Sequencing Legal DNA

NLP for Law and Political Economy

5. Deep Learning for NLP

Weekly Q&A Page

bit.ly/NLP-QA05

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 - Interpret predictions using model explanation methods.
- 4. Empirical analysis
 - Produce statistics or predictions with the trained model.
 - ► Answer the question / solve the problem.

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- ► Topic models: document is a vector of shares over topics

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 - ▶ the vector of features, x_i , is itself a compressed representation of the unprocessed document \mathcal{D}_i .
- ► Correspondingly: the learned parameters $\hat{\theta}$ can also be understood as a **learned** compressed representation of the whole dataset:
 - it contains information about the training corpus, the text features, and the outcomes.

Information in $\hat{\theta}$

Say we train a multinomial logistic regression on a bag-of-words representation of the documents:

- Let θ be the learned matrix of parameters relating words to outcomes:
 - lt contains n_y columns, which are n_x -vectors representing the outcome classes.

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 - It contains n_x rows, which are n_y -vectors representing each word in the vocabulary.
- We could already use θ ! e.g.:
 - ightharpoonup cluster the column vectors ightharpoonup which outcomes are similar/related.
 - ▶ cluster the row vectors → which features are similar/related.

Information in $\hat{\theta}$: Preview of Word Embeddings

 $\theta = \text{matrix}$ of parameters learned from logit, relating words to outcomes.

▶ If x is a bag-of-words representation for a document consisting of a list of tokens $\{w_1, ..., w_t, ..., w_n\}$, we can write

$$\mathbf{x} = \frac{1}{n} \sum_{t=1}^{n} x_t$$

• where x_t is an n_x -dimensional one-hot vector – all entries are zero except equals one for the word at t.

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- Let θ_t be the row of θ corresponding to the word w_t : a **word embedding** for w_t containing the outcome-relevant information for that word.
- ► We can construct a **document vector**

$$\vec{\boldsymbol{d}} = \frac{1}{n} \sum_{t=1}^{n_i} \theta_t$$

the sum of the n_V -dimensional word representations (the row vectors from above).

- ▶ this is called the "continuous bag of words (CBOW)" representation (Goldberg 2017).
- Note that $\vec{d} = \theta \cdot x$, and thus θ is a word embedding matrix.

Recap: Cross-Domain Learning

see link in zoom chat

Outline

Neural Networks

Intro
Multi-Layer Perceptron
Some Practicalities

Autoencoders

Convolutional Neural Nets

Embedding Layers

Recurrent Neural Nets

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 - solve machine learning problems, just like logistic regression or gradient boosted machines
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why not use neural nets?

- usually worse than standard ML on standard problems, and harder to implement.
- Computational constraints: Recent models like OpenAl's GPT-3 would take ETH Deep Learning Cluster 18 months to train.

"Neural Networks" / "Deep Learning"

- ► "Neural":
 - ▶ NN's do not work like the brain such metaphors are misleading.

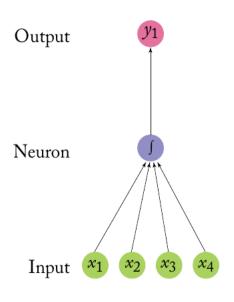
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- "Networks":
 - NNs are not "networks" as that is understood in mathematical network theory or social science.
- "Deep" Learning:
 - does not speak to profundity or effectiveness.
 - an unfortunate source of hype.

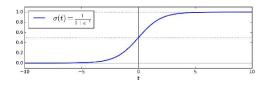
A "Neuron"



- applies dot product to vector of numerical inputs:
 - multiplies each input by a learned weight (parameter or coefficient)
 - sums these products
- applies a non-linear "activation function" to the sum
 - (e.g., the \int shape indicates a sigmoid transformation)
- passes the output.

"Neuron" = Logistic Regression

$$\hat{y} = \operatorname{sigmoid}(\mathbf{x} \cdot \theta) = \frac{1}{1 + \exp(-\mathbf{x} \cdot \theta)}$$



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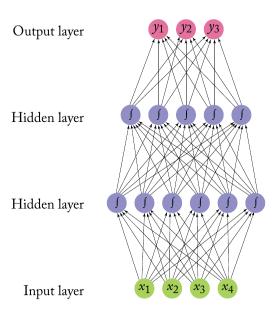
Autoencoders

Convolutional Neural Nets

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Recurrent Neural Nets

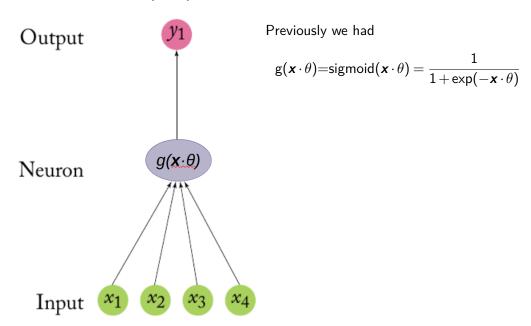
Multi-Layer Perceptron (MLP)



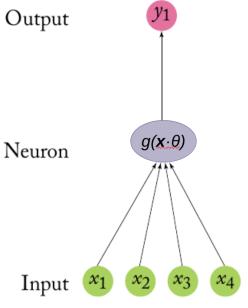
- A multilayer perceptron (also called a feed-forward network or sequential model) stacks neurons horizontally and vertically.
- alternatively, think of it as a stacked ensemble of logistic regression models.
- this vertical stacking is the "deep" in "deep learning"!

- MLP's are composed of "Dense" layers, meaning all neurons are connected.
- ► The tragic result in mathematics of neural nets (Hornik et al 1989, Cybenko 1989):
 - MLP with a single hidden layer, with sigmoid activation, can approximate any continuous function on a closed and bounded subset of \mathbb{R}^n , and any mapping from one finite discrete space to another finite discrete space.
- ► Telgarsky (2016): NN would have to be exponentially large in many cases.

Activation functions $g(x \cdot \theta)$



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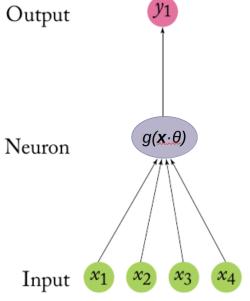


Previously we had

$$g(\mathbf{x} \cdot \theta) = sigmoid(\mathbf{x} \cdot \theta) = \frac{1}{1 + exp(-\mathbf{x} \cdot \theta)}$$

It turns out that sigmoid does not work well in hidden layers, mainly because gradient is flat except around zero

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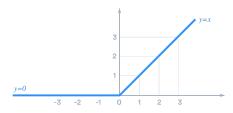
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It turns out that sigmoid does not work well in hidden layers, mainly because gradient is flat except around zero.

ReLU (rectified linear unit) function:

$$g(\mathbf{x} \cdot \theta) = ReLU(\mathbf{x} \cdot \theta) = \max\{0, \mathbf{x} \cdot \theta\}$$



Equation Notation: Multi-Layer Perceptron

An multi-layer perceptron (MLP) with two hidden layers is

$$egin{align*} oldsymbol{y} &= oldsymbol{g}_2(oldsymbol{g}_1(oldsymbol{x} \cdot oldsymbol{\omega}_1) \cdot oldsymbol{\omega}_2) \cdot oldsymbol{\omega}_y \ oldsymbol{y} \in \{0,1\}^{n_y}, oldsymbol{x} \in \mathbb{R}^{n_x}, oldsymbol{\omega}_1 \in \mathbb{R}^{n_x imes n_1}, oldsymbol{\omega}_2 \in \mathbb{R}^{n_1 imes n_2}, oldsymbol{\omega}_y \in \mathbb{R}^{n_2 imes n_y} \end{aligned}$$

- $ightharpoonup n_1, n_2 =$ dimensionality in first and second hidden layer.
- $m{\omega}_1, m{\omega}_2, m{\omega}_y = ext{set}$ of learnable weights for the first hidden, second hidden, and output layer
- $\mathbf{g}_1(\cdot), \mathbf{g}_2(\cdot) = \text{element-wise non-linear functions for first and seond layer.}$

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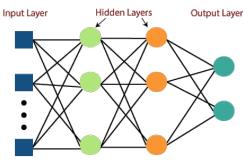
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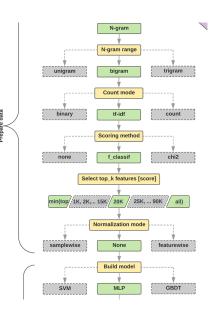
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- ▶ $\mathbf{g}_1(\cdot), \mathbf{g}_2(\cdot)$ = element-wise non-linear functions for first and seond layer.
- Can also be written in decomposed notation:

$$egin{aligned} oldsymbol{h}_1 &= oldsymbol{g}_1(oldsymbol{x} \cdot oldsymbol{\omega}_1) \ oldsymbol{h}_2 &= oldsymbol{g}_2(oldsymbol{h}_1 \cdot oldsymbol{\omega}_2) \ oldsymbol{y} &= oldsymbol{h}_2 \cdot oldsymbol{\omega}_V \end{aligned}$$

where h_l indicate hidden layers.



- The Google Developers Guide recommends an MLP for text classification with relatively few but longer documents.:
 - x = tf-idf-weighted bigrams as a baseline specification for text classification tasks.
 - select 20,000 features using supervised feature selection in training set.
 - $f(\cdot) = MLP$ with two-dimensional hidden layers.
- ▶ A simple MLP is one of the models tried by the U.K. parliament paper (Peterson and Spirling 2018).



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 - this is a major practical downside of using neural nets rather than sklearn or xgboost for most tasks.
 - cross-validating these architectural chooices is usually too computationally expensive.
 - instead, make a big model (too many layers, too many neurons) and regularize with dropout and early stopping.

Dropout

An elegant regularization technique:

- ▶ at every training step, every neuron has some probability (typically p = 0.5) of being temporarily dropped out, so that it will be ignored at this step.
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Why it works:

- \triangleright Approximates an ensemble of N models (where N is the number of neurons).
- Neurons cannot co-adapt with neighbors; they must be independently useful.
- Layers cannot rely excessively on just a few inputs.

Early Stopping

- ► A second elegant regularization technique, used in both xgboost and in neural nets:
 - gradually train the model gradients while checking fit in a held-out validation set.
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- A second elegant regularization technique, used in both xgboost and in neural nets:
 - gradually train the model gradients while checking fit in a held-out validation set.
 - when model starts overfitting, stop training.
- Requires user to specify two additional parameters:
 - validation set: a third sample of the data, separate from training set and test set
 - early stopping rounds: stop training if we have done this many epochs without improving validation set performance.

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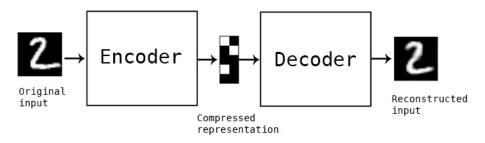
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Autoencoders: Optimal Compression Algorithms

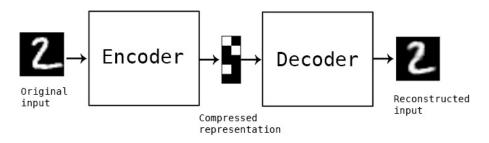
▶ Autoencoders = neural nets that perform domain-specific lossy compression:



▶ Learned encodings can be decoded back to a *reconstruction* – a (minimally) lossy representation of the original data.

Autoencoders: Optimal Compression Algorithms

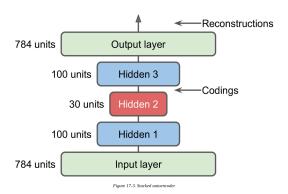
▶ Autoencoders = neural nets that perform domain-specific lossy compression:



- ▶ Learned encodings can be decoded back to a *reconstruction* a (minimally) lossy representation of the original data.
- AE's can memorize complex, unstructured data.

Autoencoder Architecture

- Stacked layers gradually decrease in dimensionality to create the compressed representation
- then gradually increase in dimensionality to try to reconstruct the input.



Reconstruction from encoded vector



Figure 17-4. Original images (top) and their reconstructions (bottom)

Autoencoders for Data Visualization

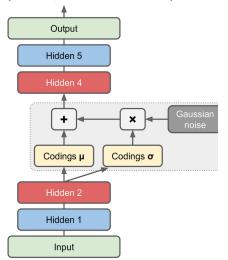


Figure 17-5. Fashion MNIST visualization using an autoencoder followed by t-SNE

- Decent baseline for visualizing the encodings:
 - use an autoencoder to compress your data to relatively low dimension (e.g. 32 dimensions)
 - then use t-SNE for mapping the compressed data to a 2D plane.

Variational Autoencoders

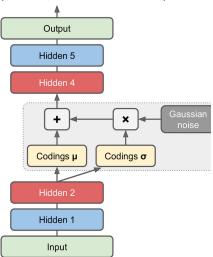
Encodings taken as parameters of a gaussian (means μ and variances σ^2)



Decoder draws from the distribution to produce first layer.

Variational Autoencoders

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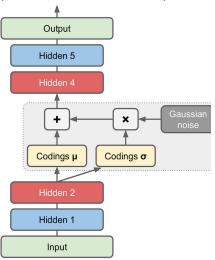


➤ Can then sample from the normal distribution (or just choose numbers) and generate reconstructions.

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Encodings taken as parameters of a gaussian (means μ and variances σ^2)



- ➤ Can then sample from the normal distribution (or just choose numbers) and generate reconstructions.
- VAE's do semantic interpolation: picking an encoding vector between two encodings will produce a reconstruction that is "between" the associated images







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Activity: Zoom Poll 5.1

► Check each true item.

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Sequence Data

- ▶ The real break-through from deep learning for NLP:
 - moving from bag-of-X representations to sequence representations.

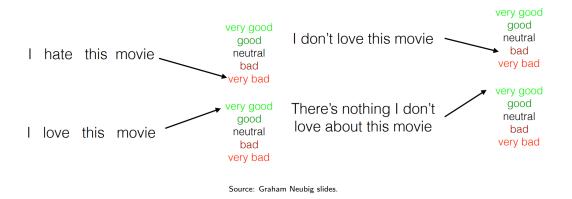
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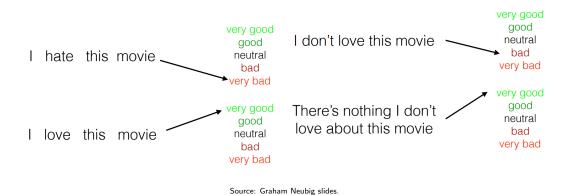
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 - moving from bag-of-X representations to sequence representations.
 - ▶ Rather than inputting counts over words x, take as input a sequence of tokens $\{w_1,...,w_t,...w_n\}$.
- "Traditional" architectures:
 - Convolutional neural nets (CNNs)
 - Recurrent Neural Nets (RNNs)
- ➤ Since 2018, CNNs and RNNs (as currently implemented) usually get worse performance than attentional neural nets (transformers).

The Classic Sentence Classification Problem



(continuous) bag of words models (even with hidden layers) won't capture the importance of "don't love" or "nothing I don't love".

The Classic Sentence Classification Problem



- ► (continuous) bag of words models (even with hidden layers) won't capture the importance of "don't love" or "nothing I don't love".
- Our current solution, N-grams, has the downsides of a large feature space and no sharing of information/weights across similar words/n-grams.

Convolutional Neural Nets ↔ N-gram Detectors

A neural net architecture that constructs **filters** that slide across input sequences and extract **local predictive structure**.

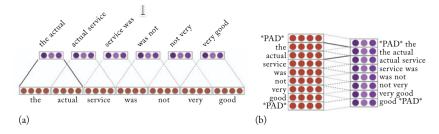


Figure 13.1: The inputs and outputs of a narrow and a wide convolution in the vector-concatenation and the vector-stacking notations. (a) A *narrow* convolution with a window of size k=2 and 3-dimensional output $(\ell=3)$, in the vector-concatenation notation. (b) A *wide* convolution with a window of size k=2, a 3-dimensional output $(\ell=3)$, in the vector-stacking notation.

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 - poor, useless, returned, not worth, return, worse, disappointed, terrible, worst, horrible
 - ▶ great, excellent, perfect, love, easy, amazing, awesome, no problems, perfectly, beat

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- CNN recovers longer, more interesting phrases:

N1	completely useless ., return policy .
N2	it won't even, but doesn't work
N3	product is defective, very disappointing !
N4	is totally unacceptable, is so bad
N5	was very poor, it has failed
P1	works perfectly !, love this product
P2	very pleased !, super easy to, i am pleased
P3	'm so happy, it works perfect, is awesome!
P4	highly recommend it, highly recommended !
P5	am extremely satisfied, is super fast

Table 5: Examples of predictive text regions in the training set.

were unacceptably bad, is abysmally bad, were universally poor, was hugely disappointed, was enormously disappointed, is monumentally frustrating, are endlessly frustrating

best concept ever, best ideas ever, best hub ever, am wholly satisfied, am entirely satisfied, am incredicbly satisfied, 'm overall impressed, am awfully pleased, am exceptionally pleased, 'm entirely happy, are acoustically good, is blindingly fast,

Table 6: Examples of text regions that contribute to prediction. They are from the *test set*, and they did *not* appear in the training set, either entirely or partially as bi-grams.

but overall, CNNs do not work well in NLP.

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- Not embeddings:
 - counts over LIWC dictionary categories.
 - sklearn CountVectorizer count vectors
- Embeddings:
 - PCA reductions of the word count vectors
 - ► LDA topic shares
 - compressed encodings from an autoencoder

Categorical Embeddings = dense representations of categorical variables

Say we have a binary classification problem with outcome Y:

- ▶ we have a high-dimensonal categorical variable (e.g. area of law with 1000 categories)
- ▶ including dummy variables *A* for each category in your ML model is computationally expensive.

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1. PCA applied to the dummy variables A to get lower-dimensional \tilde{A} .

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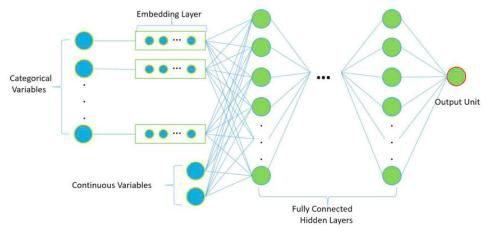
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- 1. PCA applied to the dummy variables A to get lower-dimensional \tilde{A} .
- 2. Regress Y on A, predict $\hat{Y}(A_i)$, add that as a predictor in your model instead.
 - (2) is quite close to what embedding layers do in neural nets.



An embedding layer is matrix multiplication:

$$\underbrace{h_1}_{n_E \times 1} = \underbrace{\omega_E}_{n_E \times n_W} \cdot \underbrace{x}_{n_x \times 1}$$

- \triangleright x = a categorical variable (e.g., representing a word)
 - one-hot vector with a single item equaling one. Input to the embedding layer.
- \blacktriangleright h_1 = the first hidden layer of the neural net
 - ▶ The output of the embedding layer.

The embedding matrix ω_E encodes predictive information about the categories, has a spatial interpretation when projected to two dimensions.

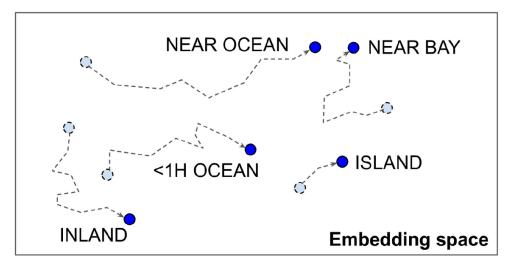


Figure 13-4. Embeddings will gradually improve during training

Embedding Layers versus Dense Layers

- An embedding layer is statistically equivalent to a fully-connected dense layer with one-hot vectors as input and linear activation.
 - ▶ embedding layers are much faster for many categories (>~50)

In practice: Embedded Hashed N-Grams

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The hashing vectorizer (keras.preprocessing.text.hashing_trick), combined with embeddings, is an efficient alternative to convolutional neural nets:

- ▶ Allocate $n_w \approx 1$ million rows to an embedding matrix ω_E
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- ▶ Allocate $n_w \approx 1$ million rows to an embedding matrix ω_E
- Assign n-grams to embedding indexes with hashing function
- train MLP on top of embedding layer.
- Captures the local predictive power of n-grams without building vocabulary or costly training of CNN.

Outline

Neural Networks

Intro

Multi-Layer Perceptron

Some Practicalities

Autoencoders

Convolutional Neural Nets

Embedding Layers

Recurrent Neural Nets

RNNs can input and output arbitrary-length sequences

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RNNs can input and output arbitrary-length sequences

- ► The models we have looked at so far (including CNNs) took inputs of fixed dimensions and output scalars or class probabilities.
- ► Recurrent Neural Nets (RNNs) work with **sequences of arbitrary length**, both as **inputs** and **outputs**:
 - can encode sequences into vectors.
 - can decode vectors into sequences.
- therefore especially useful for language tasks such as translation.

RNN Architecture

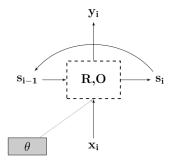
- ► At each step *t*:
 - ▶ a recursion function $R(s_{t-1}, x_t)$ computes the state vector s_t given current word x_t and previous state s_{t-1} . s_0 initialized to zeros or randomly.

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$$\hat{\boldsymbol{y}}_t = O(\boldsymbol{s}_t)$$

 $\boldsymbol{s}_t = R(\boldsymbol{s}_{t-1}, \boldsymbol{x}_t)$

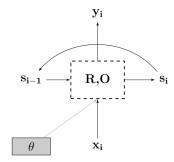


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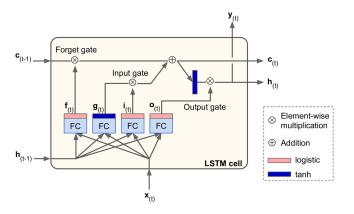
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 $\boldsymbol{s}_t = R(\boldsymbol{s}_{t-1}, \boldsymbol{x}_t)$



▶ in a "Simple RNN", $R(\cdot)$ is just a dense layer with ReLU activation, and $O(s_t) = s_t$.

Gated Architectures – LSTM (Long Short-Term Memory)



▶ gating mechanisms prevent vanishing/exploding gradients (see also GRU).

RNNs: Practical Use for Sequence-to-Vector Task

For example, sentiment analysis (using keras functional API):

- **b** tokenize the documents into $\mathbf{w}_{1:n}$
- ightharpoonup embedding $oldsymbol{x}_t = oldsymbol{w}_t \cdot oldsymbol{\omega}_E$
 - \triangleright embedding matrix ω_E can be initialized with pre-trained GloVe embeddings.
- **b** bidirectional LSTM on $x_{1:n}$ (and $x_{n:1}$) to generate document vector s
 - that is, document is fed in backwards and forwards to two parallel LSTMs,
 - ▶ Use layer normalization (normalizes each instance across feature dimensions) rather than batch normalization (normalizes each feature across a sample of instances).
- s input to MLP to predict y

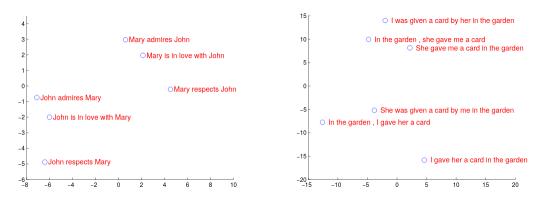
see Richard Socher's lecture notes for some additional tips re initialization, learning rate, and gradient clipping.

Geometry of Embedded Sequences

► The RNN's document vector for a sequence, **s**, is an embedding with interpretable geometry.

Geometry of Embedded Sequences

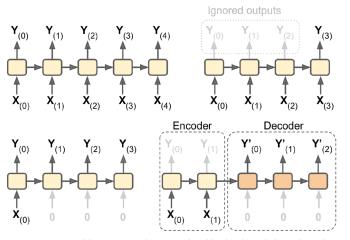
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Sutskever, Vinyals, and Le, "Sequence to sequence learning with neural networks."

Types of RNNs: Encoding and Decoding

top left: sequence to sequence; top right: sequence to vector



Figure~15-4.~Seq-to-seq~(top~left),~seq-to-vector~(top~right),~vector-to-seq~(bottom~left),~and~Encoder-Decoder~(bottom~right)~networks

bottom left: vector to sequence; bottom right: encoder-decoder.

Application: RNN's for predicting partisanship

lyyer, Enns, Boyd-Graber, and Resnik (2014)

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n	Most conservative n-grams	Most liberal n-grams
1	Salt, Mexico, housework, speculated, consensus, lawyer,	rich, antipsychotic, malaria, biodiversity, richest, gene,
	pharmaceuticals, ruthless, deadly, Clinton, redistribution	pesticides, desertification, Net, wealthiest, labor, fertilizer, nuclear, HIV
3	prize individual liberty, original liberal idiots, stock mar-	rich and poor,"corporate greed", super rich pay, carrying
	ket crash, God gives freedom, federal government inter-	the rich, corporate interest groups, young women work-
	ference, federal oppression nullification, respect individ-	ers, the very rich, for the rich, by the rich, soaking the
	ual liberty, Tea Party patriots, radical Sunni Islamists,	rich, getting rich often, great and rich, the working poor,
	Obama stimulus programs	corporate income tax, the poor migrants
5	spending on popular government programs, bailouts and	the rich are really rich, effective forms of worker partic-
	unfunded government promises, North America from	ipation, the pensions of the poor, tax cuts for the rich,
	external threats, government regulations place on busi-	the ecological services of biodiversity, poor children and
	nesses, strong Church of Christ convictions, radical Is- lamism and other threats	pregnant women, vacation time for overtime pay
		AC' A ' I I I I'
7	government intervention helped make the Depression	African Americans and other disproportionately poor
	Great, by God in His image and likeness, producing	groups; the growing gap between rich and poor; the
	wealth instead of stunting capital creation, the tradi- tional American values of limited government, trillions	Bush tax cuts for the rich; public outrage at corporate and societal greed; sexually transmitted diseases, most
	of dollars to overseas oil producers, its troubled assets to	notably AIDS; organize unions or fight for better condi-
	federal sugar daddies, Obama and his party as racialist	tions, the biggest hope for health care reform
	fanatics	tions, the orggest hope for health care reform
	Tanaucs	

Table 2: Highest probability n-grams for conservative and liberal ideologies, as predicted by the RNN2-(W2V) model.

Activity: Zoom Poll 5.2

► Check each true item.

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 - for example, wearing masks and coronavirus spread.
- There isn't a machine learning dataset to train a model on.
 - we cant experimentally force people to wear a mask or not.
- ► How do we solve that?
- ► Glossary for machine learning vs causal inference terms: https://bit.ly/ML-Econ-Glossary.

Menti Activity: Legal Briefs Dataset

Let's say we have a corpus of legal briefs with text and metadata, everything you would expect from a case, including information on the actors (litigants, attorneys, judges) and the associated outcomes (e.g. who wins).

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- ► Type four answers into menti. put the question number, then your initials, then your answer.