Equations

Schrödinger:

$$i\hbar\frac{\partial|\psi(t)\rangle}{\partial t} = H|\psi t\rangle \qquad \mathcal{L} = i\psi^*\dot{\psi} - \frac{1}{2m}\vec{\nabla}\psi^*\cdot\vec{\nabla}\psi$$

Klein-Gordon (Real Scalar Field):

$$(\partial\cdot\partial+m^2)\phi=0 \hspace{1cm} \mathcal{L}=\frac{1}{2}\Big[\partial_\mu\phi\partial^\mu\phi-m^2\phi^2\Big]=\frac{1}{2}\Big[\dot{\phi}^2-\left(\vec{\nabla}\phi\right)^2-m^2\phi^2\Big]$$

Dirac (Complex Scalar Field):

$$(i\partial \!\!\!/ - m)\varphi = 0$$
 $\overline{\varphi}(i\partial \!\!\!/ - m) = 0$ $\mathcal{L} = \partial_{\mu}\varphi \partial^{\mu}\varphi^* - m^2\varphi\varphi^*$

γ-Matrices

$$\begin{split} \{\gamma^{\mu},\gamma^{\nu}\} &= 2g^{\mu\nu} \quad \gamma_5 = +i\gamma^0\gamma^1\gamma^2\gamma^3 = -i\gamma_0\gamma_1\gamma_2\gamma_3 = -\frac{i}{4!}\epsilon^{\alpha\beta\gamma\delta}\gamma^{\alpha}\gamma^{\beta}\gamma^{\gamma}\gamma^{\delta} \\ \sigma^{\mu\nu} &= \frac{i}{2}[\gamma^{\mu},\gamma^{\nu}] \implies [\gamma^{\mu},\gamma^{\nu}] = -2i\sigma^{\mu\nu} \qquad \{\gamma_5,\gamma^{\mu}\} = 0\gamma_5\gamma_5 = +1 \end{split}$$

$$\begin{split} \gamma_L &= \frac{1-\gamma_5}{2} \qquad \gamma_R = \frac{1+\gamma_5}{2} \qquad \gamma_{L,R}^2 = \gamma_{L,R} \qquad \gamma_{L,R}\gamma_{R,L} = 0 \\ \gamma^\mu \gamma_{L,R} &= \gamma_{R,L} \gamma^\mu \qquad \gamma_5 \gamma_L = \gamma_L \gamma_5 = -\gamma_L \qquad \gamma_5 \gamma_R = \gamma_R \gamma_5 = \gamma_R \end{split}$$

$$\begin{split} \operatorname{Tr}[1] &= 4 & \operatorname{Tr}[\underline{\gamma}^{\mu}\gamma^{\nu} \dots \gamma^{\rho}] &= 0 & \operatorname{Tr}[\gamma^{\mu}\gamma^{\nu}] &= 4g^{\mu\nu} \\ \operatorname{Odd} \operatorname{Number} & \\ \operatorname{Tr}[\gamma_{5}] &= 0 & \operatorname{Tr}[\gamma_{5} \underline{\gamma}^{\mu}\gamma^{\nu} \dots \gamma^{\rho}] &= 0 & \operatorname{Tr}[\gamma_{5} \gamma^{\mu}\gamma^{\nu}] &= 0 \\ \operatorname{Odd} \operatorname{Number} & \\ \operatorname{Tr}[\gamma^{\mu}\gamma^{\nu}\gamma^{\rho}\gamma^{\sigma}] &= 4(g^{\mu\nu}g^{\rho\sigma} - g^{\mu\rho}g^{\nu\sigma} + g^{\mu\sigma}g^{\nu\rho}) & \operatorname{Tr}[\gamma_{5}\gamma^{\mu}\gamma^{\nu}\gamma^{\rho}\gamma^{\sigma}] &= -4i\epsilon^{\mu\nu\rho\sigma} \end{split}$$

Spinors

$$\overline{u}^{r}(p)u^{s}(p) = +2m\delta^{rs} \quad \overline{u}^{r}(p)v^{s}(p) = 0 \quad u^{r\dagger}(p)u^{s}(p) = 2E\delta^{rs} \quad \sum_{s=1,2} u^{s}(p)\overline{u}^{s}(p) = \not p + m$$

$$\overline{v}^{r}(p)v^{s}(p) = -2m\delta^{rs} \quad \overline{v}^{r}(p)u^{s}(p) = 0 \quad u^{r\dagger}(p)u^{s}(p) = 2E\delta^{rs} \quad \sum_{s=1,2} v^{s}(p)\overline{v}^{s}(p) = \not p - m$$

$$\sum_{s=1,2} \varepsilon_{\mu}(q,\lambda)\varepsilon_{\nu}^{*}(q,\lambda) = -g_{\mu\nu} + \frac{q_{\mu}q_{\nu}}{M^{2}}$$

Levi-Civita Symbol

$$\epsilon^{\mu\nu\rho\sigma} = \begin{cases} +1 & \text{If } (\mu\nu\rho\sigma) \text{ is an even permutation of (0123)} \\ -1 & \text{If } (\mu\nu\rho\sigma) \text{ is an odd permutation of (0123)} \\ 0 & \text{Otherwise} \end{cases}$$

$$\begin{split} \epsilon_{\alpha\beta_{1}\gamma_{1}\delta_{1}}\epsilon^{\alpha\beta_{2}\gamma_{2}\delta_{2}} &= +g_{\beta_{1}}^{\beta_{2}}g_{\gamma_{1}}^{\delta_{2}}g_{\delta_{1}}^{\gamma_{2}} - g_{\beta_{1}}^{\beta_{2}}g_{\gamma_{1}}^{\gamma_{2}}g_{\delta_{1}}^{\delta_{2}} + g_{\beta_{1}}^{\gamma_{2}}g_{\gamma_{1}}^{\beta_{2}}g_{\delta_{1}}^{\delta_{2}} - g_{\beta_{1}}^{\gamma_{2}}g_{\delta_{1}}^{\gamma_{2}}g_{\delta_{1}}^{\beta_{2}} \\ &\quad + g_{\beta_{1}}^{\delta_{2}}g_{\gamma_{1}}^{\gamma_{2}}g_{\delta_{1}}^{\beta_{2}} - g_{\beta_{1}}^{\delta_{2}}g_{\gamma_{1}}^{\gamma_{2}}g_{\delta_{1}}^{\delta_{2}} \\ &\quad + g_{\beta_{1}}^{\delta_{2}}g_{\gamma_{1}}^{\gamma_{2}}g_{\delta_{1}}^{\delta_{2}} - g_{\beta_{1}}^{\delta_{2}}g_{\gamma_{1}}^{\gamma_{2}}g_{\delta_{1}}^{\delta_{2}} \\ &\quad + g_{\beta_{1}}^{\delta_{2}}g_{\gamma_{1}}^{\gamma_{2}}g_{\gamma_{1}}^{\delta_{2}}g_{\gamma_{1}}^{\gamma_{2}}g_{\gamma_{1}}^{\delta_{2}}g_{\gamma_{1}}^{\delta_{2}}g_{\gamma_{2}}^{\delta_{2}}g_{\gamma_{2}}^{\delta_{2}}g_{\gamma_{1}}^{\delta_{2}}g_{\gamma_{2}}^{\delta_{2}}g_{\gamma_{2}}^{\delta_{2}}g_{\gamma_{2$$

Fermions

$$\begin{aligned} :&a(x)b(x'):=a(x)b(x')-b(x')a(x)\\ &\mathbf{T}[a(x)b(x')]=\theta(t-'t)a(x)b(x')-\theta(t'-t)b(x')a(x)\\ &\left\{b^{\dagger}(p,s),b(p',s')\right\}=\left\{d^{\dagger}(p,s),d(p',s')\right\}=\tilde{\delta}(p-p')\delta_{ss'}\\ &\psi(x)=\psi^{+}(x)+\psi^{-}(x)=\int\mathrm{d}\tilde{p}\sum_{s}\left[b(p,s)u(p,s)e^{-ip\cdot x}+d^{\dagger}(p,s)v(p,s)e^{+ip\cdot x}\right]\\ &\overline{\psi}(x)=\overline{\psi}^{+}(x)+\overline{\psi}^{-}(x)=\int\mathrm{d}\tilde{p}\sum_{s}\left[d(p,s)\overline{v}(p,s)e^{-ip\cdot x}+b^{\dagger}(p,s)\overline{u}(p,s)e^{+ip\cdot x}\right]\\ &\psi^{+}(b)\;\mathrm{destroys}\;\mathrm{e}^{-}&\psi^{-}(d^{\dagger})\;\mathrm{creates}\;\mathrm{e}^{+}&\overline{\psi}^{+}(d)\;\mathrm{destroy}\;\mathrm{e}^{+}&\overline{\psi}^{-}(b^{\dagger})\;\mathrm{creates}\;\mathrm{e}^{-}\\ \end{aligned}$$

Bosons

$$: a(x)b(x') := a(x)b(x') + b(x')a(x)$$

$$T[a(x)b(x')] = \theta(t - t')a(x)b(x') + \theta(t' - t)b(x')a(x)$$

$$[\phi(\vec{\mathbf{x}},t),\phi(\vec{\mathbf{y}},t)] = [\Pi(\vec{\mathbf{x}},t),\Pi(\vec{\mathbf{y}},t)] = 0 \qquad [\phi(\vec{\mathbf{x}},t),\Pi(\vec{\mathbf{y}},t)] = i\delta^{3}(\vec{\mathbf{x}} - \vec{\mathbf{y}})$$

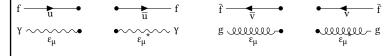
$$[a^{\dagger}(k,\lambda),a(k',\lambda')] = g^{\lambda\lambda'}\tilde{\delta}(k-k')$$

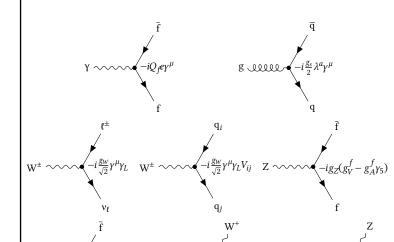
$$A_{\mu}(x) = A_{\mu}^{+}(x) + A_{\mu}^{-}(x) = \int d\tilde{k} \sum_{\lambda=0}^{3} \left[a(k,\lambda)\epsilon_{\mu}(k,\lambda)e^{-ik\cdot x} + a^{\dagger}(k,\lambda)\epsilon_{\mu}^{*}(k,\lambda)e^{+ik\cdot x}\right]$$

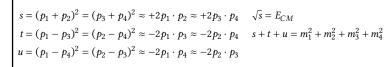
$$A^{+}(a) \text{ destroys } \gamma \qquad A^{-}(a^{\dagger}) \text{ creates } \gamma$$

Feynman Rules for i M

Goes in opposite way of arrows with the first one being adjoint, $\overline{\psi}=\psi^{\dagger}\gamma^0$:







$$\frac{G_F}{\sqrt{2}} = \frac{g_W^2}{8M_W^2} = \frac{g_W^2}{8M_Z^2 \cos^2(\theta_W)} = \frac{1}{2v^2} \qquad g_W = g_Z \cos \theta_W = \frac{e}{\sin \theta_W}$$

$$g_V^f = \frac{1}{2}T_f^3 - Q_f \sin^2(\theta_W) \qquad g_A^f = \frac{1}{2}T_f^3 \qquad M_W = M_Z \cos \theta_W = \frac{1}{2}g_W v \qquad m_H = \sqrt{2\lambda}v$$