} + \frac{Q_{20} R_0}{4 \Delta} \quad (8)$$

$$T := [\text{coeff}(g, x, 2) \cdot \text{coeff}(h, x, 0) + \text{coeff}(g, x, 0) \cdot \text{coeff}(h, x, 2), \text{coeff}(g, x, 3) \cdot \text{coeff}(h, x, 0) + \text{coeff}(g, x, 0) \cdot \text{coeff}(h, x, 3), -\text{coeff}(g, x, 3) \cdot \text{coeff}(h, x, 1) - \text{coeff}(g, x, 1) \cdot \text{coeff}(h, x, 3), 4]$$

$$T := \quad (9)$$

$$\left[\frac{(P_1 Q_{11} + P_2 Q_{10}) Q_{20} R_0}{4 \Delta} + \frac{P_0 Q_{10} (Q_{20} R_2 + Q_{21} R_1)}{4 \Delta} \frac{P_2 Q_{11} Q_{20} R_0}{4 \Delta} + \frac{P_0 Q_{10} Q_{21} R_2}{4 \Delta} - \dots \right]$$

$$\phi_1 := -\frac{1}{16 \cdot \Delta} \left(\text{coeff}(P, x, 2)^2 \cdot \text{coeff}(Q, x, 0) \cdot \text{coeff}(R, x, 0) + \text{coeff}(P, x, 2) \cdot \text{coeff}(P, x, 0) \cdot (\text{coeff}(Q, x, 2) \cdot \text{coeff}(R, x, 0) + \text{coeff}(Q, x, 1) \cdot \text{coeff}(R, x, 1) + \text{coeff}(Q, x, 0) \cdot \text{coeff}(R, x, 2)) + \text{coeff}(P, x, 0)^2 \cdot \text{coeff}(Q, x, 2) \cdot \text{coeff}(R, x, 2) \right)$$

$$\phi_1 := -\frac{P_2^2 Q_{10} Q_{20} R_0 + P_2 P_0 (Q_{11} Q_{21} R_0 + (Q_{10} Q_{21} + Q_{11} Q_{20}) R_1 + Q_{10} Q_{20} R_2) + P_0^2 Q_{11} Q_{21} R_2}{16 \Delta} \quad (10)$$

$$\phi_2 := -\frac{1}{16 \cdot \Delta} \left(\text{coeff}(Q, x, 2)^2 \cdot \text{coeff}(P, x, 0) \cdot \text{coeff}(R, x, 0) + \text{coeff}(Q, x, 2) \cdot \text{coeff}(Q, x, 0) \cdot (\text{coeff}(P, x, 2) \cdot \text{coeff}(R, x, 0) + \text{coeff}(P, x, 1) \cdot \text{coeff}(R, x, 1) + \text{coeff}(P, x, 0) \cdot \text{coeff}(R, x, 2)) + \text{coeff}(Q, x, 0)^2 \cdot \text{coeff}(P, x, 2) \cdot \text{coeff}(R, x, 2) \right)$$

$$\phi_2 := -\frac{Q_{11}^2 Q_{21}^2 P_0 R_0 + Q_{11} Q_{21} Q_{10} Q_{20} (P_0 R_2 + P_1 R_1 + P_2 R_0) + Q_{10}^2 Q_{20}^2 P_2 R_2}{16 \Delta} \quad (11)$$

$$\phi_3 := -\frac{1}{16 \cdot \Delta} \left(\text{coeff}(R, x, 2)^2 \cdot \text{coeff}(Q, x, 0) \cdot \text{coeff}(P, x, 0) + \text{coeff}(R, x, 2) \cdot \text{coeff}(R, x, 0) \cdot (\text{coeff}(Q, x, 2) \cdot \text{coeff}(P, x, 0) + \text{coeff}(Q, x, 1) \cdot \text{coeff}(P, x, 1) + \text{coeff}(Q, x, 0) \cdot \text{coeff}(P, x, 2)) + \text{coeff}(R, x, 0)^2 \cdot \text{coeff}(Q, x, 2) \cdot \text{coeff}(P, x, 2) \right)$$

$$\begin{aligned} & \cdot \text{coeff}(P, x, 0) + \text{coeff}(Q, x, 1) \cdot \text{coeff}(P, x, 1) + \text{coeff}(Q, x, 0) \cdot \text{coeff}(P, x, 2) + \text{coeff}(R, x, 0)^2 \cdot \text{coeff}(Q, \\ & x, 2) \cdot \text{coeff}(P, x, 2) \big) \\ \phi_3 := & - \frac{R_2^2 Q_{10} Q_{20} P_0 + R_2 R_0 (Q_{11} Q_{21} P_0 + (Q_{10} Q_{21} + Q_{11} Q_{20}) P_1 + Q_{10} Q_{20} P_2) + R_0^2 Q_{11} Q_{21} P_2}{16 \Delta} \end{aligned} \quad (12)$$

$$C := \begin{bmatrix} \text{coeff}(P, x, 2) & \text{coeff}(Q, x, 2) & \text{coeff}(R, x, 2) & 0 \\ -\text{coeff}(P, x, 1) & -\text{coeff}(Q, x, 1) & -\text{coeff}(R, x, 1) & 0 \\ -\text{coeff}(P, x, 0) & -\text{coeff}(Q, x, 0) & -\text{coeff}(R, x, 0) & 0 \\ \phi_1 & \phi_2 & \phi_3 & -\frac{1}{16 \cdot \Delta} \end{bmatrix} \quad (13)$$

$$C := \begin{bmatrix} P_2 & \dots \\ -P_1 & \dots \\ -P_0 & \dots \\ -\frac{P_2^2 Q_{10} Q_{20} R_0 + P_2 P_0 (Q_{11} Q_{21} R_0 + (Q_{10} Q_{21} + Q_{11} Q_{20}) R_1 + Q_{10} Q_{20} R_2) + P_0^2 Q_{11} Q_{21} \dots}{16 \Delta} \end{bmatrix} \quad (14)$$

$$C := \begin{bmatrix} P_2 & \dots \\ -P_1 & \dots \\ -P_0 & \dots \\ -\frac{P_2^2 Q_{10} Q_{20} R_0 + P_2 P_0 (Q_{11} Q_{21} R_0 + (Q_{10} Q_{21} + Q_{11} Q_{20}) R_1 + Q_{10} Q_{20} R_2) + P_0^2 Q_{11} Q_{21} \dots}{16 \Delta} \end{bmatrix} \quad (15)$$

$$W := T \cdot C$$

$$W := \left[\left(\frac{(P_1 Q_{11} + P_2 Q_{10}) Q_{20} R_0}{4 \Delta} + \frac{P_0 Q_{10} (Q_{20} R_2 + Q_{21} R_1)}{4 \Delta} \right) P_2 - \left(\frac{P_2 Q_{11} Q_{20} R_0}{4 \Delta} + \frac{P_0 Q_{10} Q_{21} R_1}{4 \Delta} \right) \right] \quad (16)$$

$$\text{simplify}(-4 \cdot \Delta \cdot W)$$

$$\begin{bmatrix} 0 & (Q_{10}^2 R_2 - Q_{10} Q_{11} R_1 + Q_{11}^2 R_0) (P_0 Q_{21}^2 - P_1 Q_{20} Q_{21} + P_2 Q_{20}^2) & 0 & 1 \end{bmatrix} \quad (16)$$