

## Problem I

### Count DFS Tree

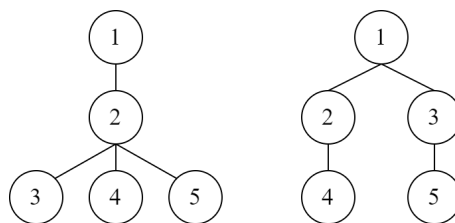
You are currently studying a tree traversal algorithm called the Depth First Search (DFS). Suppose you have a rooted tree of  $n$  nodes (numbered from 1 to  $n$ ) with a depth of  $K$  (numbered from 1 to  $K$ ). The root (the node at depth 1) is located at node 1. **All leaves are located at the same depth**, that is, at depth  $K$ . Node  $i$  has an array of children nodes  $c_i$ , which could be empty if  $i$  is a leaf node. The pseudocode of the algorithm is presented as follows.

```
DFS(u, depth):
    let res be an empty array
    append depth to res

    for each v in c[u]:
        let D be an array initialized with DFS(v, depth + 1)
        for each x in D:
            append x to res

    return res
```

Consider the trees in the following illustration. The return values of  $\text{DFS}(1, 1)$  for the tree on the left and the tree on the right are  $[1, 2, 3, 3, 3]$  and  $[1, 2, 3, 2, 3]$ , respectively.



Denote  $f_K(n)$  as the number of **distinct** return values of  $\text{DFS}(1, 1)$  across all trees consisting of  $n$  nodes and all leaves are located in depth  $K$ . You are given  $M$  integers:  $A_1, A_2, \dots, A_M$ . Determine the value of  $f_K(A_1) \times f_K(A_2) \times \dots \times f_K(A_M)$ . As the answer can be very large, find the answer modulo 998 244 353.

#### Input

The first line consists of two integers  $K$   $M$  ( $1 \leq K, M \leq 100\,000$ ).

The following line consists of  $M$  integers  $A_i$  ( $K \leq A_i \leq 200\,000$ ).

#### Output

Output a single integer representing the value of  $f_K(A_1) \times f_K(A_2) \times \dots \times f_K(A_M)$  modulo 998 244 353.

### Sample Input #1

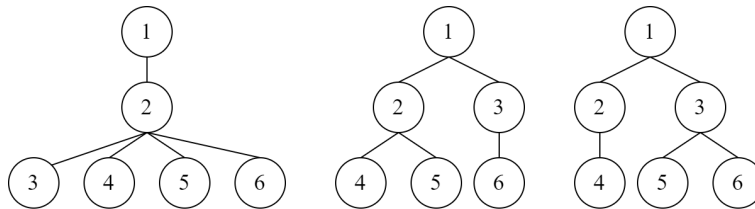
```
3 2
5 6
```

### Sample Output #1

```
6
```

*Explanation for the sample input/output #1*

The value of  $f_3(5)$  and  $f_3(6)$  are 2 and 3, respectively. The illustration on the description shows the trees of 5 nodes that give distinct return values of  $\text{DFS}(1, 1)$ . The following illustration is for the trees of 6 nodes.



### Sample Input #2

```
100000 1
200000
```

### Sample Output #2

```
269130693
```