Monte Carlo Search Tree and Its Applications

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Kasparov vs Deep Blue

Kasparov vs Deep Blue

Great display of artifical intelligence (AI)
Techniques employed by IBM

- Brute force deterministic approach
- human knowledge

Limitation

- scalability into larger search spaces

Monte Carlo tree search (MCTS) is an alternative method

Outline

Monte Carlo Tree Search (MCTS)

- Combines random sampling and game trees
- Probabilistic not deterministic
- Useful for problems with larger search spaces

Applying MCTS to Go

Go

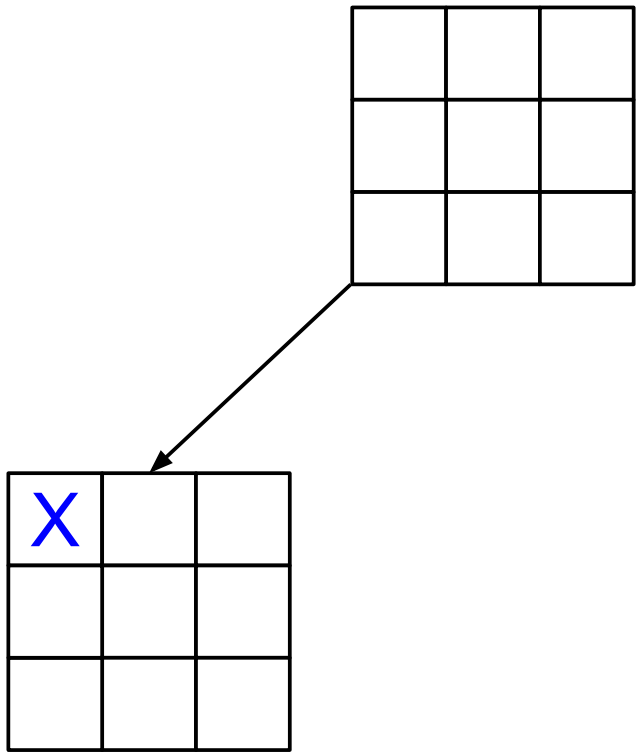
- Board game about positional advantage
- Game board for Chess:
  - 8x8
- Average possible configurations for a game of Chess:
  - 10^{120}
- Game board for Go:
  - 19x19
- Average possible configurations for a game of Go:
  - 10^{761}

Applying MCTS to Narrative Generation

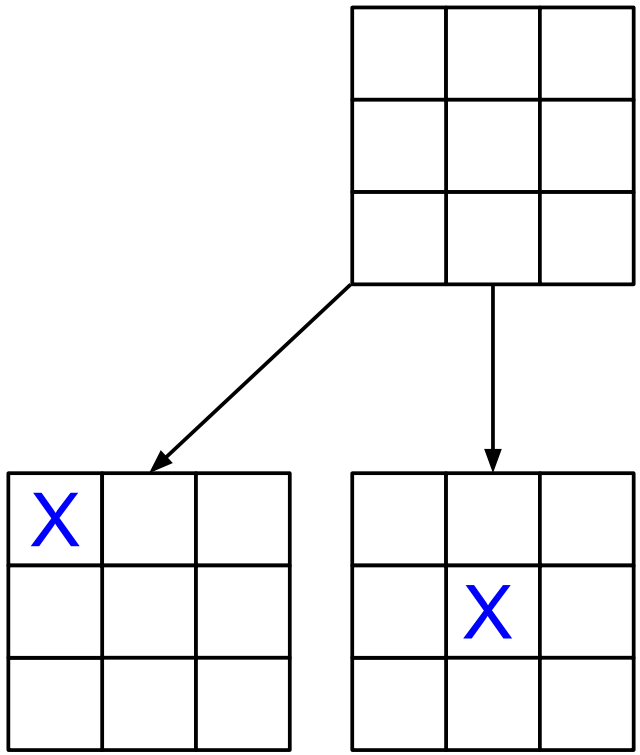
- Useful Applications
  - Video game replay value
  - Educational applications
- The search space scales with the number of characters, items, locations, and actions

Outline

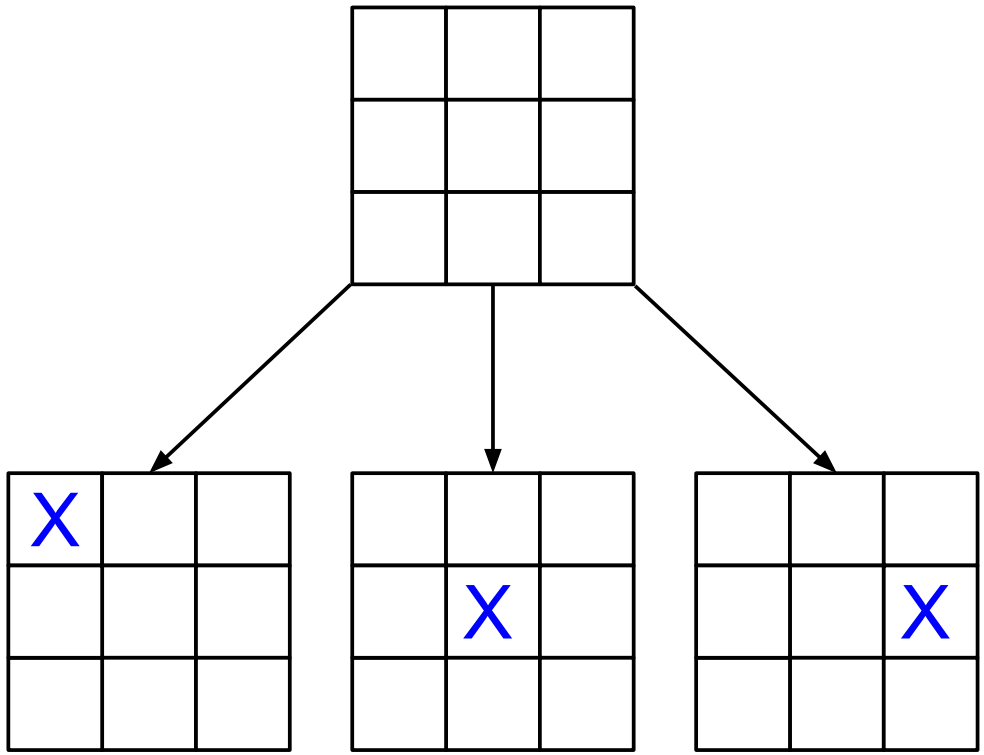
TicTacToe Diagram



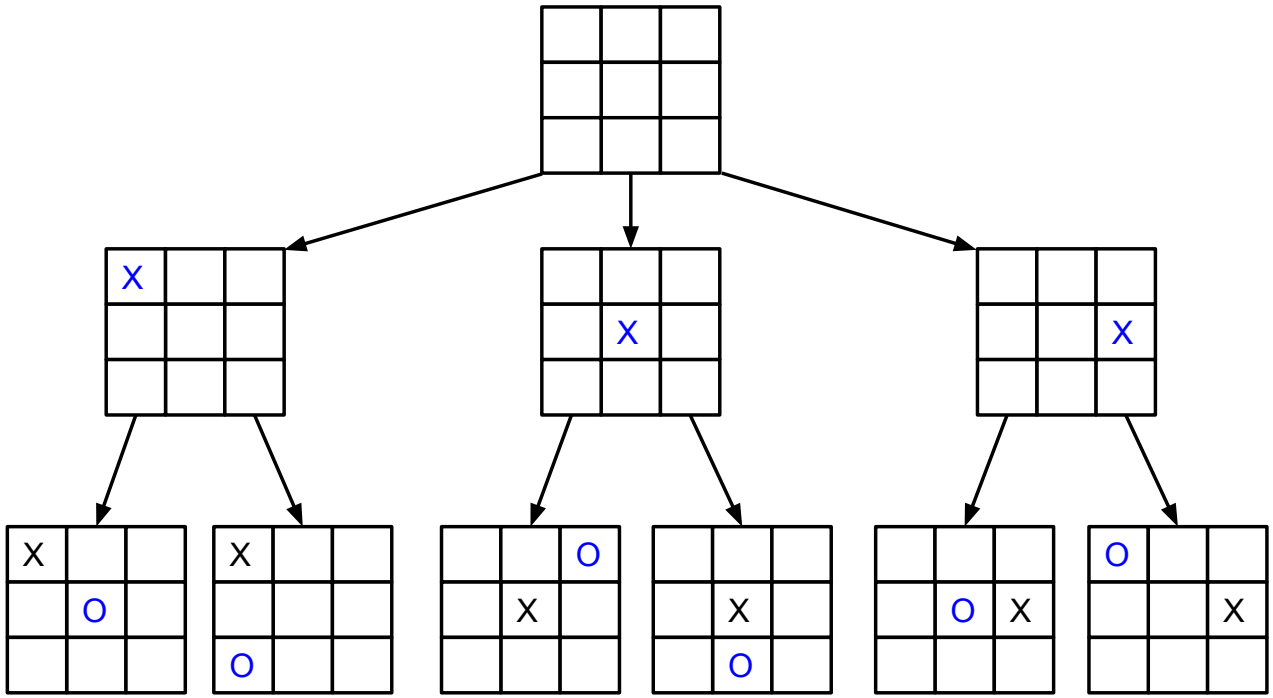
TicTacToe Diagram



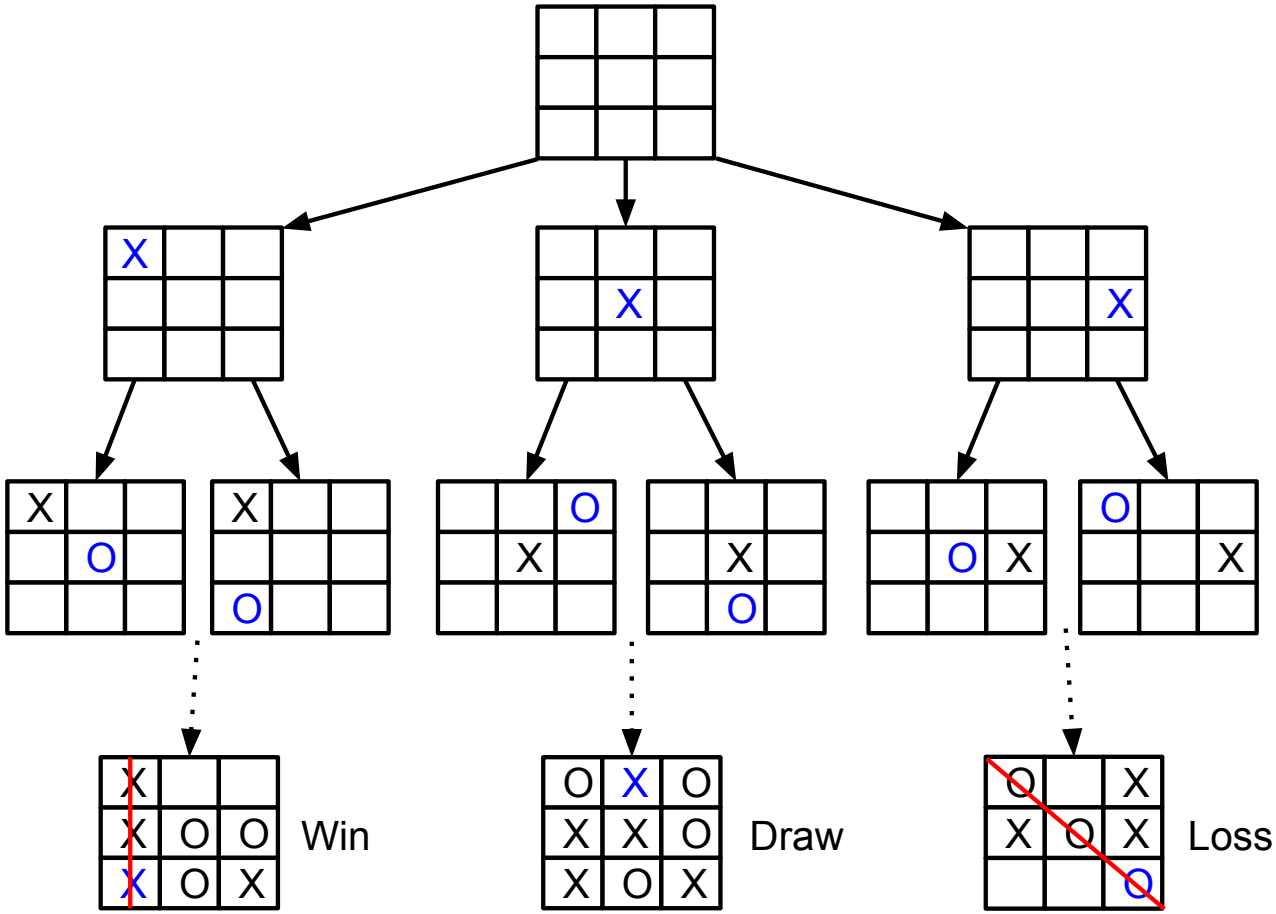
TicTacToe Diagram



TicTacToe Diagram More Levels



TicTacToe Diagram



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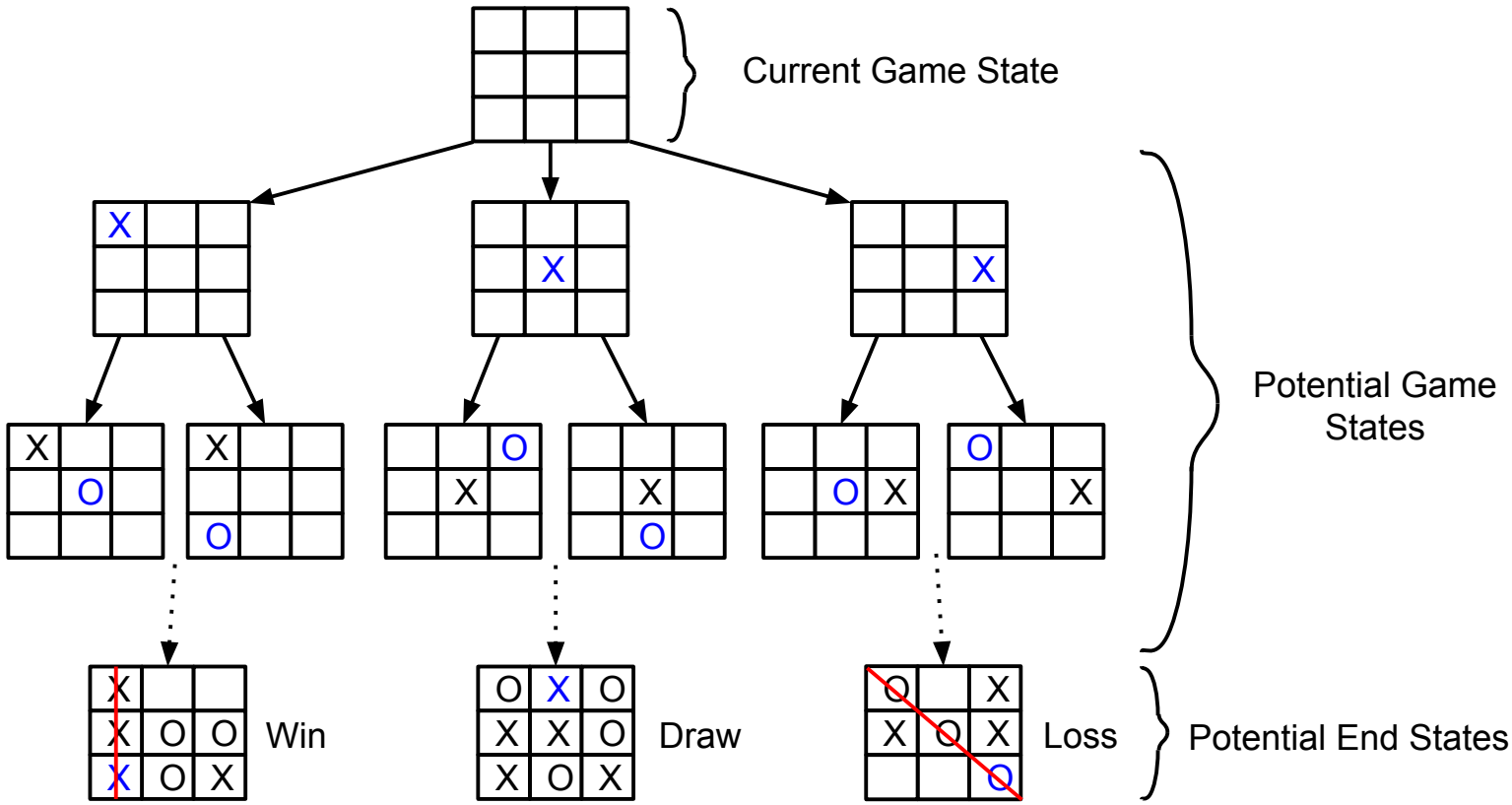
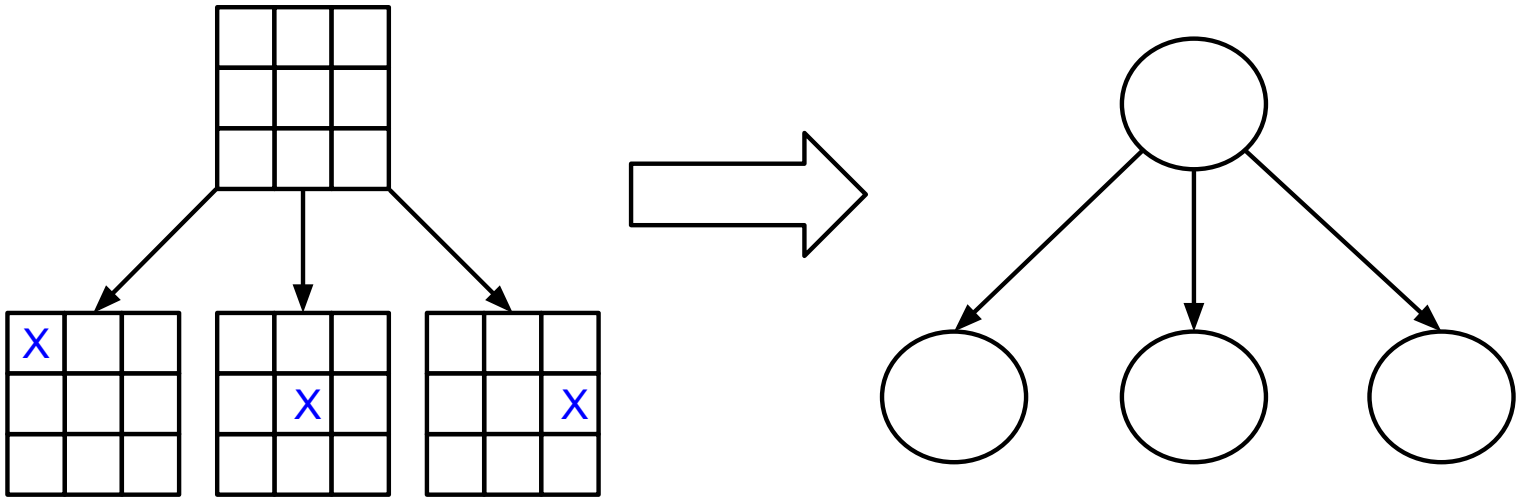
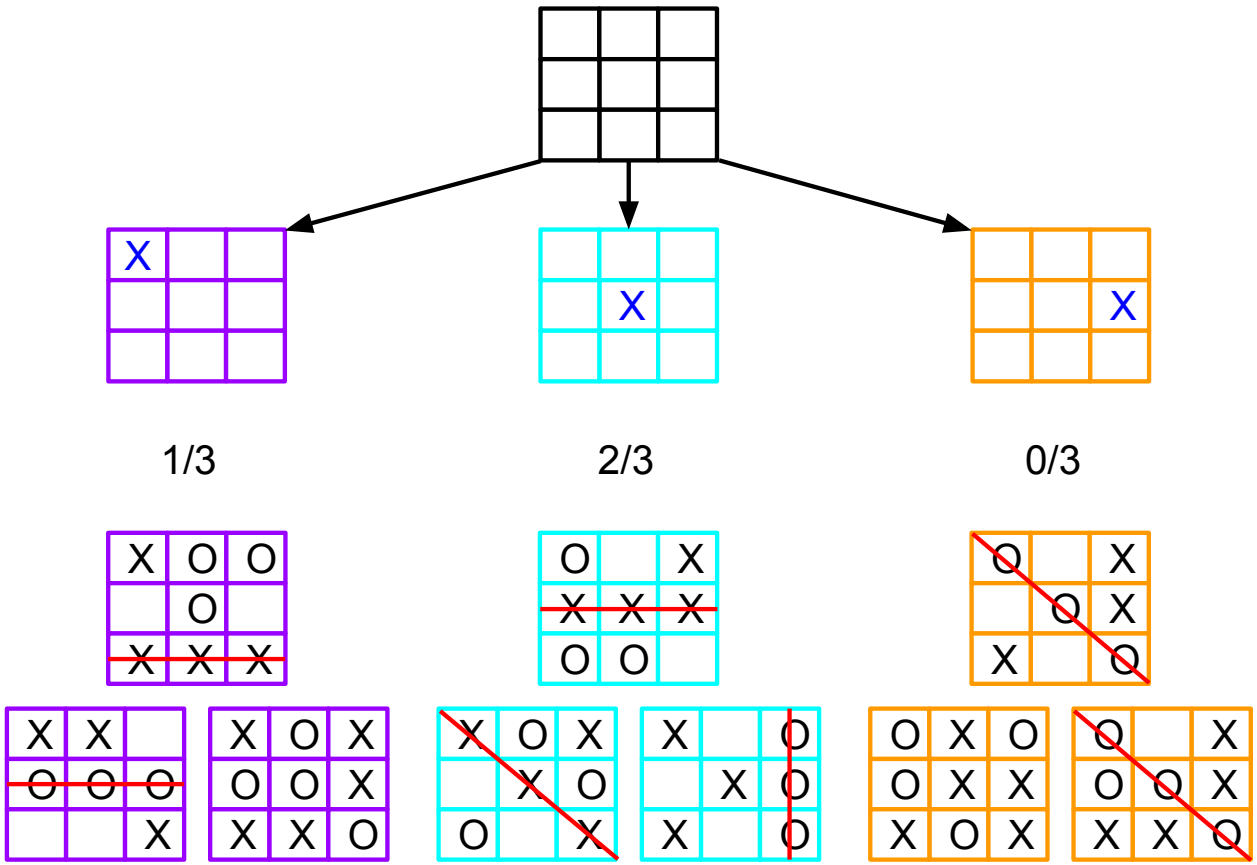


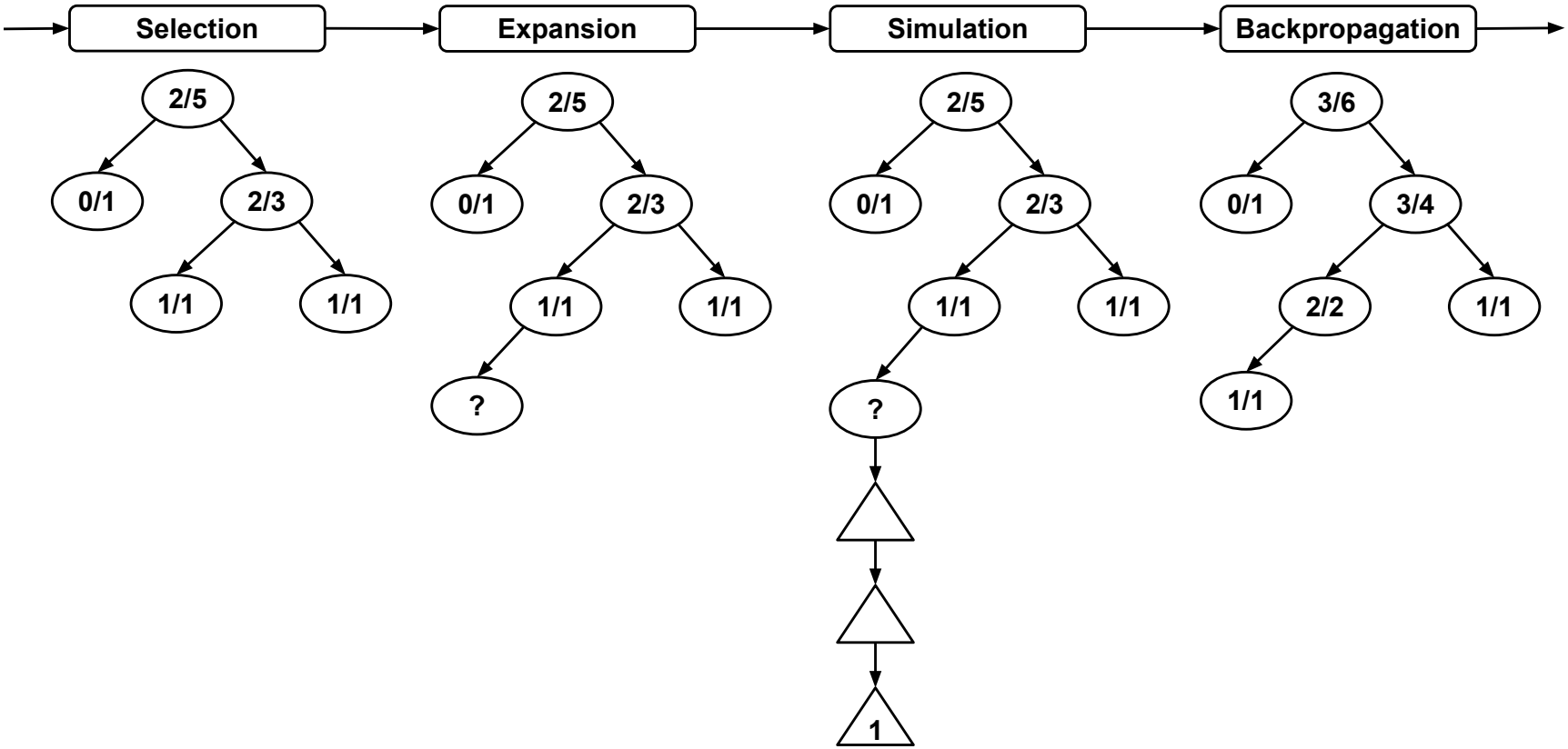
Tree Structure



Sampling



Four Steps Diagram



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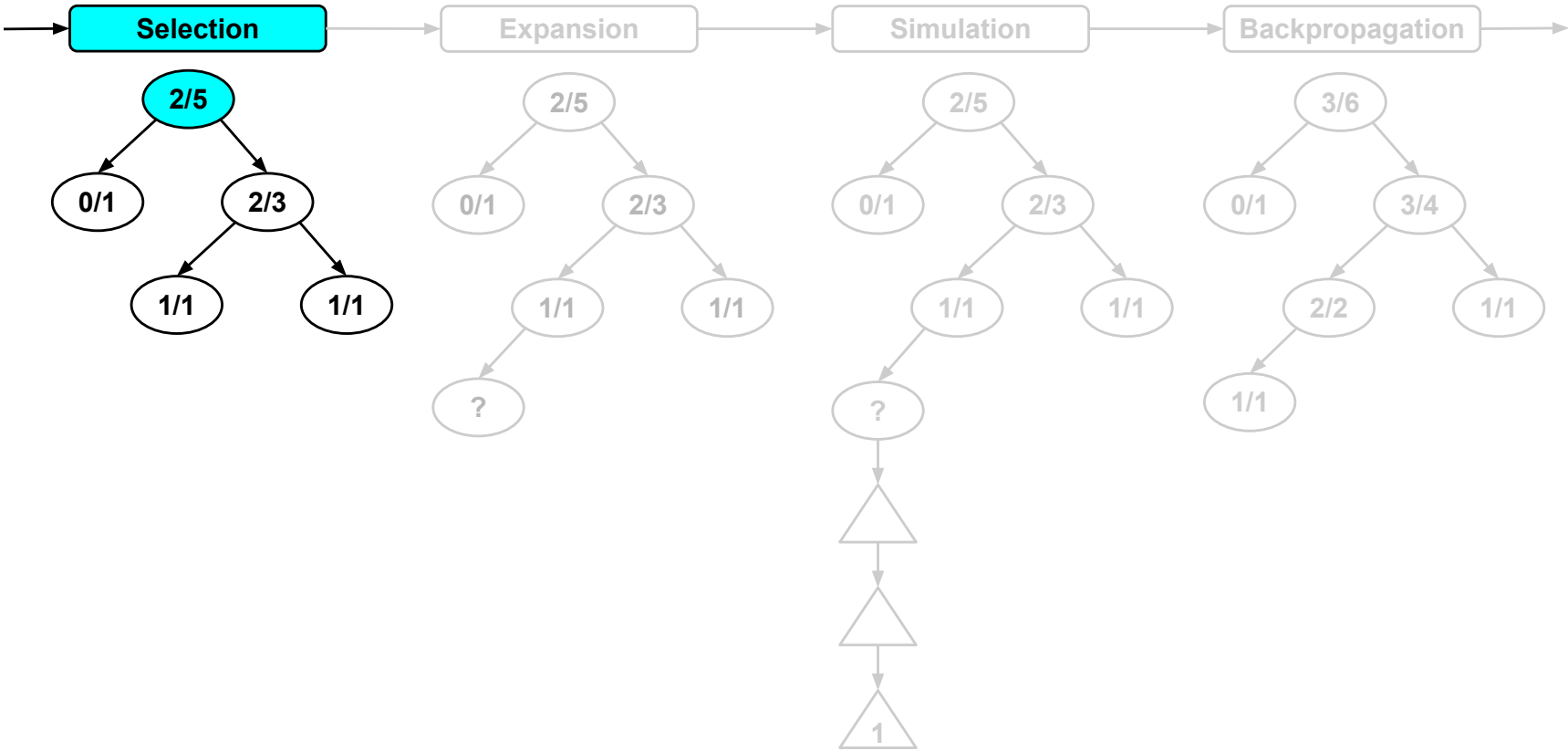

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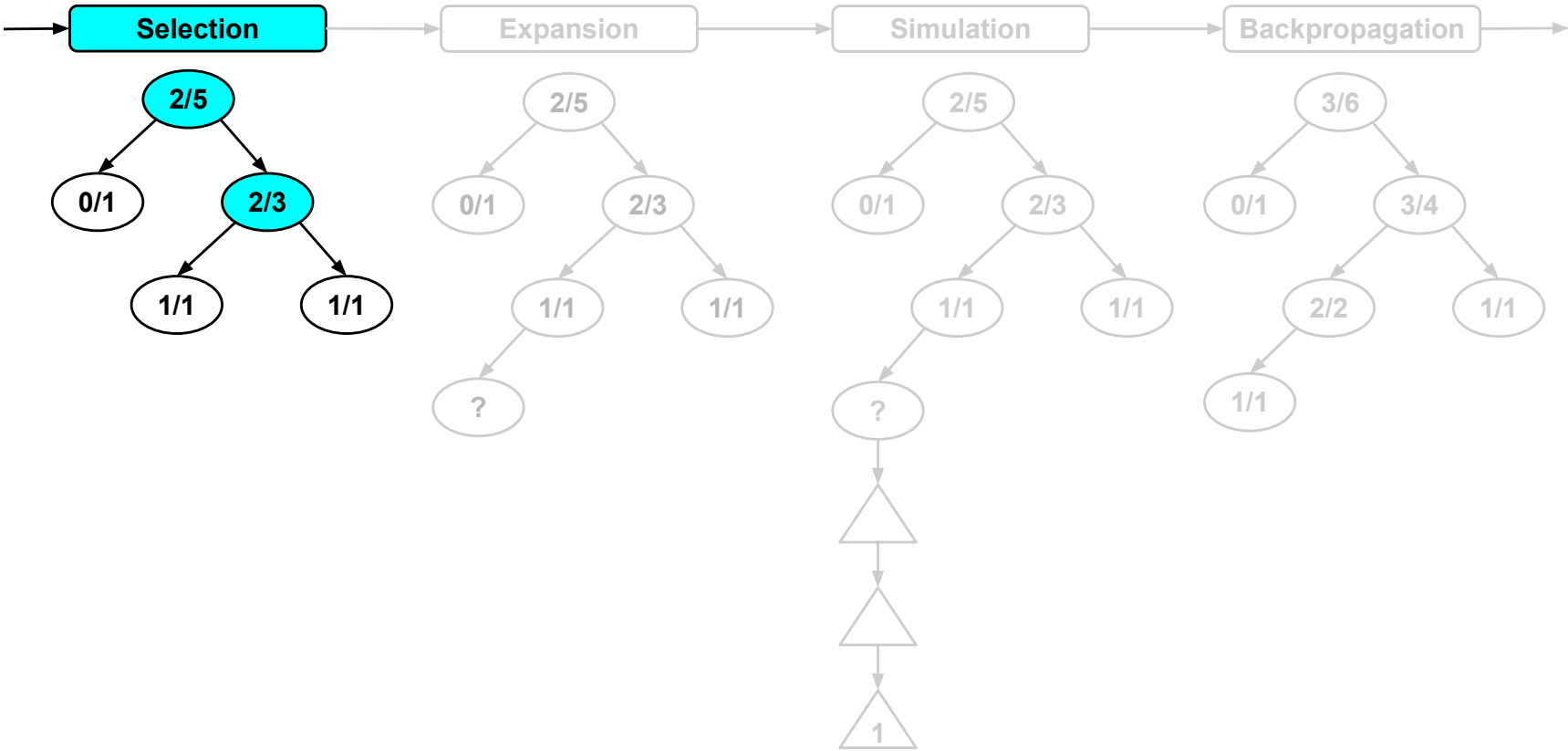

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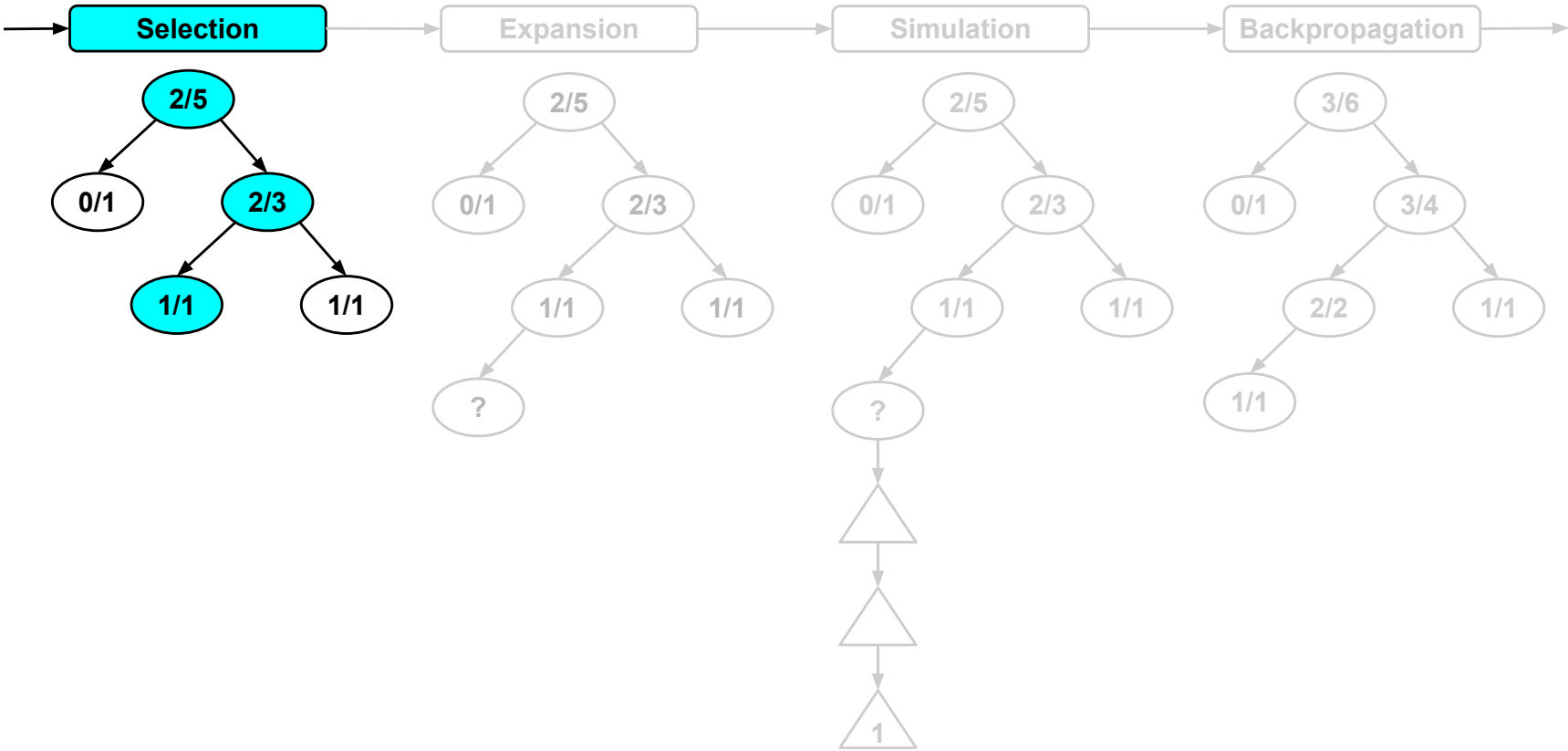

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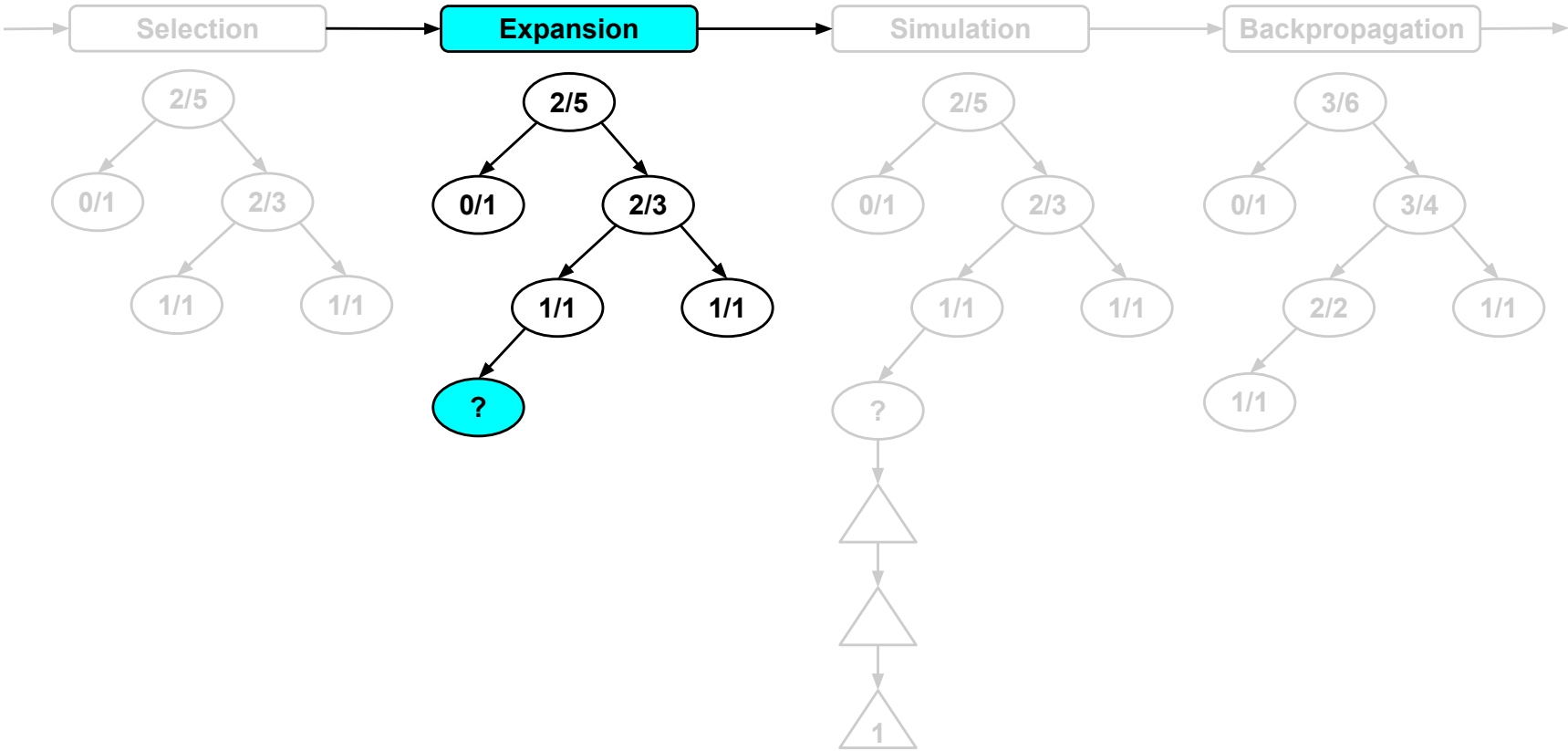

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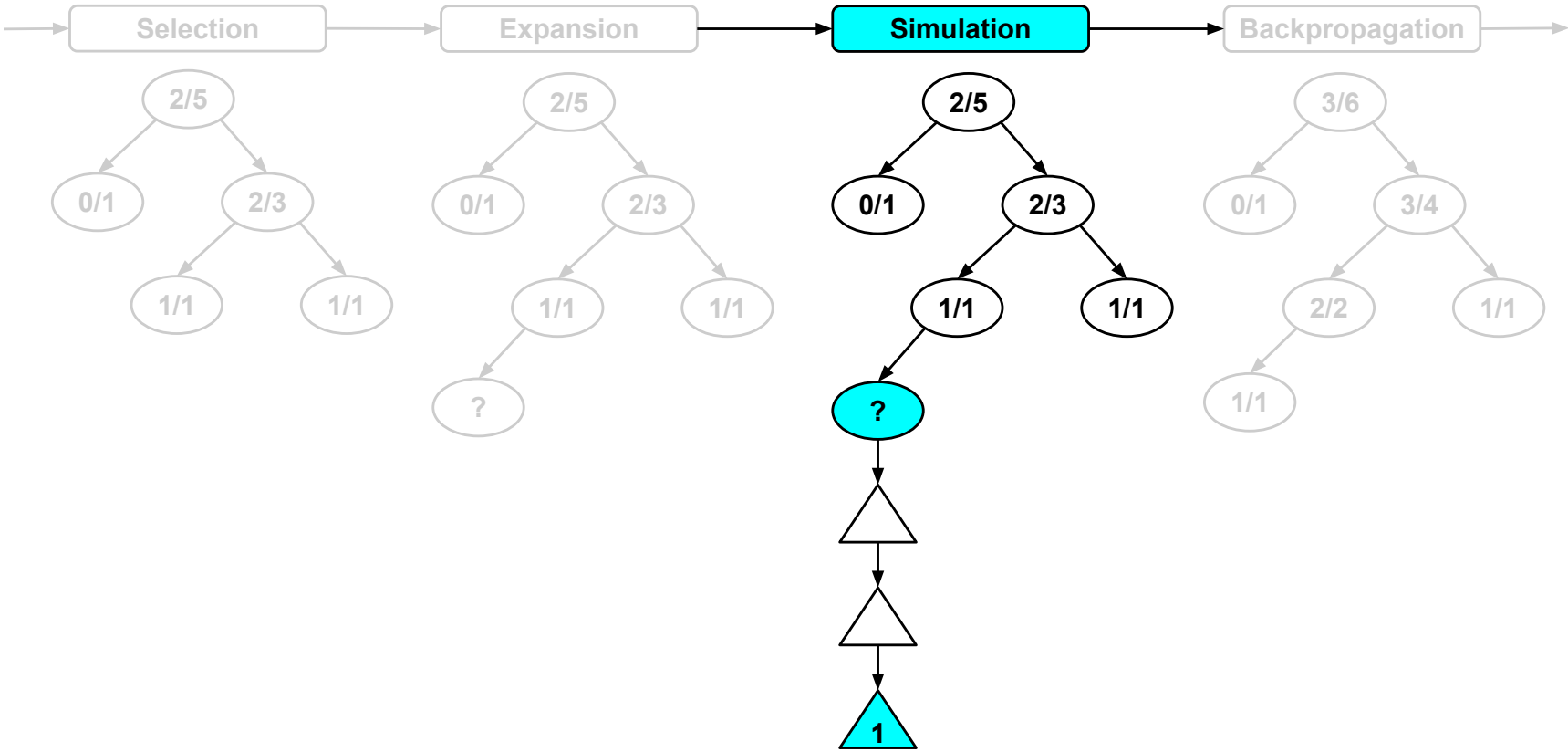

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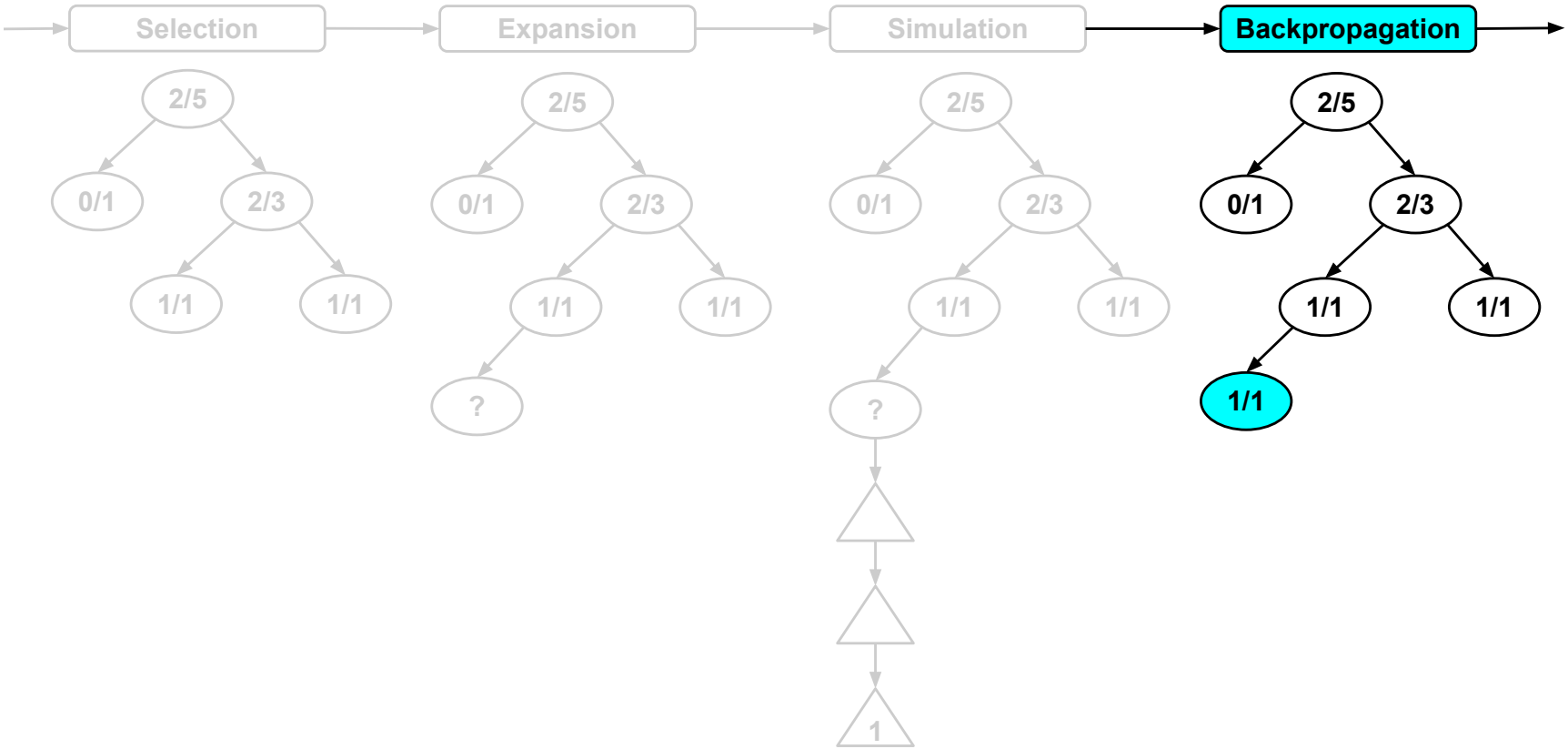

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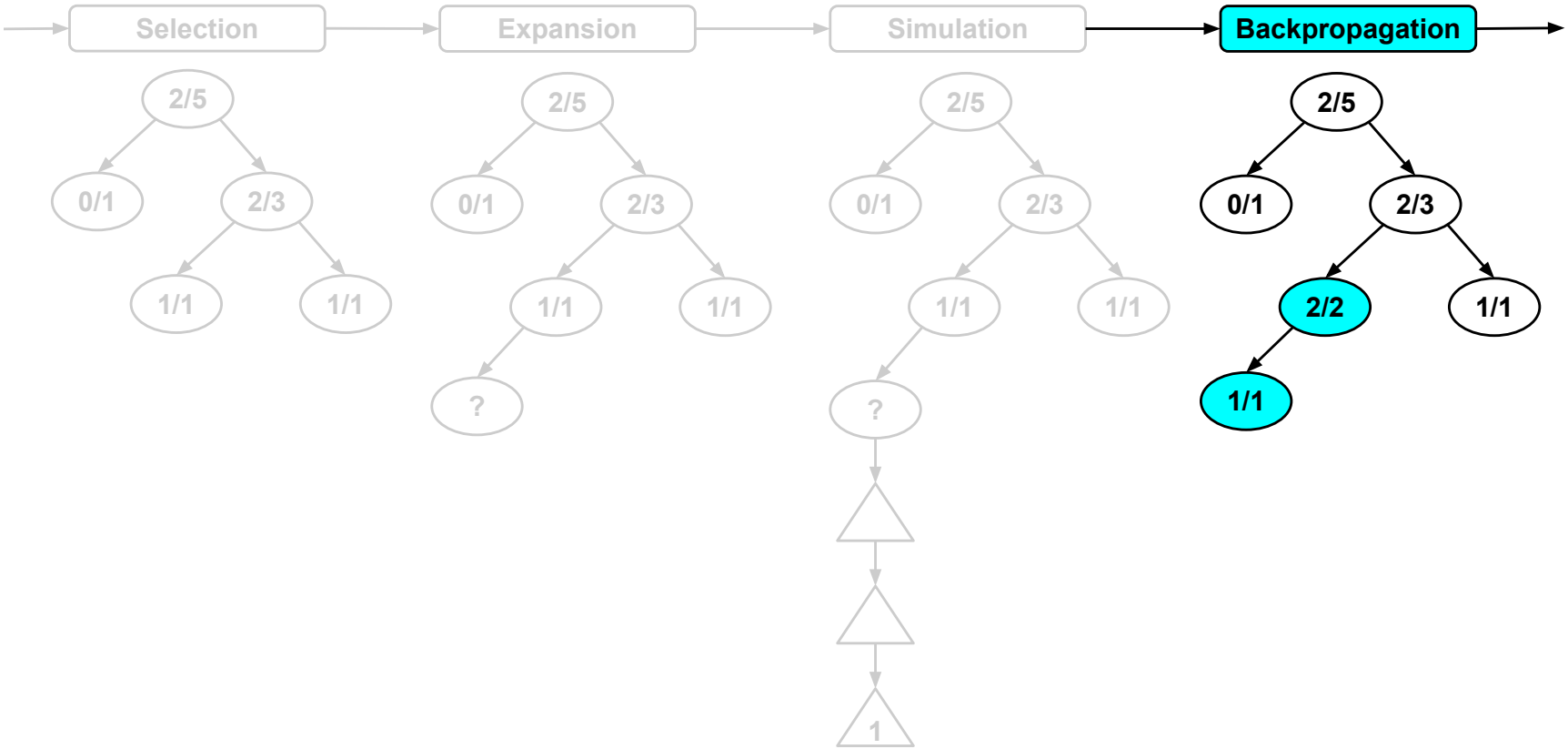

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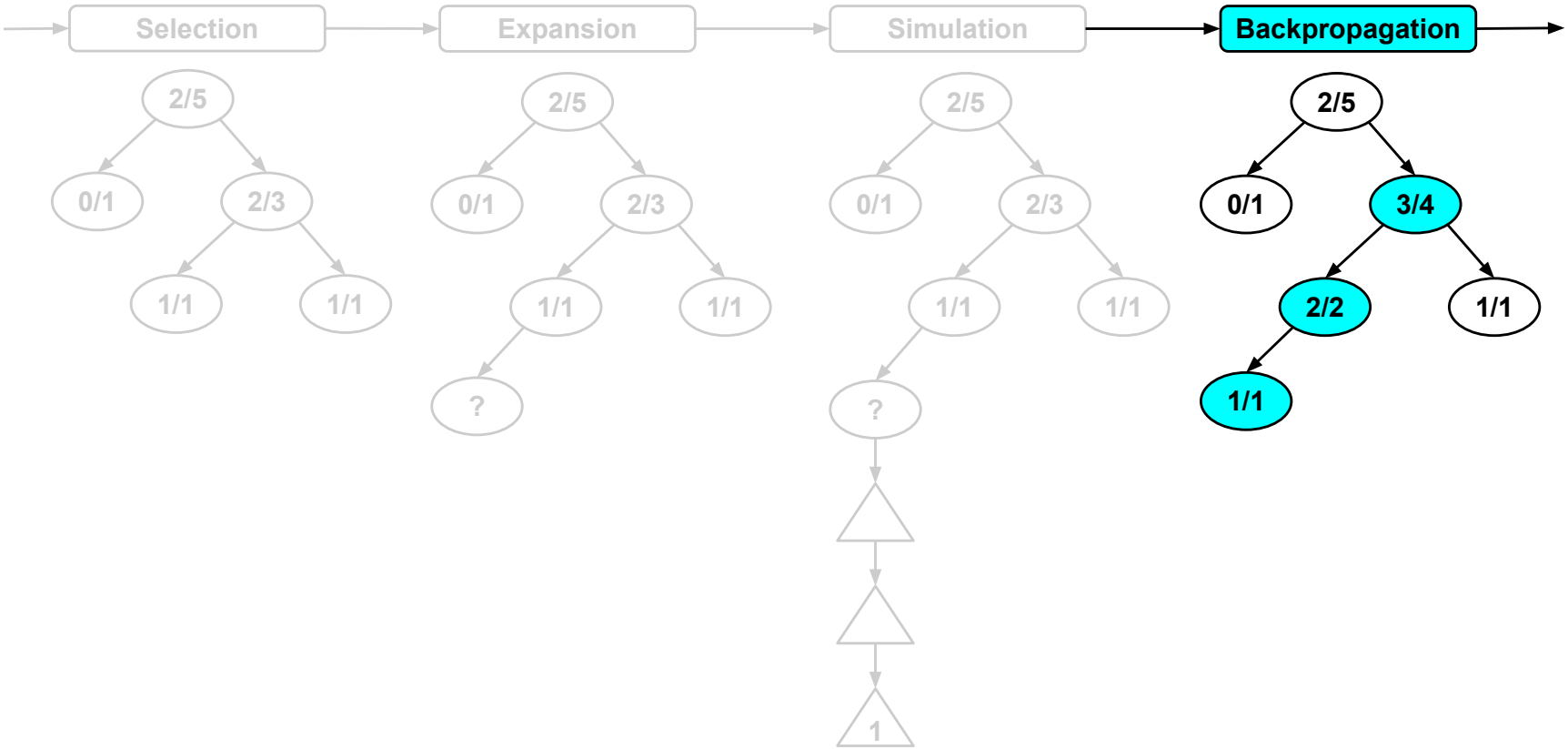

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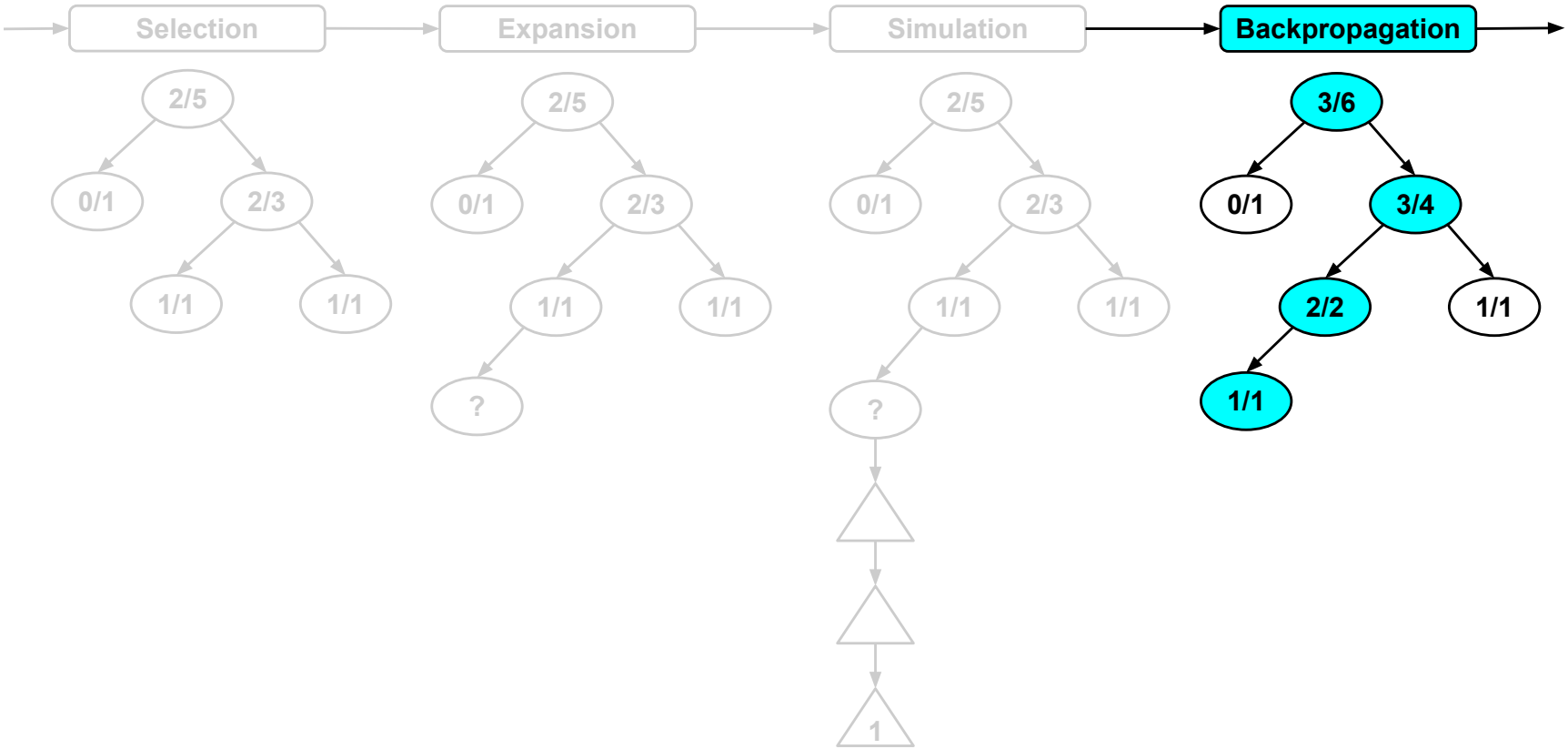

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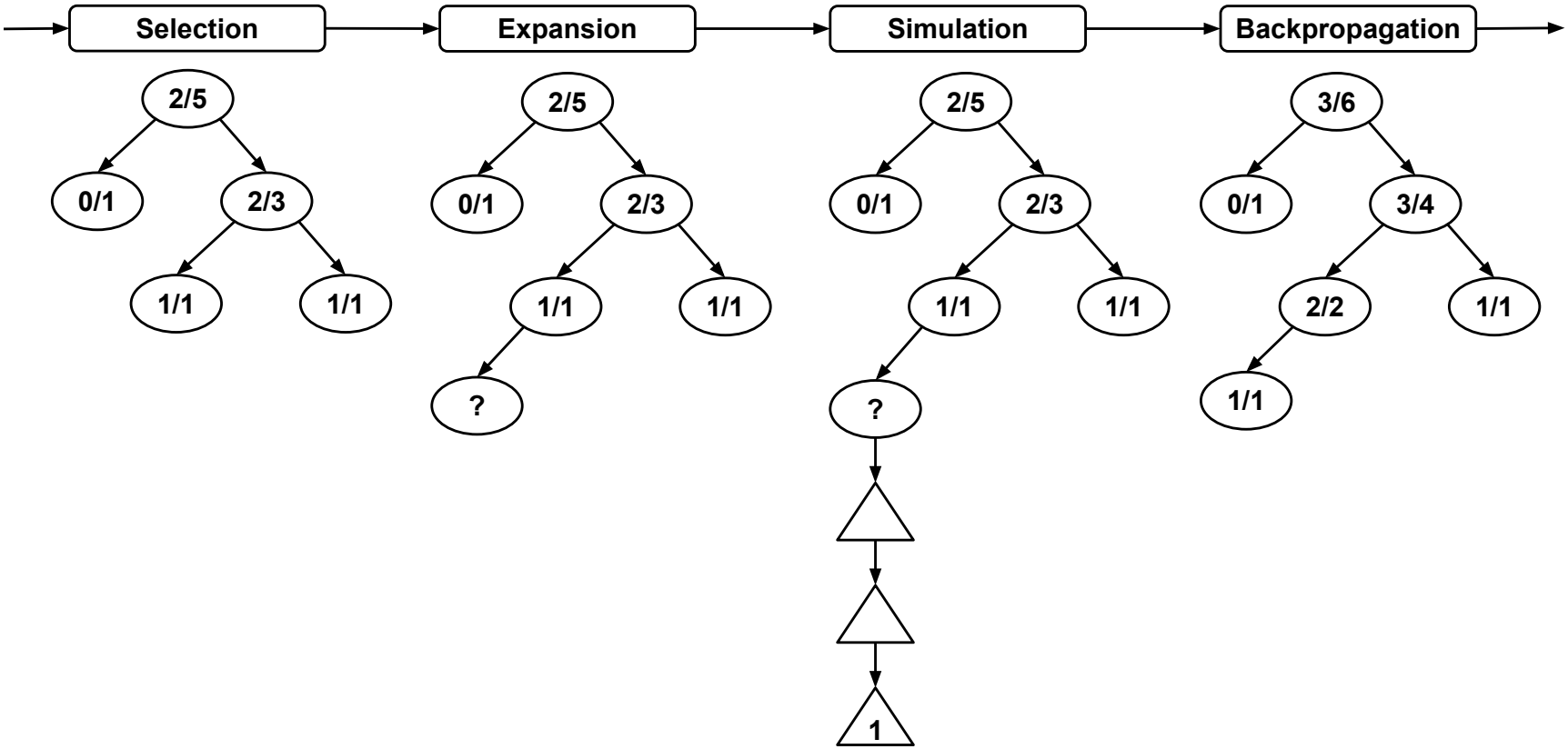

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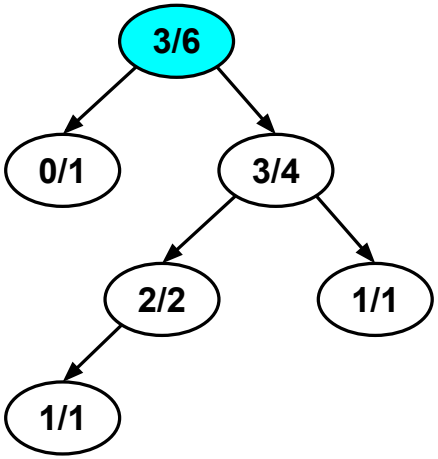

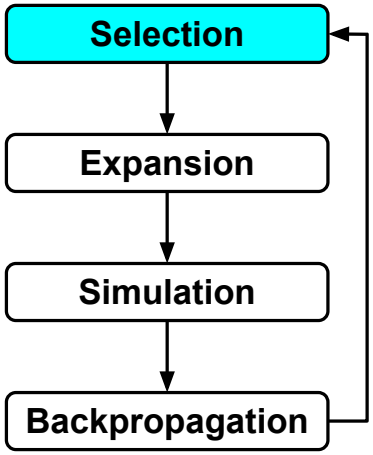

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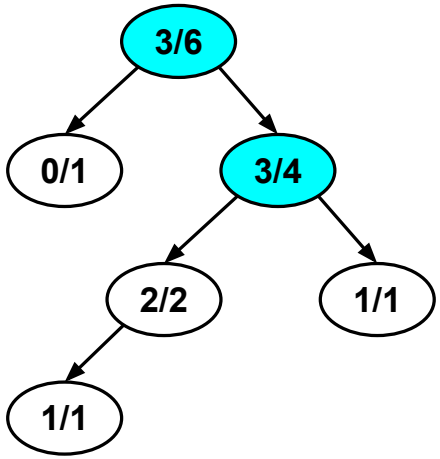

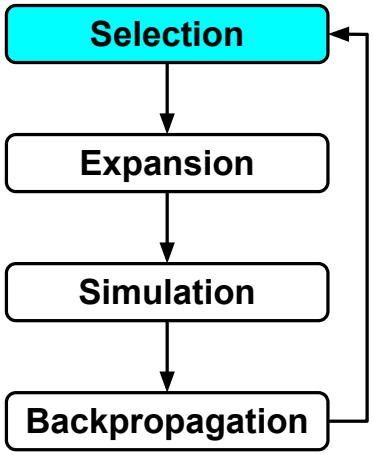

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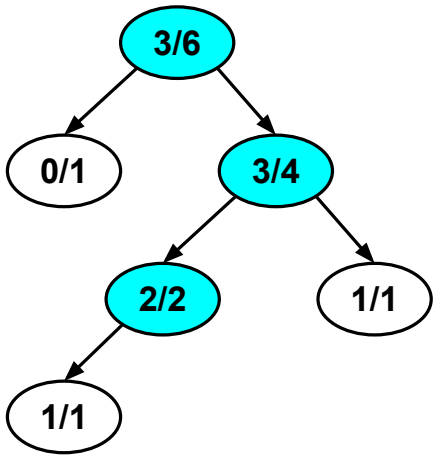

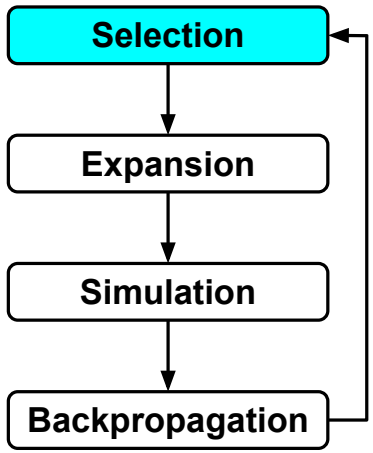

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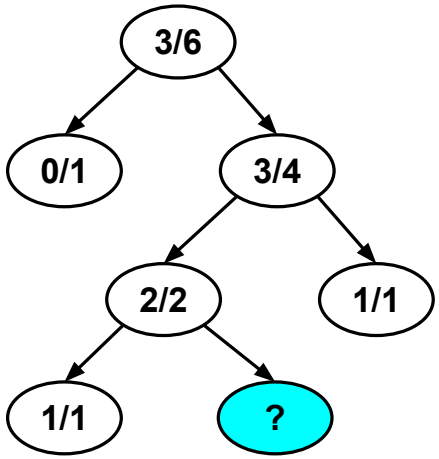

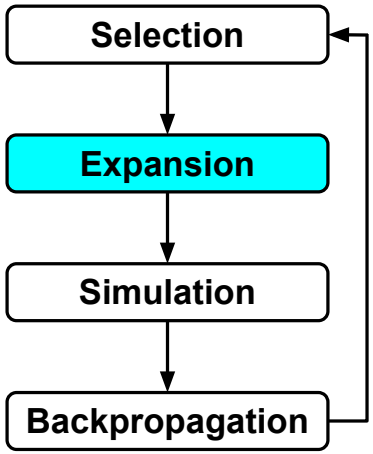

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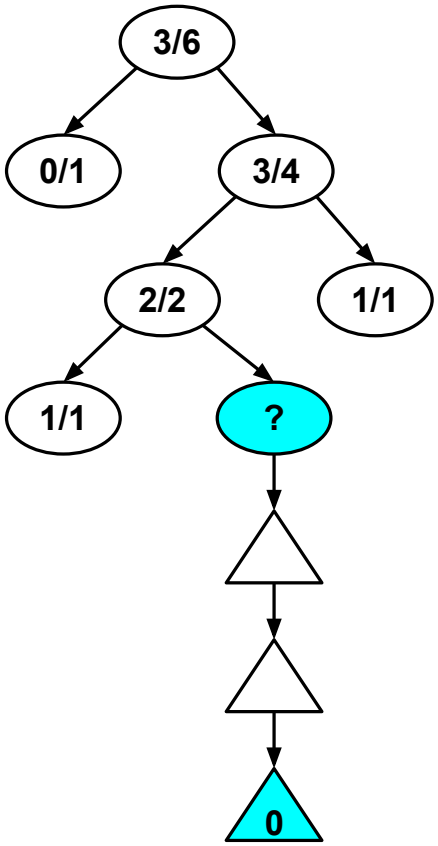

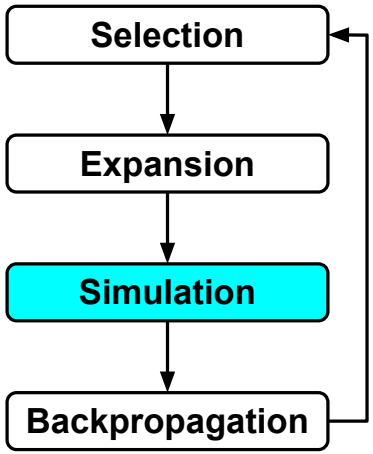

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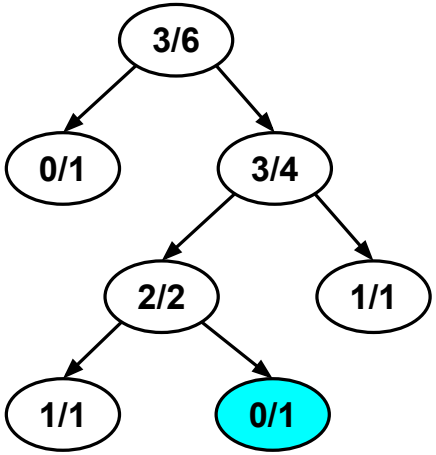

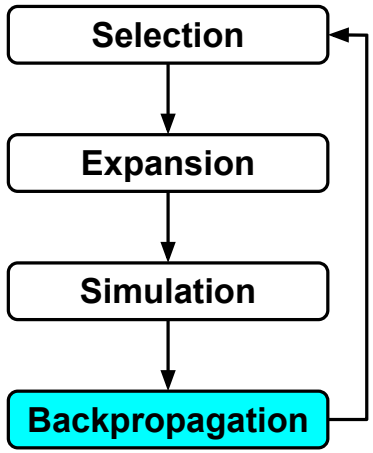

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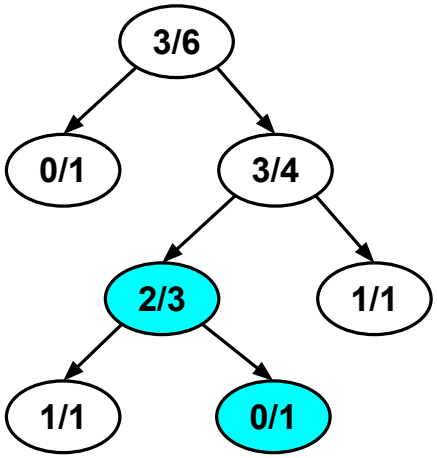

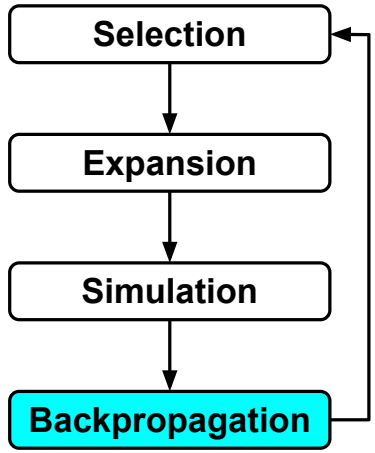

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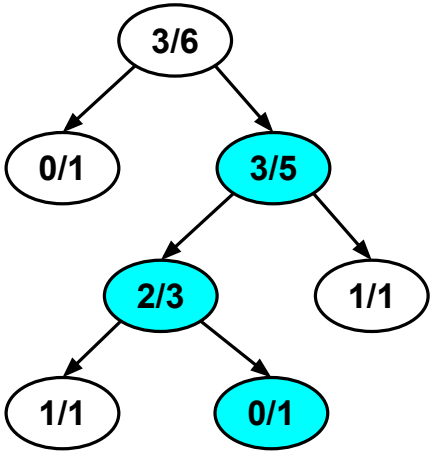

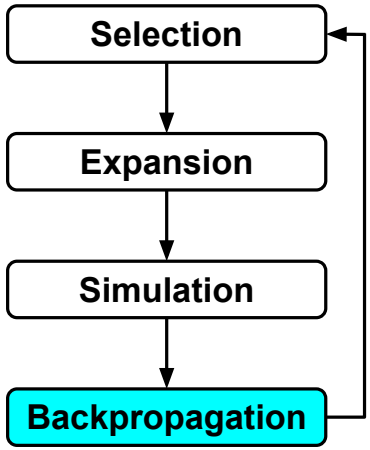

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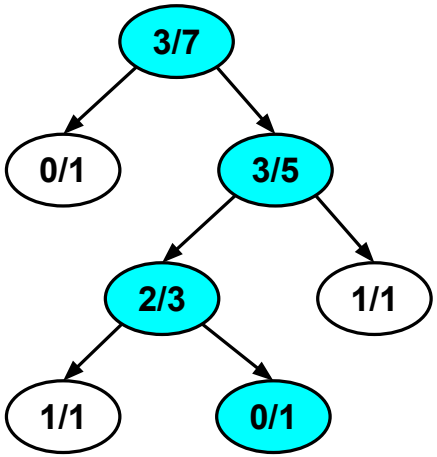

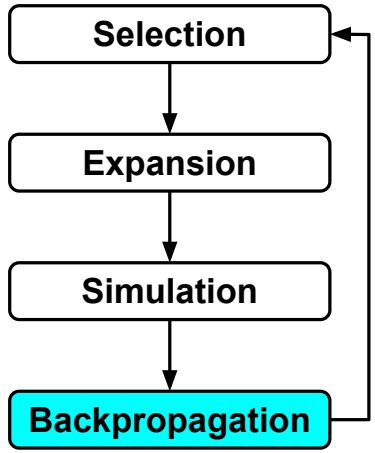

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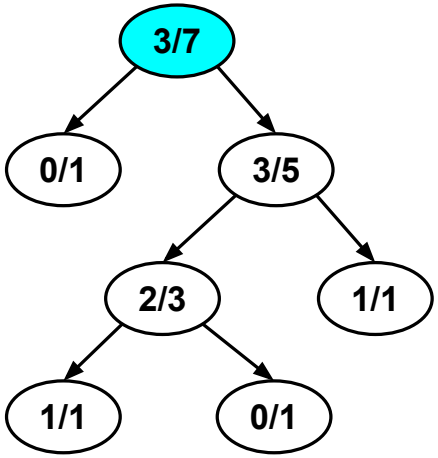

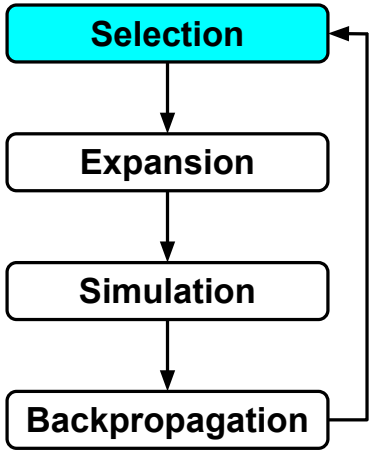

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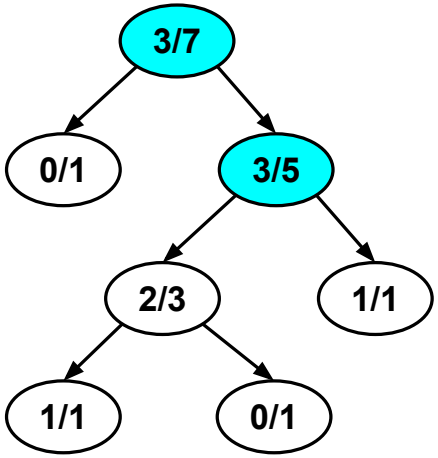

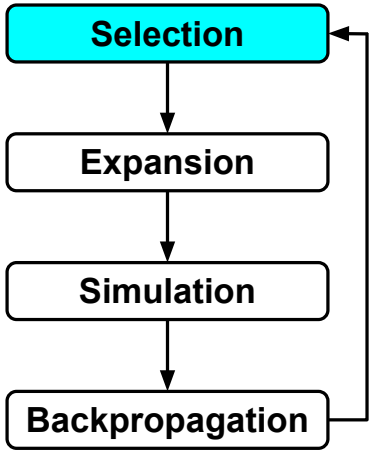

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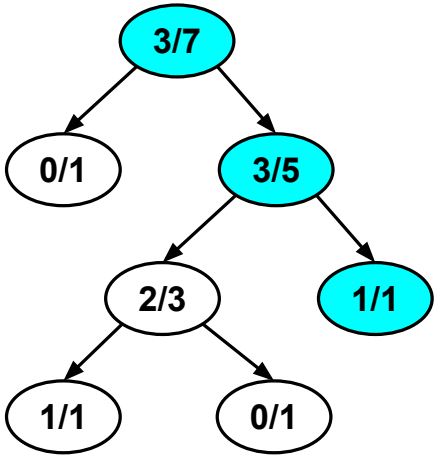

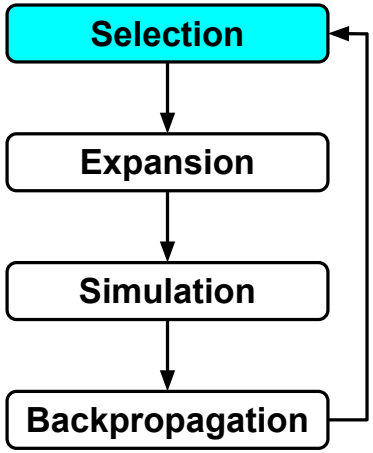

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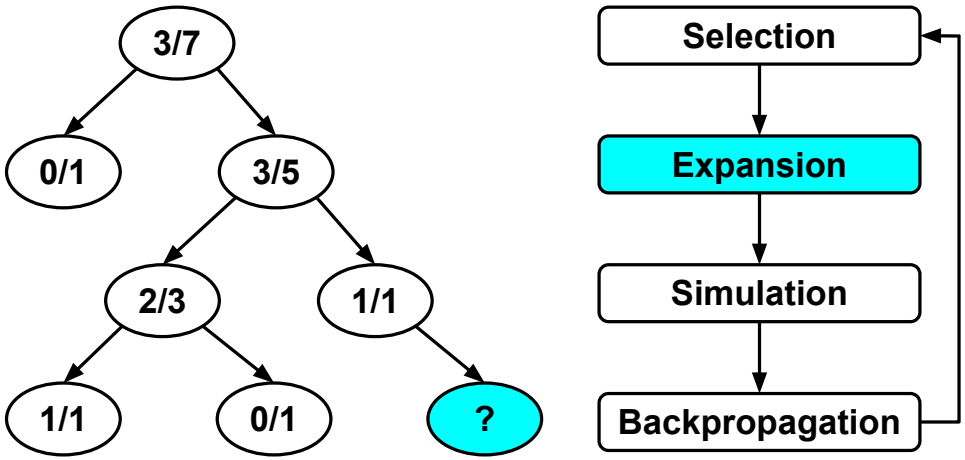

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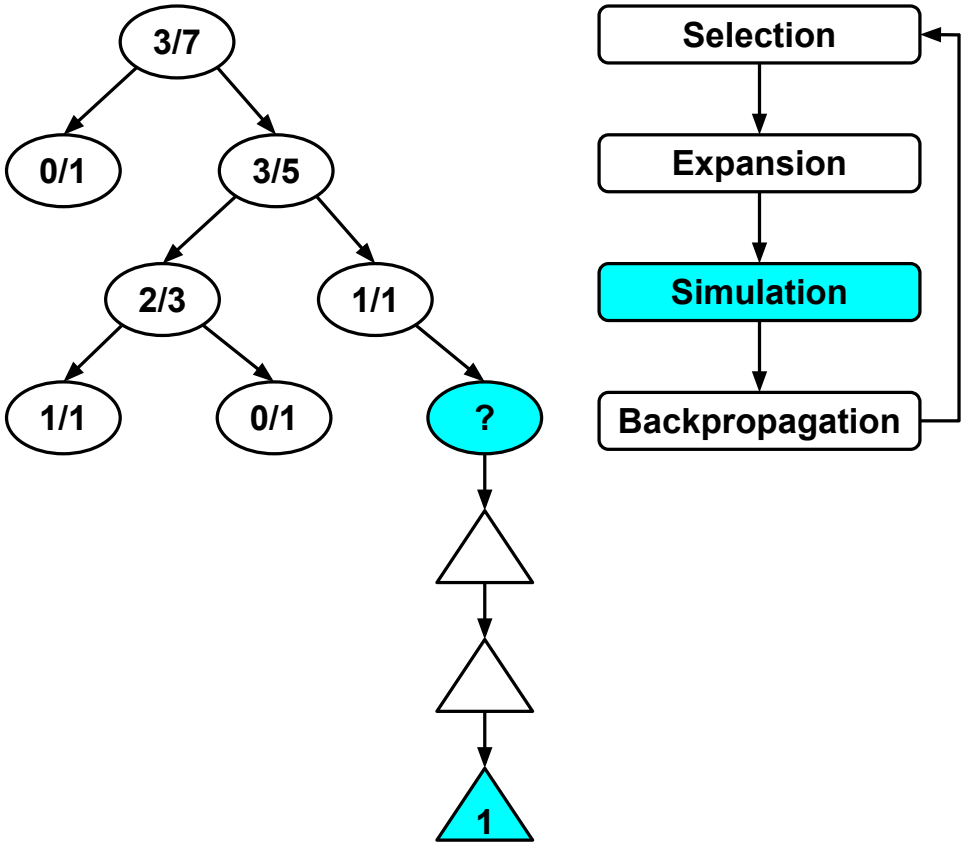

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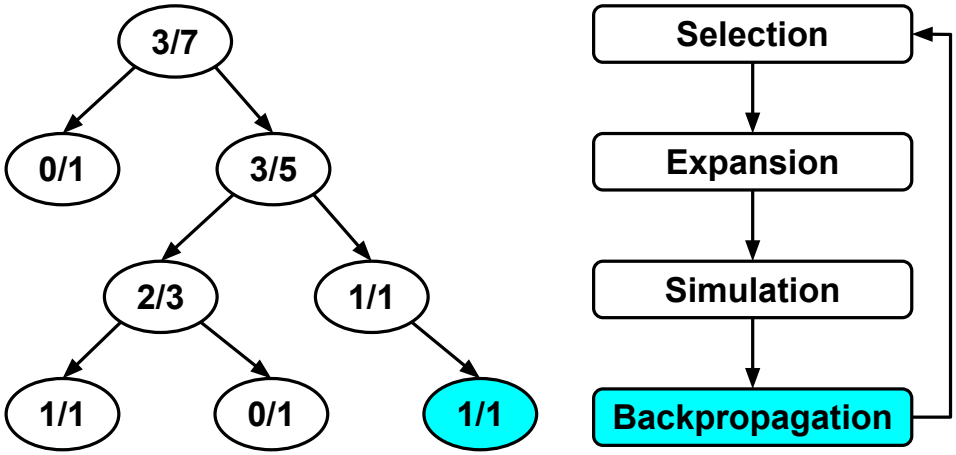

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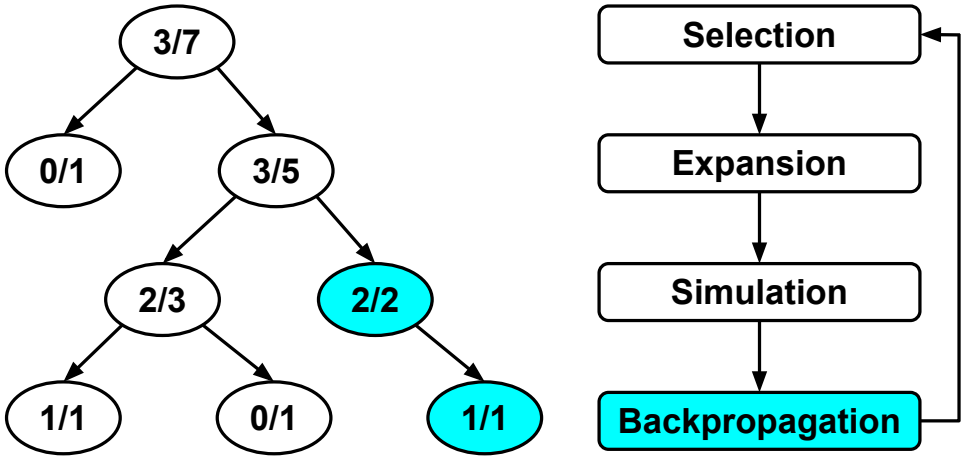

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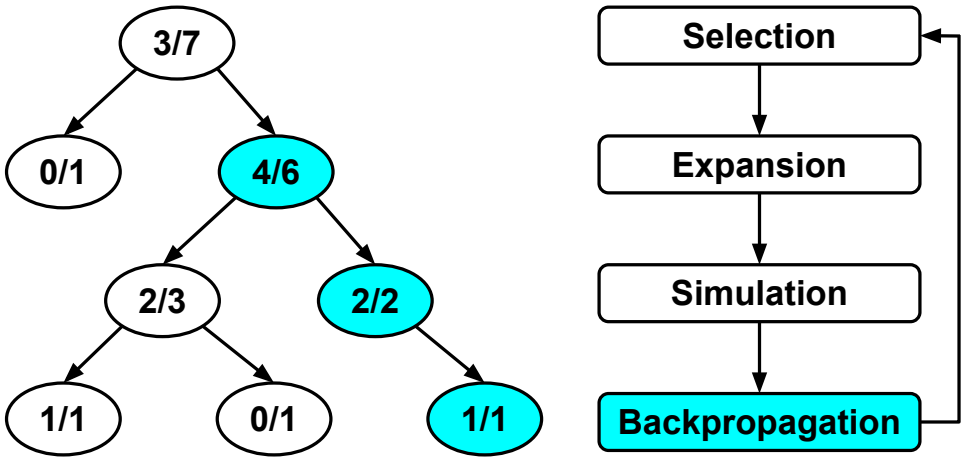

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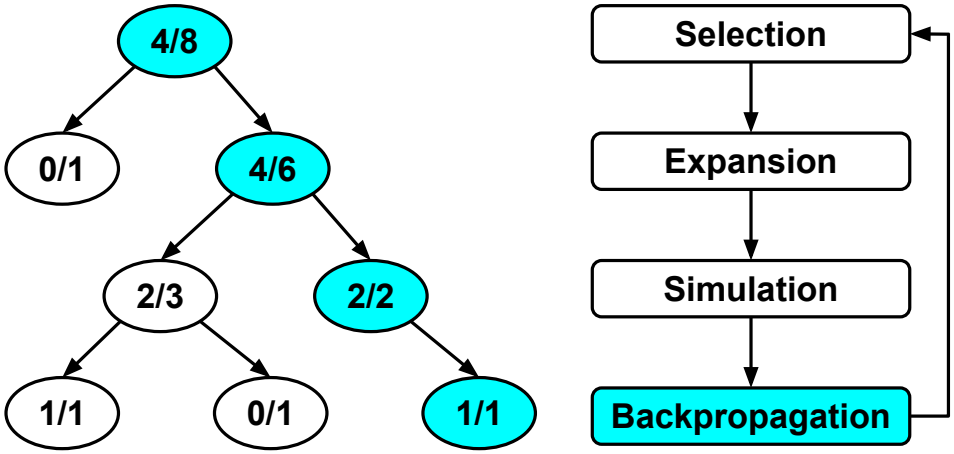


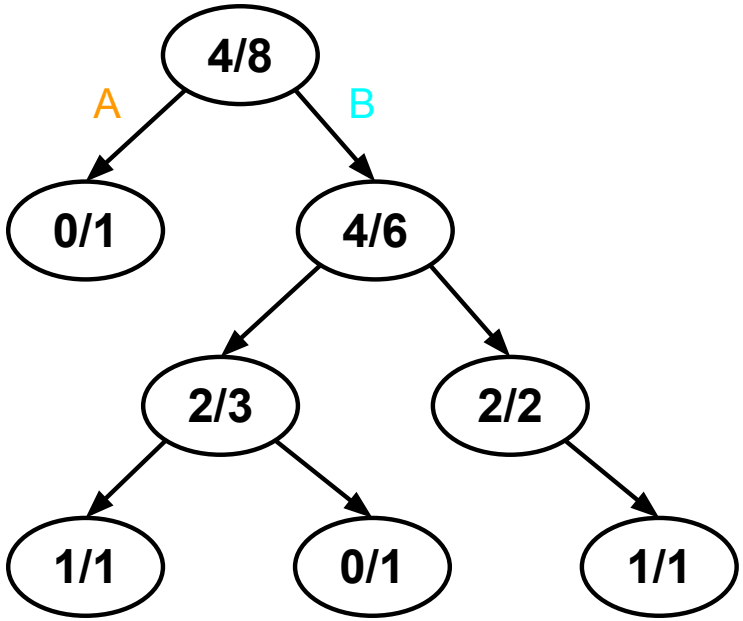
What Happens When We Choose a Move?

Now we have:

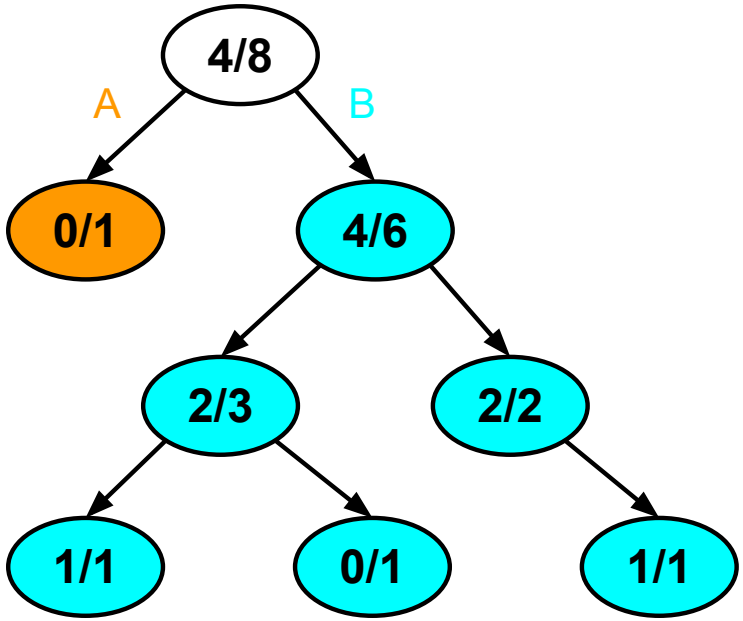
- A tree structure
- A method of generating the tree

What happens when we need to choose a move?

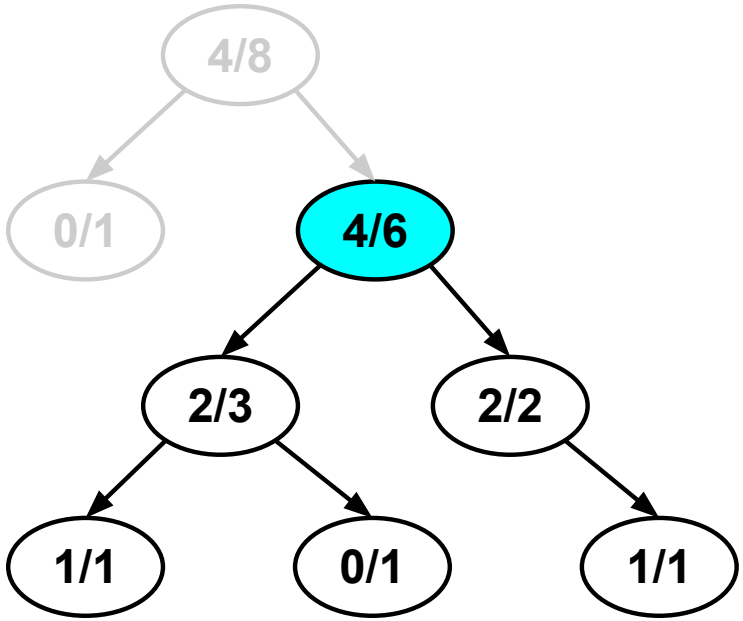
Choosing a Move



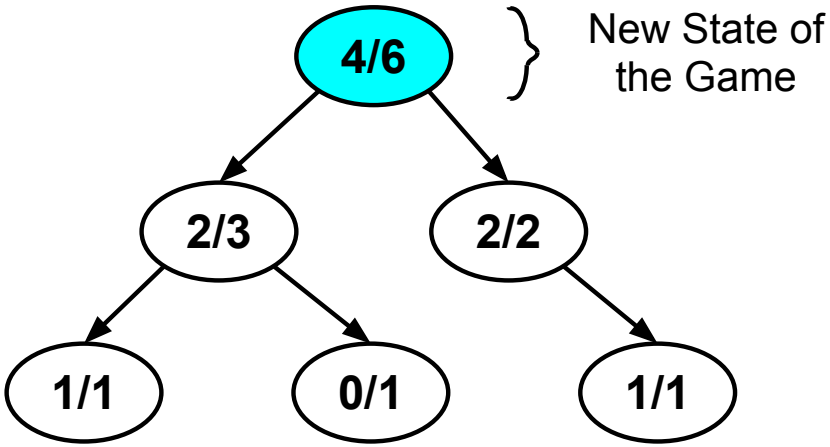
Choosing a Move



Choosing a Move



Choosing a Move



Exploration vs Exploitation

- We might overlook better paths
- Exploration vs Exploitation
  - Exploration looks at more options
  - Exploitation focuses on the most promising path
- Must find a balance between the two

Upper Confidence Bound Applied to Trees (UCT)

$$UCT(node) = \underbrace{\frac{W(node)}{N(node)}}_{\text{Value of the Node}} + \underbrace{c\sqrt{\frac{ln(N(parentNode))}{N(node)}}}_{\text{Exploration Bonus}}$$

- W represents the number of simulated wins
- N represents the total number of simulations
- C is an experimental constant
- Used during tree traversal
- Balances exploration vs exploitation

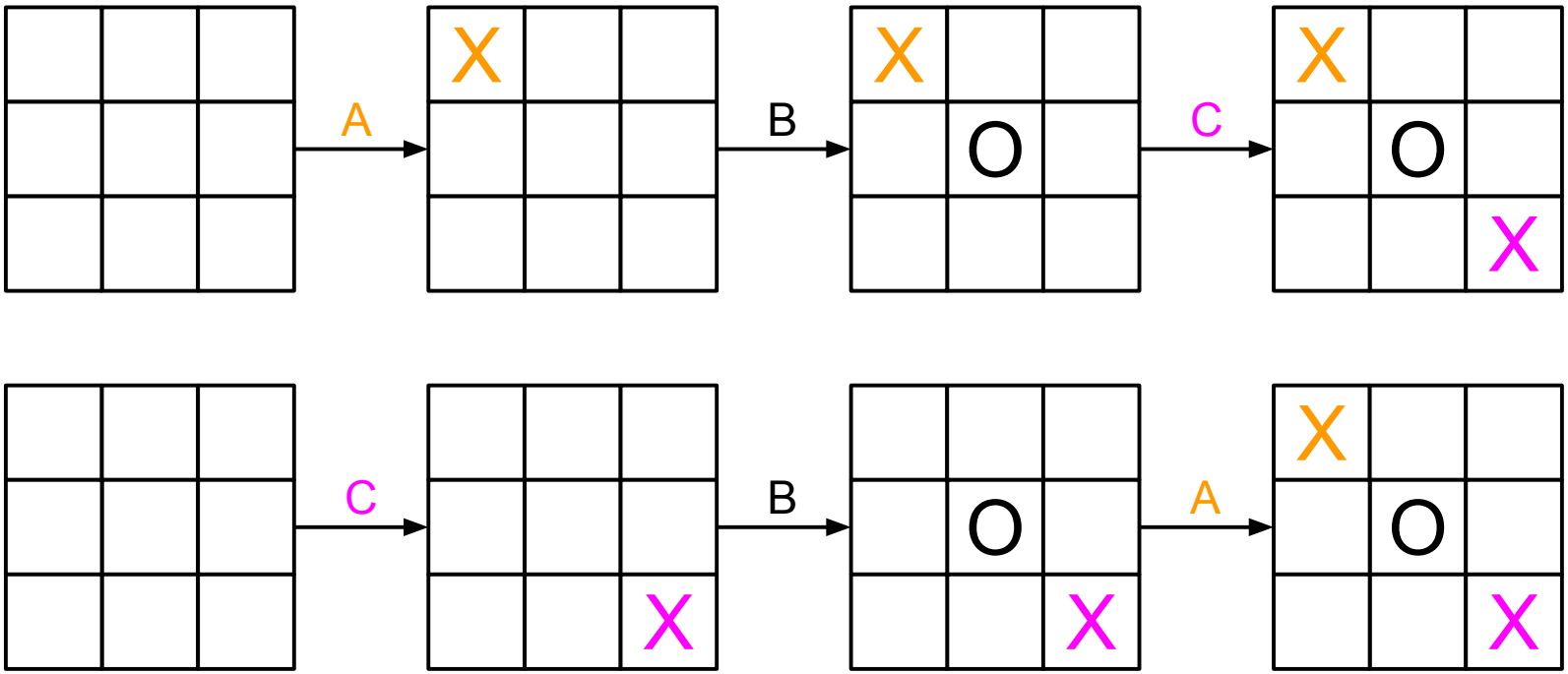
Outline

MCTS applied to Go

What variations can we make specific to Go?
In Go each player takes turn placing pieces on a game board

- How much does the order of these moves matter?
- Can we use this to improve MCTS in the context of Go?

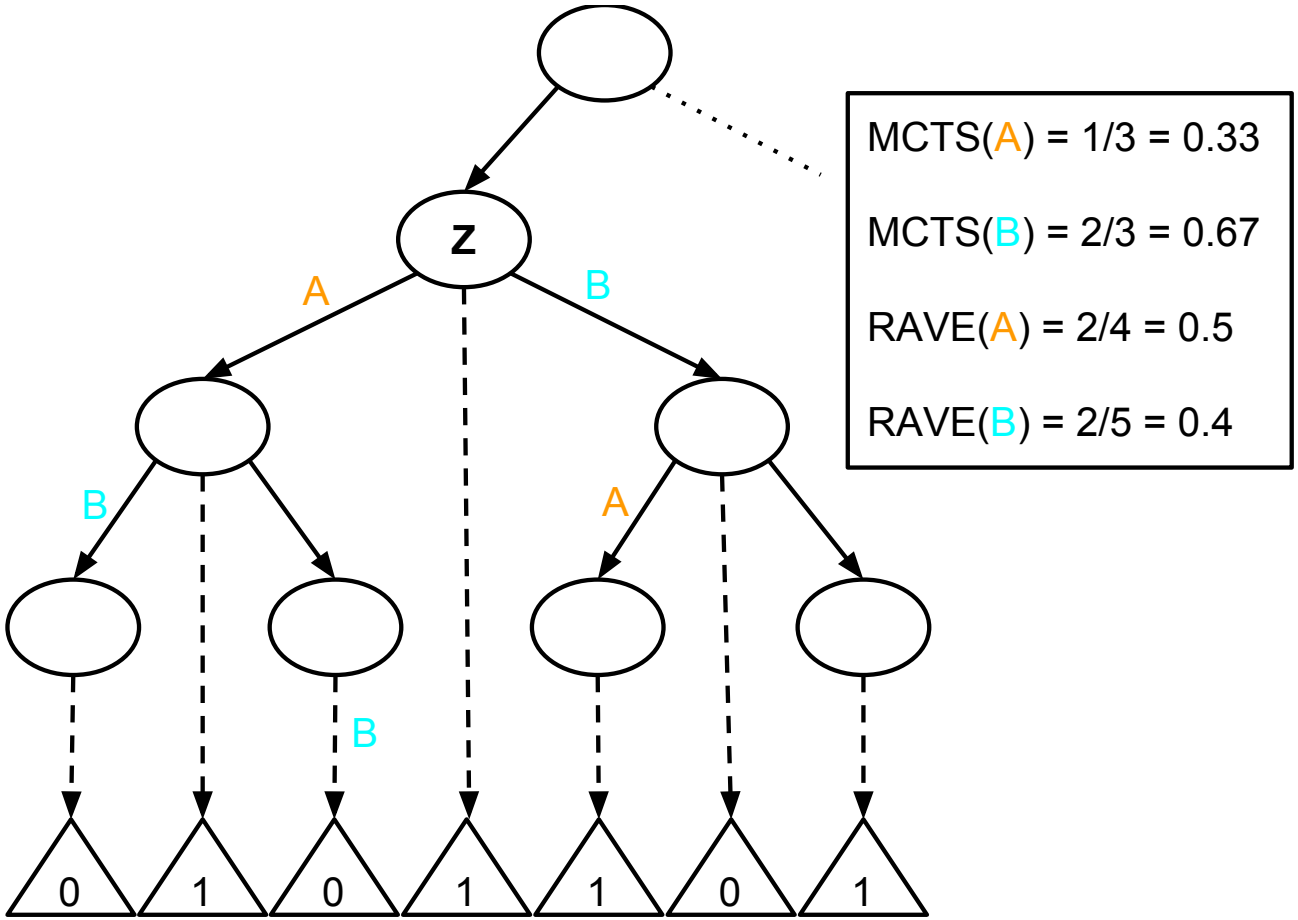
Tree Redundancy



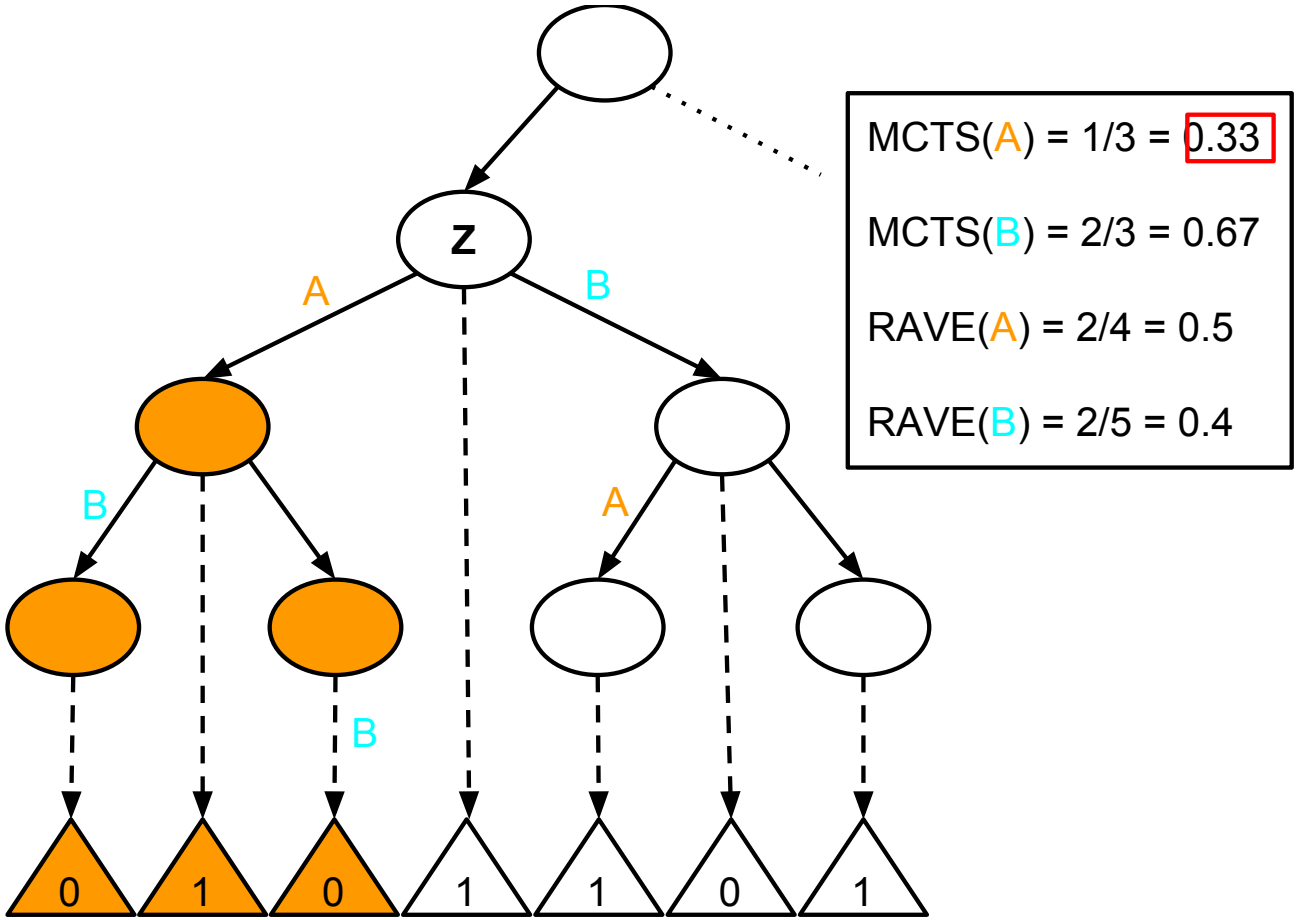
Rapid Action Value Estimate (RAVE)

- Takes advantage of tree redundancy
- Moves have no contextual dependencies
- Stores the value of a move with in a subtree at each node

RAVE Diagram



MCTS Values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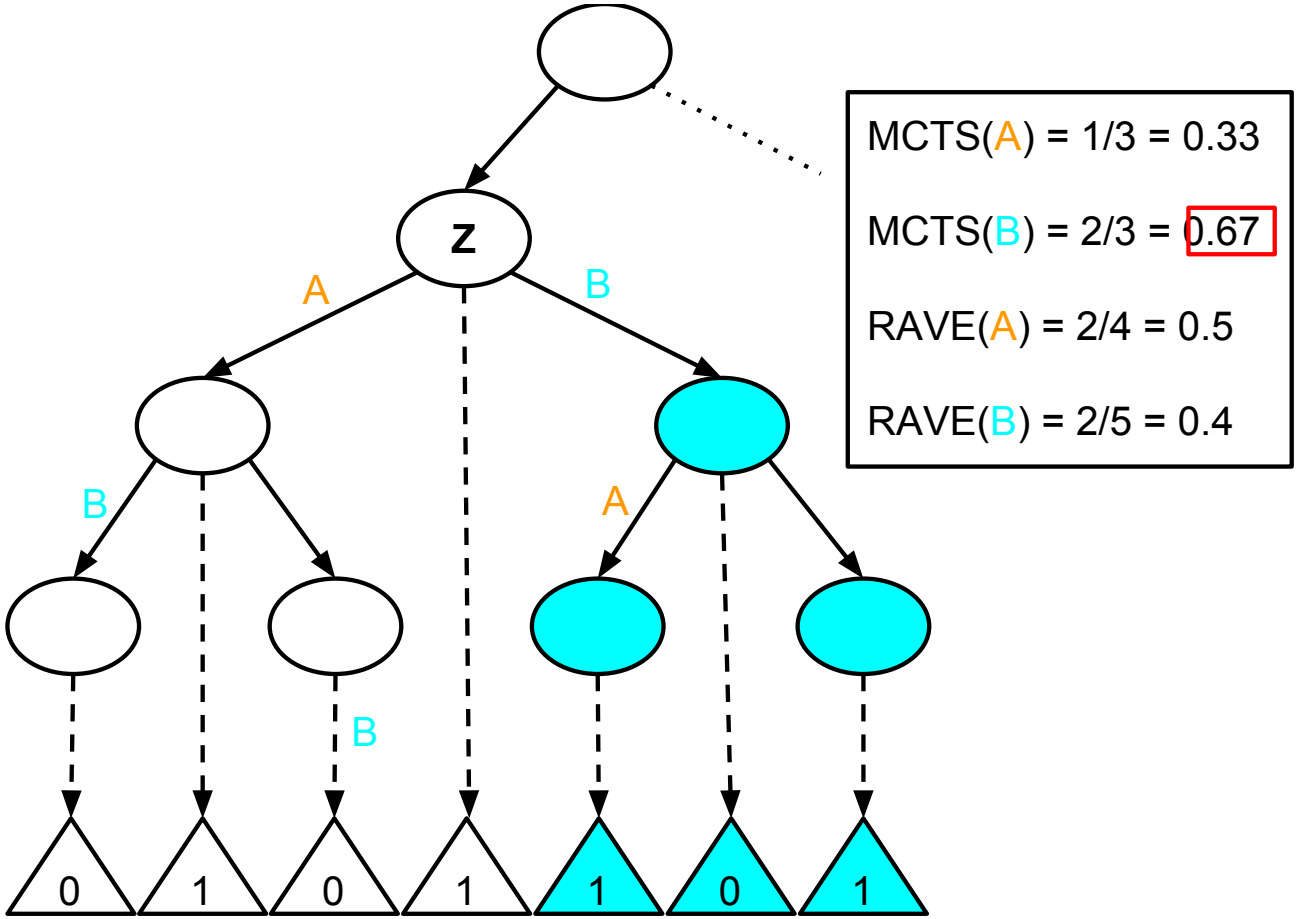
1
MCTS(A) = 1/3 = 0.33
MCTS(B) = 2/3 = 0.67
RAVE(A) = 2/4 = 0.5
RAVE(B) = 2/5 = 0.4

MCTS Values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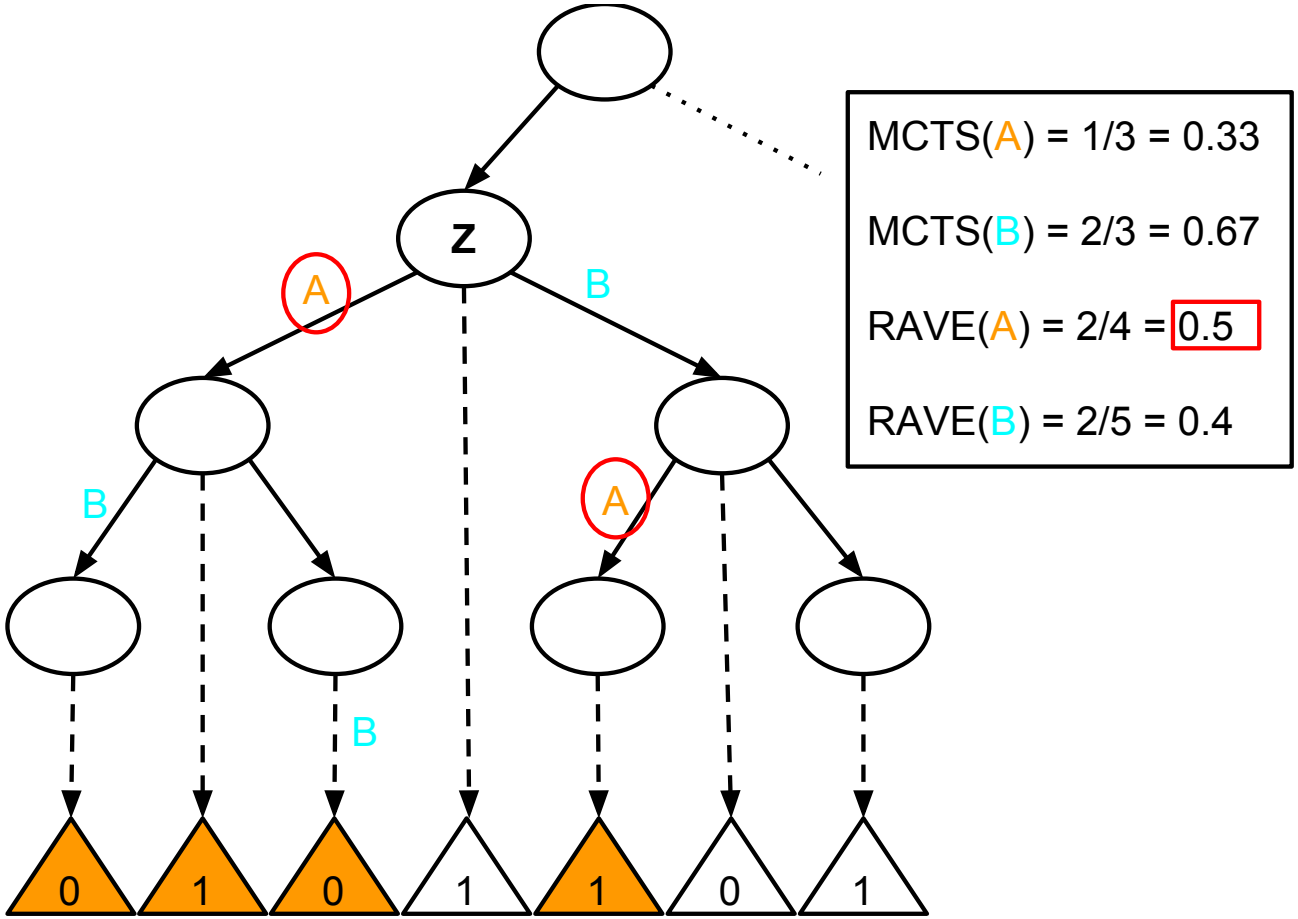
RAVE(A) = 2/4 = 0.5
RAVE(B) = 2/5 = 0.4

RAVE Values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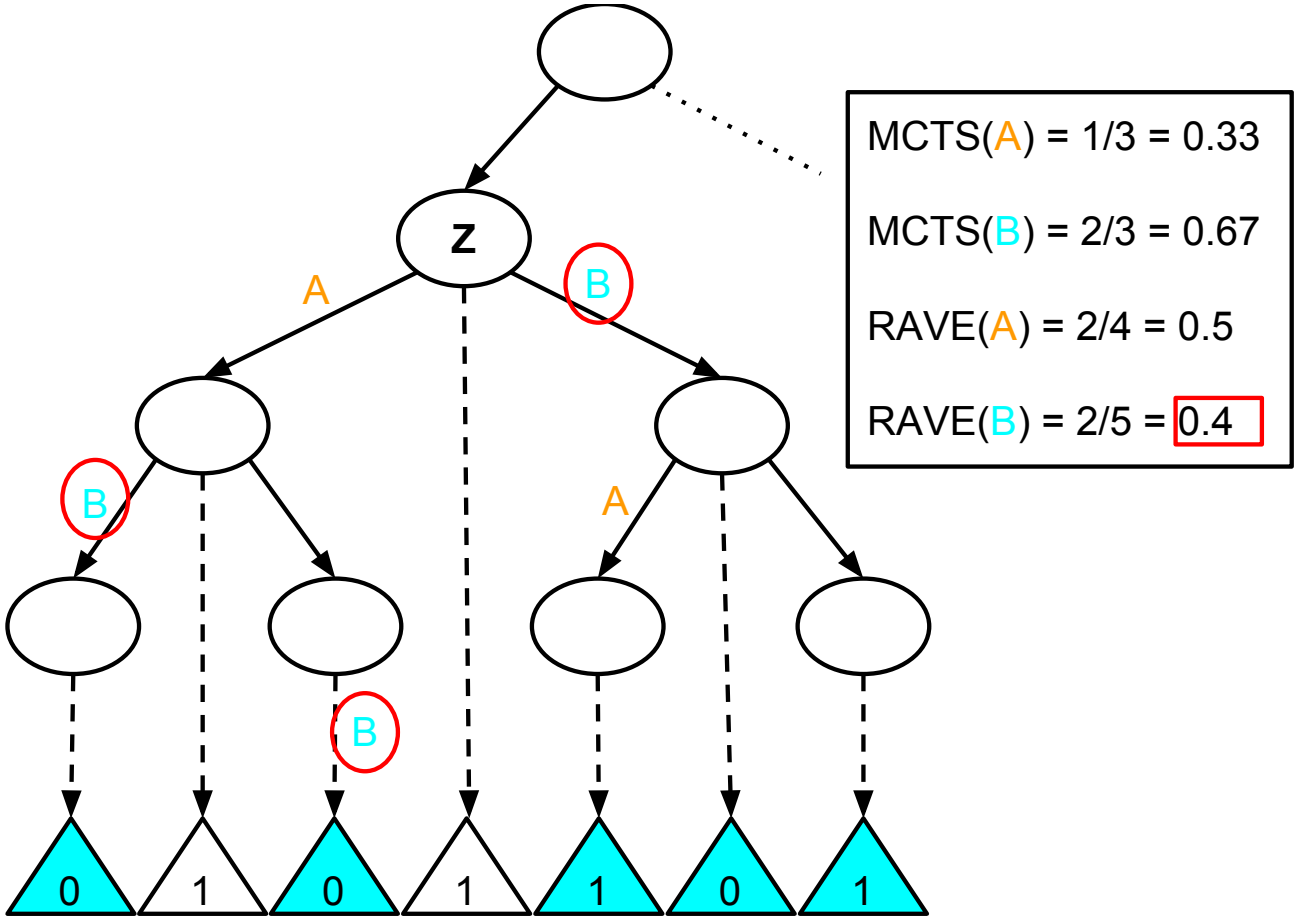
RAVE Values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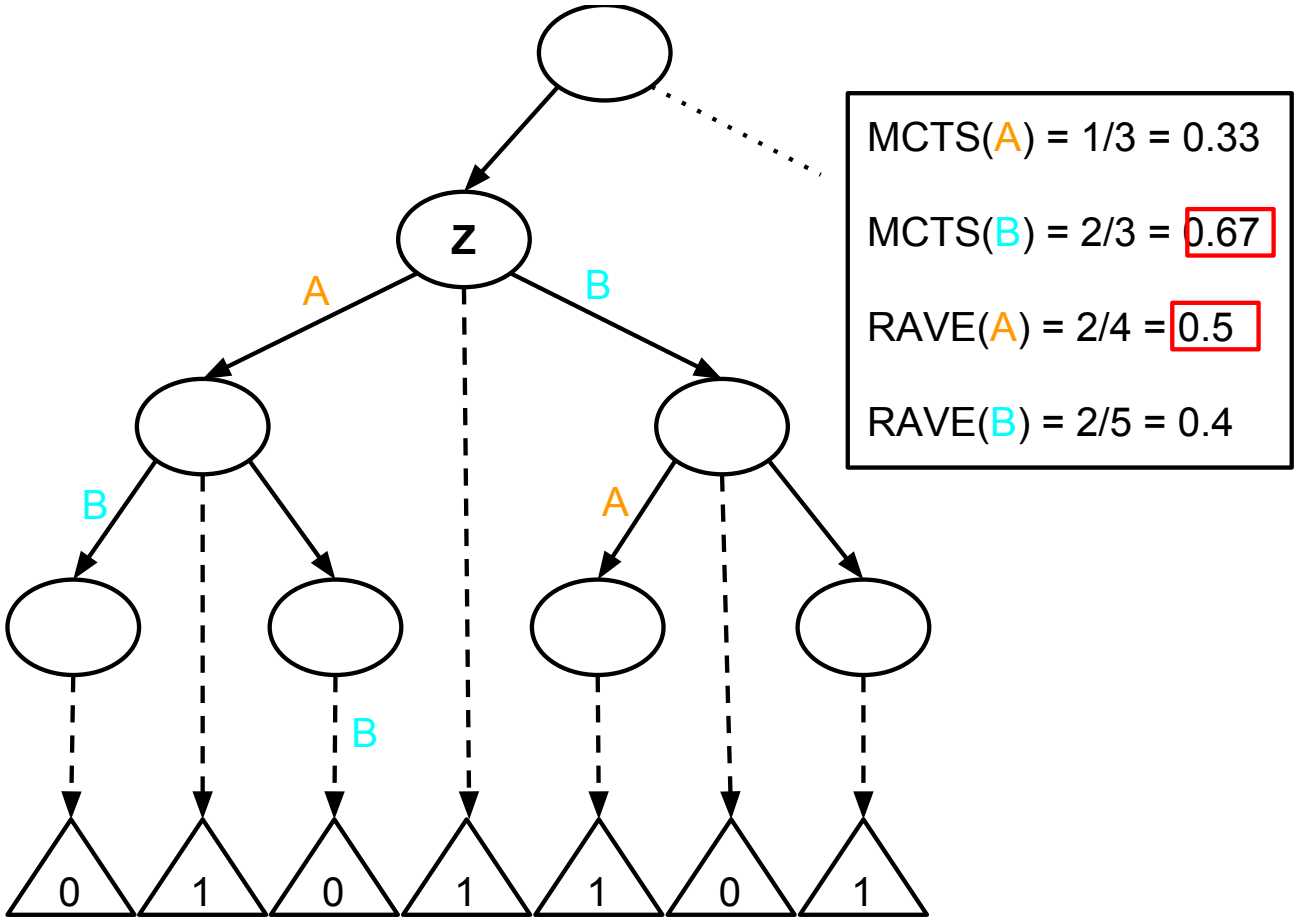
MCTS(B) = 2/3 = 0.67
RAVE(A) = 2/4 = 0.5
RAVE(B) = 2/5 = 0.4

MCTS RAVE Comparison



RAVE

- Very powerful approach
- Each simulation provides us with more information
- Sometimes we do need contextual dependencies
  - Example: Close tactical battles

MC RAVE

- Combines MCTS values with RAVE values
- Uses a weighted average
- Favors RAVE values when fewer simulations have been performed
  - Contextual dependencies are unknown
- Favors MCTS values when more simulations have been performed
  - Contextual dependencies are more developed

Go Results

- Deterministic approaches could hardly defeat low level amateurs
- Computer Go programs use MC RAVE
  - MoGo
  - Crazy Stone
- Can compete against top pros in 9x9 Go
- Can compete against top pros in handicapped 19x19 Go

Outline

Narrative Generation

Kartal et al applied MCTS to Narrative Generation

- Crime story
- User defines the set up and goals for the story
  - Example Setup: The detective starts in his office
  - Example Goal: The killer must be arrested

Unlike Go and other games

- Slightly different tree structure
- Evaluation function needed

Actions

- Actions drive the story
- Actions are believable based on context
  - Example: Inspector searches for clues
  - Example: Character A kills Character B

Example Actions

Move(A, P): A moves to place P.
Kill(A, B): B's health to zero(dead).
Earthquake(P): An earthquake strikes at place P.

- Actions take the place of moves as nodes
- No clear end state
- The researchers used a set threshold during simulation

Evaluation function

- Method of giving nodes value
- Incorporates believability and goal completion
- Ensures stories are interesting

Value(story) = Believability(story) * GoalCompletion(story)

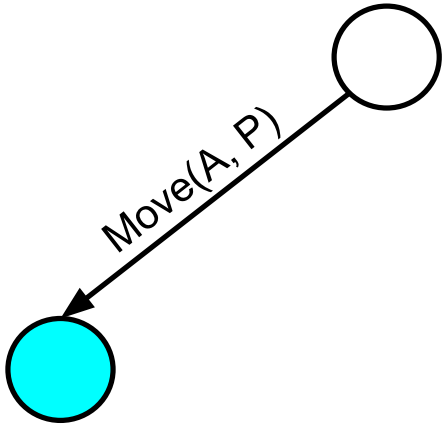
- The value is between 0 and 1
- Believability Mathematical product of every action in a story

Narrative Generation Test

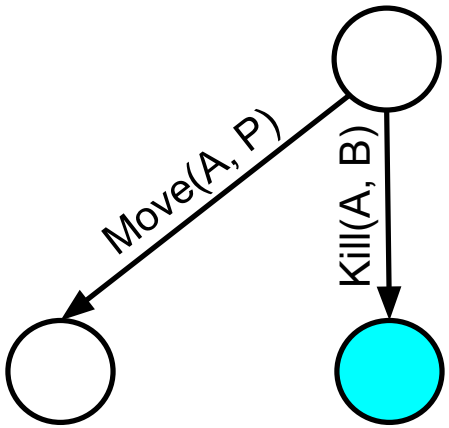
MCTS compared against three deterministic algorithms

- Breadth-first search
- Depth-first search
- Best-first search

Breadth-First Search



Breadth-First Search



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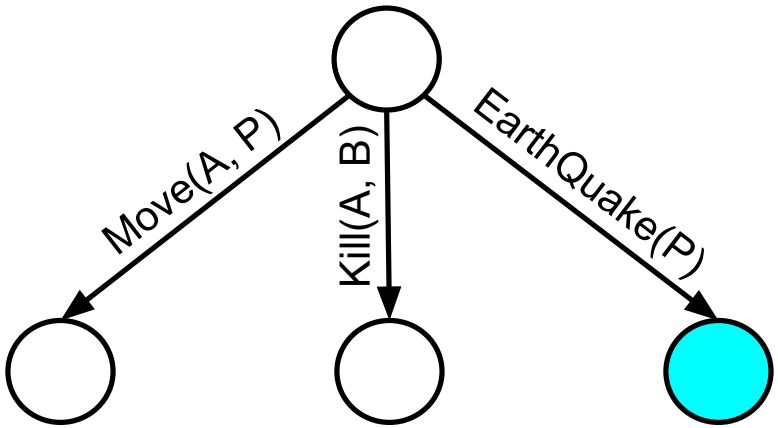
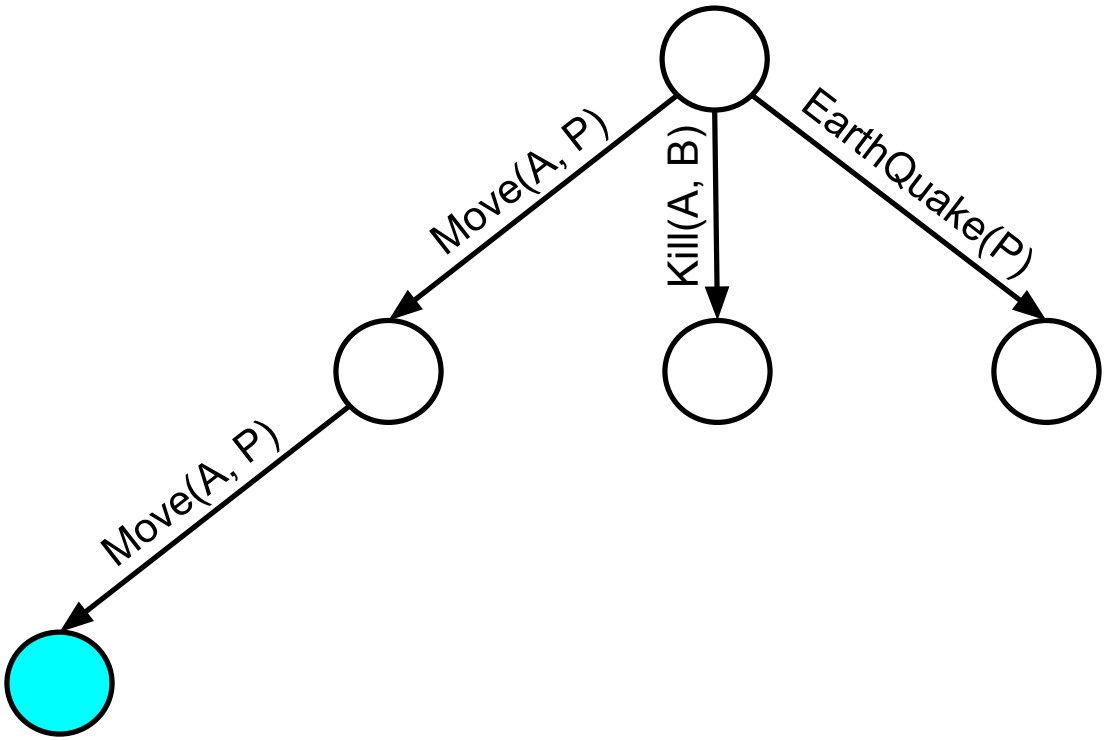


Breadth-First Search



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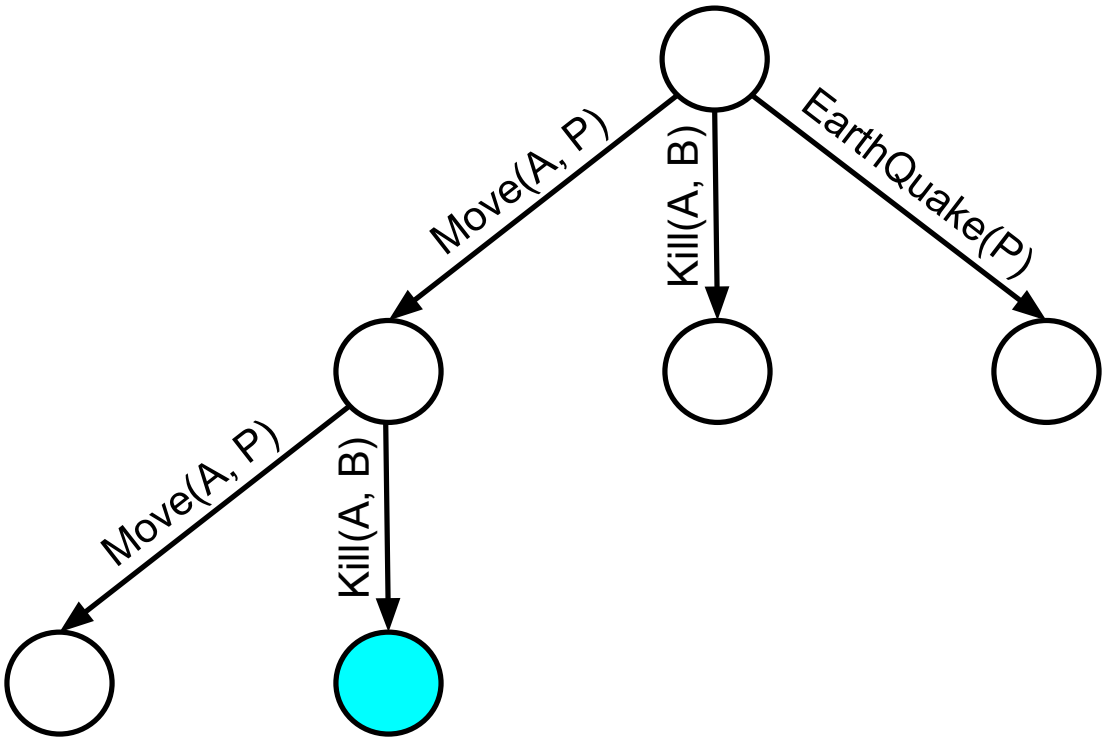
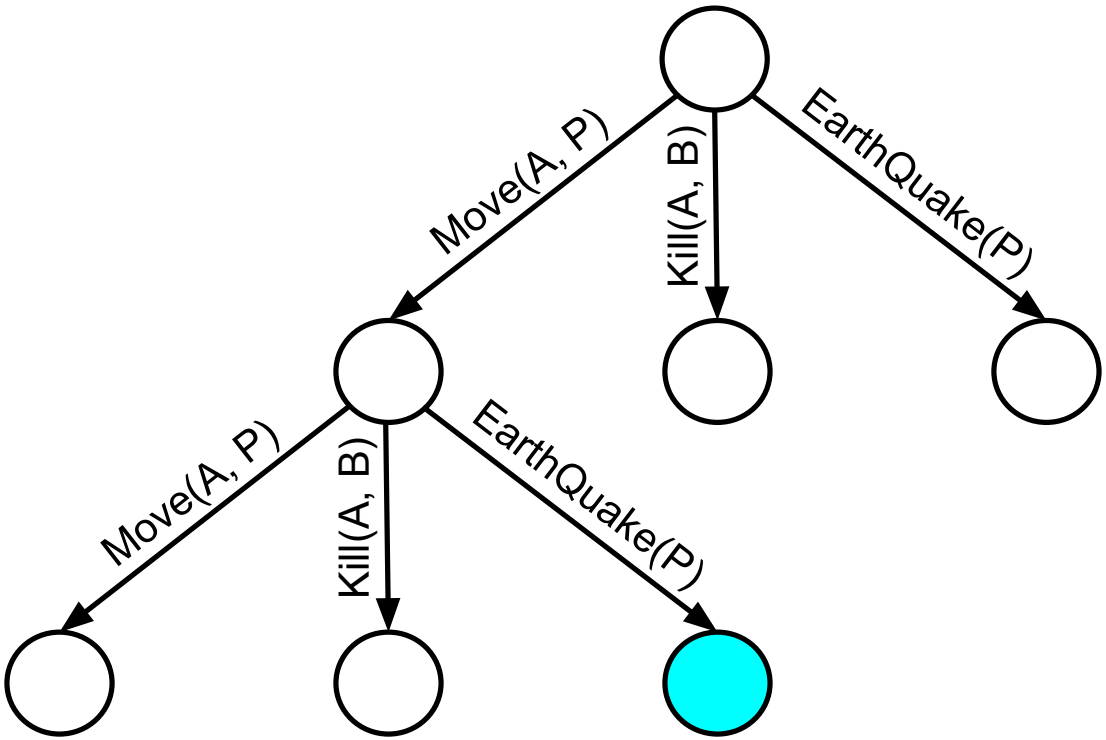
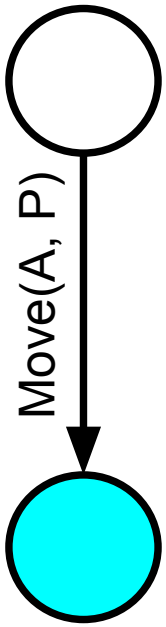


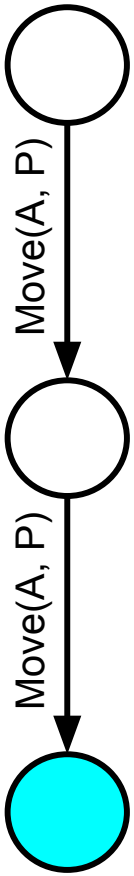
Breadth-First Search



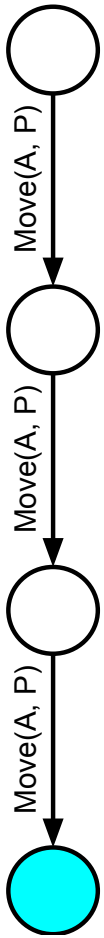
Depth-First Search



Depth-First Search



Depth-First Search



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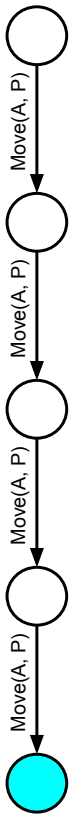

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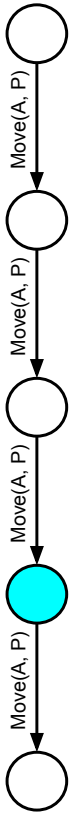

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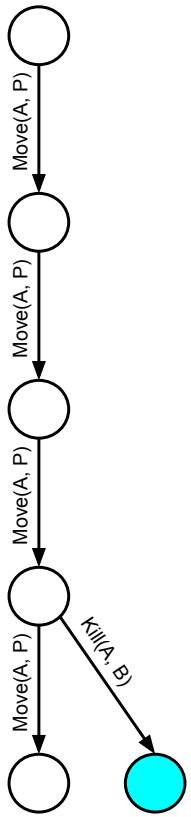
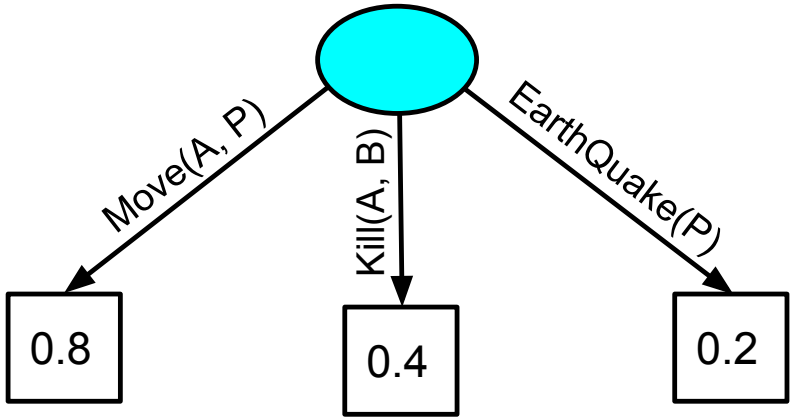
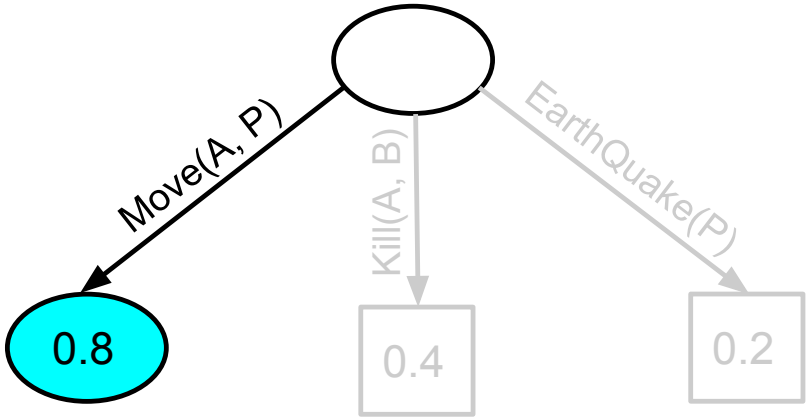


Best-First Search



Best-First Search



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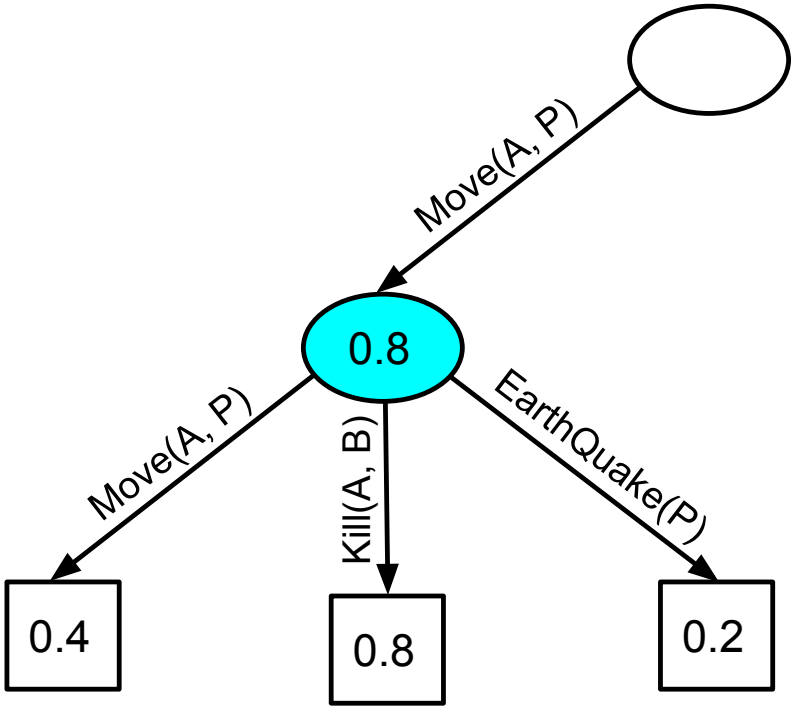

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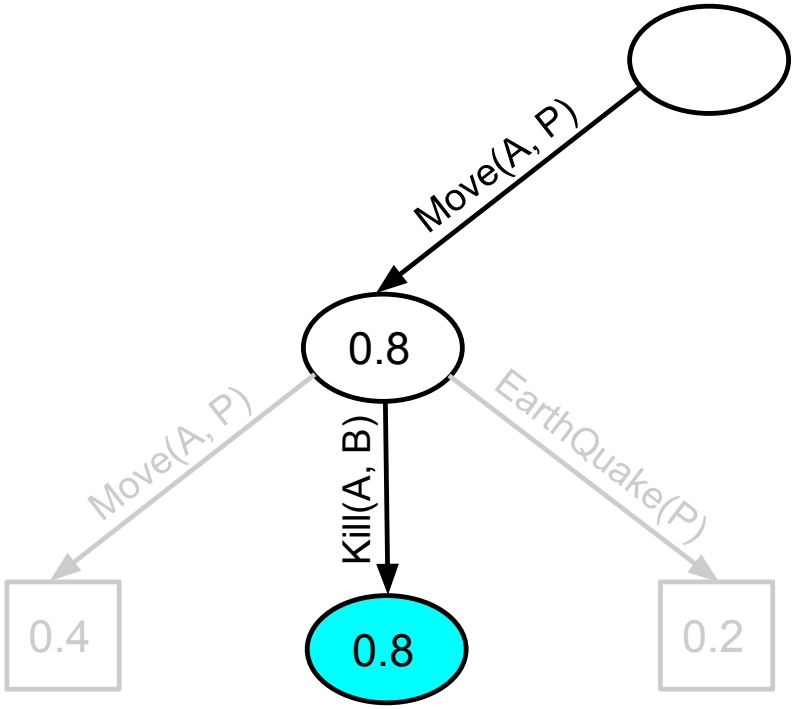
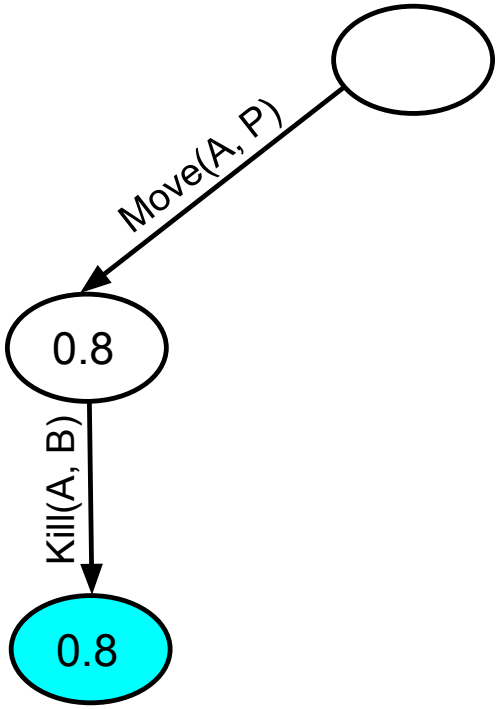


Best-First Search



Test Conditions

Goals for the narrative:

- At least two people are killed
- The killer is arrested

Each algorithm was given two budgets

- 100,000 nodes
- 3 million nodes

Each algorithm ran three times
The score of the narratives were averaged

Results

	MCTS	Breadth-first	Depth-first	Best-first
Low Budget	0.07	0.05	<0.001	0.005
High Budget	0.9	0.06	<0.01	<0.01

- MCTS performed the best in both
- Breadth-first came the closest out of the deterministic algorithms

Stories Produced by MCTS

- Stories from MCTS tended to be believable
- Completed both user defined goals
- Some Problems
- Overall reasonable narratives

Low Scoring Example from Breadth-First

Sherlock moved to Alice's House. An Earthquake occurred at Alice's House! Sherlock and Alice both died due to the earthquake.

Outline

Conclusion

- MCTS successful in extending AI capabilities
- Tackles problems with larger search spaces
- Effective in Go and Narrative Generation
- Applicable to other problems
  - Can outperform humans in many puzzles
  - Real time games
  - Super Mario Brothers

Any Questions?