Equations

Schrödinger:

$$i\hbar\frac{\partial|\psi(t)\rangle}{\partial t} = H|\psi t\rangle \qquad \mathcal{L} = i\psi^*\dot{\psi} - \frac{1}{2m}\vec{\nabla}\psi^*\cdot\vec{\nabla}\psi$$

Klein-Gordon (Real Scalar Field):

$$(\partial\cdot\partial+m^2)\phi=0 \qquad \mathcal{L}=\frac{1}{2}\Big[\partial_\mu\phi\partial^\mu\phi-m^2\phi^2\Big]=\frac{1}{2}\Big[\dot{\phi}^2-\left(\vec{\mathbf{\nabla}}\phi\right)^2-m^2\phi^2\Big]$$

Dirac (Complex Scalar Field):

$$(i\partial \!\!\!/ - m)\varphi = 0$$
 $\overline{\varphi}(i\partial \!\!\!/ + m) = 0$ $\mathcal{L} = \partial_{\mu}\varphi\partial^{\mu}\varphi^* - m^2\varphi\varphi^*$

Pauli Matrices

$$\sigma^{\mu} = \begin{pmatrix} 1, \vec{\boldsymbol{\sigma}} \end{pmatrix} \qquad \overline{\sigma}^{\mu} = \begin{pmatrix} 1, -\vec{\boldsymbol{\sigma}} \end{pmatrix}$$

$$\sigma^{1} = \sigma_{x} = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} \qquad \sigma^{2} = \sigma_{y} = \begin{pmatrix} 0 & -i \\ i & 0 \end{pmatrix} \qquad \sigma^{3} = \sigma_{z} = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} \qquad \widetilde{\boldsymbol{\Sigma}} = \begin{pmatrix} \vec{\boldsymbol{\sigma}} & 0 \\ 0 & \vec{\boldsymbol{\sigma}} \end{pmatrix}$$

$$\left\{ \boldsymbol{\sigma}^{i}, \boldsymbol{\sigma}^{j} \right\} = 2\delta^{ij} \qquad \left[\boldsymbol{\sigma}^{i}, \boldsymbol{\sigma}^{j} \right] = 2i\epsilon^{ijk}\boldsymbol{\sigma}^{k} \qquad \sigma^{i}\boldsymbol{\sigma}^{j} = \delta^{ij} + i\epsilon^{ijk}\boldsymbol{\sigma}^{k} \qquad \sigma^{2}\boldsymbol{\sigma}^{i}\boldsymbol{\sigma}^{2} = -(\boldsymbol{\sigma}^{i})^{*}$$

$$\vec{\boldsymbol{\sigma}} \cdot \vec{\boldsymbol{p}} = \begin{pmatrix} p_{z} & p_{x} - ip_{y} \\ p_{x} + ip_{y} & -p_{z} \end{pmatrix} \qquad (\vec{\boldsymbol{\sigma}} \cdot \vec{\boldsymbol{p}})^{2} = |\vec{\boldsymbol{p}}|^{2} \qquad (p \cdot \boldsymbol{\sigma})(p \cdot \vec{\boldsymbol{\sigma}}) = p^{2}$$

$$p \cdot \overline{\boldsymbol{\sigma}} = \begin{pmatrix} p^{0} + p^{3} & p^{1} - ip^{2} \\ p^{1} + ip^{2} & p^{0} - p^{3} \end{pmatrix} \qquad p \cdot \boldsymbol{\sigma} = \begin{pmatrix} p^{0} - p^{3} & -(p^{1} - ip^{2}) \\ -(p^{1} + ip^{2}) & p^{0} + p^{3} \end{pmatrix}$$

$$\sqrt{p \cdot \boldsymbol{\sigma}} = \frac{E + m - \vec{\boldsymbol{\sigma}} \cdot \vec{\boldsymbol{p}}}{\sqrt{2(E + m)}} \qquad \sqrt{p \cdot \overline{\boldsymbol{\sigma}}} = \frac{E + m + \vec{\boldsymbol{\sigma}} \cdot \vec{\boldsymbol{p}}}{\sqrt{2(E + m)}}$$

Dirac γ-Matrices

$$\begin{split} \{\gamma^{\mu},\gamma^{\nu}\} &= 2g^{\mu\nu} \quad \gamma_{5} = +i\gamma^{0}\gamma^{1}\gamma^{2}\gamma^{3} = -i\gamma_{0}\gamma_{1}\gamma_{2}\gamma_{3} = -\frac{i}{4!}\epsilon^{\alpha\beta\gamma\delta}\gamma^{\alpha}\gamma^{\beta}\gamma^{\gamma}\gamma^{\delta} \\ \sigma^{\mu\nu} &= \frac{i}{2}[\gamma^{\mu},\gamma^{\nu}] \implies [\gamma^{\mu},\gamma^{\nu}] = -2i\sigma^{\mu\nu} \quad \{\gamma_{5},\gamma^{\mu}\} = 0 \quad \gamma^{0}(\gamma^{\mu})^{\dagger}\gamma^{0} = \gamma^{\mu} \\ \left(\gamma^{0}\right)^{\dagger} &= \gamma^{0} \quad \left(\gamma^{0}\right)^{2} = 1 \quad \left(\gamma^{k}\right)^{\dagger} = -\gamma^{k} \quad \left(\gamma^{k}\right)^{2} = -1 \quad \left(\gamma^{5}\right)^{\dagger} = \gamma^{5} \quad \left(\gamma^{5}\right)^{2} = 1 \\ \overline{\Gamma} &= \gamma^{0}\Gamma^{\dagger}\gamma^{0} \quad \overline{\gamma_{5}} = -\gamma_{5} \quad \overline{\gamma^{\mu}} = \gamma^{\mu} \quad \overline{\gamma^{\mu}\gamma_{5}} = \gamma^{\mu}\gamma_{5} \quad \overline{\sigma^{\mu\nu}} = \sigma^{\mu\nu} \end{split}$$

Spin, Helicity and Chirality

$$\begin{split} \vec{\mathbf{S}} &= \frac{1}{2}\vec{\mathbf{\Sigma}} \qquad \tilde{h} = \frac{\vec{\mathbf{S}} \cdot \vec{\mathbf{p}}}{|\vec{\mathbf{p}}|} = \frac{\vec{\mathbf{\Sigma}} \cdot \vec{\mathbf{p}}}{2|\vec{\mathbf{p}}|} \qquad \tilde{h} = 2h = \frac{\vec{\mathbf{\Sigma}} \cdot \vec{\mathbf{p}}}{|\vec{\mathbf{p}}|} \qquad P_L = \frac{1-h}{2} \qquad P_R = \frac{1+h}{2} \\ \gamma_L &= \frac{1-\gamma_5}{2} \qquad \gamma_R = \frac{1+\gamma_5}{2} \qquad \gamma_{L,R}^2 = \gamma_{L,R} \qquad \gamma_{L,R}\gamma_{R,L} = 0 \qquad \gamma_L + \gamma_R = 1 \\ \gamma^\mu \gamma_{L,R} &= \gamma_{R,L} \gamma^\mu \qquad \gamma_5 \gamma_L = \gamma_{L} \gamma_5 = -\gamma_L \qquad \gamma_5 \gamma_R = \gamma_R \gamma_5 = \gamma_R \qquad \gamma_{L,R}^\dagger = \gamma_{L,R} \\ \overline{\gamma^\mu \gamma_{L,R}} &= \gamma^\mu \gamma_{L,R} \qquad \overline{\gamma_5 \gamma_L} = -\gamma_R \qquad \overline{\gamma_5 \gamma_R} = \gamma_L \qquad \overline{\gamma_{L,R}} = \gamma_0 \gamma_{L,R}^\dagger \gamma_0 = \gamma_{R,L} \end{split}$$

$$\begin{split} u_{\uparrow} &= N \begin{pmatrix} c \\ se^{i\phi} \\ kc \\ kse^{i\phi} \end{pmatrix} \approx N \begin{pmatrix} c \\ se^{i\phi} \\ c \\ se^{i\phi} \end{pmatrix} \qquad u_{\downarrow} = N \begin{pmatrix} -s \\ ce^{i\phi} \\ ks \\ -kce^{i\phi} \end{pmatrix} \approx N \begin{pmatrix} -s \\ ce^{i\phi} \\ s \\ -ce^{i\phi} \end{pmatrix} \\ v_{\uparrow} &= N \begin{pmatrix} -s \\ -ce^{i\phi} \\ -s \\ ce^{i\phi} \end{pmatrix} \approx N \begin{pmatrix} s \\ -ce^{i\phi} \\ -s \\ ce^{i\phi} \end{pmatrix} \qquad v_{\downarrow} = N \begin{pmatrix} kc \\ kse^{i\phi} \\ c \\ se^{i\phi} \end{pmatrix} \approx N \begin{pmatrix} c \\ se^{i\phi} \\ c \\ se^{i\phi} \end{pmatrix} \\ \vec{\mathbf{p}} &= p(\sin\theta\cos\phi, \sin\theta\sin\phi, \cos\theta) \\ N &= \sqrt{E+m} \approx \sqrt{E} \qquad k = \frac{p}{E+m} \approx 1 \qquad s = \sin\left(\frac{\theta}{2}\right) \qquad c = \cos\left(\frac{\theta}{2}\right) \end{split}$$

Traces

$$Tr[1] = 4 \qquad Tr[\underline{\gamma}^{\mu}\gamma^{\nu} \dots \gamma^{\rho}] = 0 \qquad Tr[\gamma^{\mu}\gamma^{\nu}] = 4g^{\mu\nu}$$

$$Tr[\gamma_{5}] = 0 \qquad Tr[\gamma_{5}\gamma^{\mu}\gamma^{\nu} \dots \gamma^{\rho}] = 0 \qquad Tr[\gamma_{5}\gamma^{\mu}\gamma^{\nu}] = 0$$

$$Tr[\gamma^{\mu}\gamma^{\nu}\gamma^{\rho}\gamma^{\sigma}] = 4(g^{\mu\nu}g^{\rho\sigma} - g^{\mu\rho}g^{\nu\sigma} + g^{\mu\sigma}g^{\nu\rho}) \qquad Tr[\gamma_{5}\gamma^{\mu}\gamma^{\nu}\gamma^{\rho}\gamma^{\sigma}] = -4i\epsilon^{\mu\nu\rho\sigma}$$

$$Tr[\gamma^{\mu}\gamma^{\nu}\gamma^{\rho}\gamma^{\sigma}\gamma_{L}] = 2(g^{\mu\nu}g^{\rho\sigma} - g^{\mu\rho}g^{\nu\sigma} + g^{\mu\sigma}g^{\nu\rho} + i\epsilon^{\mu\nu\rho\sigma})$$

$$Tr[\gamma^{\mu}\gamma^{\nu}\gamma^{\rho}\gamma^{\sigma}\gamma_{R}] = 2(g^{\mu\nu}g^{\rho\sigma} - g^{\mu\rho}g^{\nu\sigma} + g^{\mu\sigma}g^{\nu\rho} - i\epsilon^{\mu\nu\rho\sigma})$$

$$Tr[(p_{a}^{\mu} + m_{a})\gamma^{\mu}(p_{b}^{\mu} + m_{b})\gamma^{\nu}] = 4[p_{a}^{\mu}p_{b}^{\nu} + p_{b}^{\mu}p_{a}^{\nu} + (m_{a}m_{b} - p_{a} \cdot p_{b})g^{\mu\nu}]$$

$$Tr[p_{a}^{\mu}\gamma^{\mu}b_{b}^{\nu}\gamma^{\nu}] Tr[p_{a}^{\mu}\gamma^{\mu}\gamma_{b}\gamma^{\nu}\gamma_{L}] Tr[p_{a}^{\mu}\gamma^{\mu}\gamma^{\nu}\gamma_{L}] Tr[p_{a}^{\mu}\gamma^{\mu}\gamma_{L}] Tr[p_{a}^{\mu}\gamma^{\mu}\gamma_{L}] Tr[p_{a}^{\mu}\gamma^{\mu}\gamma_{L}] Tr[p_{a}^{\mu}\gamma^{\mu}\gamma^{\nu}\gamma_{L}] Tr[p_{a}^{\mu}\gamma^{\mu}\gamma_{L}] Tr[p_{a}^{\mu}\gamma^{\mu}\gamma^{\mu}\gamma_{L}] Tr[p_{a}^{\mu}\gamma^{\mu}\gamma_{L}] Tr[p_{a}^{\mu}\gamma^{\mu}\gamma_{L}] Tr[p_{a}^{\mu}\gamma^{\mu}\gamma_{L}] Tr[p_{a}^{\mu}\gamma^{\mu}\gamma^{\mu}\gamma_{L}] Tr[p_{a}^{\mu}\gamma^{\mu}\gamma_{L}] Tr[p_{a}^{\mu}\gamma^{\mu}\gamma^{\mu}\gamma_{L}] Tr[p_{a}^{\mu}\gamma^{\mu}\gamma_{L}] Tr[p_{a}^{\mu}\gamma^{\mu}\gamma_{L}] Tr[p_{a}^{\mu}\gamma^{\mu}\gamma_{L}]$$

Fermions (Dirac Equation)

$$: a(x)b(x') := a(x)b(x') - b(x')a(x)$$

$$T(a(x)b(x')) = \theta(t-t')a(x)b(x') - \theta(t'-t)b(x')a(x)$$

$$\begin{split} \left\{b^{\dagger}(p,s),b(p',s')\right\} &= \left\{d^{\dagger}(p,s),d(p',s')\right\} = \tilde{\delta}(p-p')\delta_{ss'} \\ \psi(x) &= \psi^{+}(x) + \psi^{-}(x) = \int \widetilde{\mathrm{d}p} \sum_{s} \left[b(p,s)u(p,s)e^{-ip\cdot x} + d^{\dagger}(p,s)v(p,s)e^{+ip\cdot x}\right] \\ \overline{\psi}(x) &= \overline{\psi}^{+}(x) + \overline{\psi}^{-}(x) = \int \widetilde{\mathrm{d}p} \sum_{s} \left[d(p,s)\overline{v}(p,s)e^{-ip\cdot x} + b^{\dagger}(p,s)\overline{u}(p,s)e^{+ip\cdot x}\right] \\ &|e^{-}(p_1,s_1),e^{-}(p_2,s_2)\rangle = b^{\dagger}(p_2,s_2)b^{\dagger}(p_1,s_1)|0\rangle = -|e^{-}(p_2,s_2),e^{-}(p_1,s_1)\rangle \\ \psi^{+}(b) \ \mathrm{destroys} \ e^{-} \quad \psi^{-}(d^{\dagger}) \ \mathrm{creates} \ e^{+} \quad \overline{\psi}^{\dagger}(d) \ \mathrm{destroys} \ e^{+} \quad \overline{\psi}^{-}(b^{\dagger}) \ \mathrm{creates} \ e^{-} \end{split}$$

Spinors (Fermions)

$$\psi = ue^{+i(\vec{\mathbf{P}}\cdot\vec{\mathbf{x}} - E \cdot t)} = ve^{-i(\vec{\mathbf{P}}\cdot\vec{\mathbf{x}} - E \cdot t)} \qquad \overline{\psi} = \psi^{\dagger}\gamma^{0}$$

$$(\not{p} - m)u = \overline{u}(\not{p} - m) = 0 \qquad (\not{p} + m)v = \overline{v}(\not{p} + m) = 0$$

$$\overline{u}'(p)u^{s}(p) = +2m\delta^{rs} \qquad \overline{u}'(p)v^{s}(p) = 0 \qquad u^{r\dagger}(p)u^{s}(p) = 2E\delta^{rs} \qquad \sum_{s=1,2} u^{s}(p)\overline{u}^{s}(p) = \not{p} + m$$

$$\overline{v}'(p)v^{s}(p) = -2m\delta^{rs} \qquad \overline{v}'(p)u^{s}(p) = 0 \qquad v^{r\dagger}(p)v^{s}(p) = 2E\delta^{rs} \qquad \sum_{s=1,2} v^{s}(p)\overline{v}^{s}(p) = \not{p} - m$$

Bosons (Klein-Gordon Equation)

$$: a(x)b(x') := a(x)b(x') + b(x')a(x)$$

$$T(a(x)b(x')) = \theta(t-t)a(x)b(x') + \theta(t'-t)b(x')a(x)$$

The "+" corresponds to positive frequency plane waves $e^{-ik \cdot x}$:

$$\begin{split} \left[\phi(\vec{\mathbf{x}},t),\phi(\vec{\mathbf{y}},t)\right] &= \left[\Pi(\vec{\mathbf{x}},t),\Pi(\vec{\mathbf{y}},t)\right] = 0 \qquad \left[\phi(\vec{\mathbf{x}},t),\Pi(\vec{\mathbf{y}},t)\right] = i\delta^3\left(\vec{\mathbf{x}}-\vec{\mathbf{y}}\right) \\ &= \left[a^\dagger(k,\lambda),a(k',\lambda')\right] = g^{\lambda\lambda'}\,\tilde{\delta}(k-k') \\ A_\mu(x) &= A_\mu^+(x) + A_\mu^-(x) = \int \widetilde{\mathrm{d}}k\, \sum_{\lambda=0}^3 \left[a(k,\lambda)\epsilon_\mu(k,\lambda)e^{-ik\cdot x} + a^\dagger(k,\lambda)\epsilon_\mu^*(k,\lambda)e^{+ik\cdot x}\right] \\ &|p\rangle = a^\dagger(p)|0\rangle \qquad |p_1,p_2\rangle = a^\dagger(p_2)a^\dagger(p_1)|0\rangle = |p_2,p_1\rangle \\ A^+(a) \; \mathrm{destroys}\, \gamma \quad A^-(a^\dagger) \; \mathrm{creates}\, \gamma \end{split}$$

$$\begin{split} \left[a_{+}(p),a_{+}^{\dagger}(q)\right] &= \left[a_{-}(p),a_{-}^{\dagger}(q)\right] = \tilde{\delta}(p-q) \\ \varphi(x) &= \varphi^{+}(x) + \varphi^{-}(x) = \int \widetilde{\mathrm{d}}k \Big[a_{+}(k)e^{-ik\cdot x} + a_{-}^{\dagger}(k)e^{+ik\cdot x}\Big] \\ \varphi^{\dagger}(x) &= \varphi^{+\dagger}(x) + \varphi^{-\dagger}(x) = \int \widetilde{\mathrm{d}}k \Big[a_{-}(k)e^{-ik\cdot x} + a_{+}^{\dagger}(k)e^{+ik\cdot x}\Big] \\ \left|p^{+}\right\rangle &= a_{+}^{\dagger}(p)\left|0\right\rangle \qquad \left|p^{-}\right\rangle = a_{-}^{\dagger}(p)\left|0\right\rangle \qquad \left|p_{1}^{+},p_{2}^{-}\right\rangle = a_{-}^{\dagger}(p_{2})a_{+}^{\dagger}(p_{1})\left|0\right\rangle \end{split}$$

Polarization Vectors (Bosons)

External massless & Massive:

$$\sum_{\lambda=1}^2 \epsilon^\mu(k,\lambda) \cdot \epsilon^{*\nu}(k,\lambda) = -g^{\mu\nu} \qquad \sum_{\lambda=1}^3 \epsilon_\mu(q,\lambda) \epsilon^*_\nu(q,\lambda) = -g_{\mu\nu} + \frac{q_\mu q_\nu}{M^2}$$

Virtual massless:

$$\epsilon(k,\lambda) \cdot \epsilon^*(k,\lambda') = g^{\lambda \lambda'} \qquad \sum_{1} g^{\lambda \lambda} \epsilon^{\mu}(k,\lambda) \cdot \epsilon^{*\nu}(k,\lambda) = g^{\mu\nu}$$

Wick Theorem

$$\Delta_{F}(x_{1}-x_{2}) = \overrightarrow{\phi(x_{1})}\overrightarrow{\phi(x_{2})} = \langle 0|T(\phi(x_{1})\phi(x_{2}))|0\rangle \qquad D_{F}^{\mu\nu} = \overrightarrow{A^{\mu}(x_{1})}\overrightarrow{A^{\nu}}(x_{2})$$

$$\Delta_{F}(x_{1}-x_{2}) = \overrightarrow{\phi(x_{1})}\overrightarrow{\phi^{\dagger}}(x_{2}) = \overrightarrow{\phi^{\dagger}(x_{2})}\overrightarrow{\phi(x_{1})} \qquad S_{F\alpha\beta} = \overrightarrow{\psi_{\alpha}(x_{1})}\overrightarrow{\psi_{\beta}}(x_{2}) = -\overrightarrow{\psi_{\beta}(x_{2})}\overrightarrow{\psi_{\alpha}}(x_{1})$$

Decay: Decay Rates

$$\frac{\mathrm{d}\Gamma}{\mathrm{d}\Omega} = \frac{1}{32\pi^2} \frac{|\vec{\mathbf{p}}_{\mathrm{CM}}|}{m_0^2} \frac{|\vec{\mathbf{p}}_{\mathrm{CM}}|}{|\mathcal{M}|^2} \qquad |\vec{\mathbf{p}}_{\mathrm{CM}}| = \frac{1}{2m_0} \sqrt{\left[m_0^2 - (m_1 + m_2)^2\right] \left[m_0^2 - (m_1 - m_2)^2\right]}$$

Scattering: Cross Sections

$$\frac{\mathrm{d}\sigma}{\mathrm{d}\Omega} = \frac{1}{64\pi^2 s} \frac{|\vec{\mathbf{p}}_3|}{|\vec{\mathbf{p}}_1|} \overline{|\mathcal{M}|^2} \qquad |\vec{\mathbf{p}}| = \frac{1}{2\sqrt{s}} \sqrt{\left[s - (m_a + m_b)^2\right] \left[s - (m_a - m_b)^2\right]}$$

$$s = (p_1 + p_2)^2 = (p_3 + p_4)^2 \approx +2p_1 \cdot p_2 \approx +2p_3 \cdot p_4 \qquad \sqrt{s} = E_{CM}$$

$$t = (p_1 - p_3)^2 = (p_2 - p_4)^2 \approx -2p_1 \cdot p_3 \approx -2p_2 \cdot p_4 \qquad s + t + u = m_1^2 + m_2^2 + m_3^2 + m_4^2$$

$$u = (p_1 - p_4)^2 = (p_2 - p_3)^2 \approx -2p_1 \cdot p_4 \approx -2p_2 \cdot p_3$$

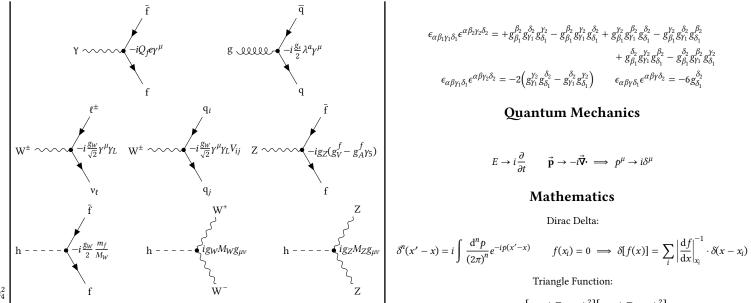
$$f + \bar{f} \longrightarrow g + \bar{g}$$

$$\begin{split} p_1 &= \frac{\sqrt{s}}{2} \Big(1,0,0,+\beta_f\Big) \qquad p_2 &= \frac{\sqrt{s}}{2} \Big(1,0,0,-\beta_f\Big) \\ p_3 &= \frac{\sqrt{s}}{2} \Big(1,+\beta_g \sin\theta,0,+\beta_g \cos\theta\Big) \qquad p_4 &= \frac{\sqrt{s}}{2} \Big(1,-\beta_g \sin\theta,0,-\beta_g \cos\theta\Big) \end{split}$$

$$m = 0$$
: $s = 2|\vec{\mathbf{p}}_{\rm CM}|^2 = 2(p_{\rm CM}^0)^2$ $t = -\frac{s}{2}(1 - \cos\theta)$ $u = -\frac{s}{2}(1 + \cos\theta)$

Feynman Rules for i M

Goes in opposite way of arrows with the first one being adjoint, $\bar{\psi} = \psi^{\dagger} \gamma^0$:



Constants

$$\begin{aligned} \frac{G_F}{\sqrt{2}} &= \frac{g_W^2}{8M_W^2} = \frac{g_W^2}{8M_Z^2\cos^2(\theta_W)} = \frac{1}{2v^2} & M_W = M_Z\cos\theta_W = \frac{1}{2}g_Wv & M_H = \sqrt{2\lambda}v \\ g_W &= g_Z\cos\theta_W = \frac{e}{\sin\theta_W} & g_V^f = \frac{1}{2}T_f^3 - Q_f\sin^2(\theta_W) & g_A^f = \frac{1}{2}T_f^3 & g_{A,V} = \frac{1}{2}c_{A,V} \\ c_L^f &= \frac{g_V^f + g_A^f}{2} & c_R^f = \frac{g_V^f - g_A^f}{2} & g_V^f = c_L^f + c_R^f & g_A^f = c_L^f - c_R^f \end{aligned}$$

Fermions	Q_f	$I_W^{(3)}$	Y_L	Y_R	c_L	c_R	c_V	c_A
v_e, v_μ, v_τ	0	+1/2	-1	0	+1/2	0	+1/2	+1/2
e ⁻ ,μ ⁻ ,τ ⁻	-1	-1/2	-1	-2	-0.27	+0.23	-0.04	-1/2
u, c, t	+2/3	+1/2	+1/3	+4/3	+0.35	-0.15	+0.19	+1/2
d, s, b	-1/3	-1/2	+1/3	-2/3	-0.42	+0.08	-0.35	-1/2

Relativity

$$\beta = \frac{\mathbf{v}}{c} = \frac{\dot{p}}{E} = \tanh(\eta) \qquad \gamma = \frac{1}{\sqrt{1 - \beta^2}} = \cosh(\eta) \qquad \gamma \beta = \sin(\eta)$$

$$E^2 = m^2 + |\mathbf{p}|^2 \qquad \frac{\mathrm{d}^3 \vec{\mathbf{p}}'}{E'} = \frac{\mathrm{d}^3 \vec{\mathbf{p}}}{E} \qquad \widetilde{\mathrm{d}} \vec{p} \equiv \frac{\mathrm{d}^3 \vec{\mathbf{p}}}{(2\pi)^3 2E_p} \qquad \widetilde{\delta}(p - q) \equiv (2\pi)^3 2E_p \, \delta^3(\vec{\mathbf{p}} - \vec{\mathbf{q}})$$

$$x^{\mu} = (t, \vec{\mathbf{x}}) \qquad p^{\mu} = (E, \vec{\mathbf{p}}) \qquad \partial^{\mu} = (\partial_t, -\vec{\mathbf{V}}) \qquad A^{\mu} = (\phi, \vec{\mathbf{A}}) \qquad J^{\mu} = (\rho, \vec{\mathbf{J}})$$

$$F^{\mu\nu} \equiv \partial^{\mu} A^{\nu} - \partial^{\nu} A^{\mu} \qquad \mathcal{F}^{\mu\nu} = \frac{1}{2} \epsilon^{\mu\nu\alpha\beta} F_{\alpha\beta} \qquad \partial_{\mu} F^{\mu\nu} = J^{\nu} \qquad \partial_{\mu} \mathcal{F}^{\mu\nu} = 0$$

$$\epsilon^{\mu\nu\rho\sigma} = \begin{cases} +1 & \text{If } (\mu\nu\rho\sigma) \text{ is an even permutation of (0123)} \\ -1 & \text{If } (\mu\nu\rho\sigma) \text{ is an odd permutation of (0123)} \end{cases}$$

$$\begin{split} \epsilon_{\alpha\beta_{1}\gamma_{1}\delta_{1}}\epsilon^{\alpha\beta_{2}\gamma_{2}\delta_{2}} &= +g_{\beta_{1}}^{\beta_{2}}g_{\gamma_{1}}^{\delta_{2}}g_{\delta_{1}}^{\gamma_{2}} - g_{\beta_{1}}^{\beta_{2}}g_{\gamma_{1}}^{\gamma_{2}}g_{\delta_{1}}^{\delta_{2}} + g_{\beta_{1}}^{\gamma_{2}}g_{\gamma_{1}}^{\beta_{2}}g_{\delta_{1}}^{\delta_{2}} - g_{\beta_{1}}^{\gamma_{2}}g_{\gamma_{1}}^{\delta_{2}}g_{\delta_{1}}^{\delta_{2}} \\ & + g_{\beta_{1}}^{\delta_{2}}g_{\gamma_{1}}^{\gamma_{2}}g_{\delta_{1}}^{\delta_{2}} - g_{\beta_{1}}^{\delta_{2}}g_{\gamma_{1}}^{\gamma_{2}}g_{\delta_{1}}^{\delta_{2}} \\ & \epsilon_{\alpha\beta\gamma_{1}\delta_{1}}\epsilon^{\alpha\beta\gamma_{2}\delta_{2}} = -2\Big(g_{\gamma_{1}}^{\gamma_{2}}g_{\delta_{1}}^{\delta_{2}} - g_{\gamma_{1}}^{\delta_{2}}g_{\delta_{1}}^{\gamma_{2}}\Big) \\ & \epsilon_{\alpha\beta\gamma\delta_{1}}\epsilon^{\alpha\beta\gamma\delta_{2}} = -6g_{\delta_{1}}^{\delta_{2}} \end{split}$$

Quantum Mechanics

$$E \to i \frac{\partial}{\partial t} \qquad \vec{\mathbf{p}} \to -i \vec{\nabla} \cdot \implies p^{\mu} \to i \delta^{\mu}$$

Mathematics

Dirac Delta:

$$\delta^{n}(x'-x) = i \int \frac{\mathrm{d}^{n} p}{\left(2\pi\right)^{n}} e^{-ip(x'-x)} \qquad f(x_{i}) = 0 \implies \delta[f(x)] = \sum_{i} \left|\frac{\mathrm{d} f}{\mathrm{d} x}\right|_{x_{i}}^{-1} \cdot \delta(x-x_{i})$$

Triangle Function:

$$\lambda(a,b,c) = \left[a - \left(\sqrt{b} + \sqrt{c}\right)^{2}\right] \left[a - \left(\sqrt{b} - \sqrt{c}\right)^{2}\right]$$

Residue Theorem:

$$\oint_{\Gamma} dz f(z) = \pm 2\pi i \sum_{k=1}^{n} \operatorname{Res}[f(a_k)] \qquad \operatorname{Res}[f(a_k)] = \lim_{z \to a_k} (z - a_k) f(z)$$

The "-" ("+") is used when Γ is oriented clockwise (counterclockwise).

$$f(z) = \frac{h(z)e^{-iz(t'-t)}}{(z-a_1)(z-a_2)\dots} \stackrel{t'-t<0}{\Longrightarrow} \int_{\Re(z)=-\infty}^{\Re(z)=+\infty} f(z) \, \mathrm{d}z = +2\pi i \sum_{a_k \text{ in UHP}} \mathrm{Res}[f(a_k)]$$

$$\stackrel{t'-t>0}{\Longrightarrow} \int_{\Re(z)=-\infty}^{\Re(z)=+\infty} f(z) \, \mathrm{d}z = -2\pi i \sum_{a_k \text{ in LHP}} \mathrm{Res}[f(a_k)]$$