multiVitamin

User Manual

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1 multiVitamin

multiVitamin is a software package which allows users to perform multiple alignments with graphs. There are two algorithms available for this task. The Bron Kerbosch (BK) [] and the algorithm originally published by Cordella et al. (VF2) []. Details on the algorithms can be found in the theory section.

The main function of the package is to align two or more graphs following a binary alignment guide tree containing the "best" alignment procedure. The resulting multiple graph alignment is represented as one single graph itself. Next to this main function, there is also the possibility to show all co-optimals of an alignment between 2 graphs or to view graphical representations of graphs. Sounds exciting, so let's get started!

2 Installation

Clone the repo from github to [yourDir] with

```
$ git clone https://github.com/mk36fyvy/multivitamin.git
Navigate to the directory containing the setup.py file
$ cd [yourDir]/multivitamin/multivitamin
and type
$ pip3 install -e .
```

Done, now you can run **multiVitamin** in the command shell. You can test if the installation was successful by typing

```
$ multiVitamin -h
```

3 Graph Format

A good first step is to familiarize yourself with the graph format. A graph file is basically a text file, we use the extension '.graph'. It is also used interiorly to identify graph files as such.

The file itself is structured as follows (see below for an example):

Every graph consists of nodes and edges. Every node has an id, which is a unique integer (handled as a String internally) for each node. Optionally, nodes can be labelled. The id and label are separated by a semicolon (;) in the '.graph'-file. The edges are two connected nodes and represented by the ids of the two nodes separated by a semicolon.

Now, let's walk through the overall structure of the '.graph'-file:

- There is a possibility to insert comment lines by preceding comments with // or writing ;comment after the comment. These lines will be ignored by the parser. They can be written anywhere in the first paragraph.
- The first line indicates the author of the graph. This line has to start with the word "author" to be recognized by the parser.
- The second and third lines show the number of nodes and edges respectively. The parser only sees two consecutive integers at the end of the lines, so it is important that the number of nodes is provided before the number of edges.

- The next three lines are booleans that indicate whether the nodes / edges are labelled and if the graph is directed. It is important to stick to the order indicated in the example below.
- The blank line indicates the start of the node section. It is important to choose an integer as node id. The label can contain any symbol, except for ;.
- The node section is separated from the edge section again by a blank line. If the Directed graph option is set to False, the edges are considered undirected. Internally, every edge's reverse is then added to the graph.

Let's look at a small example graph for illustration. The graph has 6 nodes which are all labelled with a 'c' and 6 edges which are not labelled. Your graphs need to have exactly this format to use this package. Especially the blank lines are important. You can find a decent number of further examples at multivitamin/graph_examples. Now that you are familiar with the graph format, we can take a look at how to use the package.

```
//this is a sample graph
AUTHOR: Michel K.
#nodes;6
#edges;6
Nodes labelled; True
Edges labelled; False
Directed graph; False
1;c
2;c
3;c
4;c
5;c
6;c
1;2
1;6
2;3
3;4
4;5
5;6
```

4 Multiple graph alignment

4.1 Graph alignment with BK algorithm

Consider the basic use without any optional flags for the start. You do not have to be in the directory of the package to use multiVitamin. To get an overview of all the flags you can type

```
$ multiVitamin -h
```

If you are experienced with command-line tools the information provided by this command might be sufficient to get you started.

```
usage: multiVitamin [ -h | -m | -c | -v | -d ] [-a] [-s] [-t] [-g]
for example: multiVitamin -ga VF2 -m g1.graph g2.graph g3.graph
multiVitamin - A multiple alignment tool for graphs
Required arguments (These arguments are mutually exclusive):
-h, --help
                            show this help message and exit
-m, --multiple <files...>
                            provide .graph files for multiple alignment '.'
                              takes all .graph files in the directory as
                              arguments
-c, --coopt <files...>
                            provide 2 graphs which will be aligned.
                              Co-optimals will be saved in ./results
-v, --view <files...>
                            get a visual representation of the given graphs
                              in one window. This can get confusing for
                              large or many graphs. Use -d if you want to
                             see one window per graph.
-d, --disp-mult <files...> get a visual representation of the given graphs
                             in one window per graph.
Optional arguments:
-a, --algorithm <BK|VF2>
                            indicate an alignment-algorithm (default: BK)
                              Warning: VF2 is only suited if there is true
                              graph-subgraph isomorphism!
-s, --save-all
                            save all the graphs produced during the
                              alignment. The graphs are saved as
                              "[newick].graph"
-t, --save-shorter
                            save an additional version of the alignment
                              graph with much shorter node ids
-g, --save-guide
                            save the guide tree in Newick-format as
                              "newick.txt"
```

There are three main functions resulting in four mutually exclusive flags. One of them is always required to make multiVitamin work. For starters, we look at the case of a multiple alignment of graphs, which is considered the standard use case.

Just type:

```
$ mulitVitamin -m <pathToGraphFile1.graph> <pathToGraphFile2.graph> ...
```

This aligns the given graphs with the default algorithm, which is BK. The resulting terminal output provides all the important information about the alignment. An example output can be

found below.

In order to assure the uniqueness of node's IDs in a multiple alignment, every node owns a mult_id attribute, which comes into play here. First, every graph gets a unique abbreviation string. It is built from the first two letters of the graph file name and an index, which is incremented each time, a two letter combination is already taken for the specific multiple alignment.

In the example, graphs 1 and 2 are called gr1 and gr2 respectively. This abbreviation is used to build the unique node mult_ids.

Let's look at the first line depicting a node in the nodes section:

```
gr1:4.gr2:2 'd' ( gr1:1.gr2:5, gr1:2.gr2:3, gr1:5.gr2:4 )
```

The node gr1:4.gr2:2 originates from the alignment of node 4 from graph1 and node 2 from graph2. Note that there is a ':' between the graph and the corresponding original node ID and a '.' between the nodes of different graphs.

As indicated in the terminal output, what follows written between '' is the label of the node. The label handling during alignment with BK algorithm is specified in

```
[yourDir]/]multivitamin/multivitamin/utils/modular_product.py
```

At the moment, if any semantic label checks are needed, you should use the VF2 algorithm. See below for more information.

The neighbours of the node are indicated in parentheses, again indicated by the notation explained above.

The edges section shows the edges as follows: node1 and node2 are indicated by their mult_id followed by their label.

The last section indicates the alignment guide tree in conventional Newick format.

Naturally, apart from the terminal output, multiVitamin saves the results from the alignment in actual files as well. Every generated file will be saved in the ./results folder, with '.' being your current working directory. If the folder is already present, multiVitamin simply adds the files, if not, it creates the directory automatically.

Files that will be created after successful multiple alignment:

graph_abbreviations.txt easily parseable text file which indicates the full name and abbreviation couples of the graphs used in the alignment

<g1-g2-...>.graph the graph resulting from the alignment (in .graph-format). The file contains a comment line indicating the guide tree by which it was obtained

More files can be created by using optional flags. These are summarized below.

4.2 TODOGraph alignment with VF2 algorithm

Let us still consider the basic use case with the required flag -m. This flag can be combined with all optional flags (see section advanced use). One of those optional flags is -a which specifies the algorithm that will be used for the alignment.

In order to use the VF2 algorithm for the alignment you have to use the flag -a with "vf2" as parameter in addition to the specification of the input files. So the command would be "mulitVitamin" and the command would be also well as the command would be "mulitvitamin" and the command would be a command would be "mulitvitamin" and the command would be also well as the command would be a command would

```
RESULTS
---GRAPH ABBREVIATIONS -----
gr1
       >>
              graph1
       >>
              graph2
gr2
---ALIGNMENT -----
*NODES (ID, LABEL, NEIGHBOURS)
gr1:4.gr2:2
           'd'
                 ( gr1:1.gr2:5, gr1:2.gr2:3, gr1:5.gr2:4 )
            'a '
gr1:1.gr2:5
                  ( gr1:2.gr2:3, gr1:5.gr2:4, gr1:4.gr2:2, gr1:3.gr2:6 )
            'b' (gr1:1.gr2:5, gr1:5.gr2:4, gr1:4.gr2:2, gr1:3.gr2:6)
'c' (gr1:1.gr2:5, gr1:2.gr2:3)
gr1:2.gr2:3
gr1:3.gr2:6
gr1:5.gr2:4 'e' (gr1:1.gr2:5, gr1:2.gr2:3, gr1:4.gr2:2)
*EDGES (ID, LABEL)
( gr1:2.gr2:3, gr1:3.gr2:6 )
( gr1:4.gr2:2, gr1:2.gr2:3 )
( gr1:1.gr2:5, gr1:3.gr2:6 )
( gr1:1.gr2:5, gr1:2.gr2:3 )
( gr1:4.gr2:2, gr1:1.gr2:5 )
                              , ,
( gr1:4.gr2:2, gr1:5.gr2:4 )
                              , ,
( gr1:1.gr2:5, gr1:5.gr2:4 )
( gr1:2.gr2:3, gr1:5.gr2:4 )
---NEWICK TREE-----
(graph1,graph2)
**********************
Successfully created the directory /home/micheltower/Documents/
   multivitamin_project/multivitamin/graph_examples/other/results
All files will be saved here.
Saved graph as gr1-gr2.graph
Saved graph id abbreviations as graph\_abbreviations.txt
```

-m ¡pathToGraphFile1.graph¿ ¡pathToGraphFile2¿ ¡optionalMoreGraphFiles¿" -a vf2" This option is only suited for subgraph graph isomorphisms. So the smaller graph must always fit entirely in the bigger graph. Despite this restriction the Vf2 is able to align graphs based on the label of the node ids. So a structural isomorphism is not enough in this case, but the nodes that could aligned structurally must also fulfill some kind of semantic condition. This is usefull to align chemical molecules that are represented as graphs. This condition can be determined by the user in the custom.py

4.2.1 Custom.py

The custom.py file can be found in the multivitamin directory of the root folder. This file contains a function the check_semantics function, which by default returns always true. The code of the custom.py file looks as follows:

```
def check_semantics( n, m ):
    '', This function is used in VF2 algorithm to decide,
    whether aligning to nodes is allowed from the
    label point of view.
    In the sample example below, two nodes will only
    be accepted as a legal matching, if the two
    labels are exactly the same.
    Insert your scoring logic below: '''
     if n.label == m.label:
         return True
     else:
         return False
    return True
def get_results_dir():
    ''', define, where the result files will be saved.
    Default is a dir named 'results' in the current
    working directory''
    return "/results"
```

If you untoggle the single comments and out-comment the return True, you get a simple semantic check that only allows nodes to be aligned that have the same label. However you can go as crazy as you want with it.

Besides the check_semantics method you can also specify the path where your results should be saved. Just specify your prefered path as a string as return value from get_results_dir(). Before we jump into the supplemtary clasees, which you might want to modify for a highly sophisticated check_semantics function, we want to take a look at the other flag options. Note: A change in the supplemtary classes is not recommended.

4.3 Optional flags

Apart from the flag -a which allows to specify the algorithm used for the alignment, there are some more optional flags, which can be used to let multiVitamin save a couple more useful files at the end of the alignment. All of these files will be saved in the results/ directory mentioned above. Files that can optionally be created by using flags:

- -s Saves all intermediate graphs that were produced along the alignment guide tree. Normally you would only get the final alignment graph out of the alignment. However, in some cases, it might be useful to get all the graphs produced in the alignment.
- -t Saves a version of the alignment graph with much shorter node ids. Even though this makes it impossible to get information about which nodes originated from which ones in the original graphs, it might be a good idea to use this graph for further alignment to assure, that the node IDs stay readable and unique.
- -g Saves the alignment guide tree in an easily parseable way as 'newick.txt'

5 TODOAdditional features

To make multiVitamin work you need one (exactly one) of the following flags: -m, -c, -v.

The -m option has been discussed in depth in the previous sections. It can be used with every optional flag.

The -v flag allows for graphical representation of our .graph files. You need to proved a graph file. In most cases this will be the graph of the mulitple alignent. Use: "multiVitamin -v ;file.graph;" It is not compatible with any of the optional flags.

The -c flag works only for exactely two input files. It gives all the co-optimal alignments of the two given graphs. There exist cases where two graphs have more can be aligned in different, yet optimal ways. The -c flag calculates all these cases. Since -c only works with 2 graphs the Optional flags are not helpful. Only the -a flag could be used to use the vf2 algorithm. Note lead to high computation costs. Let us consider the optional flags now. If you want to save the guide tree in an extra file use -g. If you not only want the final multiple alignment graph, but also all alignments in between use -s. If you have three graphs for example graph1, graph2 and graph3. Let us assume multiVitamin gives us a graph which multiple alignment is represented by this Newick tree: ((graph1,graph2),graph3). Now you with the option -s you will also get the alignment of graph1 and graph2 as a graph file.

5.1 TODOGetting alignment co-optimals

5.2 TODOViewing graphs

6 TODOBasic Classes

In order to implement the Bron Kerbosch and Vf2 algorithm, we used three classes. A graph class, a node class and a edge class. In general the classes should not be altered by the user. However for the sophisticated user there may be cases in which he or she wants to make adjustments to this classes. Therefore we will given a brief overview of them. Figure 2 shows simple UML diagrams of our base classes. The most important methods and attributes will be explained.

6.1 TODONode class

Our node objects are seen in the context of a graph. Thus every node contains information about its neighbours. Therefore a node has a neighbours attribute which is a set of Node objects. In case of directed graphs one can distingush between in and out neighbours. Thus a node object has a seperate set for these two kind of neighbours. This is useful in the Vf2 algorithmn. The mult_id attribute gives an option to name the node in a mulitple alignment.

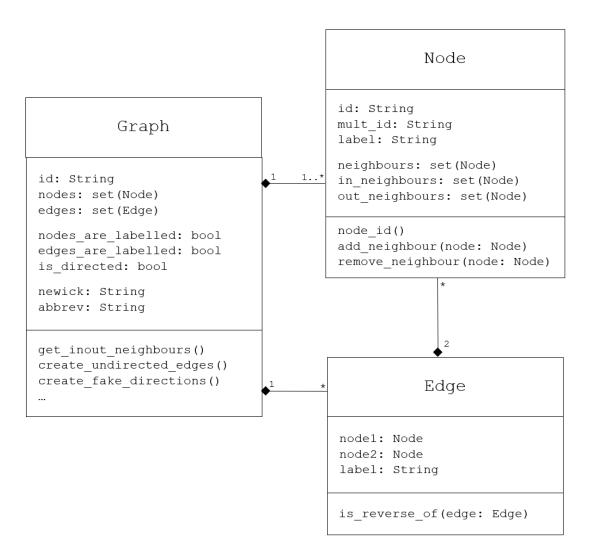


Fig. 1: A UML class diagram of the base classes

6.2 TODOEdge class

An Edge consists of two node objects and an optional label. For each Edge can be checked if it is the reverse of another edge. This only makes sense for directed graphs.

6.3 TODOGraph class

Besides the obvious attributes of nodes, edges and an id, a graph objects also as an abbrev which is TODO. Since the Vf2 only works with directed graphs, we gave our graphs the possibility to give the graph directions. Consider the Edge A-B. The create_fake_directions method now points node A to B and node B to A.

The method create_undirected_edges fills the edge set of the Graph with help of the neighbour set of the node class. The method get_inout_neighbours fills the in and outneighbour sets of the node objects in the node set.

All classes have build in print mehtods for more readable output as well as build in methods to compare the objects. So you can determine which graph is larger by the amount of nodes in the nodes sets and also determine if two graphs are equal based on their id.

Nodes can be also compared by its id and edges by the ids of their nodes.

7 TODOTheoretical background of the algorithms

7.1 TODOBron Kerbosch algorithm

The Bron Kerbosch algorithm solves the problem of finding a maximal common induced subgraphs of two graphs G and H indirectly. This is done by finding the maximal clique in the modular product of G and H s. The set of nodes of the modular product of G and H is the cartesian $N(G) \times N(H)$, with N beeing the set of al vertices of the corresponding graph. Any nodes (u,v) and (x,y), with $u,x \in G$ and $v,y \in H$ in the modular product are adjacent if:

- u and x were neighbours in G and y and x were neighbours in H
- u and x were not neighbours in G and y and x were not neighbours in H

Before giving two graphs to the Bron Kerbosch to align them we need to build the modular product of these graphs. The rest of our implementation is straight forward:

```
def bk_pivot ( self, r, p, x ):
    if not any ( [p, x] ):
        self.results.append(r)
        return r
    pivot = self.find_max_pivot( p, x )
    for v in p[:]:
        if v in pivot.neighbours:
            continue
        r_ = r | {v}
        x_ = x & v.neighbours
        p_ = [n for n in v.neighbours if n in p ]
        self.bk_pivot ( r_, p_, x_ )
        p.remove(v)
        x.add(v)
```

The goal of the Bron Kerbosch, is as mentioned, to find the maximal clique in the modular product. A clique is a subgraph where every node is connected to every other node (=complete graph). A maximal clique is a clique so that no node can added to the subgraph such that the subgraph remains complete.

The data structures are a list p, which is the list of candidates that could extend a clique, and the sets r and x. r contains all the nodes in a maximal clique and x is a set for blacklisting nodes. Blacklisting is useed to not finde the same cliques over and over again, Thus x and p are only empty when a new clique is found.

Let us consider the case without pivoting first. A short note to the pivoting: The pivoting is solely a performance optimization. It makes the recursion tree first deep and computes the widness latet. There are several ways to chose a pivot, it can be chosen rando or as we did by maximizing the intersection of the neighbours of the currently relecant node v and the union of p and x.

7.1.1 BK in multiple Alignment context

The BK only finds cliques in the modular product of two graphs. In a multiple alignment setting however we would like to get a graph. So we can align the graph further. To get a graph which one can work with out of the clique we need to modify the found clique. Since the nodes in the clique are already correct we only need to delete some edges. We allow only these edges that are in the clique as well as in one of the original input graphs.

7.2 TODOVF2 algorithm

In order to align multiple graphs we used a greedy algorithm to find the best alignments. Therefore we calculated every possible pairwise alignment of n input graphs and scored these alignment. The scoring was made as follows:

For the BK the more nodes the clique contained, the better was an alignment. In the case of the VF2, we looked at the number of nodes in the small core. The higher the number the better the alignment. Once we found the best pairwise alignemtn, we repeated this process with by aligning the best pairwise alignment with all remainin n-2 (all input graphs without the two graph that we just aligned) graphs

8 TODOProfiling

To get an idea which algorithm is better sutied for which kind of graph (size, structure), we did a profiling study. Therefore we used three different kind of graphs: random graphs, wheel graphs and tree graphs. The graphs where generate with the help of the python package networkx []. We did the profiling for the following number of nodes: (3,8,13,18,23,XX TODO). In case of the random graphs we created 10 different random graphs for each node count and took the average time per node count. The following figures show the results of our profiling study.