Short Problem Set 9

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1 Problem 1

Question: Describe in your own words the process described in the course text to efficiently identify near duplicate documents in a large collection.

Answer:

2 Problem 2

Question: Give a short definition or explanation of the following concepts:

1. web spam
2. near duplicate
3. in-degree
4. robot exclusion protocol
5. priority queue (in the context of web crawling)

Answer:

3 Problem 3

Question: For this problem work with the directed web graph shown below. In the graph there are six nodes: S, B, F, G, T, and I (for the websites Snapchat, Bing, Facebook, Google, Twitter, and Instagram). Use a teleport probability of 0.25. Assume no other pages or links exist beside those shown in the figure.

(a) Provide (i.e., write) the six recurrence equations that indicate how to iteratively calculate the PageRank score of each page at time t given scores from time t-1.

Answers:
$PR(S, t_i) = 0.042 + .75 * 0 = 0.042$
$PR(B, t_i) = 0.042 + .75 * (PR(S, t_{i-1})/2 + PR(G, t_{i-1})/2 + PR(F, t_{i-1})/1)$
$PR(F, t_i) = 0.042 + .75 * (PR(T, t_{i-1})/2)$
$PR(G, t_i) = 0.042 + .75 * (PR(S, t_{i-1})/2 + PR(B, t_{i-1})/2)$
$PR(T, t_i) = 0.042 + .75 * (PR(B, t_{i-1})/2 + PR(G, t_{i-1})/2)$
$PR(I, t_i) = 0.042 + .75 * (PR(T, t_{i-1})/2)$

(b) Using the brute-force iterative method of calculation shown in the video lecture calculate two iterations of PageRank scores for each page in the graph. Be sure to show scores at times t=0, t=1, and finally at t=2. Report scores using three digits of precision (e.g., 0.247, not 0.2 or 0.24696485932). Show work and do not merely provide a table of values.

At $t = 0$ let $PR(X) \approx 1/6$ since we have 6 pages.

	S	B	F	G	T	I
$t = 0$	.167	.167	.167	.167	.166	.166

At $t = 1$:
$PR(S, 1) = 0.042 + .75 * 0 = 0.042$

$PR(B, 1) = 0.042 + .75 * (PR(S, t_{i-1})/2 + PR(G, t_{i-1})/2 + PR(F, t_{i-1})/1)$
$PR(B, 1) = 0.042 + .75 * (.167/2 + .167/2 + .167/1)$
$PR(B, 1) = 0.042 + .75 * (0.334)$
$PR(B, 1) = 0.293$

$PR(F, 1) = 0.042 + .75 * (PR(T, t_{i-1})/2)$
$PR(F, 1) = 0.042 + .75 * (.166/2)$
$PR(F, 1) = 0.042 + .75 * (0.083)$
$PR(F, 1) = 0.104$

$PR(G, 1) = 0.042 + .75 * (PR(S, t_{i-1})/2 + PR(B, t_{i-1})/2)$
$PR(G, 1) = 0.042 + .75 * (0.167/2 + 0.167/2)$
$PR(G, 1) = 0.042 + .75 * (0.167)$
$PR(G, 1) = 0.167$

$PR(T, 1) = 0.042 + .75 * (PR(B, t_{i-1})/2 + PR(G, t_{i-1})/2)$
$PR(T, 1) = 0.042 + .75 * (0.167/2 + 0.167/2)$
$PR(T, 1) = 0.042 + .75 * (0.167)$
$PR(T, 1) = 0.167$

$PR(I, 1) = 0.042 + .75 * (PR(T, t_{i-1})/2)$
$PR(I, 1) = 0.042 + .75 * (.167/2)$
$PR(I, 1) = 0.042 + .75 * (0.0835)$
$PR(I, 1) = 0.104$

	S	B	F	G	T	I
$t = 0$	.167	.167	.167	.167	.166	.166
$t = 1$	.042	0.293	0.104	0.167	0.167	0.104

At $t = 2$:
$PR(S, 2) = 0.042 + .75 * 0 = 0.042$

$PR(B, 2) = 0.042 + .75 * (PR(S, t_{i-1})/2 + PR(G, t_{i-1})/2 + PR(F, t_{i-1})/1)$
$PR(B, 2) = 0.042 + .75 * (0.042/2 + 0.167/2 + 0.104/1)$
$PR(B, 2) = 0.042 + .75 * (0.2085)$
$PR(B, 2) = 0.198$

$PR(F, 2) = 0.042 + .75 * (PR(T, t_{i-1})/2)$
$PR(F, 2) = 0.042 + .75 * (0.167/2)$
$PR(F, 2) = 0.042 + .75 * (0.0835)$
$PR(F, 2) = 0.105$

$PR(G, 2) = 0.042 + .75 * (PR(S, t_{i-1})/2 + PR(B, t_{i-1})/2)$
$PR(G, 2) = 0.042 + .75 * (0.042/2 + 0.293/2)$
$PR(G, 2) = 0.042 + .75 * (0.1675)$
$PR(G, 2) = 0.168$

$PR(T, 2) = 0.042 + .75 * (PR(B, t_{i-1})/2 + PR(G, t_{i-1})/2)$
$PR(T, 2) = 0.042 + .75 * (0.293/2 + 0.167/2)$

$PR(T, 2) = 0.042 + .75 * (0.23)$
$PR(T, 2) = 0.215$

$PR(I, 2) = 0.042 + .75 * (PR(T, t_{i-1})/2)$
$PR(I, 2) = 0.042 + .75 * (0.167/2)$
$PR(I, 2) = 0.042 + .75 * (0.0835)$
$PR(I, 2) = 0.105$

	S	B	F	G	T	I
$t = 0$	.167	.167	.167	.167	.166	.166
$t = 1$	.042	0.293	0.104	0.167	0.167	0.104
$t = 2$	0.042	0.198	0.105	0.168	0.215	0.105

(c) Which page (or pages) has/have the lowest PageRank score after two iterations?
S(Snapchat) has the lowest PageRank score after two iterations.

(d) Which page (or pages) has/have the highest PageRank score after two iterations?
T(Twitter) has the highest PageRank score after two iterations.

(e) For part e only, suppose that we set the teleport probability in the PageRank equation to zero (0) and we let the PageRank algorithm run for many iterators (say 50 iterations). Explain succinctly what the important consequence or consequences of this choice would be? Justify your reasoning.