

## international collegiate programming contest ASIA REGIONAL CONTEST

### **ICPC JAKARTA 2024**



# Problem G X Aura

Mount ICPC can be represented as a grid of R rows (numbered from 1 to R) and C columns (numbered from 1 to C). The cell located at row r and column c is denoted as (r,c) and has a height of  $H_{r,c}$ . Two cells are adjacent to each other if they share a side. Formally, (r,c) is adjacent to (r-1,c), (r+1,c), (r,c-1), and (r,c+1), if any exists.

You can move only between adjacent cells, and each move comes with a penalty. With an aura of an **odd positive integer** X, moving from a cell with height  $h_1$  to a cell with height  $h_2$  gives you a penalty of  $(h_1-h_2)^X$ . Note that the penalty can be negative.

You want to answer Q independent scenarios. In each scenario, you start at the starting cell  $(R_s, C_s)$  and you want to go to the destination cell  $(R_f, C_f)$  with minimum total penalty. In some scenarios, the total penalty might become arbitrarily small; such a scenario is called *invalid*. Find the minimum total penalty to move from the starting cell to the destination cell, or determine if the scenario is invalid.

#### Input

The first line consists of three integers R C X ( $1 \le R$ ,  $C \le 1000$ ;  $1 \le X \le 9$ ; X is an odd integer).

Each of the next R lines consists of a string  $H_r$  of length C. Each character in  $H_r$  is a number from 0 to 9. The  $c^{\text{th}}$  character of  $H_r$  represents the height of cell (r,c), or  $H_{r,c}$ .

The next line consists of an integer Q ( $1 \le Q \le 100000$ ).

Each of the next Q lines consists of four integers  $R_s$   $C_s$   $R_f$   $C_f$   $(1 \le R_s, R_f \le R; 1 \le C_s, C_f \le C)$ .

#### Output

For each scenario, output the following in a single line. If the scenario is invalid, output INVALID. Otherwise, output a single integer representing the minimum total penalty to move from the starting cell to the destination cell.

#### Sample Input #1

3 4 1	
3359	
294	
8681	
. 1 3 4	
3 3 2 1	
2 2 1 4	
. 3 3 2	
. 1 1 1	

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#### Sample Output #1



#### Explanation for the sample input/output #1

For the first scenario, one of the solutions is to move as follows:  $(1,1) \rightarrow (2,1) \rightarrow (3,1) \rightarrow (3,2) \rightarrow (3,3) \rightarrow (3,4)$ . The total penalty of this solution is  $(3-4)^1+(4-3)^1+(3-6)^1+(6-8)^1+(8-1)^1=2$ .

#### Sample Input #2

```
2 4 5
1908
2023
2
1 1 2 4
1 1 1 1
```

#### Sample Output #2

INVALID			
INVALID			

#### Explanation for the sample input/output #2

For the first scenario, the cycle  $(1,1) \to (2,1) \to (2,2) \to (1,2) \to (1,1)$  has a penalty of  $(1-2)^5 + (2-0)^5 + (0-9)^5 + (9-1)^5 = -26250$ . You can keep repeating this cycle to make your total penalty arbitrarily small. Similarly, for the second scenario, you can move to (1,1) first, then repeat the same cycle.

#### Sample Input #3



#### Sample Output #3

