

Newton's Raphson method

It involves the use of Initial guess x_0 , tolerance, and maximum iterations are provided as inputs. The method recursively looks for roots. Moreover, the function needs the derivative, which is represented by the symbol $df(x)$.

CODE:

```
%%timeit -r 4 -n 10000
#newton raphson
import numpy as np

f = lambda x: x**4 - 2
f_prime = lambda x: 4*x**3

def newton(f, df, x0, tol):
    # output is an estimation of the root of f using the Newton Raphson method
    if abs(f(x0)) < tol:
        return x0
    else:
        #recursive call
        return newton(f, df, x0 - f(x0)/df(x0), tol)
```

Bisection Method

Given a tolerance and maximum number of iterations, this function employs the bisection method to locate the function's root. The root's location is in the range $[a, b]$. The tolerance and the maximum number of iterations are specified in the function. We start by defining a function $f(x)$ and its derivative $f'(x)$, as well as an initial guess for the root:

Bisection method

```
import numpy as np

def bisection(f, a, b, tol):

    # check if a and b have a root
    if np.sign(f(a)) == np.sign(f(b)):
        return "The scalars a and b do not bound a root"
    # get midpoint
    m = (a + b)/2

    if np.abs(f(m)) < tol:
        # print m as root
        print (m)
```

```

        elif np.sign(f(a)) == np.sign(f(m)):
            # Make recursive call with a = m
            return bisection(f, m, b, tol)
        elif np.sign(f(b)) == np.sign(f(m)):
            # Make recursive call with b = m
            return bisection(f, a, m, tol)

f = lambda x: x**4 - 2
#tolerance
tol=1e-6
#call function set bounds within which function will operate
bisection(f,1,10,tol)

```

Conclusion, Both newton raphson method and bisection method can be used to find roots but the newton raphson method is faster than the bisection method with a speed of