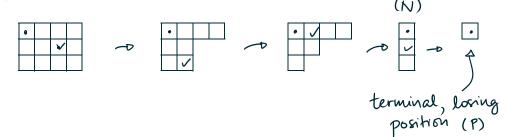
* Further examples of games (impartial, combinatorial)

* Chomp

Starting state: an MXN bar of chocolate

poisoned by A move consists of picking a square and eating all the chocolate below &

to the right. The person who cannot eat any non-poisoned squaves loser (So 1x1 is a losing position)



** Sprouts

Starting state = a number of dots

Moves: Connect two existing dots by a (curved) line, not passing through any existing dots, and draw a third dot on your segment, making sure that no dot has > 3 incident

this spot can no longer be connected to anything

[Look up on wikipedia!]

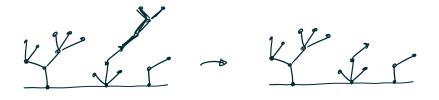
** Kayles [Look up on wikipedia]

** Hackenbush



State: A number of trees connected to the ground.

Move: Snip a single edge Anything no longer connected to the ground disappears



** All games above have lots of variants!

** Recap: In principle, we can analyse any of these games!

- 1) Draw the game graph from the starting position
- 2) Label the terminal positions as "P"
- 3) Work backwards, labelling positions as "N" or "P".

But this gets complicated quickly!

** Back to nim

Some special cases (k>0)

- 1) A single pile of k, bemies is trivially "N".
- 2) Two equal piles: (k,k) with k>o.

 This is a "P" position.

 The previous player uses a "mirroring" strategy:

 If the next move is (k-m, k),

 the move after that should be (k-m,k-m).

Eg. (4,4) no (4,2) no (2,2)Q a (k,k) type position again

** Key: (k,k) cannot lead to (0,0)

3) Two unequal piles (m,n) with m + n.
is an "N" position.
Winning strategy: Equalise the piles

Eg: (4,7) no (4,4)

** General case (3 or more piles).

Eg. (2,1,3) ~ "P"

What are some bad mover for the next player?

- Eating a whole pile (any of the three).
- (2,1,2) is bad.
- -(2,1,1), (1,1,3) are bad.
- > no good moves...

Eg: (4,5,17) ??

Next goal: Find a "value" for each game state, from which the bosing positions are clear