

University of Nantes
Master 2 in Bioinformatics

Pedagogical Support

Annotated Exercises

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FOREWORD

The solutions to the following exercises were provided by students. They are presented as such, then the erroneous sections are annotated. Afterwards, the different steps of improvement are provided, until a final correct algorithm is obtained.

CONVENTIONS

Annotations in **red** indicate an error.

The corresponding modifications are shown in **blue**.

Annotations in **green** indicate a possible further improvement or optimization.

The corresponding modifications are shown in **blue**.

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```
typedef struct {  
    int val;  
    struct TCell* next;  
} TCell;  
typedef TCell* TPointer
```

Access to position k in a chained list

Iterative version in pseudo-code

```

/*****/
// student version
accessPos (input  head : TPointer,
           input  k : integer,
           output ptrCell : TPointer,
           output found : boolean){

    found ← false
    ptrCell ← head

    i ← 0
    while ( i < k && ptrCell != NULL){
        ptrCell ← ptrCell→next
        i ← i+1
    }

    if (i == k){
        found ← true
    } else {
        found ← false
    }
}

/*****/

```

```

PROCEDURE accessPos (input  head : TPointer,
                     input  k : integer,
                     output ptrCell : TPointer,
                     output found : boolean){

```

local variables:
i : integer

found ← false
 ptrCell ← head

```

i ← 0 i ← 1
while ( (i < k) && and (ptrCell != NULL)){
    ptrCell ← ptrCell→next
    i ← i+1 i++
}

```

```

if (i == k ptrCell != NULL){
    found ← true
} else {
found ← false
}
}

```

```

/*****/

```

```

PROCEDURE accessPos (input  head : TPointer,
                    input  k : integer,
                    output ptrCell : TPointer,
                    output found : boolean){

local variables:
i : integer

found ← false
ptrCell ← head

i ← 1
while ( (i < k) and (ptrCell != NULL)){
    ptrCell ← ptrCell→next
    i++
}

if (ptrCell != NULL){
    found ← true
}
}

/*****/

```

```

PROCEDURE accessPos (input  head : TPointer,
                    input  k : integer,
                    output ptrCell : TPointer,
                    output found : boolean){

local variables:
i : integer

found ← false
ptrCell ← head

i ← 1
while ( (i < k) and (ptrCell != NULL)){
    ptrCell ← ptrCell→next
    i++
}

if (ptrCell != NULL){
    found ← true
}
}

/*****/

```



```

PROCEDURE accessPos (input  head : TPointer,
                    input  k : integer,
                    output ptrCell : TPointer,
                    output found : boolean){

local variables:
i : integer

ptrCell ← head
i      ← 1
while ( (i < k) and (ptrCell != NULL)){
  ptrCell ← ptrCell→next
  i++
}

found ← (ptrCell != NULL)
}

/*****/

```

Translation into C

```
void accessPos (TPointer    head,
                int         k,
                TPointer*   adr_ptrCell,
                boolean*    adr_found){
    int i ;

    *adr_ptrCell = head ;
    i = 1 ;
    while ( (i < k) && ( *adr_ptrCell != NULL)){
        *adr_ptrCell = *adr_ptrCell→next ;
        i++ ;
    }

    *adr_found = ( *adr_ptrCell != NULL) ;
}

/*****/

void main(){
    TPointer    head_list = create_chained_list(...) ; // not developed here
    int         k         = 4 ;
    TPointer    physical_address ;
    boolean     found ;

    accessPos(head_list, k, &physical_address, &found) ;
}

/*****/
```

Translation into C++

```
void accessPos (TPointer    head,
               int          k,
               TPointer    & ptrCell,
               boolean    & found){
    int i ;

    ptrCell = head ;
    i       = 1 ;
    while ( ( i < k) && ( ptrCell != nullptr)){
        ptrCell = ptrCell->next ;
        i++ ;
    }

    found = ( ptrCell != nullptr) ;
}

/*****/

void main(){
    TPointer    head_list = create_chained_list(...) ; // not developed here
    int         k         = 4 ;
    TPointer    physical_address ;
    boolean     found ;

    accessPos(head_list, k, physical_address, found) ;
}

/*****/
/*****/
/*****/
```

Access to position k in a chained list

Iterative version in pseudo-code, version 2

```
/******
```

```
// student version
```

```
PROCEDURE accessPos (input  head : TPointer,  
                     input  k : integer,  
                     output ptrCell : TPointer,  
                     output found : boolean){
```

```
  ptrCell ← head  
  found ← false  
  while ( (ptrCell != NULL) and (not found)){  
    k ← k-1  
    if (k==1){  
      found ← true  
    } else {  
      ptrCell ← ptrCell→next  
    }  
  }  
}
```

```
/******
```

```
PROCEDURE accessPos (input  head : TPointer,  
                     input  k : integer,  
                     output ptrCell : TPointer,  
                     output found : boolean){
```

```
  ptrCell ← head  
  found ← false  
  while ( (ptrCell != NULL) and (not found)){  
    k ← k-1 // Since paramater k is passed by value, the decrement of k will have no effect outside  
           // the procedure.  
    if (k==0){  
      found ← true  
    } else {  
      ptrCell ← ptrCell→next  
    }  
  }  
}
```

```
/******
```

```
/******
```

```
/******
```

- Copy of a chained list

Iterative version in pseudo-code
Version 1

```
/******
```

```
// student version
```

```
PROCEDURE clone( input  head1 : TPointer ,
                  output head2 : TPointer){
```

```

    p1 ← head1
    while (p1!= NULL){
        p2 ← new Pointer
        p2→val ← p1→val
        p1 ← p1→next
        p_sauv→next ← p2
    }
}
```

```
/******
```

```
PROCEDURE clone( input  head1 : TPointer ,
                  output head2 : TPointer){
```

local variables:

p1, p2, p2_prec : TPointer

```

    p1 ← head1 ; p2_prec ← NULL;
    while (p1!= NULL){
p2 ← new Pointer p2 ← allocate_memory()
        p2→val ← p1→val
        p1 ← p1→next
        p_sauv→next ← p2    if (p2_prec == NULL){
                            head2 ← p2
                            } else {
                                p2_prec→next ← p2
                            }

```

```

    p2_prec ← p2
}

```

```

if (head1 == NULL){
    head2 ← NULL
} else {
    p2→next ← NULL
}
}

```

```
/******
```

```
PROCEDURE clone( input  head1 : TPointer ,
                  output head2 : TPointer){
```

```
  local variables:
```

```
  p1, p2, p2_prec : TPointer
```

```
  p1 ← head1 ; p2_prec ← NULL;
```

```
  while (p1!= NULL){
```

```
    p2 ← allocate_memory()
```

```
    p2→val ← p1→val
```

```
    p1 ← p1→next
```

```
    if (p2_prec == NULL){
```

```
      head2 ← p2
```

```
    } else {
```

```
      p2_prec→next ← p2
```

```
    }
```

```
    p2_prec ← p2
```

```
  }
```

```
  if (head1 == NULL){
```

```
    head2 ← NULL
```

```
  } else {
```

```
    p2→next ← NULL
```

```
  }
```

```
}
```

```
/***/
```

```
PROCEDURE clone( input  head1 : TPointer ,
                  output head2 : TPointer){
```

```
    local variables:
```

```
    p1, p2, p2_prec : TPointer
```

```
    p1 ← head1 ; p2_prec ← NULL;
```

```
    while (p1!= NULL){
```

```
        p2 ← allocate_memory()
```

```
        p2→val ← p1→val
```

```
        p1 ← p1→next
```

```
        if (p2_prec == NULL){
```

```
            head2 ← p2
```

```
        } else {
```

```
            p2_prec→next ← p2
```

```
        }
```

```
        p2_prec ← p2
```

```
    }
```

```
    if (head1 == NULL){
```

```
        head2 ← NULL
```

```
    } else {
```

```
        p2→next ← NULL
```

```
    }
```

```
}
```

```
/***/
```

```
PROCEDURE clone( input  head1 : TPointer ,
                  output head2 : TPointer){
```

```
    local variables:
```

```
    p1, p2, p2_prec : TPointer
```

```
    p1 ← head1 ; p2_prec ← NULL;
```

```
    while (p1!= NULL){
```

```
        p2 ← allocate_memory()
```

```
        p2→val ← p1→val
```

```
        p1 ← p1→next
```

```
        if (p2_prec == NULL){
```

```
            head2 ← p2
```

```
        } else {
```

```
            p2_prec→next ← p2
```

```
        }
```

```
        p2_prec ← p2
```

```
    }
```

```
    if (head1 == NULL){head2 ← NULL ; return}
```

```
    p2→next ← NULL
```

```
}
```

```
/***/
```

```
/***/
```

```
/***/
```


Copy of a chained list

Iterative version in C++, version 2

```
/******
```

```
// student version
```

```
void copy(TPointer head1,
          TPointer & head2){
    boolean first = true ;
    TPointer prec ;
    TPointer p2 ;
    while(head1!= nullptr){
        p2 = new TCell ;
        if (first) {
            head2 = p2 ;
        } else {
            prec->next = p2 ;
        }
        p2->val = head1->val ;
        head1 = head1->next ;
        prec = p2 ;
        first = false ;
    }

    if (head1 == nullptr){
        head2 = nullptr;}
    else {
        p2->next = nullptr ;}
}
```

```

void copy(TPointer head1,
          TPointer & head2){
    boolean first = true ;
    TPointer prec ;
    TPointer p2 ;
    while(head1!= nullptr){
        p2 = new TCell ;
        if (first) {
            head2 = p2 ;
        } else {
            prec→next = p2 ;
        }
        p2→val = head1→val ;
        head1 = head1→next ;
        prec = p2 ;
        first = false ;
    }

    if (head1 == nullptr){
        head2 = nullptr;}
    else {
        p2→next = nullptr ;}
    }

/*****/

```

```

void copy(TPointer head1,
         TPointer & head2){
    boolean first = true ;
    TPointer prec ;
    TPointer p2 ;
    while(head1!= nullptr){
        p2 = new TCell ;
        if (first) {
            head2 = p2 ;
            first = false ;
        } else {
            prec→next = p2 ;
        }
        p2→val = head1→val ;
        head1 = head1→next ;
        prec = p2 ;
    }

    if (head1 == nullptr){
        head2 = nullptr;
    } else {
        p2→next = nullptr ;
    }
}

/*****/

```

```

void copy(TPointer head1,
         TPointer & head2){
    boolean first = true ;
    TPointer prec2 ;
    TPointer p1 = head1; // Even if parameter head1 is passed by value, as is therefore not
                          // impacted by modifications within procedure copy, it is not wise
                          // to use head1 to traverse list head1. A local variable (p1)
                          // should be used instead.

    TPointer p2 ;
    while(p1 != nullptr){
        p2 = new TCell ;
        if (first) {
            head2 = p2 ;
            first = false ;
        } else {
            prec2→next = p2 ;
        }
        p2→val = p1→val ;
        p1 = p1→next ;
        prec2 = p2 ;
    }

    if (head1 == nullptr){
        head2 = nullptr;
    } else {
        p2→next = nullptr ;
    }
}

/*****/
/*****/
/*****/

```

Copy of a chained list

Iterative version in C++, version 3

```
*****/

// student version
void clone_bis(TPointer head1,
               TPointer & head2){
    if (head1 == nullptr){
        head2 = nullptr ;
    } else {

        p1 = head1 ;
        p2 = (char *) malloc(sizeof(char)) ;

        while (p1!= nullptr){
            p2→val = p1→val ;
            p1 = p1→next ;
            if (p1!= nullptr){
                p_clone→next = (char*) malloc(sizeof(char)) ;
                p2→next = p_clone
            }
        }
    }
}

*****/
```

```

void clone_bis(TPointer head1,
              TPointer & head2){
    TPointer p1,p2 ;

    if (head1 == nullptr){
        head2 = nullptr ;
    } else {

        // The list head1 contains at least one element.
        p1 = head1 ;
p2=(char*) malloc(sizeof(char)); p2 = new TCell ;

        while (p1!= nullptr){
            p2→val = p1→val ;
            p1 = p1→next ;
            if (p1!= nullptr){
p_clone→next=(char*) malloc(sizeof(char)); p_clone = new TCell ;
                p2→next = p_clone ;
                p2 = p_clone ;
            } else {
                p2→next = nullptr ;
            }
        } // end while
    } // end else
}

/*****/

```

```

void clone_bis(TPointer head1,
              TPointer & head2){
    TPointer p1,p2 ;

    if (head1 == nullptr){
        head2 = nullptr ;
    } else {

        // The list head1 contains at least one element.
        p1 = head1 ;
        p2 = new TCell ;

        while (p1!= nullptr){
            p2→val = p1→val ;
            p1 = p1→next ;
            if (p1!= nullptr){
                p_clone = new TCell ;
                p2→next = p_clone ;
                p2 = p_clone ;
            } else {
                p2→next = nullptr ;
            }
        } // end while
    } // end else
}

/*****/

```

```

void clone_bis(TPointer head1,
              TPointer & head2){
    TPointer p1,p2 ;

    if (head1 == nullptr){head2 = nullptr ; return;}

    // The list head1 contains at least one element.
    p1 = head1 ;
    p2 = new TCell ;

    while (p1!= nullptr){
        p2→val = p1→val ;
        p1 = p1→next ;
        if (p1!= nullptr){
            p_clone = new TCell ;
            p2→next = p_clone ;
            p2 = p_clone ;
        } else {
            p2→next = nullptr ;
        }
    } // end while

}

/*****/
/*****/
/*****/

```


Insertion at position k in a chained list Iterative version in C++, version 1

/******

// student version

```
void insertPos(TPointer head,
              int info,
              int k,
              bool & possible){
    TPointer ptr_after_k ;
    TPointer ptr_cell ;

    ptr_cell = head ;

    int pos = 1 ;
    possible = false ;
    k = k-1 ;

    while (pos!= k & ptr_cell->next != nullptr){
        ptr_cell = ptr_cell->next ;
        pos++ ;
    }

    if (pos == k){
        ptr_after_k = ptr_cell->next ;
        TPointer novel_p ;
        novel_p->val = info ;
        novel_p->next = ptr_cell->next ;
        ptr_cell->next = novel_p ;
    }

    if ((k+1) == 1){
        add_front(head,info) ;
    }
}
```

/******

```
void main(){
    TPointer list = create_chained_list() ; // not developed here
    int k = 4 ;
    bool is_inserted ;
    int value_to_insert ;
    insertPos(list, value_to_insert, k, is_inserted) ;
}
```

/******

```

void insertPos(TPointer & head,
              int info,
              int k,
              bool & possible){
TPointer ptr_after_k; TPointer ptr_k ;
TPointer ptr_cell ;

ptr_cell = head ;

int pos = 1;
possible = false ;
k = k-1; // confusing

// test is missing to handle if (head == nullptr){
// the case of the if (k==1){add_front(head,info) ; possible = true ;}
// empty cell return ;
}

int pos = 1 ;
while (pos!=k & ptr_cell->next!=nullptr){ while ((pos < k-1) && (ptr_cell != nullptr)){
    ptr_cell = ptr_cell->next ;
    pos++ ;
}

if (pos==k){ if (pos == k-1){
    possible = true ;
    ptr_k = ptr_cell->next ; // ptr_k may be equal to nullptr, which indicates
                           // that cells 1 to k-1 exit, but cell k does not. In this case,
                           // the insertion is possible and will take place at the end of the list.
TPointer novel_p; TPointer novel_p = new TCell;
    novel_p->val = info ;
    novel_p->next = ptr_k ; // possibly equal to nullptr
    ptr_cell->next = novel_p ;
}

if ((k+1)==1){ if (k == 1){ // Insertion in a front of a non empty list.
    add_front(head,info) ; // The previous "while" and "if" instructions where short circuited.
    possible = true ;
}
}

/*****/

void main(){
    TPointer list = create_chained_list() ; // not developed here
    int k = 4 ;
    bool is_inserted ;
    int value_to_insert = 18;
    insertPos(list, value_to_insert, k, is_inserted) ;
}

/*****/

```

```

void insertPos(TPointer & head,
              int      info,
              int      k,
              bool      & possible){
    TPointer ptr_k ;
    TPointer ptr_cell = head ;

    possible = false ;

    if (head == nullptr){
        if (k==1){add_front(head,info) ; possible = true ;}
        return ;
    }

    int pos = 1 ;
    while ((pos < k-1) && (ptr_cell != nullptr)){
        ptr_cell = ptr_cell->next ;
        pos++ ;
    }

    if (pos == k-1){
        possible = true ;
        ptr_k = ptr_cell->next ;      // ptr_k may be equal to nullptr, which indicates
                                    // that cells 1 to k-1 exist, but cell k does not. In this case,
                                    // the insertion is possible and will take place at the end of the list.

        TPointer novel_p = new TCell;
        novel_p->val = info ;
        novel_p->next = ptr_k ; // possibly equal to nullptr
        ptr_cell->next = novel_p ;
    }

    if (k == 1){                // Insertion in a front of a non empty list.
        add_front(head,info) ; // The previous 'while' and 'if' instructions were short circuited.
        possible = true ;
    }

}

/*****/

void main(){
    TPointer list = create_chained_list() ; // not developed here
    int      k = 4 ;
    bool      is_inserted ;
    int      value_to_insert = 18 ;
    insertPos(list, value_to_insert, k, is_inserted) ;
}

/*****/
/*****/
/*****/

```

Insertion at position k in a chained list Iterative version in C++, version 2

```
/******
```

```
// student version
```

```
void addPos(TPointer & head,
            int      k,
            int      info,
            bool      & possible){
    TPointer p = head ;
    TPointer prec ;
    bool      front_insertion = true ;
    possible   = false ;
    while ((p!= nullptr) && (not possible)){
        k = k-1 ;
        if (k == 0){
            possible = true ;
        } else {
            front_insertion = false ;
            prec = p ;
            p = p->next ;
        }
    }

    if (possible){
        add_front(p,info) ;
        if (front_insertion){
            head = p ;
        } else {
            prec->next = p ;
        }
    }

    if (k-1 == 0){
        possible = true ;
        addQueue(prec,info) ;
    }
}
```

```
/******
```

```

void addPos(TPointer & head,
           int      k,
           int      info,
           bool      & possible){
    TPointer p = head ;
    TPointer prec ;
    bool     front_insertion = true ;
    possible = false ;
    while ((p!= nullptr) && (not possible)){
        k = k-1 ;
        if (k == 0){
            possible = true ;
        } else {
            front_insertion = false ;
            prec = p ;
            p = p->next ;
        }
    }

    if (possible){ // possible could only be set to true if the list was not empty
        add_front(p,info) ;
        if (front_insertion){
            head = p ;
        } else {
            prec->next = p ;
        }
    }
    return ;
}

// case of the empty list
if (k-1 == 0){ if (head == nullptr){ // The above while instruction was short circuited.
    if (k == 1) { // It is only possible to insert an element in an empty list at
        possible = true ; // the first position.
        add_front(head,info) ;
    }
    addQueue(prec,info);
}

}

/*****/

```

```

void addPos(TPointer & head,
           int      k,
           int      info,
           bool      & possible){
    TPointer p = head ;
    TPointer prec ;
    bool      front_insertion = true ;
    possible  = false ;
    while ((p!= nullptr) && (not possible)){
        k = k-1 ;
        if (k == 0){
            possible = true ;
        } else {
            front_insertion = false ;
            prec = p ;
            p = p->next ;
        }
    }

    if (possible){ // possible could only be set to true if the list was not empty
        add_front(p,info);
        if (front_insertion){
            head=p; add_front(head,info) ;
        } else {
            prec->next=p; add_front(rec_next,info) ;
        }
        return ;
    }

    // case of the empty list
    if (head == nullptr){ // The above while instruction was short circuited.
        if (k == 1) { // It is only possible to insert an element in an empty list at
            possible = true ; // the first position.
            add_front(head,info) ;
        }
    }
}

/*****/

```

```

void addPos(TPointer & head,
           int      k,
           int      info,
           bool      & possible){
    TPointer p = head ;
    TPointer prec ;
    bool      front_insertion = true ;
    possible  = false ;
    while ((p!= nullptr) && (not possible)){
        k = k-1 ;
        if (k == 0){
            possible = true ;
        } else {
            front_insertion = false ;
            prec = p ;
            p = p→next ;
        }
    }

    if (possible){ // possible could only be set to true if the list was not empty
        if (front_insertion){
            add_front(head,info) ;
        } else {
            add_front(rec_next,info) ;
        }
        return ;
    }

    // case of the empty list
    if (head == nullptr){ // The above while instruction was short circuited.
        if (k == 1) { // It is only possible to insert an element in an empty list at
            possible = true ; // the first position.
            add_front(head,info) ;
        }
    }
}

/*****/
/*****/
/*****/

```

Insertion at position k in a chained list Iterative version in C++, version 3

```
/******  
  
// student version  
  
void insertPos(TPointer & head,  
              int      k,  
              int      info,  
              bool      & possible){  
  
    TPointer p ;  
    TPointer prec ;  
  
    p = head ;  
    prec = nullptr ;  
    int cnt = 1 ;  
    possible = false ;  
    while( (p!=nullptr) && (cnt < k)){  
        prec = p ; p = p->next ;  
    }  
  
    if (k==1){  
        add_front(head,info) ;  
        possible = true ;  
        return ;  
    }  
  
    TPointer p_new = new TCell ;  
    p_new->val = info ;  
    p_new->next = p ;  
    prec->next = p_new ;  
    possible = true ;  
    return ;  
}  
  
/******
```



```

void insertPos(TPointer & head,
              int      k,
              int      info,
              bool      & possible){

    TPointer p ;
    TPointer prec ;

    possible = false ;

    if (k==1){
        add_front(head,info) ;
        possible = true ;
        return ;
    }

    p = head ;
prec = nullptr ;
    int cnt = 1 ;
possible = false ;
    while( (p!=nullptr) && (cnt <k)){
        prec = p ; p = p->next ; cnt++ ;
    }
    // postcondition :
    // p == nullptr and cpt < k : The non empty list is too short.
    // p == nullptr and cpt ==k : Insertion at the end of the non-empty list.
    // p != nullptr and cpt == k : Insertion in the middle of the non-empty list.

if (k==1){
add_front(head,info) ;
possible = true ;
return ;
}

    if ( (p==nullptr) && (cnt <k) ){return ;} // The non empty list is too short.

    TPointer p_new = new TCell ;
    p_new->val = info ;
    p_new->next = p ;
    prec->next = p_new ;
    possible = true ;
return ;
}

/*****/

```

```

void insertPos(TPointer & head,
              int      k,
              int      info,
              bool      & possible){

TPointer p ;
TPointer prec ;

possible = false ;

if (k==1){
    add_front(head,info) ;
    possible = true ;
    return ;
}

p = head ;
int cnt = 1 ;
while( (p!=nullptr) && (cnt <k)){
    prec = p ; p = p->next ; cnt++ ;
}
// postcondition :
// p == nullptr and cpt < k : The non empty list is too short.
// p == nullptr and cpt ==k : Insertion at the end of the non-empty list.
// p != nullptr and cpt == k : Insertion in the middle of the non-empty list.

if ( (p==nullptr) && (cnt <k){return ;} // The non empty list is too short.

add_front(prec->next,info) ;
possible = true ;
}

/*****/

```

```

void insertPos(TPointer & head,
              int      k,
              int      info,
              bool      & possible){

    TPointer p ;
    TPointer prec ;

    possible = false ;

    if (k==1){
        add_front(head,info) ;
        possible = true ;
        return ;
    }

    p = head ;
    int cnt = 1 ;
    while( (p!=nullptr) && (cnt < k)){
        prec = p ; p = p->next ; cnt++ ;
    }
    // postcondition :
    // p == nullptr and cpt < k : The non empty list is too short.
    // p == nullptr and cpt ==k : Insertion at the end of the non-empty list.
    // p != nullptr and cpt == k : Insertion in the middle of the non-empty list.

    if ( (p==nullptr) && (cnt < k){return ;} // The non empty list is too short.

    add_front(prec->next,info) ;
    possible = true ;
}

/*****/
/*****/
/*****/

```

Insertion at queue position in a chained list

Iterative version in C++, version 1

```
/******  
  
// student version  
  
void insertQueue(TPointer & head,  
                int      info){  
  
    TPointer p = head ;  
    if (p!= nullptr){  
        while(p->next!= nullptr){  
            p = p->next ;  
        }  
    }  
  
    TPointer p_new = new TCell ;  
    p_new->val = info ;  
    p_new->next = nullptr ;  
    p->next = p_new ;  
  
}  
  
/******
```

```

void insertQueue(TPointer & head,
                int      info){

    TPointer p  = head ;
    TPointer prec = nullptr ;
if (p!= nullptr){          while(p != nullptr){
while(p->next!= nullptr){    prec = p ; p = p->next ;
    p = p->next ;              }
}

if (prec == nullptr){
    add_front(head, info) ;
} else {

    TPointer p_new = new TCell ;
    p_new->val = info ;
    p_new->next = nullptr ;
    p->next = p_new ;
}

}

/*****/

```

```
void insertQueue(TPointer & head,  
                int      info){
```

```
    TPointer p  = head ;  
    TPointer prec = nullptr ;  
    while(p != nullptr){  
        prec = p ; p = p->next ;  
    }
```

```
    if (prec == nullptr){  
        add_front(head, info) ;  
    } else {  
        add_front(prec->next,info) ;  
    }
```

```
}
```

```
/*-----*/
```

```

void insertQueue(TPointer & head,
                int      info){

    TPointer p  = head ;
    TPointer prec = nullptr ;
    while(p != nullptr){
        prec = p ; p = p->next ;
    }

    if (prec == nullptr){
        add_front(head, info) ;
    } else {
        add_front(prec->next,info) ;
    }

}

/*****/
/*****/
/*****/

```

Reversal of a chained list

Iterative version in C++, version 1

```
/******  
  
// student version  
  
void reverse (TPointer    head1,  
              TPointer  & head2){  
  
    TPointer p1 = head1 ;  
    head2 = nullptr ;  
    if (p1!= nullptr){  
        while(p1→next != nullptr){  
            add_front(head2,p1→val) ;  
        }  
    }  
  
}  
/******
```



```

void reverse (TPointer    head1,
              TPointer  & head2){

    TPointer p1 = head1 ;
    head2 = nullptr ;
if (p1!= nullptr){
    while(p1->next != nullptr){    while (p1!= nullptr){
        add_front(head2,p1->val) ;
    }
}

}
/*****/

```

```

void reverse (TPointer    head1,
              TPointer  & head2){

    TPointer p1 = head1 ;
    head2 = nullptr ;
    while (p1!= nullptr){
        add_front(head2,p1→val) ;
    }

}

/*****/

void reverse (TPointer    head1,
              TPointer  & head2){

    TPointer p1 = head1 ;
    head2 = nullptr ;
    while (p1!= nullptr){
        add_front(head2,p1→val) ;
    }

}

/*****/
/*****/
/*****/

```

Retrieval of an information in a binary tree, with display of the values encountered along the path down to the information if existing
Recursive version in pseudo-code, version 1

```

/*****/

// student version

PROCEDURE find_elem_and_display_path (input      n : TBinTree,
                                     input      e : integer,
                                     input/output list : TPointer,
                                     input/output found : boolean){

  if (n!= null && ! found){

    add_queue(list,n→val)
    if (n→val == e){
      display_list(list)
      found ← true
    } else {
      find_elem_and_display_path(n→lc, e, list, found)
      find_elem_and_display_path(n→rc, e, list, found)
      pop_queue(list)
    }
  }
}

/*****/

void main(){
  root      : TBinTree
  path      : TPointer
  found     : boolean
  searched_val : integer

  root ← create_binary_tree() // not developed here

  found ← false ; path ← null ; searched_val = 48
  find_elem_and_display_path (root, searched_val, path, found)
}

/*****/
```

```

PROCEDURE find_elem_and_display_path (input      n : TBinTree,
                                     input      e : integer,
                                     input/output list : TPointer,
                                     input/output found : boolean){

```

```

if (n == null){
} else {

```

```

if (n!=null && !found){ if (n!= null){

```

```

    add_queue(list,n→val)
    if (n→val == e){
        display_list(list)
        found = true
    } else {
        find_elem_and_display_path(n→lc, e, list, found)
        if ( ! found){ find_elem_and_display_path(n→rc, e, list, found)}
        if ( ! found){ pop_queue(list)}
    }
}
}
}
/*****/

```

```

void main(){
    root      : TBinTree
    path      : TPointer
    found      : boolean
    searched_val : integer

    root ← create_binary_tree() // not developed here

    found ← false ; path ← null ; searched_val = 48
    find_elem_and_display_path (root, searched_val, path, found)
}

```

```

/*****/

```

```

PROCEDURE find_elem_and_display_path (input      n : TBinTree,
                                     input      e : integer,
                                     input/output list : TPointer,
                                     input/output found : boolean){

```

```

if (n == null){
}-else-{    if (n!= null){
    add_queue(list,n->val)
    if (n->val == e){
        display_list(list)
        found = true
    } else {
        find_elem_and_display_path(n->lc, e, list, found)
        if ( ! found){ find_elem_and_display_path(n->rc, e, list, found)}
        if ( ! found){pop_queue(list)}
    }
}
}
}
/*****/

```

```

void main(){
    root      : TBinTree
    path      : TPointer
    found      : boolean
    searched_val : integer

    root ← create_binary_tree() // not developed here

    found ← false ; path ← null ; searched_val = 48
    find_elem_and_display_path (root, searched_val, path, found)
}

/*****/

```

```

PROCEDURE find_elem_and_display_path (input      n : TBinTree,
                                     input      e : integer,
                                     input/output list : TPointer,
                                     input/output found : boolean){

```

```

    if (n!= null){
        add_queue(list,n->val)
        if (n->val == e){
            display_list(list)
            found = true
        } else {
            find_elem_and_display_path(n->lc, e, list, found)
            if ( ! found){
                find_elem_and_display_path(n->rc, e, list, found)
                if ( ! found){pop_queue(list)}
            }
        }
    }
}
/*****/

```

```

void main(){
    root      : TBinTree
    path      : TPointer
    found      : boolean
    searched_val : integer

    root ← create_binary_tree() // not developed here

    found ← false ; path ← null ; searched_val = 48
    find_elem_and_display_path (root, searched_val, path, found)
}

/*****/

```

```

PROCEDURE find_elem_and_display_path (input      n : TBinTree,
                                     input      e : integer,
                                     input/output list : TPointer,
                                     input/output found : boolean){

```

```

    if (n!= null){
        add_queue(list,n→val)
        if (n→val == e){
            display_list(list)
            found = true
        } else {
            find_elem_and_display_path(n→lc, e, list, found)
            if ( ! found){
                find_elem_and_display_path(n→rc, e, list, found)
            } if ( ! found){pop_queue(list)}
        }
    }
}

```

```

/*****/

```

```

void main(){
    root      : TBinTree
    path      : TPointer
    found      : boolean
    searched_val : integer

    root ← create_binary_tree() // not developed here

    found ← false ; path ← null ; searched_val = 48
    find_elem_and_display_path (root, searched_val, path, found)
}

```

```

/*****/
/*****/
/*****/

```

Retrieval of an information in a binary tree, with display of the values encountered along the path down to the information if existing
Recursive version in pseudo-code, version 2

```

/*****/
// student version

PROCEDURE find_elem_and_display_path_bis (input      n : TBinTree,
                                           input      e : integer,
                                           input/output list : TPointer,
                                           input/output found : boolean){

    if ((n→val == e) && (n!=null)){
        add_front(list, n→val)
        found = true
    } else {
        find_elem_and_display_path_bis(n→lc, e, list, found)
        if ( ! found){find_elem_and_display_path_bis(n→rc, e, list, found)}
        if ( found){add_front(list, n→val)}
    }
}

/*****/

void main(){
    root      : TbinTree
    path      : TPointer
    found      : boolean
    searched_val : integer

    root ← create_binary_tree() // not developed here

    found ← false ; path ← null ; searched_val = 48
    find_elem_and_display_path_bis (root, searched_val, path, found)
    if (path!= null) {display(path)}
}

/*****/

```



```

PROCEDURE find_elem_and_display_path_bis (input      n : TBinTree,
input      e : integer,
input/output list : TPointer,
input/output found : boolean){

if ((n->val == e) && (n!=null)){    if ((n!=null) && (n->val == e)){ // left to right evaluation,
// precondition for
// test n->val == e :
// n!= null
// Besides, the else section below applies to (n!=null and n->val!= e)
// not to the negation of the test ((n!=null) && (n->val == e))

    add_front(list, n->val)
    found = true
} else {
    find_elem_and_display_path_bis(n->lc, e, list, found)
    if ( ! found){find_elem_and_display_path_bis(n->rc, e, list, found)}
    if ( found){add_front(list, n->val)}
}
}

/*****/

void main(){
    root      : TbinTree
    path      : TPointer
    found      : boolean
    searched_val : integer

    root ← create_binary_tree() // not developed here

    found ← false ; path ← null ; searched_val = 48
    find_elem_and_display_path_bis (root, searched_val, path, found)
    if (path!= null) {display(path)}
}

/*****/

```

```

PROCEDURE find_elem_and_display_path_bis (input      n : TBinTree,
input      e : integer,
input/output list : TPointer,
input/output found : boolean){

```

```

if (n!=null){

```

```

    if (n->val == e){
        add_front(list, n->val)
        found = true
    } else {
        find_elem_and_display_path_bis(n->lc, e, list, found)
        if ( ! found){find_elem_and_display_path_bis(n->rc, e, list, found)}
        if ( found){add_front(list, n->val)}
    }

```

```

}
}

```

```

/*****/

```

```

void main(){
    root      : TbinTree
    path       : TPointer
    found      : boolean
    searched_val : integer

    root ← create_binary_tree() // not developed here

    found ← false ; path ← null ; searched_val = 48
    find_elem_and_display_path_bis (root, searched_val, path, found)
    if (path!= null) {display(path)}
}

```

```

/*****/

```

```

PROCEDURE find_elem_and_display_path_bis (input      n : TBinTree,
input      e : integer,
input/output list : TPointer,
input/output found : boolean){

```

```

if (n!=null){

    if (n->val == e){
        add_front(list, n->val)
        found = true
    } else {
        find_elem_and_display_path_bis(n->lc, e, list, found)
        if ( ! found){find_elem_and_display_path_bis(n->rc, e, list, found)}
        if ( found){add_front(list, n->val)}
    }

}
}

```

```

/*****/

```

```

void main(){
    root      : TbinTree
    path      : TPointer
    found      : boolean
    searched_val : integer

    root ← create_binary_tree() // not developed here

    found ← false ; path ← null ; searched_val = 48
    find_elem_and_display_path_bis (root, searched_val, path, found)
    if (path!= null) {display(path)}
}

```

```

/*****/

```