

## h-inf-circle-after-trim

December 22, 2023

```
[41]: import rosbag
import numpy as np
import matplotlib.pyplot as plt
from scipy.signal import butter, filtfilt

[42]: bag = rosbag.Bag('/home/miguel/catkin_ws/src/crazyflie/crazyflie_controller/src/
↳data/h_inf_bag_after_circle_trim.bag')

position_optitrack = []
desired_position = []
vel_optitrack = []
desired_vel = []
control_input = []

for topic, msg, t in bag.read_messages(topics=['position_Optitrack',
↳'vel_Optitrack', 'desired_position', 'desired_vel', 'control_input']):

    if topic == 'position_Optitrack':
        position_optitrack.append((msg.x, msg.y, msg.z))

    if topic == 'vel_Optitrack':
        vel_optitrack.append((msg.x, msg.y, msg.z))

    if topic == 'desired_position':
        desired_position.append((msg.x, msg.y, msg.z))

    if topic == 'desired_vel':
        desired_vel.append((msg.x, msg.y, msg.z))

    if topic == 'control_input':
        control_input.append((msg.x, msg.y, msg.z))
bag.close()

position_optitrack = np.array(position_optitrack)
vel_optitrack = np.array(vel_optitrack)
desired_position = np.array(desired_position)
desired_vel = np.array(desired_vel)
```

```
control_input = np.array(control_input)
```

```
[43]: time = []
      initial_time = 0
      Ts = 1/30

      for i in range(len(position_optitrack)):
          time.append(initial_time)
          initial_time+=Ts
```

## 1 X accel vs angle

```
[44]: ##### Finding the Acceleration #####
      # Filter parameters
      N = 5 # Filter order
      Wn = 0.01 # Cutoff frequency (as a fraction of the Nyquist frequency)
      b, a = butter(N, Wn, 'low')

      # Filter the velocity
      vel_optitrack_ = np.array(vel_optitrack)[: , 0]
      filtered_velocity = filtfilt(b, a, vel_optitrack_.squeeze())

      # Numerical differentiation to find acceleration
      dt = np.diff(time) # Time intervals
      acceleration = np.diff(filtered_velocity) / dt # Numerical derivative

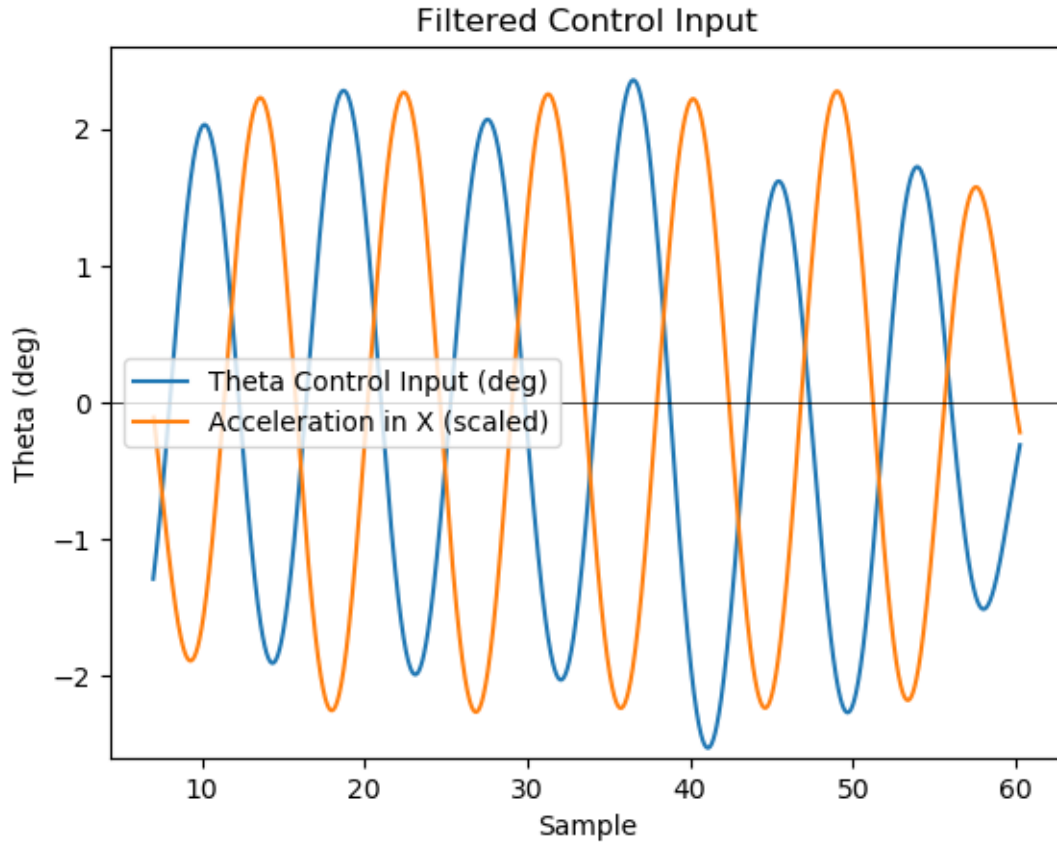
      ##### Filtering the Control Input #####
      control_input_ = np.array(control_input)[: , 0]
      # Apply the filter
      filtered_control_input = filtfilt(b, a, control_input_.squeeze())

      # Convert to degrees
      filtered_control_input_deg = np.rad2deg(filtered_control_input)

      # Plotting
      max_t = 18
      min_t = 7
      plt.plot(time[min_t*30:-max_t*30], filtered_control_input_deg[min_t*30:
          ↪-max_t*30], label='Theta Control Input (deg)')
      plt.plot(time[(1+min_t*30):-max_t*30], [x*5 for x in acceleration[min_t*30:
          ↪-max_t*30]], label='Acceleration in X (scaled)')

      plt.axhline(y=0, color='k', linewidth=0.5)
      plt.ylim(-2.6, 2.6)
      plt.xlabel('Sample')
```

```
plt.ylabel('Theta (deg)')
plt.title('Filtered Control Input')
plt.legend()
plt.show()
```



```
[45]: np.mean(filtered_control_input_deg[min_t*30:-max_t*30])
```

```
[45]: -0.040919920039939696
```

## 2 Y accel vs angle

```
[46]: ##### Finding the Acceleration #####
# Filter parameters
N = 5 # Filter order
Wn = 0.01 # Cutoff frequency (as a fraction of the Nyquist frequency)
b, a = butter(N, Wn, 'low')

# Filter the velocity
vel_optitrack_ = np.array(vel_optitrack)[: , 1]
```

```

filtered_velocity = filtfilt(b, a, vel_optitrack_.squeeze())

# Numerical differentiation to find acceleration
dt = np.diff(time) # Time intervals
acceleration = np.diff(filtered_velocity) / dt # Numerical derivative

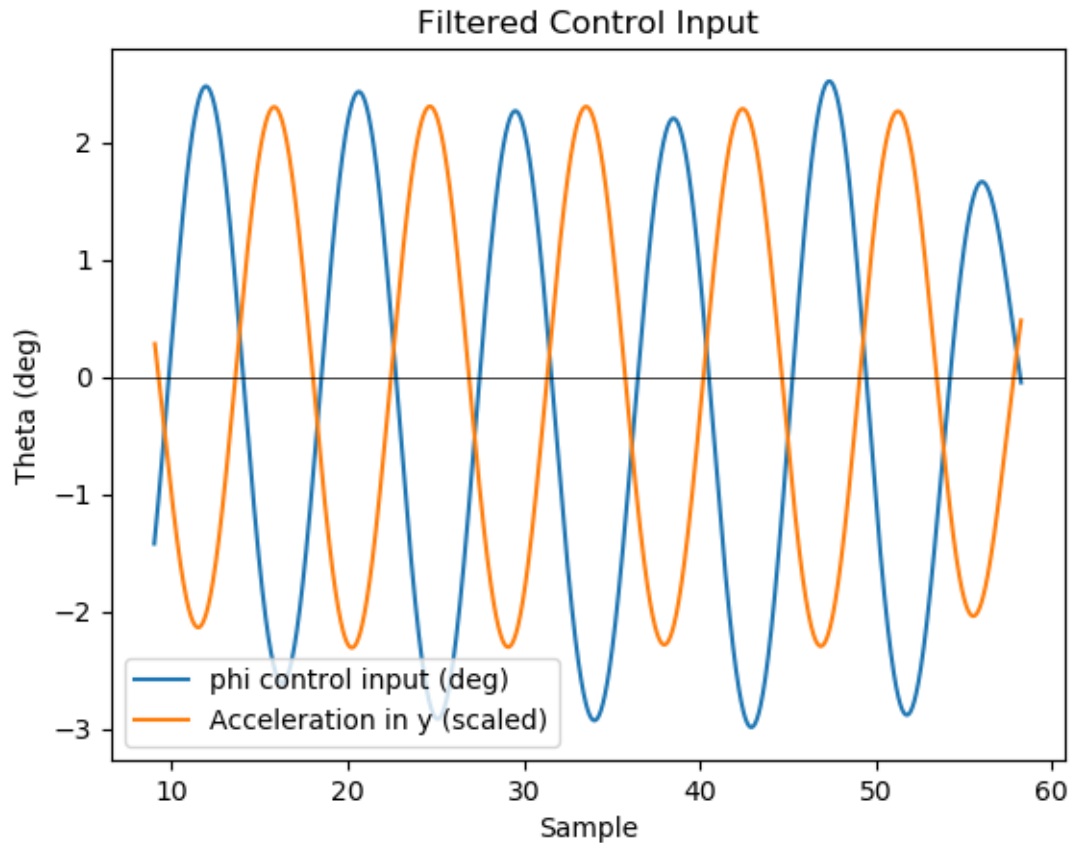
##### Filtering the Control Input #####
control_input_ = np.array(control_input)[: , 1]
# Apply the filter
filtered_control_input = filtfilt(b, a, control_input_.squeeze())

# Convert to degrees
filtered_control_input_deg = np.rad2deg(filtered_control_input)

# Plotting
max_t = 20
min_t = 9

plt.plot(time[min_t*30:-max_t*30], filtered_control_input_deg[min_t*30:
    ↪-max_t*30], label='phi control input (deg)')
plt.plot(time[(1+min_t*30):-max_t*30], [x*5 for x in acceleration[min_t*30:
    ↪-max_t*30]], label='Acceleration in y (scaled)')
plt.axhline(y=0, color='k', linewidth=0.5)
plt.xlabel('Sample')
plt.ylabel('Theta (deg)')
plt.title('Filtered Control Input')
plt.legend()
plt.show()

```

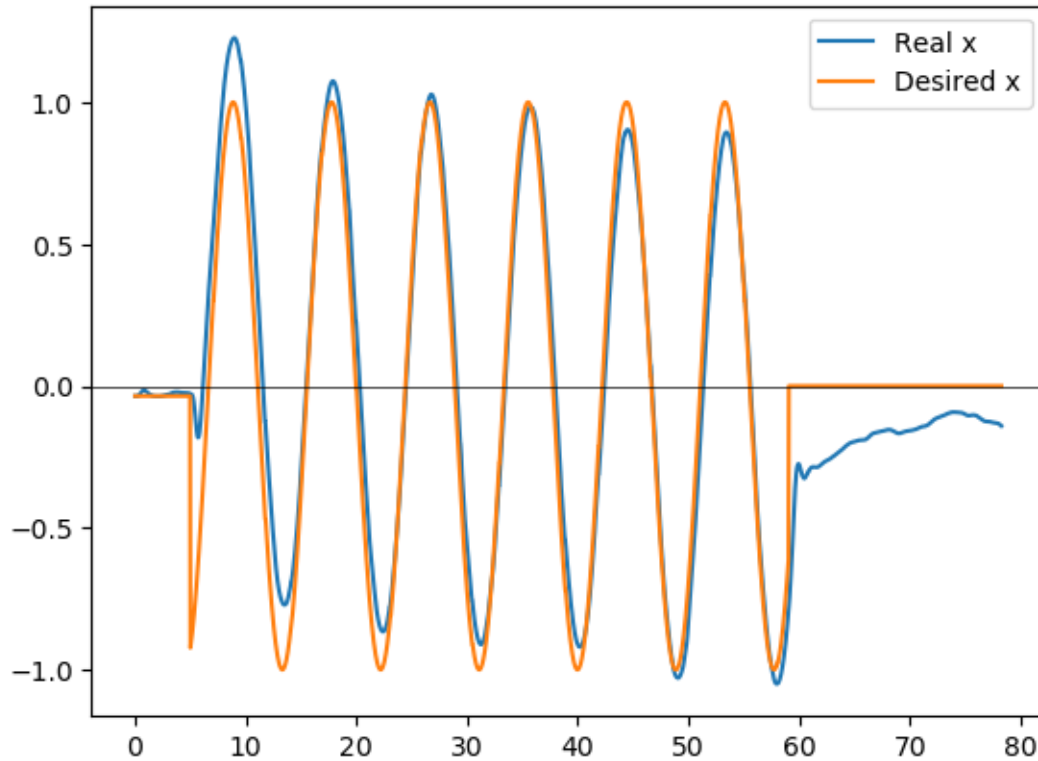


```
[47]: np.mean(filtered_control_input_deg[10*30:-10*30])
```

```
[47]: -0.14622677548351967
```

### 3 X

```
[48]: plt.plot(time, [x[0] for x in position_optitrack], label='Real x')
plt.plot(time, [x[0] for x in desired_position], label='Desired x')
plt.axhline(y=0, color='k', linewidth=0.5)
plt.legend()
plt.show()
```



### 3.0.1 X RMSE - Taking off the positioning task

```
[49]: x_square_error = (desired_position[6*30:-20*30, 1] - position_optitrack[6*30:
    ↪-20*30, 1])**2
x_mse = np.sqrt(np.mean(x_square_error))
x_mse
```

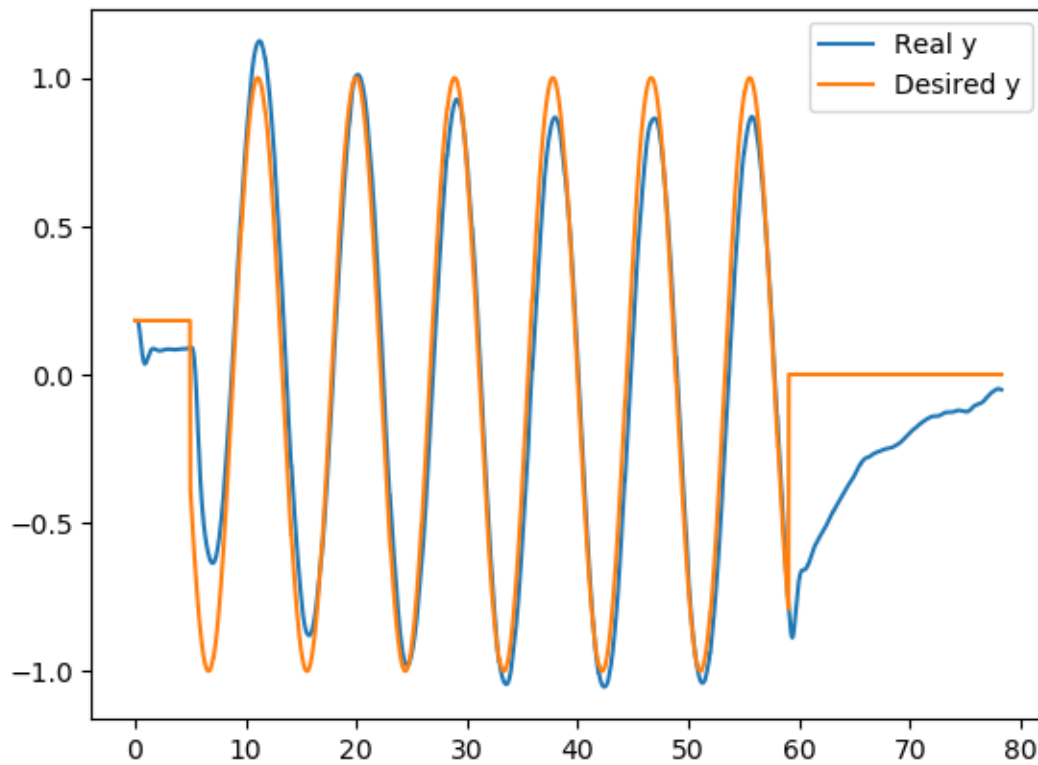
```
[49]: 0.15145306966952635
```

## 4 Y

```
[50]: # Plotting example
plt.plot(time, [x[1] for x in position_optitrack], label='Real y')
plt.plot(time, [x[1] for x in desired_position], label='Desired y')

# Adding a horizontal line
#zplt.axhline(y=10, color='r', linewidth=0.5)
# plt.scatter(range(len(position_gaussian_error)), [x[2] for x in
    ↪position_gaussian_error], label='position_gaussian_error z', s=0.7)
# Add more plots as needed
# plt.ylim(0.92, 1.02)
```

```
plt.legend()
plt.show()
```



#### 4.0.1 Y MSE - Taking off the positioning task

```
[51]: y_square_error = (desired_position[10*30:-20*30, 1] - position_optitrack[10*30:
    ↪-20*30, 1])**2
y_mse = np.sqrt(np.mean(y_square_error))
y_mse
```

```
[51]: 0.139761953289191
```

## 5 Control Effort

### 5.1 Theta

```
[52]: def control_effort(u):
    effort = 0
    for i in range(len(u) - 1):
        effort += u[i+1]-u[i]
```

```
    return effort

control_effort(np.array(control_input)[: , 0])
```

```
[52]: -0.031954224984525395
```

## 5.2 phi

```
[53]: control_effort(np.array(control_input)[: , 1])
```

```
[53]: 0.02612478006957868
```

## 5.3 Thrust

```
[54]: control_effort(np.array(control_input)[: , 2])
```

```
[54]: 0.03719884097512616
```

# 6 Conclusion

The accuracy of the drone has significantly improved just by adjusting the trim angles. Given the drone's small size, the markers have a substantial impact on its stability.

Regarding the error metrics, the H infinity control demonstrated excellent performance, exhibiting the smallest error among all the controllers during trajectory tracking. However, it should be noted that this controller takes a considerable amount of time to reach the desired position.

It's important to note that the H infinity controller was unable to effectively control the drone's z-axis positioning. Consequently, a Proportional-Derivative (PD) controller was implemented specifically to manage this aspect.