

1. Title: First-order theorem proving

2. Sources:

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(c) Date: 17th April 2013

3. Past Usage:

(a) Machine learning for first-order theorem proving: learning to select a good heuristic James P Bridge, Sean B Holden and Lawrence C Paulson Submitted for publication in the Journal of Automated Reasoning, Springer 2012/13.

Please include a citation if you use this data.

(b) We wish to predict which of a set of five heuristics will provide the fastest proof, given features derived from a theorem to be proved. A sixth possible prediction is to decline to attempt a proof, should the theorem be assessed as too difficult.

(c) In prediction terms this is a challenging problem. However we can do better than any individual heuristic and obtain performance comparable to that of a hand-crafted selection mechanism employing around 75 addition heuristics. The ability to decline a proof is also beneficial.

4. Relevant Information Paragraph:

Files:

Expanding the tarball ml-prove.tar produces a directory ml-prove/ containing the files:

| | |
|-----------------------------|--|
| all-data-raw.csv | - raw data used to derive training, validation and test data. |
| all-data-raw-statistics.txt | - min, max, mean and standard deviation for raw data. (Tabulated below.) |
| train.csv | - actual training, validation and test |
| validation.csv | sets used. |
| test.csv | |
| all-data-statistics.txt | - min, max and correlation data for combined actual data. (Tabulated below.) |

Raw data:

Columns 1 to 14 are the static features and columns 15 to 53 are

the dynamic features. (See the paper for a description of static and dynamic features.) The final five columns denote the time in seconds taken by each of the five heuristics to prove the relevant theorem. There was a time limit of 100 seconds. An entry of -100 denotes failure to obtain a proof within the time limit. The first half of this data corresponds to the training data used. The second half was permuted and split to obtain the validation and test sets.

Training, validation and test data:

These are the sets used in the reported experiments. Two redundant features (static feature 5 and dynamic feature 21 in the raw data) were removed. The features in the training set are normalised to zero mean and unit variance. Validation/test data was normalized using the coefficients computed for the training set. Labels are in the final six columns. The first five of those correspond to the five heuristics (H1 to H5) and contain +1 if the corresponding heuristic found a proof and was the fastest to do so, and -1 otherwise. The final column contains +1 where no heuristic finds a proof within the time limit and -1 otherwise (H0 in the paper).

5. Number of Instances:

6118 in the raw data.

The training, validation and test sets have 3059, 1529 and 1530 respectively.

6. Number of Attributes:

There are 13 static and 38 dynamic features for each instance. (See the paper for details regarding static/dynamic features. The raw data has two more features, which are redundant.) Columns 1 to 13 contain static features and columns 14 to 51 dynamic features.

7. Description of attributes:

The full names for each attribute are provided in the paper, tables 2 and 3.

Raw data: all attributes are numeric. Attributes 5, 9, 11, 13 and 35 are integer-valued. All other attributes are continuous.

Training, validation and test data: all data are numeric and continuous on account of being normalized.

8. Missing Attribute Values:

There are no missing values.

9. Class Distribution: number of positive instances in the sets for each heuristic (H1 to H5) and the "decline" option H0.

| | H1 | H2 | H3 | H4 | H5 | H0 |
|-----------------|-----|-----|-----|-----|-----|------|
| Training set: | 556 | 229 | 373 | 303 | 312 | 1286 |
| Validation set: | 260 | 133 | 187 | 146 | 159 | 644 |
| Test set: | 273 | 124 | 188 | 168 | 153 | 624 |

10. Attribute statistics:

Statistics for the raw data:

We do not include correlations as this data includes time measurements rather than actual classes.

| Attribute | Min | Max | Mean | SD |
|-----------|------------|---------|-----------|-----------------|
| 1 | 0 | 1 | 0.36785 | 0.31389 |
| 2 | 0.0078125 | 1 | 0.83086 | 0.21303 |
| 3 | 0 | 1 | 0.26426 | 0.26827 |
| 4 | 0 | 1 | 0.30074 | 0.26399 |
| 5 | 0 | 0 | 0 | 0 |
| 6 | 0.00038153 | 1 | 0.35776 | 0.26964 |
| 7 | 0 | 0.98214 | 0.10619 | 0.1193 |
| 8 | 0 | 0.9966 | 0.53605 | 0.30238 |
| 9 | 1 | 244 | 7.0814 | 7.3035 |
| 10 | 1 | 39.07 | 2.64 | 2.2741 |
| 11 | 1 | 86 | 7.7257 | 7.3965 |
| 12 | 1 | 11 | 2.7553 | 0.93885 |
| 13 | 12 | 16240 | 159.76 | 318.14 |
| 14 | 4.4643 | 990.14 | 26.838 | 38.297 |
| 15 | 0.14141 | 1 | 0.8451 | 0.20275 |
| 16 | 0.048106 | 1477.7 | 14.238 | 42.392 |
| 17 | 0.0031504 | 0.97917 | | 0.32239 0.17827 |
| 18 | 0.016667 | 7010 | 62.371 | 383.47 |
| 19 | 0.0040984 | 3 | 0.79035 | 0.3646 |
| 20 | 0.044484 | 3.7954 | 0.86357 | 0.30873 |
| 21 | 0.03125 | 5 | 1.0941 | 0.32019 |
| 22 | 0.21483 | 27.052 | 1.3219 | 0.58307 |
| 23 | 0.076923 | 7.5 | 0.98681 | 0.45421 |
| 24 | 0.29257 | 2.7525 | 1.0079 | 0.20582 |
| 25 | 0.23077 | 8.3333 | 1.3338 | 0.70145 |
| 26 | 0.54418 | 4.8414 | 1.1857 | 0.38731 |
| 27 | 0.0017567 | 13.647 | 0.82934 | 0.80024 |
| 28 | 0.01868 | 7.2062 | 0.86554 | 0.47486 |
| 29 | 0.051613 | 449.2 | 2.8181 | 14.844 |
| 30 | 0.22842 | 78.779 | 1.7701 | 2.4387 |
| 31 | 0 | 0.72727 | 0.04486 | 0.10227 |
| 32 | 0 | 0.85859 | 0.11004 | 0.16052 |
| 33 | 0.14141 | 1 | 0.8451 | 0.20275 |
| 34 | 0 | 7.7273 | 0.012384 | 0.14083 |
| 35 | 0 | 0 | 0 | 0 |
| 36 | 0 | 0.40404 | 0.0053444 | 0.0225 |
| 37 | 0 | 0.52525 | 0.02126 | 0.050914 |
| 38 | 0 | 5.404 | 0.029045 | 0.1183 |
| 39 | 0 | 142.7 | 4.0076 | 9.5463 |
| 40 | 0 | 176.01 | 7.0783 | 10.955 |
| 41 | 0 | 142.6 | 3.2732 | 8.7734 |
| 42 | 0 | 2.7778 | 0.024949 | 0.090029 |
| 43 | 0 | 142.7 | 3.9567 | 9.5333 |
| 44 | 0 | 1.8182 | 0.0098467 | 0.060589 |
| 45 | 0 | 7.8889 | 0.01567 | 0.14505 |
| 46 | 0 | 1 | 0.19265 | 0.33357 |
| 47 | 0 | 1 | 0.69969 | 0.29722 |
| 48 | 0 | 1 | 0.13459 | 0.25073 |
| 49 | 0 | 1 | 0.18258 | 0.32845 |
| 50 | 0 | 1 | 0.1277 | 0.26172 |
| 51 | 0 | 1 | 0.27041 | 0.32167 |
| 52 | 0 | 1 | 0.046002 | 0.10017 |
| 53 | 0 | 1 | 0.68359 | 0.32092 |

Statistics for the combined training, validation and test data:

We do not include mean and standard deviation as the data are normalized.

| attribute Attribute H5 | Correlation with predicted | | | | | |
|------------------------------|----------------------------|------------|------------|------------|-----------|---------|
| | Min H0 (decline) | Max | H1 | H2 | H3 | H4 |
| 1 | -1.1052 | 2.0094 | 0.002146 | 0.018808 | 0.053781 | - |
| 0.05868 | -0.055589 | 0.022243 | | | | |
| 2 | -3.7356 | 0.83152 | -0.0096346 | -0.0083581 | -0.10085 | |
| 0.032679 | -0.03394 | 0.079926 | | | | |
| 3 | -0.98411 | 2.7381 | 0.064511 | 0.0044296 | 0.10732 | - |
| 0.014341 | -0.061767 | -0.077094 | | | | |
| 4 | -1.0652 | 2.6448 | 0.0035693 | 0.00027939 | 0.041497 | - |
| 0.058916 | -0.047575 | 0.034685 | | | | |
| 5 | -1.2401 | 2.3662 | 0.012026 | 0.012048 | 0.15051 | - |
| 0.073614 | -0.069968 | -0.028027 | | | | |
| 6 | -0.88058 | 7.1945 | 0.012745 | 0.07273 | 0.049764 | - |
| 0.0097244 | -0.046281 | -0.048485 | | | | |
| 7 | -1.7638 | 1.4393 | -0.015752 | -0.039438 | -0.15385 | 0.06948 |
| | 0.080651 | 0.044121 | | | | |
| 8 | -0.82637 | 32.27 | 0.0638 | -0.034726 | -0.016868 | |
| 0.012842 | 0.046311 | -0.055503 | | | | |
| 9 | -0.70995 | 15.495 | 0.078303 | 0.0083392 | -0.034436 | |
| 0.002618 | 0.033225 | -0.064424 | | | | |
| 10 | -0.91358 | 10.654 | -0.13423 | -0.031277 | -0.1219 | - |
| 0.021194 | -0.096237 | 0.27425 | | | | |
| 11 | -1.8597 | 8.7417 | -0.074573 | 0.02795 | -0.027282 | - |
| 0.072398 | -0.13654 | 0.18864 | | | | |
| 12 | -0.39657 | 42.424 | -0.065158 | -0.018158 | -0.099504 | - |
| 0.026572 | -0.073284 | 0.1878 | | | | |
| 13 | -0.54978 | 23.342 | 0.041242 | 0.014417 | -0.043775 | - |
| 0.020486 | -0.032732 | 0.021781 | | | | |
| 14 | -3.4736 | 0.75143 | -0.0082202 | -0.067825 | -0.091643 | |
| 0.069091 | 0.078551 | 0.01405 | | | | |
| 15 | -0.31199 | 31.367 | 0.026761 | 0.0072152 | 0.015031 | - |
| 0.015863 | -0.0097697 | -0.019017 | | | | |
| 16 | -1.7758 | 3.5936 | 0.10717 | -0.032362 | -0.038655 | - |
| 0.058026 | 0.040632 | -0.029209 | | | | |
| 17 | -0.16059 | 18.089 | -0.0428 | 0.016927 | 0.040962 | - |
| 0.039735 | -0.043521 | 0.047678 | | | | |
| 18 | -2.2338 | 6.2511 | -0.070495 | 0.026704 | 0.018875 | - |
| 0.13101 | -0.12438 | 0.18383 | | | | |
| 19 | -2.7772 | 9.7705 | -0.045209 | -0.0076608 | 0.023149 | - |
| 0.10657 | -0.12364 | 0.16485 | | | | |
| 20 | -3.3938 | 12.535 | -0.090452 | 0.032468 | -0.081587 | - |
| 0.02245 | 0.00090069 | 0.11971 | | | | |
| 21 | -1.6224 | 37.494 | 0.00055005 | -0.013199 | -0.021748 | - |
| 0.035844 | -0.0087721 | 0.04853 | | | | |
| 22 | -2.0133 | 14.345 | 0.021364 | 0.084079 | 0.10798 | - |
| 0.10595 | -0.084204 | -0.018032 | | | | |
| 23 | -3.4243 | 8.4063 | -0.026558 | 0.061894 | 0.060129 | - |
| 0.073706 | -0.008226 | -0.0032276 | | | | |
| 24 | -1.5872 | 10.102 | -0.057337 | 0.09175 | 0.091461 | - |
| 0.059409 | -0.068288 | 0.011591 | | | | |
| 25 | -1.6551 | 9.4181 | -0.062921 | 0.060763 | 0.026404 | - |
| 0.063904 | -0.079265 | 0.085613 | | | | |

| | | | | | | |
|------------|------------|-----------|------------|-----------|------------|---|
| 26 | -0.9819 | 15.033 | -0.034107 | 0.051906 | 0.047598 | - |
| 0.08317 | -0.076884 | 0.064343 | | | | |
| 27 | -1.751 | 12.878 | -0.042957 | 0.029734 | 0.059429 | - |
| 0.096057 | -0.084145 | 0.087833 | | | | |
| 28 | -0.1774 | 27.844 | -0.03759 | 0.012154 | -0.0078761 | - |
| 0.031427 | -0.032431 | 0.066818 | | | | |
| 29 | -0.5859 | 28.717 | -0.044935 | 0.0032447 | -0.011599 | - |
| 0.046033 | -0.042716 | 0.095105 | | | | |
| 30 | -0.44033 | 6.6755 | -0.032097 | 0.058129 | 0.029079 | - |
| 0.06687 | -0.077477 | 0.062085 | | | | |
| 31 | -0.67335 | 4.6948 | 0.030832 | 0.048634 | 0.097226 | - |
| 0.044665 | -0.049855 | -0.057301 | | | | |
| 32 | -3.4736 | 0.75143 | -0.0082202 | -0.067825 | -0.091643 | |
| 0.069091 | 0.078551 | 0.01405 | | | | |
| 33 | -0.092482 | 54.739 | -0.013186 | -0.010443 | -0.018006 | - |
| 0.010453 | -0.0084866 | 0.039507 | | | | |
| 34 | -0.22559 | 16.234 | 0.065962 | 0.071334 | 0.027832 | - |
| 0.0069337 | -0.020891 | -0.091715 | | | | |
| 35 | -0.42105 | 9.9934 | 0.044079 | 0.13205 | 0.058075 | |
| 0.00014594 | -0.014078 | -0.13663 | | | | |
| 36 | -0.35232 | 68.461 | 0.041986 | 0.06243 | 0.044788 | |
| 0.00073451 | -0.014495 | -0.088107 | | | | |
| 37 | -0.41853 | 14.542 | -0.059786 | 0.046906 | 0.083345 | - |
| 0.067165 | -0.075797 | 0.052818 | | | | |
| 38 | -0.65677 | 15.754 | -0.084272 | 0.04263 | 0.09013 | - |
| 0.083737 | -0.08659 | 0.086391 | | | | |
| 39 | -0.37137 | 15.949 | -0.055556 | 0.042761 | 0.075241 | - |
| 0.059883 | -0.069622 | 0.048956 | | | | |
| 40 | -0.26431 | 29.35 | 0.041966 | 0.055452 | 0.029756 | - |
| 0.014736 | -0.014861 | -0.064608 | | | | |
| 41 | -0.41369 | 14.567 | -0.059774 | 0.046369 | 0.083293 | - |
| 0.066937 | -0.075561 | 0.052853 | | | | |
| 42 | -0.16374 | 30.596 | -0.029609 | 0.009295 | -0.008666 | - |
| 0.025563 | -0.015875 | 0.048978 | | | | |
| 43 | -0.11229 | 54.273 | -0.014475 | -0.012921 | -0.019959 | - |
| 0.011158 | -0.0094043 | 0.044156 | | | | |
| 44 | -0.57834 | 2.4111 | -0.023614 | 0.055402 | 0.04686 | - |
| 0.02783 | -0.090859 | 0.029562 | | | | |
| 45 | -2.4037 | 0.99018 | 0.008524 | -0.022984 | -0.0071944 | |
| 0.054038 | -0.011789 | -0.014992 | | | | |
| 46 | -0.54541 | 3.4576 | 0.073899 | -0.025784 | 0.068701 | |
| 0.0084746 | -0.039061 | -0.070023 | | | | |
| 47 | -0.55678 | 2.4793 | -0.02353 | 0.056086 | 0.046787 | - |
| 0.035891 | -0.091956 | 0.034767 | | | | |
| 48 | -0.4899 | 3.2982 | -0.030158 | 0.068629 | 0.062895 | - |
| 0.04733 | -0.085002 | 0.025046 | | | | |
| 49 | -0.78459 | 2.2579 | -0.032389 | 0.090761 | 0.086016 | - |
| 0.05451 | -0.091454 | 0.0076241 | | | | |
| 50 | -0.46486 | 9.5615 | 0.060724 | 0.0042777 | -0.039375 | |
| 0.071214 | 0.009376 | -0.072531 | | | | |
| 51 | -2.1318 | 0.93219 | 0.013509 | -0.092307 | -0.073924 | |
| 0.032407 | 0.088739 | 0.014998 | | | | |