Relationship between a set of variables and miles per gallon (mpg)

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Executive Summary

This looks at a dataset of a collection of cars in order to explore the relationship between a set of variables and miles per gallon, mpg, (outcome). There is interest in the following two questions:

"Is an automatic or manual transmission better for MPG"

"Quantify the MPG difference between automatic and manual transmissions"

We'll take the following steps:

- Process the data for use
- Explore the data especially focussing on the two paramaters of interest (Transmission and MPG)
- Model selection; where we try different models to help us answer our questions
- Model examination; to see if our best model holds up to our standards
- A Conclusion where we answer the questions based on the data

Processing

First change 'am' to factor (0 = automatic, 1 = manual) And make cylinders a factor as well (since it is not continious)

```
library(ggplot2)
library(GGally)
library(dplyr)
library(ggfortify)
data(mtcars)
mtcarsFactors <- mtcars
mtcarsFactors$am <- as.factor(mtcarsFactors$am)
levels(mtcarsFactors$am) <- c("automatic", "manual")
mtcarsFactors$cyl <- as.factor(mtcarsFactors$cyl)
mtcarsFactors$gear <- as.factor(mtcarsFactors$gear)
mtcarsFactors$vs <- as.factor(mtcarsFactors$vs)
levels(mtcarsFactors$vs) <- c("V", "S")
```

Exploratory data analyses

Look at the dimensions and head of the dataset to get an idea

```r
# Res 1
dim(mtcarsFactors)
```

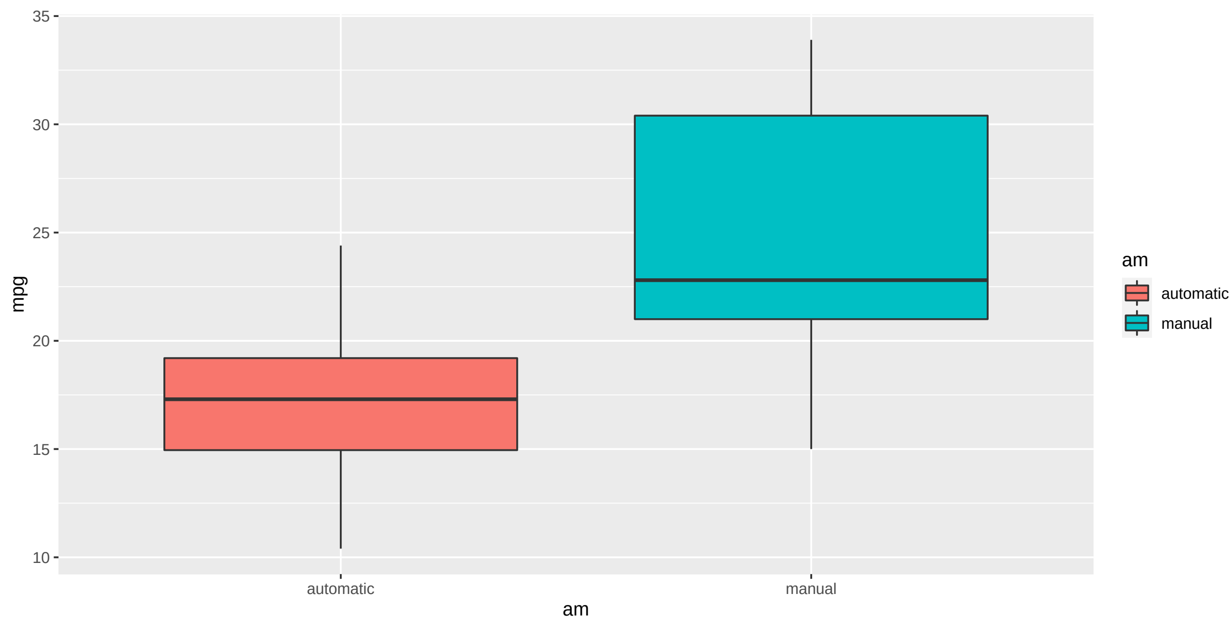
```
## [1] 32 11
```

```r
# Res 2
head(mtcarsFactors)
```

```
##                    mpg cyl disp  hp drat    wt  qsec vs        am gear carb
## Mazda RX4         21.0   6  160 110 3.90 2.620 16.46  V    manual    4    4
## Mazda RX4 Wag     21.0   6  160 110 3.90 2.875 17.02  V    manual    4    4
## Datsun 710        22.8   4  108  93 3.85 2.320 18.61  S    manual    4    1
## Hornet 4 Drive    21.4   6  258 110 3.08 3.215 19.44  S automatic    3    1
## Hornet Sportabout 18.7   8  360 175 3.15 3.440 17.02  V automatic    3    2
## Valiant           18.1   6  225 105 2.76 3.460 20.22  S automatic    3    1
```

Now we take a look at the realtionship between the two parameters we are intereseted in.

```r
# Figure 1
library(ggplot2)
p <- ggplot(mtcarsFactors, aes(am, mpg))
p + geom_boxplot(aes(fill = am))
```



This clearly shows that the manual transmissions have higher mpg's. There could be a bias in the dataset that we are overlooking. Before creating a model let us look at which paramters to include besides 'am'. We look at all correlations of parameters and take only those higher than the 'am' correlation.

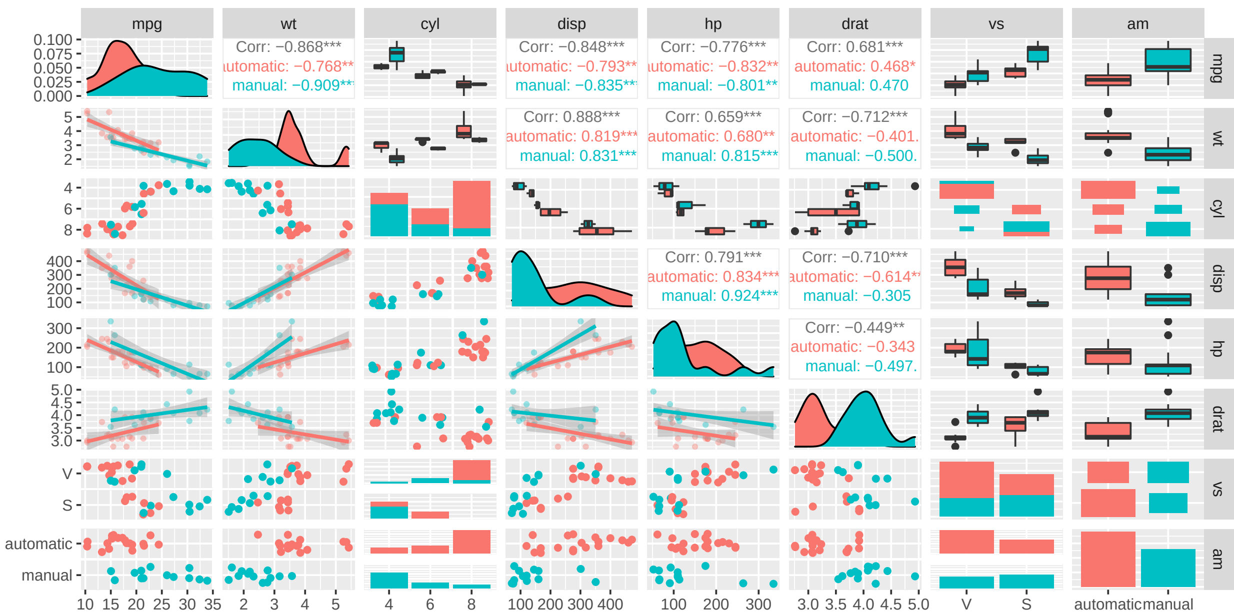
```r
# Res 3
cors <- cor(mtcars$mpg, mtcars)
orderedCors <- cors[,order(-abs(cors[1,]))]
orderedCors
```

```
##        mpg         wt        cyl       disp         hp       drat         vs         am       carb
##  1.0000000 -0.8676594 -0.8521620 -0.8475514 -0.7761684  0.6811719  0.6640389  0.5998324 -0.5509251
##       qsec
##  0.4186840
```

```r
# Res 4
amPos <- which(names(orderedCors)=="am")
subsetColumns <- names(orderedCors)[1:amPos]
subsetColumns
```

```
## [1] "mpg"  "wt"   "cyl"  "disp" "hp"   "drat" "vs"   "am"
```

```r
# Figure 2
mtcarsFactors[,subsetColumns] %>%
  ggpairs(
    mapping = ggplot2::aes(color = am),
    upper = list(continuous = wrap("cor", size = 3)),
    lower = list(continuous = wrap("smooth", alpha=0.4, size=1), combo = wrap("dot"))
  )
```



Model selection

Now that we have seen that mpg has many other (stronger) correlations other than 'am' we can guess that a model predicting the mpg solely on this parameter will not be the most accurate model. Let's check this out.

First we start with a basic linear model

```r
# Res 5
basicFit <- lm(mpg ~ am, mtcarsFactors)
summary(basicFit)
```

```
##
## Call:
## lm(formula = mpg ~ am, data = mtcarsFactors)
##
## Residuals:
##     Min      1Q  Median      3Q     Max
## -9.3923 -3.0923 -0.2974  3.2439  9.5077
##
## Coefficients:
##             Estimate Std. Error t value Pr(>|t|)
## (Intercept)   17.147      1.125  15.247 1.13e-15 ***
## ammanual       7.245      1.764   4.106 0.000285 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4.902 on 30 degrees of freedom
## Multiple R-squared:  0.3598, Adjusted R-squared:  0.3385
## F-statistic: 16.86 on 1 and 30 DF,  p-value: 0.000285
```

The p-values are actually quite low and the R-squared is problematic. Now go to the other side of the spectrum by fitting all parameters of mtcars

```
# Res 6
totalFit <- lm(mpg ~ ., mtcarsFactors)
summary(totalFit)
```

```
##
## Call:
## lm(formula = mpg ~ ., data = mtcarsFactors)
##
## Residuals:
##     Min      1Q  Median      3Q     Max
## -3.2015 -1.2319  0.1033  1.1953  4.3085
##
## Coefficients:
##             Estimate Std. Error t value Pr(>|t|)
## (Intercept) 15.09262   17.13627   0.881   0.3895
## cyl6        -1.19940    2.38736  -0.502   0.6212
## cyl8         3.05492    4.82987   0.633   0.5346
## disp         0.01257    0.01774   0.708   0.4873
## hp          -0.05712    0.03175  -1.799   0.0879 .
## drat         0.73577    1.98461   0.371   0.7149
## wt          -3.54512    1.90895  -1.857   0.0789 .
## qsec         0.76801    0.75222   1.021   0.3201
## vsS          2.48849    2.54015   0.980   0.3396
## ammanual     3.34736    2.28948   1.462   0.1601
## gear4       -0.99922    2.94658  -0.339   0.7382
## gear5        1.06455    3.02730   0.352   0.7290
## carb         0.78703    1.03599   0.760   0.4568
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.616 on 19 degrees of freedom
```

```
## Multiple R-squared:  0.8845, Adjusted R-squared:  0.8116
## F-statistic: 12.13 on 12 and 19 DF,  p-value: 1.764e-06
```

The R-squared has improved but the p-values hardly show any significance. Perhaps this is due to overfitting. We have to meet somewhere in the middle. Let's iterate using the step method

```
# Res 7
bestFit <- step(totalFit,direction="both",trace=FALSE)
summary(bestFit)
```

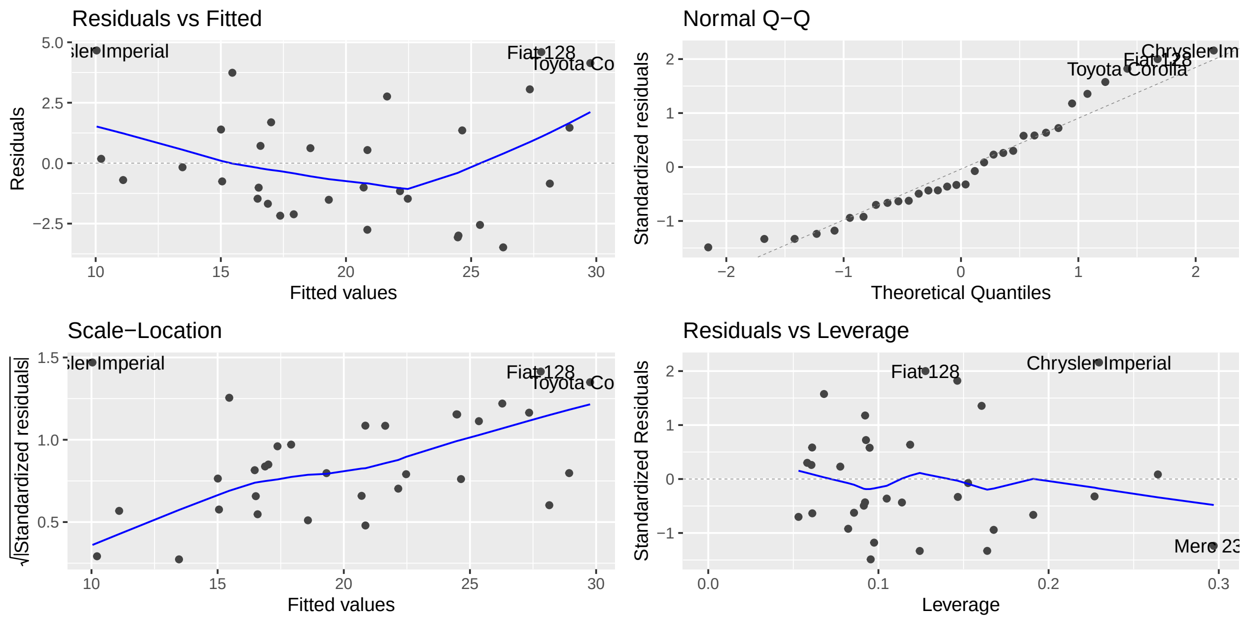
```
##
## Call:
## lm(formula = mpg ~ wt + qsec + am, data = mtcarsFactors)
##
## Residuals:
##     Min      1Q  Median      3Q     Max
## -3.4811 -1.5555 -0.7257  1.4110  4.6610
##
## Coefficients:
##             Estimate Std. Error t value Pr(>|t|)
## (Intercept)   9.6178     6.9596   1.382 0.177915
## wt           -3.9165     0.7112  -5.507 6.95e-06 ***
## qsec          1.2259     0.2887   4.247 0.000216 ***
## ammanual      2.9358     1.4109   2.081 0.046716 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.459 on 28 degrees of freedom
## Multiple R-squared:  0.8497, Adjusted R-squared:  0.8336
## F-statistic: 52.75 on 3 and 28 DF,  p-value: 1.21e-11
```

Model examination

The resulting best model `mpg ~ wt + qsec + am` is actually dependent on the transmission (am), but also weight (wt) and 1/4 mile time (qsec). All have significant p-values The R-squared is pretty good to (0.85)

Now let's look (amongst others) at the Residuals vs Fitted

```
# Figure 3
autoplot(bestFit)
```



The ‘Normal Q-Q’ plot looks ok, but the ‘Residuals vs Fitted’ and ‘Scale-Location’ both show worrisome trends.

Conclusion

The question “Is an automatic or manual transmission better for MPG” can be answered because all models (#Res5, #Res6 and #Res7) show that, holding all other paramters constant, manual transmission will increase your MPG.

The question “Quantify the MPG difference between automatic and manual transmissions” is quite tricky.

Based on the ‘bestFit’ (#Res7) model `mpg ~ wt + qsec + am` we could conclude that (with a $p < 0.05$ confidence) cars with manual transmission have 2.9358 (say 3) more miles per gallon than automatic transmissions. The model seems clean with a $p < 0.05$ and R squared of 0.85

The residuals vs fitted chart however warns us that there is something missing in our model. The real problem is that we only have 32 observations to train on (#Res1) and those observations hardly have overlap on the parameters ‘wt’ and ‘qsec’ (amongst others) if we look at the diagonal in the matrix chart (#Figure2)

Although the conclusion that mpg has better performance on manual transmissions appears to be alright, we cannot conclude that this model will fit with more observations.