

Labor Tax, rel. Pareto weights 1/2

December 22, 2017

1 Tables with Results

| | No tax | Optimal policy | Optimal SS tax | Optimal Flat tax |
|-----------------------|-----------|----------------|----------------|------------------|
| τ_0 | 0.00000 | -0.12778 | 0.02105 | 0.10000 |
| $\bar{\tau}$ | 0.00000 | 0.21661 | 0.02105 | 0.10000 |
| Half life | - | 12.00000 | - | - |
| Welfare (weighted) | -8.52094 | -8.37599 | -8.49556 | -8.45154 |
| Welfare workers | -5.86691 | -5.61742 | -5.80711 | -5.64146 |
| Welfare entrepreneurs | -19.13709 | -19.41025 | -19.24937 | -19.69184 |

| | Constant τ_0 | Constant $\bar{\tau}$ |
|-----------------------|-------------------|-----------------------|
| τ_0 | -0.12778 | 0.21661 |
| $\bar{\tau}$ | -0.12778 | 0.21661 |
| Half life | - | - |
| Welfare (weighted) | -8.78100 | -8.55986 |
| Welfare workers | -6.35120 | -5.59538 |
| Welfare entrepreneurs | -18.50019 | -20.41779 |

| Experiment | Total welfare | Worker welfare | Entrepreneur welfare |
|-----------------------|---------------|----------------|----------------------|
| Optimal policy | 0.00503 | 0.00751 | -0.01356 |
| Optimal flat tax | 0.00241 | 0.00679 | -0.02736 |
| Constant τ_0 | -0.00896 | -0.01442 | 0.03236 |
| Constant $\bar{\tau}$ | -0.00135 | 0.00818 | -0.06203 |

2 Parameters and functional forms

2.1 Functional forms etc.

- Occupational choice: No
- Workers save: No
- Decreasing returns to scale: Yes
- Productivity process: Ornstein-Uhlenbeck, $d \log(z) = -\nu \log(z)dt + \sigma dW$
- Period utility function:

$$u(c, l) = (1 - \gamma)^{-1} c^{1-\gamma} - \nu(l), \quad \nu(l) = (1 + 1/\chi)^{-1} l^{1+1/\chi}$$

- Production function: $y = F(z, k, n) = zA((k - f_k)^+)^{\alpha}((n - f_n)^+)^{\beta}$
- Tax schedule: $\tau_l(t) = \bar{\tau}_l + e^{-\gamma t}(\tau_{l,0} - \bar{\tau}_l)$

2.2 Parameter values

| | | |
|--|------------------|-------|
| Pareto weight workers | | 0.800 |
| Population share of workers | $popshare$ | 0.667 |
| Total population | $popmass$ | 1.000 |
| Discount rate entrepreneurs | ρ_e | 0.050 |
| Discount rate workers | ρ_w | 0.030 |
| Relative risk aversion | γ | 1.000 |
| Inverse Frisch elasticity | φ | 1.000 |
| Depreciation rate | δ | 0.000 |
| Death rate | θ | 0.000 |
| Fixed cost capital | f_k | 0.000 |
| Fixed cost labor | f_n | 0.000 |
| Financial constraint parameter | λ | 2.000 |
| Common TFP parameter | A | 1.000 |
| Capital share | α | 0.297 |
| Labor share | β | 0.603 |
| Returns to scale | $\alpha + \beta$ | 0.900 |
| Interest rate | r^* | 0.030 |
| Effect of productivity on effective labor supply | η | 0.000 |
| Productivity drift parameter | ν | 0.163 |
| Productivity yearly autocorrelation | $e^{-\nu}$ | 0.850 |
| Productivity standard deviation parameter | σ | 0.300 |
| Productivity mean | \bar{z} | 1.148 |
| Poisson arrival rate | | 0.100 |
| Parameter of Pareto distribution of Poisson shocks | | 1.100 |
| Contraction of initial distribution | χ | 0.100 |

2.3 Iteration parameters

| | | |
|--------------------------------------|--------------|-----------------|
| Number of grid points assets | I | 200.000 |
| Number of grid points productivity | J | 30.000 |
| Number of grid points time | N | 150.000 |
| Number of time periods | T | 150.000 |
| Max assets | a_{max} | 350.000 |
| Mean wealth relative to steady state | | 0.100 |
| Range of initial tax rate tested | τ_0 | [-0.150,-0.100] |
| Range of final tax rate tested | $\bar{\tau}$ | [0.200,0.250] |

3 Figures

Optimal steady state tax rate = 0.021

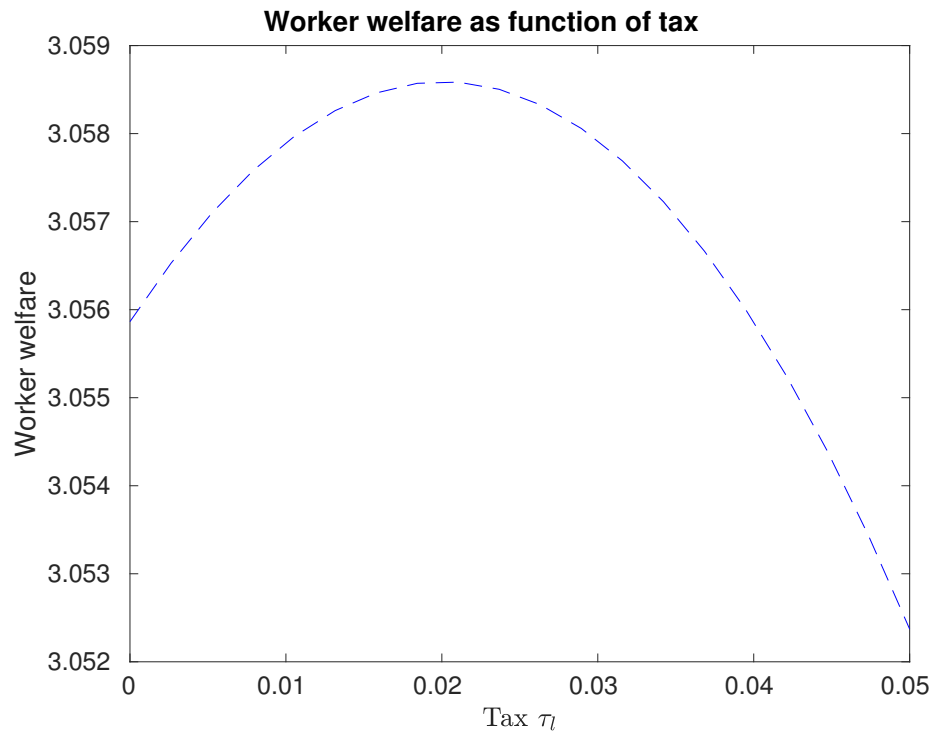


Figure 1

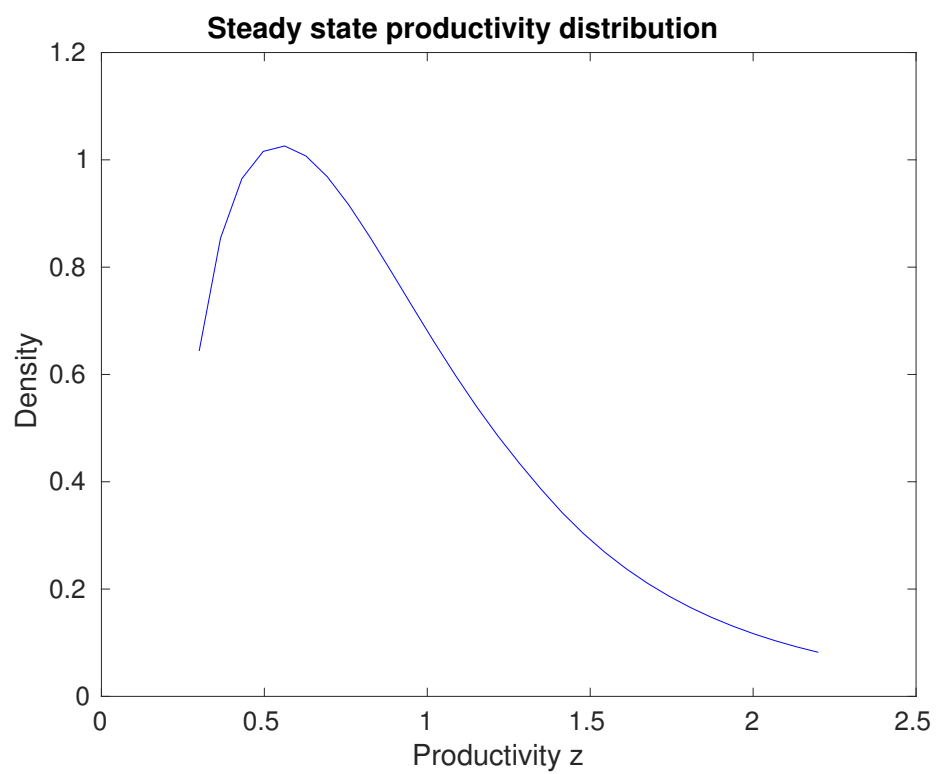


Figure 2

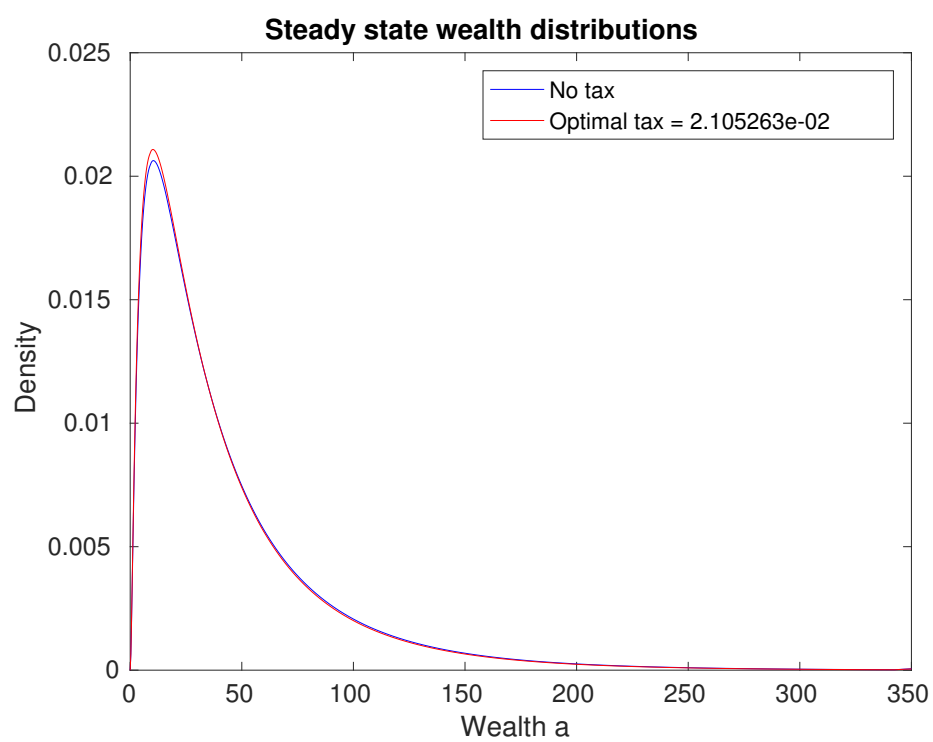


Figure 3

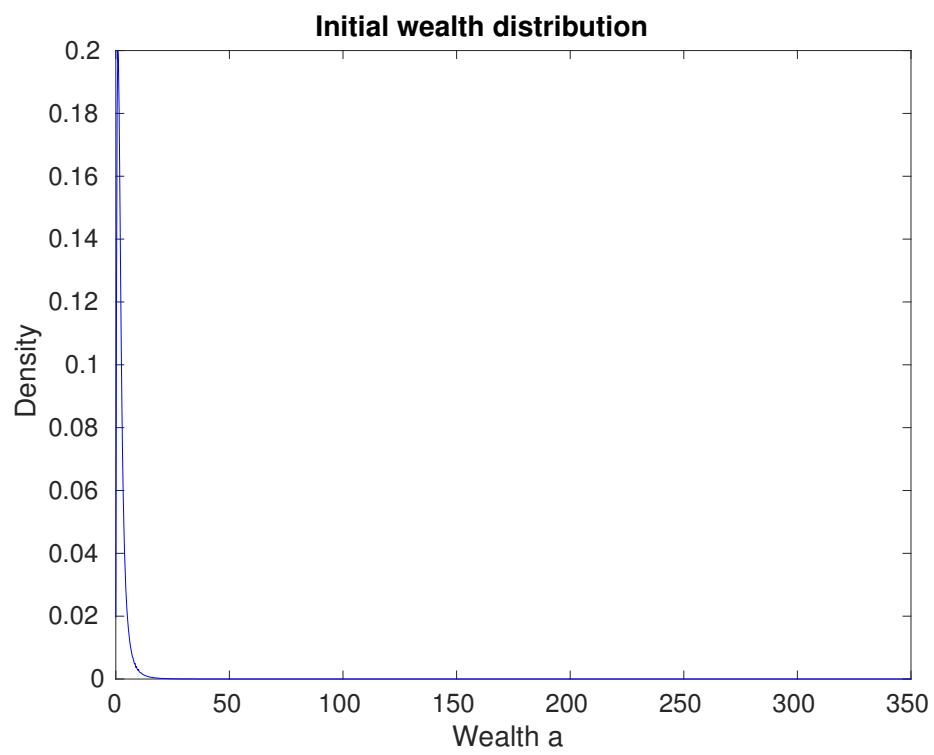


Figure 4

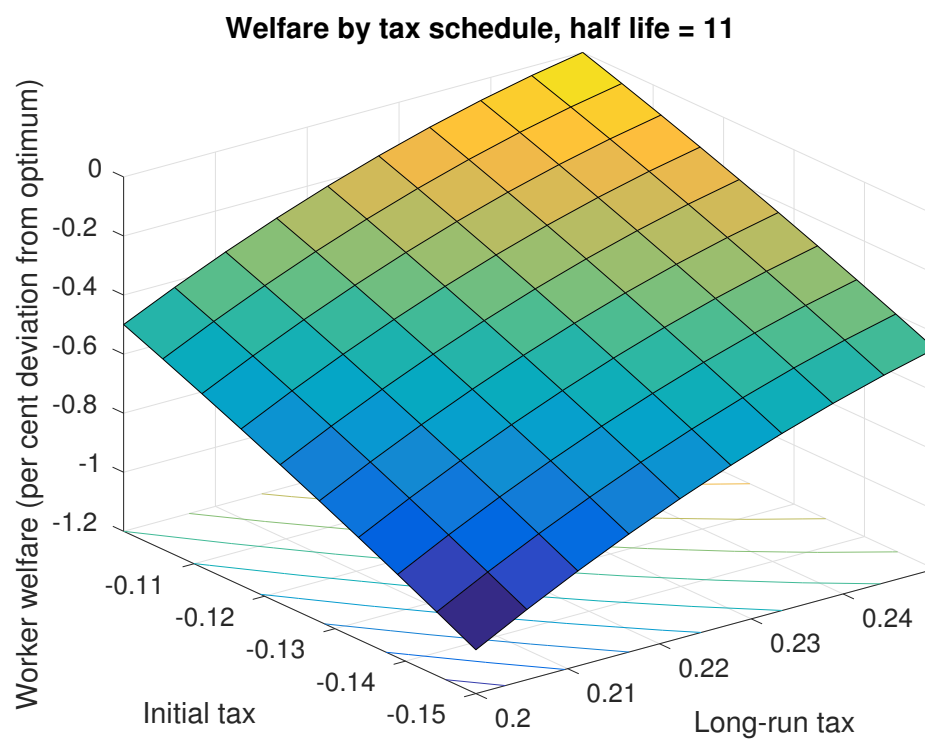


Figure 5

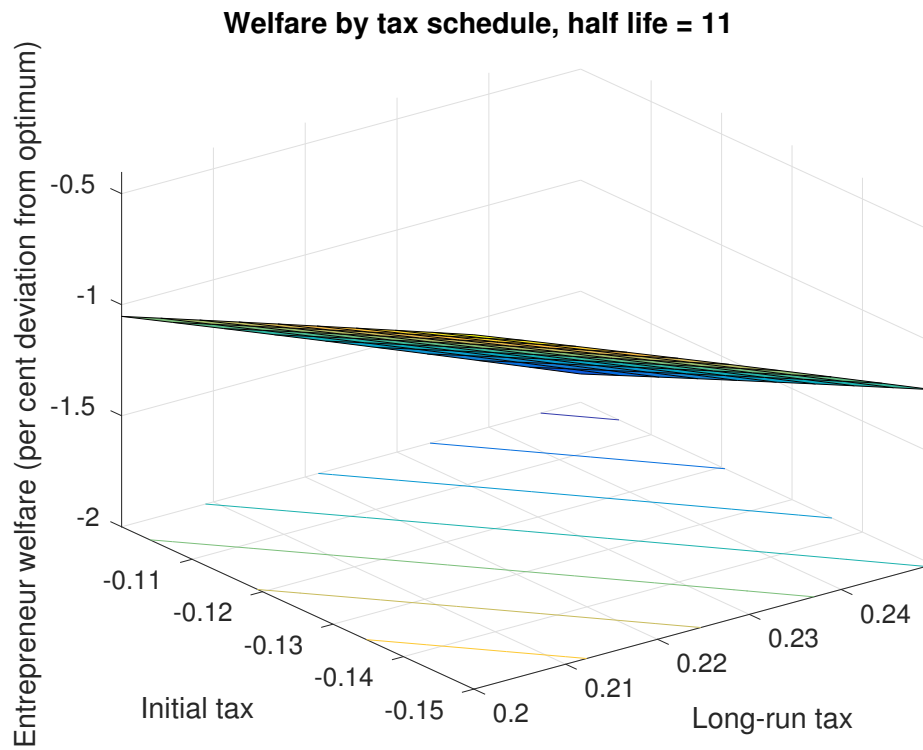


Figure 6

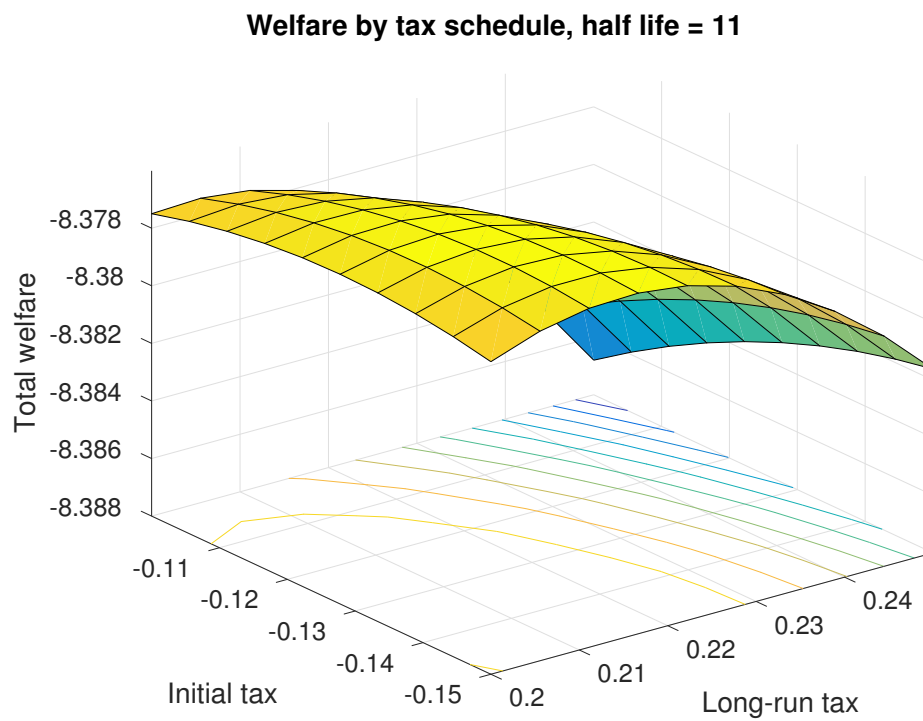


Figure 7

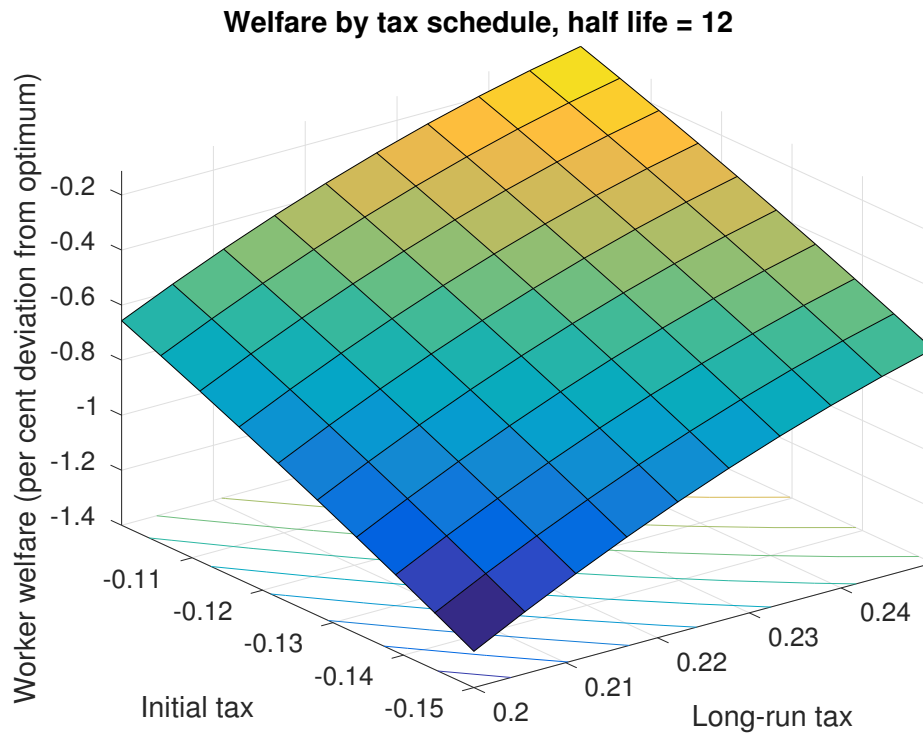


Figure 8

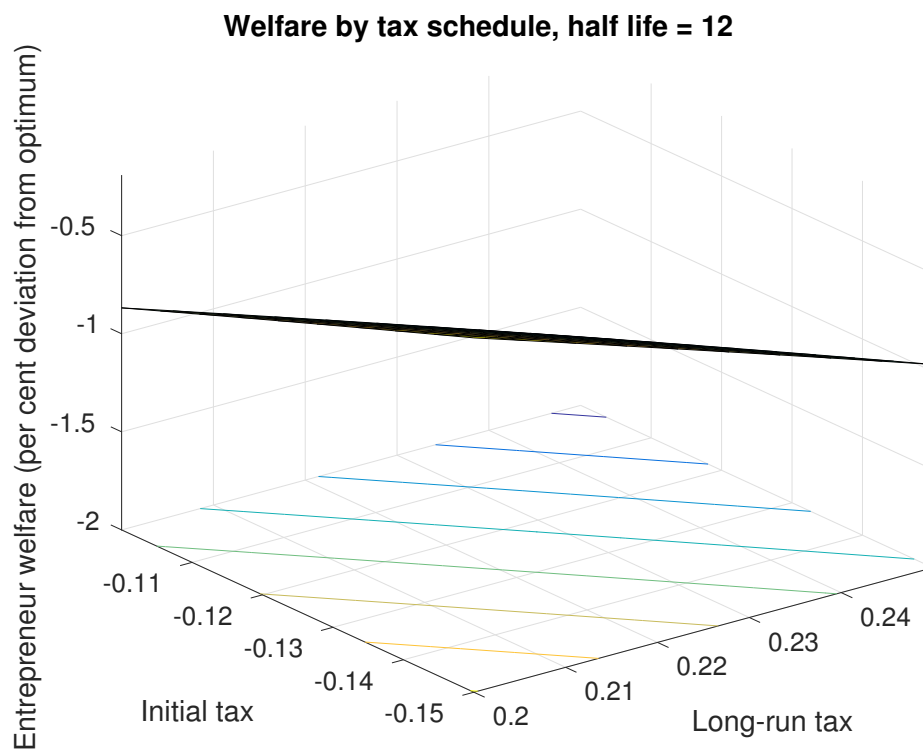


Figure 9

Welfare by tax schedule, half life = 12

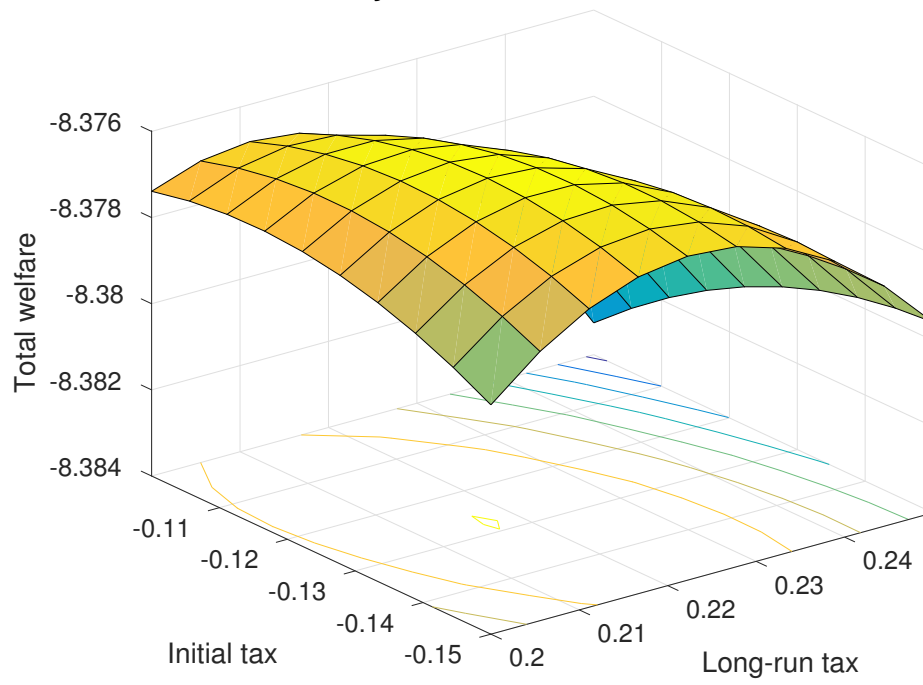


Figure 10

Welfare by tax schedule, half life = 13

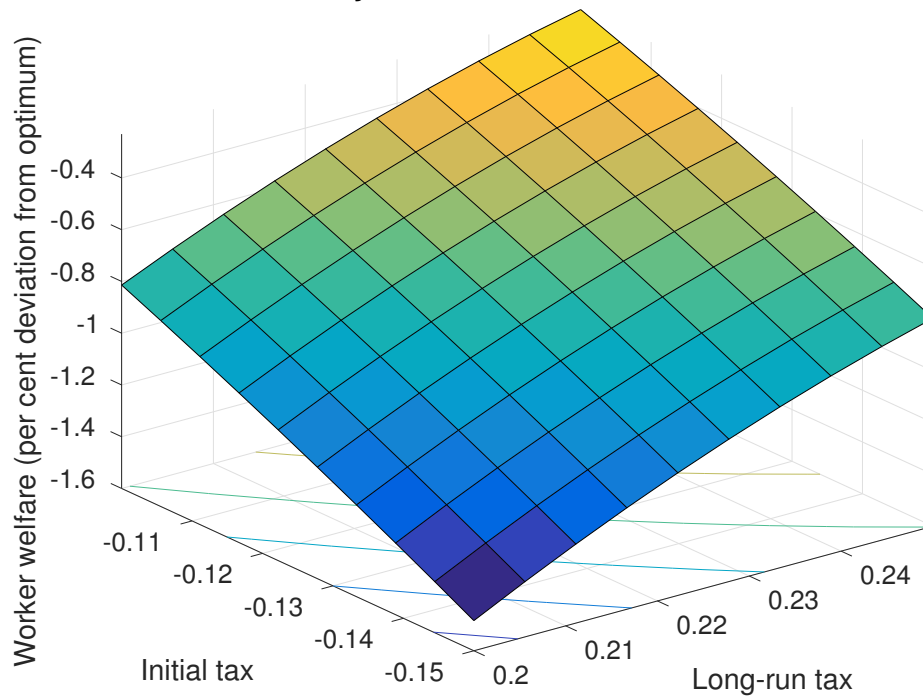


Figure 11

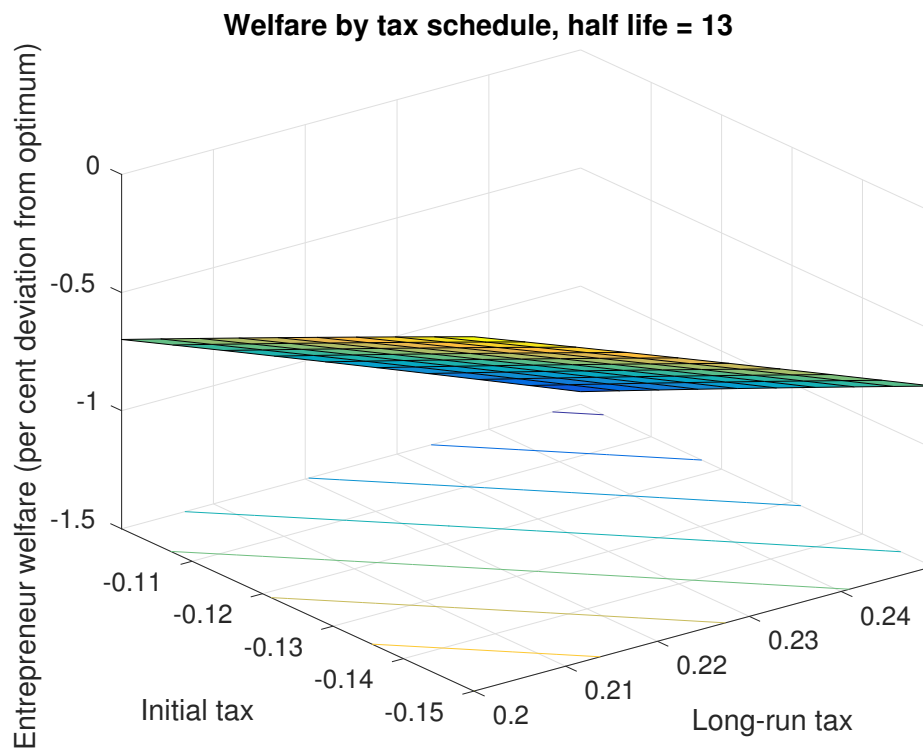


Figure 12

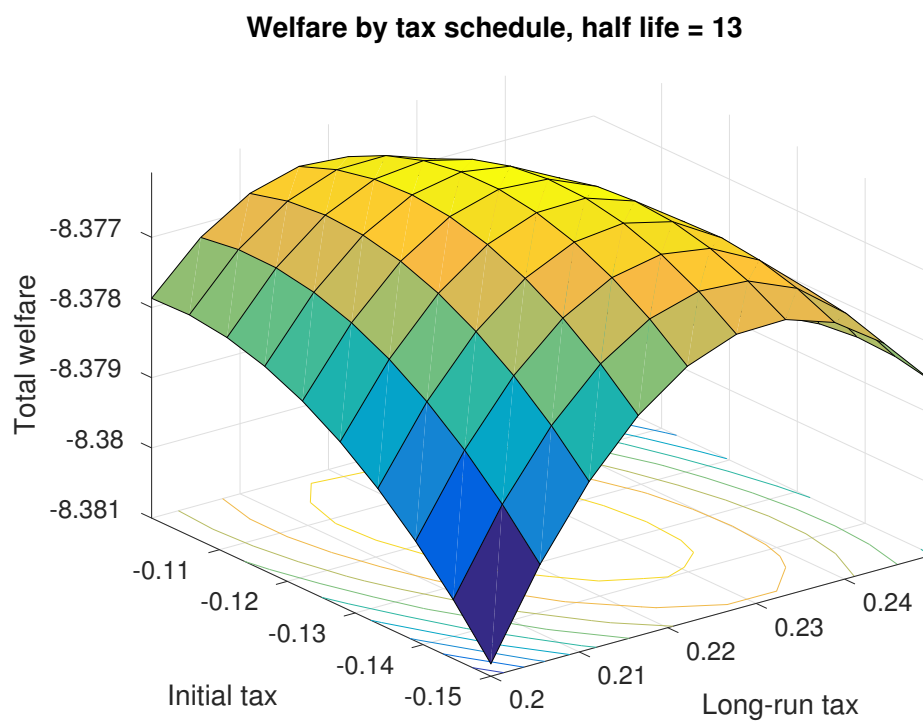


Figure 13

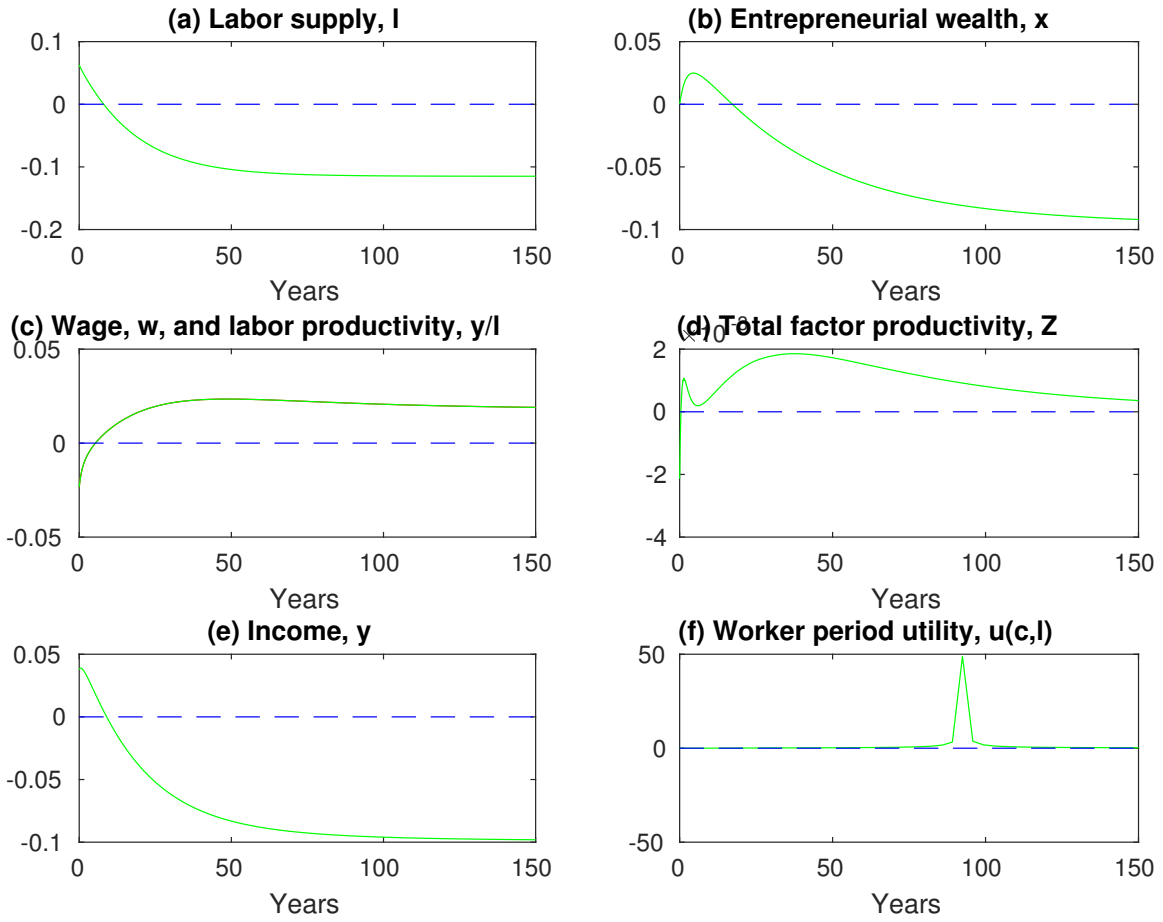


Figure 14 – Proportional deviations of optimal tax equilibrium from the laissez-faire equilibrium

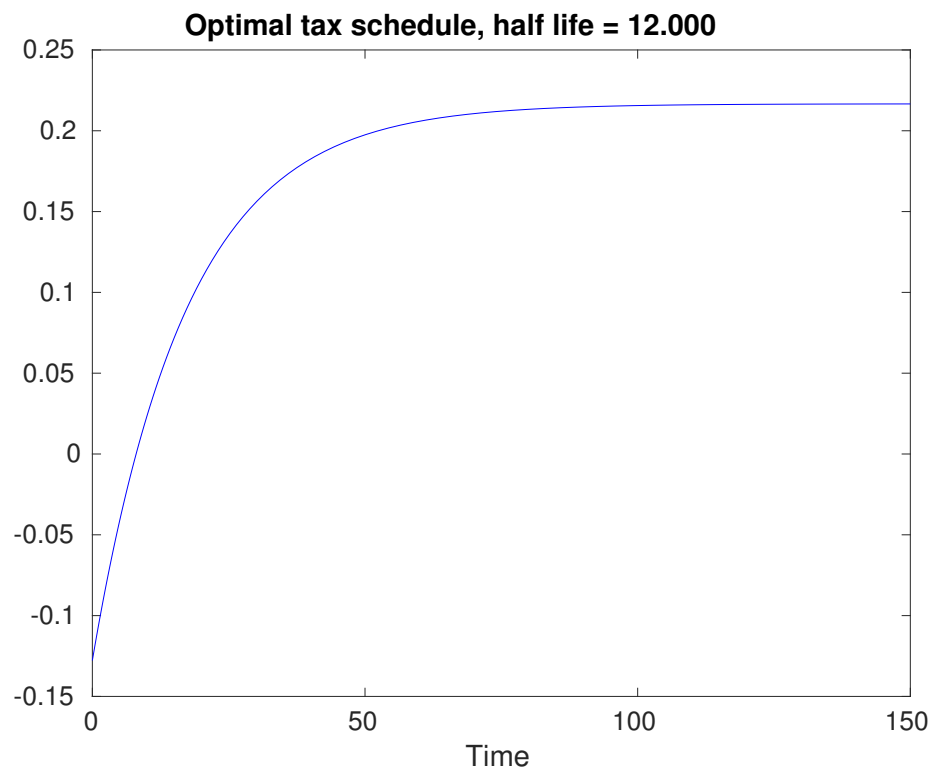


Figure 15

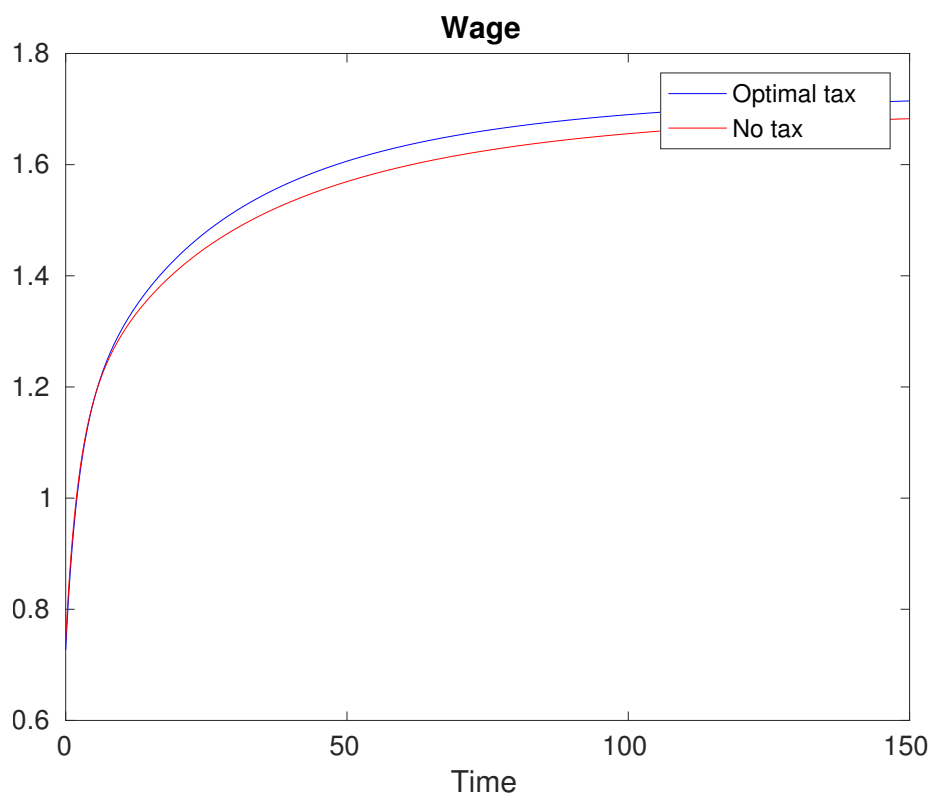


Figure 16

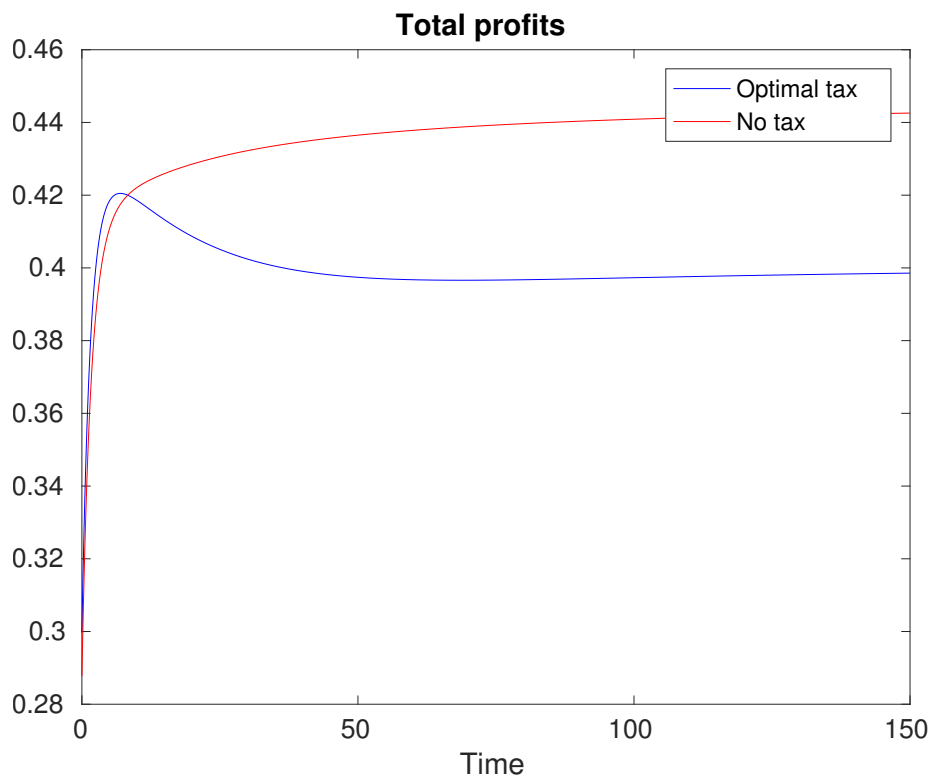


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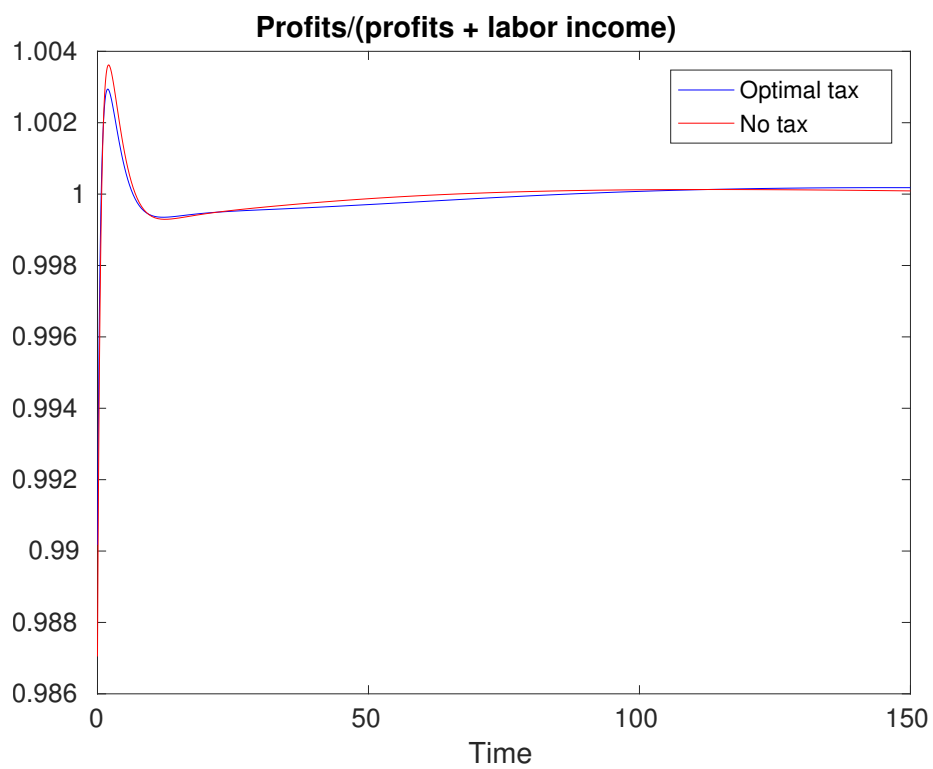


Figure 18

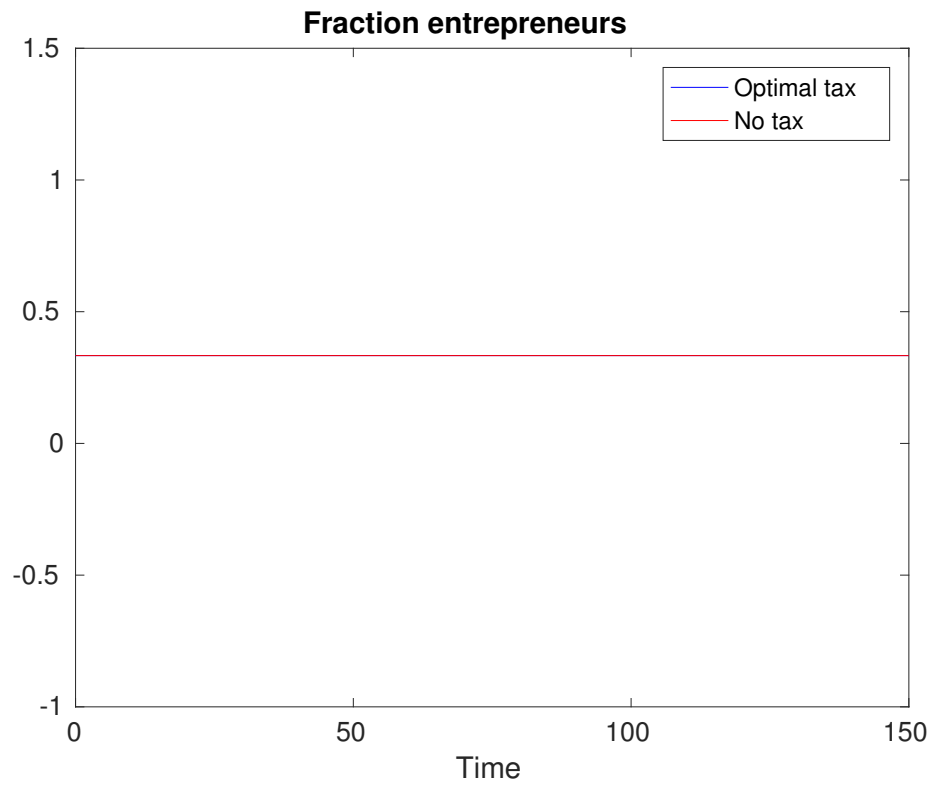


Figure 19

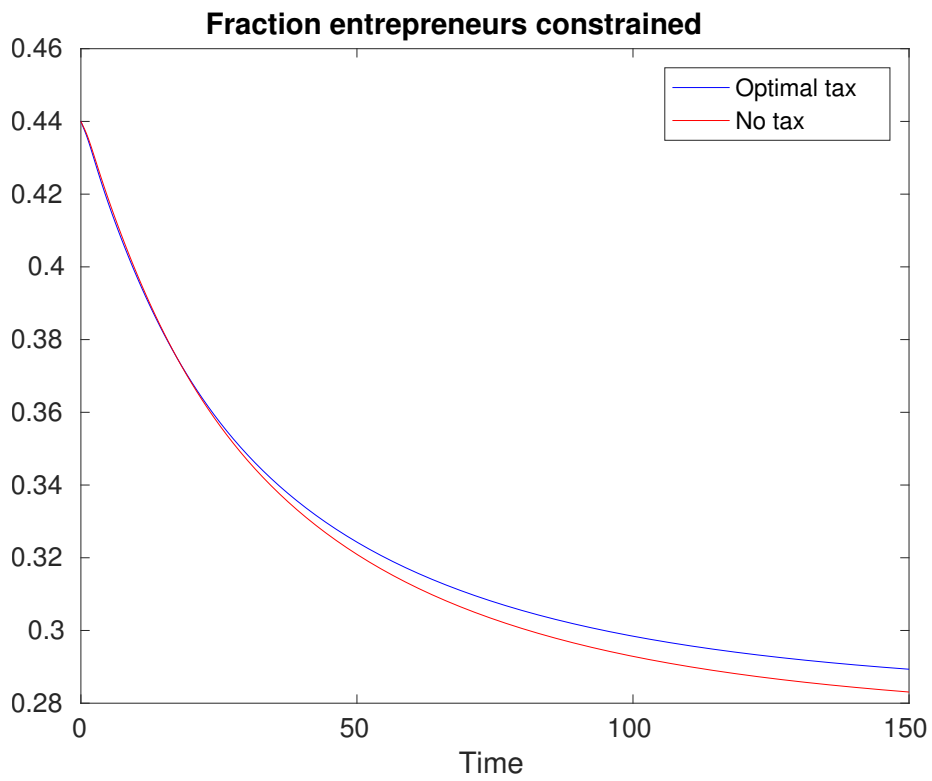


Figure 20

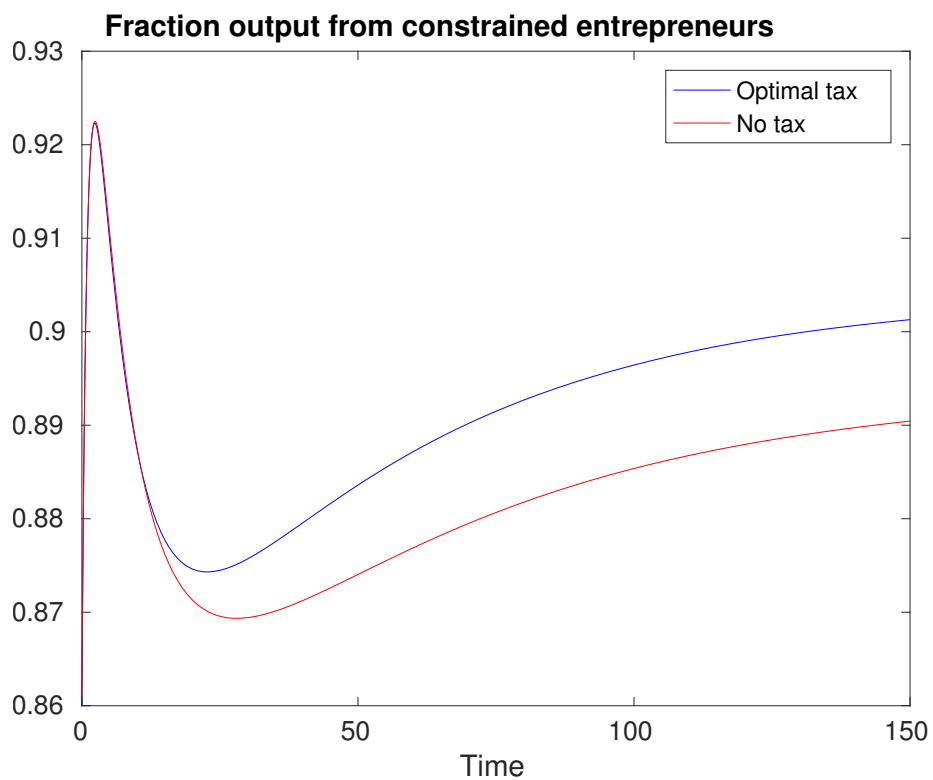


Figure 21

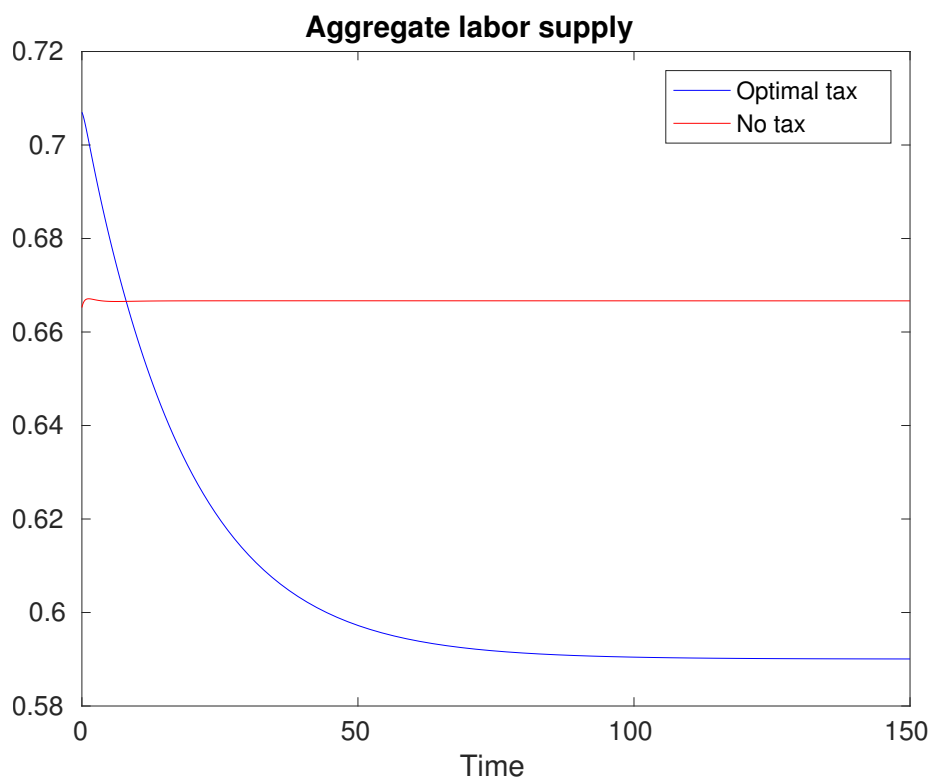


Figure 22

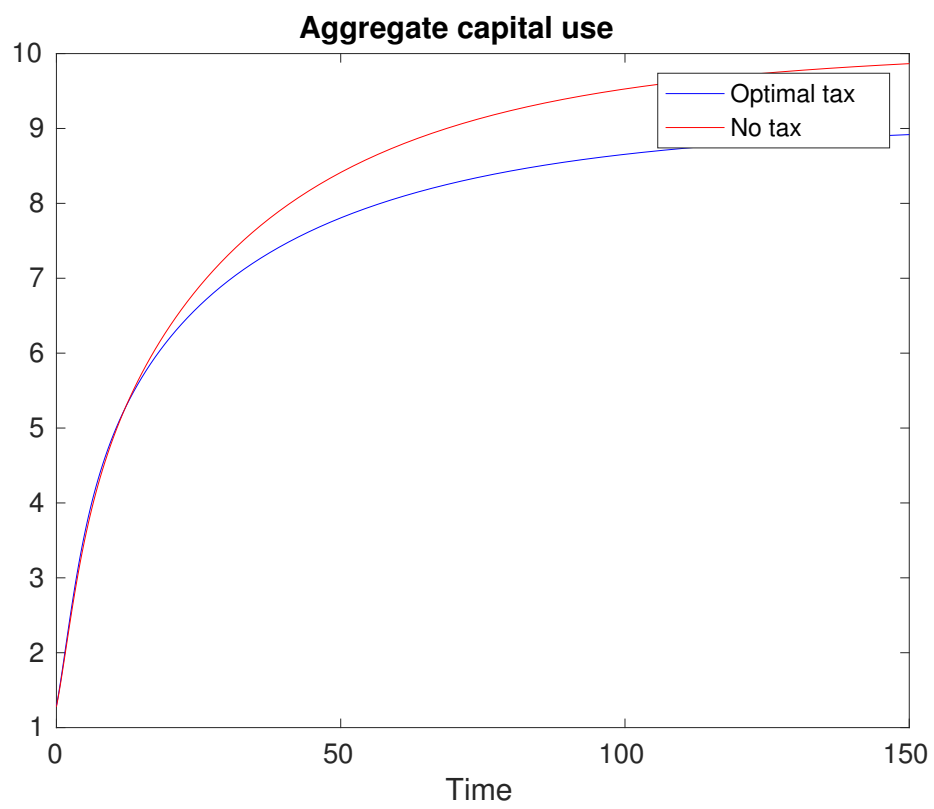


Figure 23

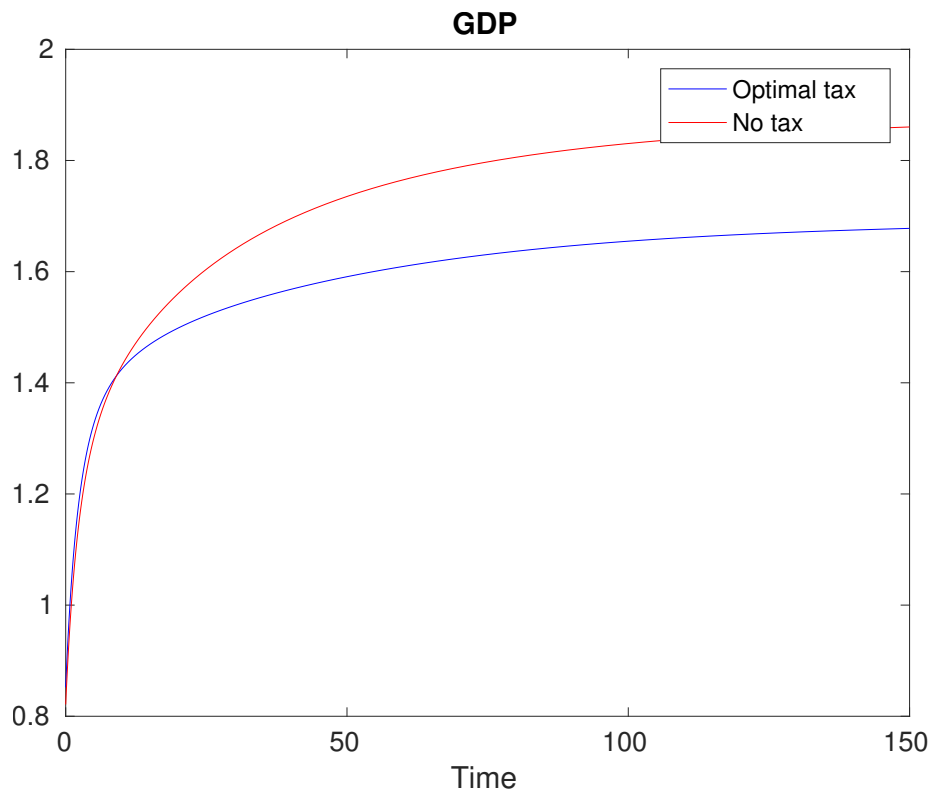


Figure 24

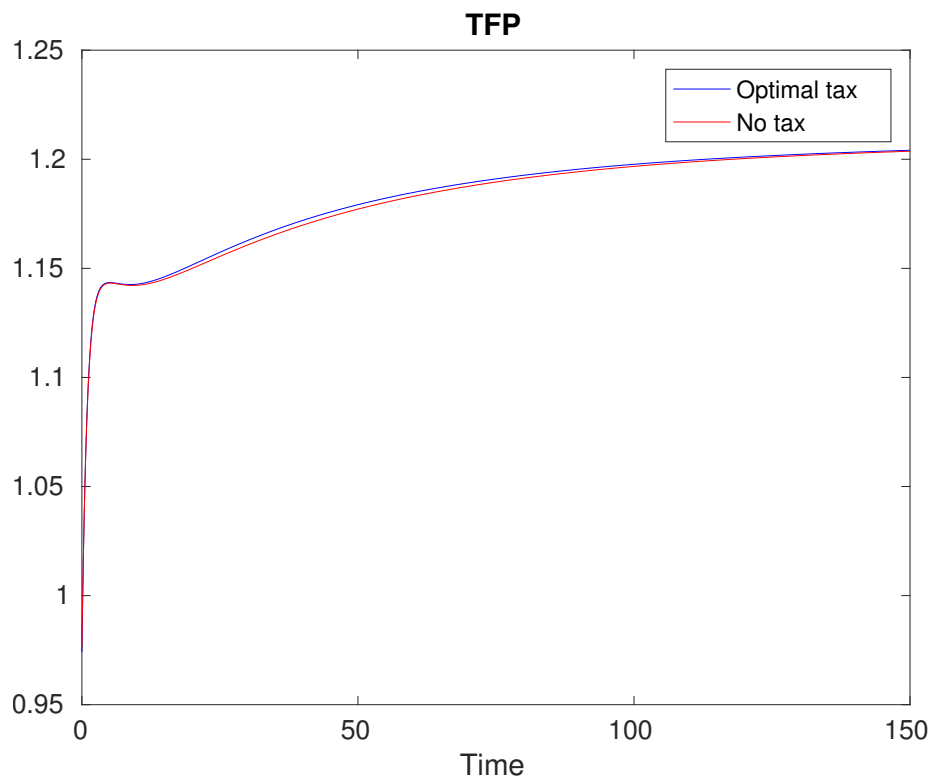


Figure 25

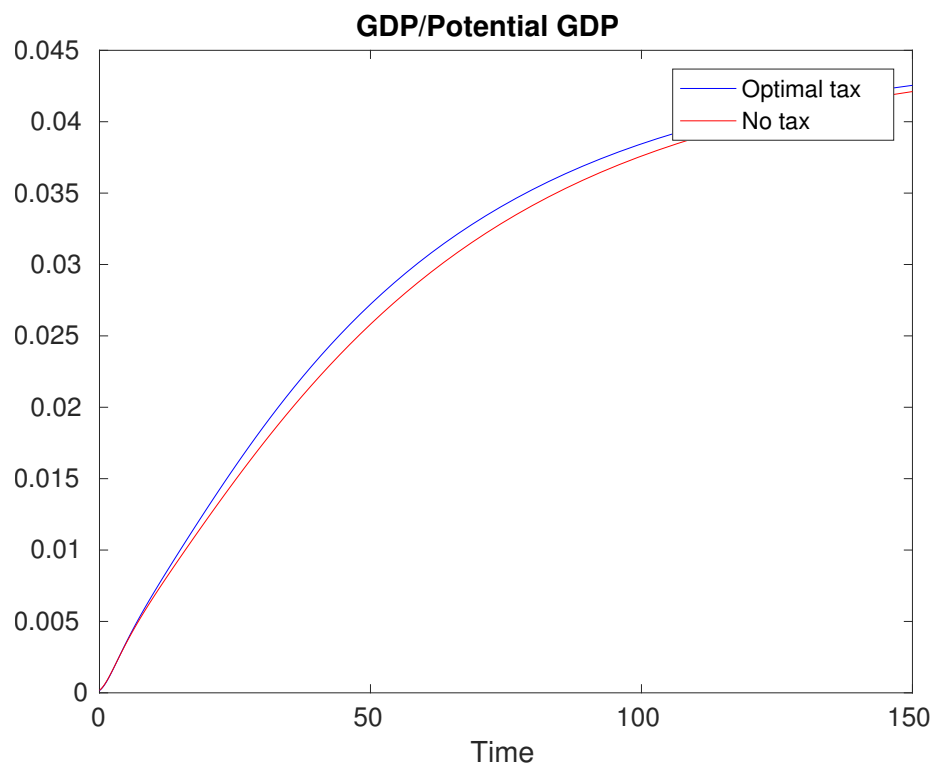


Figure 26

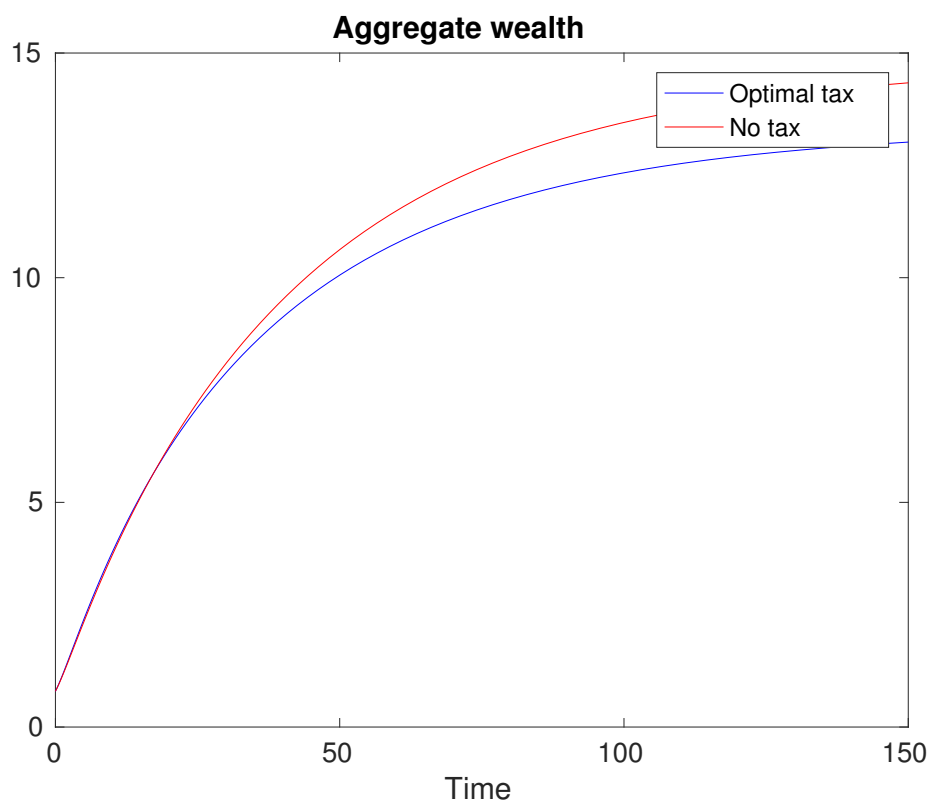


Figure 27

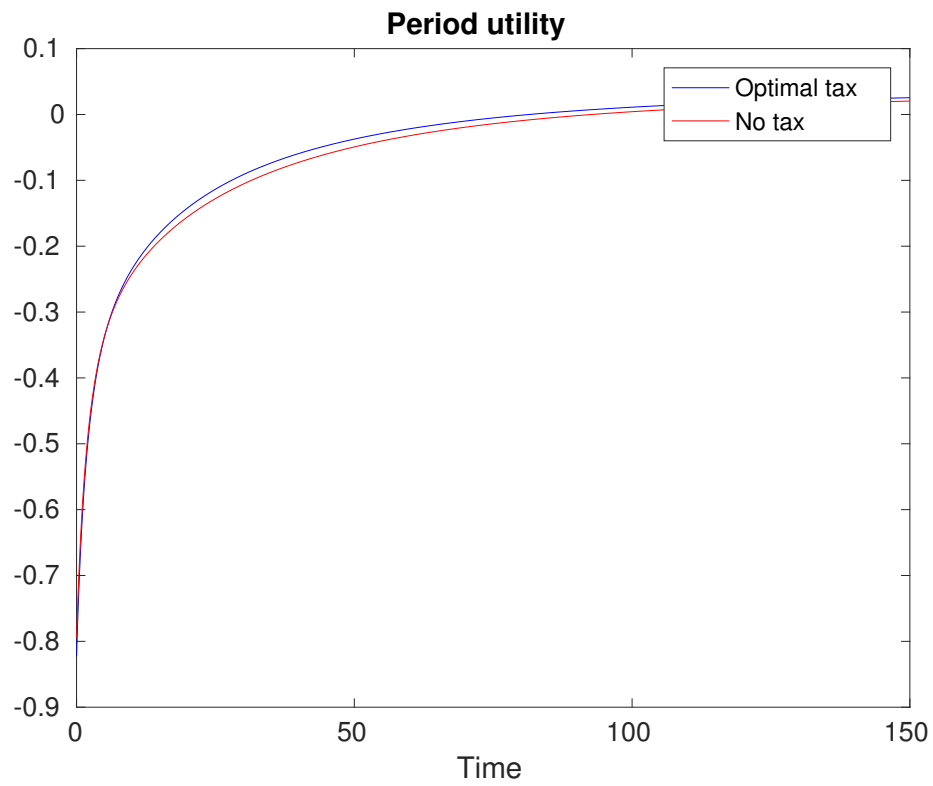


Figure 28

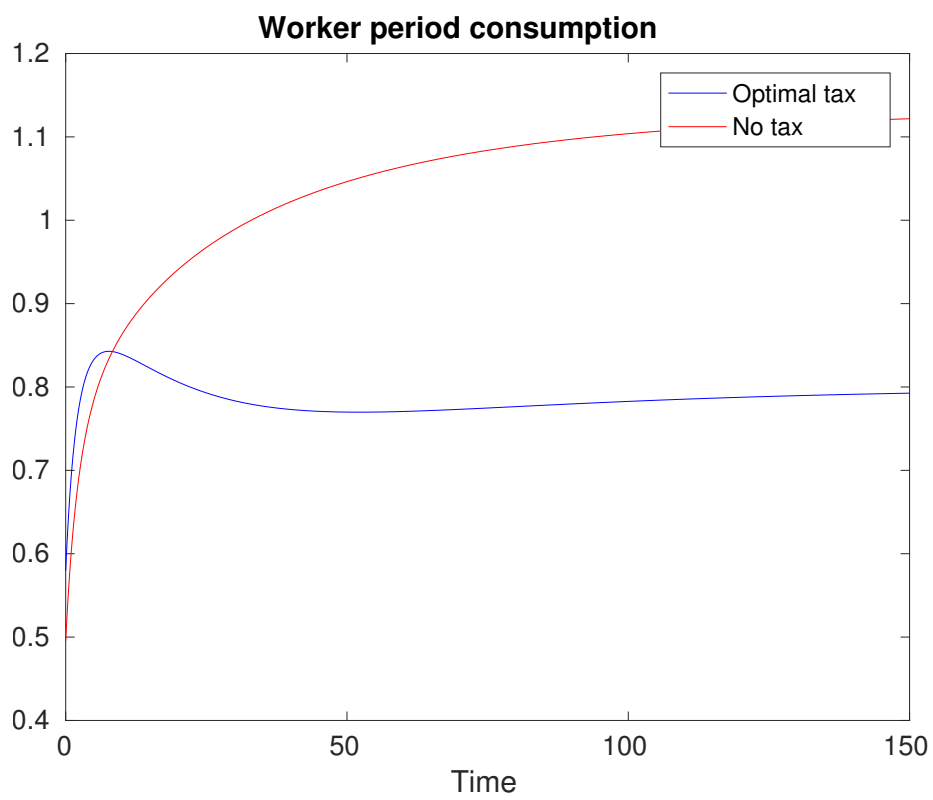


Figure 29