Source code:

```
import math
import random
# check if a number is prime
def check prime(a):
  if(a==2):
     return True
  elif((a<2) \text{ or } ((a\%2)==0)):
     return False
  elif(a>2):
     for i in range(2,a):
       if not(a%i):
         return False
  return True
# set random p and q (there is performance issue so I set the limit to 10000)
p = int(random.random()*10000)
q = int(random.random()*10000)
while not(check prime(p)):
  p = int(random.random()*10000)
while not(check prime(q)):
  q = int(random.random()*10000)
# print out p and q
print("p = " + str(p))
print("q = " + str(q))
# calculate n
n = p*q
# calculate phi(n)
phi n = (p-1)*(q-1)
# calculate e
# we have to make sure that e and phi n are relative prime
# check if e and phi n have a GCD of 1
def check_gcd(e,phi_n):
  while(phi n!=0):
     e,phi n=phi n,e%phi n
  return e
```

```
# find e and make it small for easier calculation
for i in range(20):
  if check gcd(i, phi n)==1:
     e = i
# print e out
print("e = " + str(e))
# calculate d
for i in range(phi n):
  if (e^*i)%phi n == 1:
     d = i
     break
# print d
print("d = " + str(d))
# input message
M = int(input("Enter message: "))
# calculate ciphertext C
C = pow(M, e, n)
# print ciphertext C
print("Encrypted message = " + str(C))
# calculate original message M
ori M = pow(C, d, n)
# print original message
print("Decrypted message = " + str(ori_M))
```

RESULT

```
zhaohanzhang@zhaohanzhangdeMacBook-Air ~ % /usr/local/bin/python3 "/Users/zhaohanzhang/Desktop/Spring2
22/CS3710/programming assignment/programming assignment 2/programming assignment2.py"

p = 2963

q = 7573

e = 19

d = 1180435

Enter message: 5678980

Encrypted message = 3038269

Decrypted message = 5678980

zhaohanzhang@zhaohanzhangdeMacBook-Air ~ % ■
```