

FALL 22

(1) for the node with v_1 voltage:

$$\frac{80 - v_1}{20} = \frac{v_1 - v_2}{30} + \frac{v_1 - v_x}{30} = \frac{2v_1 - v_2 - v_x}{30}$$

$$\Rightarrow 2400 - 30v_1 = 40v_1 - 20v_2 - 20v_x$$

$$\Rightarrow -70v_1 - 20v_2 - 20v_x = 2400 \quad \text{--- (1)}$$

for the node with v_2 voltage:

$$\frac{v_x - v_2}{30} + \frac{v_1 - v_2}{30} = \frac{v_2 - (-80)}{20}$$

$$\Rightarrow \frac{v_1 - 2v_2 + v_x}{30} = \frac{v_2 + 80}{20}$$

$$\Rightarrow 20v_1 - 40v_2 + 20v_x = 30v_2 + 2400$$

$$\Rightarrow 20v_1 - 70v_2 + 20v_x = 2400 \quad \text{--- (2)}$$

for the node x :

$$\frac{v_1 - v_x}{30} = \frac{v_x}{20} + \frac{v_x - v_2}{30} = \frac{3v_x + 2v_x - 2v_2}{60} = \frac{5v_x - 2v_2}{60}$$

$$\Rightarrow 2v_1 - 2v_x = 5v_x - 2v_2$$

$$\Rightarrow 2v_1 + 2v_2 - 7v_x = 0$$

solving (1), (2) and (3)

$$v_1 = 26.67$$

$$v_2 = -26.67$$

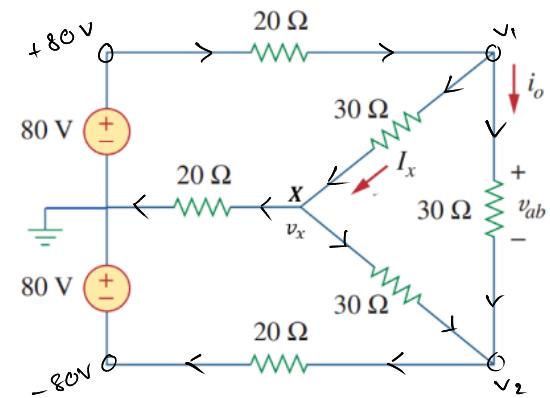
$$v_x = 0$$

$$v_{ab} = v_1 - v_2 = 26.67 + 26.67 = 53.34 V$$

$$i_o = \frac{v_{ab}}{30} = 1.78 A$$

$$I_x = \frac{v_1 - v_x}{30} = \frac{26.67 - 0}{30} = 0.89 A$$

$$v_x = 0$$



2) a)

loop 1

$$(i_1 - i_3) + 3(i_1 - i_2) - 12 = 0$$

$$\Rightarrow i_1 - i_3 + 3i_1 - 3i_2 - 12 = 0$$

$$\Rightarrow 4i_1 - 3i_2 - i_3 - 12 = 0 \quad \text{--- (1)}$$

loop 2

$$3(i_2 - i_1) + 4(i_2 - i_4) = 0$$

$$\Rightarrow 3i_2 - 3i_1 + 4i_2 - 4i_4 = 0$$

$$\Rightarrow -3i_1 + 7i_2 + 12 = 0 \quad \text{--- (2)}$$

loop 3

$$6i_3 + 8(i_3 - i_4) + (i_3 - i_1) = 0$$

$$\Rightarrow 6i_3 + 8i_3 - 8i_4 + i_3 - i_1 = 0$$

$$\Rightarrow -i_1 + 15i_3 + 24 = 0 \quad \text{--- (3)}$$

loop 4

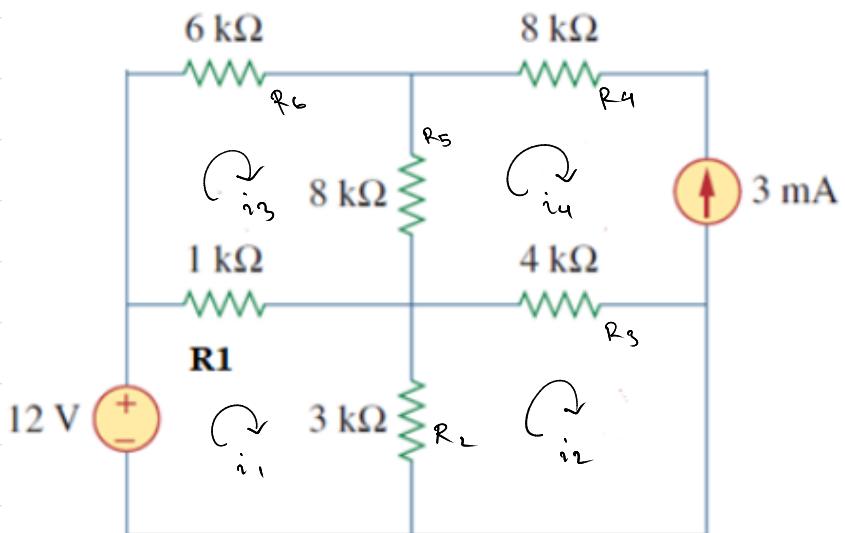
$$i_4 = -3 \text{ mA}$$

solving (1), (2) and (3)

$$i_1 = 1.9856 \text{ mA}$$

$$i_2 = -0.86 \text{ mA}$$

$$i_3 = -1.467 \text{ mA}$$



$$\text{current through } R_1 = i_1 - i_3 = 3.45 \text{ mA}$$

$$\text{---} \quad \text{---} \quad R_2 = i_1 - i_2 = 2.84 \text{ mA}$$

$$\text{---} \quad \text{---} \quad R_3 = i_2 - i_4 = 2.14 \text{ mA}$$

$$\text{---} \quad \text{---} \quad R_4 = 3 \text{ mA}$$

$$\text{---} \quad \text{---} \quad R_5 = i_4 - i_3 = -1.533 \text{ mA}$$

$$\text{---} \quad \text{---} \quad R_6 = i_3 = -1.467 \text{ mA}$$

$$\text{b) } P = i^2 R = (3.45 \text{ mA})^2 \times 1 \text{ k}\Omega$$

$$= 3.45^2 \times 10^{-6} \times 10^3 \text{ W}$$

$$= 0.0119 \text{ W}$$

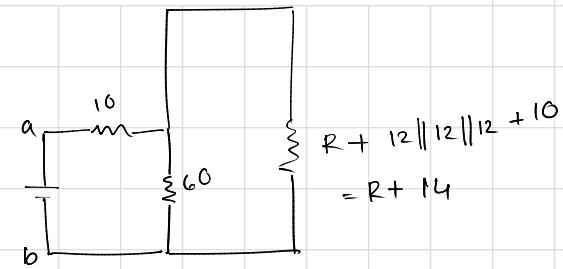
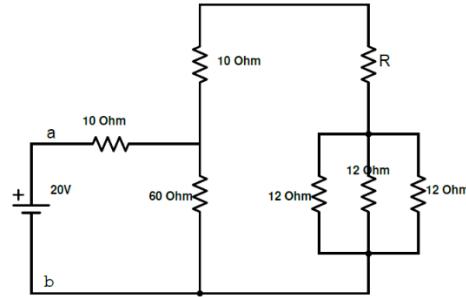
$$(3) \quad a) \quad 10 + 60 \parallel (R+14) = 50$$

$$\Rightarrow \left(60^{-1} + (R+14)^{-1} \right)^{-1} = 40$$

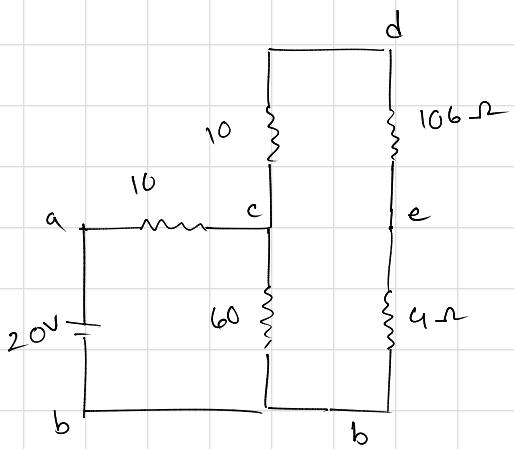
$$\Rightarrow 60^{-1} + (R+14)^{-1} = 40^{-1}$$

$$\Rightarrow R+14 = (40^{-1} - 60^{-1})^{-1}$$

$$\Rightarrow R = (40^{-1} - 60^{-1})^{-1} - 14 = 106 \Omega$$



b)



$$V_{eb} = 20 \times \frac{60 \parallel (106+10+4)}{10 + 60 \parallel (106+10+4)} = 16V$$

$$V_{eb} = 16 \times \frac{4}{10 + 106 + 4} = 0.533V$$

$$i_{ab} = \frac{20}{50} = \frac{2}{5} A = i_{cb}$$

$$i_{cdeb} = \frac{2}{5} \times \frac{60}{60+120} = 0.133A$$

$$i_{eb} = 0.133A$$

$$i(12\Omega) = 0.133 \times \frac{12 \parallel 12}{12 + 12 \parallel 12} = 0.0443A$$

Summer 23

$$(1) \quad i) \quad \text{slope}_{0,1} = \frac{-5}{1} = -5$$

$$\text{slope}_{1,2} = \frac{5}{1} = 5$$

$$\text{slope}_{2,3} = \frac{4}{1} = 4$$

$$\text{slope}_{3,4} = 0$$

$$\text{slope}_{4,5} = 0$$

$$i(2.5) = 4 \text{ A}$$

$$\text{slope}_{5,6} = \frac{-5}{1} = -5$$

$$i(5.5) = -5 \text{ A}$$

$$\text{slope}_{6,7} = 0$$

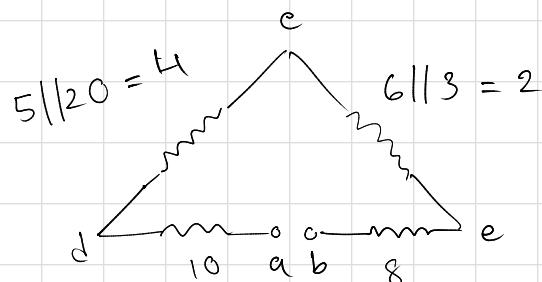
$$i(7) = 0 \text{ A}$$

ii) $P = i^2 R$ therefore P is maximum when i is maximum

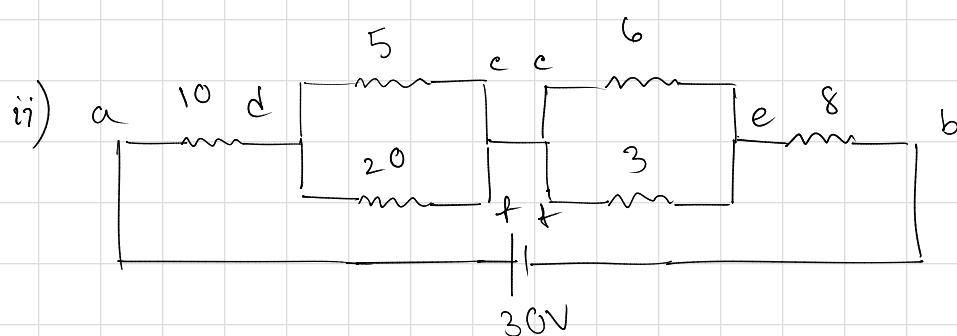
In the graph $i_{\max} = 5 \text{ A}$ from $t = 1 \text{ s}$ to $t = 2 \text{ s}$

$$\therefore P_{\max} = 5^2 \times 20 = 500 \text{ W}$$

$$(2) \quad i) \quad \text{eqv}_{ab} = 24 \text{ V}$$



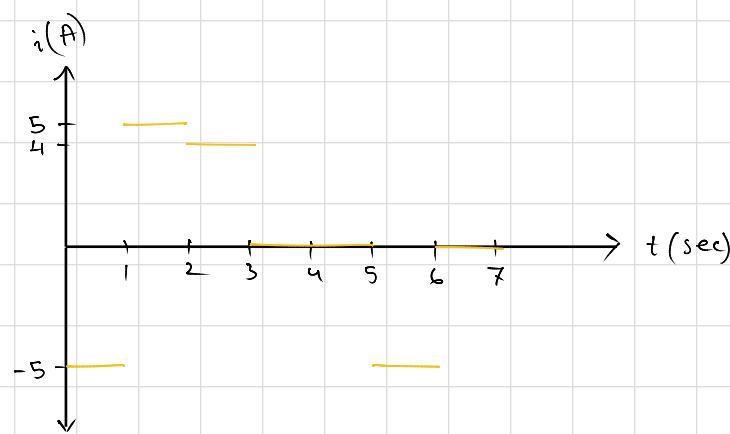
$$4 + 10 + 8 + 2 = 24$$



$$i_{ab} = \frac{30}{24} = 1.25 \text{ A}$$

$$\therefore i_{eb} = 1.25 \text{ A}$$

$$i_{ce} = 1.25 \times \frac{3}{3+6} = 0.4167$$



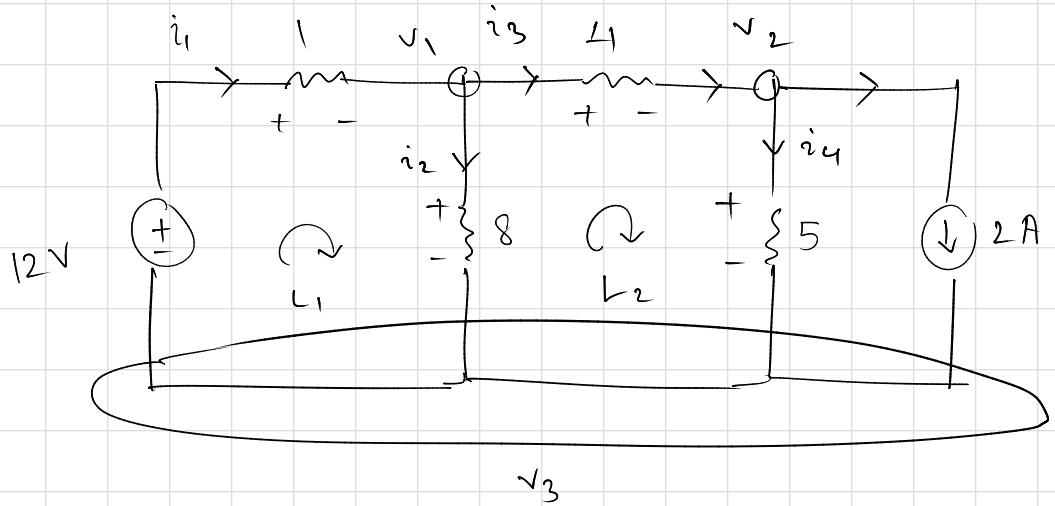
(3)

loop 1

$$i_1 + 8i_2 - 12 = 0$$

$$\Rightarrow i_1 + i_3 + 8i_2 - 12 = 0$$

$$\Rightarrow 9i_2 + i_3 - 12 = 0$$

loop 2

$$4i_3 + 5i_4 - 8i_2 = 0$$

$$\Rightarrow 4i_3 + 5i_3 - 10 - 8i_2 = 0 \quad [i_4 = i_3 - 2]$$

$$\Rightarrow -8i_2 + 9i_3 - 10 = 0$$

$$i_2 = 1.1 \text{ A} \quad i_3 = 2.09 \text{ A}$$

$$i_1 = 1.1 + 2.09 = 3.19 \text{ A}$$

$$i_4 = 2.09 - 2 = 0.09 \text{ A}$$

$$i_1 = \frac{12 - v_1}{1} \Rightarrow v_1 = 12 - 3.19 = 8.81 \text{ V}$$

$$i_2 = \frac{v_1 - v_3}{8} \Rightarrow v_3 = v_1 - 8i_2$$

$$= 8.81 - 8 \times 1.1$$

$$= 0 \text{ V}$$

$$i_3 = \frac{v_1 - v_2}{4} \Rightarrow v_2 = v_1 - 4i_3$$

$$= 8.81 - 4 \times 2.09$$

$$= 0.45 \text{ V}$$

(4)

loop 1:

$$120 + 30i_1 + 10(i_1 - i_3) = 0$$

$$\Rightarrow 120 + 30i_1 + 10(i_1 + 3i_0) = 0$$

$$\Rightarrow 120 + 30i_1 + 10i_1 - 15i_2 = 0$$

$$\Rightarrow 40i_1 - 15i_2 = -120$$

loop 2:

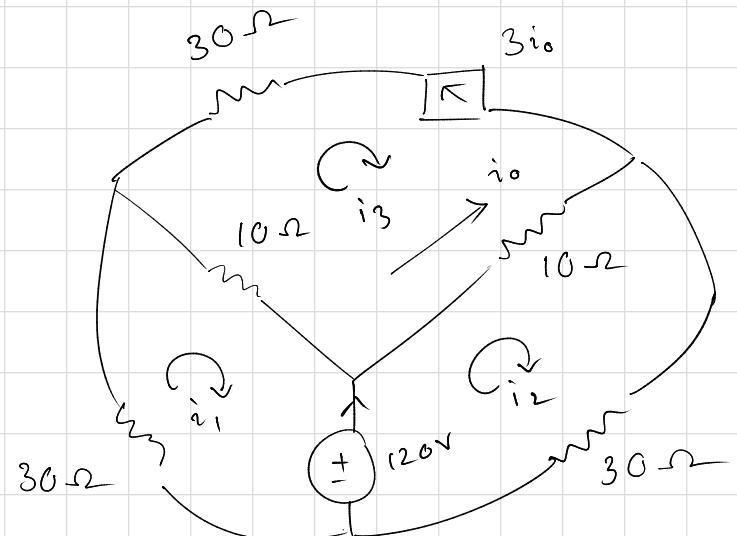
$$-120 + 10(i_2 - i_3) + 30i_2 = 0$$

$$\Rightarrow 10(i_2 + 3i_0) + 30i_2 = 120$$

$$\Rightarrow 10\left(i_2 - \frac{3}{2}i_2\right) + 30i_2 = 120$$

$$\Rightarrow 10i_2 - 15i_2 + 30i_2 = 120$$

$$\Rightarrow i_2 = \frac{120}{25} = 4.8 \text{ A}$$



$$i_0 = i_2 - i_3 = i_2 + 3i_0$$

$$\Rightarrow 2i_0 = -i_2$$

$$\Rightarrow i_0 = -\frac{i_2}{2}$$

$$i_0 = -2.4 \text{ A}$$

current through the battery

$$i_2 - i_1 = 4.8 + 1.2 = 6 \text{ A}$$

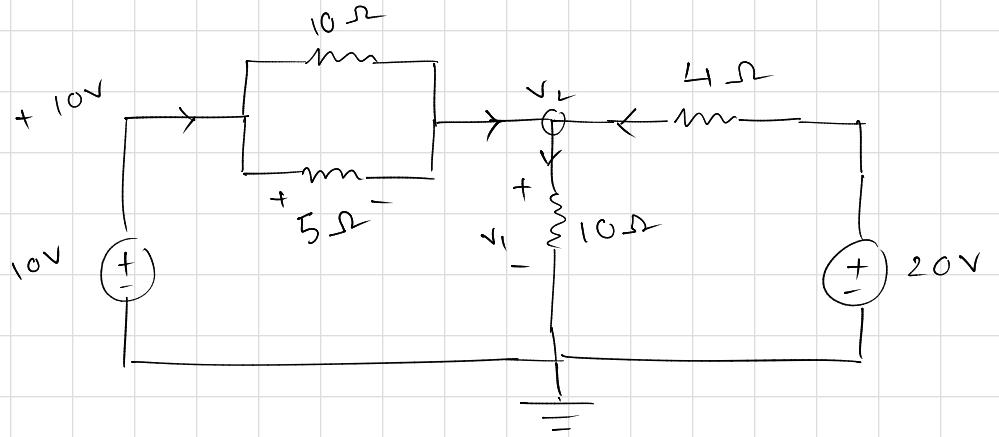
$$\therefore i_1 = \frac{-120 + 15i_2}{40}$$

$$= \frac{-120 + 72}{40}$$

$$= -1.2 \text{ A}$$

(5)

i) at the node with
 v_2 voltage



$$\frac{10 - v_2}{10/15} + \frac{20 - v_2}{4} = \frac{v_2}{10}$$

$$\Rightarrow \frac{3}{10} (10 - v_2) + \frac{20 - v_2}{4} = \frac{v_2}{10}$$

$$\Rightarrow 6(10 - v_2) + 5(20 - v_2) = 2v_2$$

$$\Rightarrow 60 - 6v_2 + 100 - 5v_2 = 2v_2$$

$$\Rightarrow 13v_2 = 160$$

$$\Rightarrow v_2 = 12.308$$

$$v_1 = v_2 - 0 = 12.308 \text{ V}$$

$$\begin{aligned} \text{current in } 5\Omega, i &= \frac{10 - v_2}{5} \\ &= \frac{10 - 12.308}{5} \\ &= -0.46 \text{ A} \end{aligned}$$

ii) current through 4Ω resistor

$$\begin{aligned} i_1 &= \frac{20 - v_2}{4} \\ &= \frac{20 - 12.308}{4} \\ &= 1.923 \text{ A} \end{aligned}$$

therefore 1.923 A current is

$$P = vi = 20 \times 1.923 = 38.46 \text{ W}$$

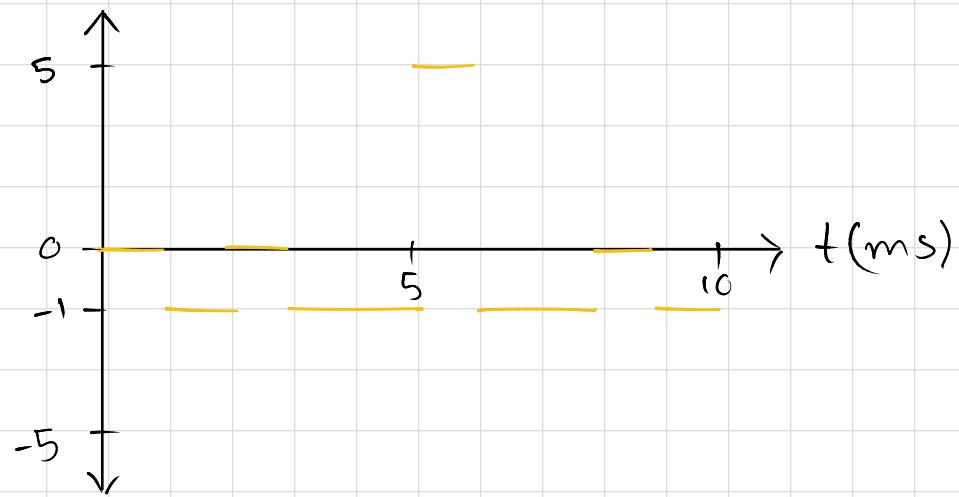
flowing out of the positive

terminal of 20V voltage source,

meaning it is supplying power.

Summer 24

① i) $i(t)$ (A)



$$\text{slope}(0,1) = 0$$

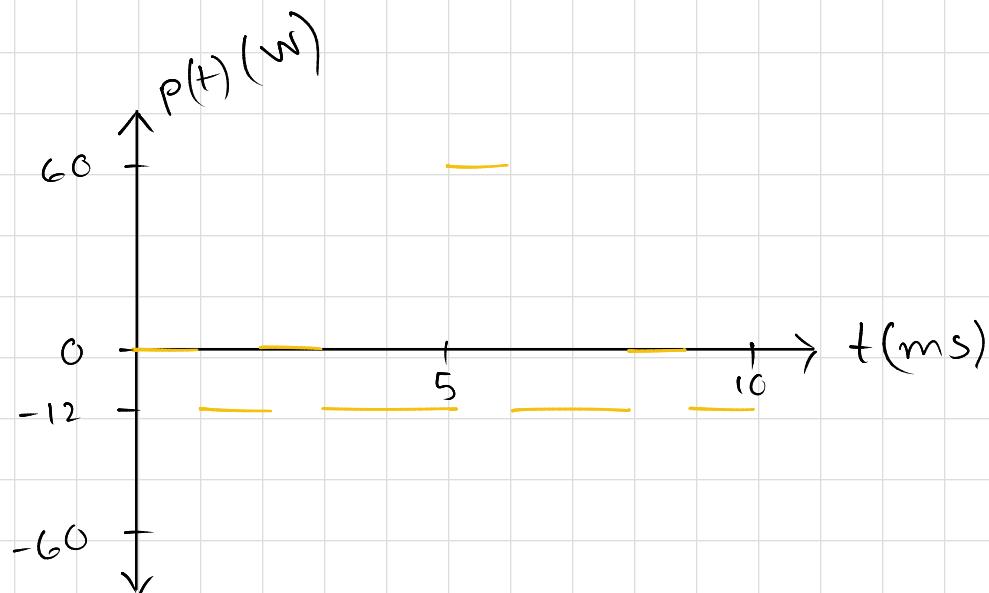
$$\text{slope}(1,2) = \frac{-1}{1} = -1$$

$$\text{slope}(2,3) = 0$$

$$\text{slope}(3,5) = \frac{-2}{2} = -1$$

$$\text{slope}(5,6) = \frac{5}{1} = 5$$

ii) $P = Vi$



$$P(0,1) = 12 \times 0 = 0 \text{ W}$$

$$P(1,2) = 12 \times (-1) = -12 \text{ W}$$

$$P(2,3) = 0$$

$$P(3,5) = 12 \times (-1) = -12 \text{ W}$$

$$P(5,6) = 12 \times (5) = 60 \text{ W}$$

$$P(6,8) = 12 \times (-1) = -12 \text{ W}$$

$$P(8,9) = 0$$

$$P(9,10) = 12 \times (-1) = -12 \text{ W}$$

power is absorbed in the interval $[5,6]$

power is delivered in the following intervals

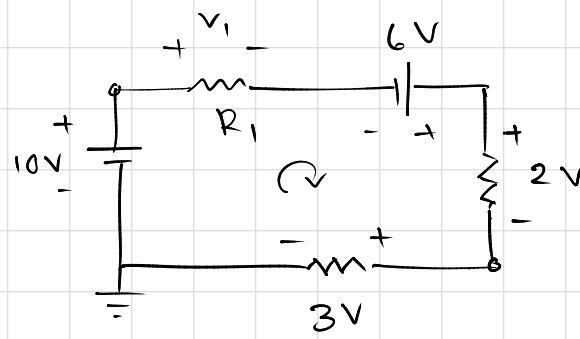
$$[1,2], [3,5], [6,8], [9,10]$$

(2) i) Applying KVL in the loop

$$-10 + v_1 - 6 + 2 + 3 = 0$$

$$\Rightarrow v_1 = 11 \text{ V}$$

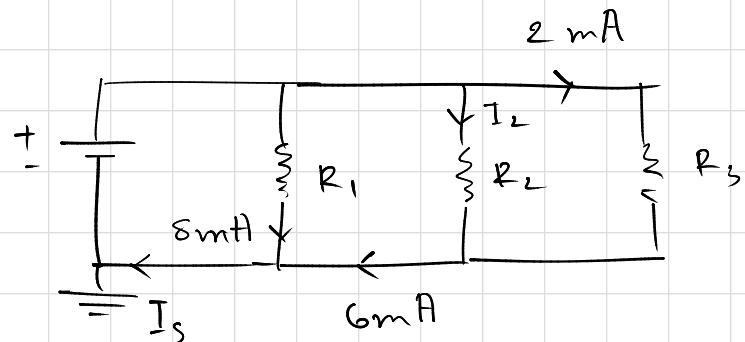
$$\therefore v_2 = v_1 - 6 + 2 = 7 \text{ V}$$



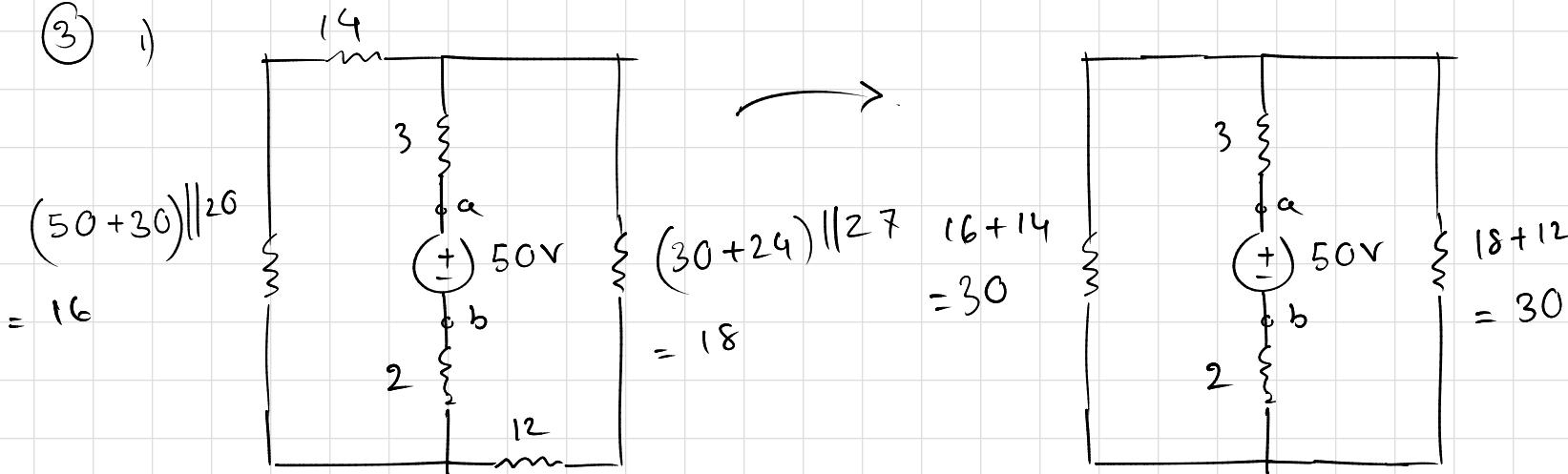
ii) $I_s = 8 + 6 = 14 \text{ mA}$

$$I_s = 8 + I_2 + 2$$

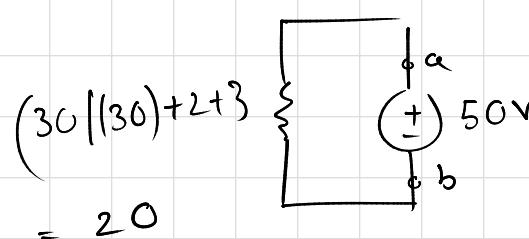
$$\Rightarrow I_2 = 14 - 10 = 4 \text{ mA}$$



(3) i)



$$R_{ab} = 20 \Omega$$



$$= 20$$

$$ii) I = \frac{50}{20} = 2.5 A$$

$$(i_2 + 27 || (30 + 24))$$

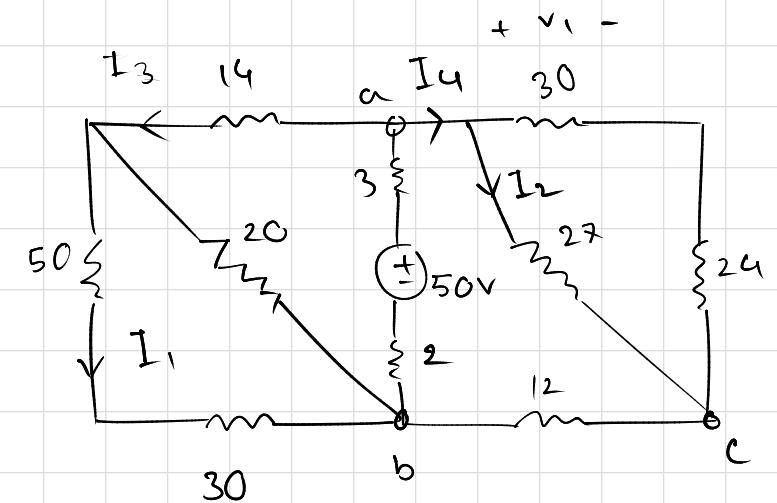
$$I_3 = 2.5 \times \frac{(14 + 20 || (50 + 30)) + (i_2 + 27 || (30 + 24))}{(14 + 20 || (50 + 30)) + (i_2 + 27 || (30 + 24))}$$

$$= 1.25 A$$

$$\therefore I_1 = 1.25 \times \frac{20}{(50 + 30) + 20} = 0.25 A$$

$$I_4 = 2.5 - I_3 = 1.25 A$$

$$I_2 = I_4 \times \frac{30 + 24}{27 + (30 + 24)} = 0.833 A$$



$$V_{ab} = 50 \times \frac{30 || 30}{3 + 2 + (30 || 30)}$$

$$= 37.5 V$$

$$V_{ac} = 37.5 \times \frac{27 || (30 + 24)}{12 + 27 || (30 + 24)}$$

$$= 22.5 V$$

$$V_i = 22.5 \times \frac{30}{30 + 24}$$

$$= 12.5 V$$

(4) i) loop 1:

$$-660 + 5i_1 + 15(i_1 - i_3) + 10(i_1 - i_2) = 0$$

$$\Rightarrow -660 + 5i_1 + 15i_1 - 15i_3 + 10i_1 - 10i_2 = 0$$

$$\Rightarrow 30i_1 - 10i_2 - 15i_3 = 660 \quad \text{--- (1)}$$

loop 2

$$-20i_\phi + 10(i_2 - i_1) + 50(i_2 - i_3) = 0$$

$$\Rightarrow -20(i_2 - i_3) + 10i_2 - 10i_1 + 50i_2 - 50i_3 = 0$$

$$\Rightarrow -10i_1 + 40i_2 - 30i_3 = 0 \quad \text{--- (11)}$$

solving (1), (10) and (11)

$$i_1 = 42 \quad i_2 = 27 \quad i_3 = 22$$

$$\therefore i_\phi = i_2 - i_3 = 5 A$$

loop 3

$$15(i_3 - i_1) + 25i_3 + 50(i_3 - i_2) = 0$$

$$\Rightarrow -15i_1 - 50i_2 + 90i_3 = 0 \quad \text{--- (11)}$$

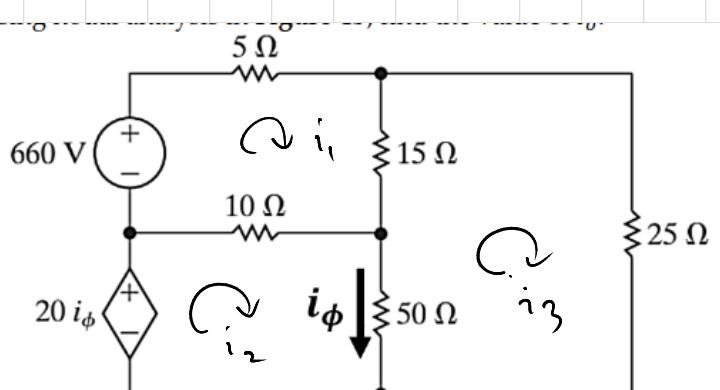


Figure 4a.

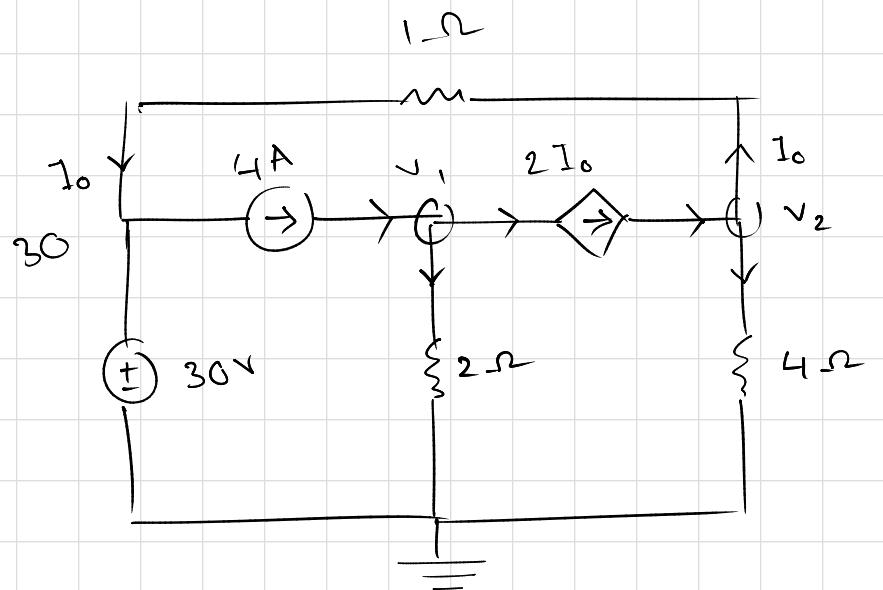
ii) node 1:

$$4 = \frac{v_1}{2} + 2I_o$$

$$\Rightarrow 4 = \frac{v_1}{2} + 2 \left(\frac{v_2 - 30}{1} \right)$$

$$\Rightarrow 4 = \frac{v_1}{2} + 2v_2 - 60$$

$$\Rightarrow \frac{1}{2}v_1 + 2v_2 = 64 \quad \text{--- (1)}$$



node 2:

$$2I_o = I_o + \frac{v_2}{4}$$

$$\therefore I_o = \frac{v_2}{4} = \frac{40}{4} = 10 \text{ A}$$

$$\Rightarrow \frac{v_2}{4} = I_o = \frac{v_2 - 30}{1}$$

$$\Rightarrow v_2 = 4v_2 - 120$$

$$\Rightarrow v_2 = \frac{120}{3} = 40$$

Spring 24

1. i) $i_1 = 5 \quad i_2 = -5$

$$q_1 = 5t + c = 5t + 1$$

$$q_2 = -5t + c = -5t + c = -5t + 21$$

$$q_1(0) = q(0) = 1$$

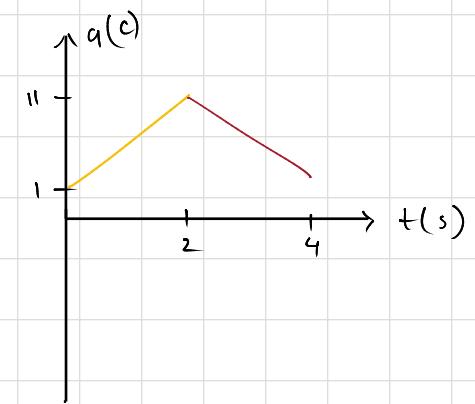
$$q_2(2) = q_1(2) = 5 \cdot 2 + 1 = 11$$

$$\Rightarrow e = 1$$

$$\Rightarrow -5 \cdot 2 + c = 11$$

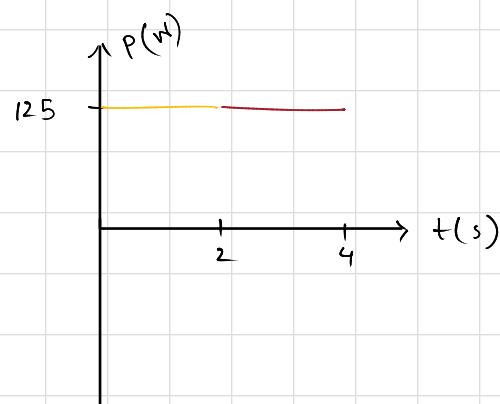
$$\Rightarrow c = 21$$

$$q_2(4) = -20 + 21 = 1$$



ii) $P = i^2 R \quad P_1 = 5^2 \times 5 = 125 \text{ W}$

$$P_2 = (-5)^2 \times 5 = 125 \text{ W}$$



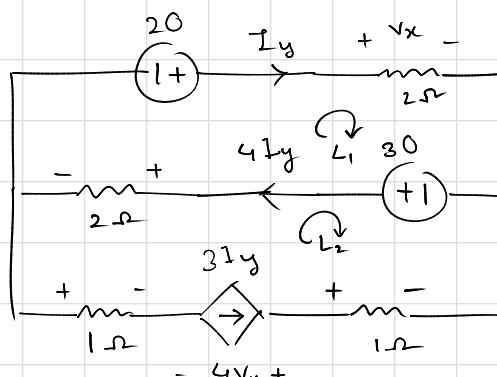
2.

Loop 1

$$-20 + 2I_y - 30 + 2 \cdot 4I_y = 0$$

$$\Rightarrow -20 + 10I_y - 30 = 0$$

$$\Rightarrow I_y = \frac{50}{10} = 5$$



Loop 2:

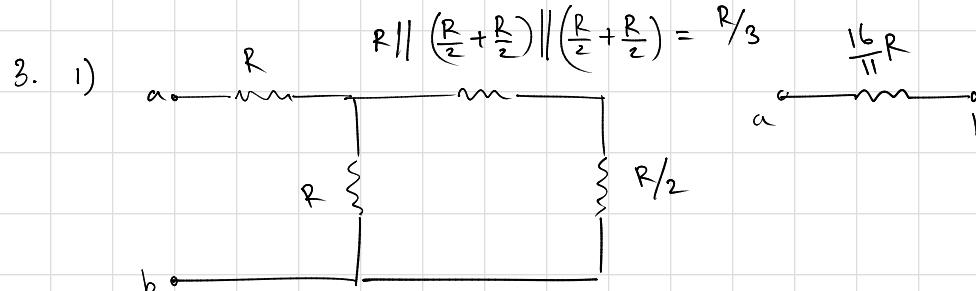
$$-2 \cdot 4I_y + 30 - 3I_y + 4v_x - 3I_y = 0$$

$$\Rightarrow -8I_y + 30 - 3I_y + 4v_x - 3I_y = 0$$

$$\Rightarrow -14I_y + 30 + 4v_x = 0$$

$$\Rightarrow 4v_x = 14 \cdot 5 - 30 = 40$$

$$\Rightarrow v_x = 10$$



$$\begin{aligned} & R + R \parallel \left(\frac{R}{3} + \frac{R}{2} \right) \\ & = R + \left(\frac{1}{\frac{R}{3}} + \frac{1}{\frac{R}{2}} \right)^{-1} \\ & = R + \left(\frac{5+6}{5R} \right)^{-1} \\ & = R + \frac{5R}{11} \\ & = \frac{16}{11} R \end{aligned}$$

$$R_{eq} = 10$$

$$\Rightarrow \frac{16}{11} R = 10$$

$$\Rightarrow R = 6.875 \Omega$$

$$\text{ii) } v_{ac} = 30 \times 5 \parallel 20 \parallel 4$$

$$= 30 \times 2$$

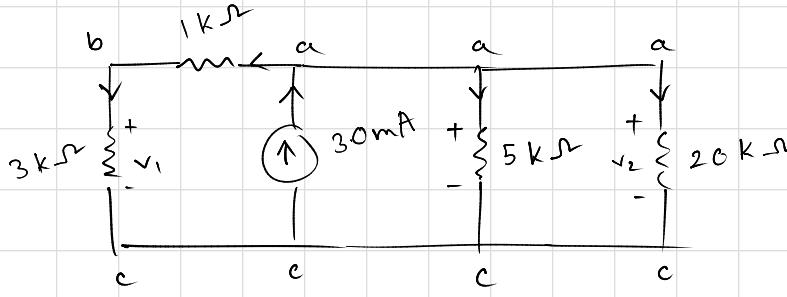
$$= 60 \text{ V}$$

$$v_2 = 60 \text{ V}$$

$$v_{bc} = 60 \times \frac{3}{3+1}$$

$$= 45 \text{ V}$$

$$v_1 = 45 \text{ V}$$



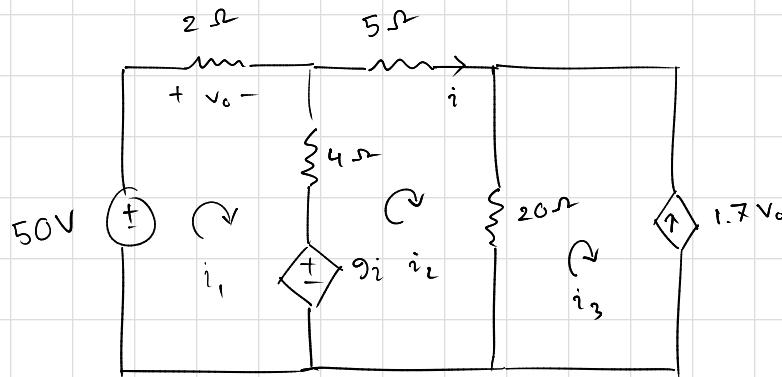
4. i) loop 1

$$-50 + 2i_1 + 4(i_2 - i_1) + 9i_2 = 0$$

$$\Rightarrow 2i_1 + 4i_2 - 4i_1 + 9i_2 - 50 = 0$$

$$\Rightarrow 6i_1 + 5i_2 = 50$$

$$\Rightarrow 3v_o + 5i_2 = 50$$



loop 2

$$-9i_1 + 4(i_2 - i_1) + 5i_2 + 20(i_2 - i_3) = 0$$

$$\Rightarrow -9i_1 + 4i_2 - 4i_1 + 5i_2 + 20i_2 - 20i_3 = 0$$

$$\Rightarrow -4i_1 + 20i_2 - 20i_3 = 0$$

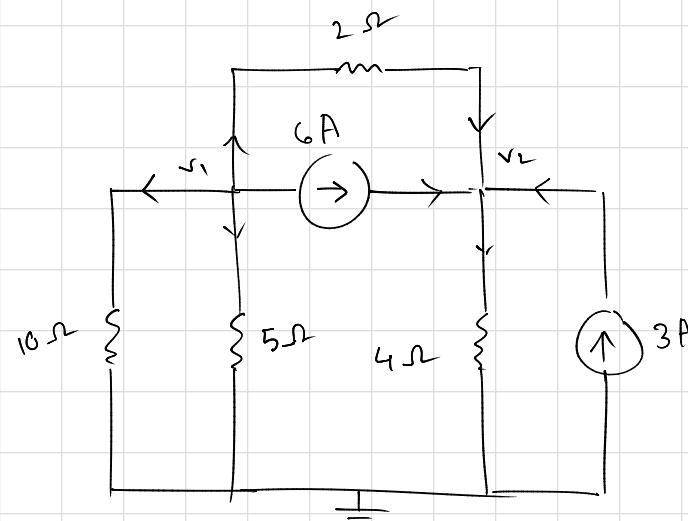
$$\Rightarrow -2v_o + 20i_2 - 20 \times 1.7v_o = 0$$

$$v_o = 4.167 \text{ V} \quad i_2 = 7.5 \text{ A} = i$$

ii) node 1

$$\frac{v_1}{10} + \frac{v_1 - v_2}{2} + 6 + \frac{v_1}{5} = 0$$

$$\Rightarrow \frac{4}{5}v_1 - \frac{1}{2}v_2 + 6 = 0 \quad \textcircled{1}$$



node 2

$$6 + \frac{v_1 - v_2}{2} + 3 = \frac{v_2}{4}$$

$$\Rightarrow \frac{v_1}{2} - \frac{v_2}{2} - \frac{v_2}{4} = -9$$

$$\Rightarrow \frac{1}{2}v_1 - \frac{3}{4}v_2 = -9 \quad \textcircled{11}$$

solve $\textcircled{1}$ and $\textcircled{11}$

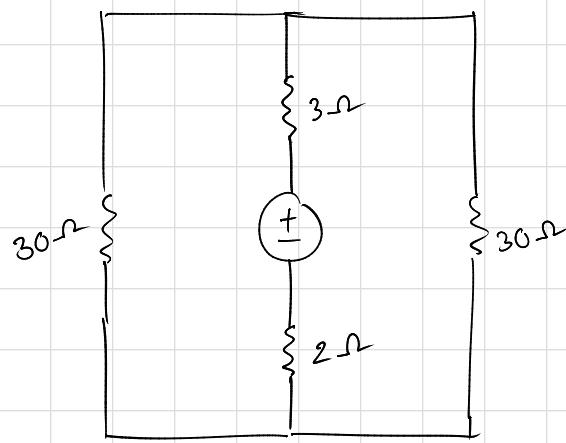
$$v_1 = 0 \quad v_2 = 12$$

Spring 23

1. a)

$$14 + 20 \parallel (50 + 30)$$

$$= 30$$

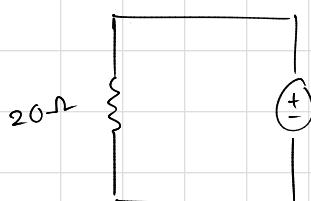


$$12 + 2 \times 1 / (30 + 24)$$

$$= 30 \Omega$$

$$2 + 3 + 30 \parallel 30$$

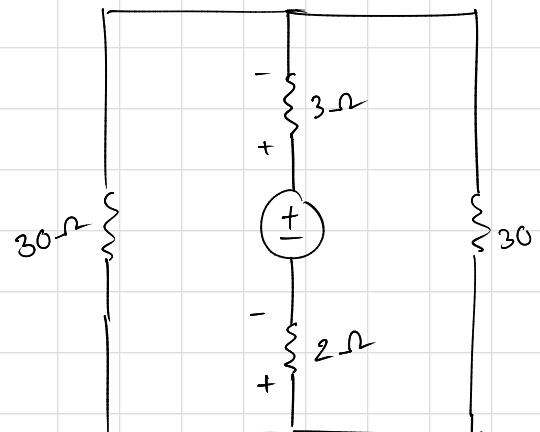
$$= 20$$



$$R_{\text{eq}} = 20 \Omega$$

b) voltage across 3Ω = $10 \times \frac{3}{2+3+30 \parallel 30} = 1.5 \text{ V}$

$\text{u} \quad \text{u} \quad 2 \Omega = 10 \times \frac{2}{2+3+30 \parallel 30} = 1 \text{ V}$

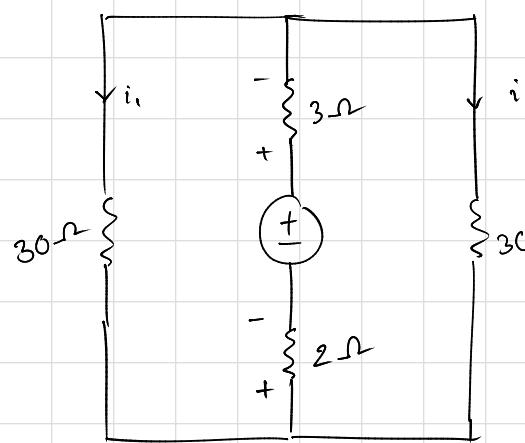


c) current through the whole circuit

$$i = \frac{10}{20} = 0.5 \text{ A}$$

$$i_1 = 0.5 \times \frac{30}{30+30} = 0.25 \text{ A}$$

$$\therefore \text{current through } 12\Omega = 0.25 \text{ A}$$

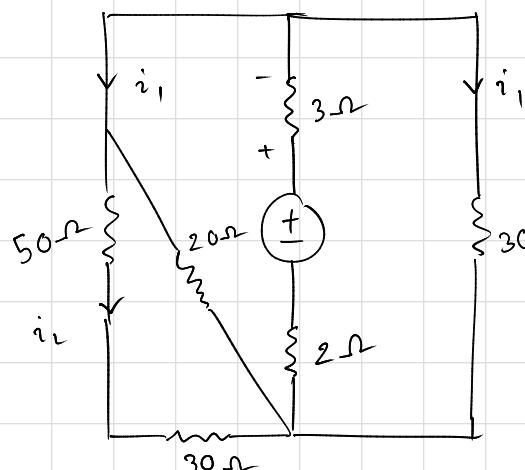


$$i_2 = i_1 \times \frac{20}{20 + (50 + 30)}$$

$$= 0.25 \times 0.2$$

$$= 0.05 \text{ A}$$

$$\therefore \text{current through } 50\Omega = 0.05 \text{ A}$$



2. a) $q_1 = 20t \quad \{0 \leq t \leq 1\}$
 $q_2 = 20 \quad \{1 \leq t < 3\}$

$$q_3 = -\frac{40}{2}t + c = -20t + c = -20t + 80 \quad \{3 \leq t \leq 5\}$$

$$q_3(3) = q_2(3)$$

$$\Rightarrow -60 + c = 20$$

$$\Rightarrow c = 80$$

$$q_4 = \frac{40}{2}t + c = 20t + c = 20t - 120 \quad \{5 \leq t \leq 7\}$$

$$q_4(5) = q_3(5)$$

$$\Rightarrow 100 + c = -20$$

$$\Rightarrow c = -120$$

$$q_5 = 20 \quad \{7 \leq t\}$$

$$i_1 = 20$$

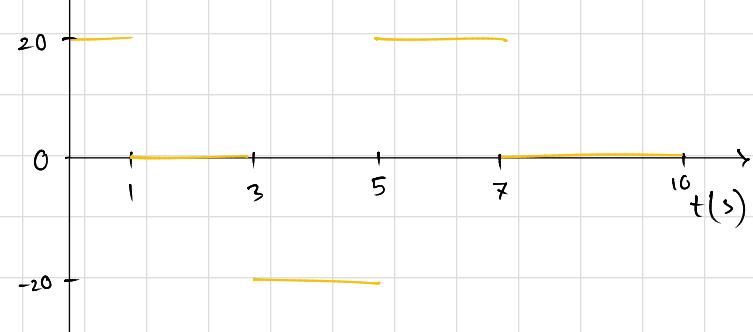
$$i_2 = 0$$

$$i_3 = -20$$

$$i_4 = 20$$

$$i_5 = 0$$

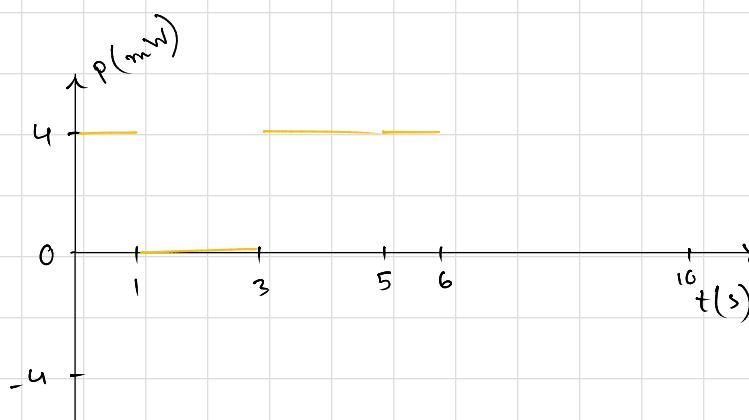
i (mA)



b) $P = i^2 R$

for $0 \leq t \leq 1$

$$P = 20^2 \times 10 = 4 \text{ mW}$$



for $1 \leq t \leq 3$

$$P = 0^2 \times 10 = 0$$

total energy delivered from 0 to 6 sec

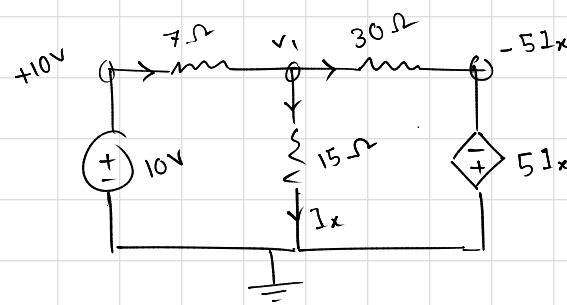
for $3 \leq t \leq 5$

$$P = (-20)^2 \times 10 = 4 \text{ mW}$$

$$E = 4 \times 1 + 0 + 4 \times 3 \\ = 16 \text{ mJ}$$

for $5 \leq t \leq 6$

$$P = 20^2 \times 10 = 4 \text{ mW}$$



3. a) node v_1 :

$$\frac{10 - v_1}{7} = \frac{v_1 + 5I_x}{30} + \frac{v_1}{15}$$

$$\Rightarrow \frac{10 - v_1}{7} = \frac{v_1 + \frac{v_1}{3}}{30} + \frac{v_1}{15} \quad [I_x = \frac{v_1}{15}]$$

$$\Rightarrow v_1 = 5.625 \text{ V} \quad \therefore I_x = 0.375 \text{ A}$$

$$\text{current through } 7\Omega = \frac{10 - v_1}{7} = 0.625 \text{ A}$$

$$\text{current through } 30\Omega = \frac{v_1 + 5I_x}{30} = 0.25 \text{ A}$$

$$\text{and } 15\Omega = I_x = 0.375 \text{ A}$$

$$\text{current through } 10\text{V} = 0.625 \text{ A}$$

$$\text{and } 5\Omega = 0.25 \text{ A}$$

b) power supplied by $10V = 10 \times 0.625 = 6.25 W$

power absorbed by $7\Omega = 7 \times 0.625^2 = 2.734 W$

power absorbed by $15\Omega = 0.375^2 \times 15 = 2.109 W$

power absorbed by $30\Omega = 0.25^2 \times 30 = 1.875 W$

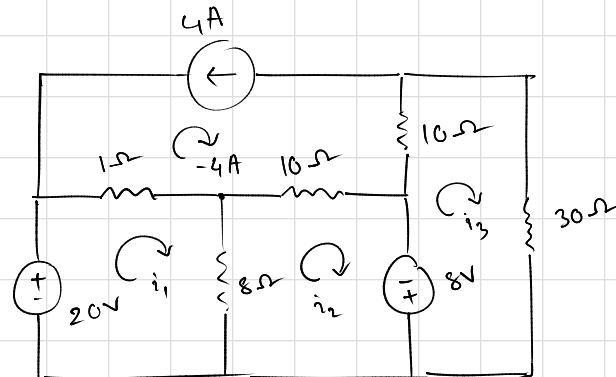
power supplied by $5A = 5 \times 0.375 \times 0.25 = 0.469 W$

4. a) loop 1:

$$1(i_1 + 4) + 8(i_1 - i_2) - 20 = 0$$

$$\Rightarrow i_1 + 4 + 8i_1 - 8i_2 - 20 = 0$$

$$\Rightarrow 9i_1 - 8i_2 = 16$$



loop 2:

$$8(i_2 - i_1) + 10(i_2 + 4) - 8 = 0$$

$$\Rightarrow 8i_2 - 8i_1 + 10i_2 + 40 - 8 = 0$$

$$\Rightarrow -8i_1 + 18i_2 = -32$$

$$\text{b) } P = i^2 R = (i_1 + 4)^2 \times 1 \\ = 18.714 W$$

loop 3:

$$10(i_3 + 4) + 30i_3 + 8 = 0$$

$$\Rightarrow 10i_3 + 40 + 30i_3 + 8 = 0$$

$$\Rightarrow 40i_3 = -48$$

$$\Rightarrow i_3 = -1.2$$

$$i_1 = 0.326 A$$

$$i_2 = -1.63 A$$

$$i_3 = -1.2 A$$

5. a) node v_1

$$3.7v_o + \frac{9i_o - v_1}{15} = 1_o$$

$$\Rightarrow 3.7(v_2 - 94) + \frac{1}{15}(9 \frac{v_1 - v_2}{11} - v_1) = \frac{v_1 - v_2}{11}$$

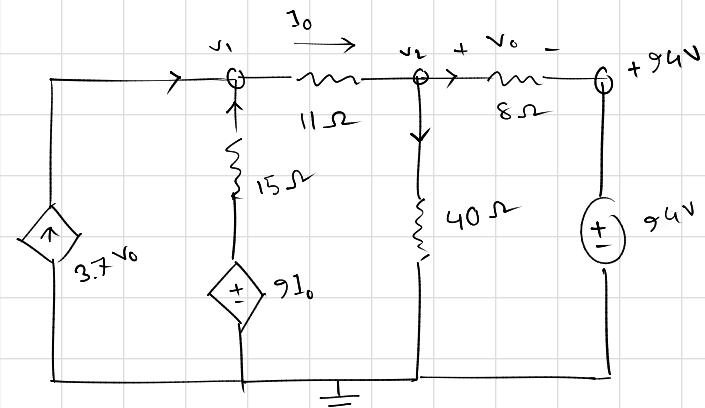
$$\Rightarrow 3.7v_2 - 347.8 + \frac{1}{15} \left(\frac{9}{11}v_1 - \frac{9}{11}v_2 - v_1 \right)$$

$$= \frac{1}{11}v_1 - \frac{1}{11}v_2$$

$$\Rightarrow 3.7v_2 - 347.8 + \frac{3}{55}v_1 - \frac{3}{55}v_2 - \frac{1}{15}v_1 = \frac{1}{11}v_1 - \frac{1}{11}v_2$$

$$\Rightarrow \left(\frac{3}{55} - \frac{1}{15} - \frac{1}{11} \right) v_1 + \left(3.7 - \frac{3}{55} + \frac{1}{11} \right) v_2 = 347.8$$

$$\Rightarrow -\frac{17}{165}v_1 + \frac{411}{110}v_2 = 347.8 \quad \text{--- (1)}$$



node v₁:

$$\frac{v_1 - v_2}{11} = \frac{v_2 - 94}{11} + \frac{v_2}{40}$$

$$\Rightarrow \frac{1}{11}v_1 - \frac{1}{11}v_2 = \frac{1}{11}v_2 - \frac{94}{11} + \frac{v_2}{40}$$

$$\Rightarrow \frac{1}{11}v_1 + \left(-\frac{1}{11} - \frac{1}{11} - \frac{1}{40}\right)v_2 = -\frac{94}{11} \quad \text{--- (i)}$$

$$\Rightarrow \frac{1}{11}v_1 - \frac{91}{440}v_2 = -\frac{94}{11}$$

solve (i) and (ii)

$$v_1 = 125.65$$

$$v_2 = 96.55$$

b) $v_o = v_2 - 94 = 2.55 \text{ V}$

$$I_o = \frac{v_1 - v_2}{11} = 2.65 \text{ A}$$