

Les ensembles

- θ : parameters
- \mathcal{A} : action set
- \mathcal{S} : State set
- \mathcal{V} : The value-function
- \mathcal{Q} : the Q-value
- $\Phi(s, a)$: accessible states
- $\mathcal{T}(s'|s, a)$: Transition function
- $\Gamma(s) = \{a \in \mathcal{A} | \exists s' \in \mathcal{T}(s'|s, a) \neq 0\}$
- $\pi_\theta(s)$: policy function
- $\nabla(s, a, s')$: instant reward
- $R(s, a) = \sum_{s' \in \Phi(s, a)} \mathcal{T}(s'|s, a) * \nabla(s, a, s')$

Formules

- $(e_i)_{i \in \llbracket 1; N \rrbracket} / \forall i \in \llbracket 1; N \rrbracket, e_i = (S_t^i, A_t^i, R_t^i = \nabla(S_{t-1}^i, A_{t-1}^i, S_t^i))_{t \in \llbracket 1; L_i \rrbracket}$
- $C_s = \{(i, t) / S_t^i = s\}$
- $U_{s,a} = \{(i, t) \in C_s / A_t^i = a\}$
- $K_{s,a,s'} = \{(i, t) \in U_{s,a} / S_{t+1}^i = s'\}$
- $G_t^i = \sum_{k=0}^{L_i-t} \gamma^k R_{t+k}^i$: Gain function
- $\mathcal{T}(s'|s, a) \approx \frac{|K_{s,a,s'}|}{|U_{s,a}|}$
- Bellman's equation for the Valuation function

$$\mathcal{V}(s) = \frac{1}{|C_s|} \sum_{(i,t) \in C_s} G_t^i \quad (1)$$

$$\mathcal{V}(s) = \frac{1}{|C_s|} \sum_{(i,t) \in C_s} R_t^i + \gamma G_{t+1}^i \quad (2)$$

$$\mathcal{V}(s) = \frac{1}{|C_s|} \sum_{(i,t) \in C_s} R_t^i + \gamma V(S_{t+1}^i) \quad (3)$$

$$\mathcal{V}(s) = \sum_{a \in \Gamma(s)} \frac{|U_{s,a}|}{\sum_{a' \in \Gamma(s)} |U_{s,a'}|} * \mathcal{Q}(s, a) \quad (4)$$

$$\mathcal{V}(s) = \sum_{a \in \Gamma(s)} \pi(a|s) \mathcal{Q}(s, a) \quad (5)$$

- Bellmans's equation for the Q value function

$$\mathcal{Q}(s, a) = \frac{1}{|U_{s,a}|} \sum_{(i,t) \in U_{s,a}} G_t^i \quad (6)$$

$$\mathcal{Q}(s, a) = \frac{1}{|U_{s,a}|} \sum_{(i,t) \in U_{s,a}} R_t^i + \gamma G_{t+1}^i \quad (7)$$

$$\mathcal{Q}(s, a) = \frac{1}{|U_{s,a}|} \sum_{(i,t) \in U_{s,a}} R_t^i + \gamma V(S_{t+1}^i) \quad (8)$$

$$\mathcal{Q}(s, a) = \frac{1}{|U_{s,a}|} \sum_{(i,t) \in U_{s,a}} R_t^i + \gamma \sum_{a' \in \Gamma(S_{t+1}^i)} \pi(a'|S_{t+1}^i) \mathcal{Q}(S_{t+1}^i, a') \quad (9)$$