

Monte Carlo Search Tree and Its Applications

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Kasparov vs Deep Blue



Kasparov vs Deep Blue

Great display of artificial intelligence

Techniques employed by IBM

- ▶ Brute force deterministic approach
- ▶ human knowledge

Limitation

- ▶ scalability into larger search spaces

Monte Carlo tree search (MCTS) is an alternative method

Outline

Introduction

Naive MCTS Implementation

Applying MCTS to Go

Monte Carlo Tree Search (MCTS)

- ▶ Combines random sampling and game trees
- ▶ Probabilistic not deterministic
- ▶ Useful for problems with larger search spaces

Two MCTS Applications

Go

- ▶ Board game about positional advantage
- ▶ Game board for Chess: 8x8
- ▶ Possible games of Chess: 10^{120}
- ▶ Game board for Go: 19x19
- ▶ Possible games of Go: 10^{761}

Narrative generation

- ▶ Useful Applications
 - ▶ Video game replay value
 - ▶ educational applications
- ▶ The search space scales with the number of characters, items, locations, and actions

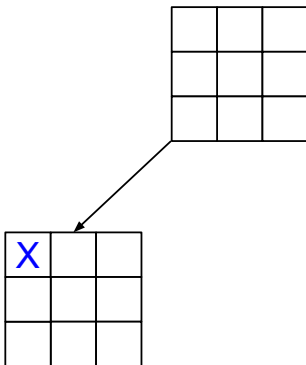
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Introduction

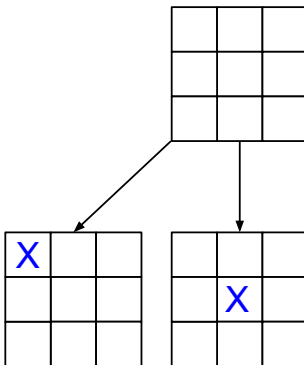
Naive MCTS Implementation

Applying MCTS to Go

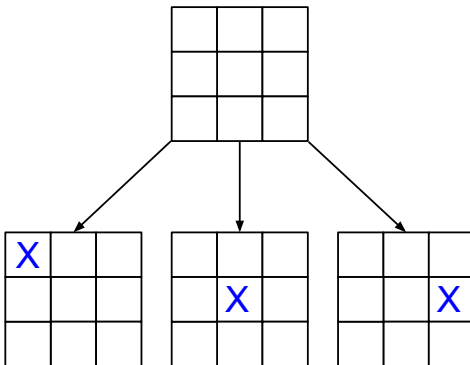
TicTacToe Diagram



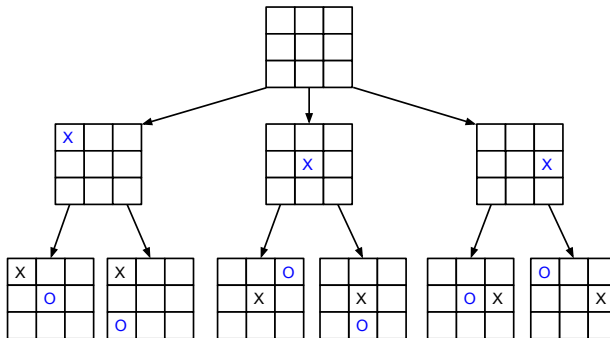
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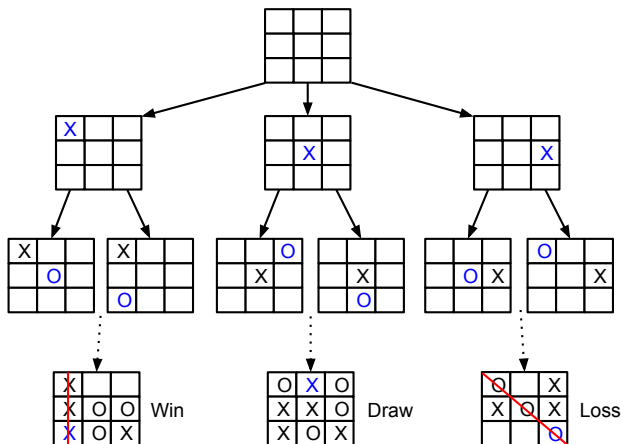
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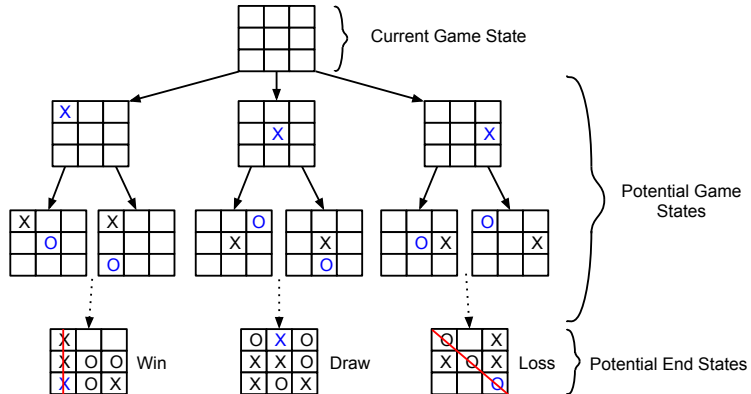
TicTacToe Diagram More Levels



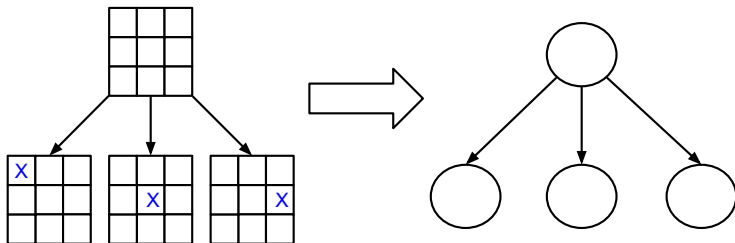
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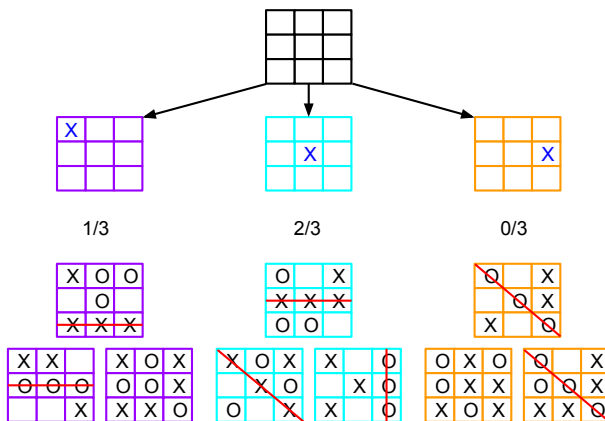
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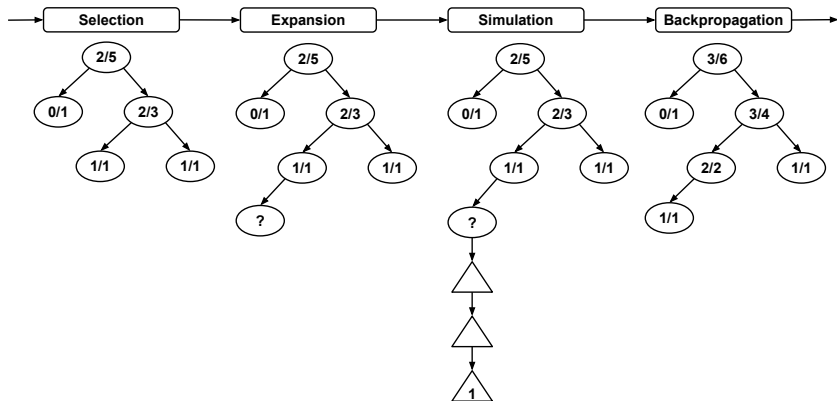
Tree Structure



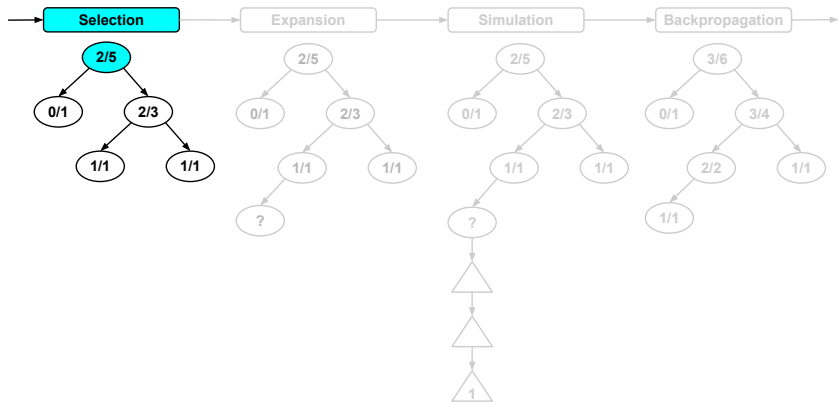
Sampling



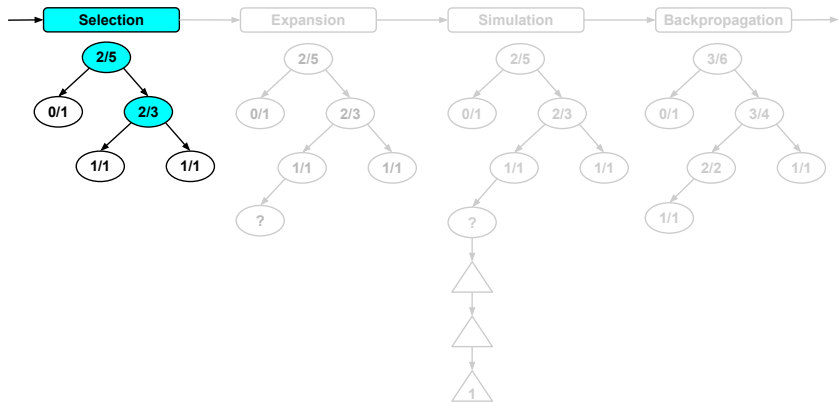
Four Steps Diagram



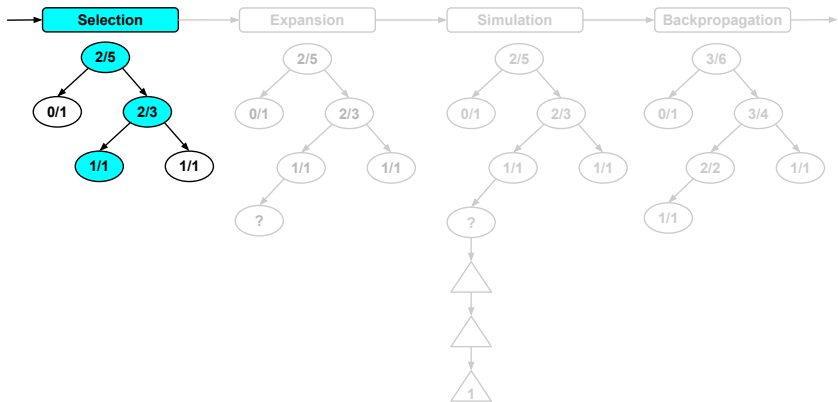
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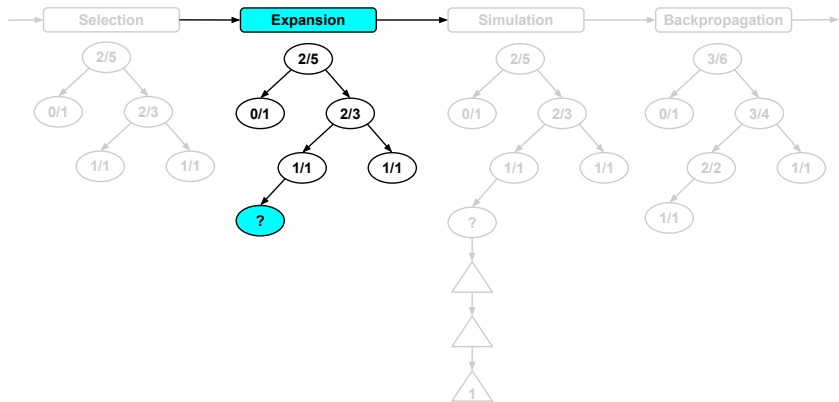
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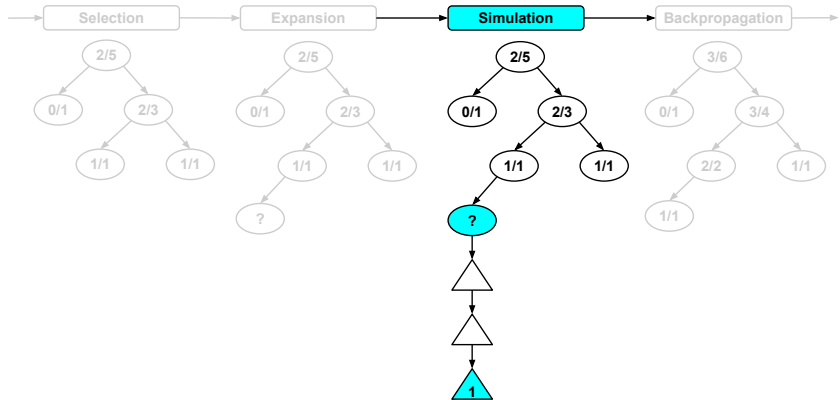
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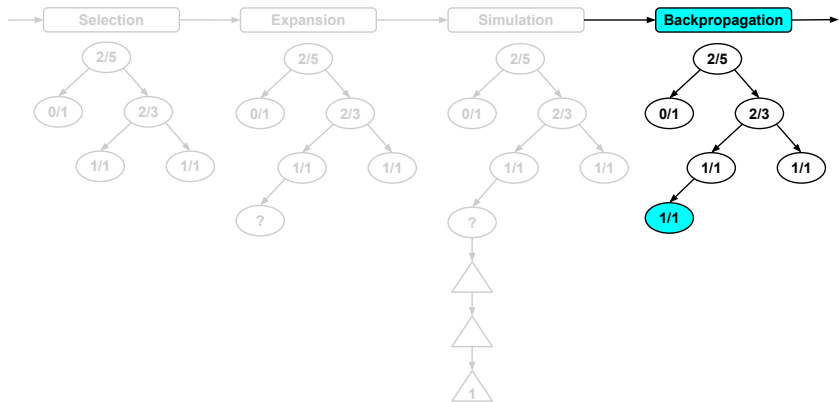
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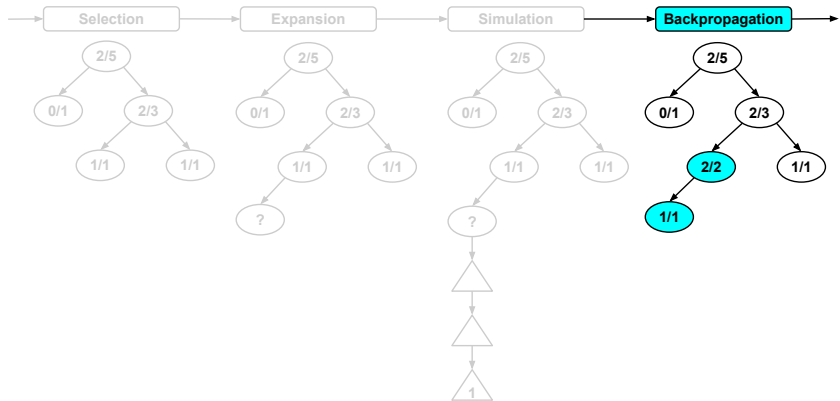
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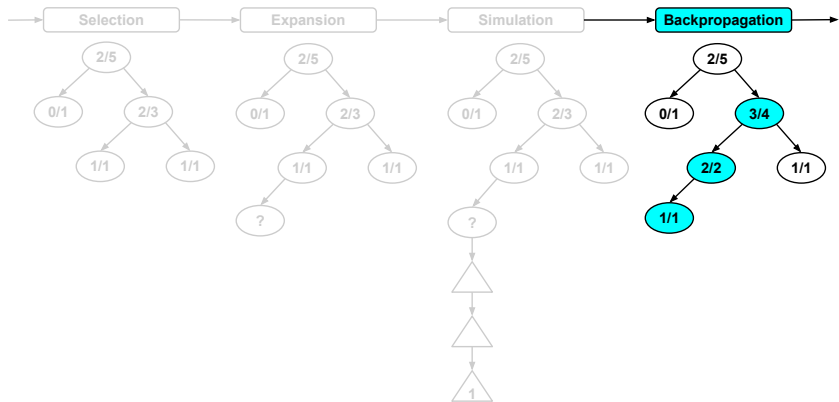
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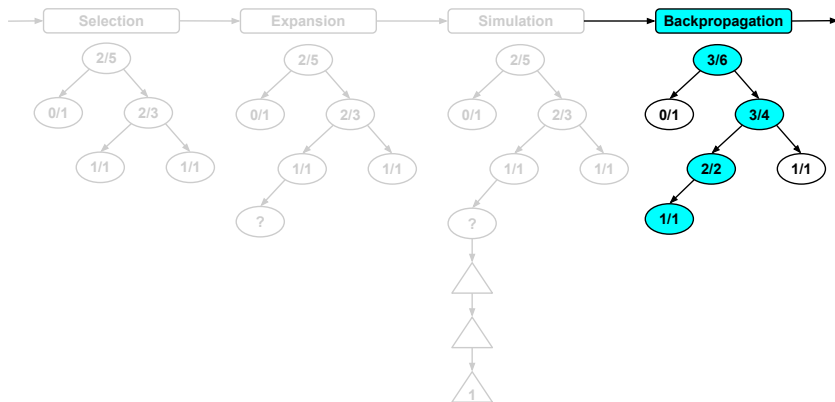
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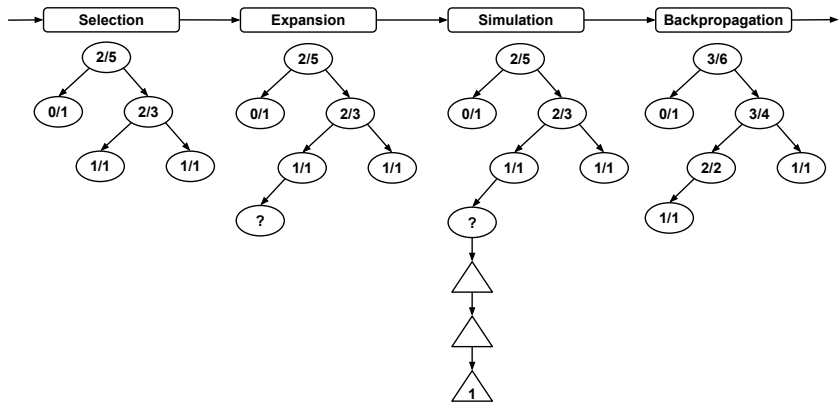
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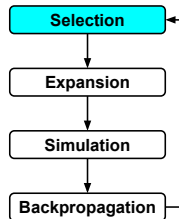
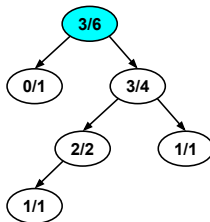
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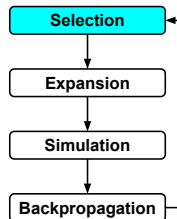
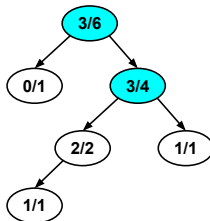
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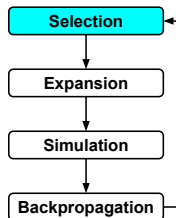
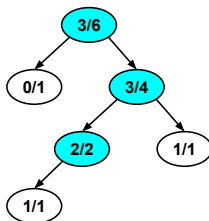
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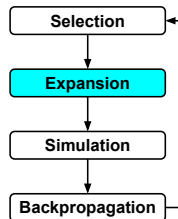
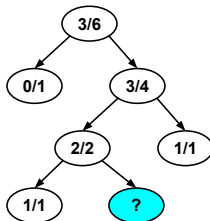
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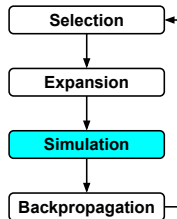
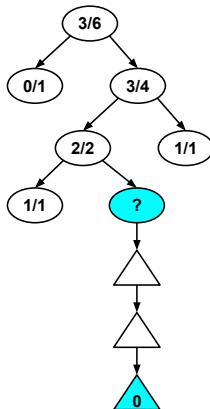
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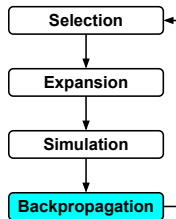
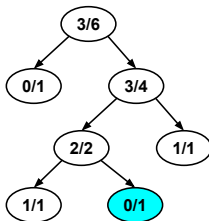
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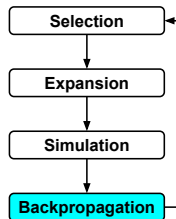
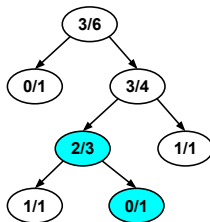
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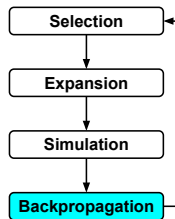
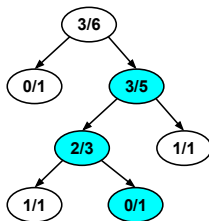
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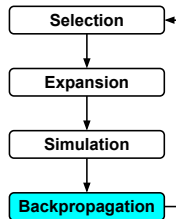
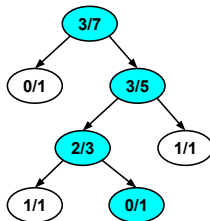
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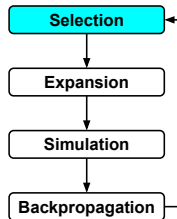
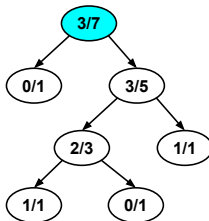
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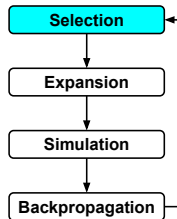
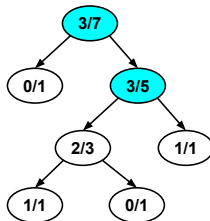
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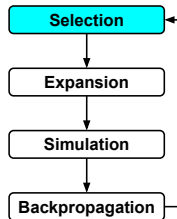
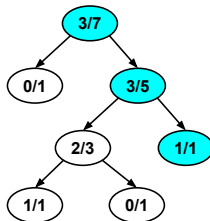
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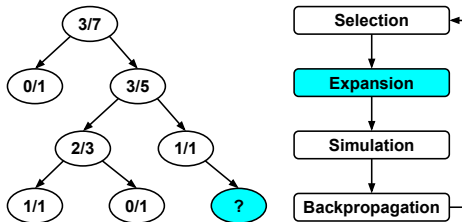
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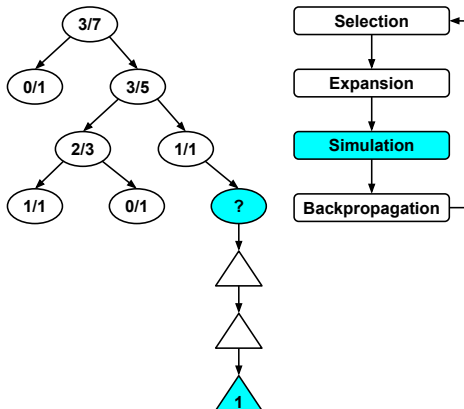
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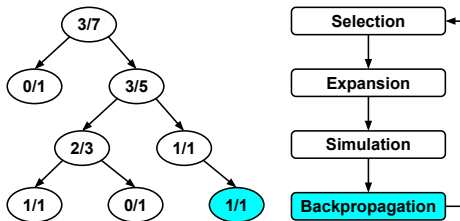
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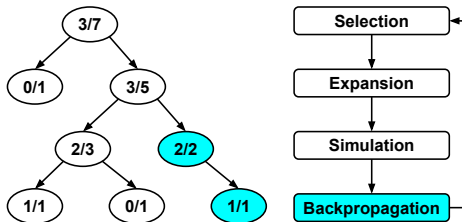
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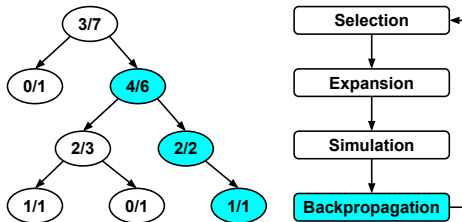
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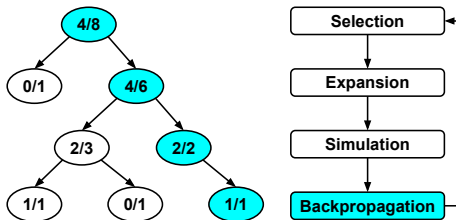
Four Steps Diagram



Four Steps Diagram



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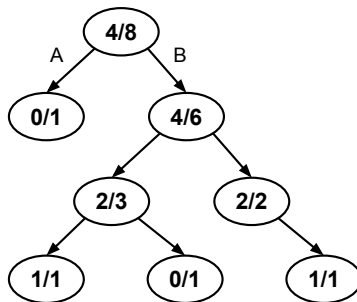
What Happens When We Choose a Move?

Now we have:

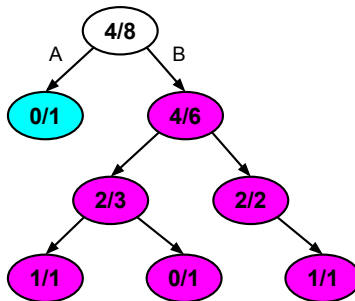
- ▶ A tree structure
- ▶ A method of generating the tree

What happens when we need to choose a move?

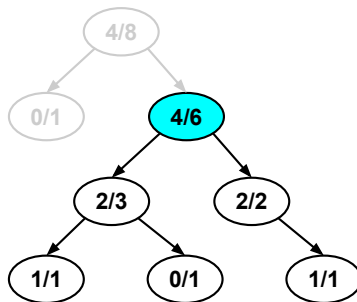
Choosing a Move



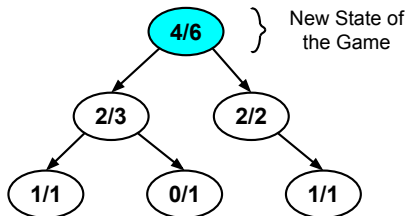
Choosing a Move



Choosing a Move



Choosing a Move



Exploration vs Exploitation

- ▶ We might overlook better paths
- ▶ Exploration vs Exploitation
 - ▶ Exploration looks at more options
 - ▶ Exploitation focuses on the most promising path
- ▶ Must find a balance between the two

Upper Confidence Bound Applied to Trees (UCT)

$$UCT(node) = \underbrace{\frac{W(node)}{N(node)}}_{\text{Value of the Node}} + \underbrace{c \sqrt{\frac{\ln(N(\text{parentNode}))}{N(node)}}}_{\text{Exploration Bonus}}$$

- ▶ W represents the number of simulated wins
- ▶ N represents the total number of simulations
- ▶ C is an experimental constant
- ▶ Used during tree traversal
- ▶ Balances exploration vs exploitation

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Applying MCTS to Go

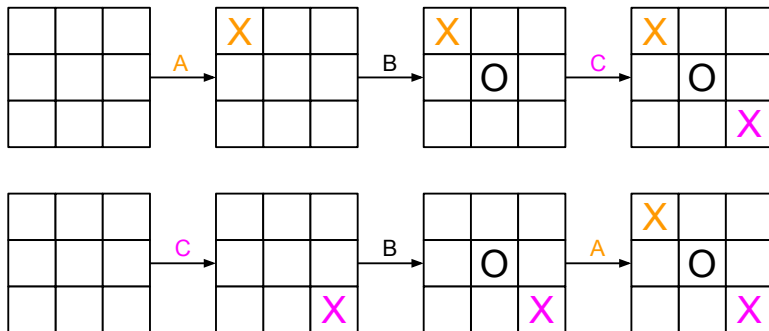
MCTS applied to Go

What variations can we make specific to Go?

In Go each player takes turn placing pieces on a game board

- ▶ How much does the order of these moves matter?
- ▶ Can we use this to improve MCTS in the context of Go?

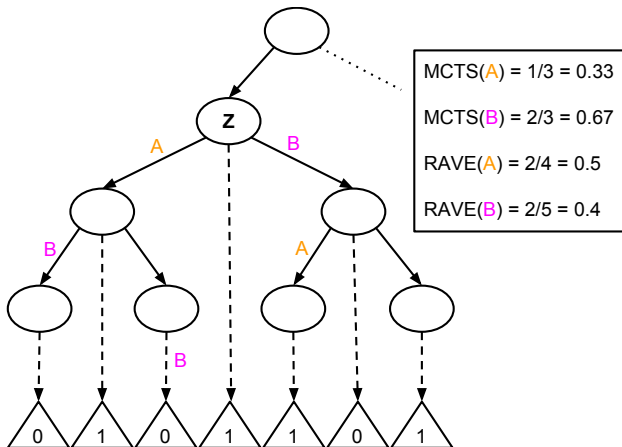
Tree Redundancy



Rapid Action Value Estimate (RAVE)

- ▶ Takes advantage of tree redundancy
- ▶ Stores the value of a move within a subtree at each node

RAVE Diagram



RAVE

- ▶ Very powerful approach
- ▶ Each simulation provides us with more information
- ▶ This approach is used by the top computer Go programs

Results

- ▶ Deterministic approaches could hardly defeat low level amateurs
- ▶ Computer Go programs use RAVE with MCTS
 - ▶ MoGo
 - ▶ Crazy Stone
- ▶ Can compete against top pros in 9x9 Go
- ▶ Can compete against top pros in handicapped 19x19 Go