# Labor Tax, rel. Pareto weights 1

December 22, 2017

### 1 Tables with Results

	No tax	Optimal policy	Optimal SS tax	Optimal Flat tax
$ au_0$	0.00000	-0.29444	-0.10526	0.02222
$ar{ au}$	0.00000	0.19428	-0.10526	0.02222
Half life	_	13.00000	-	-
Welfare (weighted)	-10.29030	-10.17092	-10.37036	-10.28787
Welfare workers	-5.86691	-5.81440	-6.25191	-5.80398
Welfare entrepreneurs	-19.13709	-18.88397	-18.60728	-19.25567

	Constant $\tau_0$	Constant $\bar{\tau}$
$\overline{\tau_0}$	-0.29444	0.19428
$ar{ au}$	-0.29444	0.19428
Half life	_	_
Welfare (weighted)	-10.75017	-10.47927
Welfare workers	-7.24267	-5.58331
Welfare entrepreneurs	-17.76516	-20.27119

Experiment	Total welfare	Worker welfare	Entrepreneur welfare
Optimal policy	0.00414	0.00158	0.01274
Optimal flat tax	0.00008	0.00189	-0.00591
Constant $\tau_0$	-0.01579	-0.04043	0.07100
Constant $\bar{\tau}$	-0.00652	0.00854	-0.05513

### 2 Parameters and functional forms

#### 2.1 Functional forms etc.

- Occupational choice: No
- Workers save: No
- Decreasing returns to scale: Yes
- Productivity process: Ornstein-Uhlenbeck,  $d \log(z) = -\nu \log(z) dt + \sigma dW$
- Period utility function:

$$u(c,l) = (1-\gamma)^{-1}c^{1-\gamma} - \nu(l), \quad \nu(l) = (1+1/\chi)^{-1}l^{1+1/\chi}$$

- Production function:  $y = F(z, k, n) = zA((k f_k)^+)^{\alpha}((n f_n)^+)^{\beta}$
- Tax schedule:  $\tau_l(t) = \bar{\tau}_l + e^{-\gamma t} (\tau_{l,0} \bar{\tau}_l)$

### 2.2 Parameter values

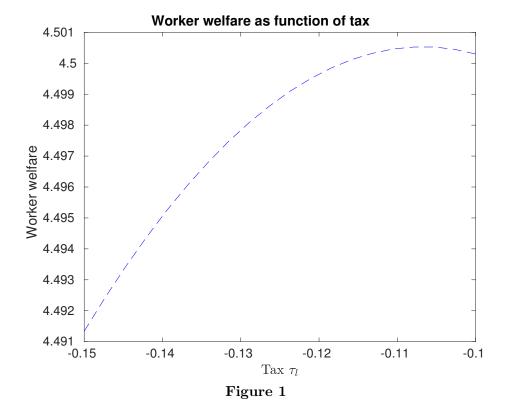
Pareto weight workers0.667Population share of workerspopshare0.667Total populationpopmass1.000Discount rate entrepreneurs $\rho_e$ 0.050Discount rate workers $\rho_w$ 0.030Relative risk aversion $\gamma$ 1.000Inverse Frisch elasticity $\varphi$ 1.000Depreciation rate $\delta$ 0.000Fixed cost capital $f_k$ 0.000Fixed cost labor $f_n$ 0.000Financial constraint parameter $\lambda$ 2.000Common TFP parameter $A$ 1.000Capital share $\alpha$ 0.297Labor share $\alpha$ 0.297Interest rate $\alpha$ 0.900Interest rate $\alpha$ 0.900Productivity drift parameter $\nu$ 0.163Productivity drift parameter $\nu$ 0.163Productivity standard deviation parameter $\sigma$ 0.850Productivity mean $\bar{x}$ 1.148Poisson arrival rate0.100Parameter of Pareto distribution of Poisson shocks1.100Contraction of initial distribution $\chi$ 0.100			
Total populationpopmass1.000Discount rate entrepreneurs $\rho_e$ 0.050Discount rate workers $\rho_w$ 0.030Relative risk aversion $\gamma$ 1.000Inverse Frisch elasticity $\varphi$ 1.000Depreciation rate $\delta$ 0.000Death rate $\theta$ 0.000Fixed cost capital $f_k$ 0.000Fixed cost labor $f_n$ 0.000Financial constraint parameter $\lambda$ 2.000Common TFP parameter $A$ 1.000Capital share $\alpha$ 0.297Labor share $\beta$ 0.603Returns to scale $\alpha + \beta$ 0.900Interest rate $r^*$ 0.300Effect of productivity on effective labor supply $\eta$ 0.000Productivity drift parameter $\nu$ 0.163Productivity yearly autocorrelation $e^{-\nu}$ 0.850Productivity standard deviation parameter $\sigma$ 0.300Productivity mean $\bar{z}$ 1.148Poisson arrival rate0.100Parameter of Pareto distribution of Poisson shocks1.100	Pareto weight workers		0.667
Discount rate entrepreneurs  Discount rate workers $\rho_e$ 0.030  Relative risk aversion  Inverse Frisch elasticity  Depreciation rate $\delta$ 0.000  Depreciation rate $\delta$ 0.000  Fixed cost capital  Fixed cost labor  Financial constraint parameter $\delta$ 0.000  Capital share $\delta$ 0.200  Capital share $\delta$ 0.603  Returns to scale  Interest rate $\delta$ 0.900  Interest rate $\delta$ 0.900  Productivity drift parameter $\delta$ 0.900  Productivity standard deviation parameter $\delta$ 0.300  Productivity mean  Parameter of Pareto distribution of Poisson shocks $\delta$ 0.030  Capital share $\delta$ 0.050 $\delta$ 0.000 $\delta$ 0.000 $\delta$ 0.000 $\delta$ 0.000  Productivity standard deviation of Poisson shocks $\delta$ 0.0100 $\delta$ 0.000 $\delta$ 0.000  Parameter of Pareto distribution of Poisson shocks $\delta$ 0.100	Population share of workers	popshare	0.667
Discount rate workers $\rho_w$ 0.030 Relative risk aversion $\gamma$ 1.000 Inverse Frisch elasticity $\varphi$ 1.000 Depreciation rate $\delta$ 0.000 Death rate $\theta$ 0.000 Fixed cost capital $f_k$ 0.000 Fixed cost labor $f_n$ 0.000 Financial constraint parameter $\lambda$ 2.000 Common TFP parameter $\lambda$ 1.000 Capital share $\lambda$ 0.297 Labor share $\lambda$ 0.603 Returns to scale $\lambda$ 0.900 Interest rate $\lambda$ 0.900 Interest rate $\lambda$ 0.900 Productivity drift parameter $\lambda$ 0.900 Productivity drift parameter $\lambda$ 0.030 Productivity standard deviation parameter $\lambda$ 0.300 Productivity mean $\lambda$ 1.148 Poisson arrival rate Parameter of Pareto distribution of Poisson shocks	Total population	popmass	1.000
Relative risk aversion $\gamma$ 1.000Inverse Frisch elasticity $\varphi$ 1.000Depreciation rate $\delta$ 0.000Death rate $\theta$ 0.000Fixed cost capital $f_k$ 0.000Fixed cost labor $f_n$ 0.000Financial constraint parameter $\lambda$ 2.000Common TFP parameter $A$ 1.000Capital share $\alpha$ 0.297Labor share $\beta$ 0.603Returns to scale $\alpha + \beta$ 0.900Interest rate $r^*$ 0.030Effect of productivity on effective labor supply $\eta$ 0.000Productivity drift parameter $\nu$ 0.163Productivity yearly autocorrelation $e^{-\nu}$ 0.850Productivity mean $\bar{z}$ 1.148Poisson arrival rate0.100Parameter of Pareto distribution of Poisson shocks1.100	Discount rate entrepreneurs	$ ho_e$	0.050
Inverse Frisch elasticity $\varphi$ 1.000  Depreciation rate $\delta$ 0.000  Death rate $\theta$ 0.000  Fixed cost capital $f_k$ 0.000  Fixed cost labor $f_n$ 0.000  Financial constraint parameter $\lambda$ 2.000  Common TFP parameter $\lambda$ 1.000  Capital share $\lambda$ 0.297  Labor share $\lambda$ 0.603  Returns to scale $\lambda$ 0.900  Interest rate $\lambda$ 0.900  Effect of productivity on effective labor supply $\lambda$ 0.000  Productivity drift parameter $\lambda$ 0.163  Productivity standard deviation parameter $\lambda$ 0.300  Productivity mean $\lambda$ 1.148  Poisson arrival rate $\lambda$ 0.100  Parameter of Pareto distribution of Poisson shocks 0.100	Discount rate workers	$ ho_w$	0.030
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Fixed cost labor  Financial constraint parameter  Common TFP parameter  Capital share  Capital share  Capital share  Capital share $\alpha$ $\alpha$ $\alpha$ $\alpha$ $\alpha$ $\alpha$ $\alpha$ $\alpha$	Death rate	$\theta$	0.000
Financial constraint parameter $\lambda$ 2.000 Common TFP parameter $A$ 1.000 Capital share $\alpha$ 0.297 Labor share $\beta$ 0.603 Returns to scale $\alpha + \beta$ 0.900 Interest rate $\alpha$ 0.300 Effect of productivity on effective labor supply $\alpha$ 0.000 Productivity drift parameter $\alpha$ 0.163 Productivity standard deviation parameter $\alpha$ 0.300 Productivity mean $\alpha$ 0.300 Productivity mean $\alpha$ 0.100 Parameter of Pareto distribution of Poisson shocks 1.100 Capital share $\alpha$ 0.100	Fixed cost capital	$f_k$	0.000
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Productivity mean $\bar{z}$ 1.148  Poisson arrival rate 0.100  Parameter of Pareto distribution of Poisson shocks 1.100	Productivity yearly autocorrelation	$e^{-\nu}$	0.850
Poisson arrival rate  O.100  Parameter of Pareto distribution of Poisson shocks  1.100	Productivity standard deviation parameter	$\sigma$	0.300
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0.100	Poisson arrival rate		0.100
Contraction of initial distribution $\chi$ 0.100	Parameter of Pareto distribution of Poisson shocks		1.100
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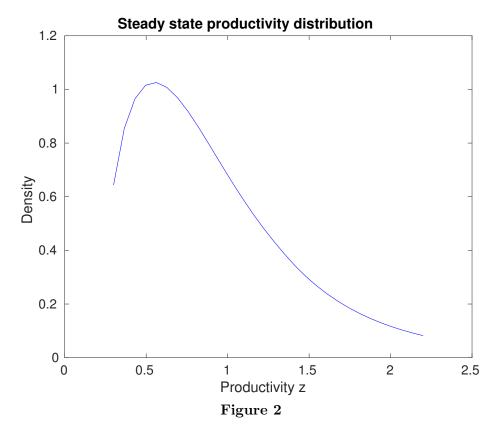
## 2.3 Iteration parameters

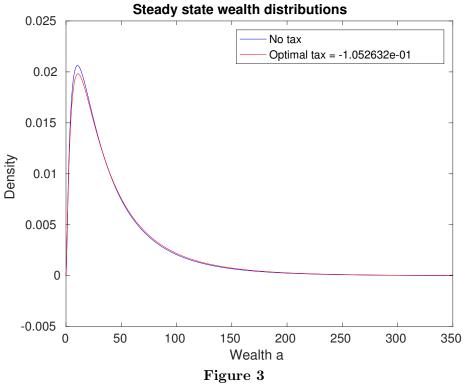
Number of grid points assets	I	200.000
Number of grid points productivity		30.000
Number of grid points time		150.000
Number of time periods		150.000
Max assets	$a_{max}$	350.000
Mean wealth relative to steady state		0.100
Range of initial tax rate tested	$ au_0$	[-0.350,-0.250]
Range of final tax rate tested	$ar{ au}$	[0.150, 0.250]

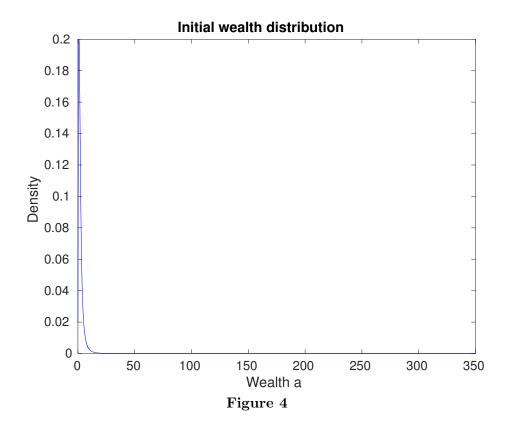
## 3 Figures

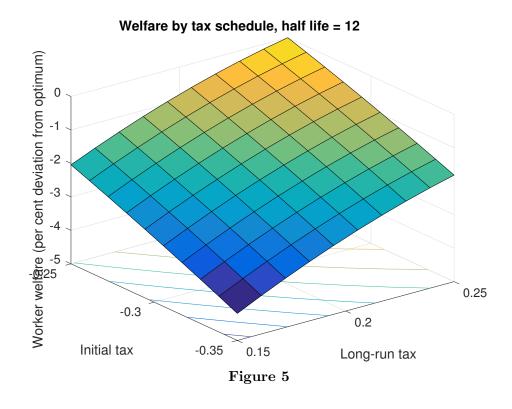
Optimal steady state tax rate = -0.105

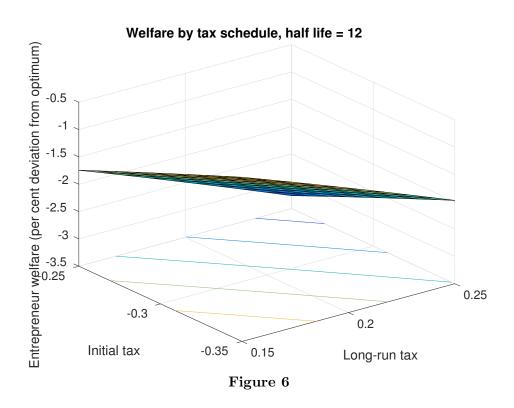


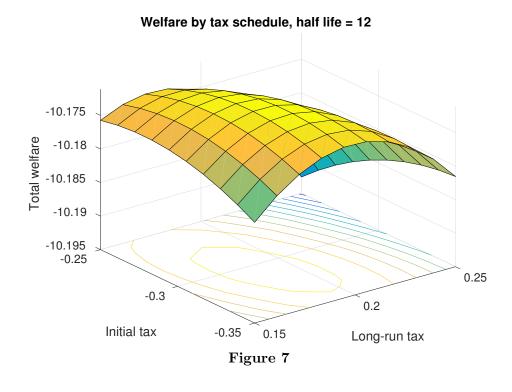


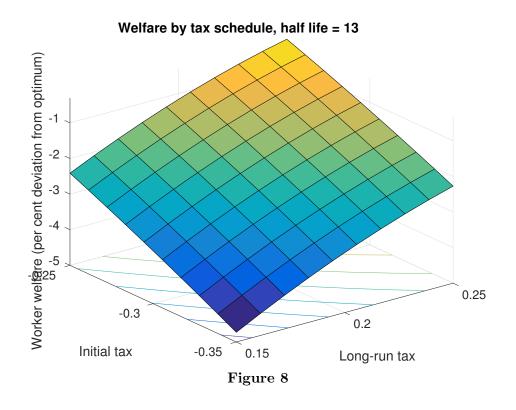


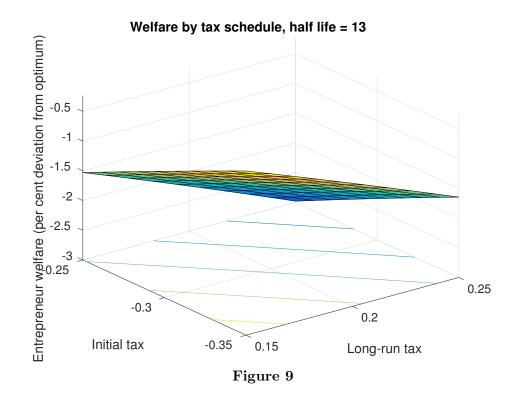


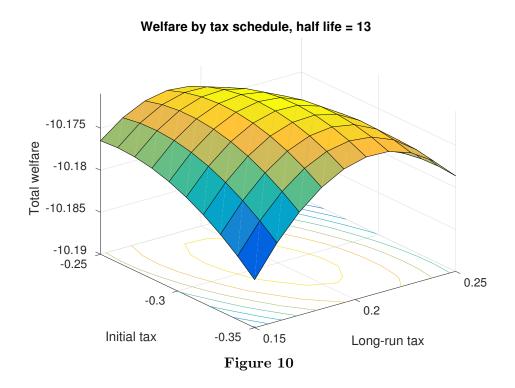


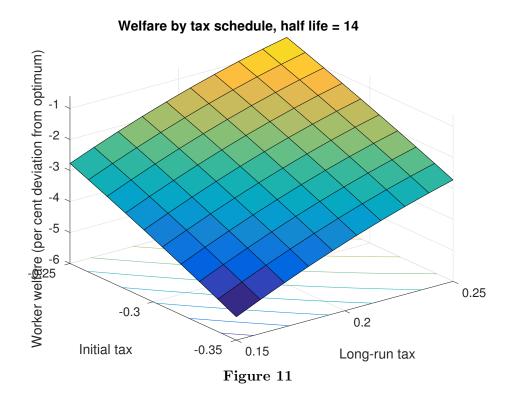


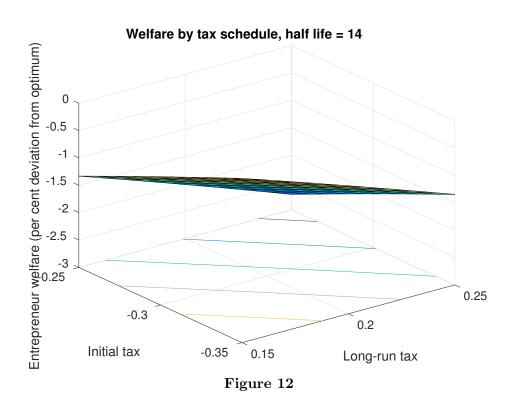


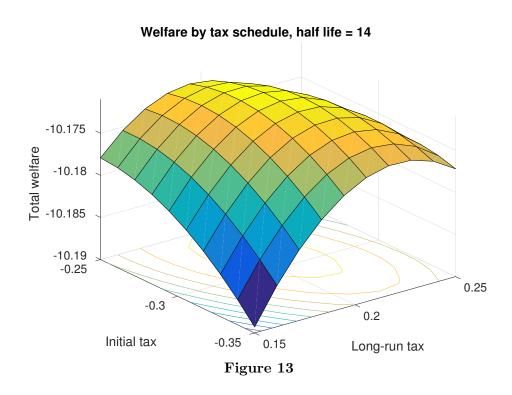


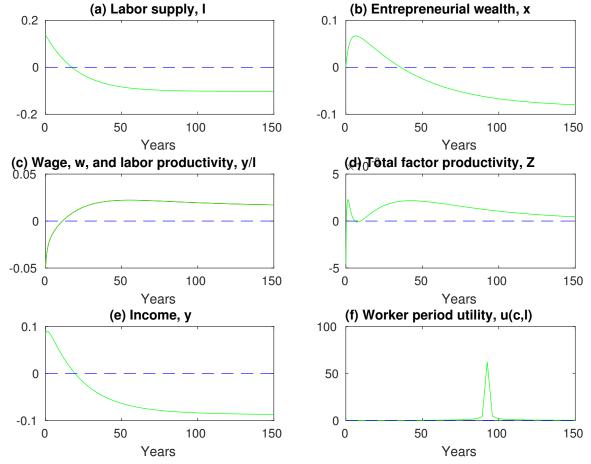












 ${\bf Figure} \ {\bf 14} - {\bf Proportional} \ deviations \ of \ optimal \ tax \ equilibrium \ from \ the \ laissez-faire \ equilibrium$ 

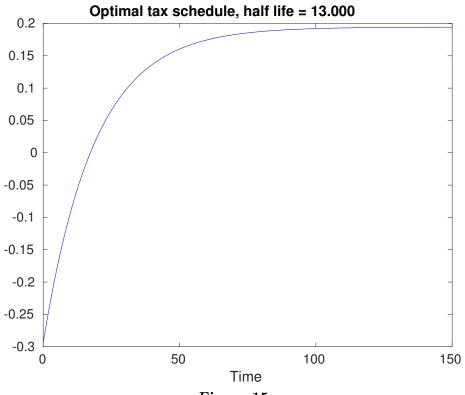
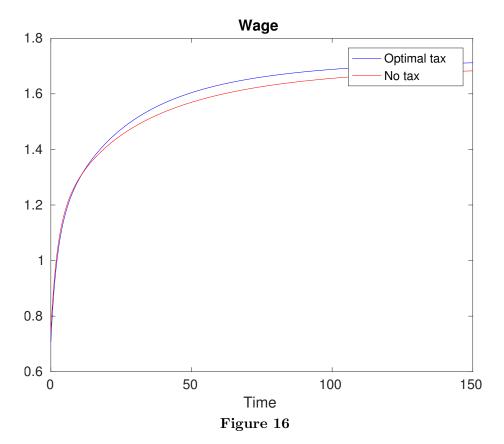


Figure 15



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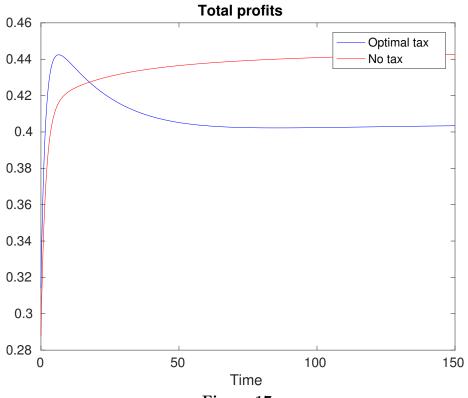
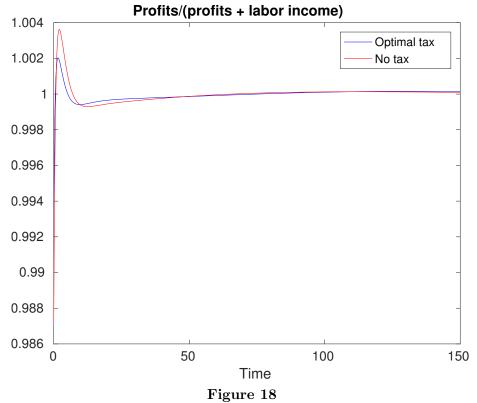
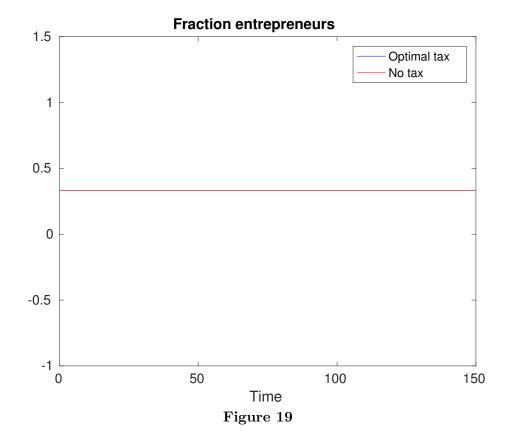
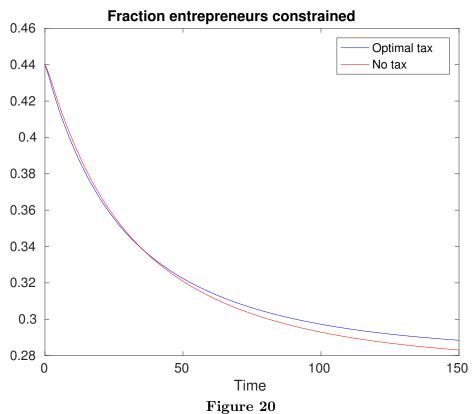
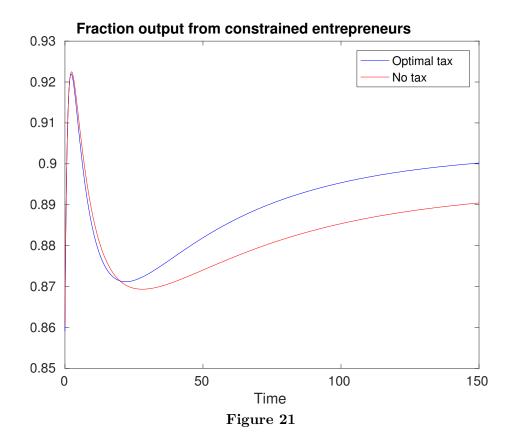


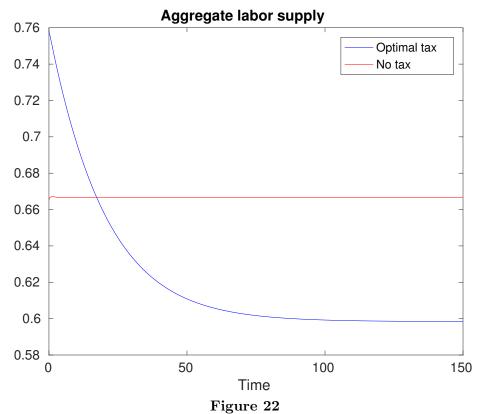
Figure 17

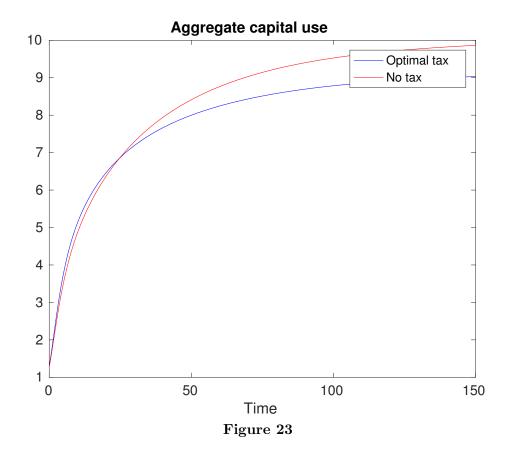












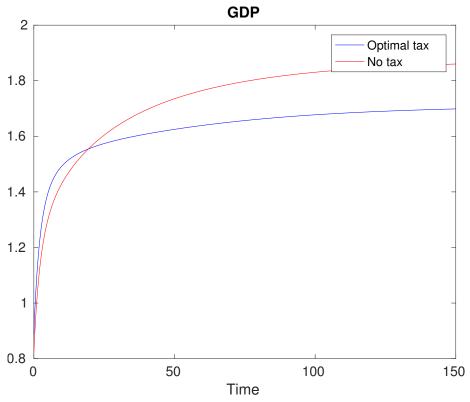
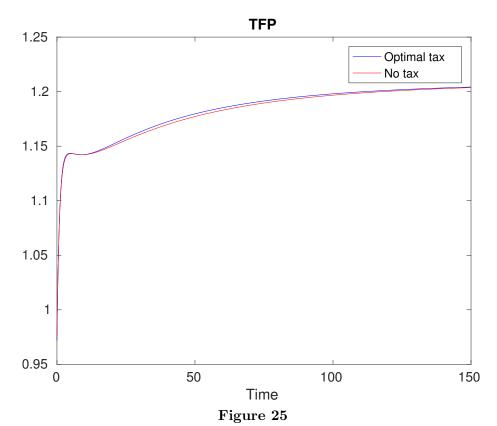
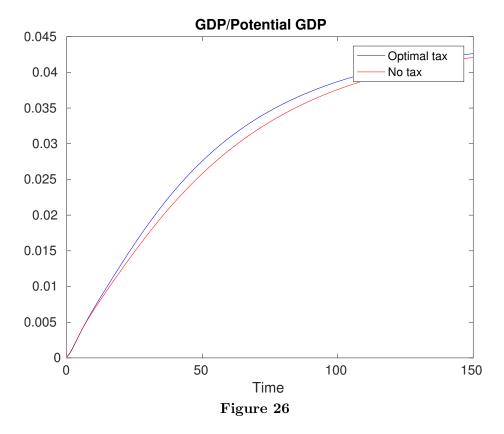
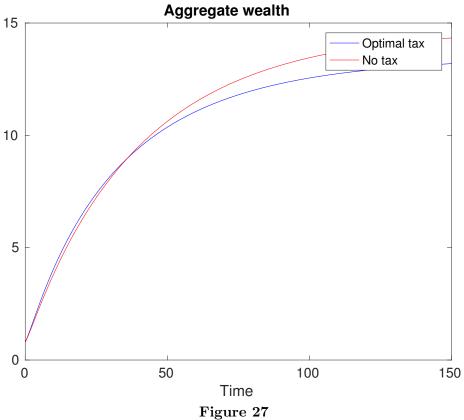


Figure 24



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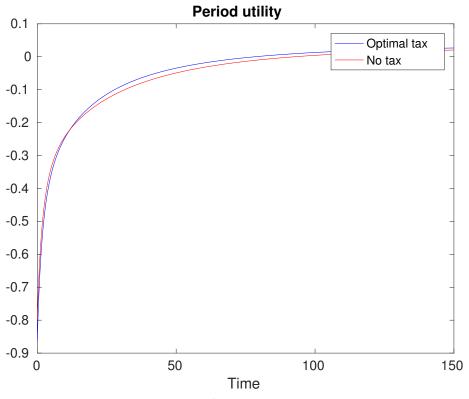


Figure 28

