演示报告 (内容为示例简述特征向量) 标题小字 (示例全英, 可自行修改为中文)

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- 1 图片与枚举示例
- 2 公式显示示例 Vector in Geometry
- 3 公式显示示例 Determinant in Geometry
- 4 公式显示示例 Eigenvalue in Geometry
- 5 参考文献示例 Refference





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Review of Higher Algebra



■ Full of matrix







- Full of matrix
- No geometric graphics at all







- Full of matrix
- No geometric graphics at all
- Not intuitive





Review of Higher Algebra









- 2 公式显示示例 Vector in Geometry

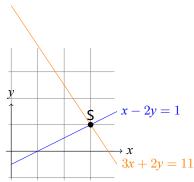




Introduce a linear simultaneous equations

$$x - 2y = 1$$

 $3x + 2y = 11$ (1)



Row picture:

$$x - 2y = 1$$
$$3x + 2y = 11$$

Point S = (3, 1) is the solution.

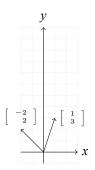


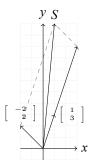


Vector

Column picture:

$$x \begin{bmatrix} 1 \\ 3 \end{bmatrix} + y \begin{bmatrix} -2 \\ 2 \end{bmatrix} = \begin{bmatrix} 1 \\ 11 \end{bmatrix}$$
 (2)





Where we take

$$\left[\begin{array}{c} -2 \\ 2 \end{array}\right]$$
 and $\left[\begin{array}{c} 1 \\ 3 \end{array}\right]$

as vectors,

when
$$x = 3$$
, $y = 1$, the $b = \begin{bmatrix} 1 \\ 11 \end{bmatrix}$





- 3 公式显示示例 Determinant in Geometry





Coefficient matrix
$$A = \begin{bmatrix} 3 & 1 \\ 0 & 2 \end{bmatrix}$$
 is also a rectangular matrix.

$$det(A) = \left| \begin{array}{cc} 3 & 1 \\ 0 & 2 \end{array} \right| = 6$$

Obvious matrix A has two vectors: $\begin{bmatrix} 3 \\ 0 \end{bmatrix}$, $\begin{bmatrix} 1 \\ 2 \end{bmatrix}$



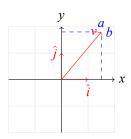


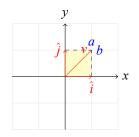
Unit vectors in the 2-dimensional plane are $\hat{i} = \begin{bmatrix} 1 \\ 0 \end{bmatrix}$, $\hat{j} = \begin{bmatrix} 0 \\ 1 \end{bmatrix}$.

$$a \cdot i + b \cdot j$$

$$= a \begin{bmatrix} 1 \\ 0 \end{bmatrix} + b \begin{bmatrix} 0 \\ 1 \end{bmatrix}$$

$$= \begin{bmatrix} a \\ b \end{bmatrix}$$





 $a \cdot i + b \cdot j$ is a linear transformations. a = 1, b = 1, then area is 1.

$$\mathsf{also} \left[\begin{array}{c} i & j \end{array} \right] \left[\begin{array}{c} a \\ b \end{array} \right] = \left[\begin{array}{c} a \\ b \end{array} \right] \quad \Rightarrow \quad \left[\begin{array}{c} 1 & 0 \\ 0 & 1 \end{array} \right] \left[\begin{array}{c} a \\ b \end{array} \right] = \left[\begin{array}{c} a \\ b \end{array} \right]$$



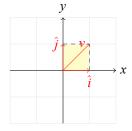


Hense, we can tell that

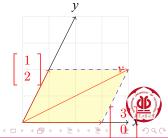
$$\left[\begin{array}{cc} 3 & 1 \\ 0 & 2 \end{array}\right] \left[\begin{array}{c} a \\ b \end{array}\right] = \left[\begin{array}{cc} 3 & 1 \\ 0 & 2 \end{array}\right] \left[\begin{array}{cc} 1 & 0 \\ 0 & 1 \end{array}\right] \left[\begin{array}{c} a \\ b \end{array}\right]$$

Which is actually the original two-dimensional space of the unit vector is linearly transformed. $\rightarrow \times \begin{bmatrix} 3 & 1 \\ 0 & 2 \end{bmatrix}$

$$\hat{i} = \left[egin{array}{c} 1 \\ 0 \end{array}
ight]
ightarrow \left[egin{array}{c} 3 \\ 0 \end{array}
ight] \hspace{0.2cm} , \hspace{0.2cm} \hat{j} = \left[egin{array}{c} 0 \\ 1 \end{array}
ight]
ightarrow \left[egin{array}{c} 1 \\ 2 \end{array}
ight]$$

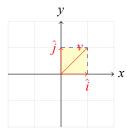




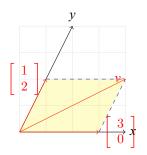


Determinant in Geometry

Since
$$\begin{vmatrix} 3 & 1 \\ 0 & 2 \end{vmatrix} = 6$$
, Area: $1 \rightarrow 6$



Area scaled by 6 times.



We can conclude that:

The Determinant in Geometry is how much are areas scaled.



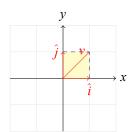
(内容为示例简述特征向量)

CONTENT

- 4 公式显示示例 Eigenvalue in Geometry

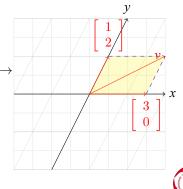






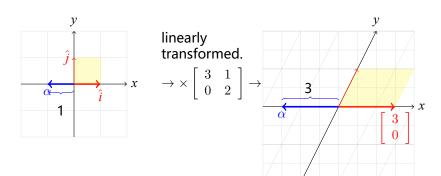
linearly transfórmed.

$$\rightarrow x \qquad \rightarrow \times \left[\begin{array}{cc} 3 & 1 \\ 0 & 2 \end{array} \right] \rightarrow$$





Vectors remain on their own span

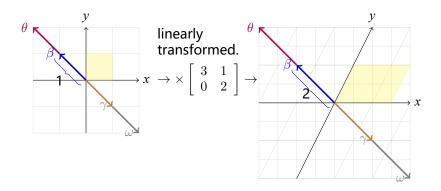


 $\overrightarrow{\alpha}$ remains on the line of the x-axis, stretched by a factor of **3**.





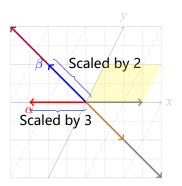
Vectors remain on their own span



 $\overrightarrow{\beta}$ remains on the line of the x-axis, stretched by a factor of **2**.

The other vectors(γ, θ, ω) on the line are also stretched by a factor of 2



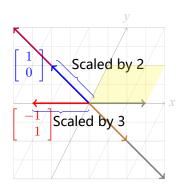


The vector representing these lines are

$$\begin{bmatrix} 1 \\ 0 \end{bmatrix}, \begin{bmatrix} -1 \\ 1 \end{bmatrix}$$







$$A = \left[\begin{array}{cc} 3 & 1 \\ 0 & 2 \end{array} \right]$$

The vector representing the line is called the eigenvector of the matrix A.

特征向量:
$$\begin{bmatrix} 1 \\ 0 \end{bmatrix}$$
, $\begin{bmatrix} -1 \\ 1 \end{bmatrix}$

The eigenvalue of the matrix A is just the factor by which it stretched or squashed during the transformation

特征值:2,3





Eigenvalue & Eigenvector

So maybe you can tell why we can get eigenvalue of matrix from this equation:

$$Ax = \lambda x$$





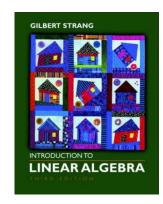
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Refference

Introduction to Linear Algebra(Strang)



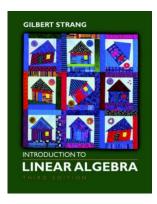




Refference

Introduction to Linear Algebra(Strang)

■ Essense of Linear Algebra @3Blue1Brown





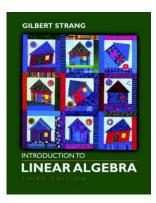


Refference

Introduction to Linear Algebra(Strang)

■ Essense of Linear Algebra @3Blue1Brown

■ Linear algebra and its applications 4th







Acknowledgements

Thank you for listening!



