

```
clearvars
format long
```

Research Techniques Project: Unit test

This is a unit test using the KIC 11924311 source since it has documented periodicity

Data Exploration

In this section we are exploring and displaying the raw data so it can be used for analysis

```
opts = detectImportOptions("KIC_11924311_Photometry.txt");
opts.DataLines = 2;
%opts.VariableNames = {'B_time','B_flux','R_time','R_flux','V_time','V_flux'};
opts.VariableNames = {'Time','Filter','Flux','error'};
```

"time" is in the units of days and "flux" is "rel_flux_T1" from AstrolmageJ outputs.

```
opts.VariableTypes = {'double','char','double','double'};
KIC_11924311 = rmmissing(readtable("KIC_11924311_Photometry.txt",opts)); %the matrix data of th
preview("KIC_11924311_Photometry.txt",opts)
```

ans = 8x4 table

	Time	Filter	Flux	error
1	5.79853725...	'B'	0.67636...	0.00297...
2	5.79853734...	'B'	0.68590...	0.00300...
3	5.79853742...	'B'	0.68147...	0.00299...
4	5.79853758...	'B'	0.69522...	0.00301...
5	5.79853766...	'B'	0.69789...	0.00303...
6	5.79853775...	'B'	0.69234...	0.00300...
7	5.79853783...	'B'	0.70016...	0.00303...
8	5.79853791...	'B'	0.69389...	0.00299...

```
whos KIC_11924311
```

Name	Size	Bytes	Class	Attributes
KIC_11924311	2957x4	386047	table	

```
filters = unique(KIC_11924311{:,2},'stable');
poscount = [1 0 0 0 0];
temp = zeros(1,4);

count = 1;
poscount(count+1) = poscount(count);
while char(filters(count))==char(KIC_11924311{poscount(count+1),2})
    poscount(count+1) = poscount(count+1) + 1;
end
KICB = KIC_11924311(poscount(count):poscount(count+1)-1,:)
```

KICB = 349x4 table

	Time	Filter	Flux	error
1	5.79853725...	'B'	0.67636...	0.00297...
2	5.79853734...	'B'	0.68590...	0.00300...
3	5.79853742...	'B'	0.68147...	0.00299...
4	5.79853758...	'B'	0.69522...	0.00301...
5	5.79853766...	'B'	0.69789...	0.00303...
6	5.79853775...	'B'	0.69234...	0.00300...
7	5.79853783...	'B'	0.70016...	0.00303...
8	5.79853791...	'B'	0.69389...	0.00299...
9	5.79853799...	'B'	0.70966...	0.00305...
10	5.79853807...	'B'	0.70262...	0.00302...
11	5.79853815...	'B'	0.70943...	0.00305...
12	5.79853823...	'B'	0.71280...	0.00305...
13	5.79853831...	'B'	0.71538...	0.00306...
14	5.79853840...	'B'	0.71921...	0.00314...

⋮

```
count = 2;
poscount(count+1) = poscount(count);
while char(filters(count))=char(KIC_11924311{poscount(count+1),2})
    poscount(count+1) = poscount(count+1) + 1;
end
KICV = KIC_11924311(poscount(count):poscount(count+1)-1,:)
```

KICV = 350x4 table

	Time	Filter	Flux	error
1	5.79853728...	'V'	0.72607...	0.00284...
2	5.79853736...	'V'	0.72676...	0.00284...
3	5.79853744...	'V'	0.72876...	0.00283...
4	5.79853752...	'V'	0.73102...	0.00284...
5	5.79853760...	'V'	0.73476...	0.00285...
6	5.79853769...	'V'	0.74009...	0.00287...
7	5.79853777...	'V'	0.74062...	0.00285...
8	5.79853785...	'V'	0.74477...	0.00287...
9	5.79853793...	'V'	0.74259...	0.00285...
10	5.79853801...	'V'	0.74713...	0.00287...
11	5.79853809...	'V'	0.74955...	0.00288...

	Time	Filter	Flux	error
12	5.79853817...	'V'	0.75450...	0.00289...
13	5.79853826...	'V'	0.76023...	0.00291...
14	5.79853834...	'V'	0.76027...	0.00292...

⋮

```
count = 3;
poscount(count+1) = poscount(count);
while char(filters(count))==char(KIC_11924311{poscount(count+1),2})
    poscount(count+1) = poscount(count+1) + 1;
end
KICR = KIC_11924311(poscount(count):poscount(count+1)-1,:)
```

KICR = 350x4 table

	Time	Filter	Flux	error
1	5.79853729...	'R'	0.74284...	0.00304...
2	5.79853737...	'R'	0.74455...	0.00306...
3	5.79853746...	'R'	0.75454...	0.00309...
4	5.79853754...	'R'	0.75485...	0.00307...
5	5.79853762...	'R'	0.75807...	0.00307...
6	5.79853770...	'R'	0.76211...	0.00308...
7	5.79853778...	'R'	0.76860...	0.00311...
8	5.79853787...	'R'	0.77020...	0.00313...
9	5.79853795...	'R'	0.76533...	0.00309...
10	5.79853803...	'R'	0.76891...	0.00309...
11	5.79853811...	'R'	0.76780...	0.00309...
12	5.79853819...	'R'	0.77622...	0.00313...
13	5.79853827...	'R'	0.78118...	0.00314...
14	5.79853835...	'R'	0.78604...	0.00316...

⋮

```
count = 4;
poscount(count+1) = poscount(count);
while char(filters(count))==char(KIC_11924311{poscount(count+1),2})
    poscount(count+1) = poscount(count+1) + 1;
end
KICI = KIC_11924311(poscount(count):poscount(count+1)-1,:)
```

KICI = 350x4 table

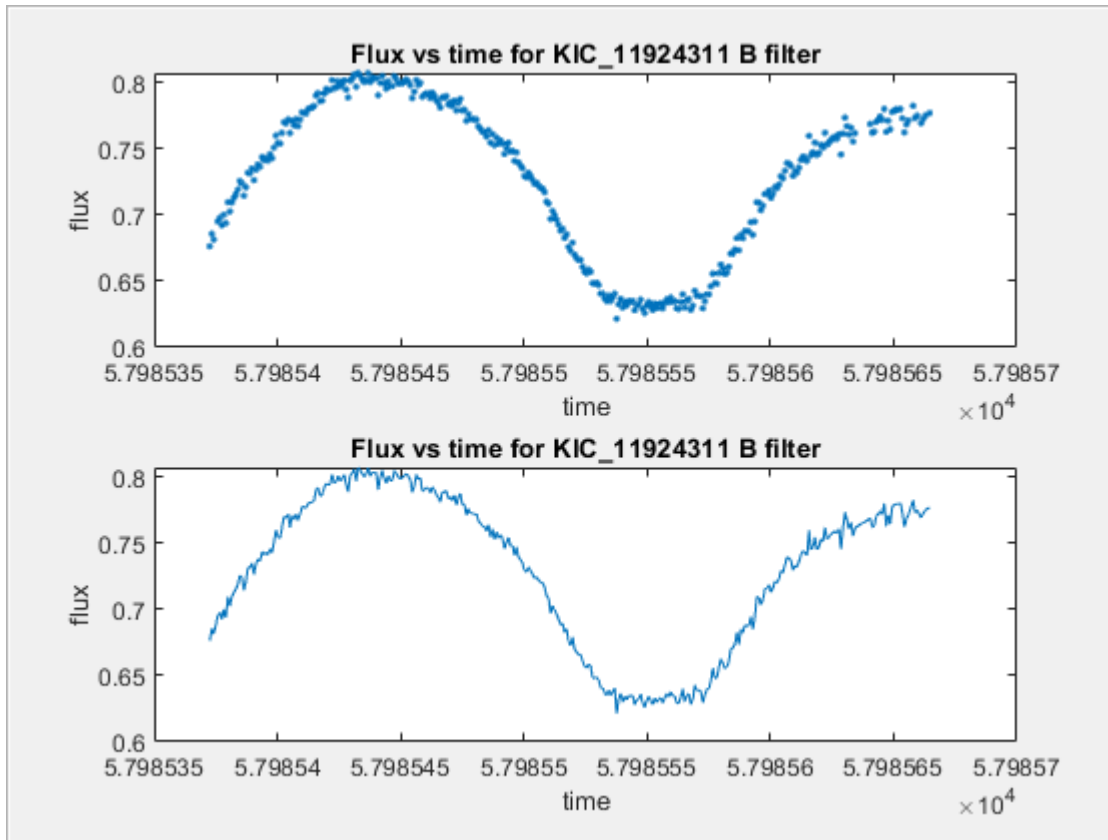
	Time	Filter	Flux	error
1	5.79853731...	'I'	0.76493...	0.00514...

	Time	Filter	Flux	error
2	5.79853739...	'I'	0.78074...	0.00526...
3	5.79853747...	'I'	0.77509...	0.00512...
4	5.79853755...	'I'	0.77435...	0.00518...
5	5.79853763...	'I'	0.78233...	0.00519...
6	5.79853772...	'I'	0.78959...	0.00518...
7	5.79853780...	'I'	0.78702...	0.00513...
8	5.79853788...	'I'	0.78799...	0.00519...
9	5.79853796...	'I'	0.79257...	0.00515...
10	5.79853805...	'I'	0.79262...	0.00514...
11	5.79853813...	'I'	0.79891...	0.00518...
12	5.79853821...	'I'	0.80309...	0.00517...
13	5.79853829...	'I'	0.81053...	0.00517...
14	5.79853837...	'I'	0.80186...	0.00522...

⋮

To understand the nature of the data, it is important to visualise it. This example is from the B filter. Error is ignored for the analysis in this project.

```
hf_sub(1) = figure(1);
hp(1) = uipanel('Parent',hf_sub(1),'Position',[0 0 1 1]);
subplot(2,1,1,'Parent',hp(1));
plot(KICB.Time,KICB.Flux,'.')
title('Flux vs time for KIC\11924311 B filter');
xlabel('time'),ylabel('flux');
subplot(2,1,2,'Parent',hp(1));
plot(KICB.Time,KICB.Flux),title('Flux vs time for KIC\11924311 B filter')
xlabel('time');
ylabel('flux');
```



Noting the graph above - displayed in discrete points and as a line graph - there is some periodicity.

```
r = abs([0; KICB.Time] - [KICB.Time;0]);
round(mean(r(3:end-1)),8)
```

```
ans =
    8.393100000000000e-04
```

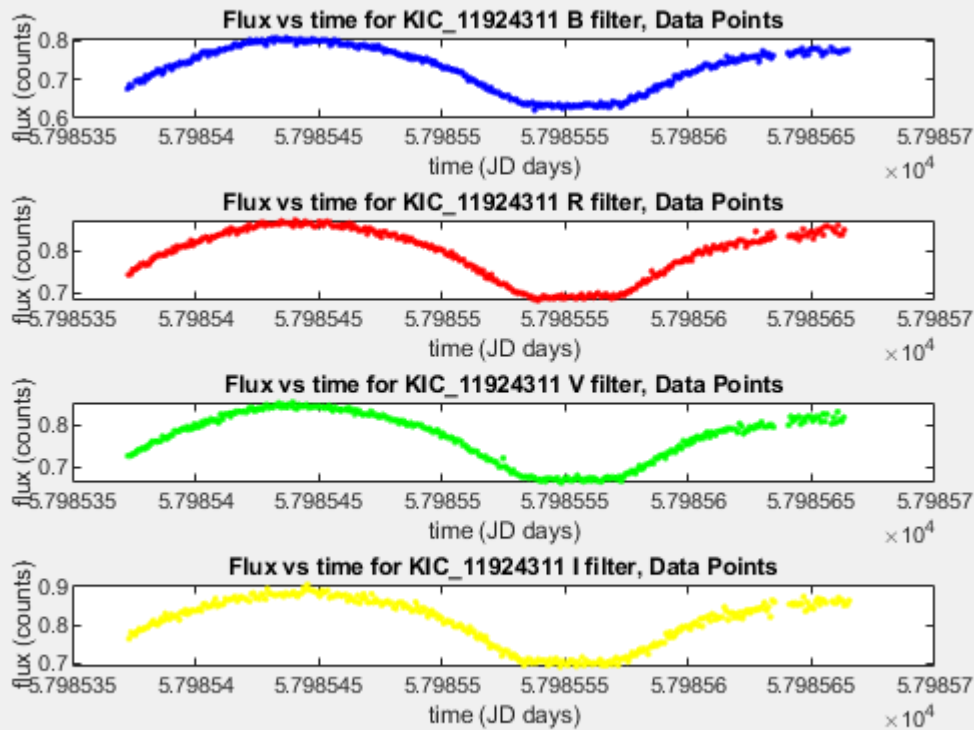
Periodicity between filters

```
hf_sub(2) = figure(2);
hp(2) = uipanel('Parent',hf_sub(2),'Position',[0 0 1 1]);
subplot(4,1,1,'Parent',hp(2));
% plotting in blue because B filter is blue light (~400-500 nm)
plot(KICB.Time,KICB.Flux,'.b');
title('Flux vs time for KIC_11924311 B filter, Data Points');
xlabel('time (JD days)');
ylabel('flux (counts)');
subplot(4,1,2,'Parent',hp(2));
% plotting in red because R filter is red light (~550-800 nm)
plot(KICR.Time,KICR.Flux,'.r');
title('Flux vs time for KIC_11924311 R filter, Data Points');
xlabel('time (JD days)');
ylabel('flux (counts)');
subplot(4,1,3,'Parent',hp(2));
% plotting green but V filter is visible light (~500-700 nm)
plot(KICV.Time,KICV.Flux,'.g');
title('Flux vs time for KIC_11924311 V filter, Data Points');
```

```

xlabel('time (JD days)');
ylabel('flux (counts)');
subplot(4,1,4,'Parent',hp(2));
% plotting green but I filter is visible light (~500-700 nm)
plot(KICI.Time,KICI.Flux,'.y');
title('Flux vs time for KIC_11924311 I filter, Data Points');
xlabel('time (JD days)');
ylabel('flux (counts)');

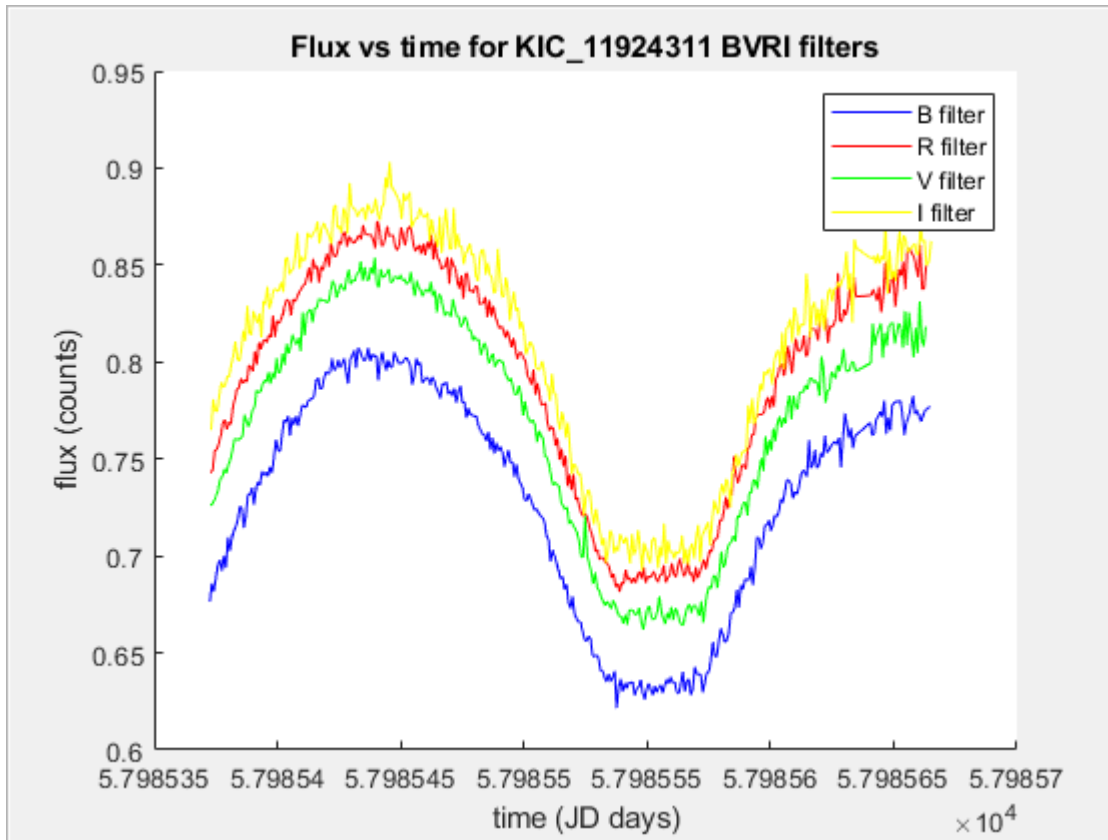
```



```

hf_sub(3) = figure(3);
hp(3) = uipanel('Parent',hf_sub(3),'Position',[0 0 1 1]);
subplot(1,1,1,'Parent',hp(3))
hold on
plot(KICB.Time,KICB.Flux, 'b')
plot(KICR.Time,KICR.Flux, 'r')
plot(KICV.Time,KICV.Flux, 'g')
plot(KICI.Time,KICI.Flux, 'y')
hold off
title('Flux vs time for KIC_11924311 BVRI filters');
xlabel('time (JD days)');
legend('B filter', 'R filter', 'V filter', 'I filter');
ylabel('flux (counts)');

```



Interpolation investigation

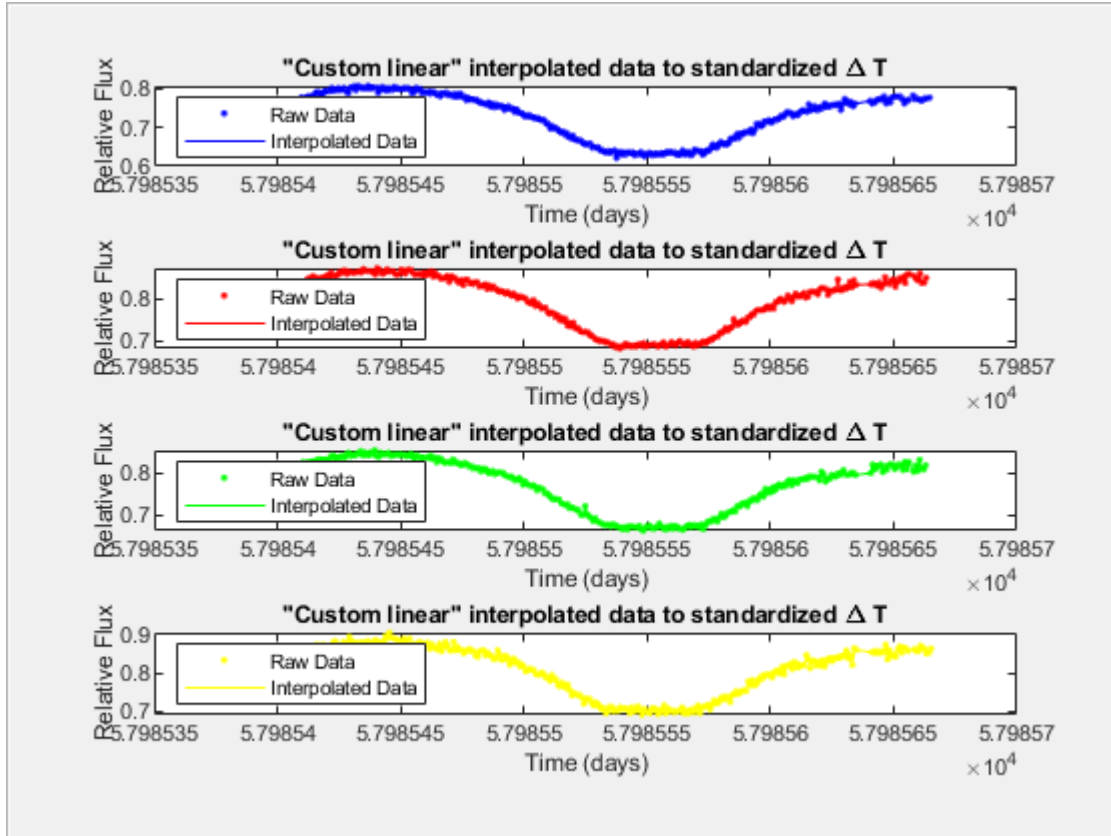
Custom linear function interpolation is shown here. Polyfit was a poor approximation but nearest or spline could also be used - check progress work.

```
hf_sub(4) = figure(4);
hp(4) = uipanel('Parent',hf_sub(4),'Position',[0 0 1 1]);
subplot(4,1,1,'Parent',hp(4));
[Tnew,Mnew] = Interp_Lin(KICB.Time,KICB.Flux);
plot(KICB.Time,KICB.Flux,'.b',Tnew,Mnew,'b');
title('"Custom linear" interpolated data to standardized \Delta T');
legend('Raw Data','Interpolated Data','location','northwest');
xlabel('Time (days)');
ylabel('Relative Flux');
subplot(4,1,2,'Parent',hp(4));
[Tnew,Mnew] = Interp_Lin(KICR.Time,KICR.Flux);
plot(KICR.Time,KICR.Flux,'.r',Tnew,Mnew,'r');
title('"Custom linear" interpolated data to standardized \Delta T');
legend('Raw Data','Interpolated Data','location','northwest');
xlabel('Time (days)');
ylabel('Relative Flux');
subplot(4,1,3,'Parent',hp(4));
[Tnew,Mnew] = Interp_Lin(KICV.Time,KICV.Flux);
plot(KICV.Time,KICV.Flux,'.g',Tnew,Mnew,'g');
title('"Custom linear" interpolated data to standardized \Delta T');
legend('Raw Data','Interpolated Data','location','northwest');
xlabel('Time (days)');
```

```

ylabel('Relative Flux');
subplot(4,1,4,'Parent',hp(4));
[Tnew,Mnew] = Interp_Lin(KICI.Time,KICI.Flux);
plot(KICI.Time,KICI.Flux,'.y',Tnew,Mnew,'y');
title('"Custom linear" interpolated data to standardized \Delta T');
legend('Raw Data','Interpolated Data','location','northwest');
xlabel('Time (days)');
ylabel('Relative Flux');

```



Fourier transform

This is the source for implementing Fourier Transform for a Noisy Signal from the MathWorks documentation

We chose linear interpolation for the purposes of this experiment at random.

Documentation: We used a combination of the following sources to develop this:

1. https://www.mathworks.com/help/matlab/ref/fft.html?searchHighlight=fft&s_tid=srchtitle (This is the source for implementing Fourier Transform for a Noisy Signal from the MathWorks documentation)
2. Gilat, Example 7-6 (pg. 281)
3. Gilat, Example 7-8 (pg 287)

```

[Tnew,Mnew] = Interp_Lin(KICB.Time,KICB.Flux);
Tnew = Tnew*86400; %convert time from days to seconds
deltaT = Tnew(2)-Tnew(1);
Fs = 1/deltaT; % Sampling frequency

```

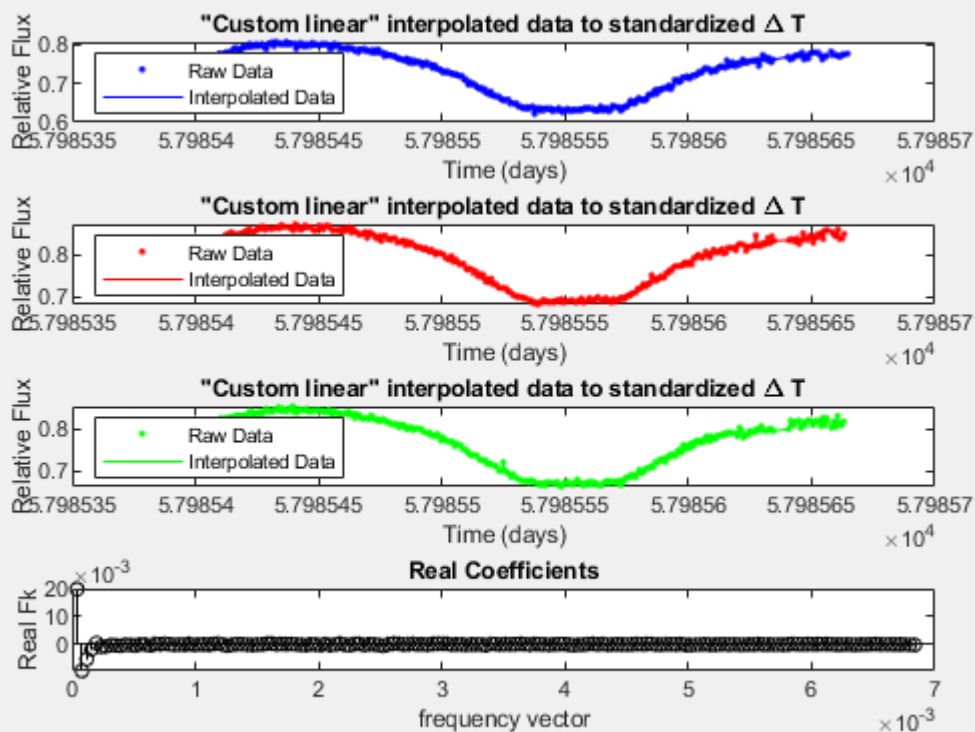


```

T = deltaT; % Sampling period
t = Tnew-Tnew(1); % Time vector
L = numel(Tnew); % Length of signal
X = Mnew ; %signal with noise

%Fourier transformation %Based on Ex 7-6 Gilat
F = fft(X)/L ; %fourier transform divided by number of data points
power = F.*conj(F)/L;
powernorm = power/max(power); %normalized power spectrum
fk = (0:L-1)*(Fs/L); %frequency vector Gilat 7-6
stem(fk(2:floor(L/2)),real(F(2:floor(L/2))), 'ko','markersize',5) %Threw out first
xlabel('frequency vector')
ylabel('Real Fk')
title('Real Coefficients')

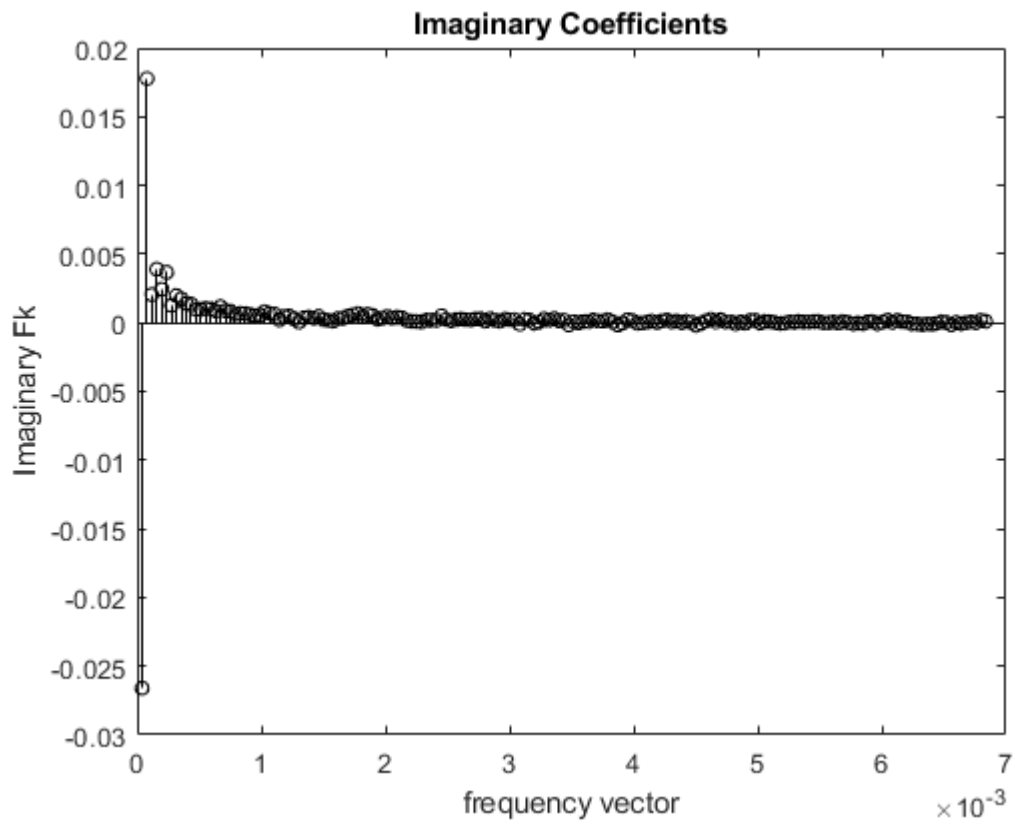
```



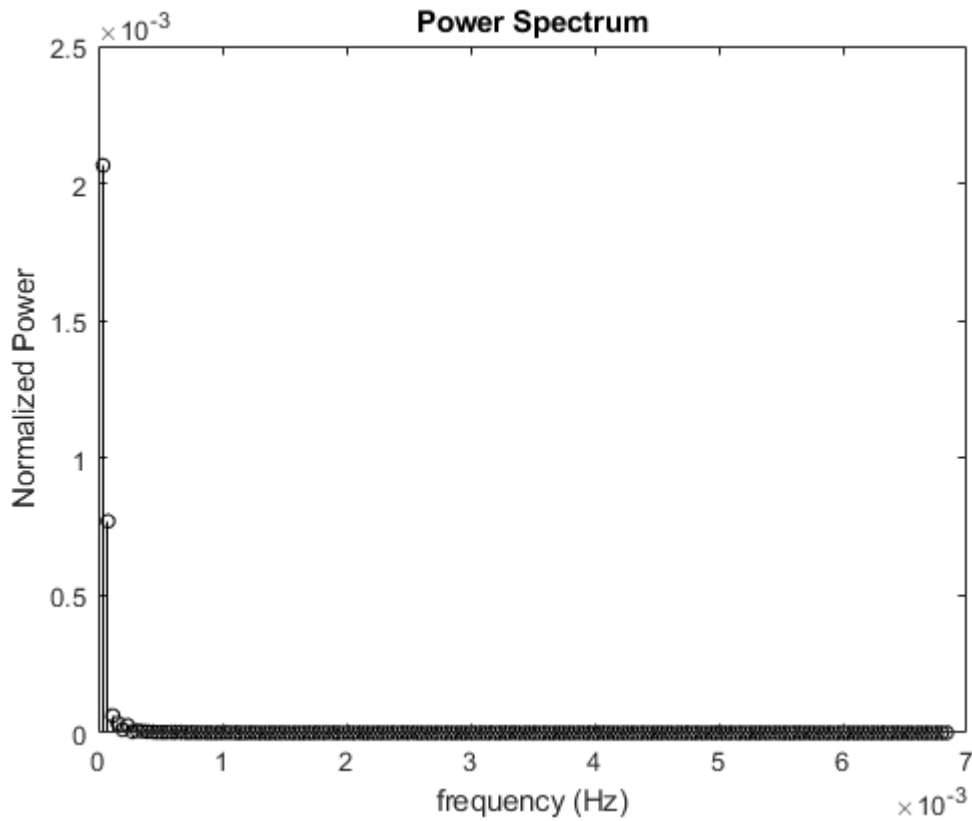
```

figure, stem(fk(2:floor(L/2)),imag(F(2:floor(L/2))), 'ko','markersize',5)
xlabel('frequency vector')
ylabel('Imaginary Fk')
title('Imaginary Coefficients')

```



```
figure, stem(fk(2:floor(L/2)),powernorm(2:floor(L/2)),'ko','markersize',5)
xlabel('frequency (Hz)')
ylabel('Normalized Power')
title('Power Spectrum')
```



```
%Rearrange the spectrum using fftshift
```

```
C0 = fftshift(F(2:L)); %zero frequency in center (threw out first number of F as a
```

```
power0 = C0.*conj(C0)/L-1;
```

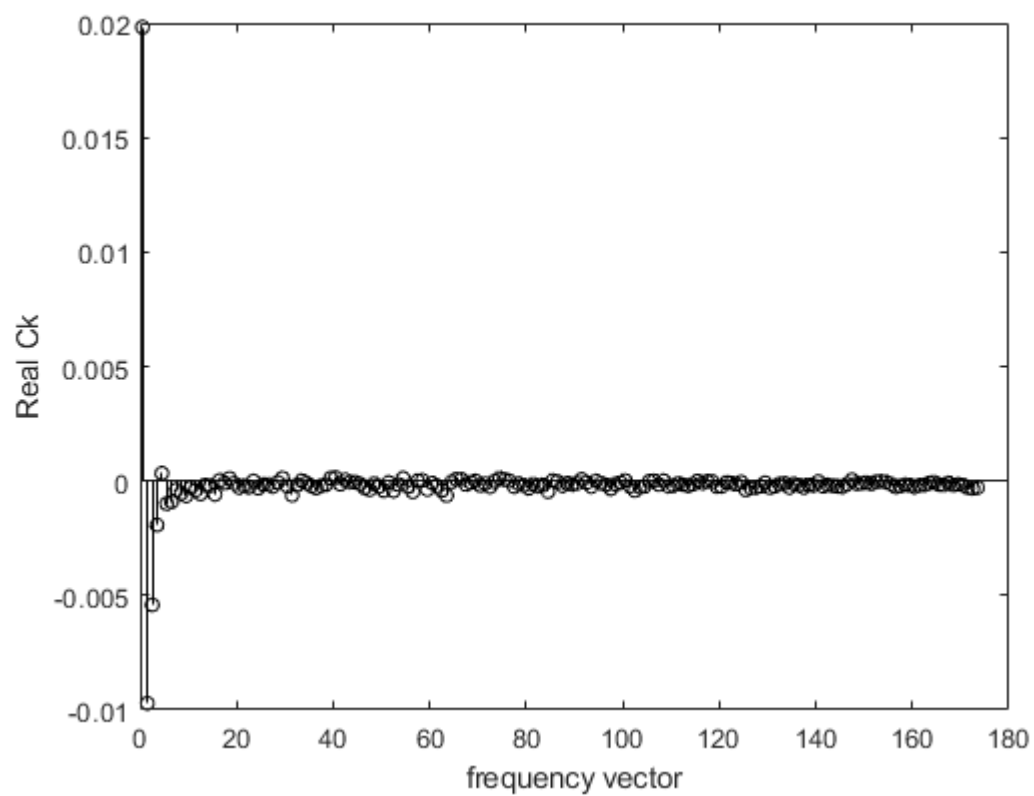
```
powernorm0 = power0/max(power0); %normalized power spectrum
```

```
fk0 = (-L/2+1:L/2-1)*(Fs/L-1); %frequency vector Gilat 7-6
```

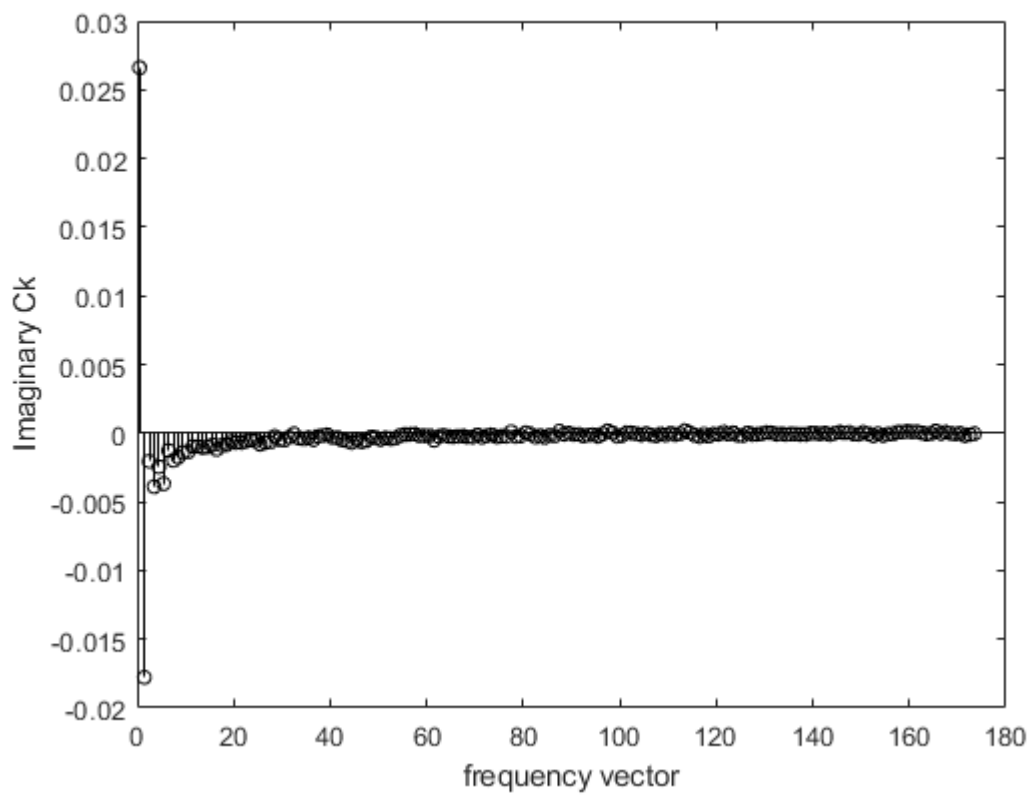
```
stem(fk0(1:floor(L/2)),real(C0(1:floor(L/2))), 'ko','markersize',5)
```

```
xlabel('frequency vector')
```

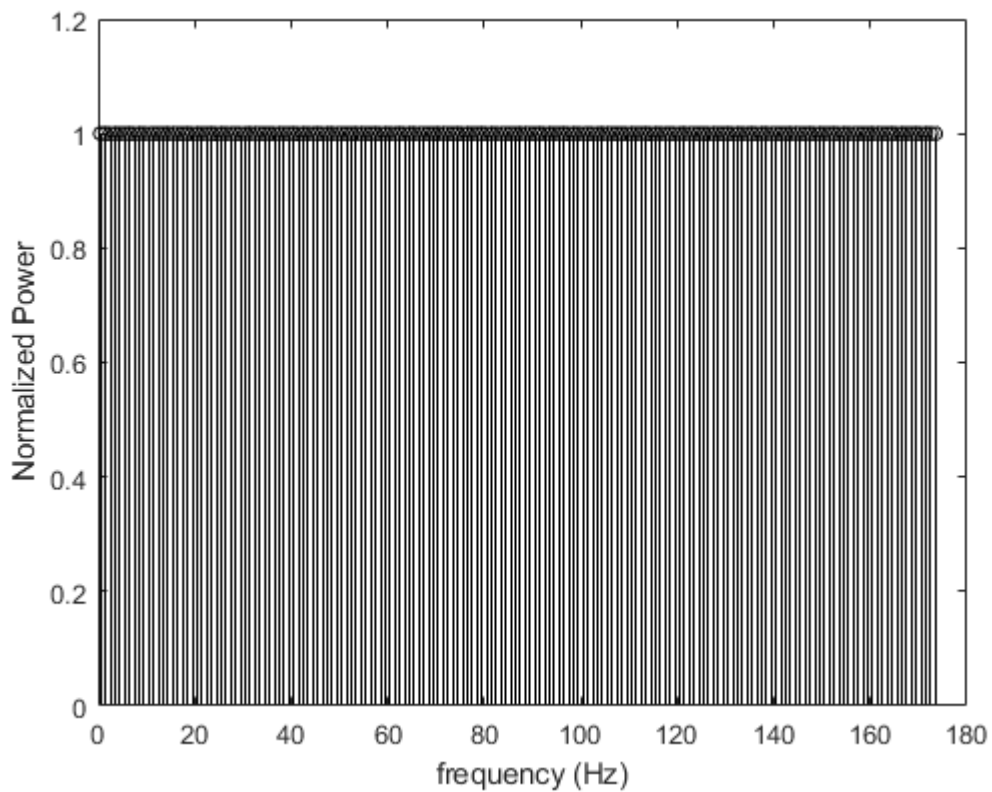
```
ylabel('Real Ck')
```



```
figure, stem(fk0(1:floor(L/2)),imag(C0(1:floor(L/2))), 'ko', 'markersize', 5)
xlabel('frequency vector')
ylabel('Imaginary Ck')
```



```
figure, stem(fk0(1:floor(L/2)),powernorm0(1:floor(L/2)),'ko','markersize',5)
xlabel('frequency (Hz)')
ylabel('Normalized Power')
```



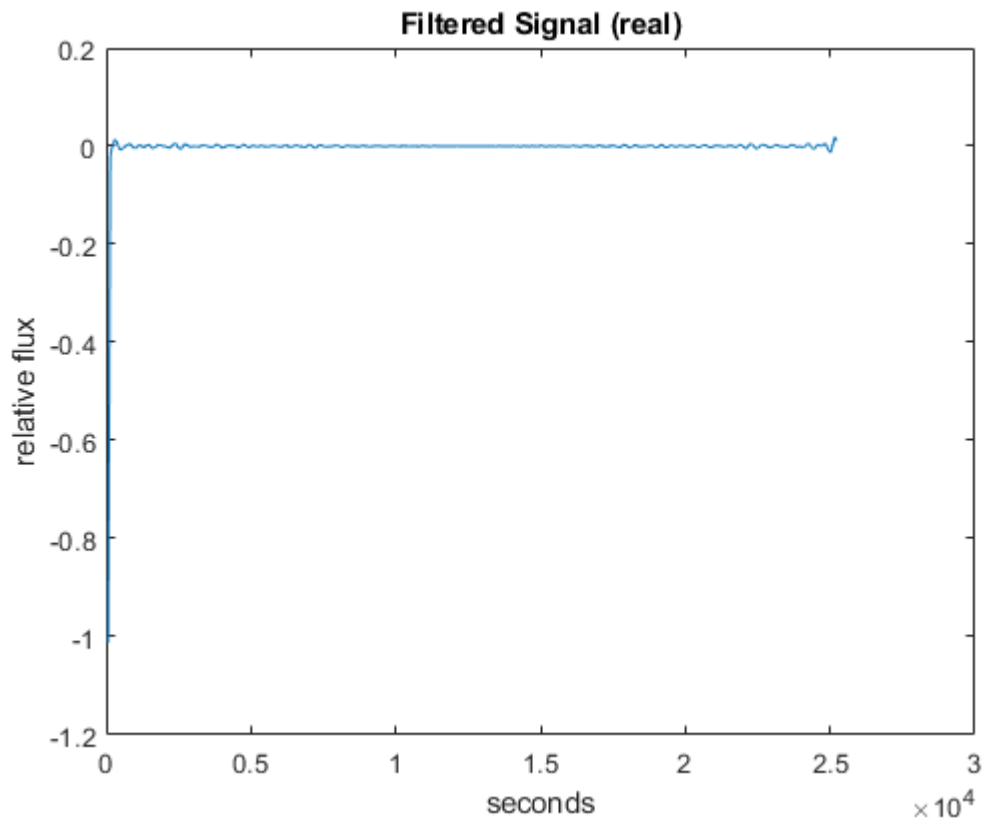
This approach has failed because there appears to not be much noise in the original source which has led to a difficulty to remove noise.

%Filtering out the noise **Based on Gilat Example 7-8**

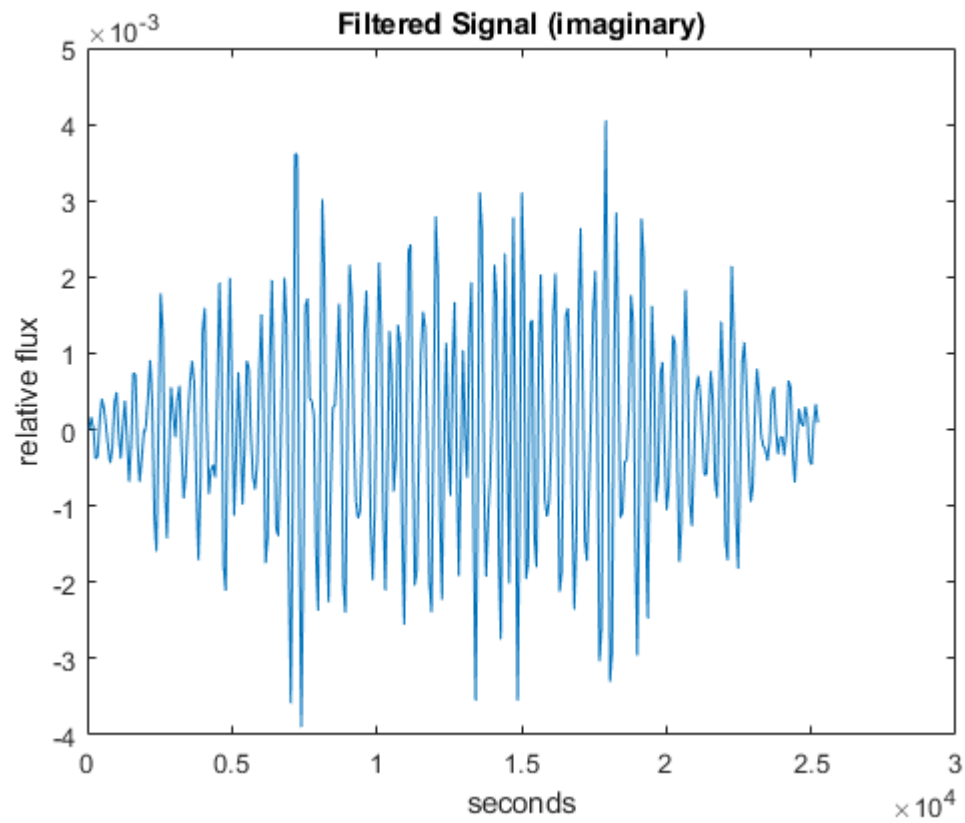
```
for k = 1:L-1
    if abs(fk0(k)) <= 50 || abs(fk0(k)) >= 90
        C0filter(k) = 0+0i;

    else
        C0filter(k) = C0(k);
    end
end
```

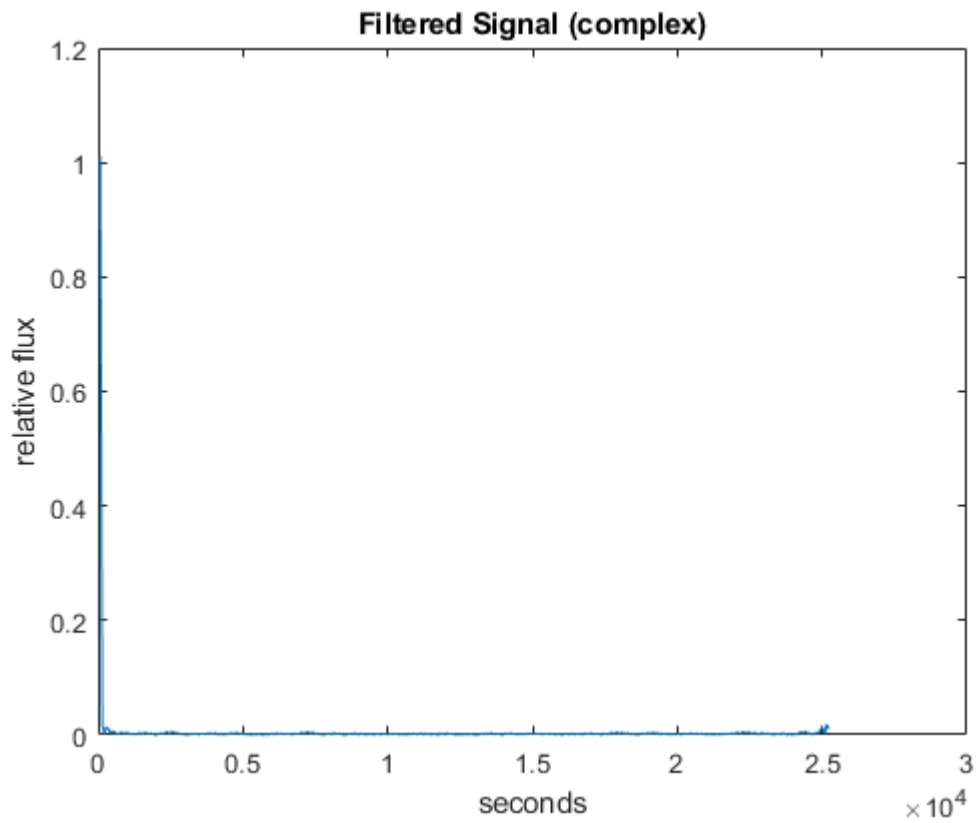
```
F0i = ifftshift(C0filter) * L-1;
finv = ifft(F0i);
figure, plot(t(2:L),real(finv))
title('Filtered Signal (real)')
xlabel('seconds')
ylabel('relative flux')
```



```
F0i = ifftshift(C0flter) * L-1;
finv = ifft(F0i);
figure, plot(t(2:L),imag(finv))
title('Filtered Signal (imaginary)')
xlabel('seconds')
ylabel('relative flux')
```

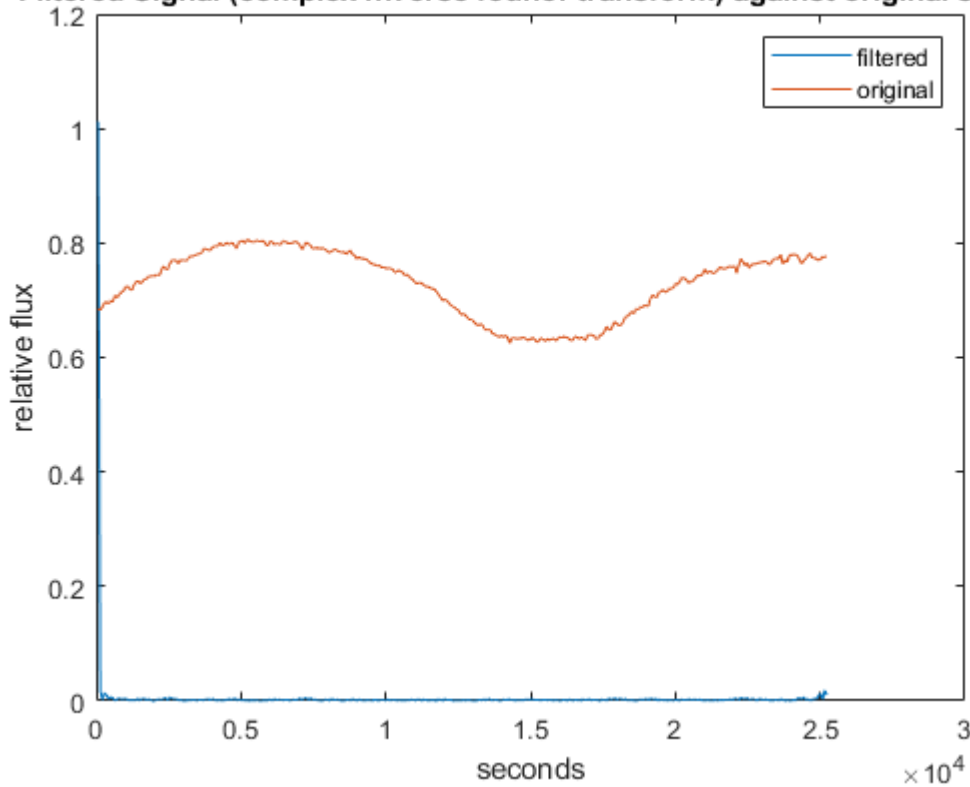


```
F0i = ifftshift(C0filter) * L-1;
finv = ifft(F0i);
figure, plot(t(2:L),abs(finv))
title('Filtered Signal (complex)')
xlabel('seconds')
ylabel('relative flux')
```

```
F0i = ifftshift(C0flter) * L-1;
finv = ifft(F0i);
figure, plot(t(2:L),abs(finv),t(2:L),X(2:L))
legend('filtered','original')
title('Filtered Signal (complex inverse fourier transform) against original signal')
xlabel('seconds')
ylabel('relative flux')
```

Filtered Signal (complex inverse fourier transform) against original signal

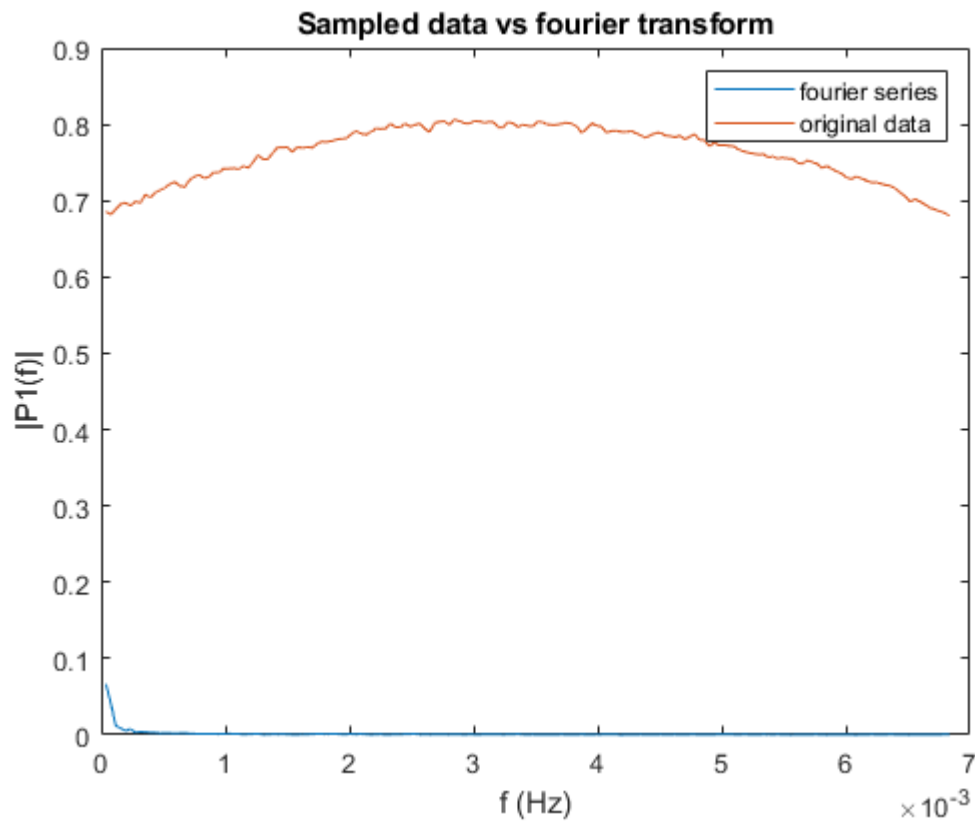


This approach failed for this star because the signal was read as noise.

```
F = 1./t(2:L);

%Fourier transformation
Y = fft(X);
P2complex = abs(Y/L); %real and imaginary parts together
P2real = 2*real(Y);
P2imaginary = 2*imag(Y);
P1complex = P2complex(1:floor(L/2)+1);
P1complex(2:end-1) = 2*P1complex(2:end-1);

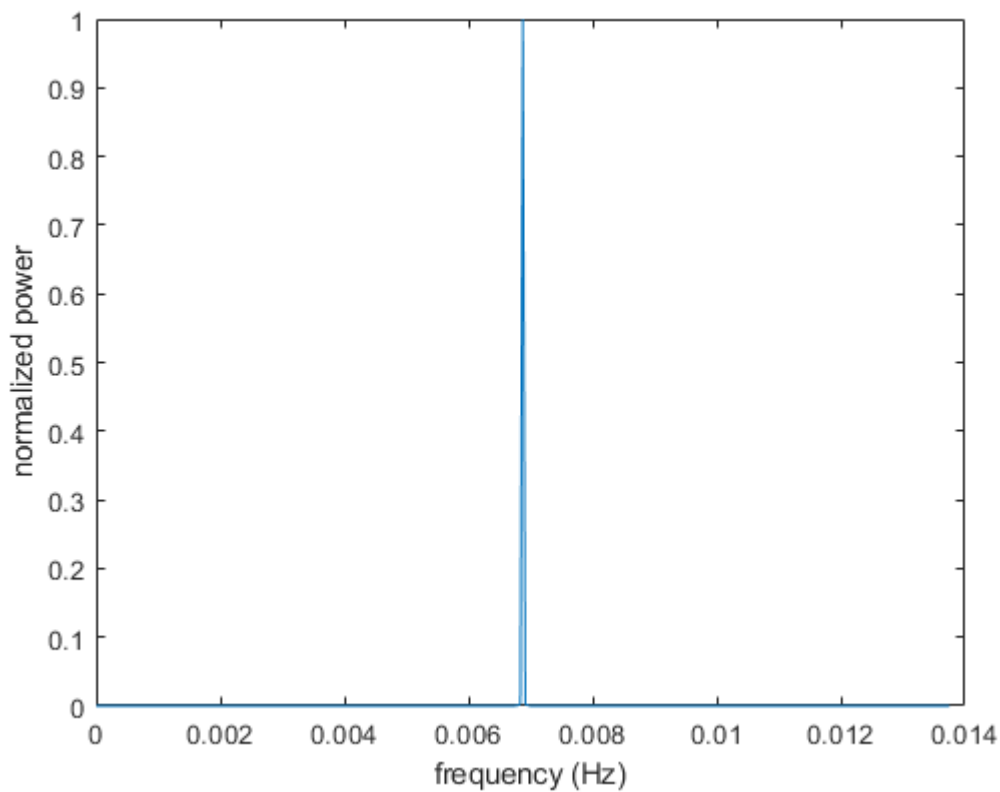
%Plot
f = Fs*(0:(L/2))/L;
plot(f(2:end-1),P1complex(2:end-1),f(2:end-1),X(2:floor(L/2)))
title('Sampled data vs fourier transform')
xlabel('f (Hz)')
ylabel('|P1(f)|')
legend('fourier series','original data')
```



Identify key frequencies

Use Linear Interpolation, then use a Fourier transform to attain the power spectrum

```
[Tnew,Mnew] = Interp_Lin(KICB.Time,KICB.Flux);
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt)
```



```
fk = 1×349
      0    0.000039515546795    0.000079031093589    0.000118546640384 ...
powerNor = 1×349
      0.000000160823491    0.000000219864278    0.000000231469475    0.000000063474372 ...
```

0.006876 Hz is the frequency of the peak.

```
0.006876*3600*24
```

```
ans =
    5.940864000000000e+02
```

Therefore 594.0864 per day

```
sampling_freq = 1/( mean( diff(Tnew) ) *86400 )
```

```
sampling_freq =
    0.013790925761080
```

```
sampling_freq/0.006876
```

```
ans =
    2.005661105450841
```

Linear Combination of non-linear functions

Guess 1: Linear functions with original data

```
F1 = @(x) x./x;
F2 = @(x) cos(2*pi*(594.0864)).*(x);
```

```
F3 = @(x) sin(2*pi*(594.0864)).*(x);
```

```
%call the NLfit function
```

```
c = NLfit(F1,F2,F3,KICB.Time,KICB.Flux)
```

Warning: Matrix is close to singular or badly scaled. Results may be inaccurate. RCOND = 5.138544e-22.

```
c = 3×1
```

```
104 ×
```

```
1.185510087304766
```

```
-0.000004915681730
```

```
-0.000031426510335
```

```
%plot
```

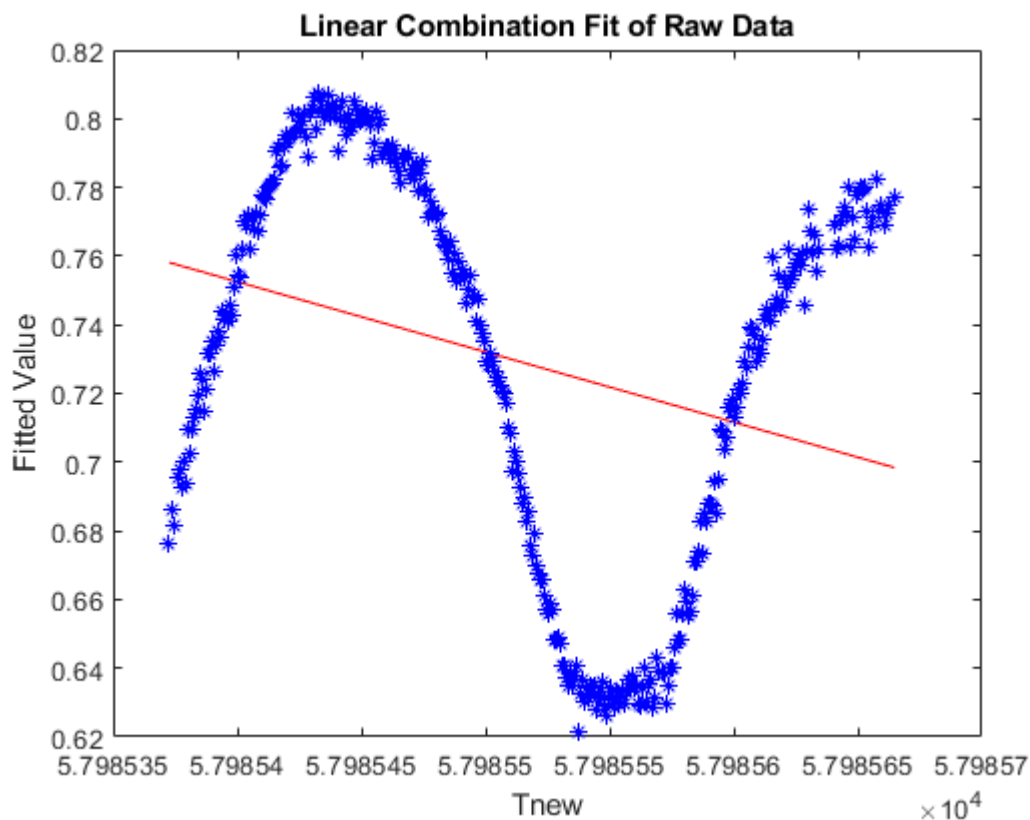
```
yfit = c(1).*F1(Tnew) + c(2).*F2(Tnew) + c(3).*F3(Tnew) ;
```

```
plot(Tnew,yfit,'r',KICB.Time,KICB.Flux,'*b')
```

```
title('Linear Combination Fit of Raw Data')
```

```
xlabel('Tnew')
```

```
ylabel('Fitted Value')
```



Poor guess. There is a clear periodicity so attempting periodic functions should help.

Guess 2: Periodic functions from Gilat with original data

```
F1 = @(x) x./x;
```

```
F2 = @(x) cos(2*pi*(594.0864).*(x));
```

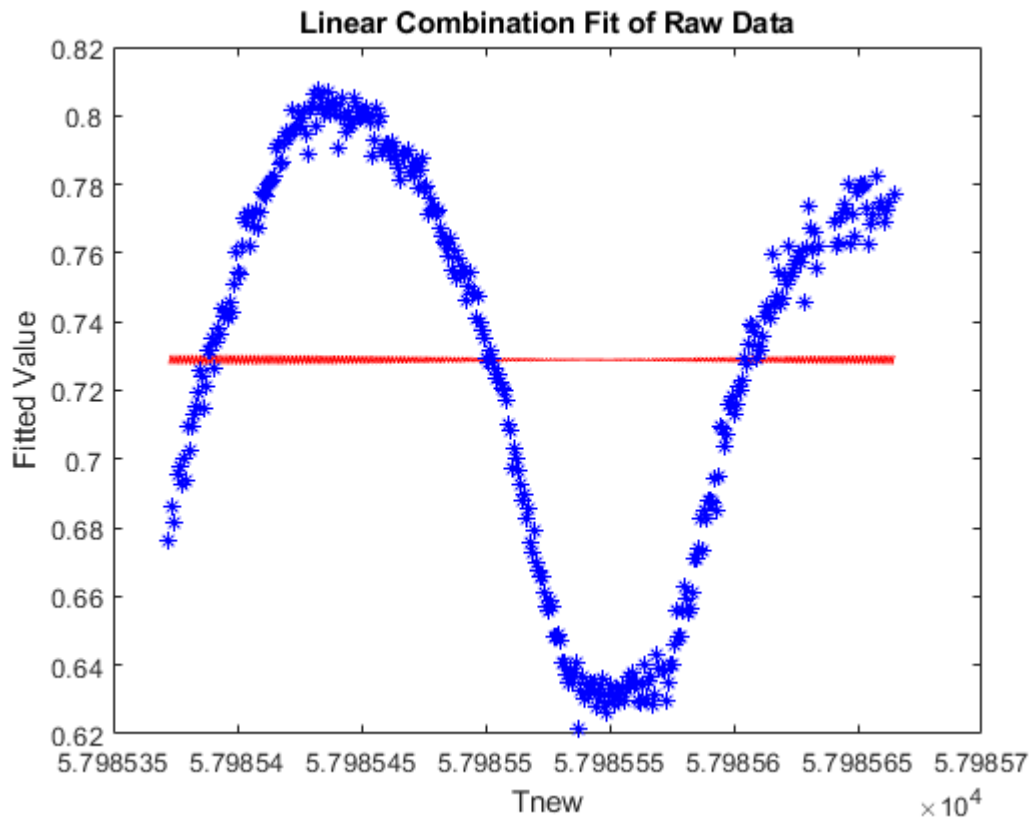
```
F3 = @(x) sin(2*pi*(594.0864).*(x));
```

```
%call the NLfit function
```

```
c = NLfit(F1,F2,F3,KICB.Time,KICB.Flux)
```

```
c = 3×1
    0.728950545958452
   -0.000343714572927
   -0.001342684040425
```

```
%plot
yfit = c(1).*F1(Tnew) + c(2).*F2(Tnew) + c(3).*F3(Tnew) ;
plot(Tnew,yfit,'r',KICB.Time,KICB.Flux,'*b')
title('Linear Combination Fit of Raw Data')
xlabel('Tnew')
ylabel('Fitted Value')
```



The period is too small so the factor $2\pi f$ is too large. A smaller guess is necessary.

Guess 3: Adjusted Gilat periodic functions in seconds and interpolated

```
F1 = @(x) x./x;
F2 = @(x) cos(0.006876/(6*pi).*x);
F3 = @(x) sin(0.006876/(6*pi)*(x));
```

```
%call the NLfit function
```

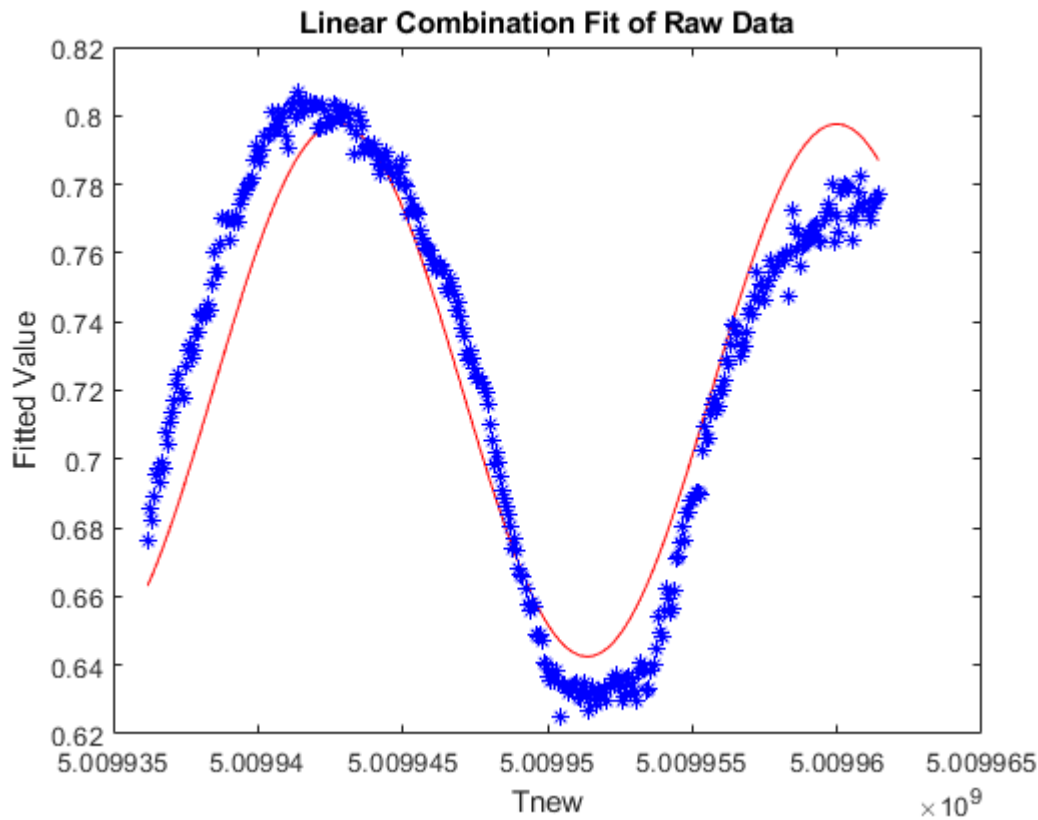
```
c = NLfit(F1,F2,F3,Tnews,Mnew)
```

```
c = 3×1
    0.720055170068848
   -0.071758258314959
```

0.029364893043408

```
%plot
```

```
yfit = c(1).*F1(Tnews) + c(2).*F2(Tnews) + c(3).*F3(Tnews) ;  
plot(Tnews,yfit,'r',Tnews,Mnew,'*b')  
title('Linear Combination Fit of Raw Data')  
xlabel('Tnew')  
ylabel('Fitted Value')
```



This is a good fit but the question is why these functions and what the factor means.

Guess 4: Another hypothesis similar to Guess 3

```
F1 = @(x) x./x;  
F2 = @(x) cos(0.006876/(2*pi^2).*x);  
F3 = @(x) sin(0.006876/(2*pi^2)*(x));
```

```
%call the NLfit function
```

```
c = NLfit(F1,F2,F3,Tnews,Mnew)
```

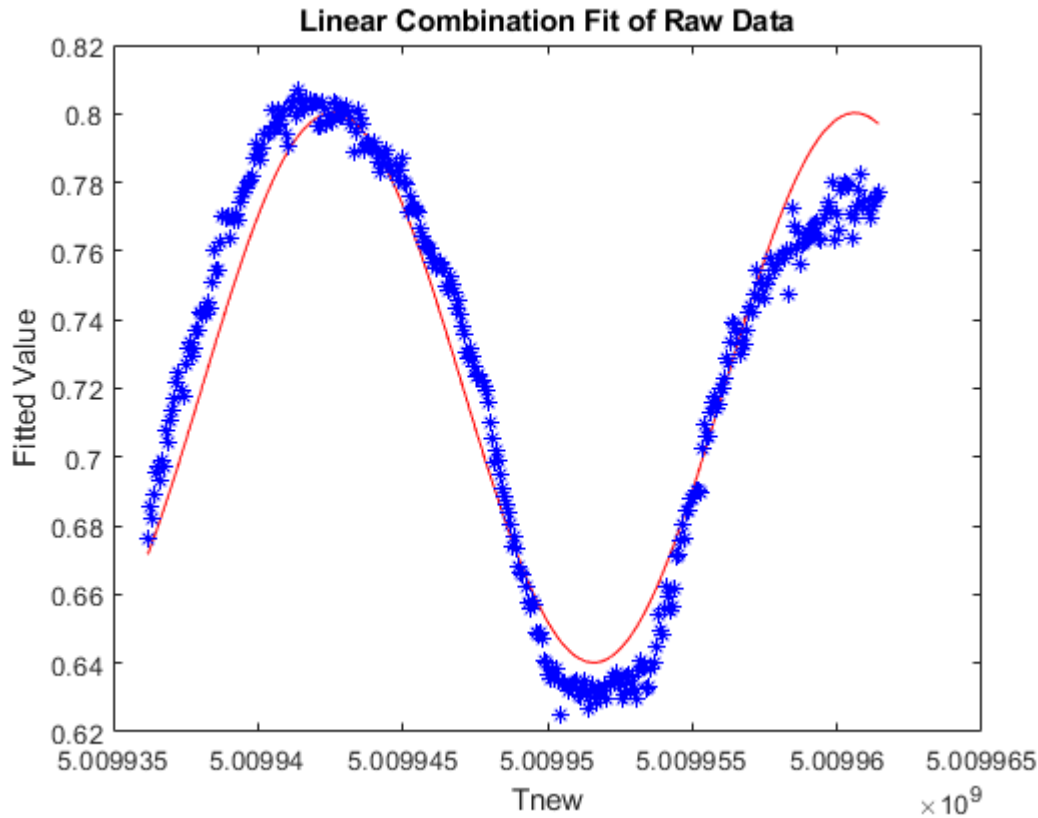
```
c = 3x1  
0.720202359323187  
0.043460932500827  
0.067217964506493
```

```
%plot
```

```

yfit = c(1).*F1(Tnews) + c(2).*F2(Tnews) + c(3).*F3(Tnews) ;
plot(Tnews,yfit,'r',Tnews,Mnew,'*b')
title('Linear Combination Fit of Raw Data')
xlabel('Tnew')
ylabel('Fitted Value')

```



This fit looks visually better than guess 3.

Chi-squared

```

%use guess 4
F1 = @(x) x./x;
F2 = @(x) cos(0.006876/(2*pi^2).*x);
F3 = @(x) sin(0.006876/(2*pi^2)*(x));
c = NLfit(F1,F2,F3,Tnews,Mnew)

```

```

c = 3x1
    0.720202359323187
    0.043460932500827
    0.067217964506493

```

```

yfit = @(c,x) c(1).*F1(x) + c(2).*F2(x) + c(3).*F3(x);
Options.ErrorsUnknown = 1;
[params,dParams,gof,stddev] = fitChiSquare(Tnews,Mnew,yfit,c,[],[],Options)

```

Fitting function parameters...

Local minimum possible.
lsqnonlin stopped because the size of the current step is less than

the value of the step size tolerance.

```
<stopping criteria details>
Finding parameter 1 lower bound
Finding parameter 1 upper bound
Finding parameter 2 lower bound
Finding parameter 2 upper bound
Finding parameter 3 lower bound
Finding parameter 3 upper bound
Parameter 1 = 0.720202 + 0.000727965 - 0.000828687
Parameter 2 = 0.0434609 + 0.00113562 - 0.00113562
Parameter 3 = 0.067218 + 0.00115737 - 0.00115737
Reduced chi-square = 1.000000
params = 3x1
    0.720202359323187
    0.043460932500827
    0.067217964506493
```

```
dParams = 1x3 struct
```

Fields	dl	lVal	du	uVal	d
1	8.286872192...	[0.71937...	7.279648038...	[0.72093...	7.783260115...
2	0.001135...	[0.72044...	0.001135...	[0.71995...	0.001135...
3	0.001157...	[0.72020...	0.001157...	[0.72019...	0.001157...

```
gof = struct with fields:
    chi2: 3.459999999999897e+02
    dof: 346
    eta2: 0.933310427281549
    probChi2: 0.510110660453937
```

```
stddev = 349x1
    0.014784046905323
    0.014784046905323
    0.014784046905323
    0.014784046905323
    0.014784046905323
    0.014784046905323
    0.014784046905323
    0.014784046905323
    0.014784046905323
    0.014784046905323
    :
```

```
%use guess 3
F1 = @(x) x./x;
F2 = @(x) cos(0.006876/(6*pi).*x);
F3 = @(x) sin(0.006876/(6*pi)*(x));
c = NLfit(F1,F2,F3,Tnews,Mnew)
```

```
c = 3x1
    0.720055170068848
   -0.071758258314959
    0.029364893043408
```

```
yfit = @(c,x) c(1).*F1(x) + c(2).*F2(x) + c(3).*F3(x);
Options.ErrorsUnknown = 1;
[params,dParams,gof,stddev] = fitChiSquare(Tnews,Mnew,yfit,c,[],[],Options)
```

Fitting function parameters...

Local minimum found.

Optimization completed because the size of the gradient is less than the value of the optimality tolerance.

```
<stopping criteria details>
Finding parameter 1 lower bound
Finding parameter 1 upper bound
Finding parameter 2 lower bound
Finding parameter 2 upper bound
Finding parameter 3 lower bound
Finding parameter 3 upper bound
Parameter 1 = 0.720055 + 0.00108043 - 0.00107076
Parameter 2 = -0.0717583 + 0.00146135 - 0.00146135
Parameter 3 = 0.0293649 + 0.00149639 - 0.00149639
Reduced chi-square = 1.000000
params = 3x1
    0.720055170068928
   -0.071758258313813
    0.029364893043243
dParams = 1x3 struct
```

Fields	dI	IVal	du	uVal	d
1	0.001070...	[0.71898...	0.001080...	[0.72113...	0.001075...
2	0.001461...	[0.71997...	0.001461...	[0.72013...	0.001461...
3	0.001496...	[0.72036...	0.001496...	[0.71974...	0.001496...

```
gof = struct with fields:
    chi2: 3.459999999999922e+02
    dof: 346
    eta2: 0.889033384590889
    probChi2: 0.510110660453900
stddev = 349x1
    0.019070432132037
    0.019070432132037
    0.019070432132037
    0.019070432132037
    0.019070432132037
    0.019070432132037
    0.019070432132037
    0.019070432132037
    0.019070432132037
    0.019070432132037
    :
```

eta is better for guess 4 and 0.933 is a very good fit. Else guess 3 and 4 are similar.

Important functions

```
function [Tnew,Mnew] = Interp_Lin(T,M)
%Interp_Lin user-defined linear interpolation function
%
% Usage:
% [Tnew,Mnew] = Interp_nearest(T,M)
%     Uses data and y=mx+b to interpolate.
%
% Author:      J. Evans
% Updated:     11/29/2021
```

```

%
% Inputs:
%     T   - A length m vector of independent variable data (time)
%     M   - A length m vector of dependent variable data (flux)
%
% Outputs:
%     Tnew   - A length m vector of independent variable data (time at
%     regular intervals)
%     Mnew   - A length m vector of dependent variable data (interpolated flux)
%
%
% Example:
% Enclosed in live script.
%
% Notes:
% N/A
%
% References:
% N/A
%


---


% --Sum all of the time differences between measurements--
n = numel(T);
sum = 0;
for l = 1:n-1
    sum = sum + abs(T(l+1) - T(l));
end

% --Find averaged time scale--
avg_dT = sum / (n-1);
Tnew = T(1):avg_dT:T(n);

% --Calculate Mnew values--
m = numel(Tnew);
Mnew = zeros(1,m);
Mnew(1) = M(1);
Mnew(m) = M(n);

for l = 2:m-1
    for k = 1:n
        if T(k) <= Tnew(l)
            if Tnew(l) <= T(k+1)
                Mnew(l) = (M(k+1) - M(k))./(T(k+1) - T(k)).*(Tnew(l)-T(k)) + M(k);
                %eq for a line. i.e. y = mx + b
            end
        end
    end
end
end
end

function [Tnew,Mnew] = Interp_nearest(T,M)
%Interp_nearest uses the built-in function 'interp1' with method 'nearest'
%
% Usage:

```

```

% [Tnew,Mnew] = Interp_nearest(T,M)
%     Uses data and built in functions to interpolate.
%
% Author:      J. Evans
% Updated:     11/29/2021
%
% Inputs:
%     T        - A length m vector of independent variable data (time)
%     M        - A length m vector of dependent variable data (flux)
%
% Outputs:
%     Tnew     - A length m vector of independent variable data (time at
%               regular intervals)
%     Mnew     - A length m vector of dependent variable data (interpolated flux)
%
% Example:
% Enclosed in live script.
%
% Notes:
% N/A
%
% References:
% N/A
%


---


% --Sum all of the time differences between measurements--
n = numel(T);
sum = 0;
for l = 1:n-1
    sum = sum + abs(T(l+1) - T(l));
end

% --Find averaged time scale--
avg_dT = sum / (n-1);
Tnew = T(1):avg_dT:T(n);

% --Calculate Mnew values--
Mnew = interp1(T,M,Tnew,'nearest');
end

```

```

function [Tnew,Mnew] = Interp_linear(T,M)
%Interp_linear uses the built-in function 'interp1' with method 'linear'
%
% Usage:
% [Tnew,Mnew] = Interp_linear(T,M)
%     Uses data and built in functions to interpolate.
%
% Author:      J. Evans
% Updated:     11/29/2021
%
% Inputs:

```

```

%      T   - A length m vector of independent variable data (time)
%      M   - A length m vector of dependent variable data (flux)
%
%  Outputs:
%      Tnew   - A length m vector of independent variable data (time at
%      regular intervals)
%      Mnew   - A length m vector of dependent variable data (interpolated flux)
%
%
%  Example:
%  Enclosed in live script.
%
%  Notes:
%  N/A
%
%  References:
%  N/A
%


---


% --Sum all of the time differences between measurements--
n = numel(T);
sum = 0;
for l = 1:n-1
    sum = sum + abs(T(l+1) - T(l));
end

% --Find averaged time scale--
avg_dT = sum / (n-1);
Tnew = T(1):avg_dT:T(n);

%--Calculate Mnew values--
Mnew = interp1(T,M,Tnew,'linear');
end

```

```

function [Tnew,Mnew] = Interp_spline(T,M)
%Interp_spline uses the built-in function 'interp1' with method 'spline'
%
%  Usage:
%  [Tnew,Mnew] = Interp_spline(T,M)
%      Uses data and built in functions to interpolate.
%
%  Author:      J. Evans
%  Updated:     11/29/2021
%
%  Inputs:
%      T   - A length m vector of independent variable data (time)
%      M   - A length m vector of dependent variable data (flux)
%
%  Outputs:
%      Tnew   - A length m vector of independent variable data (time at
%      regular intervals)
%      Mnew   - A length m vector of dependent variable data (interpolated flux)

```

```

%
%
% Example:
% Enclosed in live script.
%
% Notes:
% N/A
%
% References:
% N/A
%


---



% --Sum all of the time differences between measurements--
n = numel(T);
sum = 0;
for l = 1:n-1
    sum = sum + abs(T(l+1) - T(l));
end

% --Find averaged time scale--
avg_dT = sum / (n-1);
Tnew = T(1):avg_dT:T(n);

% --Calculate Mnew values--
Mnew = interp1(T,M,Tnew,'spline');
end

```

```

function [Tnew,Mnew] = Interp_polyfit(T,M)
%Interp_polyfit uses the built-in function 'interp1' with method 'polyfit'
%
% Usage:
% [Tnew,Mnew] = Interp_polyfit(T,M)
%     Uses data and built in functions to interpolate.
%
% Author:      J. Evans
% Updated:     11/29/2021
%
% Inputs:
%     T       - A length m vector of independent variable data (time)
%     M       - A length m vector of dependent variable data (flux)
%
% Outputs:
%     Tnew    - A length m vector of independent variable data (time at
%               regular intervals)
%     Mnew    - A length m vector of dependent variable data (interpolated flux)
%
% Example:
% Enclosed in live script.
%

```

```

% Notes:
% N/A
%
% References:
% N/A
%


---


% --Sum all of the time differences between measurements--
n = numel(T);
sum = 0;
for l = 1:n-1
    sum = sum + abs(T(l+1) - T(l));
end

% --Find averaged time scale--
avg_dT = sum / (n-1);
Tnew = T(1):avg_dT:T(n);

% --Calculate Mnew values--
n = numel(T);
p = polyfit(T,M,5);
Mnew = polyval(p,Tnew);
end

```

```

function [fk,powerNor] = EnergySpec(t,f,dt)
%EnergySpec Performs a fourier transform and plots a shifted power spectrum.
%
% Usage:
% [fk,powerNor] = EnergySpec(t,f,dt)
%     Uses data and built in functions to plot Power Spectrum.
%
% Author:      J. Evans
% Updated:     11/29/2021
%
% Inputs:
%     t        - A length m vector of independent variable data (time)
%     f        - A length m vector of dependent variable data (flux)
%     dt       - A scalar value of the difference between values of t
%
% Outputs:
%     fk       - resulting frequencies
%     powerNor - resulting normalised power spectrum
%
% Example:
% Enclosed in live script.
%
% Notes:
% N/A
%

```

```

% References:
% 1. this function is developed with refeernce to Gilat Program 7-4 and Example 7-6
%


---



N = length(f);
F = fft(f)/N;
F0 = fftshift(F);

power = F0.*conj(F0)/N;
powerNor = power/max(power);

%Plot power Spectrum
fs = 1/dt;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
end

```

```

function C = NLfit(F1,F2,F3,x,y)
%NLfit Performs a fit on a linear combination of nonlinear functions.
%
% Usage:
% C = NLfit(F1,F2,F3,x,y)
%     Uses matrix operations and given functions to model the x and y
%     data.
%
% Author:      J. Evans
% Updated:     11/29/2021
%
% Inputs:
%   F1 - A modeling function guess (anonymous function):
%   F2 - A modeling function guess (anonymous function):
%   F3 - A modeling function guess (anonymous function):
%   x  - A length m vector of independent variable data.
%   y  - A length m vector of dependent variable data.
%
% Outputs:
%   C  - a length 3 vector of fit model parameters
%
% Example:
% Enclosed in live script.
%
% Notes:
% N/A
%
% References:
% 1. Gilat example 6-9

```



```

%
F1 = F1(x);
F2 = F2(x);
F3 = F3(x);

A(1,1) = sum(F1 .* F1);
A(1,2) = sum(F1 .* F2);
A(1,3) = sum(F1 .* F3);
A(2,2) = sum(F2 .* F2);
A(2,3) = sum(F2 .* F3);
A(3,3) = sum(F3 .* F3);

A(2,1) = A(1,2);    % A is symmetric
A(3,1) = A(1,3);
A(3,2) = A(2,3);

B(1,1) = sum(y .* F1);
B(2,1) = sum(y .* F2);
B(3,1) = sum(y .* F3);

%form is A*C=B, Therefore,

C = A\B;

end

```

Chisquared function from mathworks site

```

function [params,dParams,gof,stddev]...
    = fitChiSquare(xData,yData,modelFun,guess,dxData,dyData,options)
%FITCHISQUARE Performs a chi-square fit returning parameter uncertainty.
%
% Usage:
%
% [params,dParams,gof,stddev] =
%     fitChiSquare(xData,yData,modelFun,guess,dxData,dyData)
%
%     Performs a least-squares fit of the parameters of modelFun,
%     minimizing the chi-square between the model and the data, using the
%     specified uncertainties in x and y data.
%
% ... = fitChiSquare(xData,yData,modelFun,guess,dxData,dyData,options)
%
%     As above, with the specified options.
%
% ... = fitChiSquare(xData,yData,modelFun,guess)
%
%     Uses empty data uncertainty arrays, sets ErrorsUnknown to true.
%
% Author:      N. Brahms
% Contact:     Contact via Matlab File Exchange website

```

```

% Version:      2.5
% Updated:      5/26/06
%
% Inputs:
%   xData      - A m x n matrix of independent variable data, where
%               columns represent independent variables, and rows
%               represent successive observations thereof.
%   yData      - A length m vector of dependent variable data.
%   dxData     - A m x n matrix of uncertainties corresponding to each
%               measurement in xData. May be [] if
%               Options.ErrorsUnknown = 1.
%   dyData     - A length m vector of uncertainties corresponding to each
%               measurement in yData. May be [] blank if
%               Options.ErrorsUnknown = 1.
%   modelFun- A pointer to a vectorized modeling function:
%
%               [result] = modelFun(params,xData)
%
%               which returns a length m vector of f(x) using the parameters
%               passed.
%
%   guess      - A length k vector of initial guesses for the parameters.
%   options     - An options struct to pass to the fitting routine;
%               this is the same as described in optimset, but with the
%               following additional fields. If any of the following
%               fields are absent from the struct, the default value is
%               used. This parameter is optional.
%
%   Display = 'iter' | {'on'} | 'off'
%               Passed to the fitting routine. If set to 'on' or 'iter',
%               also causes fitChiSquare to display the fitting results in
%               the command window.
%   Plot = {0} | 1
%               Plots the fit result. If PlotResiduals is also on, the fit
%               result is plotted in subplot [1 2] and the residuals are
%               plotted in subplot 3.
%   PlotVariable = {1} | ... | k
%               Which independent variable to plot against.
%   PlotResiduals = {0} | 1
%               Plots the weighted fit residuals
%   ErrorsUnknown = {0} | 1
%               Set this option to 1 if data uncertainties (dxData or dyData)
%               are unknown. fitChiSquare produces an error if
%               ErrorsUnknown is 0 and either dxData or dyData is empty.
%               If 0, then
%                   chi2 may be interpreted as a statistic indicating the
%                   likelihood that the model is appropriate for describing
%                   the observed data. See definitions of chi2 and
%                   probChi2 above. The delta chi2 = 1 bounds (dParams.dl
%                   and dParams.du) may be interpreted as 68% confidence
%                   intervals for the parameters (given that the parameters
%                   are gaussian-distributed). stddev is given by
%                       stddev = sqrt(dy^2 + sum( (df/dxi*dxi)^2 ) )
%                   where dy and dxi are the data uncertainties and df/dxi

```

```

%           is the finite-difference derivative of the model versus xi.
%
%       If 1, then
%           chi2 is set to 1, and neither chi2 nor probChi2 carry
%           meaning. The delta chi2 = 1 bounds may be interpreted
%           as "68% confidence intervals for the parameters given
%           the model is correct."
%
%       If 1, assumes the model is correct (that is, chi2 is set to 1)
%       and uses the model to calculate the data standard deviation.
%       Assumes standard deviation is uniform by datum.
%       If using ErrorsUnknown, the delta chi2 = 1 bounds for the
%       parameters can only be interpreted as the "68%
%       confidence interval given the model is correct" (and then
%       only if the parameters are gaussian-distributed).
%       If 0, uses measurement errors to calculate the data
%       standard deviation. Chi2 is a meaningful estimate of model
%       accuracy. The delta chi2 = 1 bounds may be interpreted as
%       the "68% confidence interval" (if the parameters are
%       gaussian-distributed).
%
%       FitUncertainty = 0 | {1} | k-vector
%       If 1 (default), fits uncertainties
%       If 0, does not fit uncertainties (returns empty dparams)
%       If length k boolean vector, fits uncertainties only to 'on'
%       indices. Example for a three parameter fit:
%           FitUncertainty = [0 1 1];
%
%       FitIndex = {ones(size(guess))} | k-vector
%       fitChiSquare only fits each parameter if the corresponding
%       index in FitIndex is true.
%
%       LowerBound      = vector | {[ -Inf ... -Inf]}
%       a length k row vector of parameter lower bounds
%
%       UpperBound      = vector | {[ Inf ... Inf]}
%       a length k row vector of parameter upper bounds
%
%       DisplayUncVal    = {0} | 1
%       shows additional information when fitting the uncertainties
%
%       MaxUncIter = {10}
%       maximum number of iterations in uncertainty solver
%
%       MaxUncCount = {20}
%       maximum number of function calls in uncertainty solver
%
%       UncOptions = optimset options |
%                   {optimset('TolFun',1e-2,'Display','off')}
%       optimset options to pass to uncertainty solver (fzero)
%
%       Scale = {0} | 1
%       If 1, uses parameter scaling to make optimization radix
%       equally sensitive to each parameter. This is useful if
%       parameters take on values different by more than an order
%       of magnitude (i.e. p = [1 1e10]). Note that the scaling
%       factor is determined from the guess, so zero guesses are
%       not scaled.
%
% Outputs:
%
%       params - a length k vector of fit model parameters
%       dParams - a length k cell array of structures with the following
%               fields:
%
%           d - equals (dl+du)/2

```

```
%
%      dl - absolute lower deviation at dChi^2=1 of the indexed
%           parameter
%      du - absolute upper deviation at dChi^2=1 of the indexed
%           parameter
%      lVal- a length k vector of the value of each parameter at the
%            dChi^2=1 projection point for the lower deviation of the
%            indexed parameter
%      uVal- a length k vector of the value of each parameter at the
%            dChi^2=1 projection point for the upper deviation of the
%            indexed parameter
%      gof - a goodness-of-fit struct with the following fields:
%      chi2- the chi-square of the fit
%      dof - degrees-of-freedom of the fit
%      eta2- the eta-square of the fit (a.k.a. correlation index) -
%            this quantity is analogous to the r-square (correlation
%            coefficient) of a linear least-squares fitting [3]
%      probChi2 - the probability of obtaining a chi-square equal to or
%                greater than chi2 given the data is drawn from the
%                model using the best-fit parameters
%      stddev - the expected deviation from the fit for each observation
%
```

% Example:

% Run and edit fitChiSquareExample for example use.

% Notes:

% fitChiSquare is a generalized chi-square fitting routine for any
 % model function when data measurement errors are known; it returns the
 % model parameters and their uncertainties at the delta chi-squared = 1
 % boundary (68% confidence interval). Alternatively, it can be used to
 % determine measurement errors when the theoretical function is known.

% This function uses the optimization toolbox function lsqnonlin to first
 % perform a nonlinear least squares fit of the data to the model. It
 % then calculates the standard deviation of each point to the fit value,
 % then calculates the chi squared. Finally, the function fzero is
 % used on each parameter to find the value at which delta chi-squared is
 % equal to 1 while minimizing chi^2 with respect to the other parameters.
 % In the case that the parameter uncertainties are normally distributed,
 % the delta chi^2 = 1 method gives the 68% confidence limit for the
 % parameters. Monte Carlo or investigations of many data sets should be
 % used to confirm the parameter uncertainties are normally distributed.
 % This method gives upper and lower bounds for each parameter.[1,2]

% If one encounters the following error message:

```
%      Unexpected termination flag 0 in non-estimating variable
%      minimization during uncertainty estimation
```

% this is because the non-varying parameter minimization routine has
 % encountered its iteration or evaluation limit. Raise
 % options.UncOptions.MaxFunEvals or options.UncOptions.MaxIter.

% Note: If the user can not use lsqnonlin (i.e., the optimization
 % toolbox is not installed), the program will use the built-in function

```

% fminsearch instead. This may reduce the robustness and/or speed of
% the calculation.
%
% References:
% 1. W.H. Press, B.P. Flannery, S.A. Teukolsky, W.T. Vetterling.
% Numerical Recipes; The Art of Scientific Computing. (Cambridge
% University Press: Cambridge). 1986.
% 2. P.R. Bevington, D.K. Robinson. Data Reduction and Error Analysis
% for the Physical Sciences. (McGraw-Hill: New York). 1992.
% 3. http://mathworld.wolfram.com
%-----
% (c) 2006 N. Brahms
%
% History
% 1.0 - Initial version
% 1.1 - Changed syntax and added the doError switch
% 1.1.1 - Added more detailed reporting
% 1.2 - Changed parameter uncertainty minimization function from
% fminbnd to fminsearch with coded constraints
% 1.3 - Changed non-estimating parameter minimization to occur
% inside fminsearch in uncertainty minimization. Also,
% fixed a bug causing improper weighting of initial chi2
% minimization. Removed doError switch.
% 1.3.1 - Minor code rearrangement
% 1.3.2 - Can run without the optimization toolbox
% 1.3.3 - Added UncMaxFunEvals & UncMaxIter options
% 1.3.4 - Fixed a bug whereby the uncertainty estimator would
% return bogus values instead of an error if the included
% non-varying parameter minimization routine halted
% unexpectedly.
% 2.0 - File name change to fitChiSquare. Added example use
% file and included between function in release. Added
% stddev output.
% 2.1 - Added bounds, uncertainty options. Updated
% documentation.
% 2.2 - Added ErrorsUnknown option, cleaned up documentation.
% 2.3 - Added plotting options, changed to allow FitUncertainty
% with ErrorsUnknown. Changed dParams to normal array.
% 2.4 - Added gof struct - note syntax change
% 2.4.1 - Fixed bug where struct was misassigned if
% FitUncertainty(1) was equal to 0
% 2.4.2 - Added probchi2 field to gof struct
% 2.4.3 - M-Lint optimization
% 2.4.4 - Changed options handling to make code cleaner, added
% ability to fit only a variable subspace
% 2.5 - Added Scale option
% 2.5.1 - Help updates, options is now optional :)
% 2.6 - Added 4 parameter syntax
%
% Known problems / suggested features
% - Add flags indicating that the fit has stopped at bounds
%-----
% Uncertainty loop constants and defaults

```

```

LARGE_NUM = realmax;    % The number used in the minimization routine when
                        % the minimizing variable is out of bounds
if ~exist('options','var')
    options = optimset;
end
options = initializeOptions(options,guess);
opEPar = initializeUncOptions(options);
if nargin==4
    options.ErrorsUnknown = true;
    dxData = [];
    dyData = [];
end
% Check degrees of freedom
if (length(yData) <= length(guess))
    error('Nonpositive degrees of freedom');
end
% Condition input
[xData, dxData, yData, dyData] = conditionInput(xData, dxData,...
    yData, dyData, ~options.ErrorsUnknown);
% Force bound vectors to be row vectors
options.LowerBound = conditionBound(options.LowerBound);
options.UpperBound = conditionBound(options.UpperBound);
% Scale input for unit radix
scale = ones(size(guess));
if options.Scale
    scale(guess~=0) = abs(guess(guess~=0));
    guess = guess./scale;
    if ~isempty(options.OutputFcn)
        unscaledOutputFcn = options.OutputFcn;
        options.OutputFcn = @(p,ov,s) feval(unscaledOutputFcn,p*scale,ov,s);
    end
end
% Check guess is in bounds
for ia=1:length(guess)
    if any(options.LowerBound>options.UpperBound)
        error('Lower bound exceeds upper bound')
    end
    if ~between(guess(ia)*scale(ia),[options.LowerBound(ia) options.UpperBound(ia)],1)
        error('Guess %d is not in bound',ia);
    end
end
% Nested function variable initialization
pVarIndex = 0;
pVar      = 0;
pFix      = 0;
pEVarVal  = zeros(length(guess)-1,1);
pEVarInd  = zeros(length(guess)-1,1);
pVarBnd   = [-Inf, Inf];
pVarMult  = 1;
if ~strcmp(options.Display,'off')
    disp('Fitting function parameters...');
end
% Calculate the degrees of freedom of the problem
dof = length(yData)-length(guess);

```

```

% Calculate the fit with uniform uncertainty
stddev = 1;
% Average deviation from the guess
stddev = sqrt(sum(model(guess).^2)/dof);
if ~options.ErrorsUnknown
    startOptions = options; startOptions.TolFun = 1e-2; startOptions.TolX = 1e-8;
    params = trylsq(@model,guess,[],[],startOptions);
    % Calculate the standard deviation for each datum
    stddev = calcStdDev;
    % Calculate the least-squares fit
    params = trylsq(@model,params,[],[],options);
else
    % Calculate the least-squares fit
    params = trylsq(@model,guess,[],[],options);
    stddev = 1;
    stddev = sqrt(sum(model(params).^2)/dof)*ones(length(yData),1);
end
% Calculate the chi-square function
chiSquare = sum( model(params).^2 );
% Fill goodness-of-fit struct
gof.chi2 = chiSquare;
gof.dof = dof;
gof.eta2 = (std( (yData-model(params)).*stddev ) / std( yData ) )^2;
gof.probChi2 = chi2prob(chiSquare,dof);
% Fits parameter uncertainties
% Be careful not to use ia in any nested functions!
dParams = initializedDParams;
dParams(1:length(params)) = dParams;
for ia=1:length(params)
    if options.FitUncertainty(ia)
        dParams(ia)=delta(ia);
    end
end
% Rescale data back from unity
params = params.*scale;
for ia=1:length(dParams)
    dParams(ia).du = dParams(ia).du*scale(ia);
    dParams(ia).dl = dParams(ia).dl*scale(ia);
    dParams(ia).d = dParams(ia).d*scale(ia);
    dParams(ia).lVal = dParams(ia).lVal*scale(ia);
    dParams(ia).uVal = dParams(ia).uVal*scale(ia);
end
% If a verbose mode is on, display the answer and reduced chi-squared
if ~strcmp(options.Display,'off')
    for id=1:length(params)
        disp(sprintf('Parameter %d = %g + %g - %g',...
            id,params(id),dParams(id).du,dParams(id).dl));
    end
    disp(sprintf('Reduced chi-square = %f',chiSquare/dof));
end
% Plot the fit
if options.Plot
    % Subplot if also plotting residuals
    if options.PlotResiduals

```

```

        subplot(3,1,[1 2]);
    end
    holdstate = ishold;
    errorbar(xData(:,options.PlotVariable),yData,stddev,'. ');
    plotHandle = gca;
    hold on
    plot(xData(:,options.PlotVariable),...
        yData - model(params./scale).*stddev,'-r');
    switch holdstate
        case 0
            hold off
    end
    xlabel('x1');
    ylabel('y');
    title('Fit plot');
    lstring = sprintf('Fit: ~\chi^2 = %0.2g\n',chiSquare/dof);
    for ia = 1:length(params);
        lstring = [lstring ...
            sprintf('Par. %d = %0.2g + %0.1g - %0.1g\n',...
                ia,params(ia),dParams(ia).du,dParams(ia).dl)];
    end
    legend({sprintf('Data \pm \sigma'),lstring(1:end-1)});

end
% Plots the weighted fit residual
if options.PlotResiduals
    if options.Plot
        subplot(3,1,3);
    end
    holdstate = ishold;
    plot(xData(:,options.PlotVariable),model(params./scale),' ');
    hold on
    line([min(xData(:,options.PlotVariable)) max(xData(:,options.PlotVariable))],...
        [0 0], 'Color',[1 0 0]);
    switch holdstate
        case 0
            hold off
    end
    xlabel('x1');
    ylabel('Residual');
    title('Weighted residual plot');
    if options.Plot
        set(gca,'XLim',get(plotHandle,'XLim'));
    end
end
if options.Plot || options.PlotResiduals
    drawnow
end
% Last executing line of fitChiSquare
% --- Internal functions follow -----
% ----- model -----
% This calls the model function. It returns the residual at each
% datum.
function F = model(x)

```



```

% If we scaled to unit radix, we must scale back before calling the
% model. Since scale was initialized to ones, we just multiply in
% any case.
x = x.*scale;

% Handle boundary
testInBound = between(x,[options.LowerBound; options.UpperBound],1);

if ~all(testInBound)
    % Return ridiculously large number
    F = sqrt(LARGE_NUM)/(length(x)+1)*ones(length(xData),1);
else
    % Return the chi-value
    F = (yData - feval(modelFun,x,xData))./(stddev+eps);
    %eps to avoid problems with zero weights
end
end
% ----- modelError -----
% Used in finding the point-by-point standard deviation
function F = modelError(x,xbndData)
    % See model
    x = x.*scale;

    F = feval(modelFun,x,xbndData);
end
% ----- calcStdDev -----
% Calculates the std. dev. of (f(x_i)-y_i) using finite methods
function sigma = calcStdDev
    dim = size(xData);
    dm2 = zeros(dim(1),1);
    for ib=1:dim(2)
        xtestu = xData;
        xtestl = xData;
        xtestu(:,ib) = xtestu(:,ib)+dxData(:,ib);
        xtestl(:,ib) = xtestl(:,ib)-dxData(:,ib);
        dmodelu = modelError(params,xtestu);
        dmodell = modelError(params,xtestl);
        dm2 = dm2 + (dmodelu-dmodell).^2/4;
    end
    sigma = sqrt(dyData.^2+dm2);
end
%----- fzeroOutput -----
% Used with fzero to stop when UncIter is exceeded
function stop = fzeroOutput(x,o)

    if o.iteration > options.MaxUncIter || o.funccount > options.MaxUncCount
        stop = 1;
    else
        stop = 0;
    end

    % Display iterative function information
    if options.DisplayUncVal

```

```

        str1 = sprintf('Iteration = %d\tVarA = %6.4g\tVarB = %6.4g\tFValA = %6.4g\tFValB = %6.4g\t',
            o.iteration,o.intervala,o.intervalb,o.fvala,o.fvalb);
        str2 = sprintf('%g\t',pEVarVal);
        disp([str1 str2]);
    end

end

%----- modelFix -----
% This function is used to fit only one variable to delta chi2 = 1. It
% is used with fzero, not lsqnonlin.
function F = modelFix(var)

    if between(var,pVarBnd,1)

        pVar = var;
        if length(params)>1
            [pEVarVal,eflag] = trylsq(@modelNFix,pEVarVal,[],[],opEPar);
            if(eflag<=0)
                disp(sprintf(['\tUnexpected termination flag %d in'...
                    ' non-estimating variable minimization\n\tduring'...
                    ' uncertainty estimation'],eflag));
                F=NaN;
            else
                x = reconstruct(pVar);
                F = (chiSquare+1) - sum( model(x).^2 );
            end
        else
            F = (chiSquare+1) - sum( model(var).^2 );
        end

        % If past the variable-side bound, make F large. If past the
        % extent-side bound, make F infinitely negative.
        elseif var<min(pVarBnd)
            F = pVarMult*LARGE_NUM;
            eflag = 1;
        elseif var>max(pVarBnd)
            F = -pVarMult*LARGE_NUM;
            eflag = 1;
        end
    end
end % modelFix

% ----- reconstruct -----
% Builds the parameter array from pEVar and pVar
function x = reconstruct(in)
    x = zeros(size(params));
    for ic=1:length(pEVarInd)
        x(pEVarInd(ic)) = pEVarVal(ic);
    end
    x(pVarIndex) = in;
end

% ----- modelNFix -----
% This function is used to fit all but one variable
function F = modelNFix(x)
    xu = zeros(size(params));
    for ig=1:length(pEVarInd)

```

```

        xu(pEVarInd(ig)) = x(ig);
    end
    xu(pVarIndex) = pVar;
    F = model(xu);
end
% ----- delta -----
% This function finds the variation to delta chi-squared = 1
% One variable minimizes chi-square+1, while the other variables minimize
% chi-squared
function bnd = delta(varyingIndex)

    bnd = initializedDParams;

    % These are the shared variables for the fitting functions
    pVarIndex = varyingIndex; % The index of the variable being solved

    j=1; % Load all the other variables in an array
    for ie=1:length(params)
        if ie~=varyingIndex
            pEVarVal(j)=params(ie);
            pEVarInd(j)=ie;
            j=j+1;
        end
    end
    pEVarValStatic = pEVarVal; % The non-varying initial array value

    pVar = params(pVarIndex); % The solution is stored here, but must
                                % start at the minimized value

    % This is the original variable value
    pFix = params(pVarIndex);

    if ~strcmp(options.Display,'off')
        disp(sprintf('Finding parameter %d lower bound',varyingIndex));
    end
    % Calculate the lower bound
    [bnd.dl,bnd.lVal] = uncMin('lb');
    bnd.dl = pFix-bnd.dl;

    % Here we have to reinitiate the variables
    pEVarVal = pEVarValStatic;
    pVar = params(pVarIndex);

    % Calculate the upper bound
    if ~strcmp(options.Display,'off')
        disp(sprintf('Finding parameter %d upper bound',varyingIndex));
    end

    [bnd.du,bnd.uVal] = uncMin('ub');
    bnd.du = bnd.du-pFix;

    bnd.d = mean([bnd.du bnd.dl]);

    % This function finds the parameter deviation for delta chi-squared

```

```

% = 1, and then re-minimizes the other variables.
function [bnd,val] = uncMin(lbub)

    % Set the search bounds on the uncertainty
    switch(lbub)
        case 'ub'
            pVarBnd = [pFix, options.UpperBound(varyingIndex)]; A=1;
        case 'lb'
            pVarBnd = [options.LowerBound(varyingIndex), pFix]; A=-1;
    end
    pVarMult = A;

    opParDev = initializeUncOptions(options);
    opParDev.OutputFcn = @(x,o,s) fzeroOutput(x,o);
    % Find the parameter deviation to get delta chi2 = 1
    [bnd,fval,exitflag] = fzero(@modelFix,pFix,opParDev);
    bnd = fzero(@modelFix,pFix,opParDev);

    % Assign the result
    val = reconstruct(bnd);

    if options.DisplayUncVal
        disp(sprintf('Fix = %g\tVar = %g\tChi2 = %g',...
            pFix,pVar,chiSquare));
    end
end % uncMin
end % delta
end % fitChiSquare
% ----- initializeUncOptions -----
function uncOp = initializeUncOptions(options)
% Set a relatively high finishing tolerance
uncOp = options.UncOptions;
end %initializeUncOptions

% ----- initializeOptions -----
function options = initializeOptions(optionsIn,guess)
% Manufacture the fit options defaults
options = optimset;
options.Plot = false;
options.PlotResiduals = false;
options.PlotVariable = true;
options.FitUncertainty = true(1,length(guess));
options.FitIndex = true(1,length(guess));
options.ErrorsUnknown = false(1,length(guess));
options.UncOptions=optimset('TolFun',1e-2,'Display','off');
options.DisplayUncVal=false;
options.LowerBound=-Inf*ones(1,length(guess));
options.UpperBound=Inf*ones(1,length(guess));
options.Scale = false;
options.MaxUncIter = 10;
options.MaxUncCount = 20;
names = fieldnames(options);
for i = 1:length(names)
    if isfield(optionsIn,names{i})

```

```

        if length(optionsIn.(names{i})) == 1 &&...
            length(options.(names{i})) == length(guess) &&...
            length(guess)>1
            optionsIn.(names{i}) = optionsIn.(names{i})*ones(1,length(guess));
        end
        if islogical(options.(names{i}))
            options.(names{i}) = convertBoolean(optionsIn.(names{i}));
        else
            options.(names{i}) = optionsIn.(names{i});
        end %if islogical
    end %if isfield
end %for
end

% ----- chi2fun -----
% Returns the probability of chi-square equal to or greater than x, with r
% degrees of freedom. This is 1-D(x,r), where D is the cumulative
% distribution function. See
% http://mathworld.wolfram.com/Chi-SquaredDistribution.html
% Note that MATLAB's gammainc is the "regularized gamma function" used in
% MathWorld.
function p = chi2prob(x,r)
p = gammainc(r/2,x/2);
end
% ----- trylsq -----
% Uses lsqnonlin if it exists
function [sol,exitflag] = trylsq(fun,x0,lb,ub,options)
    if(exist('lsqnonlin','file'))
        [sol,trash,trash,exitflag] = lsqnonlin(fun,x0,lb,ub,options);
    else
        [sol,trash,exitflag] = fminsearch(@modelChi2,x0,options);
    end
    % For use when substituting fminsearch for lsqnonlin
    function F = modelChi2(x)
        F = sum(feval(fun,x).^2);
    end
end

% ----- between -----
% Returns the portion of vector in and out of the range ( as determined by
% the inclusive tag )
function [inner,outer] = between(vector,range,inclusive)
    if ~exist('inclusive','var')
        inclusive = 0;
    end
    if inclusive
        inner = vector<=max(range) & vector>=min(range);
        outer = vector<=min(range) & vector>=max(range);
    else
        inner = vector<max(range) & vector>min(range);
        outer = vector<min(range) & vector>max(range);
    end
end

end
% ----- conditionInput -----

```

```

function [xData, dxData, yData, dyData] = conditionInput(xin, dxin, yin, dyin,...
    doError)
xData = xin; dxData = dxin; yData = yin; dyData = dyin;
% Force yData and dyData to be column vectors
siy = size(yData);
if siy(1)>1 && siy(2)>1
    error('Y is not a vector');
end
yData = yData(:);
siy = size(yData);
if doError
    sidy = size(dyData);
    if sidy(1)>1 && sidy(2)>1
        error('dY is not a vector');
    end
    dyData = dyData(:);
    sidy = size(yData);
end
% Transpose xData if it is n x m, not m x n
six = size(xData);
if (siy(1) == six(2) && siy(1) ~= six(1))
    xData = xData';
    six = size(xData);
end
if doError
    sidx = size(dxData);
    if (siy(1) == sidx(2) && siy(1) ~= sidx(1))
        dxData = dxData';
        sidx = size(dxData);
    end
end
% Check that vectors match
if (siy(1) ~= six(1))
    error('X and Y data vectors do not match.')
end
if doError
    % Grow error vectors if the user passed scalar errors
    if sidx(1) == 1 && sidx(2) == six(2)
        for i=1:six(2)
            dxData(2:length(xData(:,1)),i)=dxData(1,i);
        end
        sidx = size(dxData);
    end
    if sidy(1) == 1 && sidy(2) == 1
        dyData(2:length(yData(:,1)),1)=dyData(1);
        sidy = size(dyData);
    end
    if any((sidx ~= six) | (sidy ~= siy))
        error('Data vectors do not match error vectors');
    end
end
end
end
% ----- initializeDParams -----
function dParamsEmpty = initializeDParams()

```

```

dParamsEmpty = struct('dl', NaN, 'lVal', [], 'du', NaN, 'uVal', [],...
    'd',NaN);
end
% ----- conditionBound -----
function boundVecOut = conditionBound(boundVecIn)
sib = size(boundVecIn);
if (sib(1)~=1 && sib(2)==1)
    boundVecOut = boundVecIn';
elseif (sib(1)~=1)
    error('Badly formed bound vector');
else
    boundVecOut = boundVecIn;
end
end
% ----- convertBoolean -----
% Converts vectors of {>0, <=0} or {'on', 'off'} to
% vectors of {1, 0}
function value = convertBoolean(in)
warning off MATLAB:sprintf:InputForPercentSIsNotOfClassChar;
errstr = ['Input vector' sprintf(' %s',in)...
    ' can not be converted to a boolean value'];
warning on MATLAB:sprintf:InputForPercentSIsNotOfClassChar;
% Handles cell arrays
if iscell(in)
    % All cells are numbers
    if all(isnumeric(cell2mat(in)))
        value = cell2mat(in) > 0;
    elseif islogical(cell2mat(in))
        value = cell2mat(in);
    % All cells are 'on' or not 'on'
    elseif iscellstr('in');
        in = lower(in);
        for i=1:length(in)
            switch in{i}
                case 'on'
                    value(i)=true;
                case 'off'
                    value(i)=false;
                otherwise
                    error(errstr);
            end %switch
        end %for
    else
        error(errstr);
    end %if number or string
% Array of numbers or booleans, or single string
else
    if all(isnumeric(in))
        value = in > 0;
    elseif all(islogical(in))
        value = in;
    elseif isa(in,'char') && all(isstrprop(in,'alpha'));
        switch lower(in)
            case 'on'

```

```
        value=true;
    case 'off'
        value=false;
    case 'true'
        value=true;
    case 'false'
        value=false;
    otherwise
        error(errstr);
    end %switch
else
    error(errstr);
end %if number or string
end %if cell
end %convertBoolean
```



```
clearvars
format long
```

Research Techniques Project

Milestone 1 (6 October)

Data Exploration of BD+55_441

For this milestone, BD+55_441 is displayed and explored in detail. The other sources are briefly imported in upcoming sections.

```
opts = detectImportOptions("BD+55_441.txt");
opts.DataLines = 3;
opts.VariableNames = {'B_time', 'B_flux', 'R_time', 'R_flux', 'V_time', 'V_flux'};
```

"time" is in the units of days and "flux" is "rel_flux_T1" from AstrolmageJ outputs.

```
opts.VariableTypes = {'double', 'double', 'double', 'double', 'double', 'double'};
preview("BD+55_441.txt",opts)
```

ans = 8x6 table

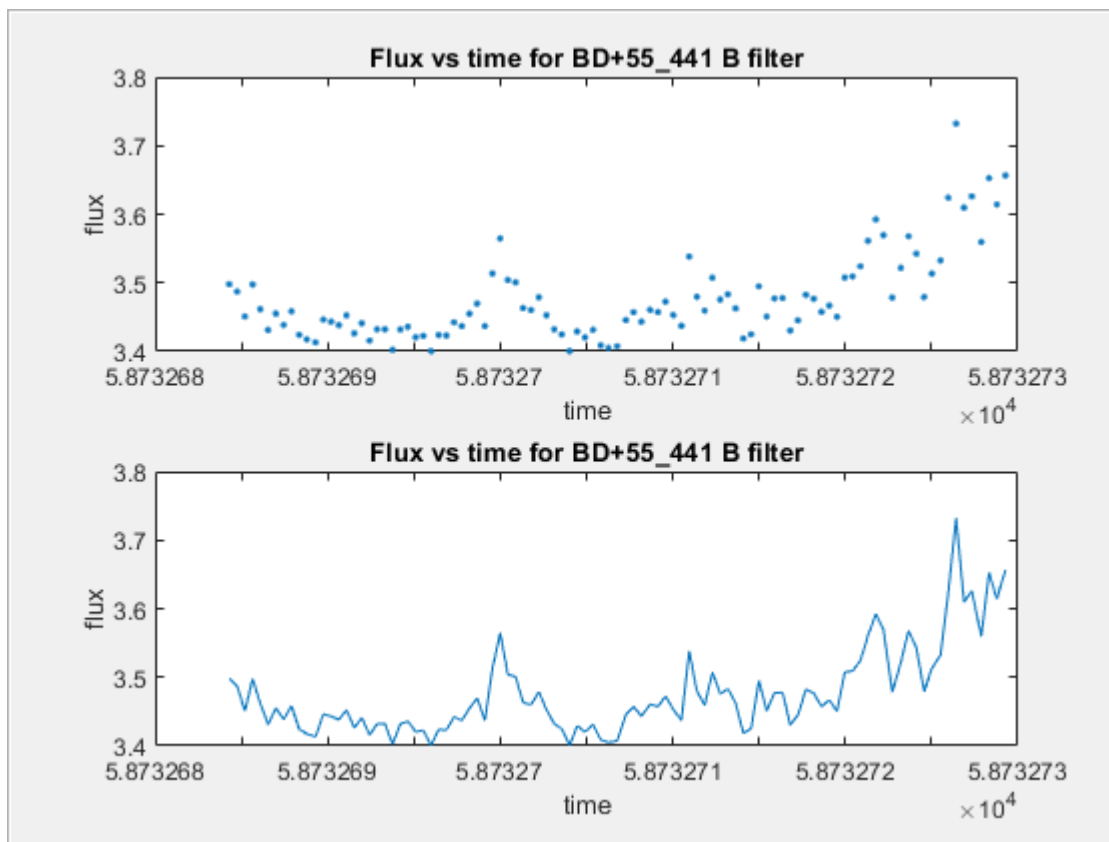
	B_time	B_flux	R_time	R_flux	V_time	V_flux
1	5.873268430...	3.497996...	5.873268459...	1.961830...	5.873268445...	2.352058...
2	5.873268430...	3.497996...	5.873268504...	1.942857...	5.873268490...	2.360458...
3	5.873268475...	3.487289...	5.873268549...	1.947021...	5.873268535...	2.329957...
4	5.873268520...	3.450942...	5.873268594...	1.930594...	5.873268580...	2.344889...
5	5.873268565...	3.497567...	5.873268639...	1.942537...	5.873268625...	2.361048...
6	5.873268610...	3.461555...	5.873268684...	1.935141...	5.873268669...	2.333341...
7	5.873268655...	3.431248...	5.873268729...	1.931290...	5.873268714...	2.331904...
8	5.873268700...	3.455091...	5.873268774...	1.928260...	5.873268759...	2.323782...

```
BD55_441 = readmatrix("BD+55_441.txt",opts);
whos BD55_441
```

Name	Size	Bytes	Class	Attributes
BD55_441	101x6	4848	double	

```
hf_sub(1) = figure(1);
hp(1) = uipanel('Parent',hf_sub(1),'Position',[0 0 1 1]);
subplot(2,1,1,'Parent',hp(1));
plot(BD55_441(:,1),BD55_441(:,2),'.')
title('Flux vs time for BD+55_441 B filter');
xlabel('time'),ylabel('flux');
subplot(2,1,2,'Parent',hp(1));
plot(BD55_441(:,1),BD55_441(:,2)),title('Flux vs time for BD+55_441 B filter')
xlabel('time');
```

```
ylabel('flux');
```



Noting the graph above - displayed in discrete points and as a line graph - there is some periodicity. There are peaks at 58732.70, 58732.711 and 58732.722.

```
r = abs([0; BD55_441(:,1)] - [BD55_441(:,1);0]);
round(mean(r(3:end-1)),8) %average period between measurements
```

```
ans =
    4.543400000000000e-04
```

```
round(std(r(3:end-1)),8) %standard deviation - as a measurement of variation in period
```

```
ans =
    1.885000000000000e-05
```

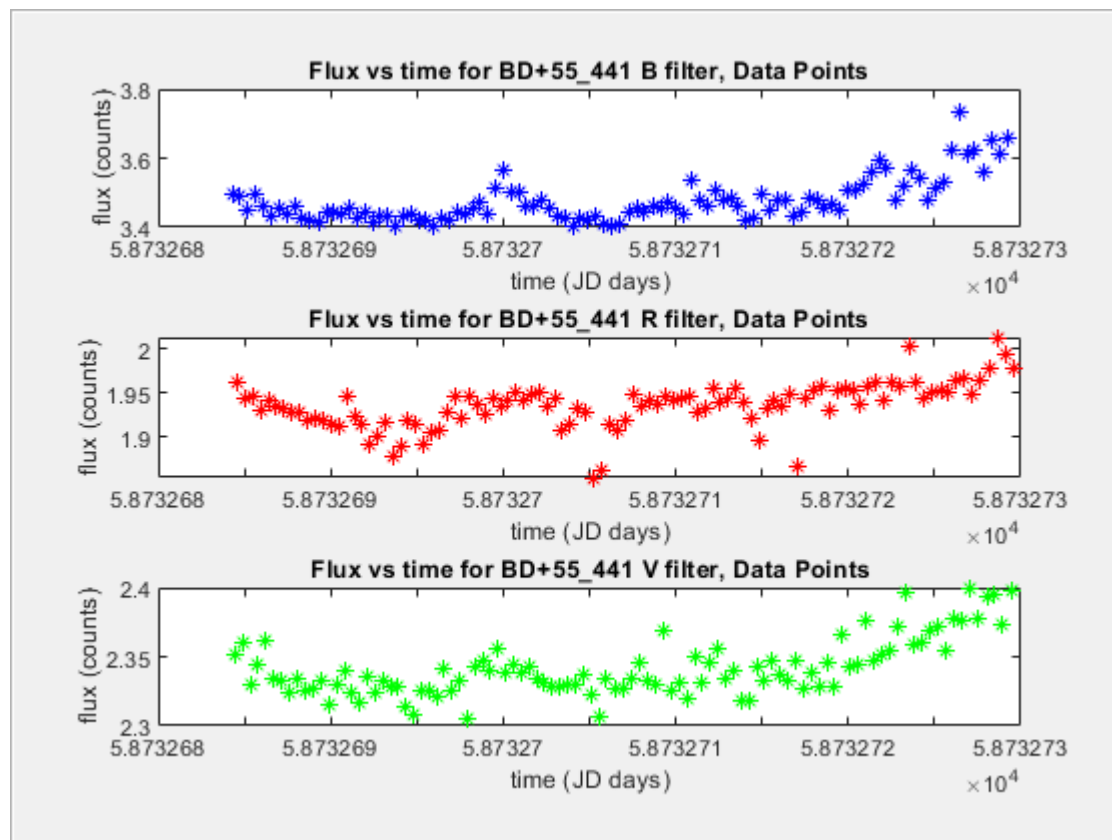
Periodicity between filters

```
hf_sub(2) = figure(2);
hp(2) = uipanel('Parent',hf_sub(2),'Position',[0 0 1 1]);
subplot(3,1,1,'Parent',hp(2));
% plotting in blue because B filter is blue light (~400-500 nm)
plot(BD55_441(:,1),BD55_441(:,2),'*b')
title('Flux vs time for BD+55_441 B filter, Data Points');
xlabel('time (JD days)');
ylabel('flux (counts)');
```

```

subplot(3,1,2,'Parent',hp(2));
% plotting in red because R filter is red light (~550-800 nm)
plot(BD55_441(:,3),BD55_441(:,4),'*r');
title('Flux vs time for BD+55_441 R filter, Data Points');
xlabel('time (JD days)');
ylabel('flux (counts)');
subplot(3,1,3,'Parent',hp(2));
% plotting green but V filter is visible light (~500-700 nm)
plot(BD55_441(:,5),BD55_441(:,6),'*g');
title('Flux vs time for BD+55_441 V filter, Data Points');
xlabel('time (JD days)');
ylabel('flux (counts)');

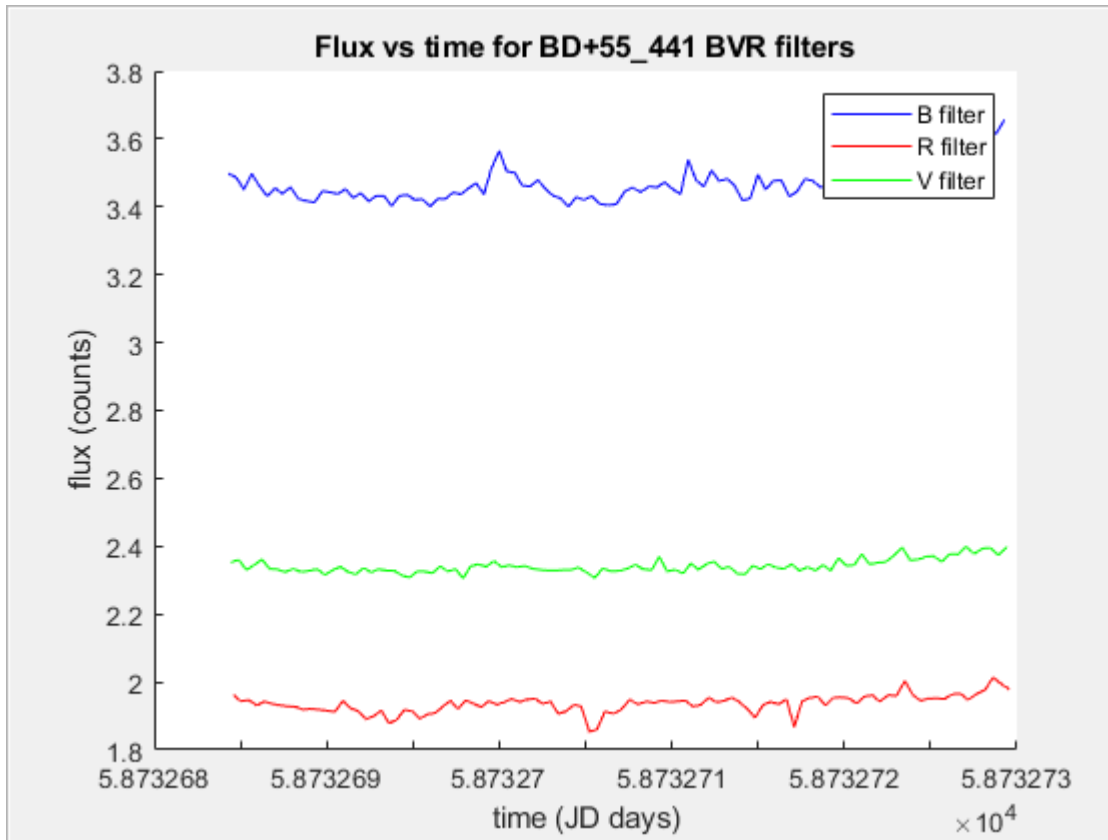
```



```

hf_sub(3) = figure(3);
hp(3) = uipanel('Parent',hf_sub(3),'Position',[0 0 1 1]);
subplot(1,1,1,'Parent',hp(3))
hold on
plot(BD55_441(:,1),BD55_441(:,2), 'b')
plot(BD55_441(:,3),BD55_441(:,4), 'r')
plot(BD55_441(:,5),BD55_441(:,6), 'g')
hold off
title('Flux vs time for BD+55_441 BVR filters');
xlabel('time (JD days)');
legend('B filter', 'R filter', 'V filter');
ylabel('flux (counts)');

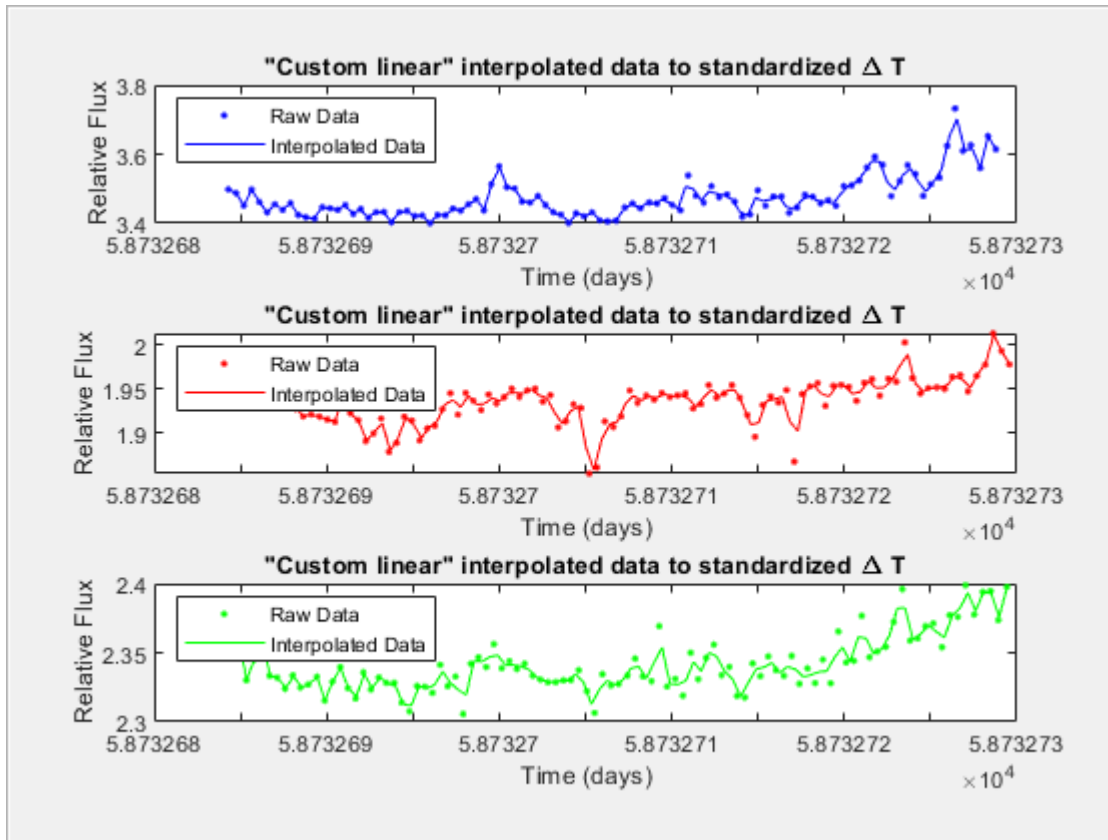
```



Interpolation investigation

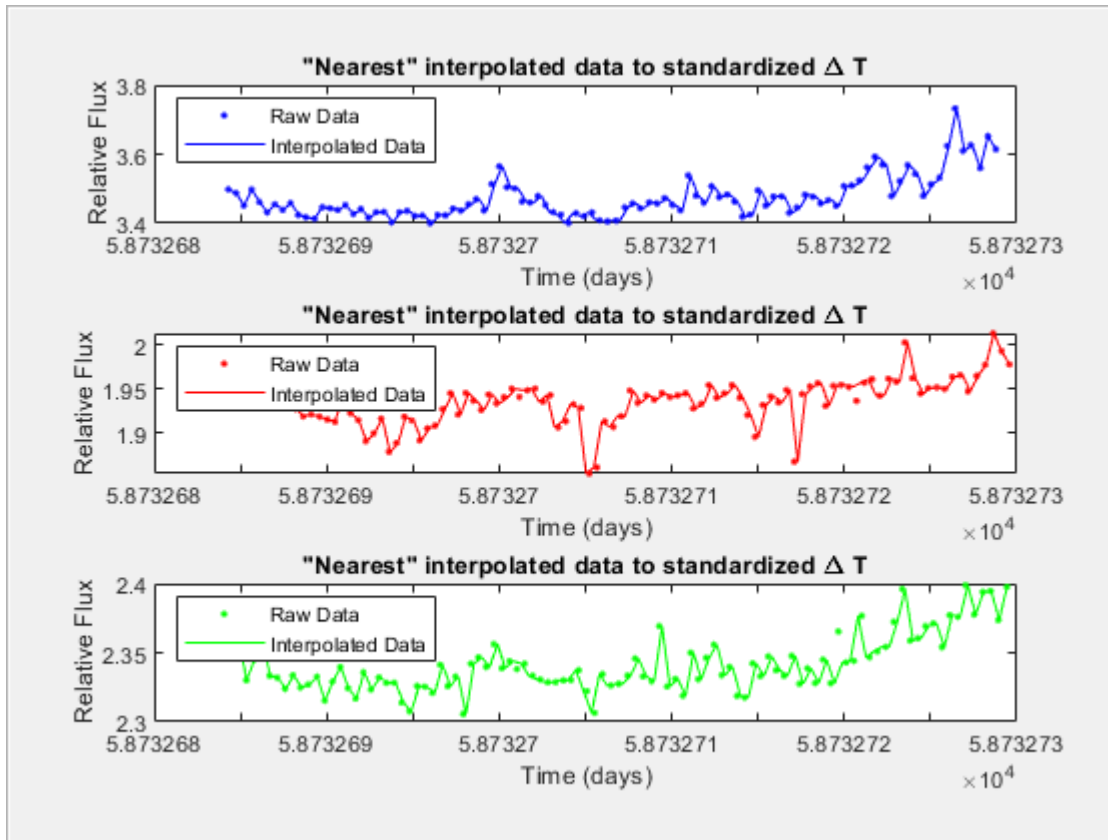
custom linear

```
hf_sub(4) = figure(4);
hp(4) = uipanel('Parent',hf_sub(4),'Position',[0 0 1 1]);
subplot(3,1,1,'Parent',hp(4));
[Tnew,Mnew] = Interp_Lin(BD55_441(1:100,1),BD55_441(1:100,2));
plot(BD55_441(1:100,1),BD55_441(1:100,2),'.b',Tnew,Mnew,'b');
title('"Custom linear" interpolated data to standardized \Delta T');
legend('Raw Data','Interpolated Data','location','northwest');
xlabel('Time (days)');
ylabel('Relative Flux');
subplot(3,1,2,'Parent',hp(4));
[Tnew,Mnew] = Interp_Lin(BD55_441(1:100,3),BD55_441(1:100,4));
plot(BD55_441(1:100,3),BD55_441(1:100,4),'.r',Tnew,Mnew,'r');
title('"Custom linear" interpolated data to standardized \Delta T');
legend('Raw Data','Interpolated Data','location','northwest');
xlabel('Time (days)');
ylabel('Relative Flux');
subplot(3,1,3,'Parent',hp(4));
[Tnew,Mnew] = Interp_Lin(BD55_441(1:100,5),BD55_441(1:100,6));
plot(BD55_441(1:100,5),BD55_441(1:100,6),'.g',Tnew,Mnew,'g');
title('"Custom linear" interpolated data to standardized \Delta T');
legend('Raw Data','Interpolated Data','location','northwest');
xlabel('Time (days)');
ylabel('Relative Flux');
```



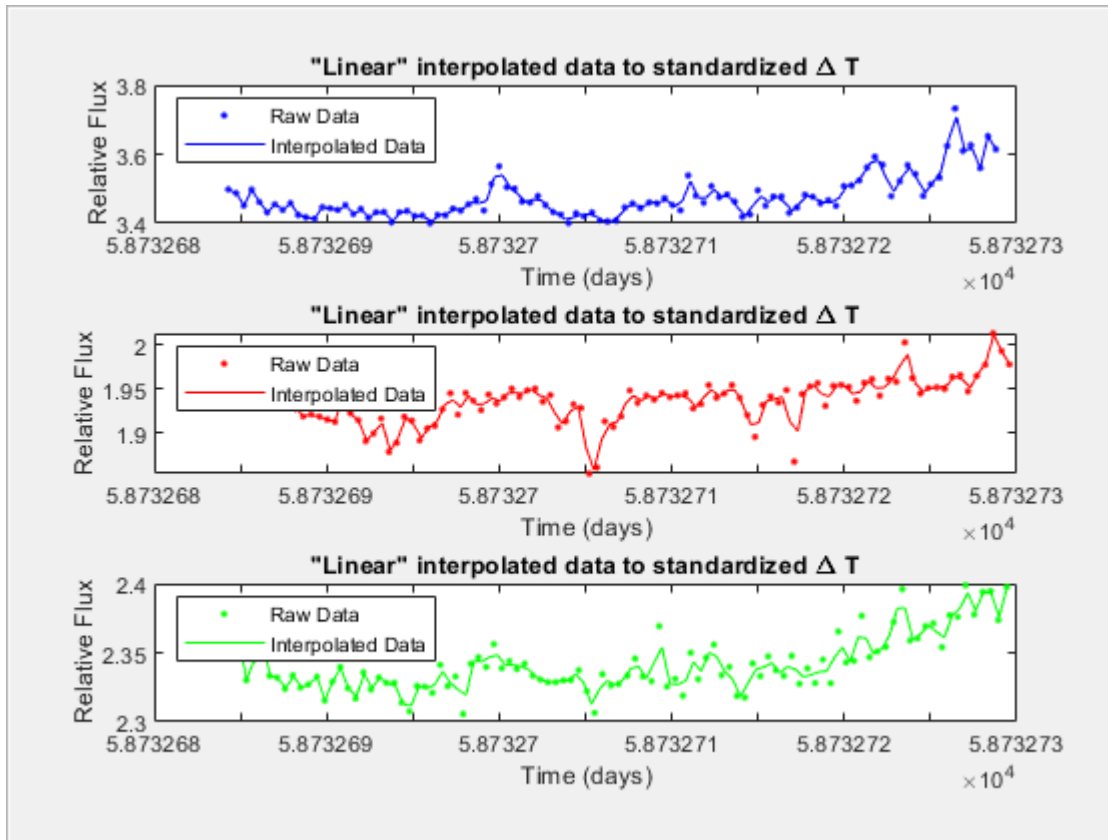
Nearest

```
hf_sub(5) = figure(5);
hp(5) = uipanel('Parent',hf_sub(5),'Position',[0 0 1 1]);
subplot(3,1,1,'Parent',hp(5));
[Tnew,Mnew] = Interp_nearest(BD55_441(2:100,1),BD55_441(2:100,2));
plot(BD55_441(1:100,1),BD55_441(1:100,2),'.b',Tnew,Mnew,'b');
title('"Nearest" interpolated data to standardized \Delta T');
legend('Raw Data','Interpolated Data','location','northwest');
xlabel('Time (days)');
ylabel('Relative Flux');
subplot(3,1,2,'Parent',hp(5));
[Tnew,Mnew] = Interp_nearest(BD55_441(1:100,3),BD55_441(1:100,4));
plot(BD55_441(1:100,3),BD55_441(1:100,4),'.r',Tnew,Mnew,'r');
title('"Nearest" interpolated data to standardized \Delta T');
legend('Raw Data','Interpolated Data','location','northwest');
xlabel('Time (days)');
ylabel('Relative Flux');
subplot(3,1,3,'Parent',hp(5));
[Tnew,Mnew] = Interp_nearest(BD55_441(1:100,5),BD55_441(1:100,6));
plot(BD55_441(1:100,5),BD55_441(1:100,6),'.g',Tnew,Mnew,'g');
title('"Nearest" interpolated data to standardized \Delta T');
legend('Raw Data','Interpolated Data','location','northwest');
xlabel('Time (days)');
ylabel('Relative Flux');
```



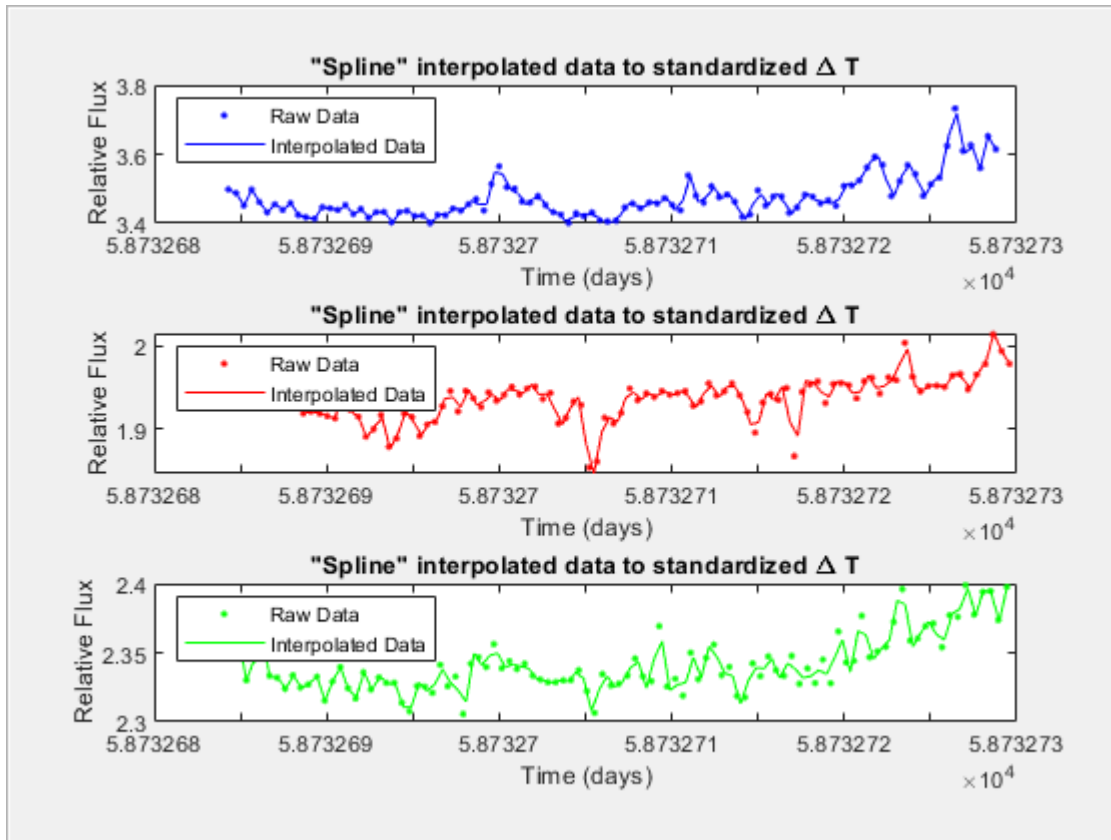
linear

```
hf_sub(6) = figure(6);
hp(6) = uipanel('Parent',hf_sub(6),'Position',[0 0 1 1]);
subplot(3,1,1,'Parent',hp(6));
[Tnew,Mnew] = Interp_linear(BD55_441(2:100,1),BD55_441(2:100,2));
plot(BD55_441(1:100,1),BD55_441(1:100,2),'.b',Tnew,Mnew,'b');
title('"Linear" interpolated data to standardized \Delta T');
legend('Raw Data','Interpolated Data','location','northwest');
xlabel('Time (days)');
ylabel('Relative Flux');
subplot(3,1,2,'Parent',hp(6));
[Tnew,Mnew] = Interp_linear(BD55_441(1:100,3),BD55_441(1:100,4));
plot(BD55_441(1:100,3),BD55_441(1:100,4),'.r',Tnew,Mnew,'r');
title('"Linear" interpolated data to standardized \Delta T');
legend('Raw Data','Interpolated Data','location','northwest');
xlabel('Time (days)');
ylabel('Relative Flux');
subplot(3,1,3,'Parent',hp(6));
[Tnew,Mnew] = Interp_linear(BD55_441(1:100,5),BD55_441(1:100,6));
plot(BD55_441(1:100,5),BD55_441(1:100,6),'.g',Tnew,Mnew,'g');
title('"Linear" interpolated data to standardized \Delta T');
legend('Raw Data','Interpolated Data','location','northwest');
xlabel('Time (days)');
ylabel('Relative Flux');
```



spline

```
hf_sub(7) = figure(7);
hp(7) = uipanel('Parent',hf_sub(7),'Position',[0 0 1 1]);
subplot(3,1,1,'Parent',hp(7));
[Tnew,Mnew] = Interp_spline(BD55_441(2:100,1),BD55_441(2:100,2));
plot(BD55_441(1:100,1),BD55_441(1:100,2),'.b',Tnew,Mnew,'b');
title('"Spline" interpolated data to standardized \Delta T');
legend('Raw Data','Interpolated Data','location','northwest');
xlabel('Time (days)');
ylabel('Relative Flux');
subplot(3,1,2,'Parent',hp(7));
[Tnew,Mnew] = Interp_spline(BD55_441(1:100,3),BD55_441(1:100,4));
plot(BD55_441(1:100,3),BD55_441(1:100,4),'.r',Tnew,Mnew,'r');
title('"Spline" interpolated data to standardized \Delta T');
legend('Raw Data','Interpolated Data','location','northwest');
xlabel('Time (days)');
ylabel('Relative Flux');
subplot(3,1,3,'Parent',hp(7));
[Tnew,Mnew] = Interp_spline(BD55_441(1:100,5),BD55_441(1:100,6));
plot(BD55_441(1:100,5),BD55_441(1:100,6),'.g',Tnew,Mnew,'g');
title('"Spline" interpolated data to standardized \Delta T');
legend('Raw Data','Interpolated Data','location','northwest');
xlabel('Time (days)');
ylabel('Relative Flux');
```



polyfit - needs to be conditioned appropriately.

```
hf_sub(8) = figure(8);
hp(8) = uipanel('Parent',hf_sub(8),'Position',[0 0 1 1]);
subplot(3,1,1,'Parent',hp(8));
[Tnew,Mnew] = Interp_polyfit(BD55_441(2:100,1),BD55_441(2:100,2));
```

Warning: Polynomial is badly conditioned. Add points with distinct X values, reduce the degree of the polynomial, or try centering and scaling as described in HELP POLYFIT.

```
plot(BD55_441(1:100,1),BD55_441(1:100,2),'.b',Tnew,Mnew,'b');
title('"Polyfit" interpolated data to standardized \Delta T');
legend('Raw Data','Interpolated Data','location','northwest');
xlabel('Time (days)');
ylabel('Relative Flux');
subplot(3,1,2,'Parent',hp(8));
[Tnew,Mnew] = Interp_polyfit(BD55_441(1:100,3),BD55_441(1:100,4));
```

Warning: Polynomial is badly conditioned. Add points with distinct X values, reduce the degree of the polynomial, or try centering and scaling as described in HELP POLYFIT.

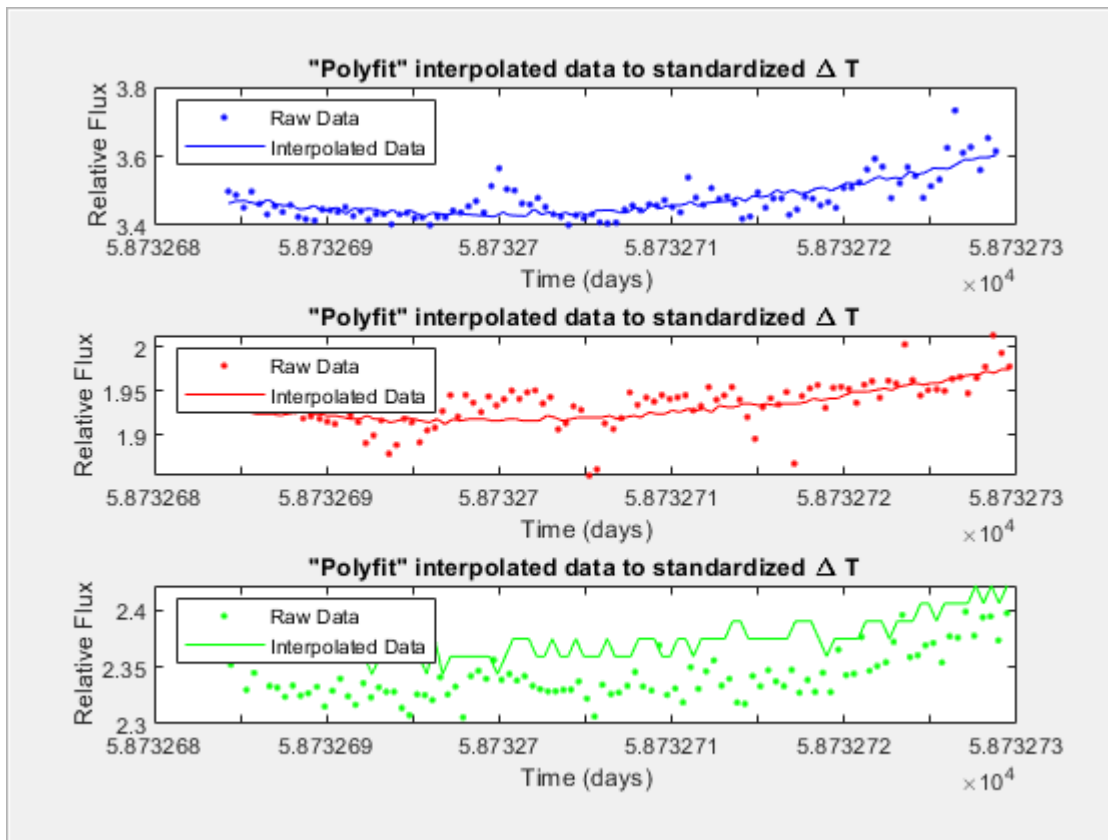
```
plot(BD55_441(1:100,3),BD55_441(1:100,4),'.r',Tnew,Mnew,'r');
title('"Polyfit" interpolated data to standardized \Delta T');
legend('Raw Data','Interpolated Data','location','northwest');
xlabel('Time (days)');
```



```
ylabel('Relative Flux');
subplot(3,1,3,'Parent',hp(8));
[Tnew,Mnew] = Interp_polyfit(BD55_441(1:100,5),BD55_441(1:100,6));
```

Warning: Polynomial is badly conditioned. Add points with distinct X values, reduce the degree of the polynomial, or try centering and scaling as described in HELP POLYFIT.

```
plot(BD55_441(1:100,5),BD55_441(1:100,6),'.g',Tnew,Mnew,'g');
title('"Polyfit" interpolated data to standardized \Delta T');
legend('Raw Data','Interpolated Data','location','northwest');
xlabel('Time (days)');
ylabel('Relative Flux');
```



Input all data

Text files:

```
%BD+48_1098
opts = detectImportOptions("BD+48_1098.txt");
opts.DataLines = 3;
opts.VariableNames = {'B_time','B_flux','R_time','R_flux','V_time','V_flux'};
opts.VariableTypes = {'double','double','double','double','double','double'};
BD48_1098 = rmmissing(readmatrix("BD+55_441.txt",opts)); %the matrix data of the text file
```

```
%preview("BD+48_1098.txt",opts)
whos BD48_1098
```

Name	Size	Bytes	Class	Attributes
BD48_1098	100x6	4800	double	

```
%HD28497
opts = detectImportOptions("HD28497.txt");
opts.DataLines = 3;
opts.VariableNames = {'B_time','B_flux','R_time','R_flux','V_time','V_flux'};
opts.VariableTypes = {'double','double','double','double','double','double'};
HD28497 = rmmissing(readmatrix("HD28497.txt",opts)) %the matrix data of the text file
```

```
HD28497 = 600x6
104 x
 5.844163256000000 0.151884039400000 5.844163279000000 0.047485834000000 ...
 5.844163294000000 0.157713255000000 5.844163317000000 0.047850097100000
 5.844163332000000 0.147648080800000 5.844163355000000 0.050717498800000
 5.844163370000000 0.154105058200000 5.844163393000001 0.048745268800000
 5.844163409000000 0.154416998300000 5.844163431999999 0.046480291500000
 5.844163447000000 0.154034530100000 5.844163470000000 0.052878906200000
 5.844163485000000 0.158524561400000 5.844163508000000 0.050080829500000
 5.844163523000000 0.159731365000000 5.844163546000000 0.053844298900000
 5.844163560999999 0.140623476800000 5.844163584000000 0.050871022200000
 5.844163599000000 0.159835953000000 5.844163622000000 0.053311599500000
  :
```

```
%preview("HD28497.txt",opts)
whos HD28497
```

Name	Size	Bytes	Class	Attributes
HD28497	600x6	28800	double	

```
%HD46131
opts = detectImportOptions("HD46131.txt");
opts.DataLines = 3;
opts.VariableNames = {'B_time','B_flux','R_time','R_flux','V_time','V_flux'};
opts.VariableTypes = {'double','double','double','double','double','double'};
HD46131 = rmmissing(readmatrix("HD46131.txt",opts)); %the matrix data of the text file
%preview("HD46131.txt",opts)
whos HD46131
```

Name	Size	Bytes	Class	Attributes
HD46131	250x6	12000	double	

```
%HD88661
opts = detectImportOptions("HD88661.txt");
opts.DataLines = 3;
opts.VariableNames = {'B_time','B_flux','R_time','R_flux','V_time','V_flux'};
opts.VariableTypes = {'double','double','double','double','double','double'};
HD88661 = rmmissing(readmatrix("HD88661.txt",opts)); %the matrix data of the text file
%preview("HD88661.txt",opts)
whos HD88661
```

Name	Size	Bytes	Class	Attributes
HD88661	35x6	1680	double	

```
%HD105521
opts = detectImportOptions("HD105521.txt");
opts.DataLines = 3;
opts.VariableNames = {'B_time','B_flux','R_time','R_flux','V_time','V_flux'};
opts.VariableTypes = {'double','double','double','double','double','double'};
HD105521 = rmmissing(readmatrix("HD105521.txt",opts)); %the matrix data of the text file
%preview("HD105521.txt",opts)
whos HD105521
```

Name	Size	Bytes	Class	Attributes
HD105521	180x6	8640	double	

```
%HD105521
opts = detectImportOptions("HD105521.txt");
opts.DataLines = 3;
opts.VariableNames = {'B_time','B_flux','R_time','R_flux','V_time','V_flux'};
opts.VariableTypes = {'double','double','double','double','double','double'};
HD105521 = rmmissing(readmatrix("HD105521.txt",opts)); %the matrix data of the text file
%preview("HD105521.txt",opts)
whos HD105521
```

Name	Size	Bytes	Class	Attributes
HD105521	180x6	8640	double	

CSV files

```
%HD106306
%B_filter
opts = detectImportOptions('HD106306_B.csv');
opts.DataLines = [2 Inf];
All_fields_available = opts.VariableNames;
opts.SelectedVariableNames = {'J_D__2400000','rel_flux_T1'};
%preview("HD106306_B.csv",opts)
HD106306_B = readmatrix("HD106306_B.csv",opts);

%R_filter
opts = detectImportOptions('HD106306_R.csv');
opts.DataLines = [2 Inf];
All_fields_available = opts.VariableNames;
opts.SelectedVariableNames = {'J_D__2400000','rel_flux_T1'};
%preview("HD106306_R.csv",opts)
HD106306_R = readmatrix("HD106306_R.csv",opts);

%V_filter
opts = detectImportOptions('HD106306_V.csv');
opts.DataLines = [2 Inf];
All_fields_available = opts.VariableNames;
opts.SelectedVariableNames = {'J_D__2400000','rel_flux_T1'};
%preview("HD106306_V.csv",opts)
HD106306_V = readmatrix("HD106306_V.csv",opts);
```

```
HD106306 = rmmissing([HD106306_B HD106306_R HD106306_V]); %the matrix data of the text file
whos HD106306
```

Name	Size	Bytes	Class	Attributes
HD106306	100x6	4800	double	

```
%HD147302
%B_filter
opts = detectImportOptions('HD147302_B.csv');
opts.DataLines = [2 Inf];
All_fields_available = opts.VariableNames;
opts.SelectedVariableNames = {'J_D__2400000','rel_flux_T1'};
%preview("HD147302_B.csv",opts)
HD147302_B = readmatrix("HD147302_B.csv",opts);
```

```
%R_filter
opts = detectImportOptions('HD147302_R.csv');
opts.DataLines = [2 Inf];
All_fields_available = opts.VariableNames;
opts.SelectedVariableNames = {'J_D__2400000','rel_flux_T1'};
%preview("HD147302_R.csv",opts)
HD147302_R = readmatrix("HD147302_R.csv",opts);
```

```
%V_filter
opts = detectImportOptions('HD147302_V.csv');
opts.DataLines = [2 Inf];
All_fields_available = opts.VariableNames;
opts.SelectedVariableNames = {'J_D__2400000','rel_flux_T1'};
%preview("HD147302_V.csv",opts)
HD147302_V = readmatrix("HD147302_V.csv",opts);
```

```
HD147302 = rmmissing([HD147302_B HD147302_R HD147302_V]); %the matrix data of the text file
whos HD147302
```

Name	Size	Bytes	Class	Attributes
HD147302	100x6	4800	double	

HD152060 and HD209522 can't be described in the same form as the others.

```
%HD152060
%R_filter
opts = detectImportOptions('HD152060_R.csv');
opts.DataLines = [2 Inf];
All_fields_available = opts.VariableNames;
opts.SelectedVariableNames = {'J_D__2400000','rel_flux_T1'};
%preview("HD147302_R.csv",opts)
HD152060_R = readmatrix("HD152060_R.csv",opts);
```

```
%V_filter
opts = detectImportOptions('HD152060_V.csv');
opts.DataLines = [2 Inf];
All_fields_available = opts.VariableNames;
```

```

opts.SelectedVariableNames = {'J_D_2400000','rel_flux_T1'};
%preview("HD147302_V.csv",opts)
HD152060_V = readmatrix("HD152060_V.csv",opts);

HD152060 = rmmissing([HD147302_R HD147302_V]); %the matrix data of the text file
whos HD152060

```

Name	Size	Bytes	Class	Attributes
HD152060	100x4	3200	double	

```

%HD209522
%B_filter
opts = detectImportOptions('HD209522_B.csv');
opts.DataLines = [2 Inf];
All_fields_available = opts.VariableNames;
opts.SelectedVariableNames = {'J_D_2400000','rel_flux_T1'};
%preview("HD147302_R.csv",opts)
HD209522 = readmatrix("HD209522_B.csv",opts);

%the matrix data of the text file
whos HD209522

```

Name	Size	Bytes	Class	Attributes
HD209522	408x2	6528	double	

```

close all %closes all previous figures from milestone 1 so that the plots in milestone 2 and

```

Milestone 2 (13 October)

https://www.mathworks.com/help/matlab/ref/fft.html?searchHighlight=fft&s_tid=srchtitle

This is the source for implementing Fourier Transform for a Noisy Signal from the MathWorks documentation

Using fft for HD28497

This star had the most data which made it ideal for performing a fourier transform. We chose linear interpolation for the purposes of this experiment at random. This is a feature to be explored later.

```

[Tnew,Mnew] = Interp_linear(HD28497(2:end,1),HD28497(2:end,2));
Tnew = Tnew*86400; %convert time from days to seconds
deltaT = Tnew(2)-Tnew(1);
Fs = 1/deltaT; % Sampling frequency
T = deltaT; % Sampling period
t = Tnew; % Time vector
L = numel(Tnew); % Length of signal
X = Mnew; %signal with noise
%Fourier transformation
Y = fft(X);
P2complex = abs(Y/L); %real and imaginary parts together
%Bk

```

```

P2real = 2*real(Y);
P2imaginary = 2*imag(Y);
P1complex = P2complex(1:floor(L/2)+1);
P1complex(2:end-1) = 2*P1complex(2:end-1);

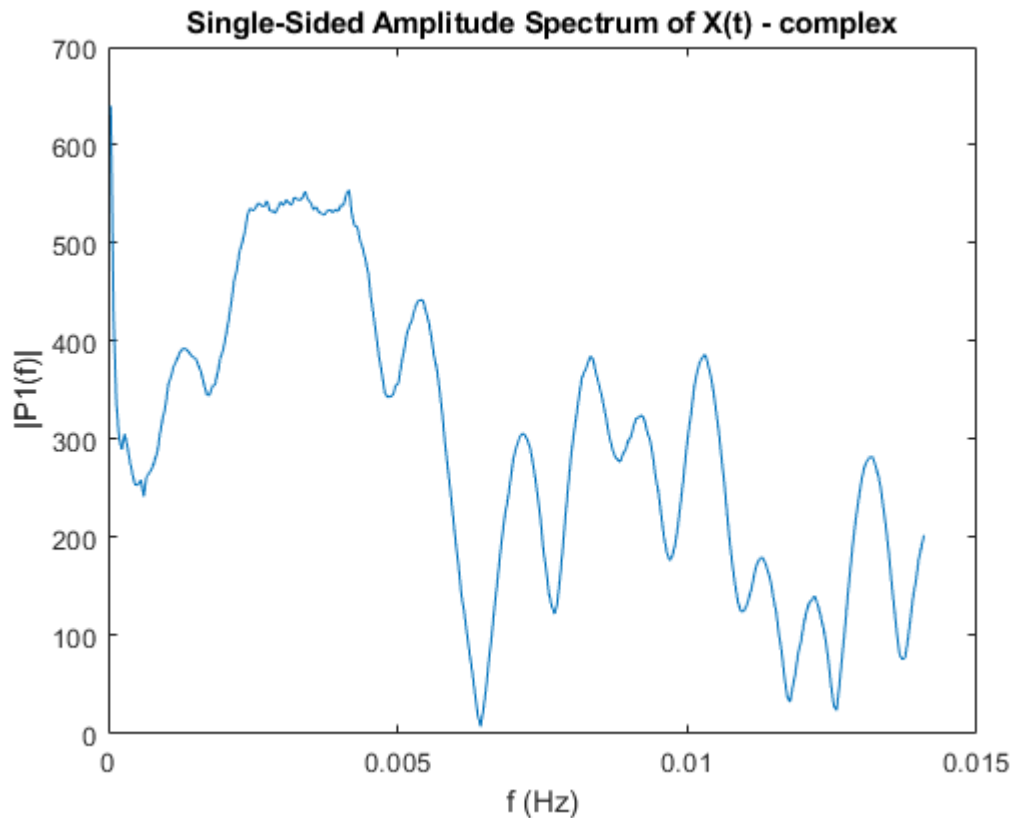
```

```
%Plot
```

```

f = Fs*(0:(L/2))/L;
plot(f(2:end-1),P1complex(2:end-1))
title('Single-Sided Amplitude Spectrum of X(t) - complex')
xlabel('f (Hz)')
ylabel('|P1(f)|')

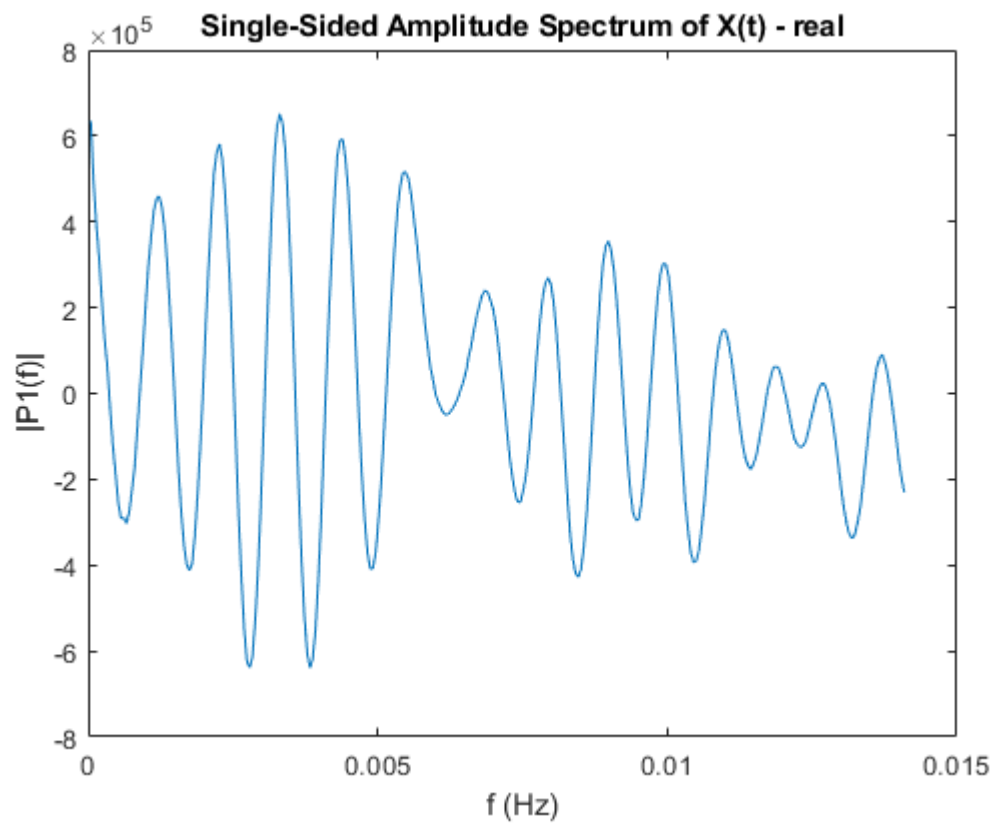
```



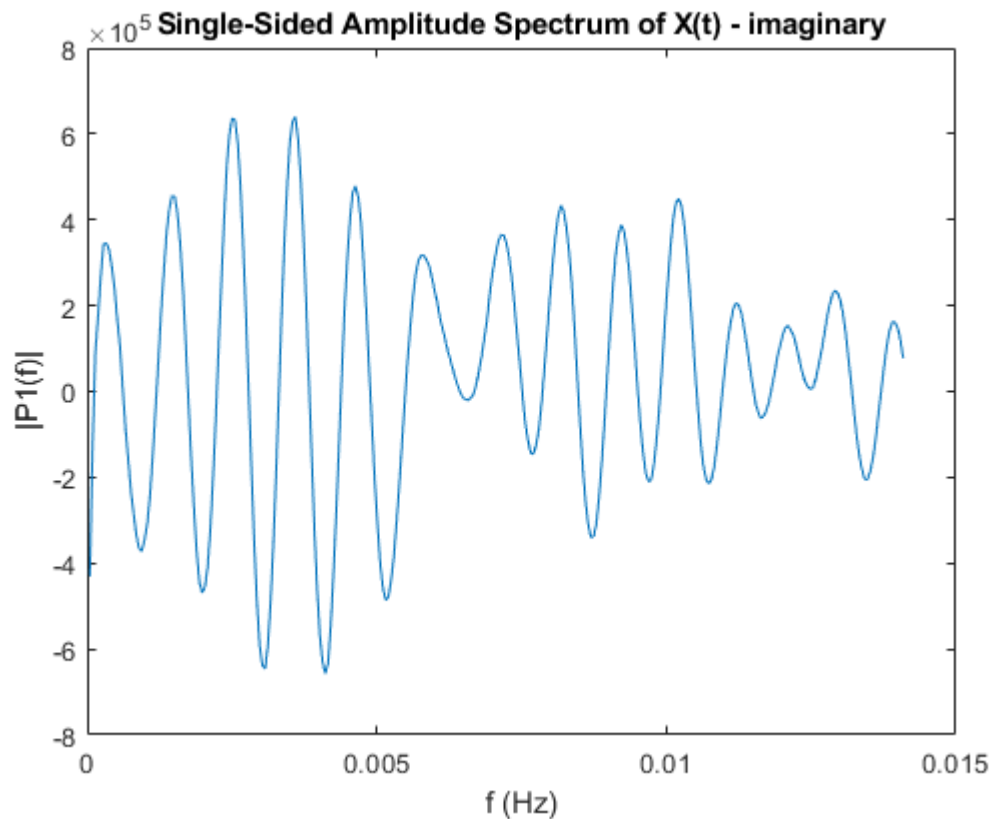
```

P1real = P2real(1:floor(L/2)+1);
P1real(2:end-1) = 2*P1real(2:end-1);
%plotting piece
f = Fs*(0:(L/2))/L;
plot(f(2:end-1),P1real(2:end-1))
title('Single-Sided Amplitude Spectrum of X(t) - real')
xlabel('f (Hz)')
ylabel('|P1(f)|')

```



```
P1imaginary = P2imaginary(1:floor(L/2)+1);
P1imaginary(2:end-1) = 2*P1imaginary(2:end-1);
%plotting piece
f = Fs*(0:(L/2))/L;
plot(f(2:end-1),P1imaginary(2:end-1))
title('Single-Sided Amplitude Spectrum of X(t) - imaginary')
xlabel('f (Hz)')
ylabel('|P1(f)|')
```



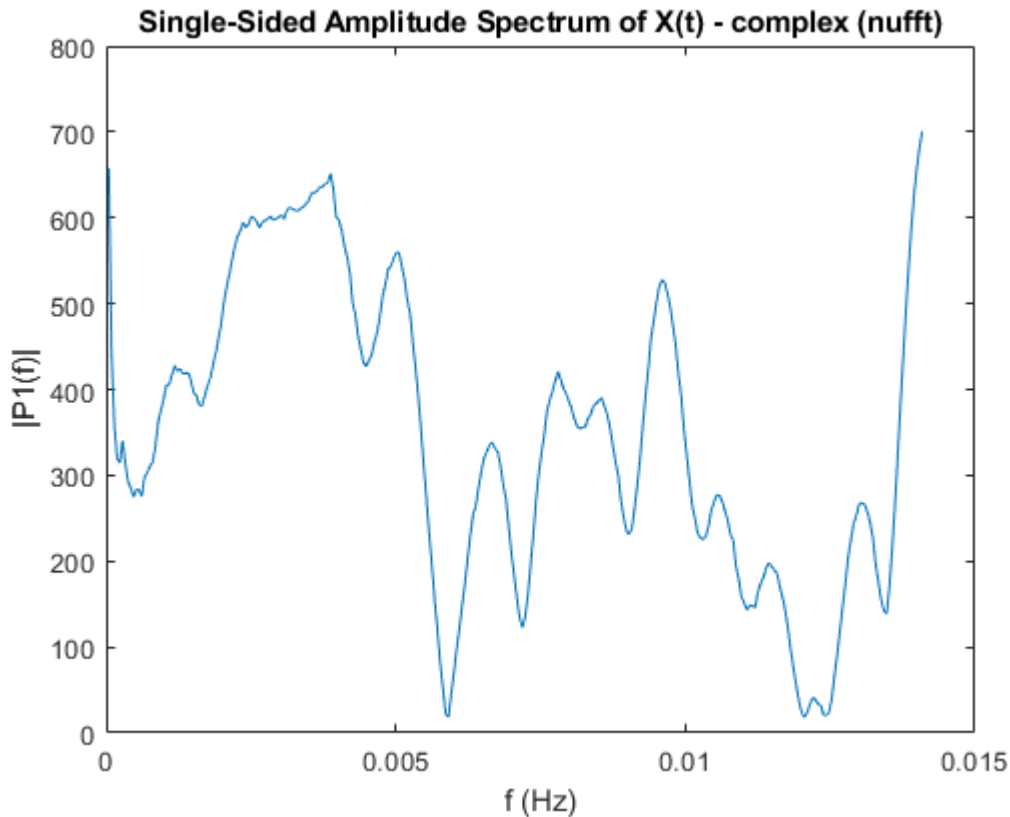
Using NUFFT - used the data without interpolation

Results for this one star using the complex combination was very similar to fft.

```
Tnew = HD28497(2:end,1);
Mnew = HD28497(2:end,2);
Tnew = Tnew*86400;
% --Find averaged time scale--
n = numel(Tnew);
sum = 0;
for l = 1:n-1
    sum = sum + abs(Tnew(l+1) - Tnew(l));
end
deltaT = sum / (n-1); %average time between points
Fs = 1/deltaT;        % Sampling frequency
T = deltaT;           % Sampling period
t = Tnew;             % Time vector
L = numel(Tnew);      % Length of signal
X = Mnew;              %signal with noise
%Fourier transformation
Y = nufft(X);
P2complex = abs(Y/L); %combination of real and imaginary
P2real = 2*real(Y);
P2imaginary = 2*imag(Y);
P1complex = P2complex(1:floor(L/2)+1);
P1complex(2:end-1) = 2*P1complex(2:end-1);
%plotting piece
f = Fs*(0:(L/2))/L;
```



```
plot(f(2:end-1),P1complex(2:end-1))
title('Single-Sided Amplitude Spectrum of X(t) - complex (nufft)')
xlabel('f (Hz)')
ylabel('|P1(f)|')
```



The investigation of the inverse fourier transform will be explored at a later date to complete milestone 2.

Milestone 3 (including previously unfinished parts of milestone 2)

Getting the Power Spectrum for HD28497

This star had the most data which made it ideal for performing a fourier transform. We chose linear interpolation for the purposes of this experiment at random. This is a feature to be explored late

Documentation: We used a combination of the following sources to develop this:

1. https://www.mathworks.com/help/matlab/ref/fft.html?searchHighlight=fft&s_tid=srchtitle (This is the source for implementing Fourier Transform for a Noisy Signal from the MathWorks documentation)
2. Gilat, Example 7-6 (pg. 281)
3. Gilat, Example 7-8 (pg 287)

Bd+55_441 and HD 28497 have documented periodicity - citation pending

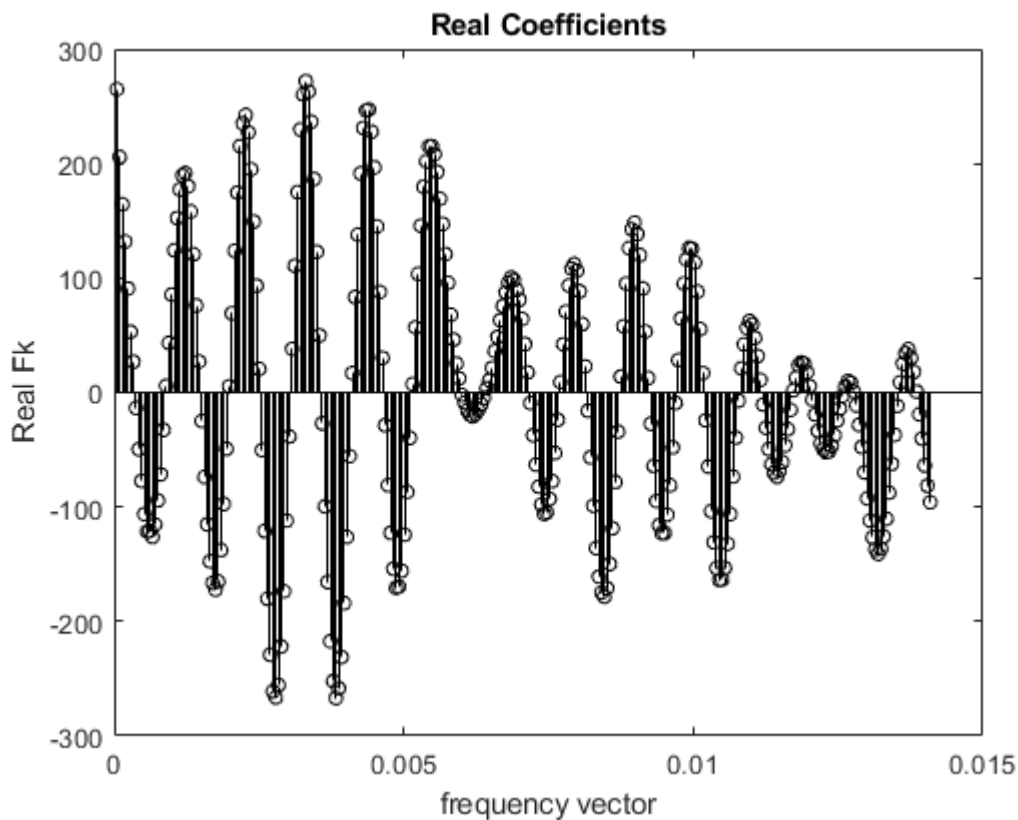
```
[Tnew,Mnew] = Interp_linear(HD28497(2:end,1),HD28497(2:end,2));
Tnew = Tnew*86400; %convert time from days to seconds
deltaT = Tnew(2)-Tnew(1);
```

```

Fs = 1/deltaT;           % Sampling frequency
T = deltaT;              % Sampling period
t = Tnew-Tnew(1);        % Time vector
L = numel(Tnew);         % Length of signal
X = Mnew ;               %signal with noise

%Fourier transformation   %Based on Ex 7-6 Gilat
F = fft(X)/L ;           %fourier transform divided by number of data points
power = F.*conj(F)/L;
powernorm = power/max(power); %normalized power spectrum
fk = (0:L-1)*(Fs/L);      %frequency vector Gilat 7-6
stem(fk(2:floor(L/2)),real(F(2:floor(L/2))), 'ko','markersize',5) %Threw out first
xlabel('frequency vector')
ylabel('Real Fk')
title('Real Coefficients')

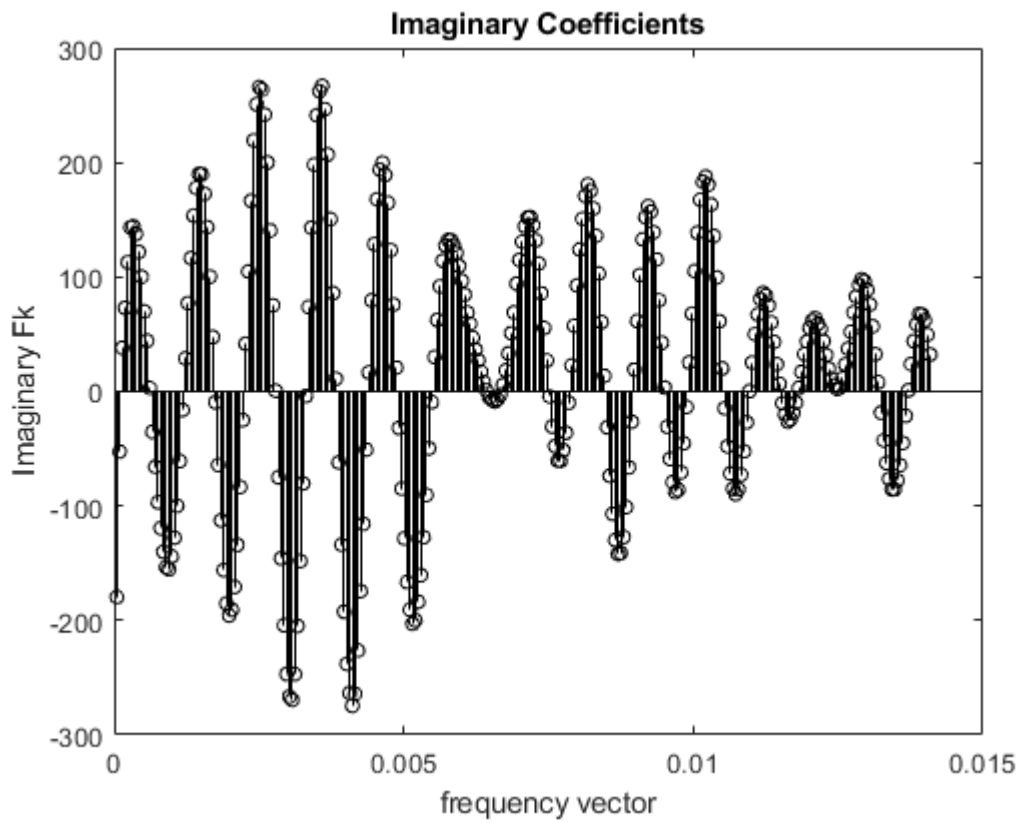
```



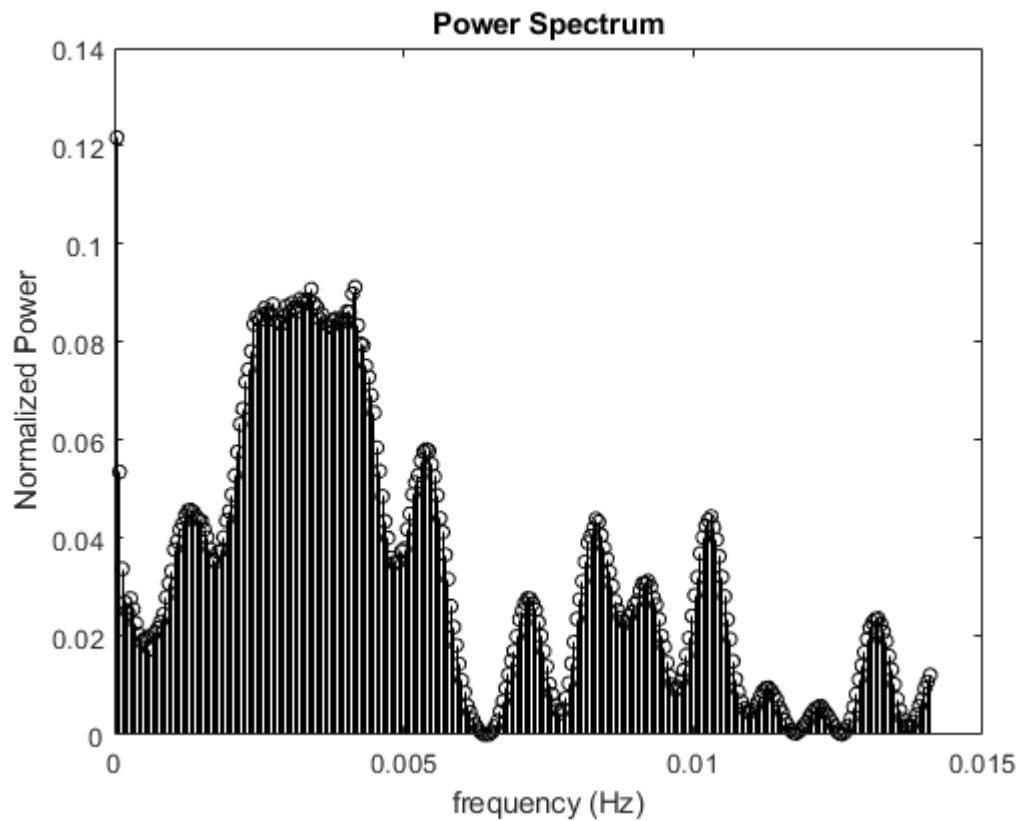
```

figure, stem(fk(2:floor(L/2)),imag(F(2:floor(L/2))), 'ko','markersize',5)
xlabel('frequency vector')
ylabel('Imaginary Fk')
title('Imaginary Coefficients')

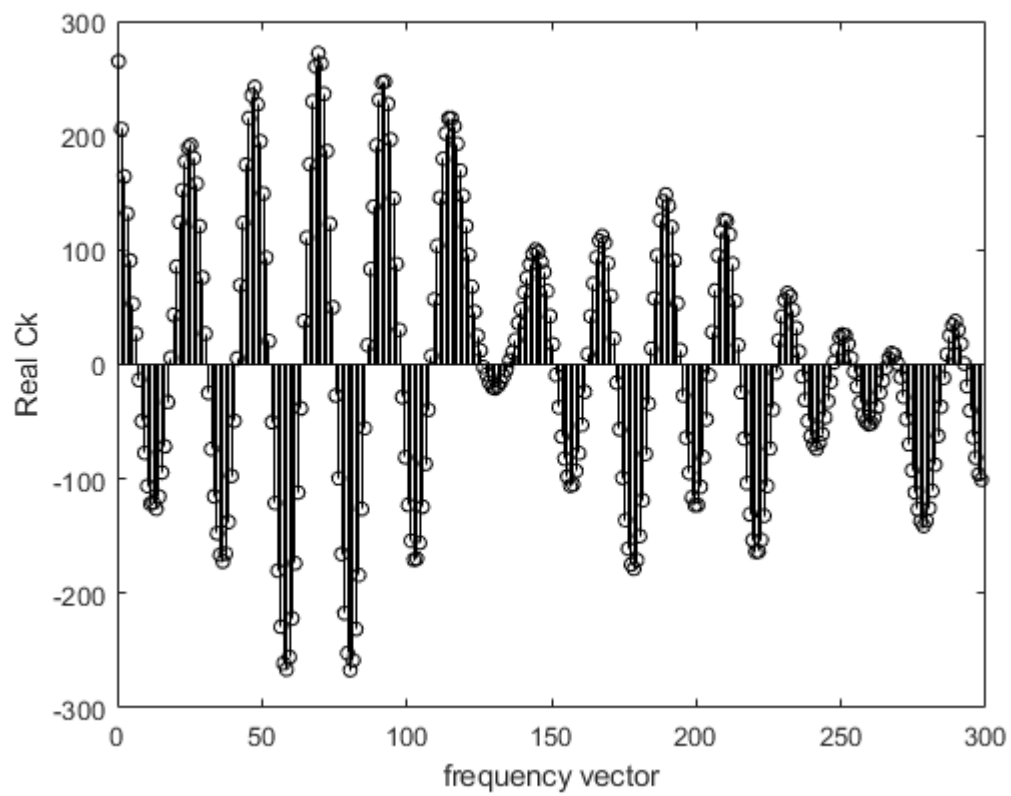
```



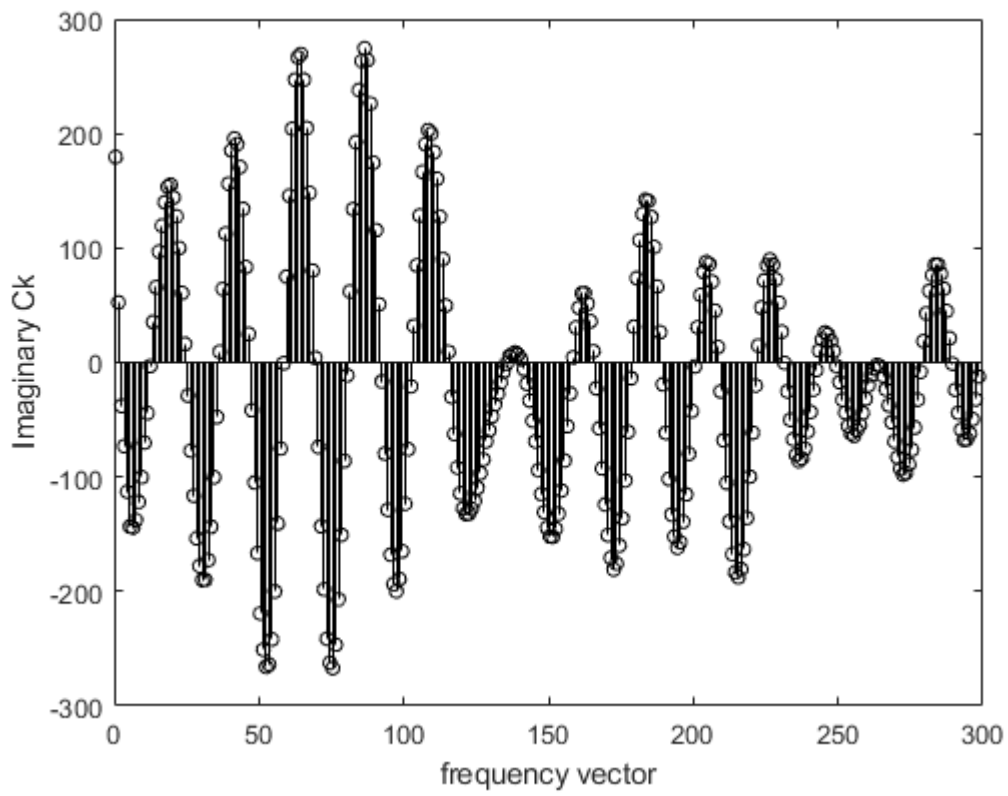
```
figure, stem(fk(2:floor(L/2)),powernorm(2:floor(L/2)),'ko','markersize',5)
xlabel('frequency (Hz)')
ylabel('Normalized Power')
title('Power Spectrum')
```



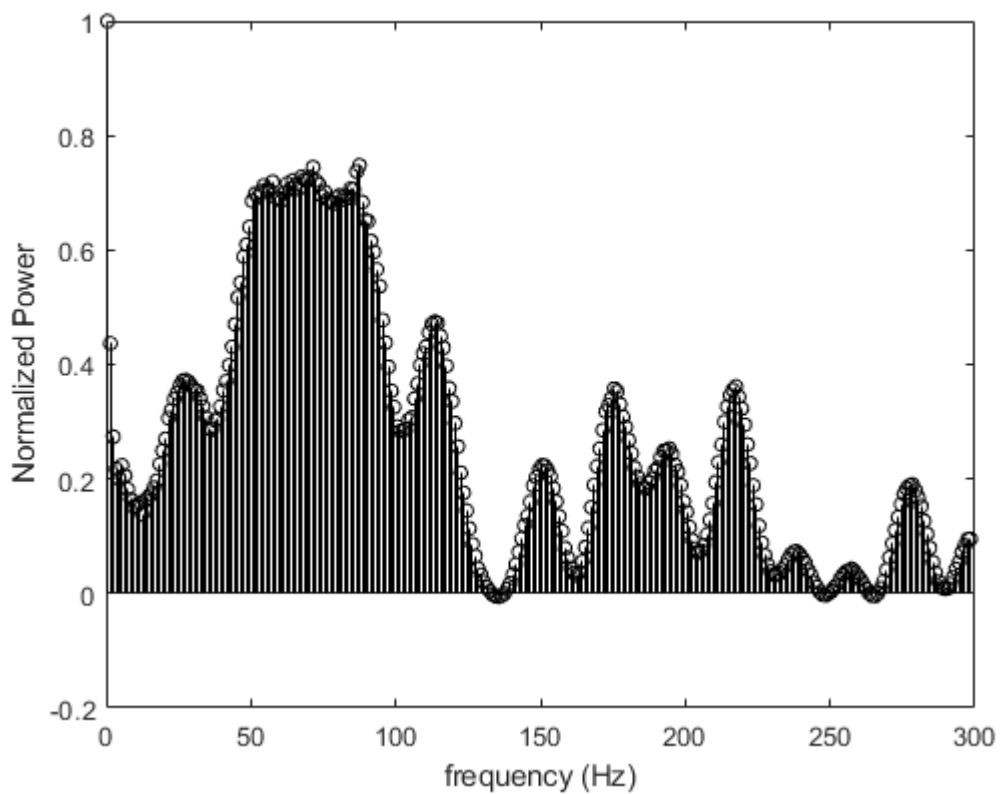
```
%Rearrange the spectrum using fftshift
C0 = fftshift(F(2:L));           %zero frequency in center (threw out first number of F as a
power0 = C0.*conj(C0)/L-1;
powernorm0 = power0/max(power0); %normalized power spectrum
fk0 = (-L/2+1:L/2-1)*(Fs/L-1);  %frequency vector Gilat 7-6
stem(fk0(1:floor(L/2)),real(C0(1:floor(L/2))), 'ko','markersize',5)
xlabel('frequency vector')
ylabel('Real Ck')
```



```
figure, stem(fk0(1:floor(L/2)),imag(C0(1:floor(L/2))), 'ko', 'markersize', 5)
xlabel('frequency vector')
ylabel('Imaginary Ck')
```



```
figure, stem(fk0(1:floor(L/2)),powernorm0(1:floor(L/2)),'ko','markersize',5)
xlabel('frequency (Hz)')
ylabel('Normalized Power')
```

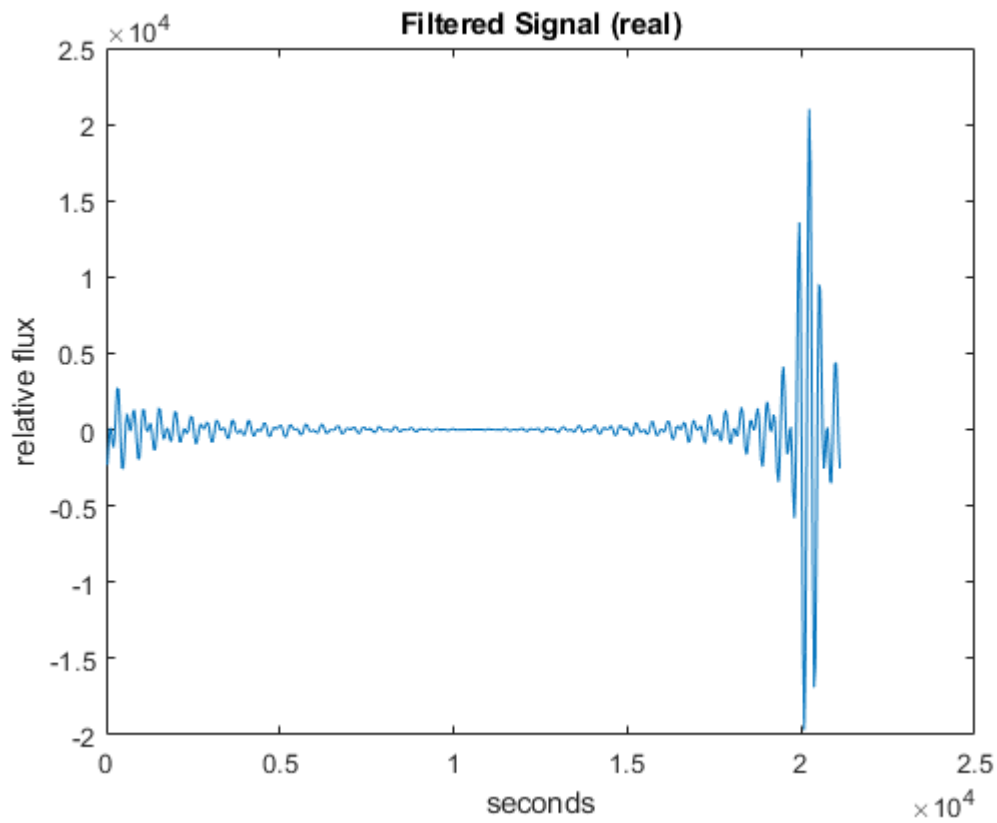


%Filtering out the noise Based on Gilat Example 7-8

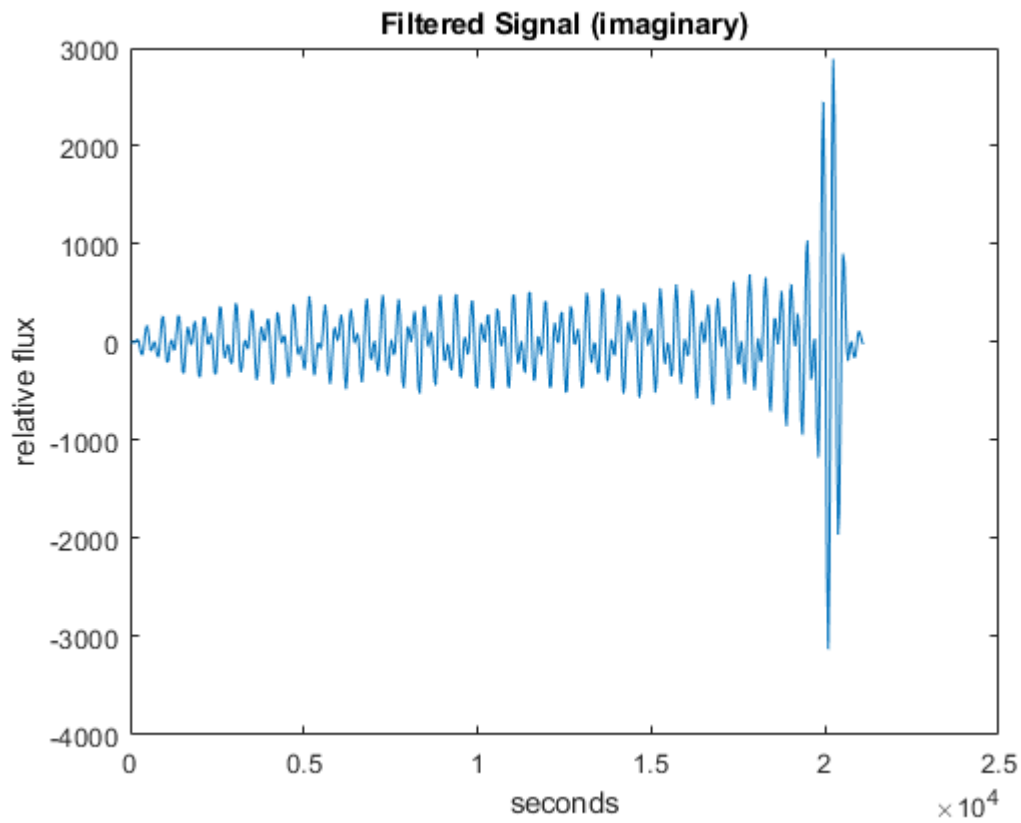
```
for k = 1:L-1
    if abs(fk0(k)) <= 50 || abs(fk0(k)) >= 90
        C0filter(k) = 0+0i;

    else
        C0filter(k) = C0(k);
    end
end
```

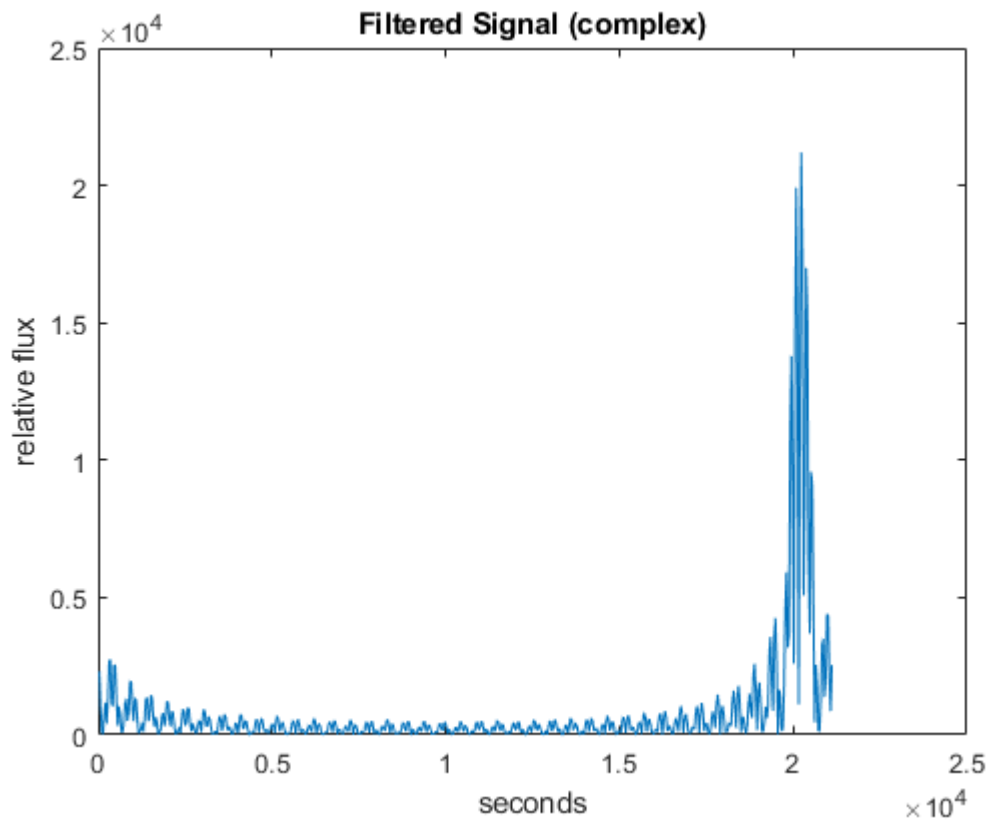
```
F0i = ifftshift(C0filter) * L-1;
finv = ifft(F0i);
figure, plot(t(2:L),real(finv))
title('Filtered Signal (real)')
xlabel('seconds')
ylabel('relative flux')
```



```
F0i = ifftshift(C0filter) * L-1;
finv = ifft(F0i);
figure, plot(t(2:L),imag(finv))
title('Filtered Signal (imaginary)')
xlabel('seconds')
ylabel('relative flux')
```

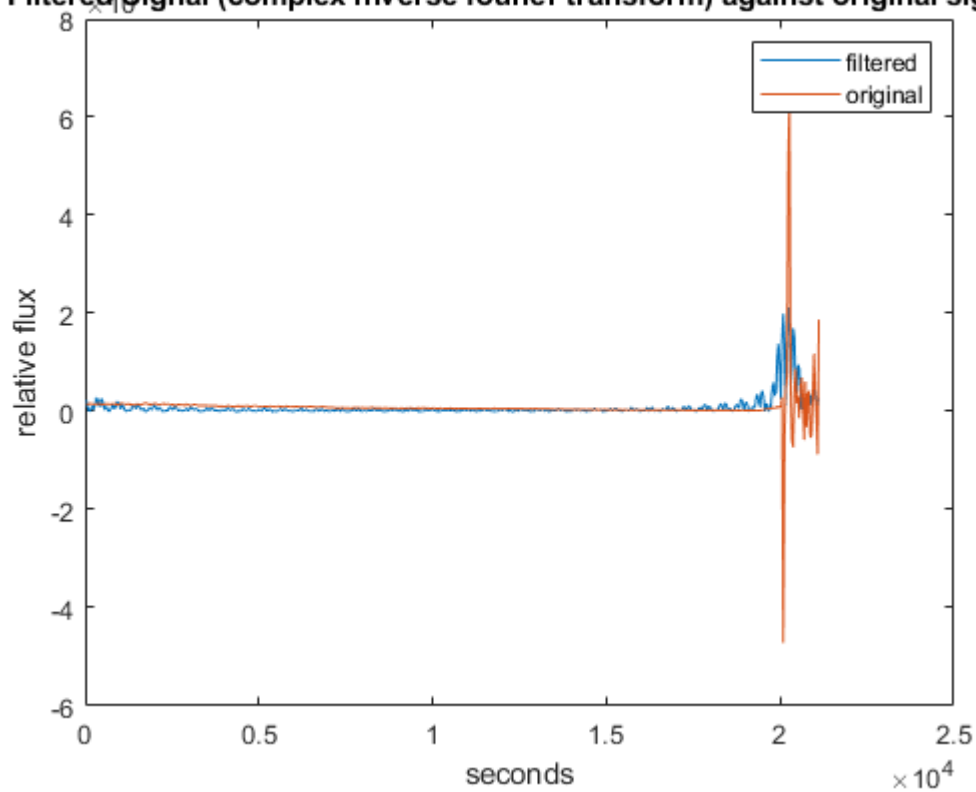



```
F0i = ifftshift(C0flter) * L-1;
finv = ifft(F0i);
figure, plot(t(2:L),abs(finv))
title('Filtered Signal (complex)')
xlabel('seconds')
ylabel('relative flux')
```



```
F0i = ifftshift(C0flter) * L-1;
finv = ifft(F0i);
figure, plot(t(2:L),abs(finv),t(2:L),X(2:L))
legend('filtered','original')
title('Filtered Signal (complex inverse fourier transform) against original signal')
xlabel('seconds')
ylabel('relative flux')
```

Filtered Signal (complex inverse fourier transform) against original signal

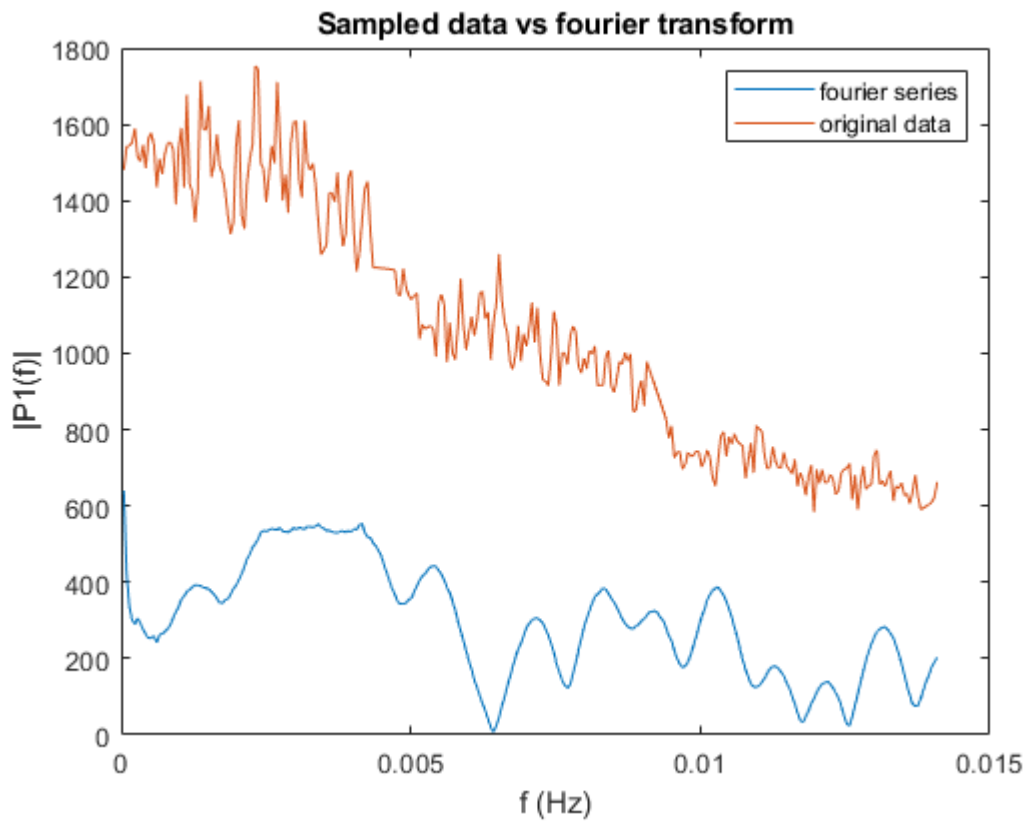


```
F = 1./t(2:L);

%Fourier transformation
Y = fft(X);
P2complex = abs(Y/L); %real and imaginary parts together
P2real = 2*real(Y);
P2imaginary = 2*imag(Y);
P1complex = P2complex(1:floor(L/2)+1);
P1complex(2:end-1) = 2*P1complex(2:end-1);

%Plot

f = Fs*(0:(L/2))/L;
plot(f(2:end-1),P1complex(2:end-1),f(2:end-1),X(2:floor(L/2)))
title('Sampled data vs fourier transform')
xlabel('f (Hz)')
ylabel('|P1(f)|')
legend('fourier series','original data')
```

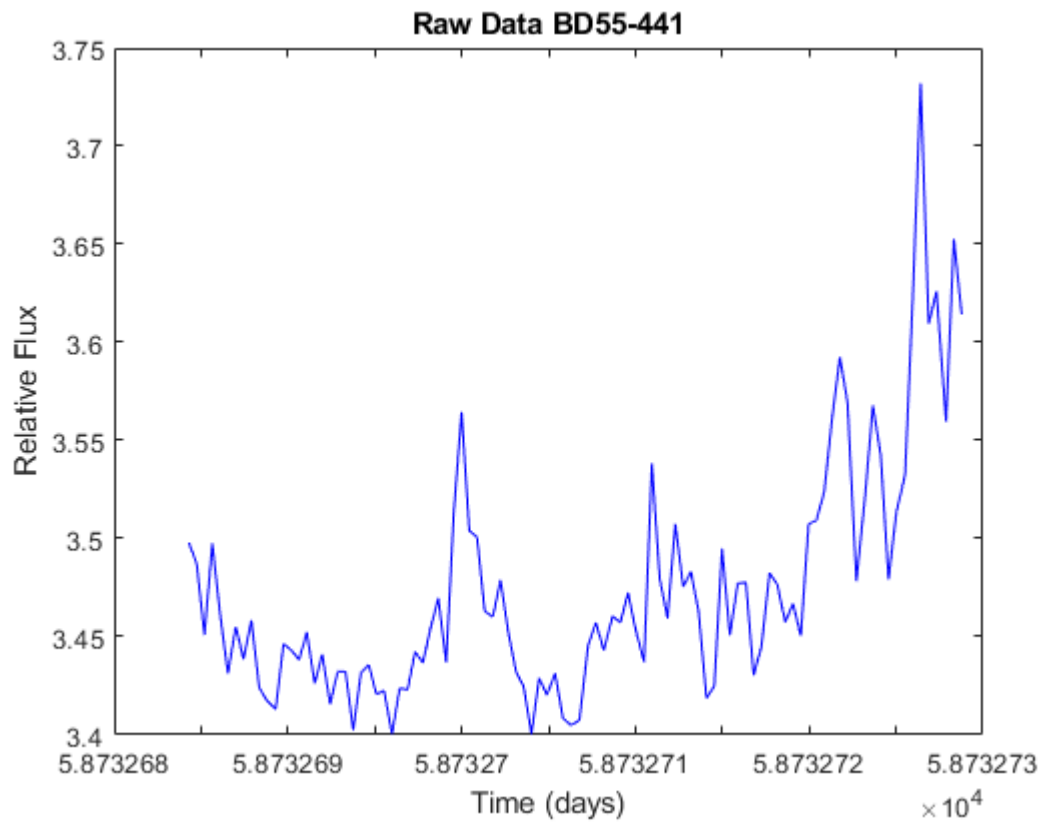


Milestone 4: Linear Combination of non-linear functions

BD55

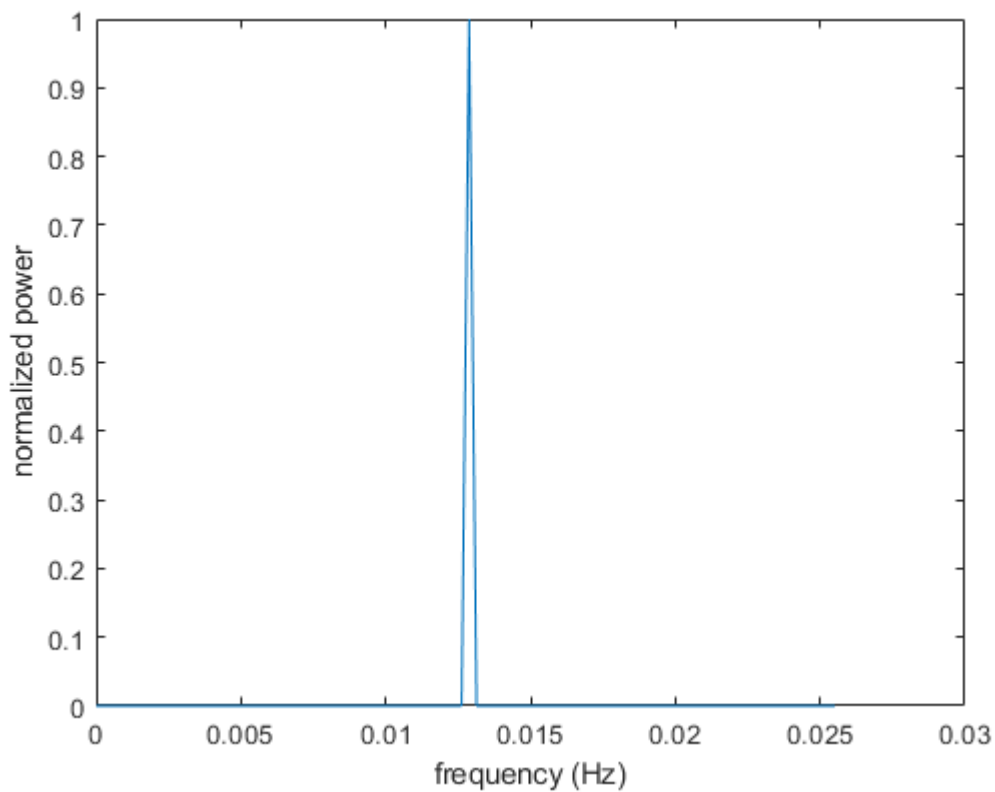
Plot the raw data

```
plot(BD55_441(1:100,1),BD55_441(1:100,2),'b');
title('Raw Data BD55-441');
xlabel('Time (days)');
ylabel('Relative Flux');
```



Use Linear Interpolation, then use a Fourier transform to attain the power spectrum

```
[Tnew,Mnew] = Interp_Lin(BD55_441(1:100,1),BD55_441(1:100,2));
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt)
```



```
fk = 1×100
      0    0.000257606417519    0.000515212835038    0.000772819252558 ...
powerNor = 1×100
      0.000000000470212    0.000000116089656    0.000000017611039    0.000000053274678 ...
```

Functions for linear combination:

(main frequency is 0.0129 HZ, or 1,115 per Day. Use this to choose my non-linear functions)

```
F1 = @(x) x./x;
F2 = @(x) cos(2*pi*(1115)).*(x);
F3 = @(x) sin(2*pi*(1115)).*(x);
```

```
%call the NLfit function
```

```
c = NLfit(F1,F2,F3,BD55_441(1:100,1),BD55_441(1:100,2))
```

```
Warning: Matrix is close to singular or badly scaled. Results may be inaccurate. RCOND = 2.980448e-42.
```

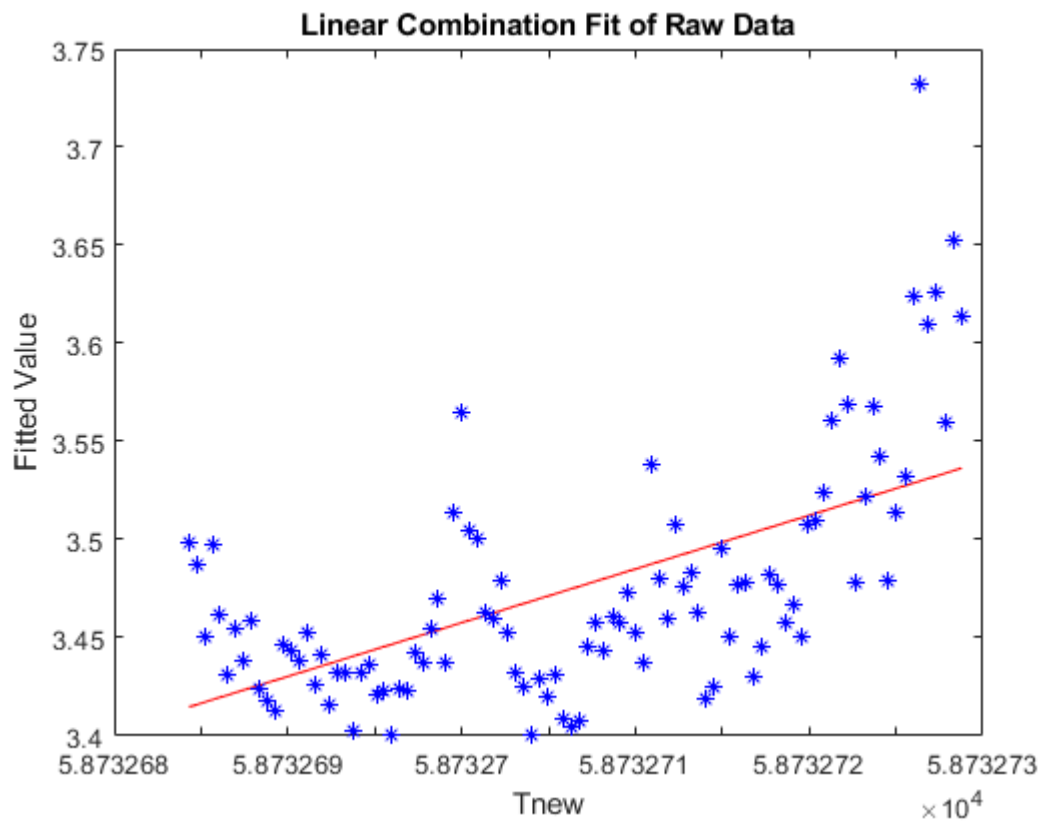
```
c = 3×1
1013 x
-0.000000016070897
0.000000000000894
3.724622381729035
```

```
%plot
```

```

yfit = c(1).*F1(Tnew) + c(2).*F2(Tnew) + c(3).*F3(Tnew) ;
plot(Tnew,yfit,'r',BD55_441(1:100,1),BD55_441(1:100,2),'*b')
title('Linear Combination Fit of Raw Data')
xlabel('Tnew')
ylabel('Fitted Value')

```



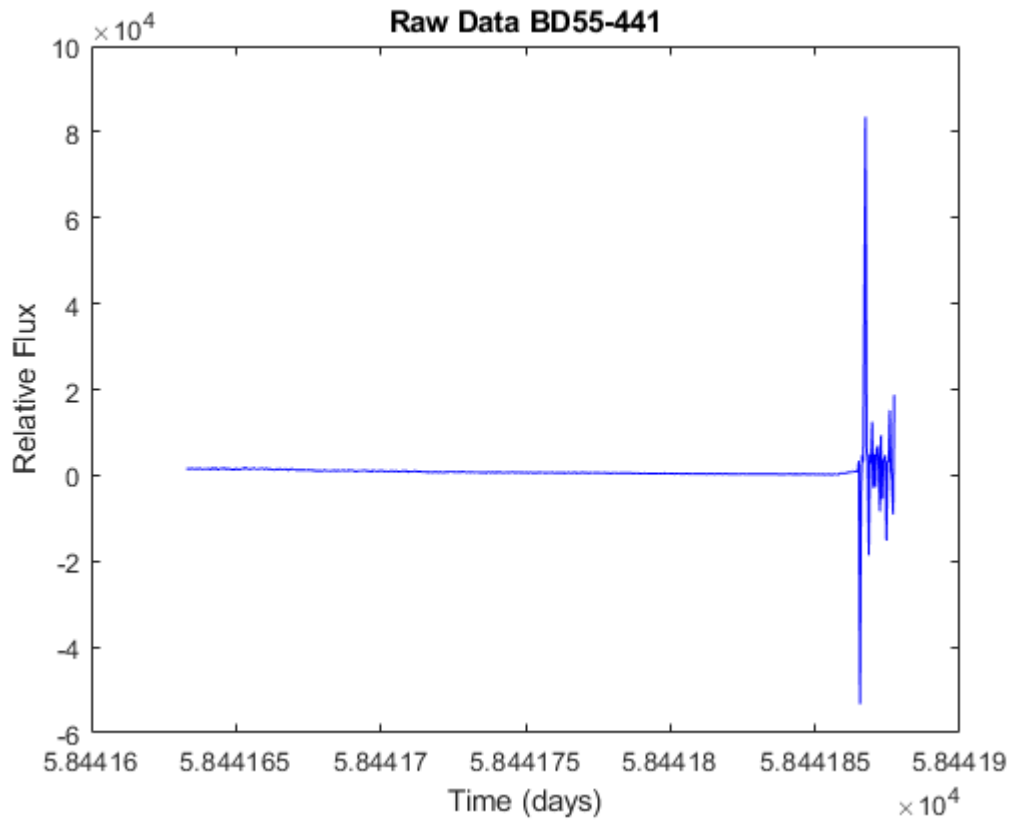
HD28497

Plot the raw data

```

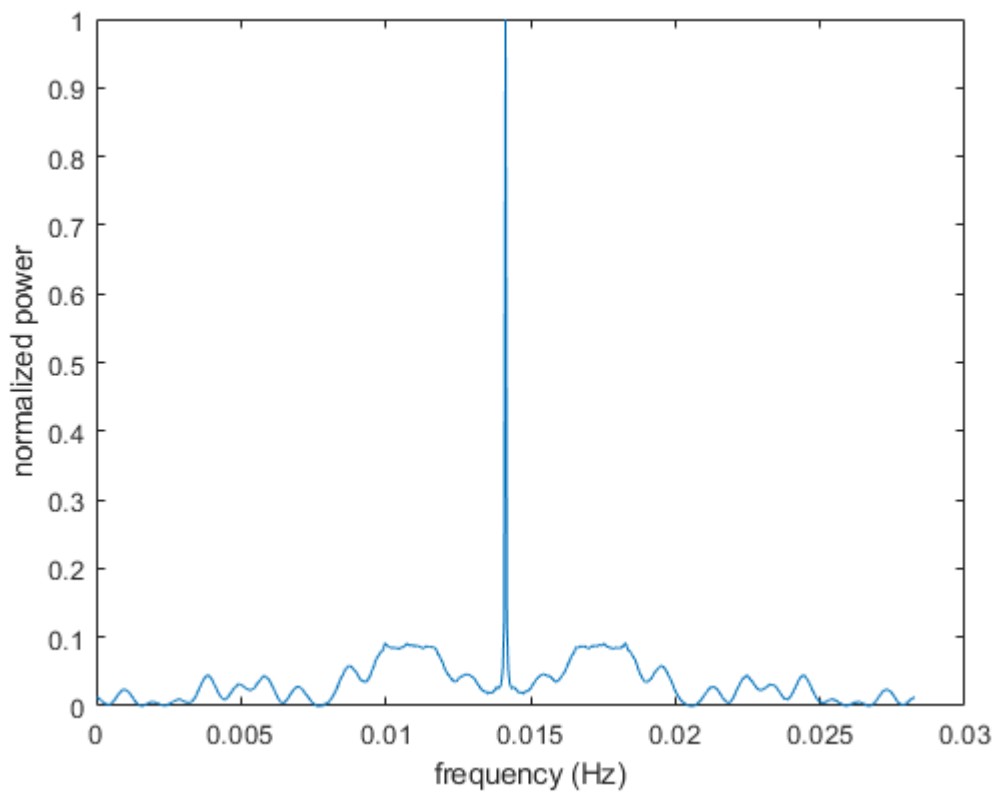
plot(HD28497(2:end,1),HD28497(2:end,2),'b');
title('Raw Data BD55-441');
xlabel('Time (days)');
ylabel('Relative Flux');

```



Use Linear Interpolation, then use a Fourier transform to attain the power spectrum

```
[Tnew,Mnew] = Interp_Lin(HD28497(2:end,1),HD28497(2:end,2));
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```

Functions for linear combination:

(main frequency at 0.0175 Hz or 1512 / day. use this for non-linear functions)

```
F1 = @(x) x./x;
F2 = @(x) cos(2*pi*(1512)).*(x);
F3 = @(x) sin(2*pi*(1512)).*(x);
```

```
%call the NLfit function
```

```
c = NLfit(F1,F2,F3,HD28497(2:end,1),HD28497(2:end,2))
```

```
Warning: Matrix is close to singular or badly scaled. Results may be inaccurate. RCOND = 1.465326e-41.
```

```
c = 3x1
1014 x
 0.000000417432818
-0.000000000006085
-7.488964229280974
```

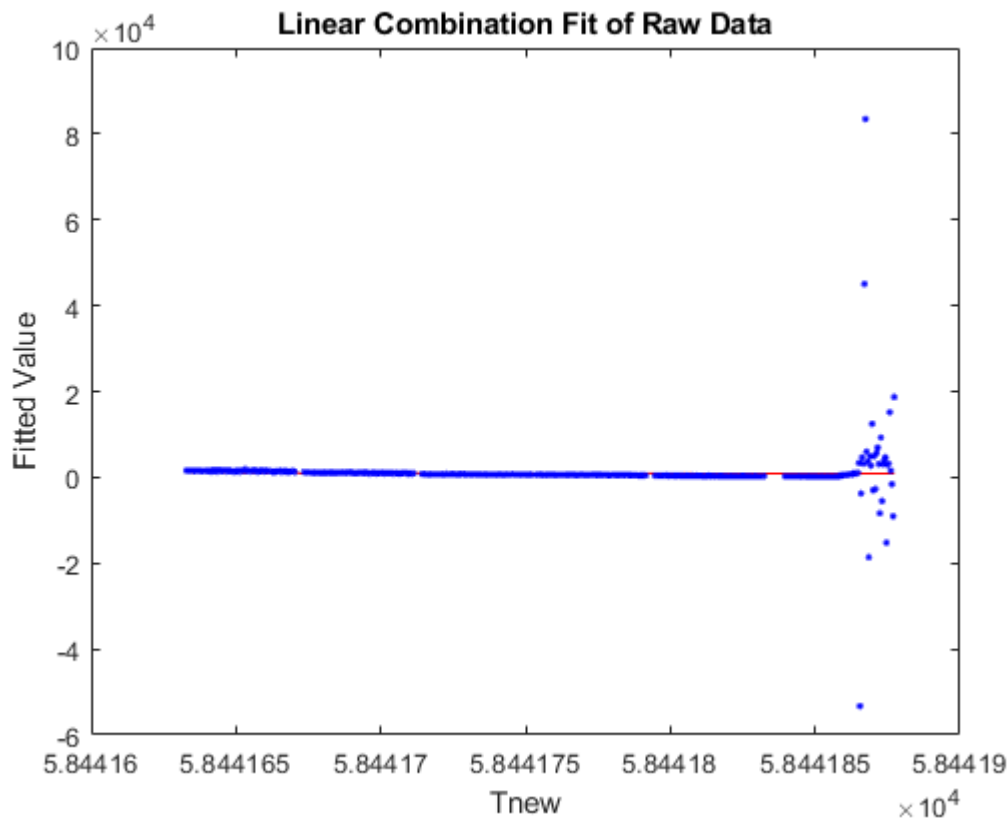
```
%plot
```

```
yfit = c(1).*F1(Tnew) + c(2).*F2(Tnew) + c(3).*F3(Tnew) ;
plot(Tnew,yfit, 'r',HD28497(2:end,1),HD28497(2:end,2), '.b')
```

```

title('Linear Combination Fit of Raw Data')
xlabel('Tnew')
ylabel('Fitted Value')

```



%This section should be run independently. This is a copy of what was
 %formerly titled Milestone 5v7

```

clearvars
format long

```

Research Techniques Project Just Milestone 5

Input all data

Text files:

```

opts = detectImportOptions("BD+55_441.txt");
opts.DataLines = 3;
opts.VariableNames = {'B_time', 'B_flux', 'R_time', 'R_flux', 'V_time', 'V_flux'};

```

"time" is in the units of days and "flux" is "rel_flux_T1" from AstrolmageJ outputs.

```
opts.VariableTypes = {'double','double','double','double','double','double'};
preview("BD+55_441.txt",opts)
```

ans = 8x6 table

	B_time	B_flux	R_time	R_flux	V_time	V_flux
1	5.873268430...	3.497996...	5.873268459...	1.961830...	5.873268445...	2.352058...
2	5.873268430...	3.497996...	5.873268504...	1.942857...	5.873268490...	2.360458...
3	5.873268475...	3.487289...	5.873268549...	1.947021...	5.873268535...	2.329957...
4	5.873268520...	3.450942...	5.873268594...	1.930594...	5.873268580...	2.344889...
5	5.873268565...	3.497567...	5.873268639...	1.942537...	5.873268625...	2.361048...
6	5.873268610...	3.461555...	5.873268684...	1.935141...	5.873268669...	2.333341...
7	5.873268655...	3.431248...	5.873268729...	1.931290...	5.873268714...	2.331904...
8	5.873268700...	3.455091...	5.873268774...	1.928260...	5.873268759...	2.323782...

```
BD55_441 = readmatrix("BD+55_441.txt",opts);
whos BD55_441
```

Name	Size	Bytes	Class	Attributes
BD55_441	101x6	4848	double	

```
%BD+48_1098
opts = detectImportOptions("BD+48_1098.txt");
opts.DataLines = 3;
opts.VariableNames = {'B_time','B_flux','R_time','R_flux','V_time','V_flux'};
opts.VariableTypes = {'double','double','double','double','double','double'};
BD48_1098 = rmmissing(readmatrix("BD+55_441.txt",opts)); %the matrix data of the text file
%preview("BD+48_1098.txt",opts)
whos BD48_1098
```

Name	Size	Bytes	Class	Attributes
BD48_1098	100x6	4800	double	

```
%HD28497
opts = detectImportOptions("HD28497.txt");
opts.DataLines = 3;
opts.VariableNames = {'B_time','B_flux','R_time','R_flux','V_time','V_flux'};
opts.VariableTypes = {'double','double','double','double','double','double'};
HD28497 = rmmissing(readmatrix("HD28497.txt",opts)) %the matrix data of the text file
```

HD28497 = 600x6

```
104 ×
5.844163256000000 0.151884039400000 5.844163279000000 0.047485834000000 ...
5.844163294000000 0.157713255000000 5.844163317000000 0.047850097100000
5.844163332000000 0.147648080800000 5.844163355000000 0.050717498800000
5.844163370000000 0.154105058200000 5.844163393000001 0.048745268800000
5.844163409000000 0.154416998300000 5.844163431999999 0.046480291500000
5.844163447000000 0.154034530100000 5.844163470000000 0.052878906200000
```

```

5.844163485000000    0.158524561400000    5.844163508000000    0.050080829500000
5.844163523000000    0.159731365000000    5.844163546000000    0.053844298900000
5.844163560999999    0.140623476800000    5.844163584000000    0.050871022200000
5.844163599000000    0.159835953000000    5.844163622000000    0.053311599500000
:

```

```

%preview("HD28497.txt",opts)
whos HD28497

```

Name	Size	Bytes	Class	Attributes
HD28497	600x6	28800	double	

```

%HD46131
opts = detectImportOptions("HD46131.txt");
opts.DataLines = 3;
opts.VariableNames = {'B_flux','B_time','R_time','R_flux','V_time','V_flux'};
opts.VariableTypes = {'double','double','double','double','double','double'};
HD46131 = rmmissing(readmatrix("HD46131.txt",opts)); %the matrix data of the text file
preview("HD46131.txt",opts)

```

ans = 8x6 table

	B_flux	B_time	R_time	R_flux	V_time	V_flux
1	80.30418...	5.844670852...	29.69434...	5.844670891...	43.24278...	5.844670875...
2	87.01571...	5.844670916...	29.50730...	5.844670956...	43.89599...	5.844670939...
3	86.15075...	5.844670981...	29.59417...	5.844671021...	43.11367...	5.844671004...
4	84.58512...	5.844671046...	29.01948...	5.844671085...	43.53672...	5.844671069...
5	82.72335...	5.844671111...	29.25732...	5.844671150...	44.34534...	5.844671134...
6	79.70069...	5.844671175...	30.09976...	5.844671215...	43.52612...	5.844671199...
7	84.42755...	5.844671240...	29.99023...	5.844671280...	42.63575...	5.844671263...
8	79.15342...	5.844671305...	29.78040...	5.844671344...	43.53322...	5.844671329...

```
whos HD46131
```

Name	Size	Bytes	Class	Attributes
HD46131	250x6	12000	double	

```

%HD88661
opts = detectImportOptions("HD88661.txt");
opts.DataLines = 3;
opts.VariableNames = {'B_time','B_flux','R_time','R_flux','V_time','V_flux'};
opts.VariableTypes = {'double','double','double','double','double','double'};
HD88661 = rmmissing(readmatrix("HD88661.txt",opts)); %the matrix data of the text file
%preview("HD88661.txt",opts)
whos HD88661

```

Name	Size	Bytes	Class	Attributes
HD88661	35x6	1680	double	

```
%HD105521
opts = detectImportOptions("HD105521.txt");
opts.DataLines = 3;
opts.VariableNames = {'B_time','B_flux','R_time','R_flux','V_time','V_flux'};
opts.VariableTypes = {'double','double','double','double','double','double'};
HD105521 = rmmissing(readmatrix("HD105521.txt",opts)); %the matrix data of the text file
%preview("HD105521.txt",opts)
whos HD105521
```

Name	Size	Bytes	Class	Attributes
HD105521	180x6	8640	double	

```
%HD105521
opts = detectImportOptions("HD105521.txt");
opts.DataLines = 3;
opts.VariableNames = {'B_time','B_flux','R_time','R_flux','V_time','V_flux'};
opts.VariableTypes = {'double','double','double','double','double','double'};
HD105521 = rmmissing(readmatrix("HD105521.txt",opts)); %the matrix data of the text file
%preview("HD105521.txt",opts)
whos HD105521
```

Name	Size	Bytes	Class	Attributes
HD105521	180x6	8640	double	

```
%KIC_11924311
opts = detectImportOptions("KIC_11924311_Photometry.txt");
opts.DataLines = 3;
%opts.VariableNames = {'B_time','B_flux','R_time','R_flux','V_time','V_flux'};
opts.VariableNames = {'Time','Filter','Flux','error'};
opts.VariableTypes = {'double','char','double','double'};
KIC_11924311 = rmmissing(readtable("KIC_11924311_Photometry.txt",opts)); %the matrix data of th
preview("KIC_11924311_Photometry.txt",opts)
```

ans = 8x4 table

	Time	Filter	Flux	error
1	5.79853734...	'B'	0.68590...	0.00300...
2	5.79853742...	'B'	0.68147...	0.00299...
3	5.79853758...	'B'	0.69522...	0.00301...
4	5.79853766...	'B'	0.69789...	0.00303...
5	5.79853775...	'B'	0.69234...	0.00300...
6	5.79853783...	'B'	0.70016...	0.00303...
7	5.79853791...	'B'	0.69389...	0.00299...
8	5.79853799...	'B'	0.70966...	0.00305...

```
filters = unique(KIC_11924311{:,2},'stable');
poscount = [1 0 0 0 0];
[n,~] = size(KIC_11924311);
KIC_11924311temp = table;
l = {0};
```

```

for count=1:4
    poscount(count+1)=poscount(count);
    while (char(filters(count))==char(KIC_11924311{poscount(count+1),2}) && poscount(count+1)<=
        poscount(count+1) = poscount(count+1) + 1;
    end
    KIC = KIC_11924311(poscount(count):poscount(count+1)-1,:);
    KIC = KIC(1:348,:);
    KIC_11924311temp.J_D__2400000 = KIC.Time;
    KIC_11924311temp.rel_flux_T1 = KIC.Flux;
    l{2*count-1} = sprintf('%s_time', char(filters(count)));
    l{2*count} = sprintf('%s_flux', char(filters(count)));
    KIC_11924311temp.Properties.VariableNames = l;
end

```

KIC = 348×4 table

	Time	Filter	Flux	error
1	5.79853734...	'B'	0.68590...	0.00300...
2	5.79853742...	'B'	0.68147...	0.00299...
3	5.79853758...	'B'	0.69522...	0.00301...
4	5.79853766...	'B'	0.69789...	0.00303...
5	5.79853775...	'B'	0.69234...	0.00300...
6	5.79853783...	'B'	0.70016...	0.00303...
7	5.79853791...	'B'	0.69389...	0.00299...
8	5.79853799...	'B'	0.70966...	0.00305...
9	5.79853807...	'B'	0.70262...	0.00302...
10	5.79853815...	'B'	0.70943...	0.00305...
11	5.79853823...	'B'	0.71280...	0.00305...
12	5.79853831...	'B'	0.71538...	0.00306...
13	5.79853840...	'B'	0.71921...	0.00314...
14	5.79853848...	'B'	0.72563...	0.00327...
⋮				

KIC = 350×4 table

	Time	Filter	Flux	error
1	5.79853728...	'V'	0.72607...	0.00284...
2	5.79853736...	'V'	0.72676...	0.00284...
3	5.79853744...	'V'	0.72876...	0.00283...
4	5.79853752...	'V'	0.73102...	0.00284...
5	5.79853760...	'V'	0.73476...	0.00285...
6	5.79853769...	'V'	0.74009...	0.00287...
7	5.79853777...	'V'	0.74062...	0.00285...
8	5.79853785...	'V'	0.74477...	0.00287...

	Time	Filter	Flux	error
9	5.79853793...	'V'	0.74259...	0.00285...
10	5.79853801...	'V'	0.74713...	0.00287...
11	5.79853809...	'V'	0.74955...	0.00288...
12	5.79853817...	'V'	0.75450...	0.00289...
13	5.79853826...	'V'	0.76023...	0.00291...
14	5.79853834...	'V'	0.76027...	0.00292...

⋮

KIC = 350×4 table

	Time	Filter	Flux	error
1	5.79853729...	'R'	0.74284...	0.00304...
2	5.79853737...	'R'	0.74455...	0.00306...
3	5.79853746...	'R'	0.75454...	0.00309...
4	5.79853754...	'R'	0.75485...	0.00307...
5	5.79853762...	'R'	0.75807...	0.00307...
6	5.79853770...	'R'	0.76211...	0.00308...
7	5.79853778...	'R'	0.76860...	0.00311...
8	5.79853787...	'R'	0.77020...	0.00313...
9	5.79853795...	'R'	0.76533...	0.00309...
10	5.79853803...	'R'	0.76891...	0.00309...
11	5.79853811...	'R'	0.76780...	0.00309...
12	5.79853819...	'R'	0.77622...	0.00313...
13	5.79853827...	'R'	0.78118...	0.00314...
14	5.79853835...	'R'	0.78604...	0.00316...

⋮

KIC = 350×4 table

	Time	Filter	Flux	error
1	5.79853731...	'I'	0.76493...	0.00514...
2	5.79853739...	'I'	0.78074...	0.00526...
3	5.79853747...	'I'	0.77509...	0.00512...
4	5.79853755...	'I'	0.77435...	0.00518...
5	5.79853763...	'I'	0.78233...	0.00519...
6	5.79853772...	'I'	0.78959...	0.00518...
7	5.79853780...	'I'	0.78702...	0.00513...
8	5.79853788...	'I'	0.78799...	0.00519...

	Time	Filter	Flux	error
9	5.79853796...	'I'	0.79257...	0.00515...
10	5.79853805...	'I'	0.79262...	0.00514...
11	5.79853813...	'I'	0.79891...	0.00518...
12	5.79853821...	'I'	0.80309...	0.00517...
13	5.79853829...	'I'	0.81053...	0.00517...
14	5.79853837...	'I'	0.80186...	0.00522...

⋮

poscount

```
poscount = 1×5
          1          349          699          1049          1399
```

```
KIC_11924311 = KIC_11924311temp;
whos KIC_11924311
```

Name	Size	Bytes	Class	Attributes
KIC_11924311	348x8	24799	table	

CSV files

```
%HD106306
%B_filter
opts = detectImportOptions('HD106306_B.csv');
opts.DataLines = [2 Inf];
All_fields_available = opts.VariableNames;
opts.SelectedVariableNames = {'J_D_2400000','rel_flux_T1'};
%preview("HD106306_B.csv",opts)
HD106306_B = readmatrix("HD106306_B.csv",opts);

%R_filter
opts = detectImportOptions('HD106306_R.csv');
opts.DataLines = [2 Inf];
All_fields_available = opts.VariableNames;
opts.SelectedVariableNames = {'J_D_2400000','rel_flux_T1'};
%preview("HD106306_R.csv",opts)
HD106306_R = readmatrix("HD106306_R.csv",opts);

%V_filter
opts = detectImportOptions('HD106306_V.csv');
opts.DataLines = [2 Inf];
All_fields_available = opts.VariableNames;
opts.SelectedVariableNames = {'J_D_2400000','rel_flux_T1'};
%preview("HD106306_V.csv",opts)
HD106306_V = readmatrix("HD106306_V.csv",opts);

HD106306 = rmmissing([HD106306_B HD106306_R HD106306_V]); %the matrix data of the text file
whos HD106306
```


Name	Size	Bytes	Class	Attributes
HD106306	100x6	4800	double	

```
%HD147302
%B_filter
opts = detectImportOptions('HD147302_B.csv');
opts.DataLines = [2 Inf];
All_fields_available = opts.VariableNames;
opts.SelectedVariableNames = {'J_D__2400000','rel_flux_T1'};
%preview("HD147302_B.csv",opts)
HD147302_B = readmatrix("HD147302_B.csv",opts);

%R_filter
opts = detectImportOptions('HD147302_R.csv');
opts.DataLines = [2 Inf];
All_fields_available = opts.VariableNames;
opts.SelectedVariableNames = {'J_D__2400000','rel_flux_T1'};
%preview("HD147302_R.csv",opts)
HD147302_R = readmatrix("HD147302_R.csv",opts);

%V_filter
opts = detectImportOptions('HD147302_V.csv');
opts.DataLines = [2 Inf];
All_fields_available = opts.VariableNames;
opts.SelectedVariableNames = {'J_D__2400000','rel_flux_T1'};
%preview("HD147302_V.csv",opts)
HD147302_V = readmatrix("HD147302_V.csv",opts);

HD147302 = rmmissing([HD147302_B HD147302_R HD147302_V]); %the matrix data of the text file
whos HD147302
```

Name	Size	Bytes	Class	Attributes
HD147302	100x6	4800	double	

HD152060 and HD209522 can't be described in the same form as the others. Will investigate

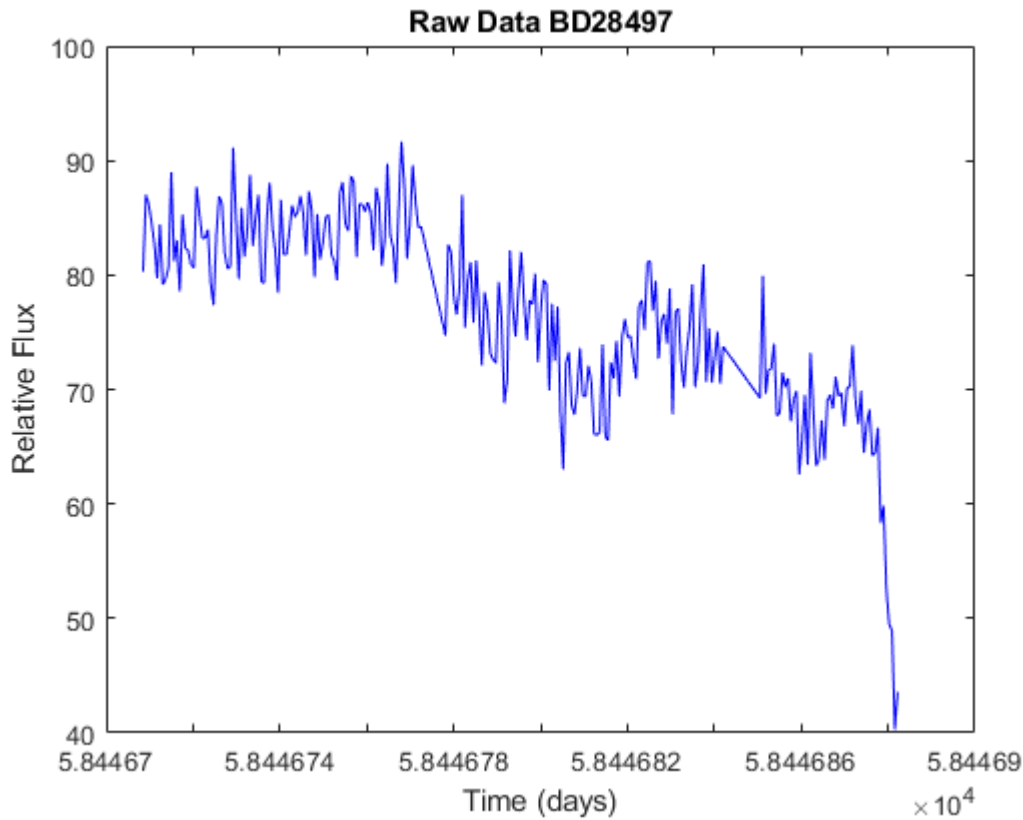
```
close all %closes all previous figures from milestone 1 so that the plots in milestone 2 and
```

HD46131

Plot the raw data

```
plot(HD46131(:,2),HD46131(:,1),'b');
title('Raw Data BD28497');
```

```
xlabel('Time (days)');
ylabel('Relative Flux');
```



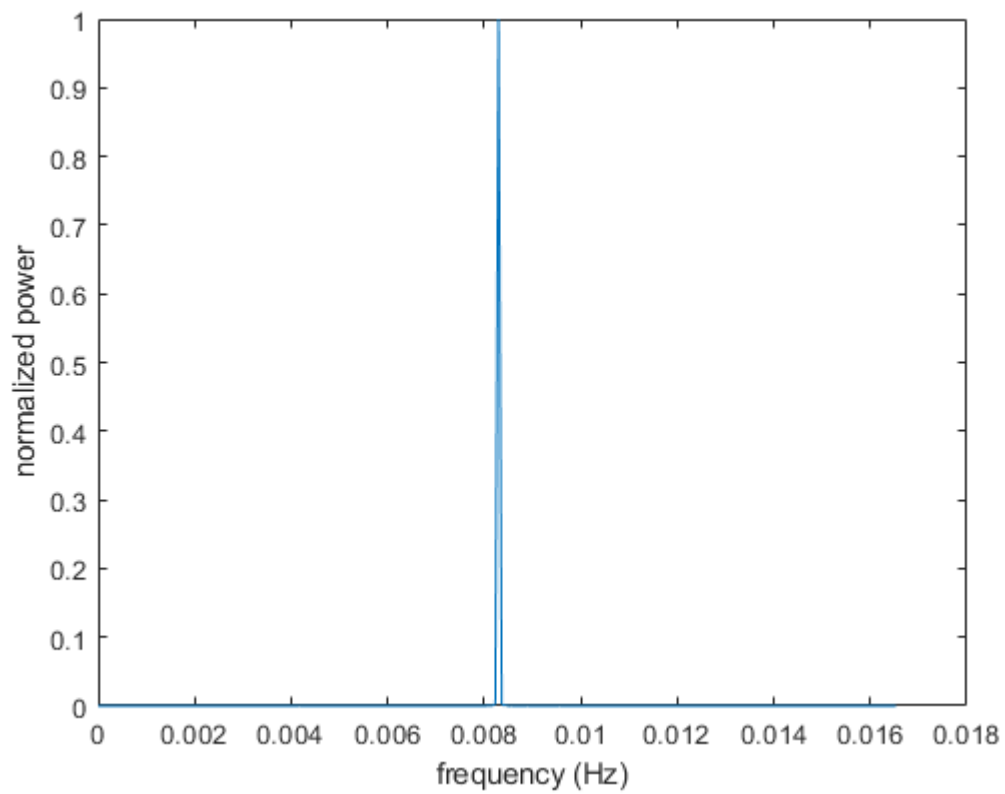
```
avg_freq = 1/( mean( diff(HD46131(:,2)) ) * 86400 )
```

%Dr. Rioussset showed us how to use

```
avg_freq =
    0.016592460385689
```

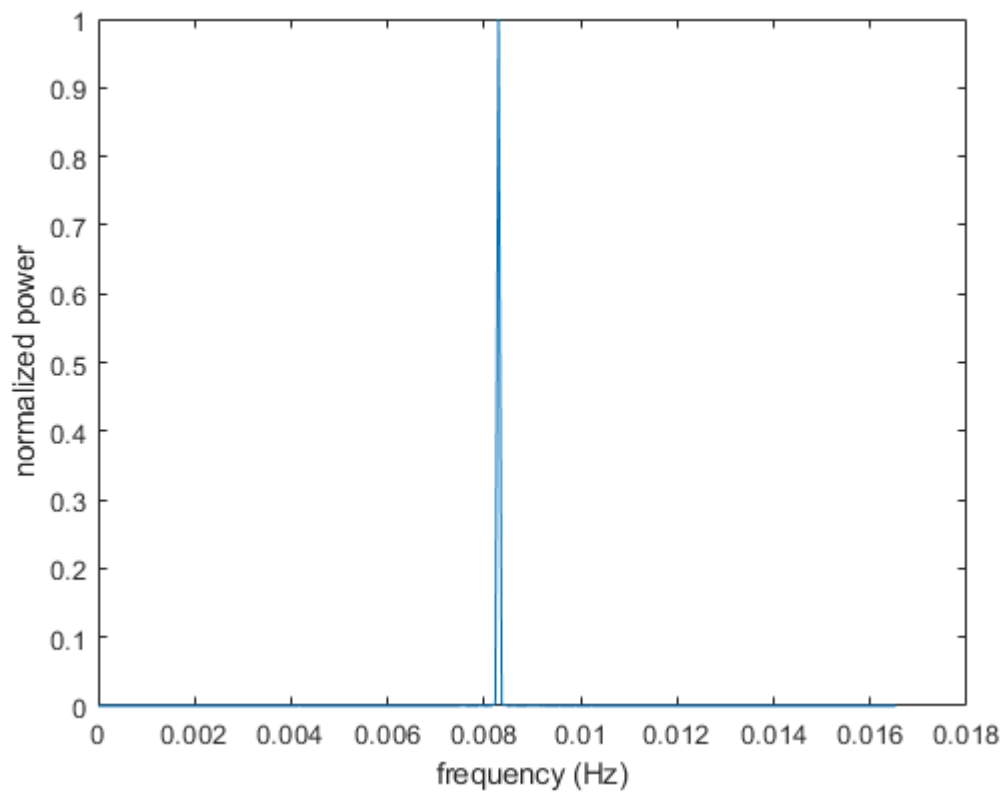
Use Linear Interpolation, then use a Fourier transform to attain the power spectrum

```
[Tnew,Mnew] = Interp_Lin(HD46131(:,2),HD46131(:,1));
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```



Use Spline Interpolation, then use a Fourier transform to attain the power spectrum

```
[Tnew,Mnew] = Interp_spline(HD46131(:,2),HD46131(:,1));  
Tnews = Tnew*86400; %convert time from days to seconds  
dt = Tnews(2) - Tnews(1);  
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```



Try non-uniform built in function "nufft"

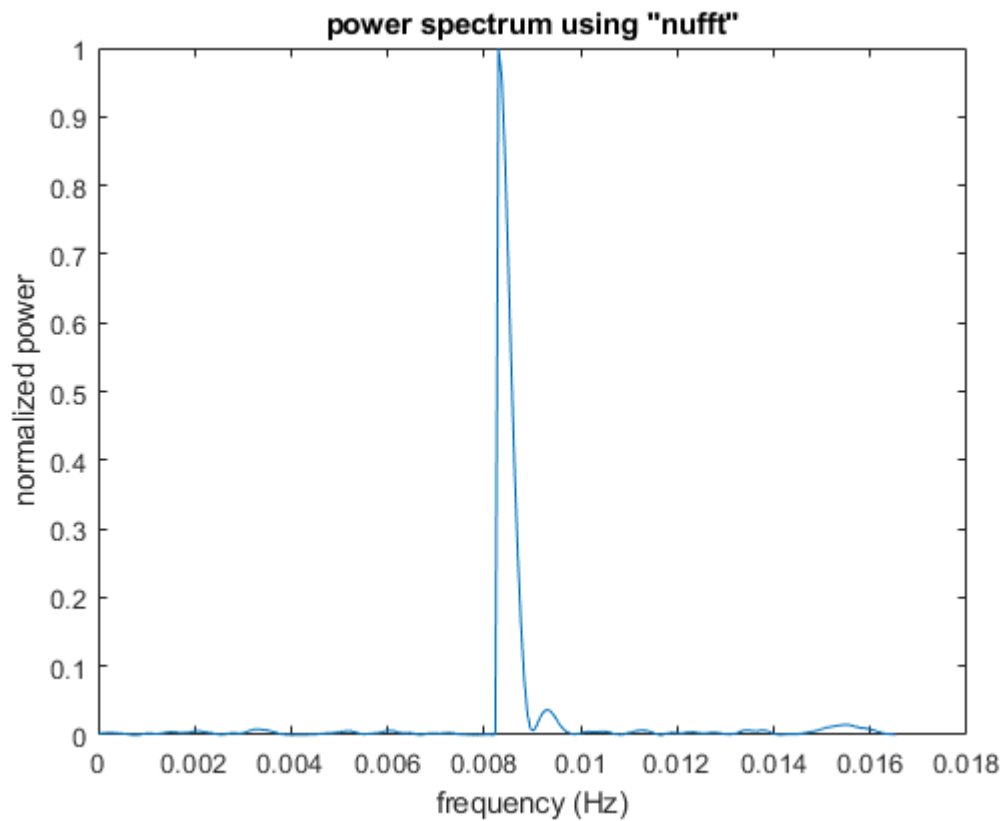
```
N = length(HD46131(:,2));
F = nufft( HD46131(:,2),HD46131(:,1) )/N;
F0 = fftshift(F);

power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')
```



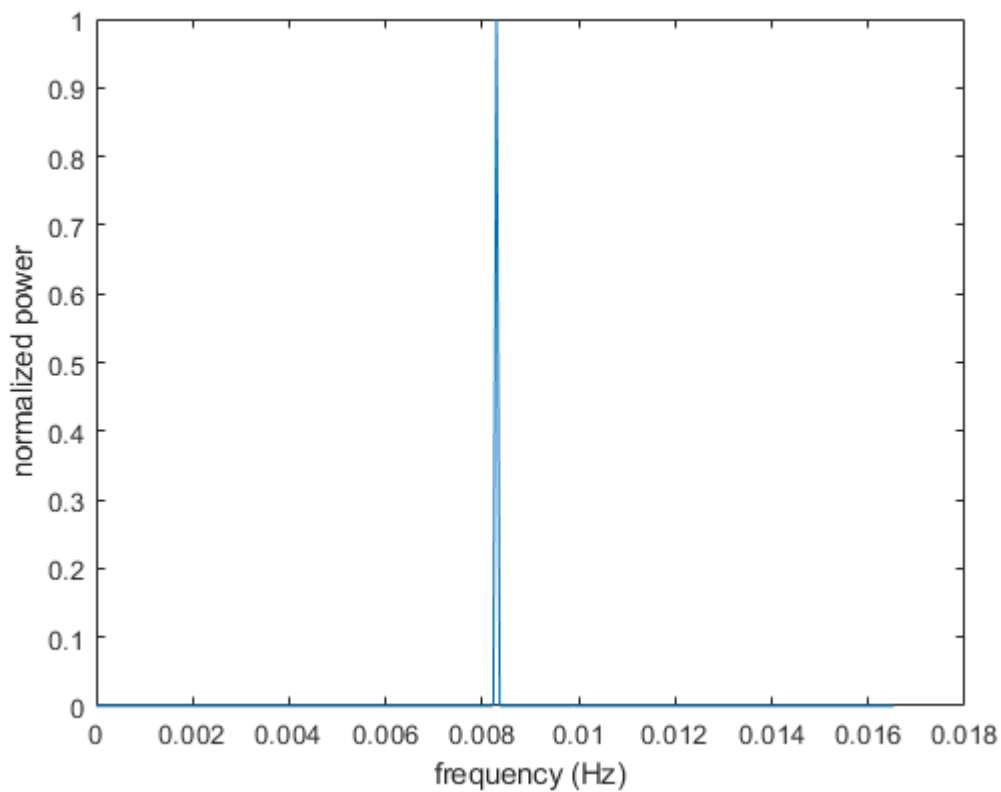
```
key_freq = 0.008296;
avg_freq = 1/( mean( diff(HD46131(:,2)) ) *86400 )
```

```
avg_freq =
    0.016592460385689
```

```
avg_freq/key_freq
```

```
ans =
    2.000055494899830
```

```
%R
[Tnew,Mnew] = Interp_spline(HD46131(:,4),HD46131(:,3));
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```



```

avg_freq = 1/( mean( diff(HD46131(:,4)) ) *86400 );
N = length(HD46131(:,4));
F = nufft( HD46131(:,4),HD46131(:,3) )/N;
F0 = fftshift(F);

power = F0.*conj(F0)/N;
N = length(HD46131(:,4));
F = nufft( HD46131(:,4),HD46131(:,3) )/N;
F0 = fftshift(F);

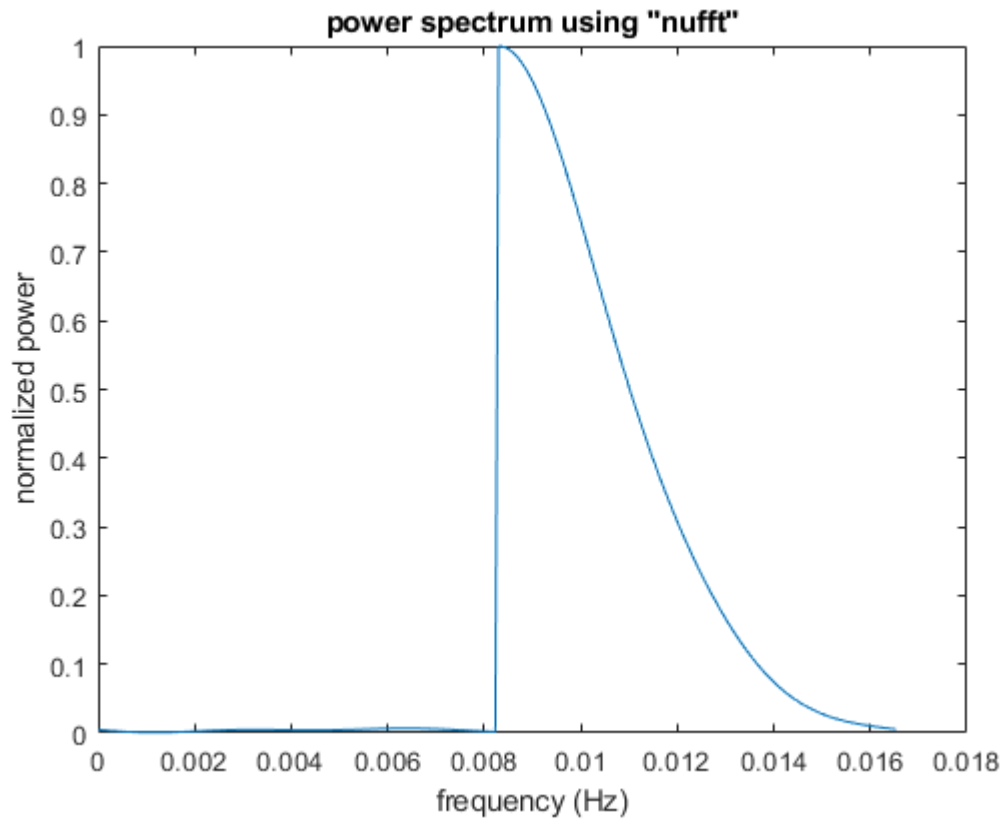
power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')

```



```
key_freq = 0.00829623;
avg_freq = 1/( mean( diff(HD46131(:,4)) ) *86400 )
```

```
avg_freq =
    0.016592460386384
```

```
avg_freq/key_freq
```

```
ans =
    2.000000046573450
```

```
powerNor = power/max(power);
```

```
%Plot power Spectrum
```

```
fs = avg_freq;
```

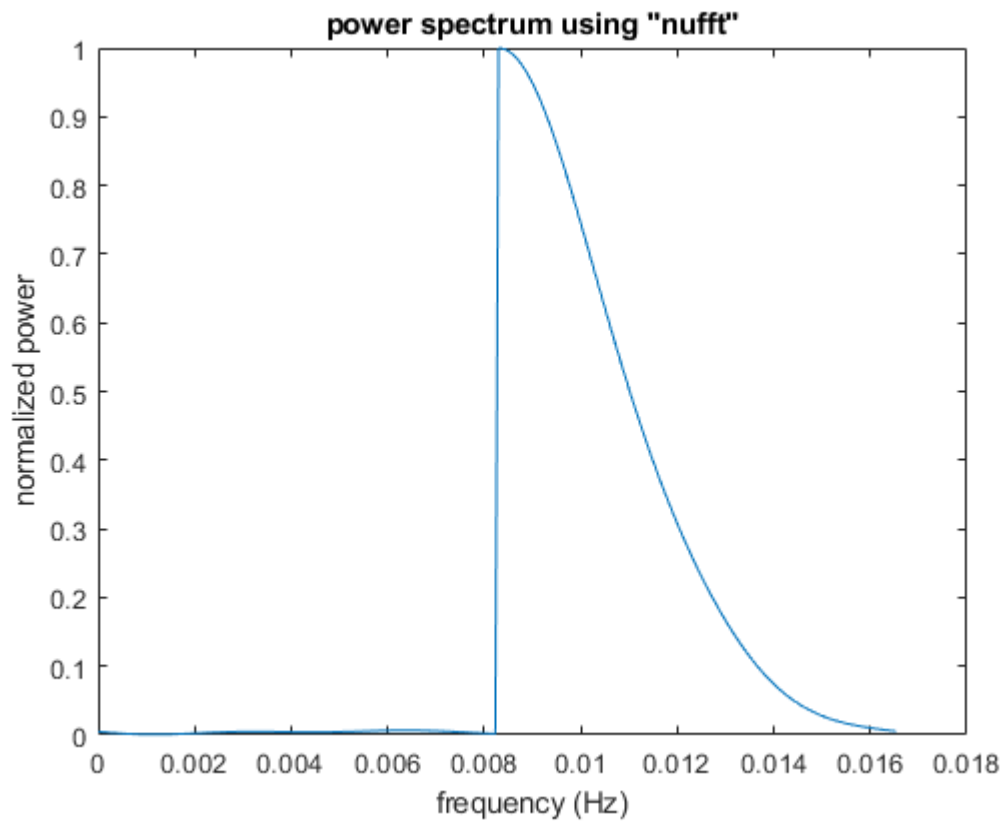
```
fk = (0:N-1)*(fs/N);
```

```
plot(fk, powerNor)
```

```
xlabel('frequency (Hz)')
```

```
ylabel('normalized power')
```

```
title('power spectrum using "nufft"')
```



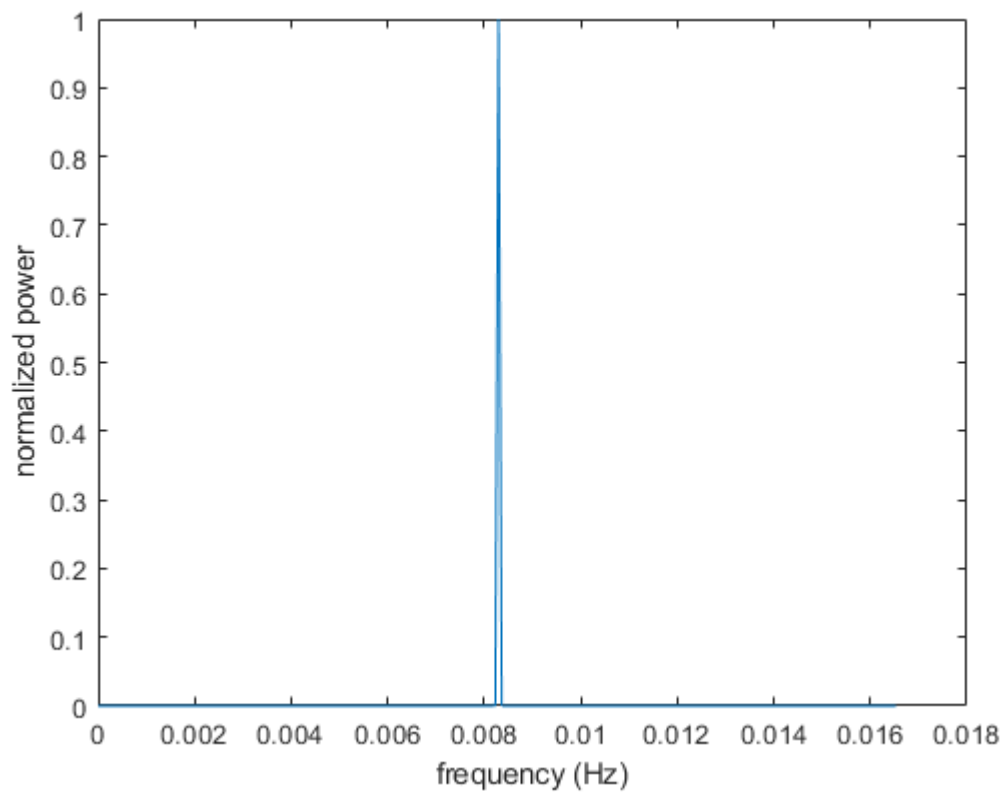
```
key_freq = 0.008296;
avg_freq = 1/( mean( diff(HD46131(:,4)) ) *86400 )
```

```
avg_freq =
    0.016592460386384
```

```
avg_freq/key_freq
```

```
ans =
    2.000055494983613
```

```
%v
[Tnew,Mnew] = Interp_spline(HD46131(:,6),HD46131(:,5));
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```

```

avg_freq =1/( mean( diff(HD46131(:,6)) ) *86400 );
N = length(HD46131(:,6));
F = nufft( HD46131(:,6),HD46131(:,5) )/N;
F0 = fftshift(F);

power = F0.*conj(F0)/N;
N = length(HD46131(:,6));
F = nufft( HD46131(:,6),HD46131(:,5) )/N;
F0 = fftshift(F);

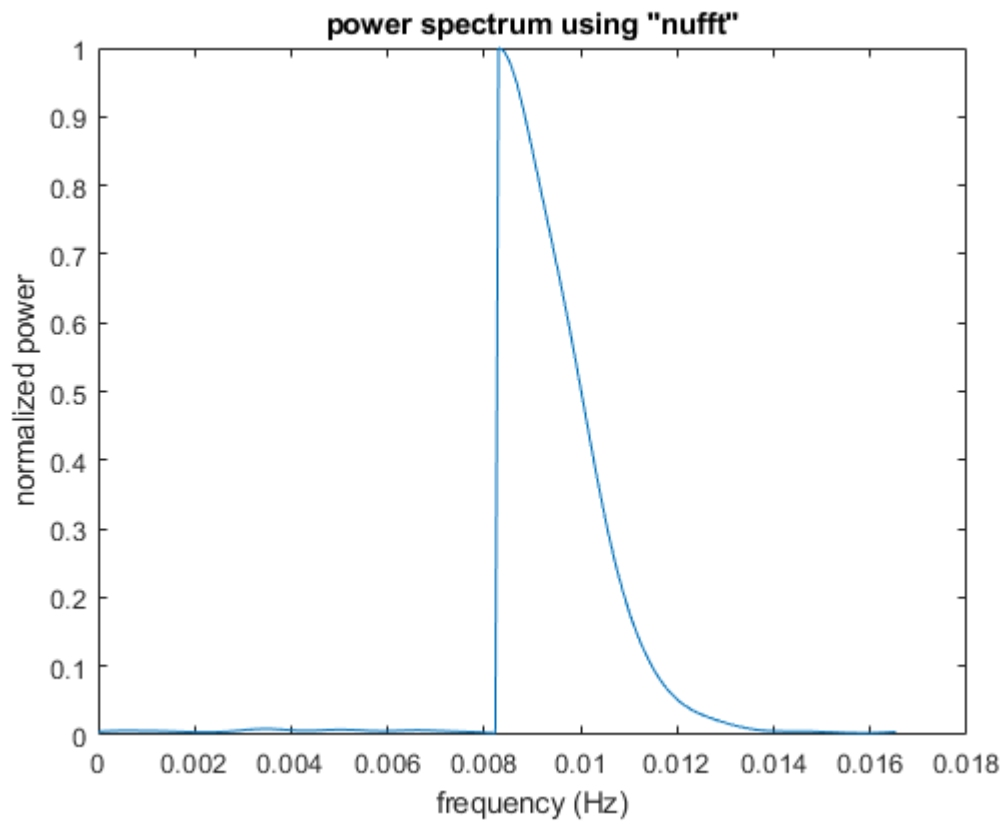
power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')

```



```
key_freq = 0.00829623;
avg_freq = 1/( mean( diff(HD46131(:,6)) ) *86400 )
```

```
avg_freq =
    0.016592460385689
```

```
avg_freq/key_freq
```

```
ans =
    2.000000046489669
```

```
powerNor = power/max(power);
```

```
%Plot power Spectrum
```

```
fs = avg_freq;
```

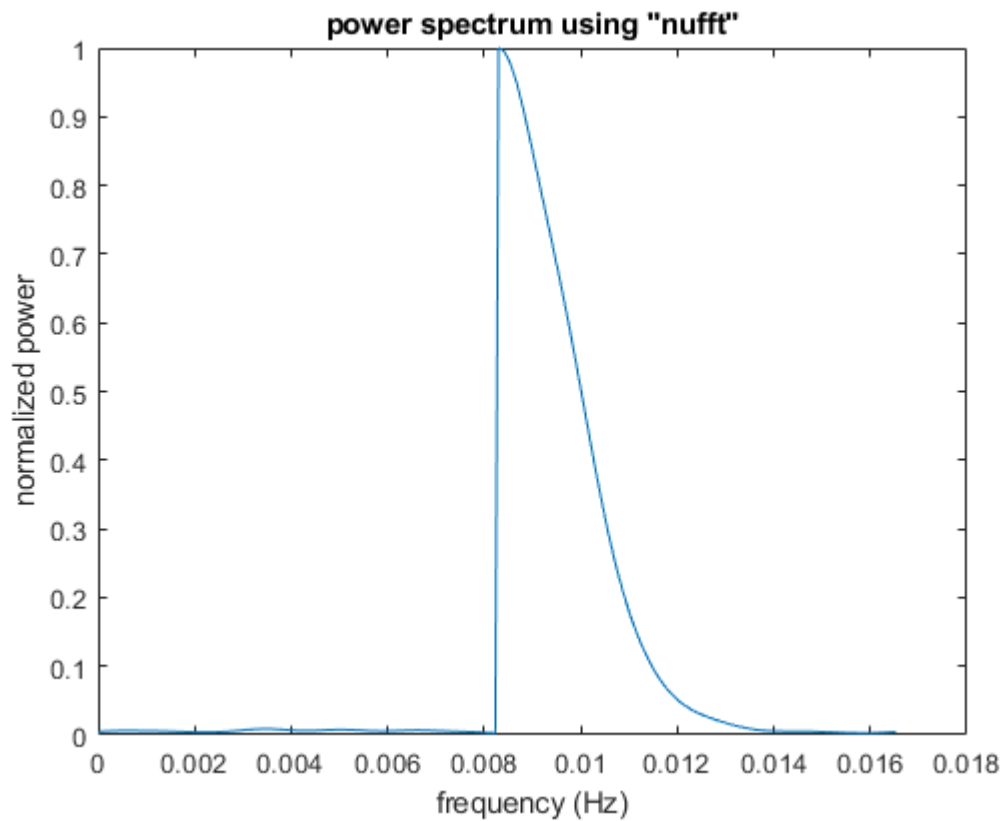
```
fk = (0:N-1)*(fs/N);
```

```
plot(fk, powerNor)
```

```
xlabel('frequency (Hz)')
```

```
ylabel('normalized power')
```

```
title('power spectrum using "nufft"')
```



```
key_freq = 0.008296;
avg_freq = 1/( mean( diff(HD46131(:,4)) ) *86400 )
```

```
avg_freq =
    0.016592460386384
```

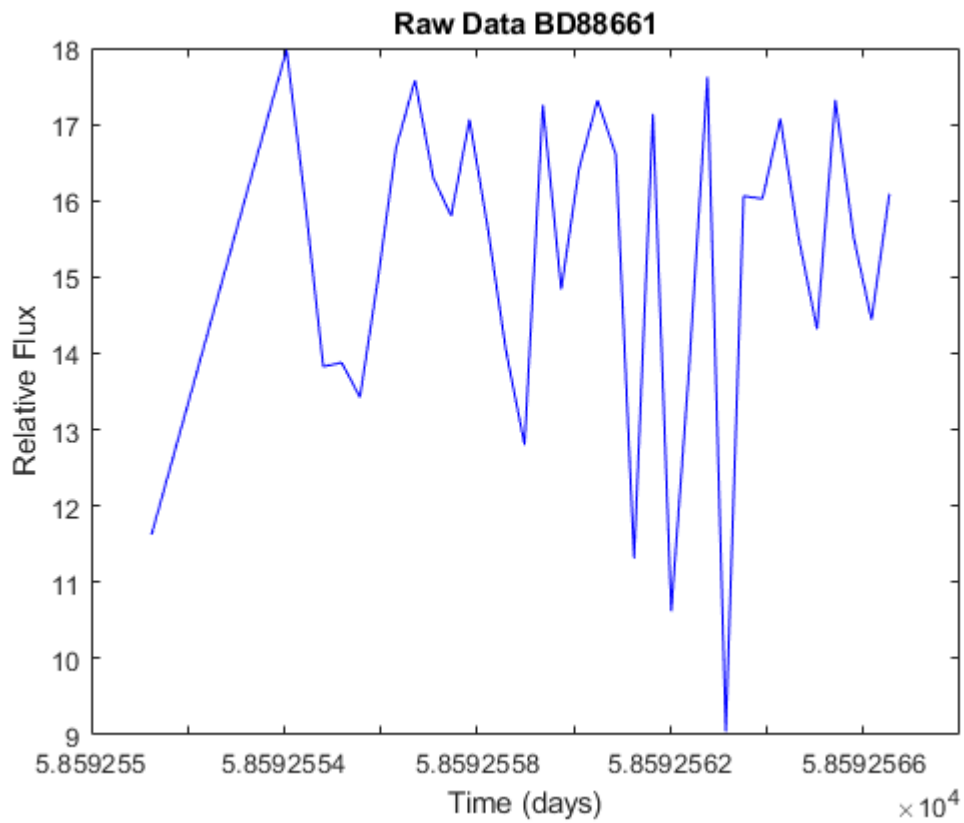
```
avg_freq/key_freq
```

```
ans =
    2.000055494983613
```

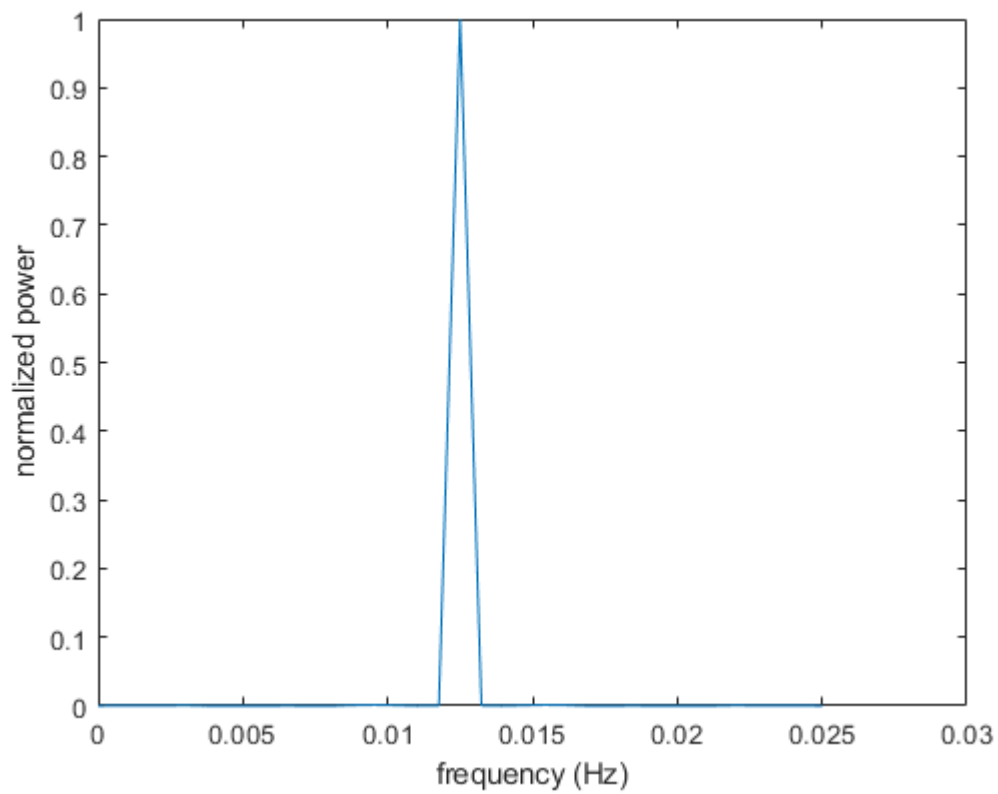
HD88661

Plot the raw data

```
plot(HD88661(:,2),HD88661(:,1),'b');
title('Raw Data BD88661');
xlabel('Time (days)');
ylabel('Relative Flux');
```

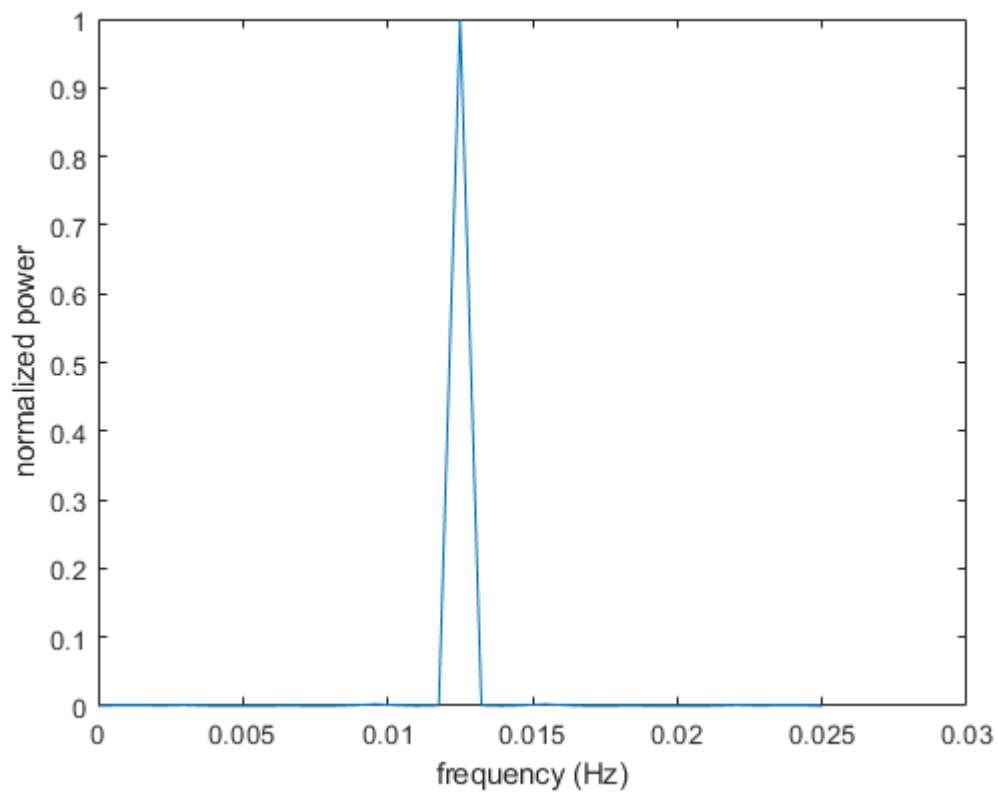


```
%B
avg_freq = 1/( mean( diff(HD88661(:,2)) ) * 86400 );
[Tnew,Mnew] = Interp_Lin(HD88661(:,2),HD88661(:,1));
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```



Use Spline Interpolation, then use a Fourier transform to attain the power spectrum

```
[Tnew,Mnew] = Interp_spline(HD88661(:,2),HD88661(:,1));  
Tnews = Tnew*86400; %convert time from days to seconds  
dt = Tnews(2) - Tnews(1);  
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```



Try non-uniform built in function "nufft"

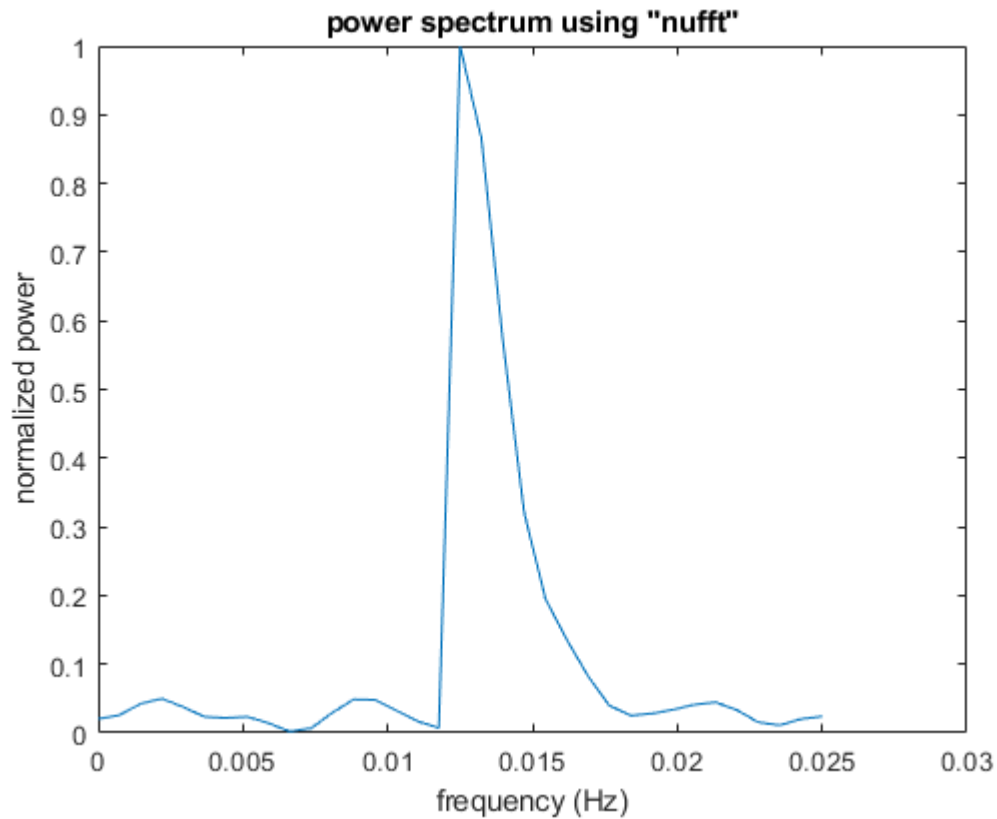
```
N = length(HD88661(:,2));
F = nufft( HD88661(:,2),HD88661(:,1) )/N;
F0 = fftshift(F);

power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')
```



```
key_freq = 0.0125008
```

```
key_freq =  
0.0125008000000000
```

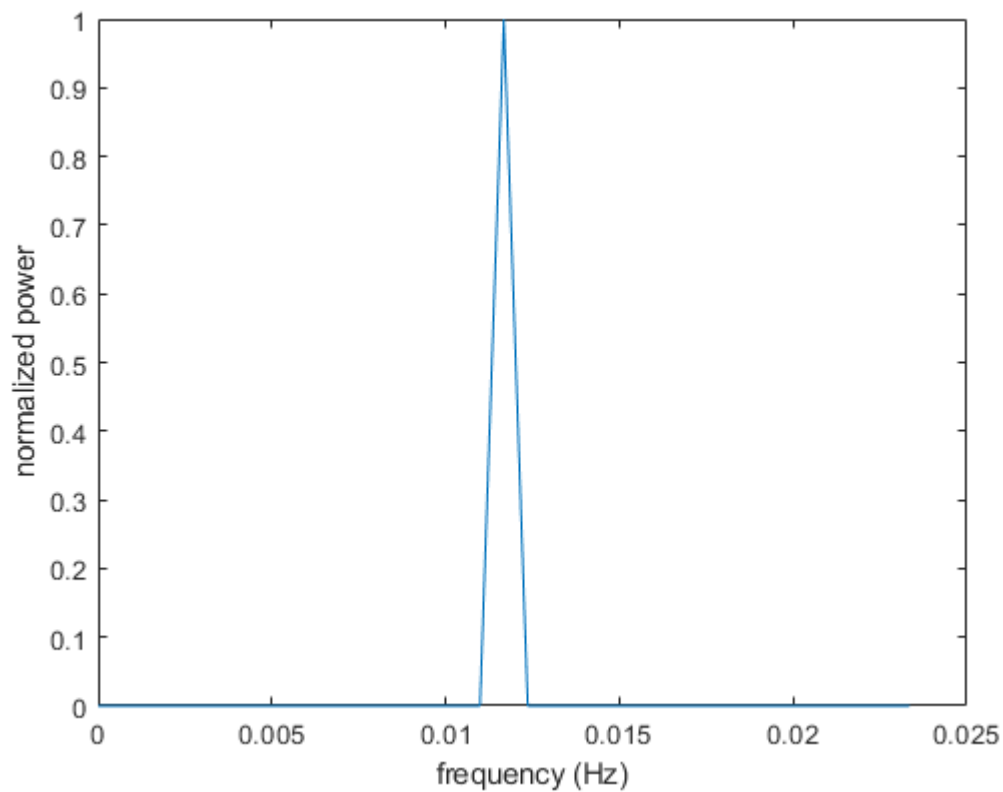
```
avg_freq =1/( mean( diff(HD88661(:,2)) ) *86400 )
```

```
avg_freq =  
0.025736986163581
```

```
avg_freq/key_freq
```

```
ans =  
2.058827128150297
```

```
%R  
avg_freq =1/( mean( diff(HD88661(:,4)) ) *86400 );  
[Tnew,Mnew] = Interp_Lin(HD88661(:,4),HD88661(:,3));  
Tnews = Tnew*86400; %convert time from days to seconds  
dt = Tnews(2) - Tnews(1);  
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```



```

N = length(HD88661(:,4));
F = nufft( HD88661(:,4),HD88661(:,3) )/N;
F0 = fftshift(F);

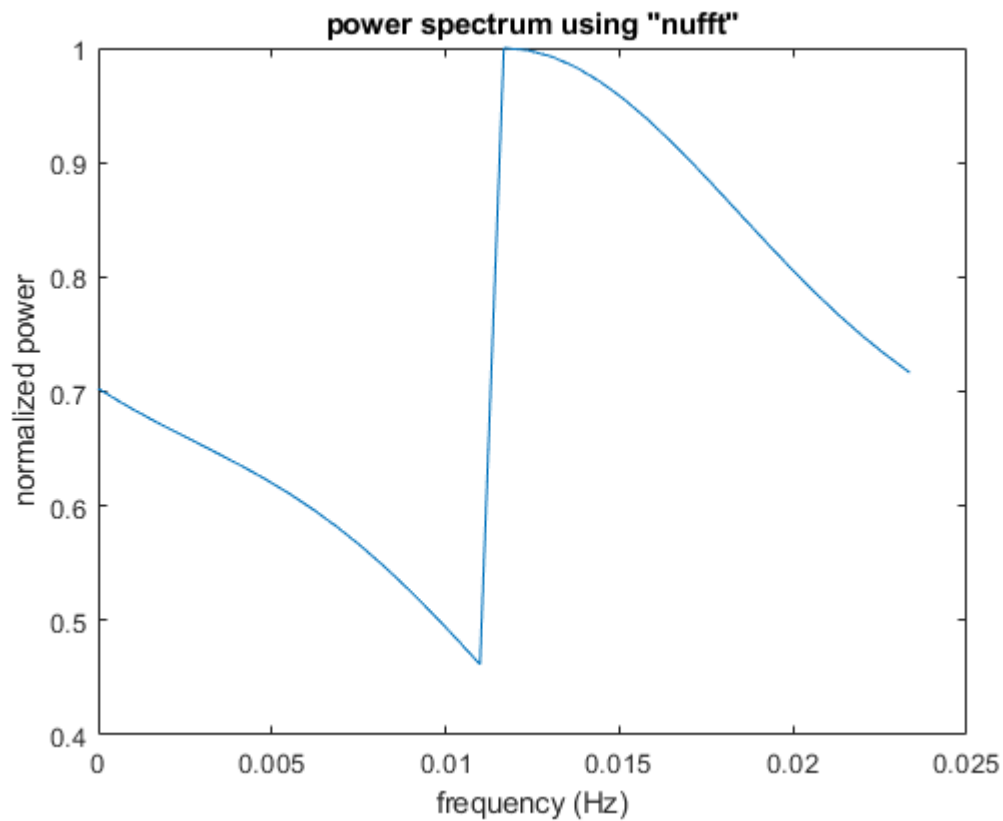
power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')

```

```
key_freq = 0.0116761
```

```
key_freq =  
0.011676100000000
```

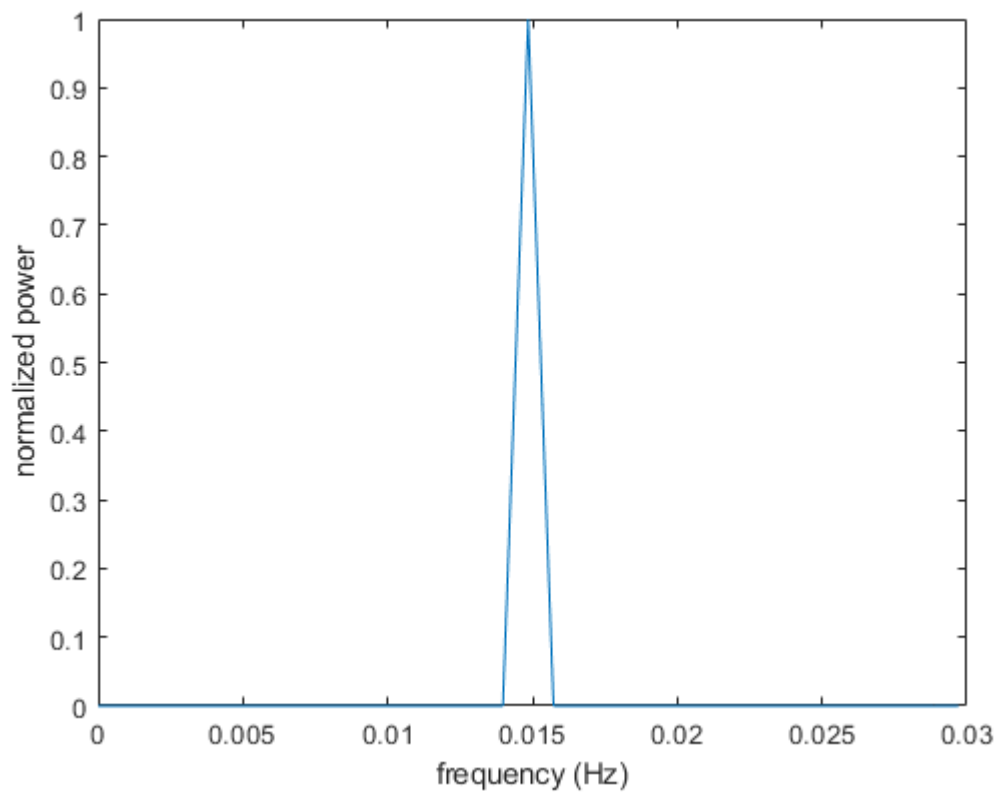
```
avg_freq =1/( mean( diff(HD88661(:,4)) ) *86400 )
```

```
avg_freq =  
0.024039005400274
```

```
avg_freq/key_freq
```

```
ans =  
2.058821472946825
```

```
%V  
avg_freq =1/( mean( diff(HD88661(:,6)) ) *86400 );  
[Tnew,Mnew] = Interp_Lin(HD88661(:,6),HD88661(:,5));  
Tnews = Tnew*86400; %convert time from days to seconds  
dt = Tnews(2) - Tnews(1);  
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```



```

N = length(HD88661(:,6));
F = nufft( HD88661(:,6),HD88661(:,5) )/N;
F0 = fftshift(F);

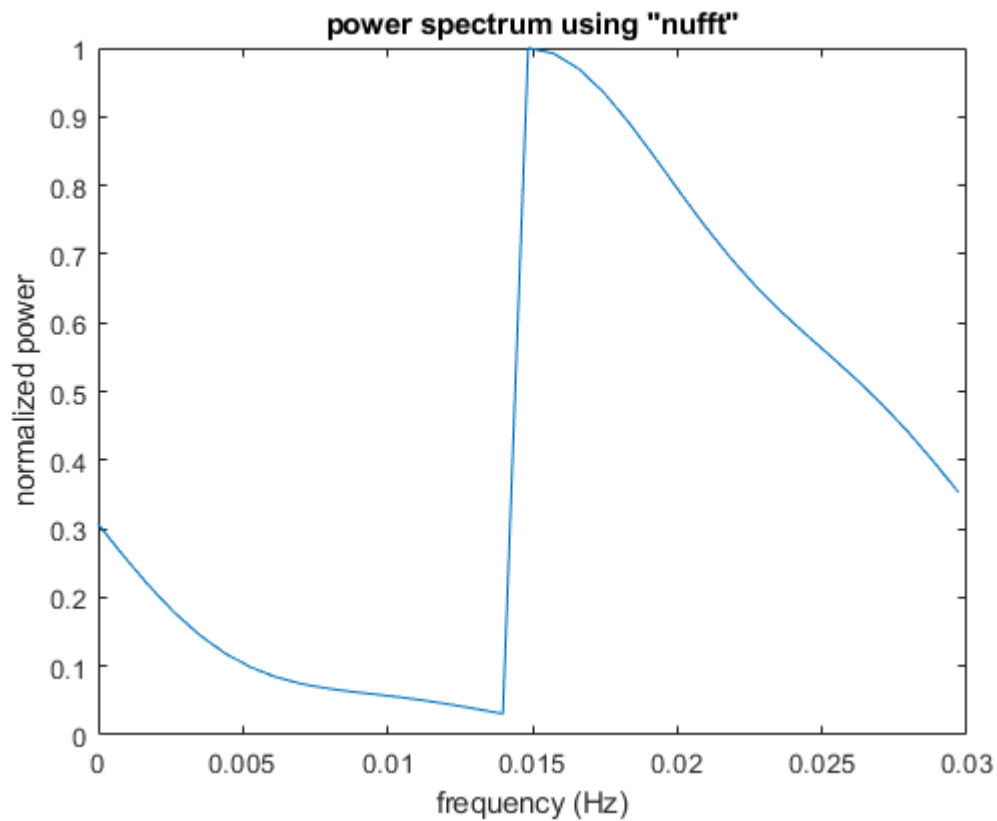
power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')

```



```
key_freq = 0.0148514;
avg_freq = 1/( mean( diff(HD88661(:,6)) ) *86400 )
```

```
avg_freq =
    0.030576419468500
```

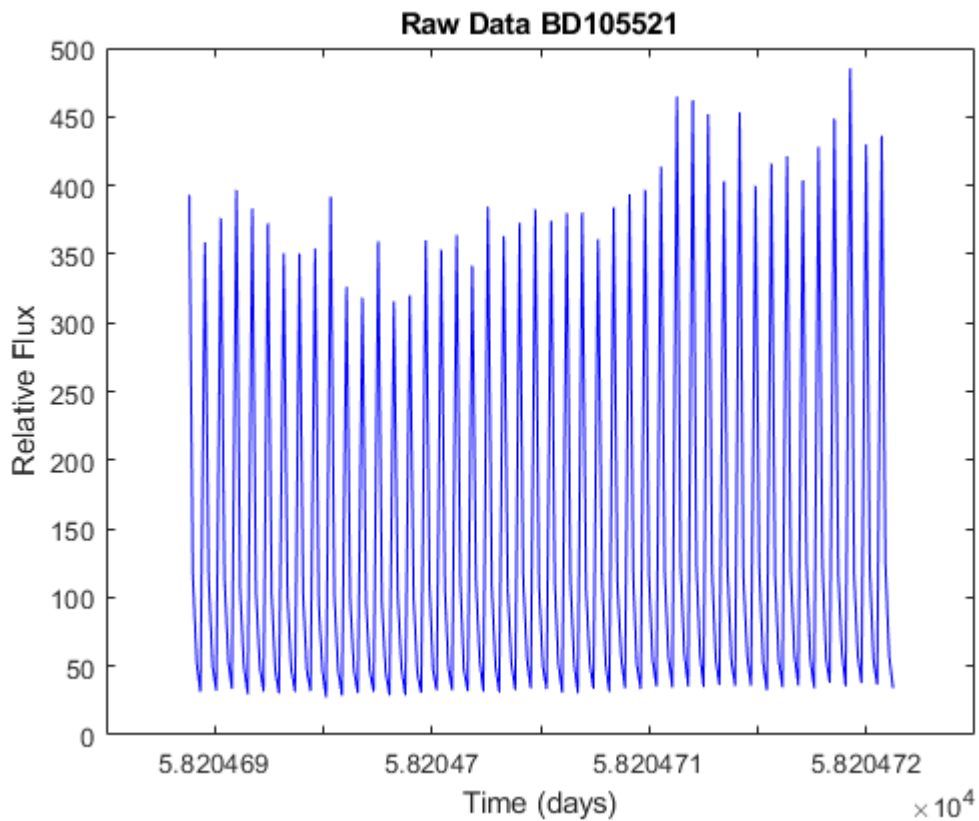
```
avg_freq/key_freq
```

```
ans =
    2.058824048136881
```

HD105521

Plot the raw data

```
plot(HD105521(:,1),HD105521(:,2), 'b');
title('Raw Data BD105521');
xlabel('Time (days)');
ylabel('Relative Flux');
```

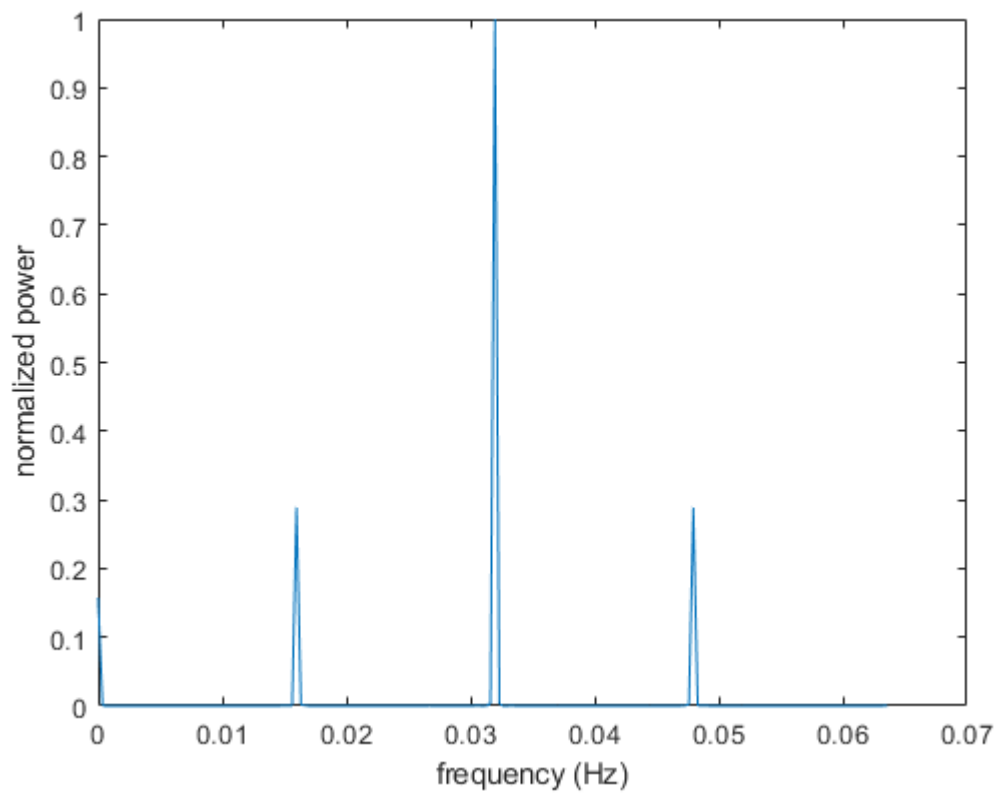


```
%B
avg_freq = 1/( mean( diff(HD105521(:,1)) ) * 86400 )
```

```
avg_freq =
    0.063943187006892
```

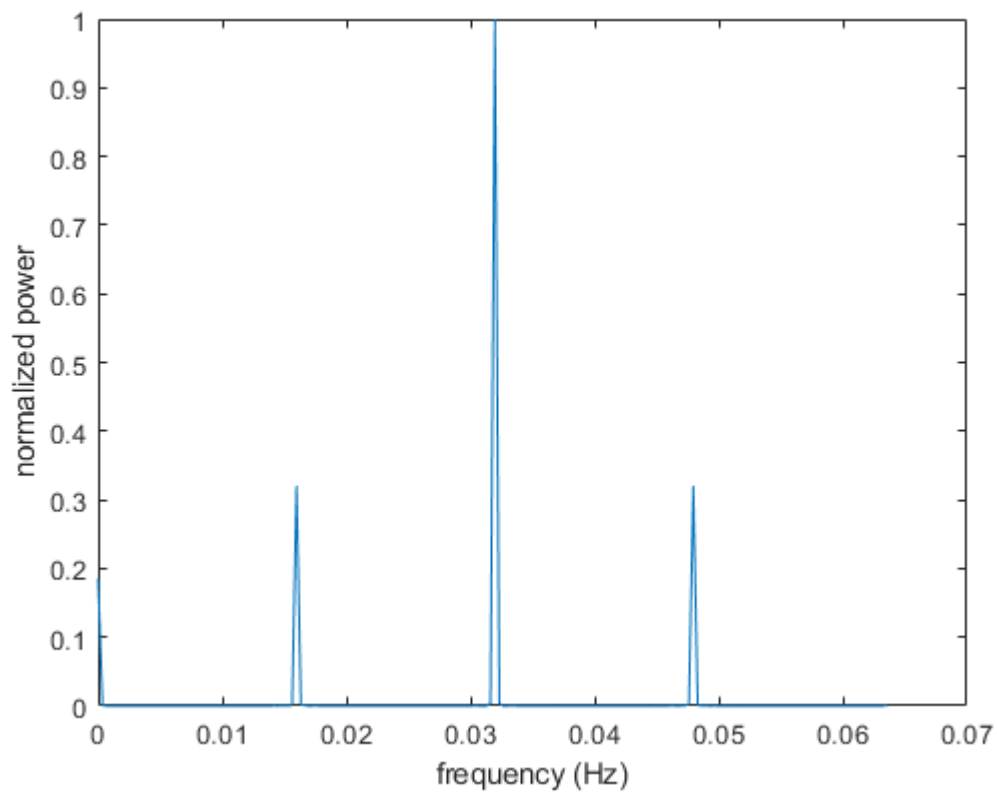
Use Linear Interpolation, then use a Fourier transform to attain the power spectrum

```
[Tnew,Mnew] = Interp_Lin(HD105521(:,1),HD105521(:,2));
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```



Use Spline Interpolation, then use a Fourier transform to attain the power spectrum

```
[Tnew,Mnew] = Interp_spline(HD105521(:,1),HD105521(:,2));
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```



Try non-uniform built in function "nufft"

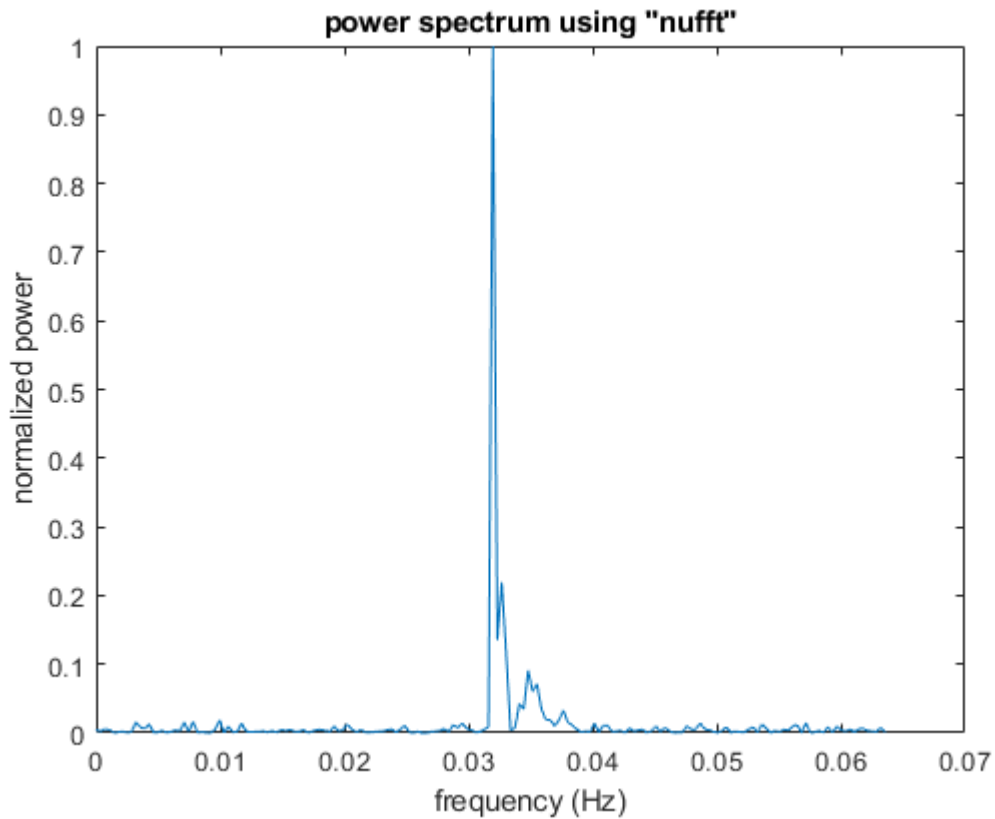
```
N = length(HD105521(:,1));
F = nufft( HD105521(:,1),HD105521(:,2) )/N;
F0 = fftshift(F);

power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')
```



```
key_freq = 0.0319716
```

```
key_freq =  
0.031971600000000
```

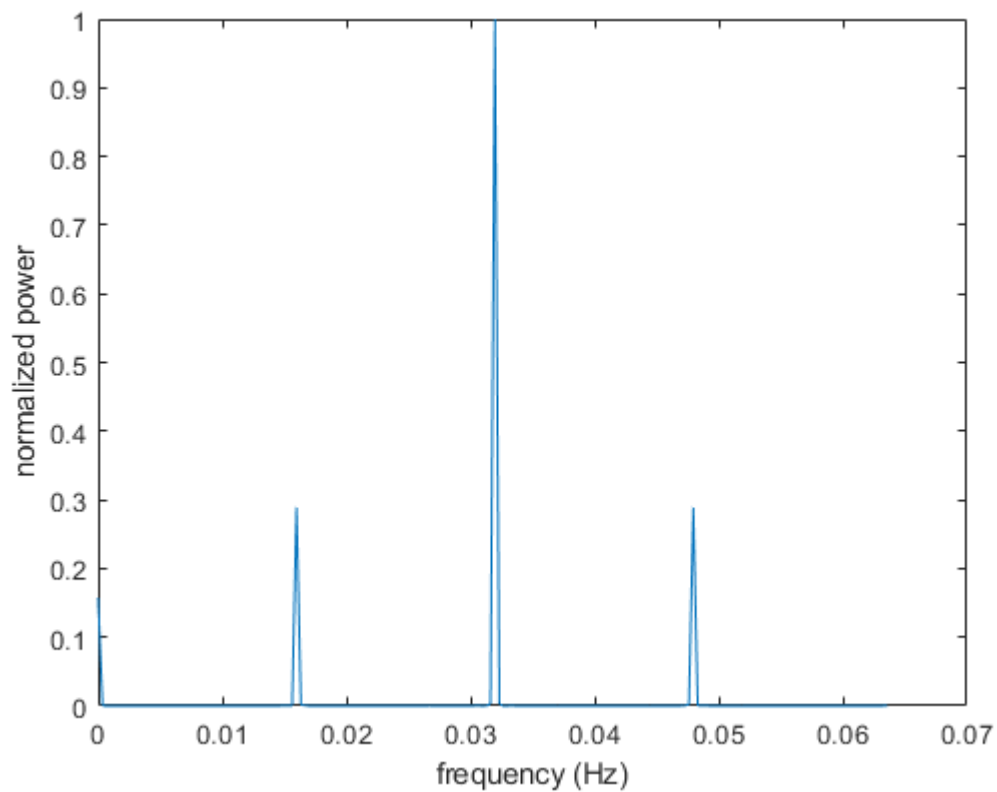
```
avg_freq =1/( mean( diff(HD105521(:,1)) ) *86400 )
```

```
avg_freq =  
0.063943187006892
```

```
avg_freq/key_freq
```

```
ans =  
1.999999593604684
```

```
%R  
avg_freq =1/( mean( diff(HD105521(:,3)) ) *86400 );  
[Tnew,Mnew] = Interp_Lin(HD105521(:,3),HD105521(:,4));  
Tnews = Tnew*86400; %convert time from days to seconds  
dt = Tnews(2) - Tnews(1);  
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```



```

N = length(HD105521(:,3));
F = nufft( HD105521(:,3),HD105521(:,4) )/N;
F0 = fftshift(F);

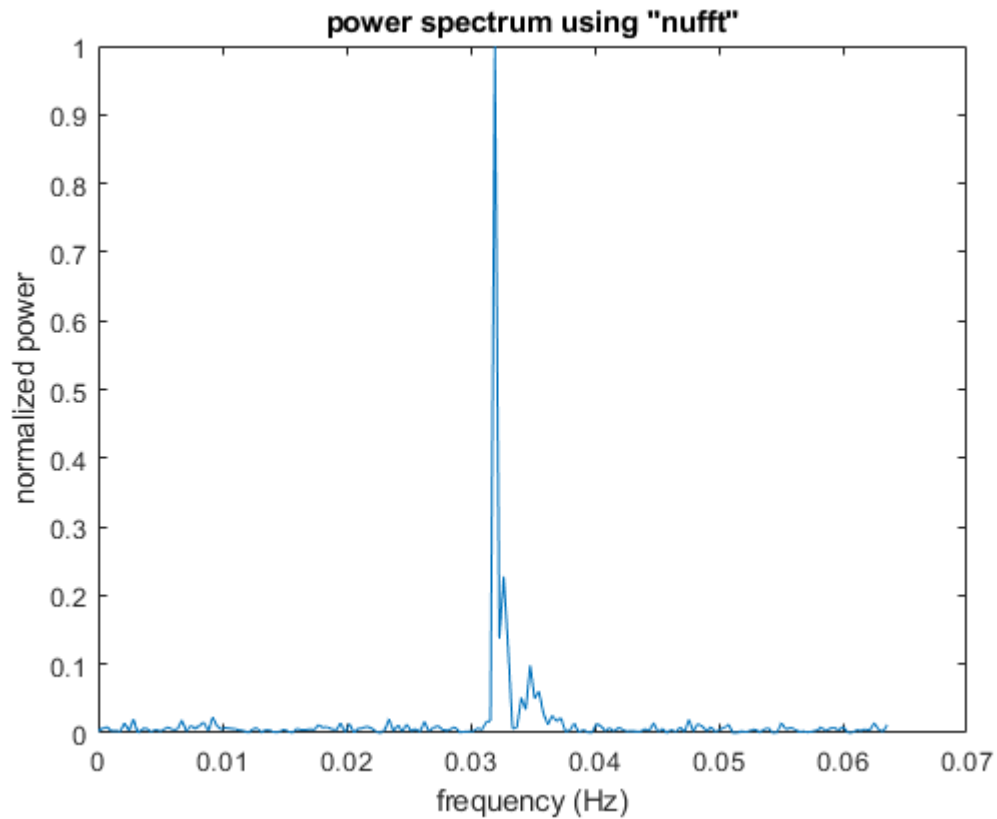
power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')

```

```
key_freq = 0.0319716
```

```
key_freq =  
0.031971600000000
```

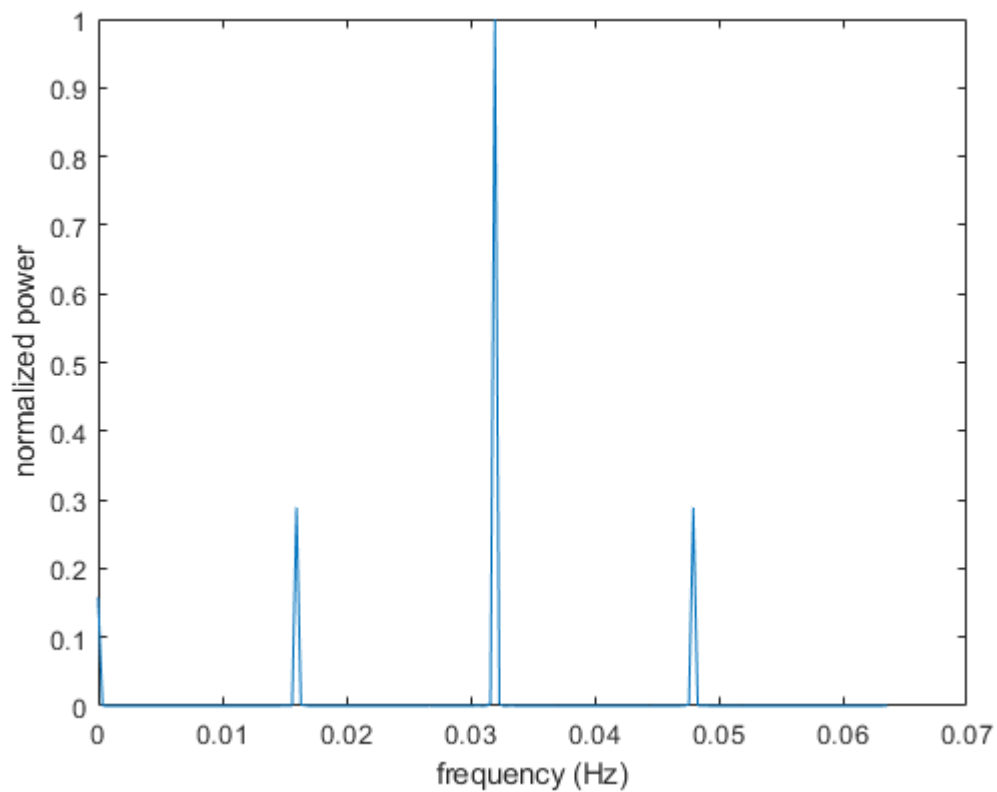
```
avg_freq =1/( mean( diff(HD105521(:,3)) ) *86400 )
```

```
avg_freq =  
0.063943187006892
```

```
avg_freq/key_freq
```

```
ans =  
1.999999593604684
```

```
%V  
avg_freq =1/( mean( diff(HD105521(:,5)) ) *86400 );  
[Tnew,Mnew] = Interp_Lin(HD105521(:,5),HD105521(:,6));  
Tnews = Tnew*86400; %convert time from days to seconds  
dt = Tnews(2) - Tnews(1);  
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```



```

N = length(HD105521(:,5));
F = nufft( HD105521(:,5),HD105521(:,6) )/N;
F0 = fftshift(F);

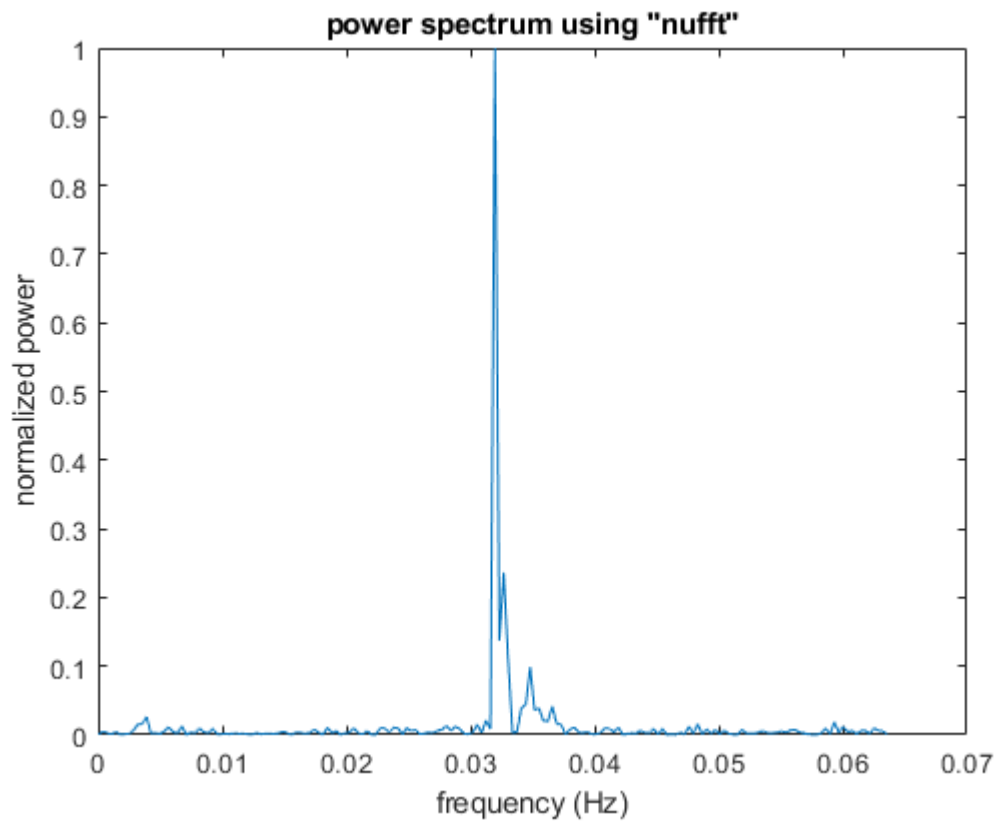
power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')

```



```
key_freq = 0.0319716
```

```
key_freq =  
0.031971600000000
```

```
avg_freq =1/( mean( diff(HD105521(:,5)) ) *86400 )
```

```
avg_freq =  
0.063943187006892
```

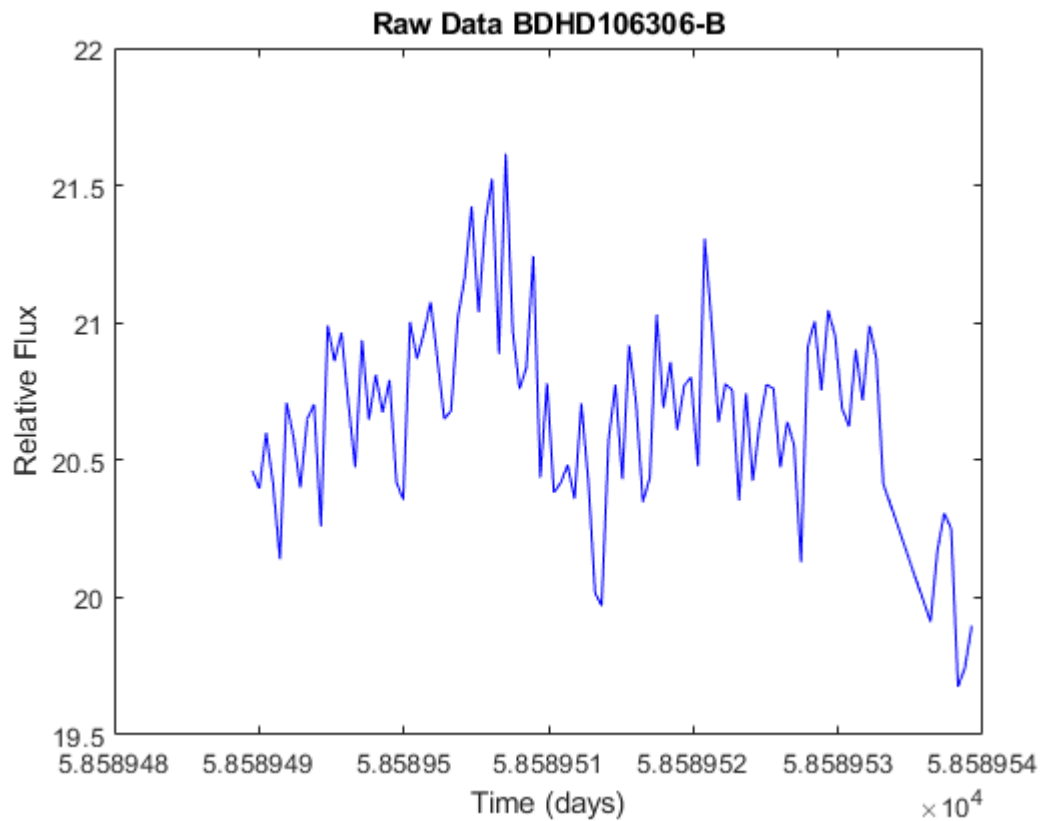
```
avg_freq/key_freq
```

```
ans =  
1.999999593604684
```

HD106306 B

Plot the raw data

```
plot(HD106306_B(:,1),HD106306_B(:,2), 'b');  
title('Raw Data BDHD106306-B');  
xlabel('Time (days)');  
ylabel('Relative Flux');
```

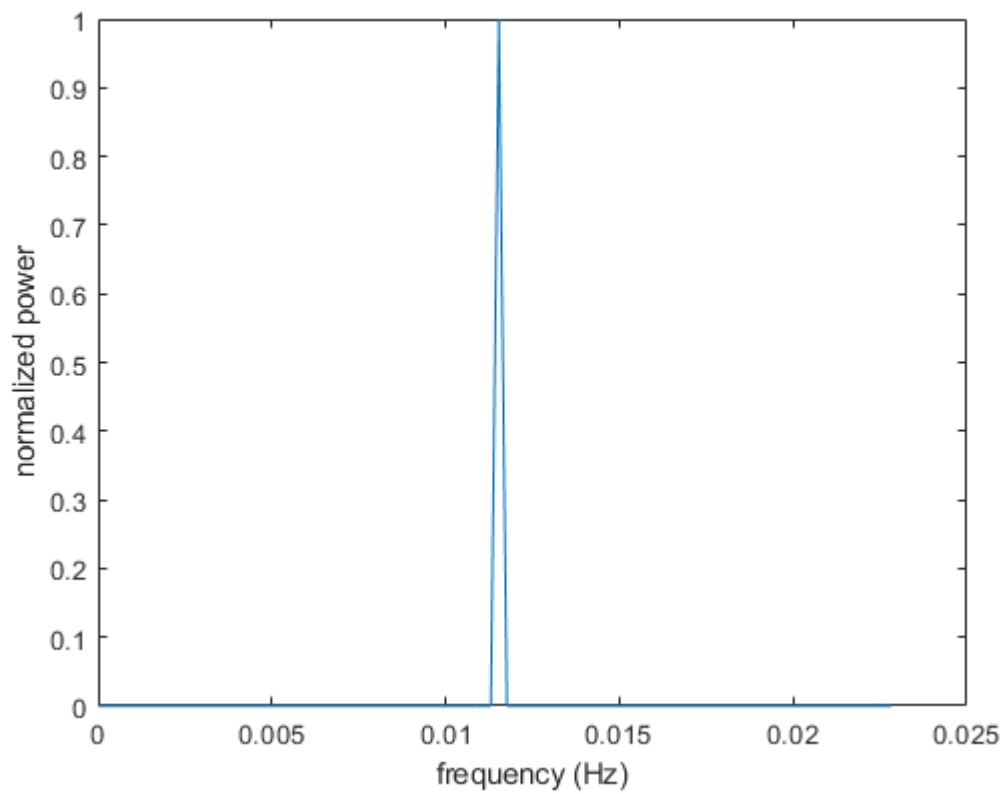


```
avg_freq = 1/( mean( diff(HD106306_B(:,1)) ) * 86400 )
```

```
avg_freq =  
0.023064278044436
```

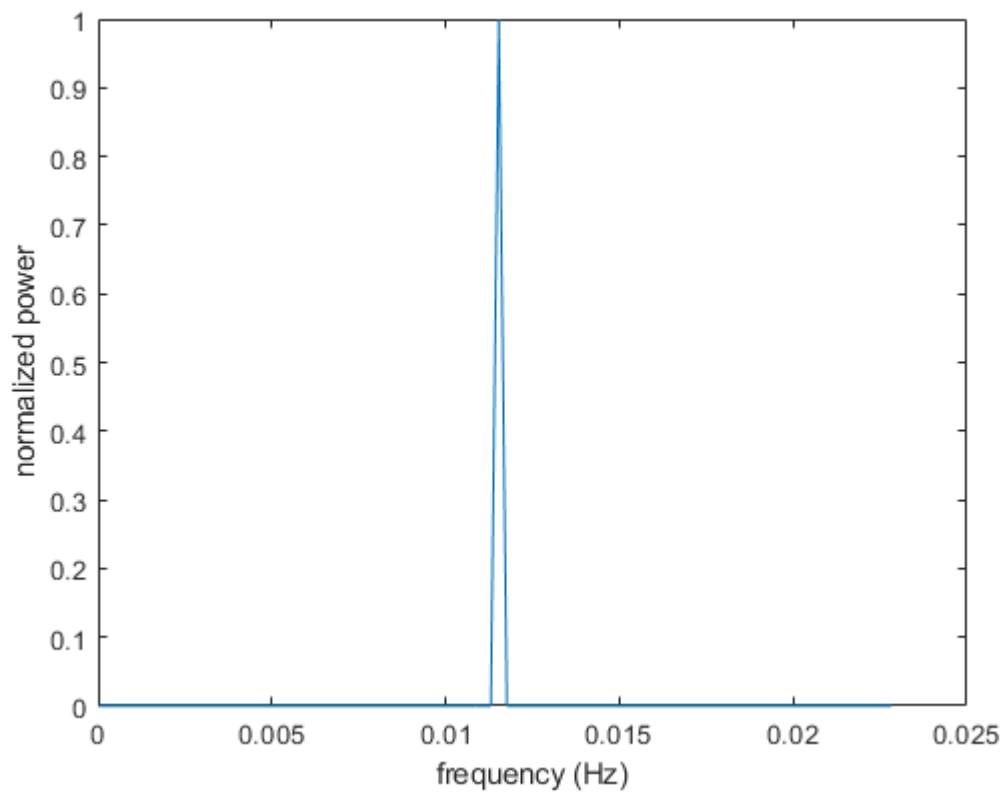
Use Linear Interpolation, then use a Fourier transform to attain the power spectrum

```
[Tnew,Mnew] = Interp_Lin(HD106306_B(:,1),HD106306_B(:,2));  
Tnews = Tnew*86400; %convert time from days to seconds  
dt = Tnews(2) - Tnews(1);  
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```



Use Spline Interpolation, then use a Fourier transform to attain the power spectrum

```
[Tnew,Mnew] = Interp_spline(HD106306_B(:,1),HD106306_B(:,2));
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```



Try non-uniform built in function "nufft"

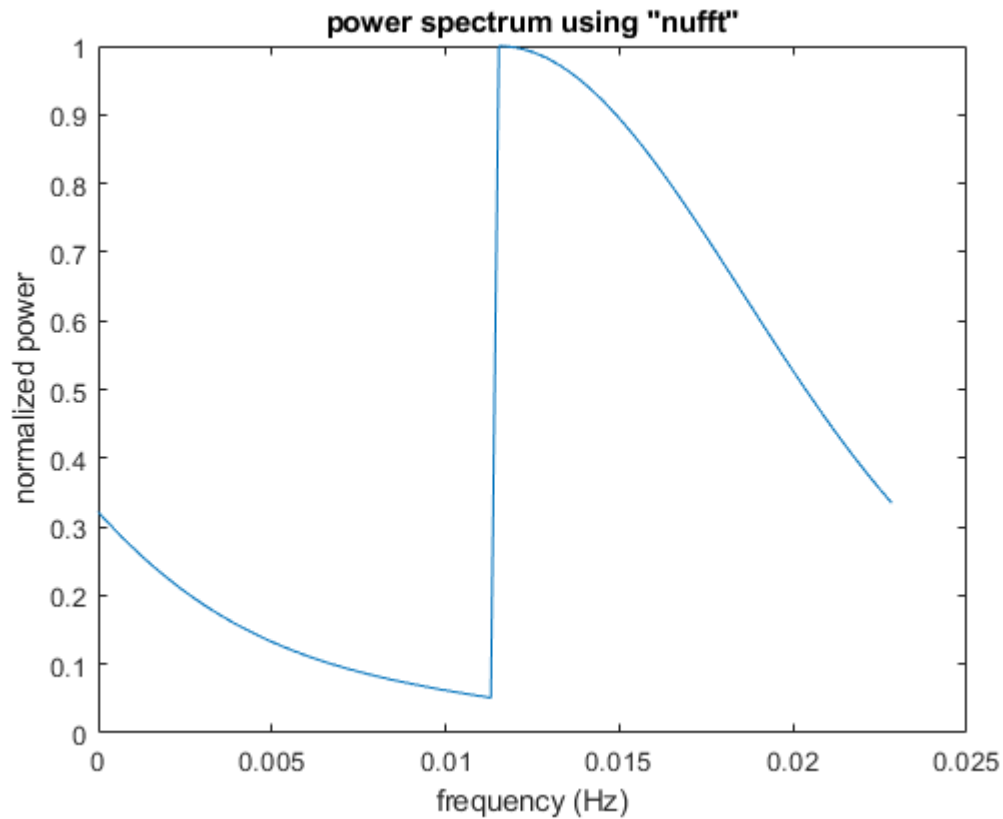
```
N = length(HD106306_B(:,1));
F = nufft( HD106306_B(:,1),HD106306_B(:,2) )/N;
F0 = fftshift(F);

power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')
```



```
key_freq = 0.0115321
```

```
key_freq =  
0.011532100000000
```

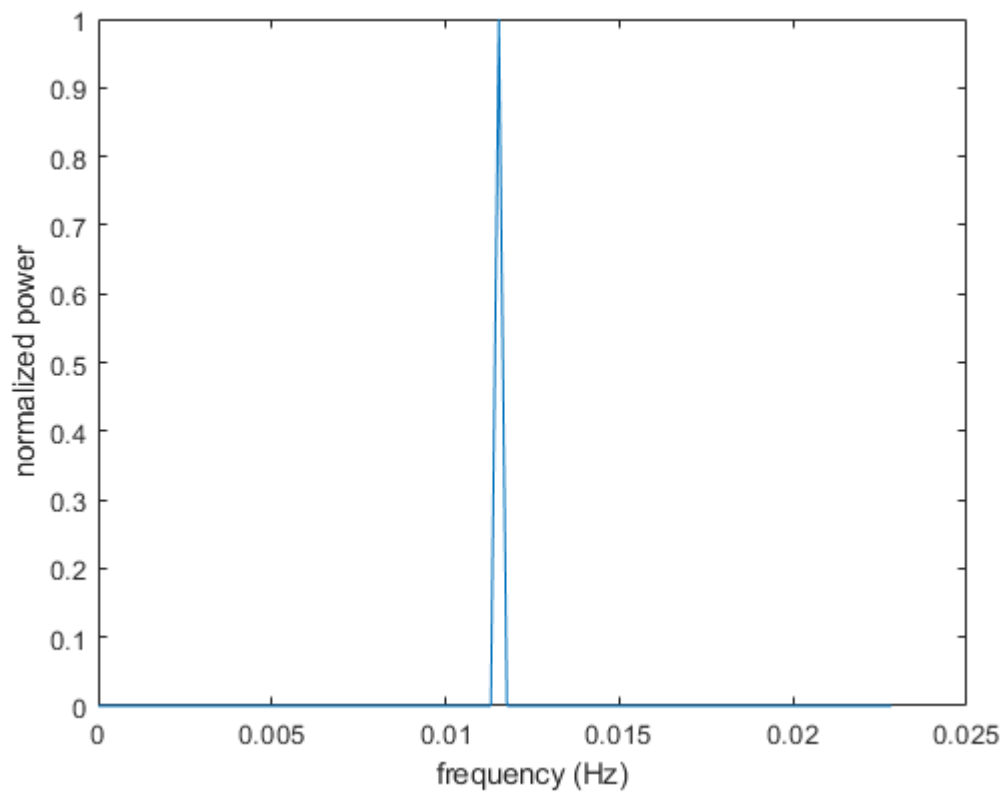
```
avg_freq =1/( mean( diff(HD106306_B(:,1)) ) *86400 )
```

```
avg_freq =  
0.023064278044436
```

```
avg_freq/key_freq
```

```
ans =  
2.000006767582301
```

```
%R  
avg_freq =1/( mean( diff(HD106306_R(:,1)) ) *86400 );  
[Tnew,Mnew] = Interp_Lin(HD106306_R(:,1),HD106306_R(:,2));  
Tnews = Tnew*86400; %convert time from days to seconds  
dt = Tnews(2) - Tnews(1);  
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```



```

N = length(HD106306_R(:,1));
F = nufft( HD106306_R(:,1),HD106306_R(:,2) )/N;
F0 = fftshift(F);

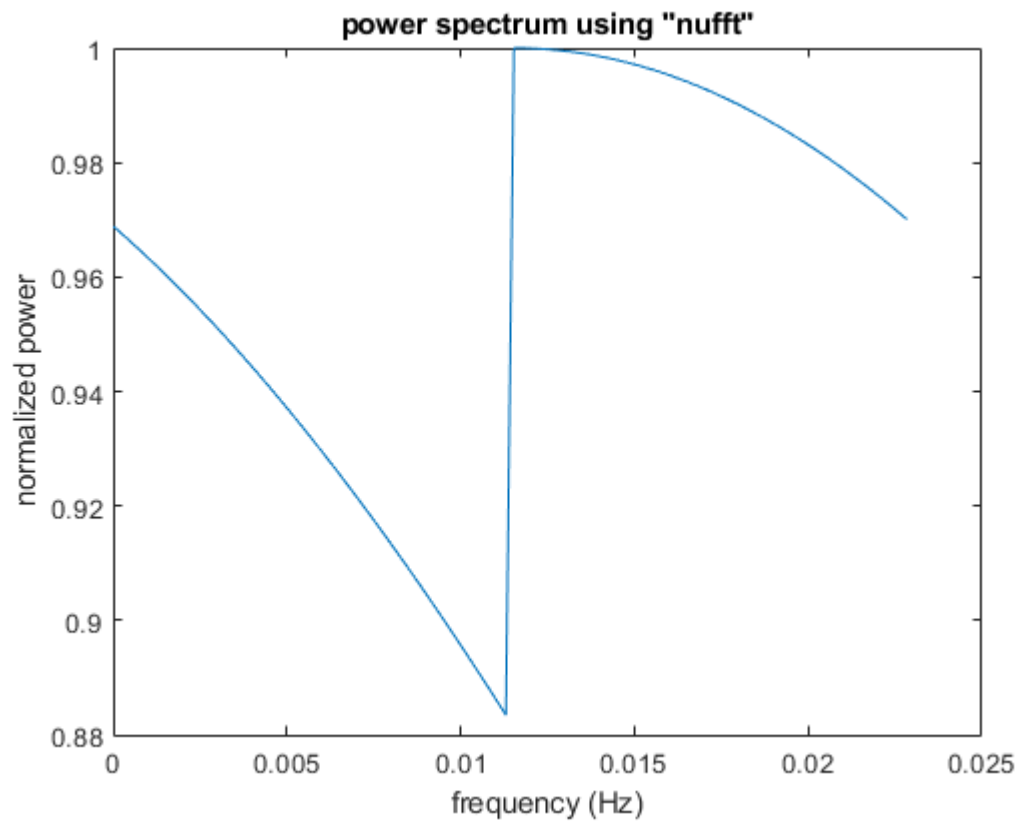
power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')

```

```
key_freq = 0.0115326
```

```
key_freq =  
    0.011532600000000
```

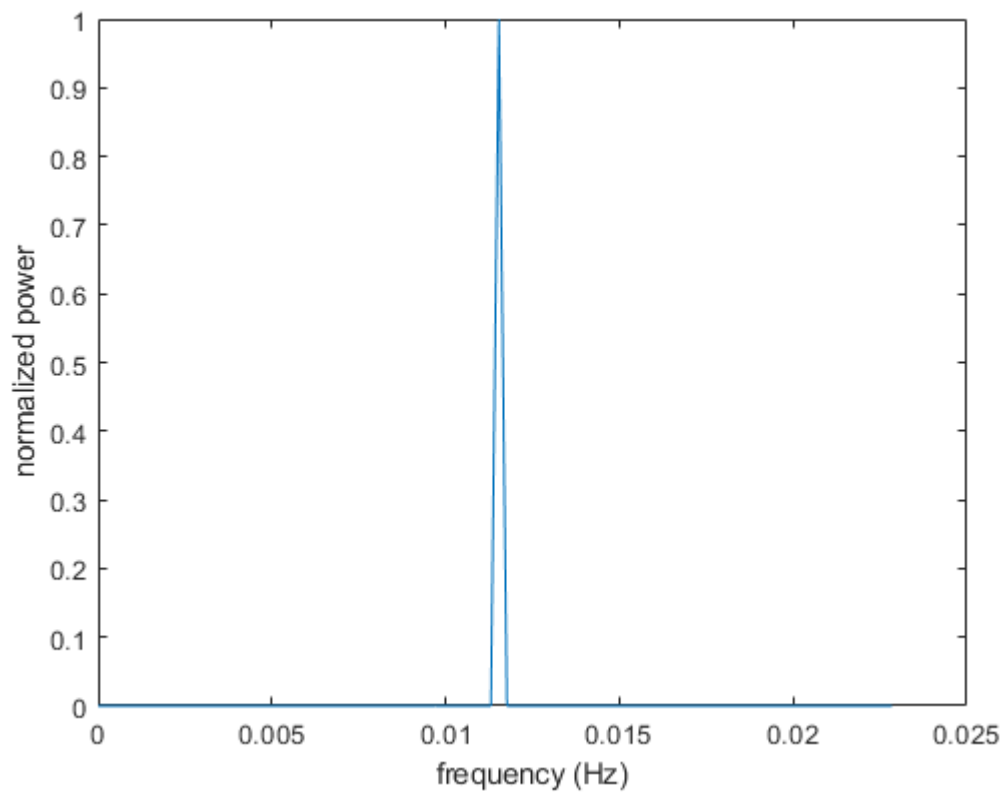
```
avg_freq =1/( mean( diff(HD106306_R(:,1)) ) *86400 )
```

```
avg_freq =  
    0.023065206595740
```

```
avg_freq/key_freq
```

```
ans =  
    2.000000571921362
```

```
%V  
avg_freq =1/( mean( diff(HD106306_V(:,1)) ) *86400 );  
[Tnew,Mnew] = Interp_Lin(HD106306_V(:,1),HD106306_V(:,2));  
Tnews = Tnew*86400; %convert time from days to seconds  
dt = Tnews(2) - Tnews(1);  
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```



```

N = length(HD106306_V(:,1));
F = nufft( HD106306_V(:,1),HD106306_V(:,2) )/N;
F0 = fftshift(F);

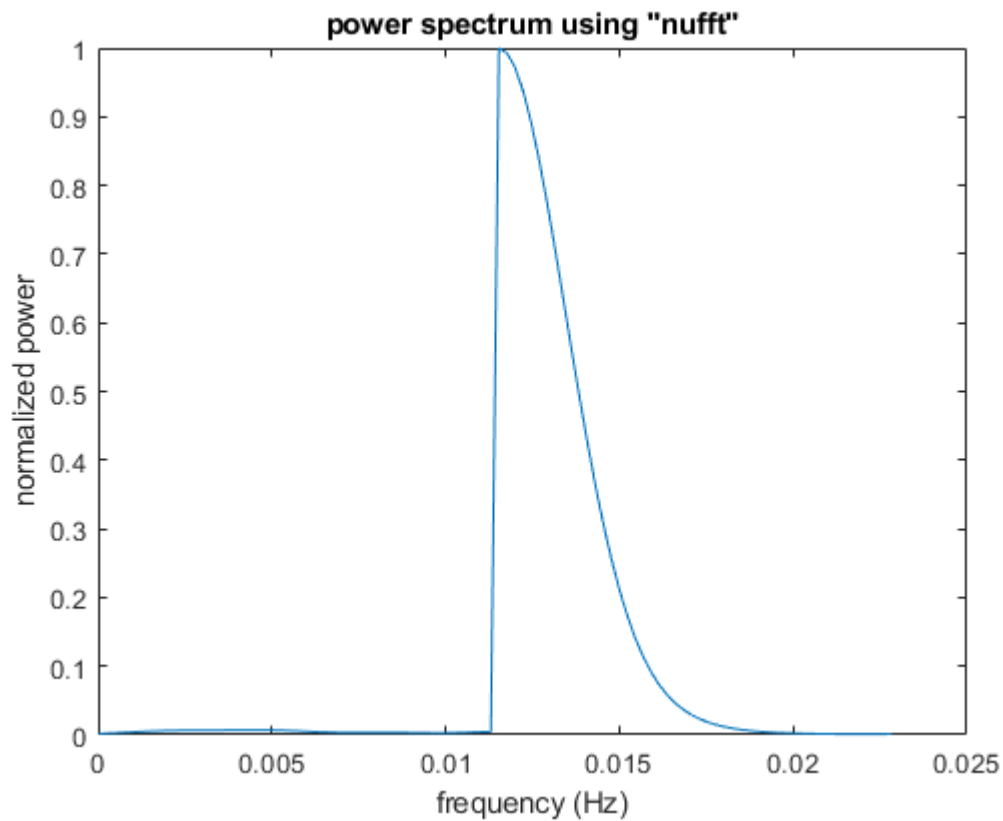
power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')

```



```
key_freq = 0.0115335
```

```
key_freq =  
0.011533500000000
```

```
avg_freq =1/( mean( diff(HD106306_V(:,1)) ) *86400 )
```

```
avg_freq =  
0.023067063922664
```

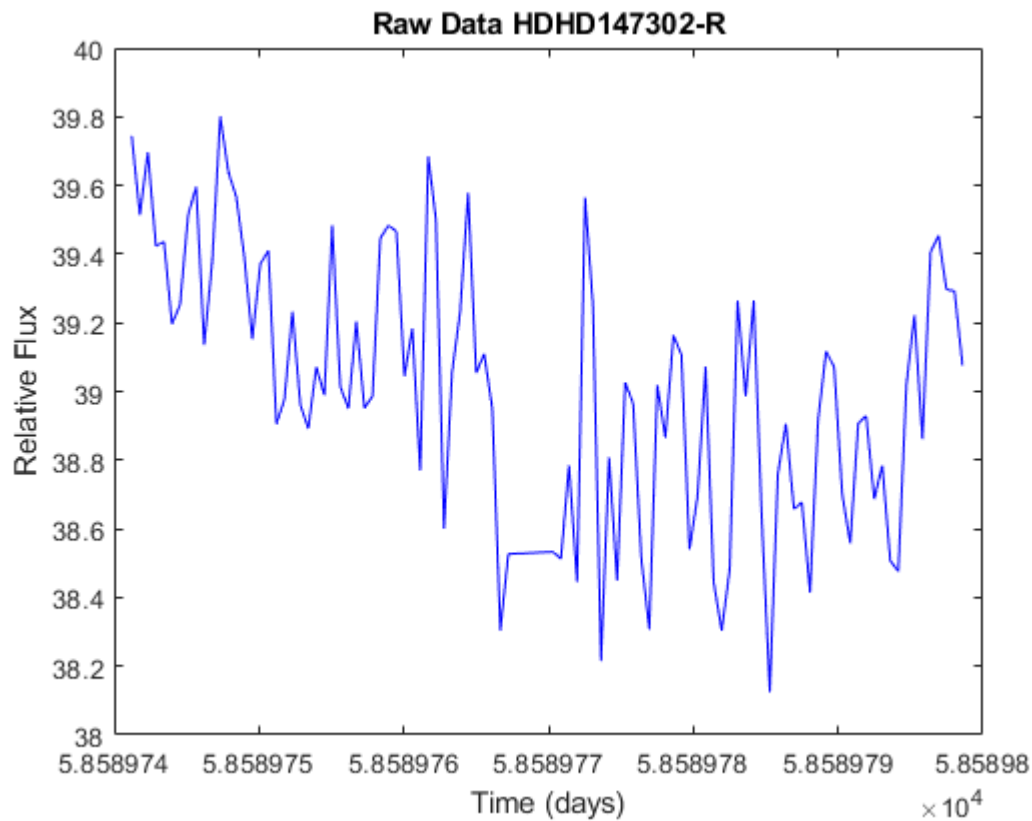
```
avg_freq/key_freq
```

```
ans =  
2.000005542347433
```

HD147302_R

Plot the raw data

```
plot(HD147302_R(:,1),HD147302_R(:,2), 'b');  
title('Raw Data HDHD147302-R');  
xlabel('Time (days)');  
ylabel('Relative Flux');
```

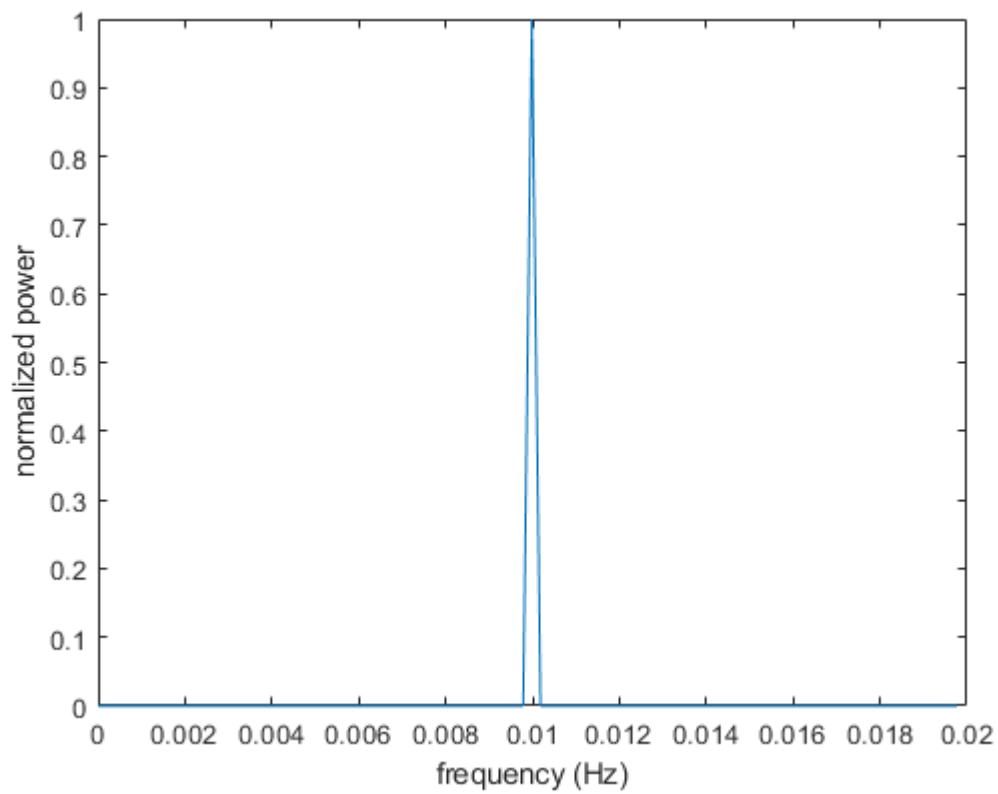


```
avg_freq = 1/( mean( diff(HD147302_R(:,1)) ) * 86400 )
```

```
avg_freq =  
0.019970951344655
```

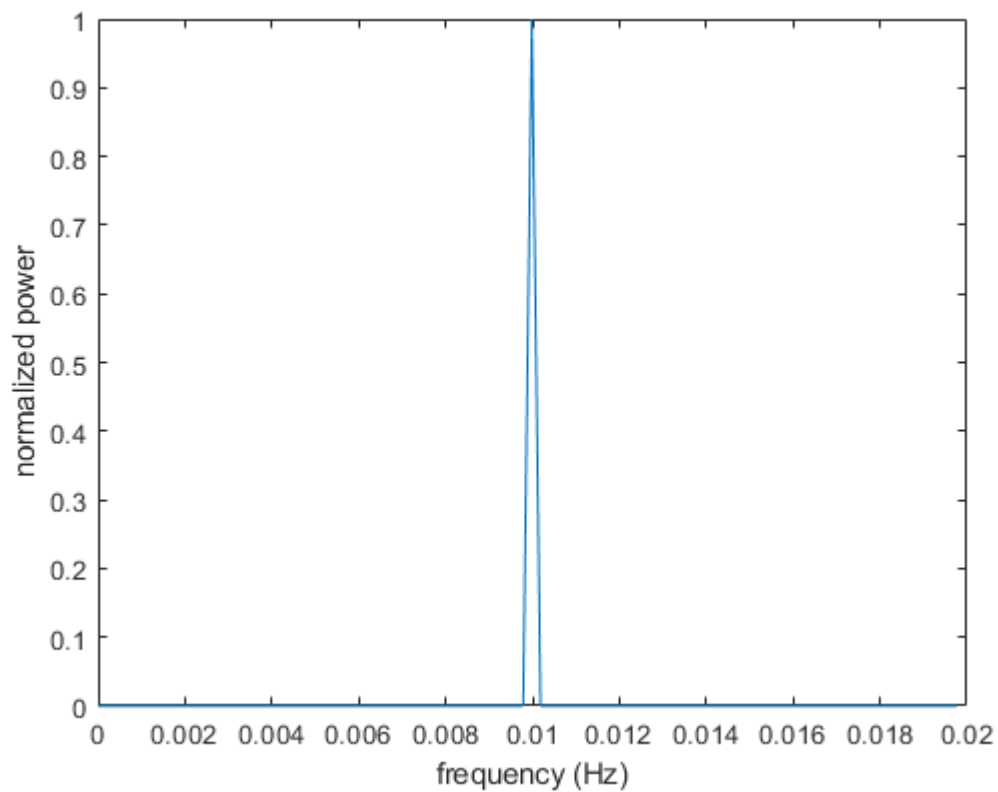
Use Linear Interpolation, then use a Fourier transform to attain the power spectrum

```
[Tnew,Mnew] = Interp_Lin(HD147302_R(:,1),HD147302_R(:,2));  
Tnews = Tnew*86400; %convert time from days to seconds  
dt = Tnews(2) - Tnews(1);  
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```



Use Spline Interpolation, then use a Fourier transform to attain the power spectrum

```
[Tnew,Mnew] = Interp_spline(HD147302_R(:,1),HD147302_R(:,2));
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```



Try non-uniform built in function "nufft"

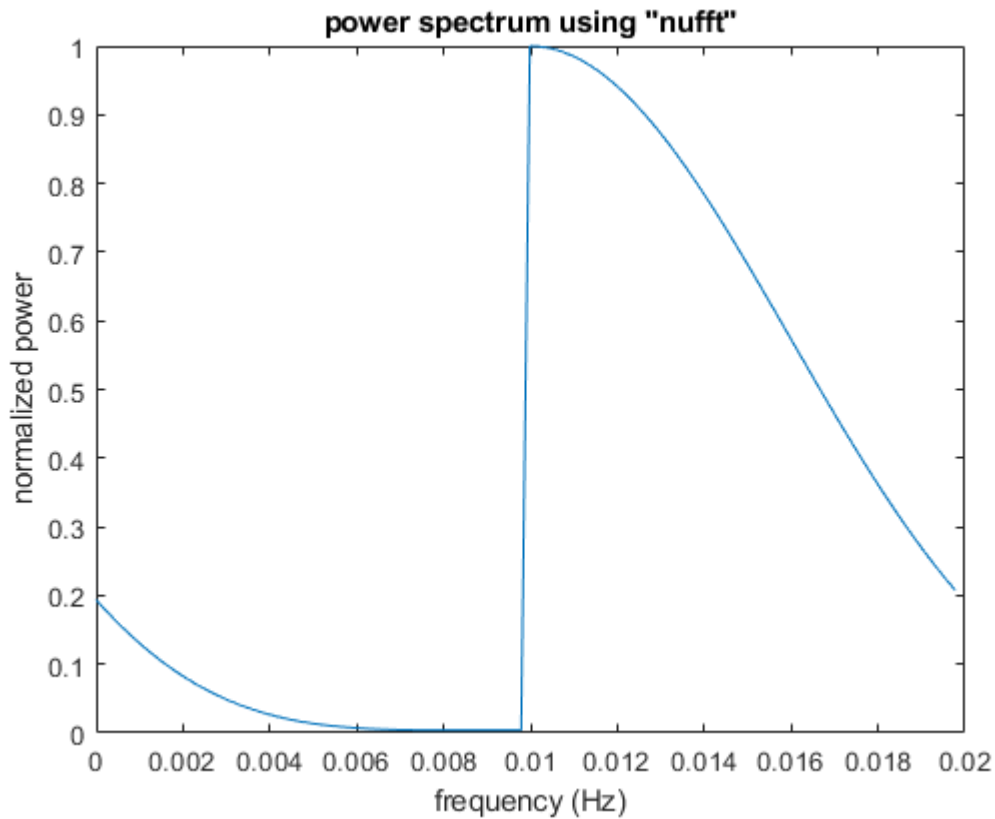
```
N = length(HD147302_R(:,1));
F = nufft( HD147302_R(:,1),HD147302_R(:,2) )/N;
F0 = fftshift(F);

power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')
```



```
key_freq = 0.00998548
```

```
key_freq =  
    0.009985480000000
```

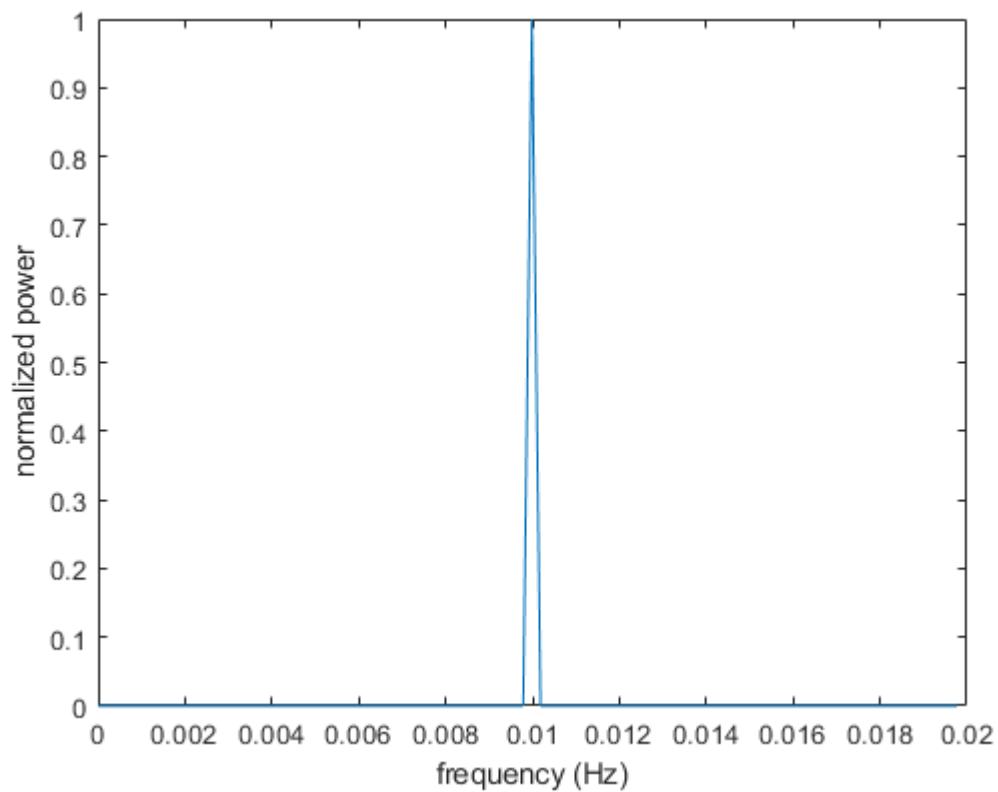
```
avg_freq = 1/( mean( diff(HD147302_R(:,1)) ) * 86400 )
```

```
avg_freq =  
    0.019970951344655
```

```
avg_freq/key_freq
```

```
ans =  
    1.999999133206939
```

```
%V  
avg_freq = 1/( mean( diff(HD147302_V(:,1)) ) * 86400 );  
[Tnew,Mnew] = Interp_Lin(HD147302_V(:,1),HD147302_V(:,2));  
Tnews = Tnew*86400; %convert time from days to seconds  
dt = Tnews(2) - Tnews(1);  
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```



```

N = length(HD147302_V(:,1));
F = nufft( HD147302_V(:,1),HD147302_V(:,2) )/N;
F0 = fftshift(F);

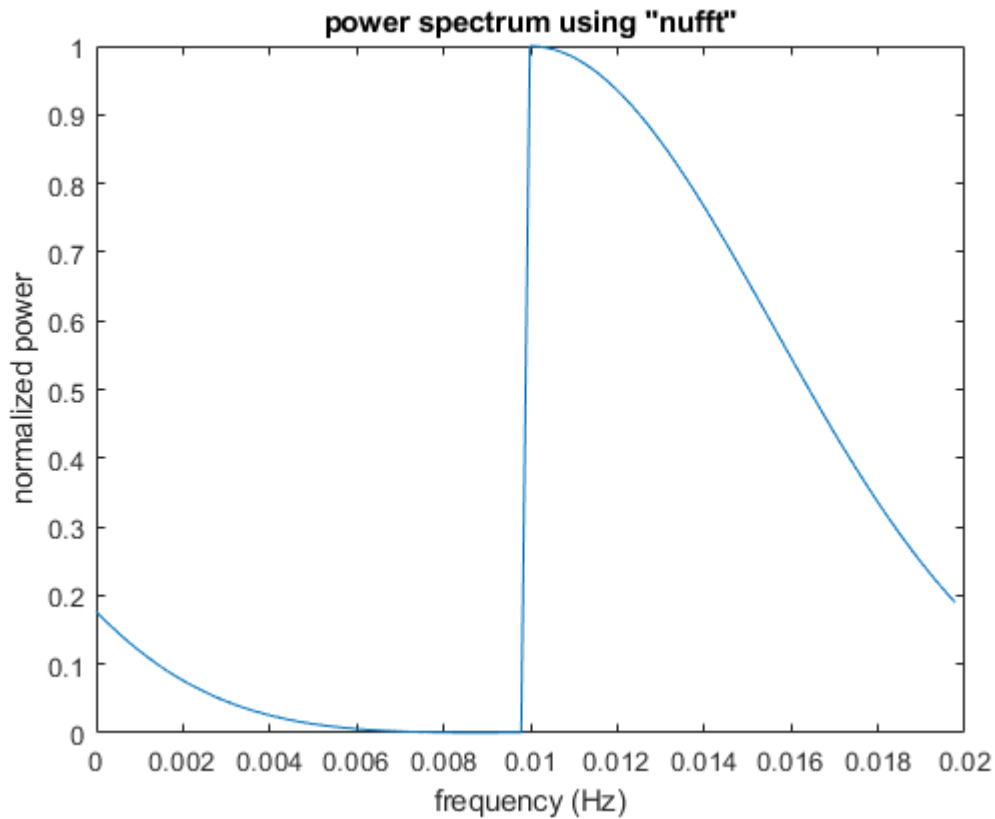
power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')

```

```
key_freq = 0.00998635
```

```
key_freq =  
0.009986350000000
```

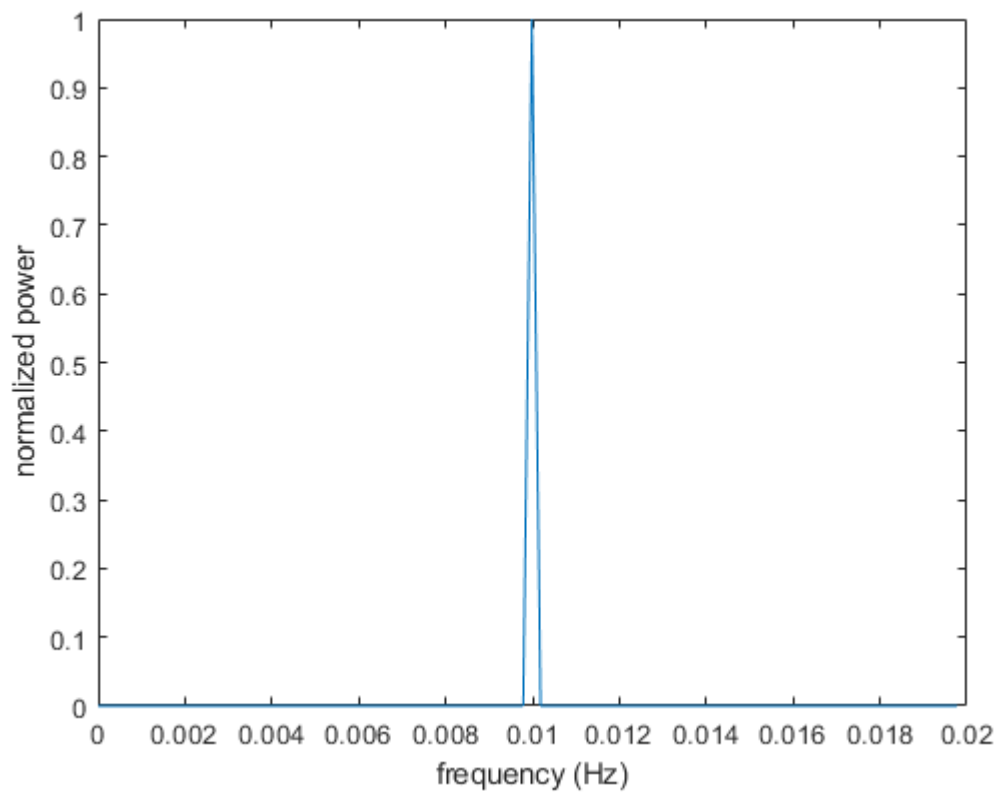
```
avg_freq =1/( mean( diff(HD147302_V(:,1)) ) *86400 )
```

```
avg_freq =  
0.019972691882309
```

```
avg_freq/key_freq
```

```
ans =  
1.999999187121354
```

```
%B  
avg_freq =1/( mean( diff(HD147302_B(:,1)) ) *86400 );  
[Tnew,Mnew] = Interp_Lin(HD147302_B(:,1),HD147302_B(:,2));  
Tnews = Tnew*86400; %convert time from days to seconds  
dt = Tnews(2) - Tnews(1);  
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```



```

N = length(HD147302_B(:,1));
F = nufft( HD147302_B(:,1),HD147302_B(:,2) )/N;
F0 = fftshift(F);

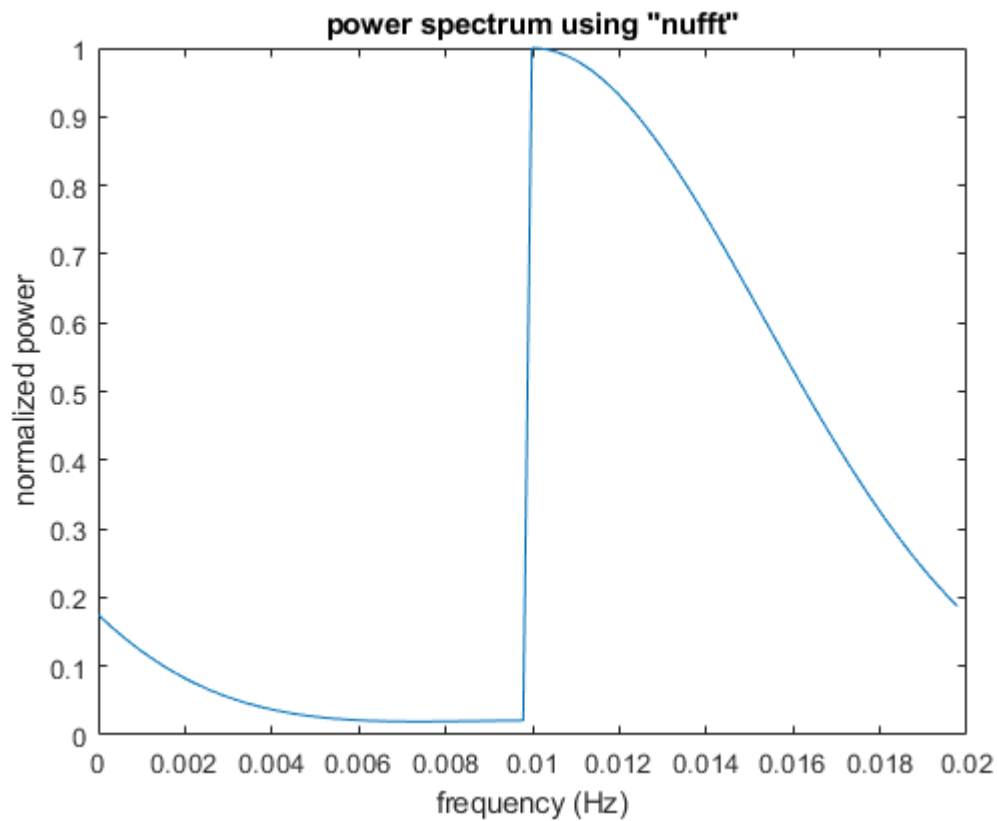
power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')

```



```
key_freq = 0.00998669
```

```
key_freq =  
0.0099866900000000
```

```
avg_freq =1/( mean( diff(HD147302_B(:,1)) ) *86400 )
```

```
avg_freq =  
0.019973388183336
```

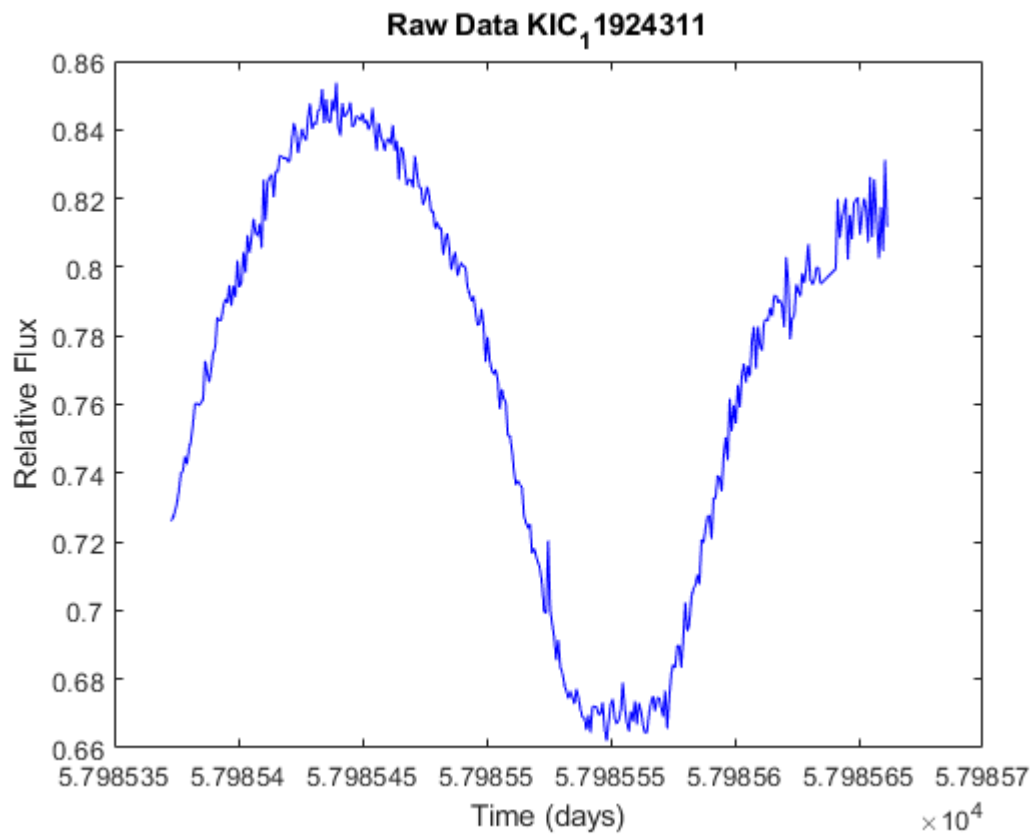
```
avg_freq/key_freq
```

```
ans =  
2.000000819424234
```

KIC_11924311

Plot the raw data

```
plot(KIC_11924311.V_time,KIC_11924311.V_flux,'b');  
title('Raw Data KIC_11924311');  
xlabel('Time (days)');  
ylabel('Relative Flux');
```

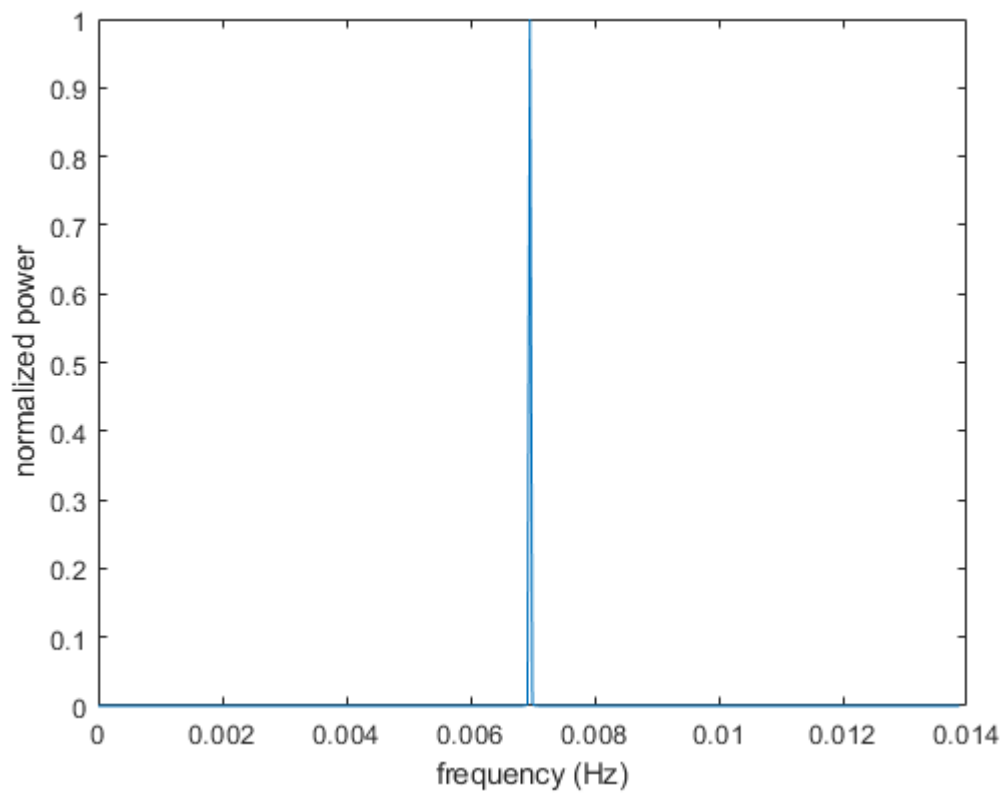


```
avg_freq = 1/( mean( diff(KIC_11924311.V_time) ) * 86400 )
```

```
avg_freq =  
    0.013917606486280
```

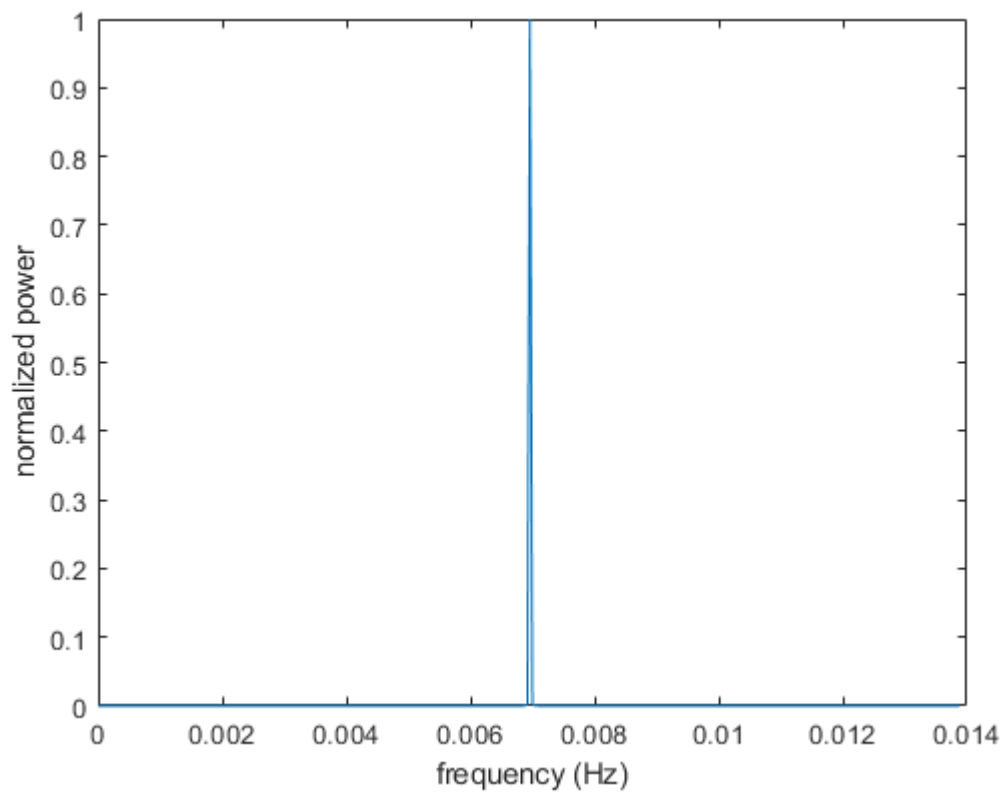
Use Linear Interpolation, then use a Fourier transform to attain the power spectrum

```
[Tnew,Mnew] = Interp_Lin(KIC_11924311.V_time,KIC_11924311.V_flux);  
Tnews = Tnew*86400; %convert time from days to seconds  
dt = Tnews(2) - Tnews(1);  
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```



Use Spline Interpolation, then use a Fourier transform to attain the power spectrum

```
[Tnew,Mnew] = Interp_spline(KIC_11924311.V_time,KIC_11924311.V_flux);  
Tnews = Tnew*86400; %convert time from days to seconds  
dt = Tnews(2) - Tnews(1);  
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```



Try non-uniform built in function "nufft"

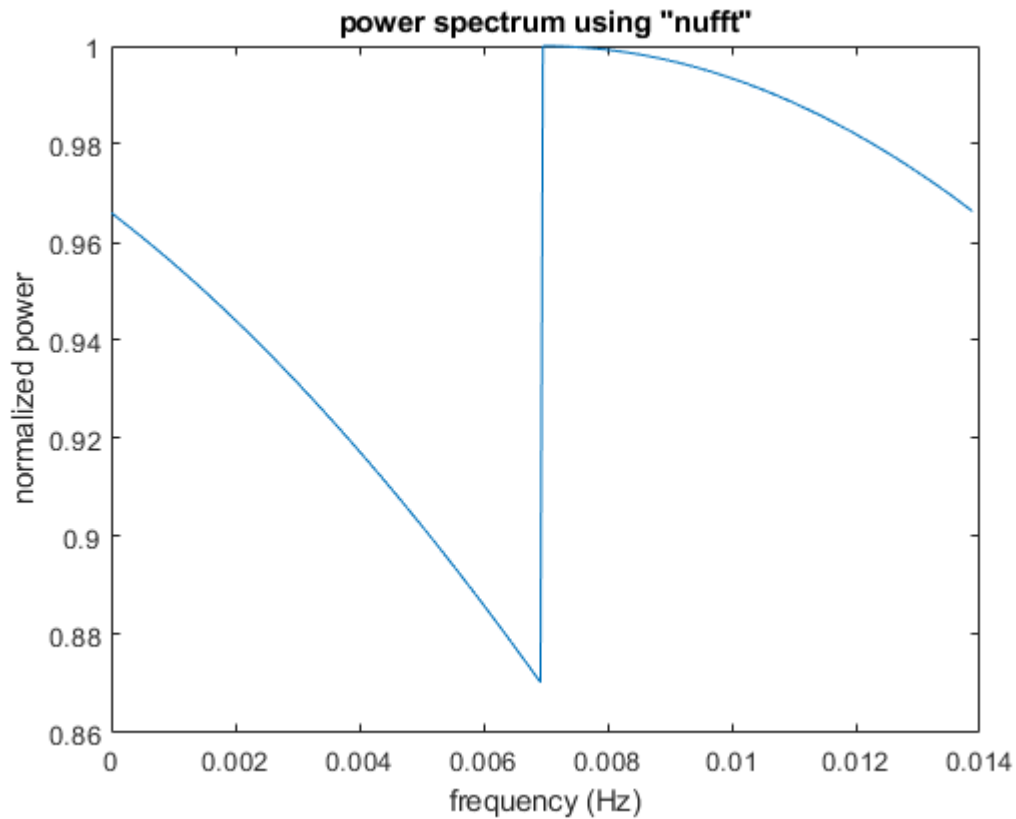
```
N = length(KIC_11924311.V_time);
F = nufft( KIC_11924311.V_time,KIC_11924311.V_flux )/N;
F0 = fftshift(F);

power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')
```



```
key_freq = 0.0069588
```

```
key_freq =  
0.0069588000000000
```

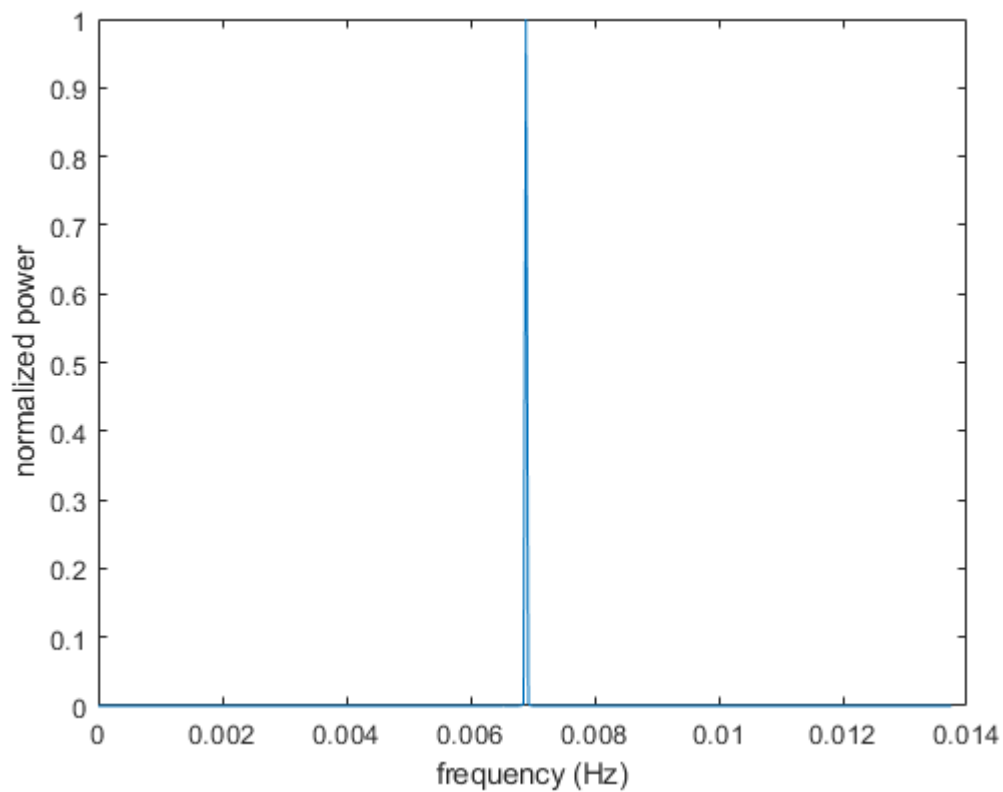
```
avg_freq =1/( mean( diff(KIC_11924311.V_time) ) *86400 )
```

```
avg_freq =  
0.013917606486280
```

```
avg_freq/key_freq
```

```
ans =  
2.000000932097445
```

```
%B  
avg_freq =1/( mean( diff(KIC_11924311.B_time) ) *86400 );  
[Tnew,Mnew] = Interp_spline(KIC_11924311.B_time,KIC_11924311.B_flux);  
Tnews = Tnew*86400; %convert time from days to seconds  
dt = Tnews(2) - Tnews(1);  
[fk,powerNor] = EnergySpec(KIC_11924311.B_time,KIC_11924311.B_flux,dt);
```



```

N = length(KIC_11924311.B_time);
F = nufft( KIC_11924311.B_time,KIC_11924311.B_flux )/N;
F0 = fftshift(F);

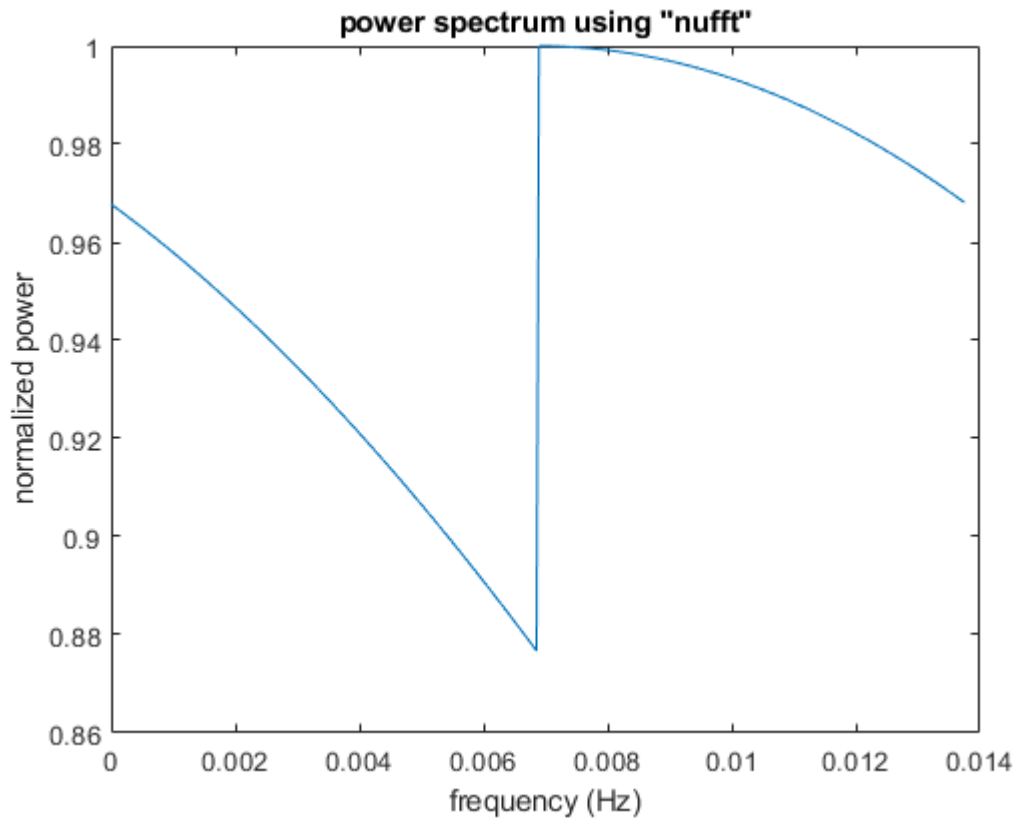
power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')

```

```
key_freq = 0.00689501
```

```
key_freq =  
0.006895010000000
```

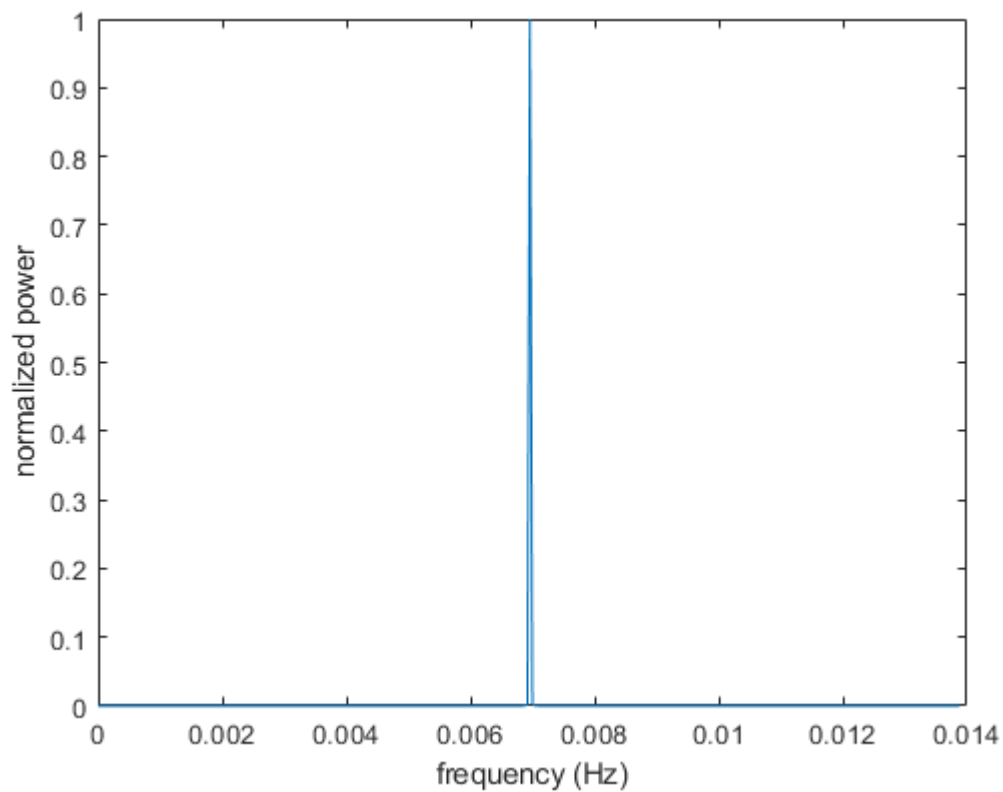
```
avg_freq =1/( mean( diff(KIC_11924311.B_time) ) *86400 )
```

```
avg_freq =  
0.013790014090173
```

```
avg_freq/key_freq
```

```
ans =  
1.999999142883464
```

```
%R  
avg_freq =1/( mean( diff(KIC_11924311.R_time) ) *86400 );  
[Tnew,Mnew] = Interp_spline(KIC_11924311.R_time,KIC_11924311.R_flux);  
Tnews = Tnew*86400; %convert time from days to seconds  
dt = Tnews(2) - Tnews(1);  
[fk,powerNor] = EnergySpec(KIC_11924311.R_time,KIC_11924311.R_flux,dt);
```



```

N = length(KIC_11924311.R_time);
F = nufft( KIC_11924311.R_time,KIC_11924311.R_flux )/N;
F0 = fftshift(F);

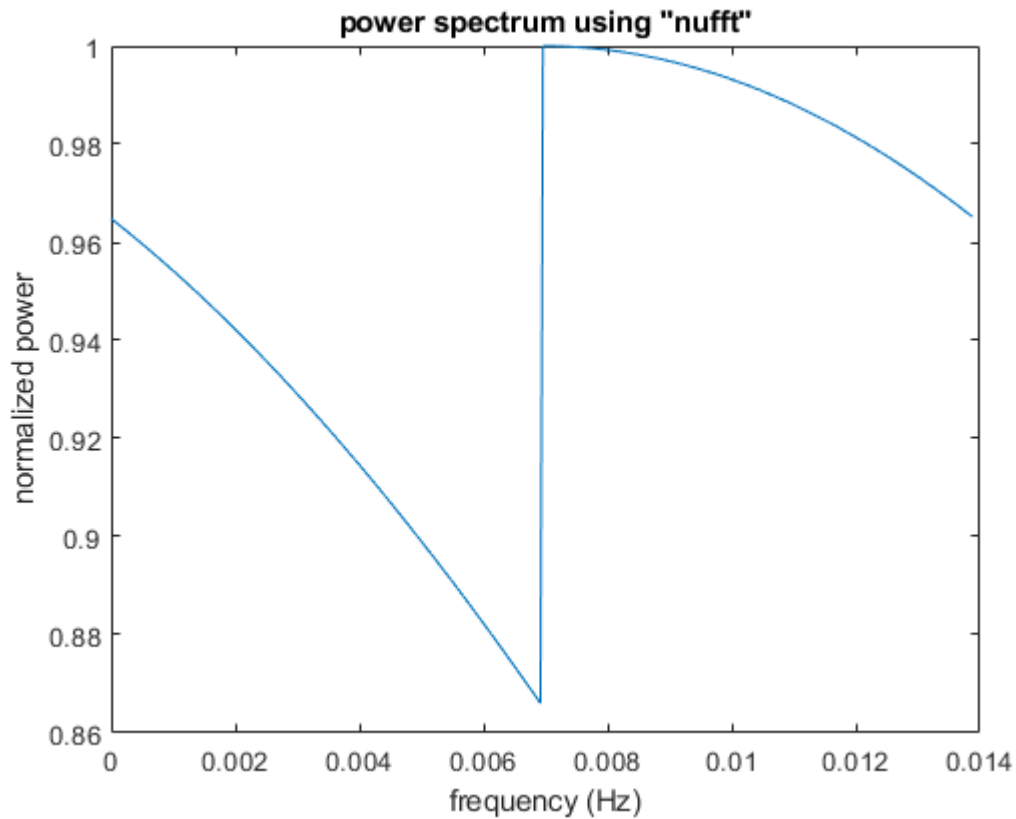
power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')

```



```
key_freq = 0.0069588
```

```
key_freq =  
0.0069588000000000
```

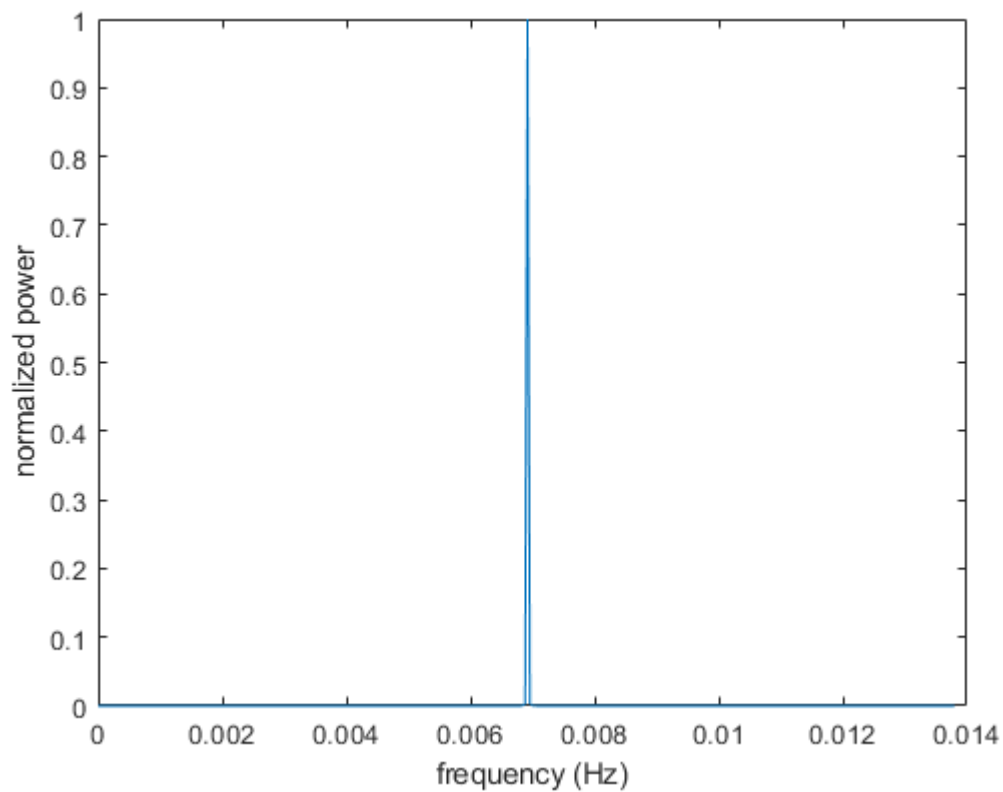
```
avg_freq =1/( mean( diff(KIC_11924311.R_time) ) *86400 )
```

```
avg_freq =  
0.013917606486280
```

```
avg_freq/key_freq
```

```
ans =  
2.000000932097445
```

```
%I  
avg_freq =1/( mean( diff(KIC_11924311.I_time) ) *86400 );  
[Tnew,Mnew] = Interp_spline(KIC_11924311.I_time,KIC_11924311.I_flux);  
Tnews = Tnew*86400; %convert time from days to seconds  
dt = Tnews(2) - Tnews(1);  
[fk,powerNor] = EnergySpec(KIC_11924311.I_time,KIC_11924311.I_flux,dt);
```



```

N = length(KIC_11924311.I_time);
F = nufft( KIC_11924311.I_time,KIC_11924311.I_flux )/N;
F0 = fftshift(F);

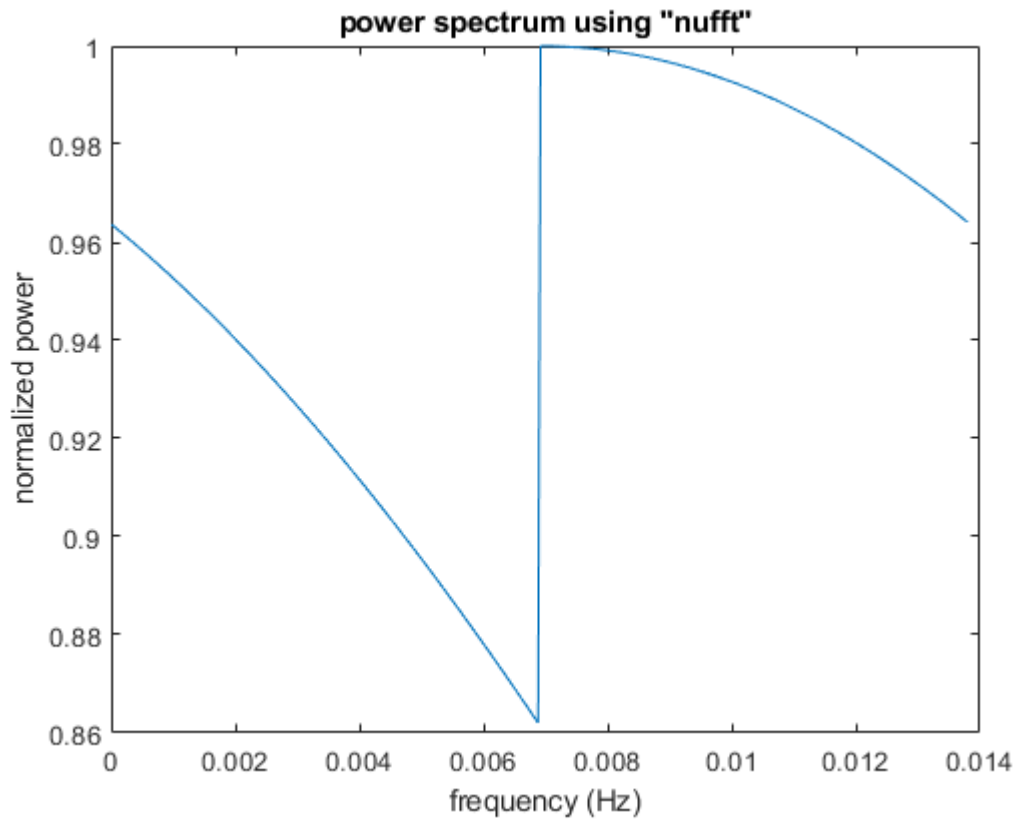
power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')

```



```
key_freq = 0.00691972
```

```
key_freq =  
    0.006919720000000
```

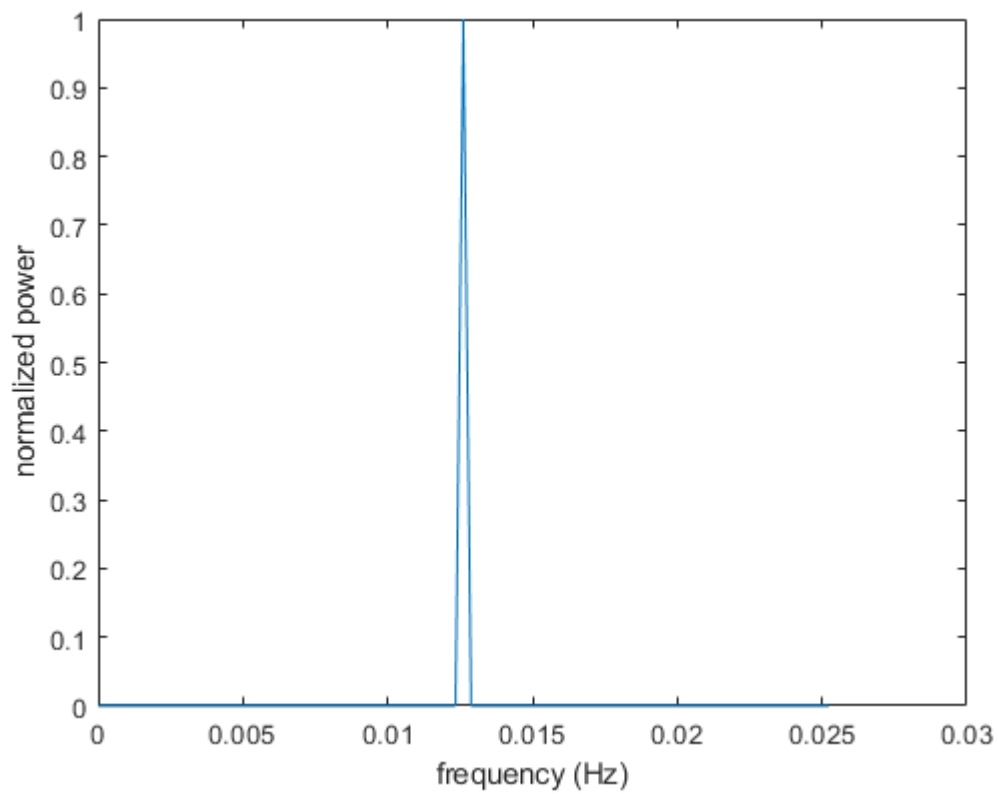
```
avg_freq = 1/( mean( diff(KIC_11924311.I_time) ) *86400 )
```

```
avg_freq =  
    0.013839433851694
```

```
avg_freq/key_freq
```

```
ans =  
    1.999999111480495
```

```
%BD48_1098  
BD48_1098 = BD48_1098(2:end,:);  
%B  
avg_freq = 1/( mean( diff(BD48_1098(:,1)) ) *86400 );  
  
[Tnew,Mnew] = Interp_spline(BD48_1098(:,1),BD48_1098(:,2));  
Tnews = Tnew*86400; %convert time from days to seconds  
dt = Tnews(2) - Tnews(1);  
[fk,powerNor] = EnergySpec(BD48_1098(:,1),BD48_1098(:,2),dt);
```



```

N = length(BD48_1098(:,1));
F = nufft(BD48_1098(:,1),BD48_1098(:,2) )/N;
F0 = fftshift(F);

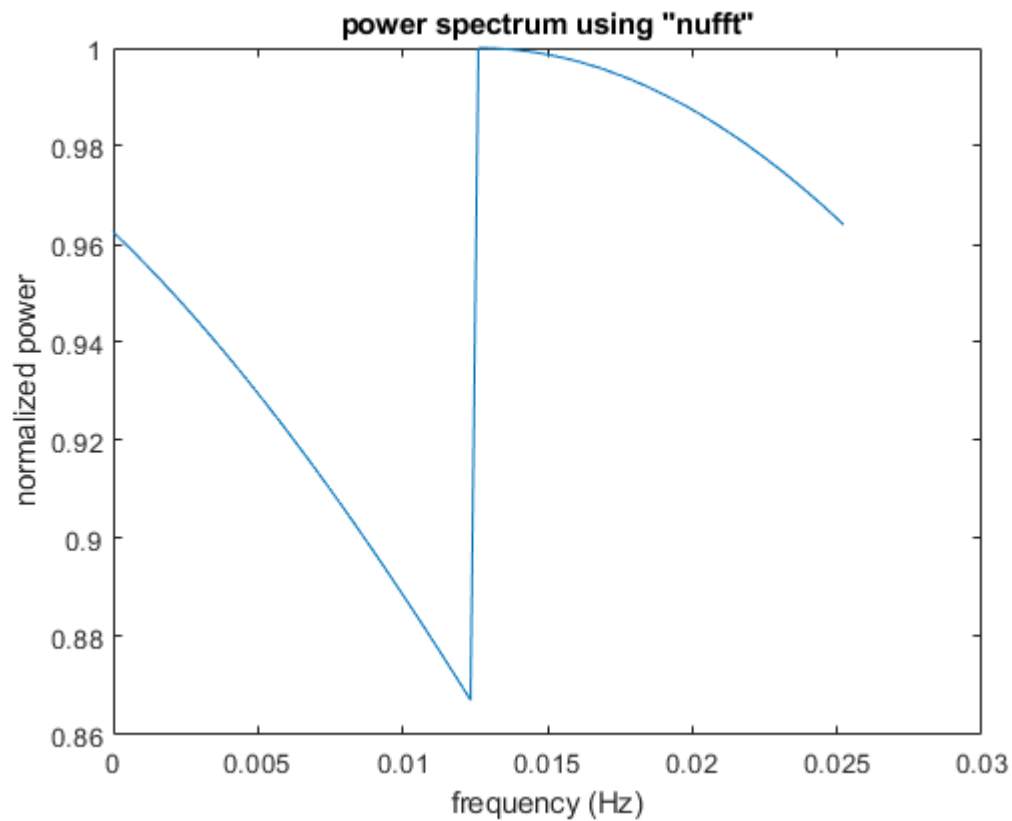
power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')

```



```
key_freq = 0.01275
```

```
key_freq =  
    0.0127500000000000
```

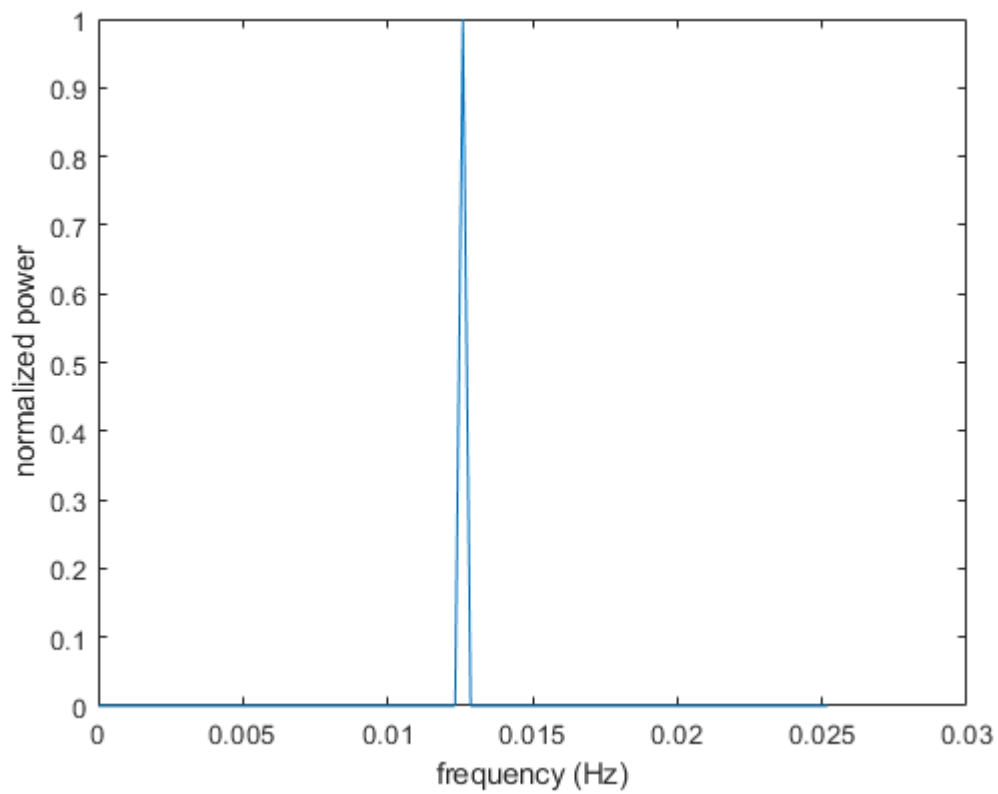
```
avg_freq = 1/( mean( diff(BD48_1098(:,1)) ) * 86400 )
```

```
avg_freq =  
    0.025491165955887
```

```
avg_freq/key_freq
```

```
ans =  
    1.999307133795079
```

```
%R  
avg_freq = 1/( mean( diff(BD48_1098(:,3)) ) * 86400 );  
  
[Tnew,Mnew] = Interp_spline(BD48_1098(:,3),BD48_1098(:,4));  
Tnews = Tnew*86400; %convert time from days to seconds  
dt = Tnews(2) - Tnews(1);  
[fk,powerNor] = EnergySpec(BD48_1098(:,3),BD48_1098(:,4),dt);
```



```

N = length(BD48_1098(:,3));
F = nufft(BD48_1098(:,3),BD48_1098(:,4) )/N;
F0 = fftshift(F);

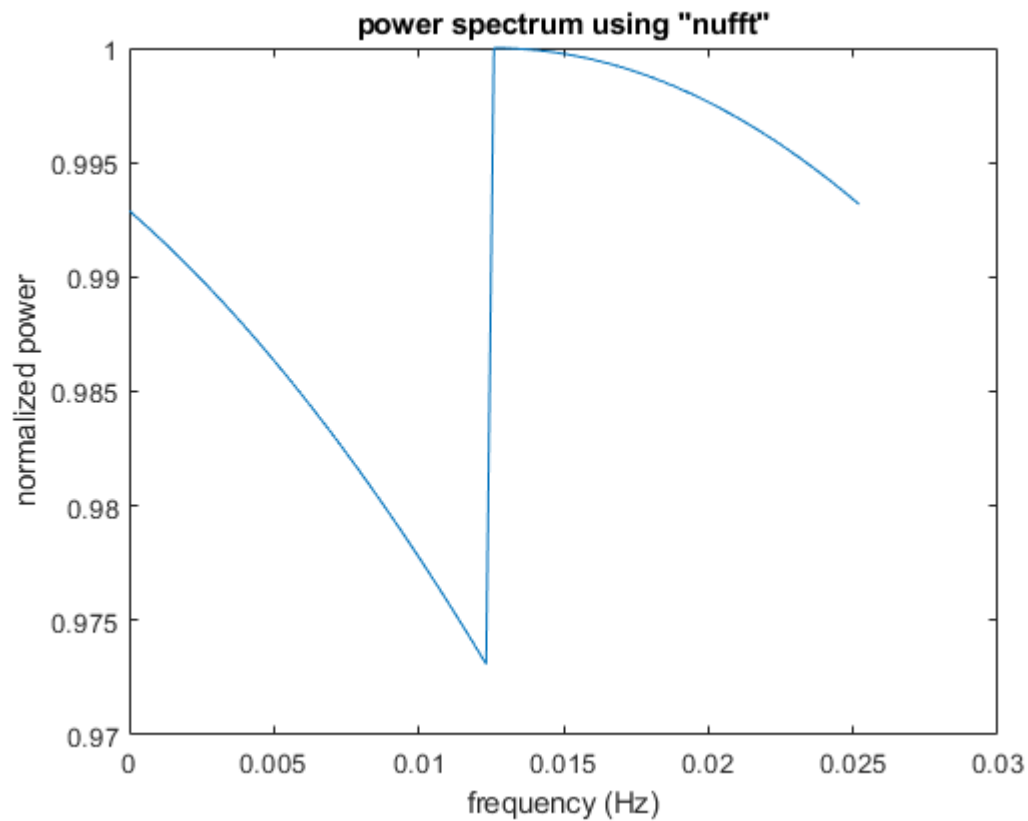
power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')

```

```
key_freq = 0.0125967
```

```
key_freq =  
0.012596700000000
```

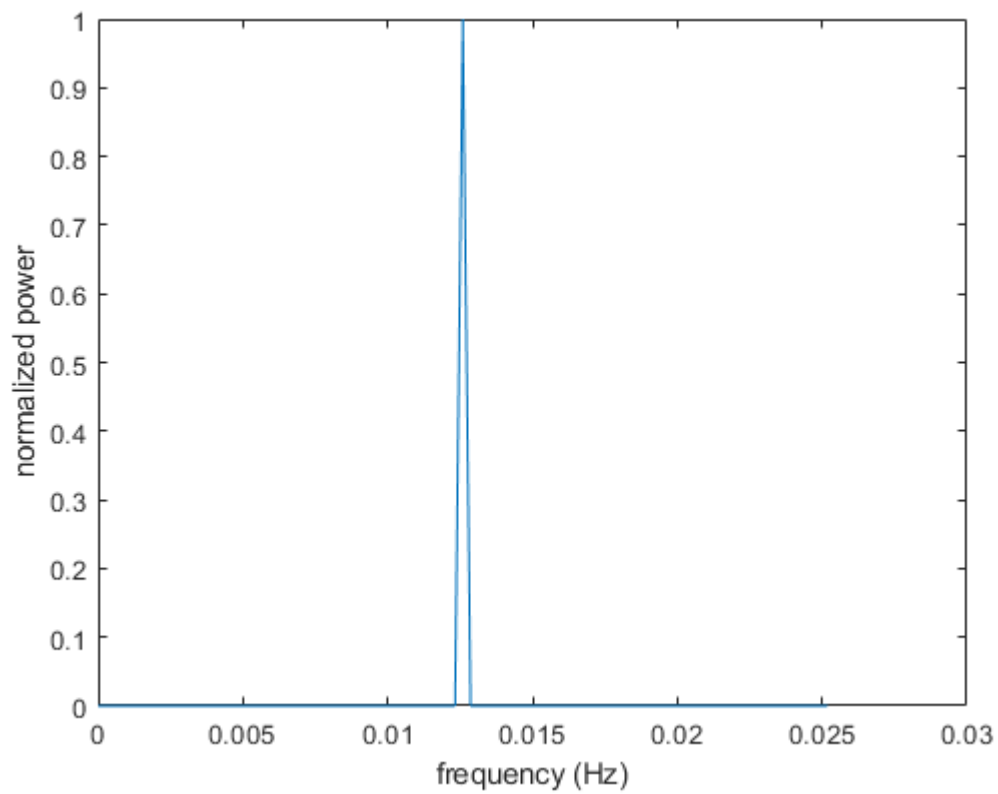
```
avg_freq =1/( mean( diff(BD48_1098(:,3)) ) *86400 )
```

```
avg_freq =  
0.025461337770577
```

```
avg_freq/key_freq
```

```
ans =  
2.021270473264992
```

```
%V  
avg_freq =1/( mean( diff(BD48_1098(:,5)) ) *86400 );  
  
[Tnew,Mnew] = Interp_spline(BD48_1098(:,5),BD48_1098(:,6));  
Tnews = Tnew*86400; %convert time from days to seconds  
dt = Tnews(2) - Tnews(1);  
[fk,powerNor] = EnergySpec(BD48_1098(:,5),BD48_1098(:,6),dt);
```



```

N = length(BD48_1098(:,5));
F = nufft(BD48_1098(:,5),BD48_1098(:,6) )/N;
F0 = fftshift(F);

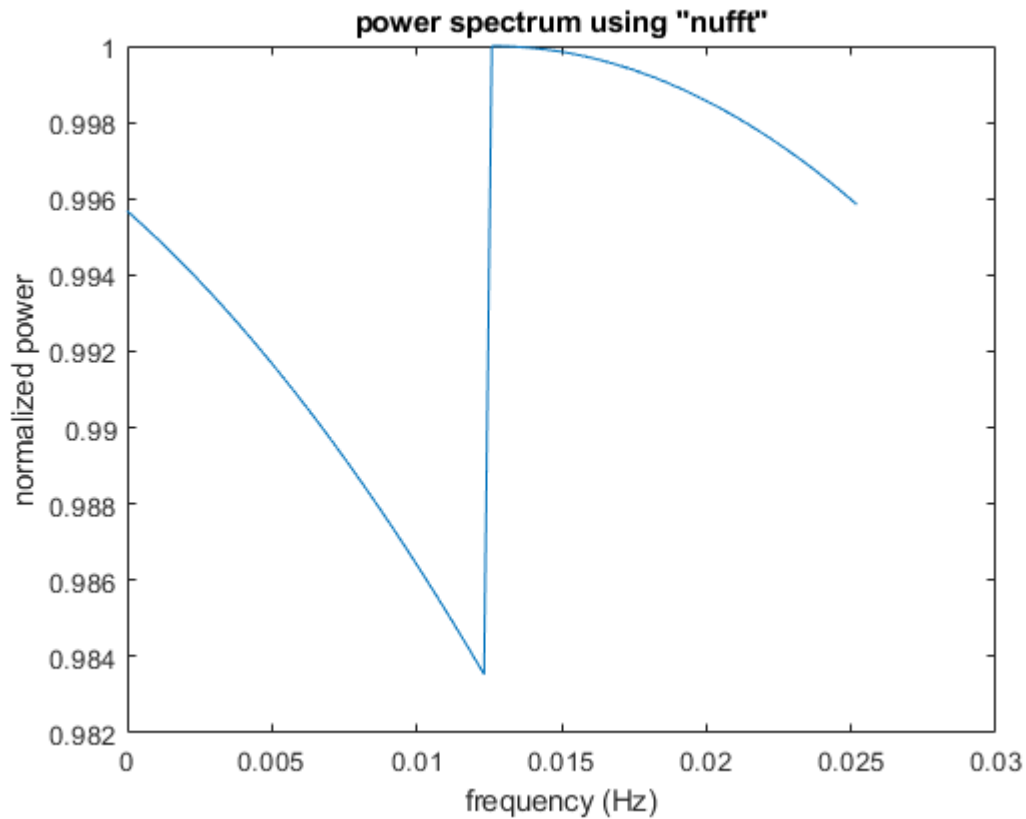
power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')

```



```
key_freq = 0.0127234
```

```
key_freq =  
0.012723400000000
```

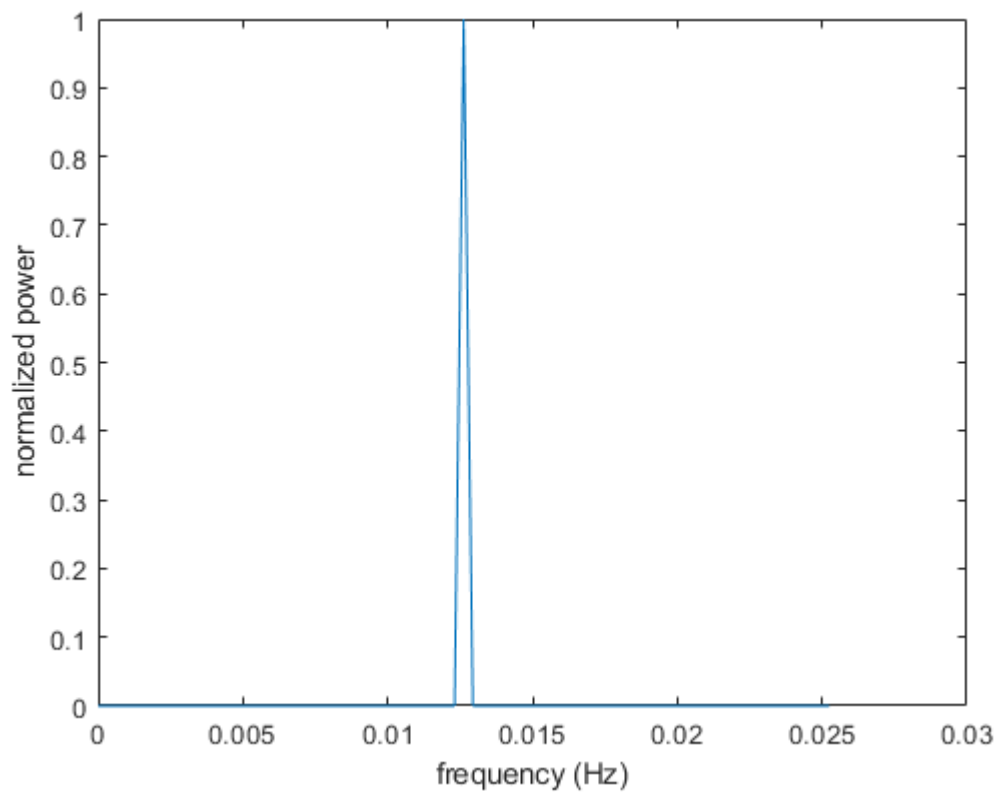
```
avg_freq = 1/( mean( diff(BD48_1098(:,5)) ) *86400 )
```

```
avg_freq =  
0.025455380510899
```

```
avg_freq/key_freq
```

```
ans =  
2.000674388205868
```

```
%BD5_441  
BD55_441 = BD55_441(2:end-1,:);  
%V  
avg_freq = 1/( mean( diff(BD55_441(:,5)) ) *86400 );  
  
[Tnew,Mnew] = Interp_spline(BD55_441(:,5),BD55_441(:,6));  
Tnews = Tnew*86400; %convert time from days to seconds  
dt = Tnews(2) - Tnews(1);  
[fk,powerNor] = EnergySpec(BD55_441(:,5),BD55_441(:,6),dt);
```



```

N = length(BD55_441(:,5));
F = nufft(BD55_441(:,5),BD55_441(:,6) )/N;
F0 = fftshift(F);

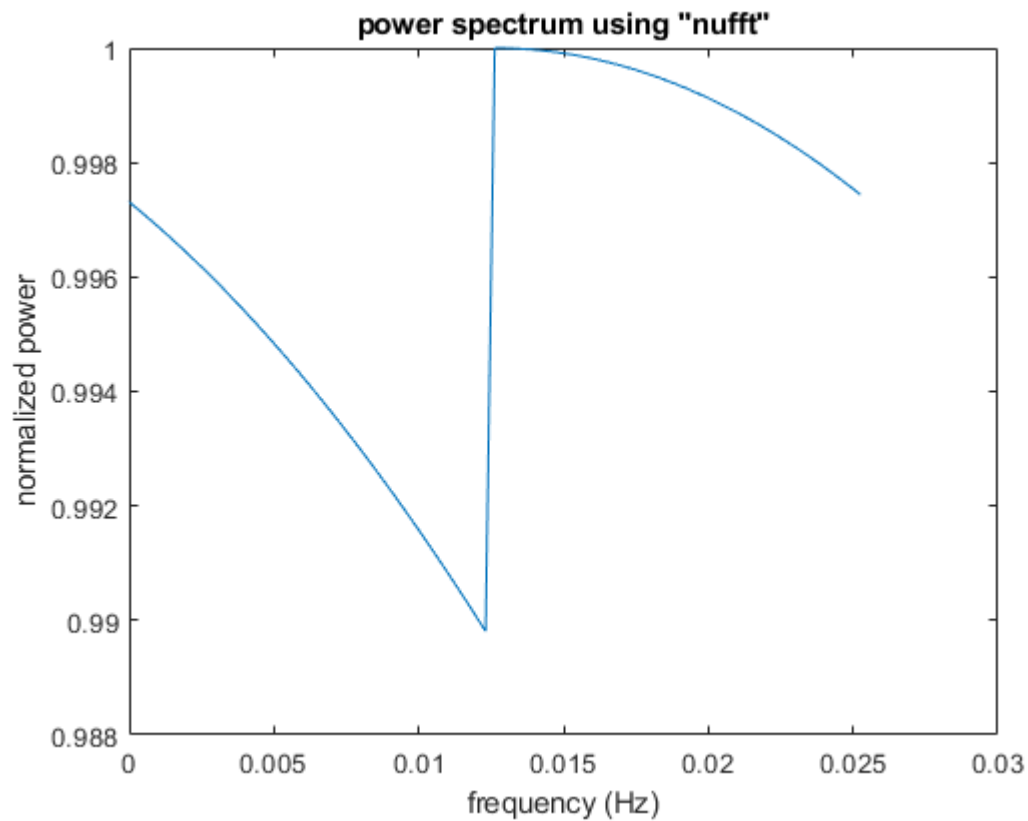
power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')

```



```
key_freq = 0.0127232
```

```
key_freq =  
0.012723200000000
```

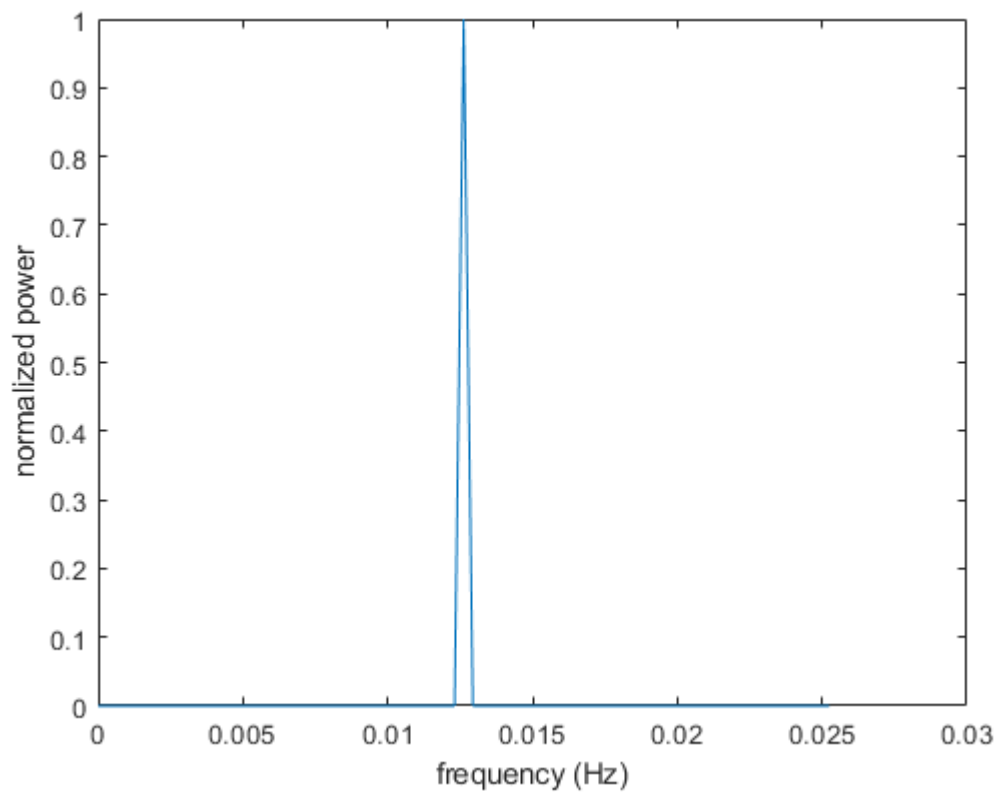
```
avg_freq =1/( mean( diff(BD55_441(:,5)) ) *86400 )
```

```
avg_freq =  
0.025563940526795
```

```
avg_freq/key_freq
```

```
ans =  
2.009238283355988
```

```
%B  
avg_freq =1/( mean( diff(BD55_441(:,1)) ) *86400 );  
  
[Tnew,Mnew] = Interp_spline(BD55_441(:,1),BD55_441(:,2));  
Tnews = Tnew*86400; %convert time from days to seconds  
dt = Tnews(2) - Tnews(1);  
[fk,powerNor] = EnergySpec(BD55_441(:,1),BD55_441(:,2),dt);
```



```

N = length(BD55_441(:,1));
F = nufft(BD55_441(:,1),BD55_441(:,2) )/N;
F0 = fftshift(F);

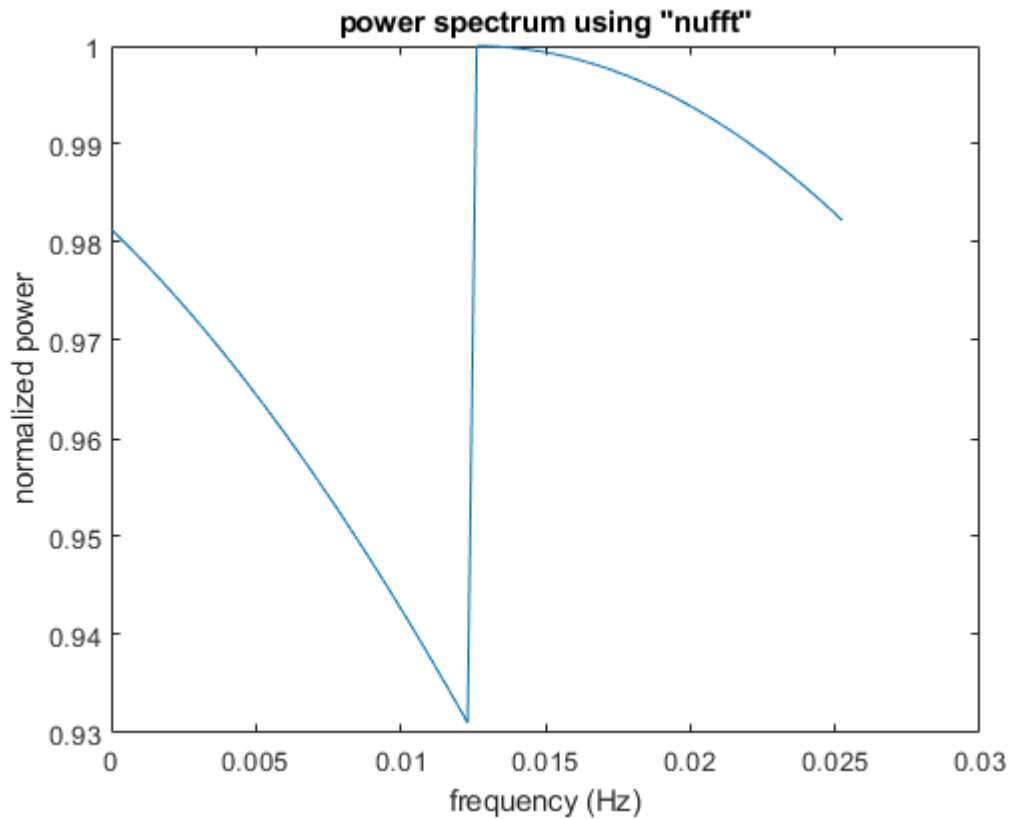
power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')

```



```
key_freq = 0.0127699
```

```
key_freq =  
0.0127699000000000
```

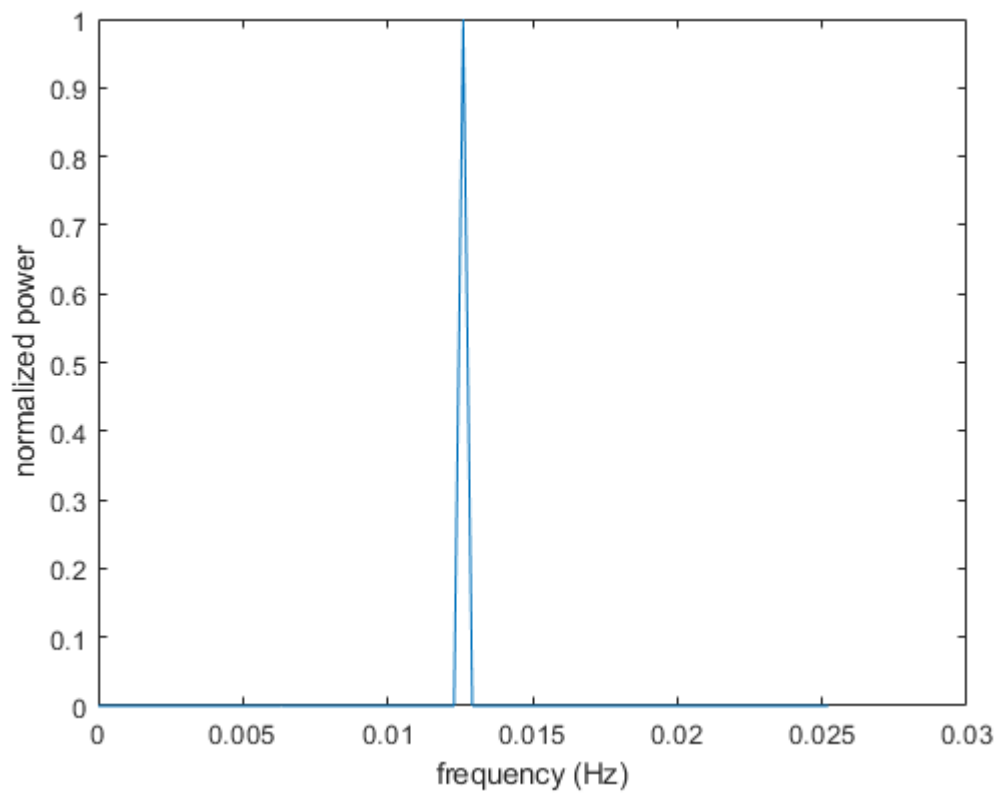
```
avg_freq =1/( mean( diff(BD55_441(:,1)) ) *86400 )
```

```
avg_freq =  
0.025563940526795
```

```
avg_freq/key_freq
```

```
ans =  
2.001890424106290
```

```
%R  
avg_freq =1/( mean( diff(BD55_441(:,3)) ) *86400 );  
  
[Tnew,Mnew] = Interp_spline(BD55_441(:,3),BD55_441(:,4));  
Tnews = Tnew*86400; %convert time from days to seconds  
dt = Tnews(2) - Tnews(1);  
[fk,powerNor] = EnergySpec(BD55_441(:,3),BD55_441(:,4),dt);
```



```

N = length(BD55_441(:,3));
F = nufft(BD55_441(:,3),BD55_441(:,4) )/N;
F0 = fftshift(F);

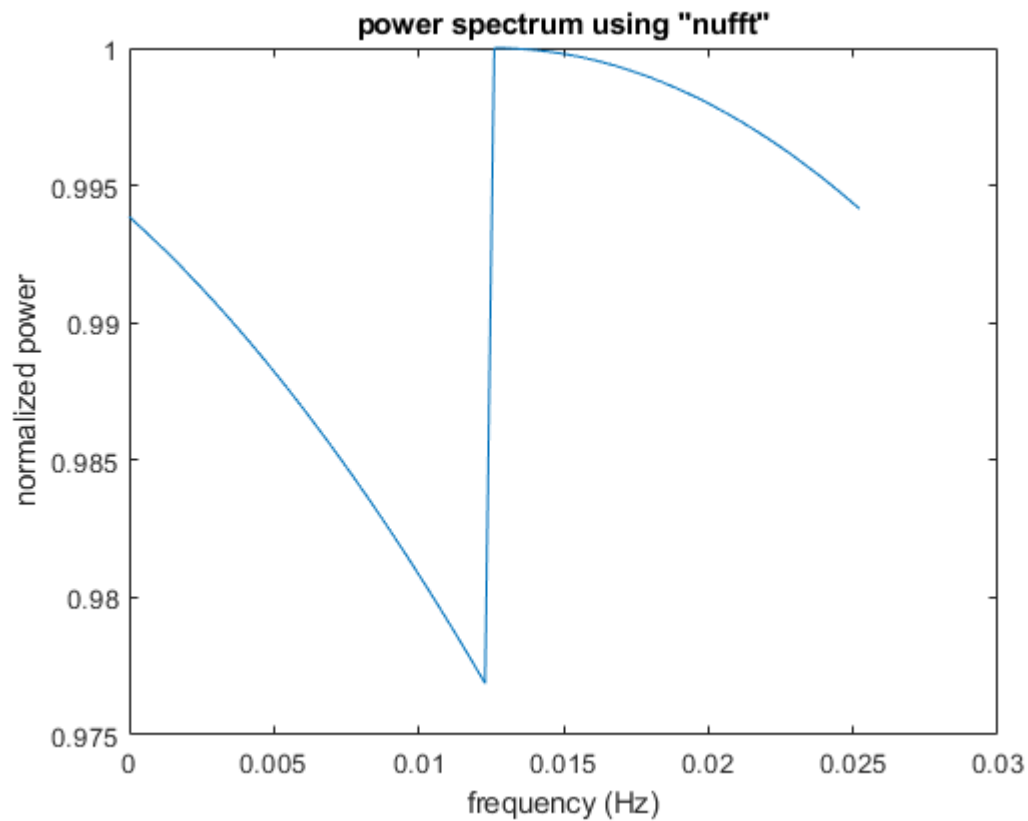
power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')

```

```
key_freq = 0.0127829
```

```
key_freq =  
0.0127829000000000
```

```
avg_freq =1/( mean( diff(BD55_441(:,3)) ) *86400 )
```

```
avg_freq =  
0.025528699366024
```

```
avg_freq/key_freq
```

```
ans =  
1.997097635593180
```

```
%HD28497
```

```
%B
```

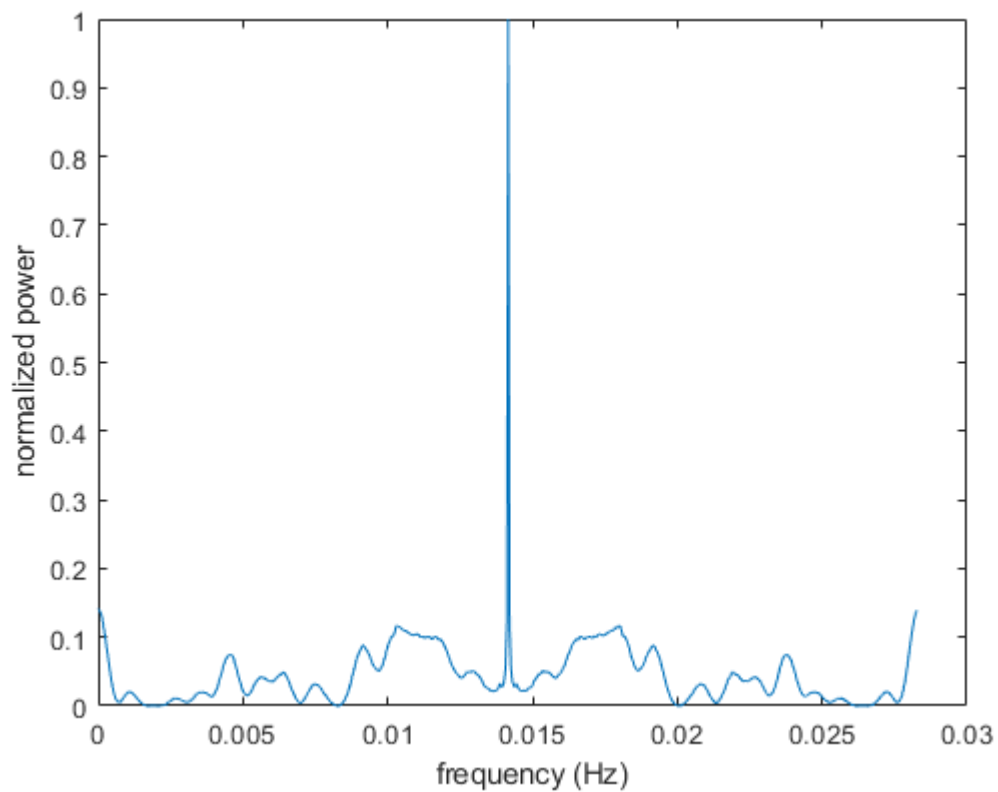
```
avg_freq =1/( mean( diff(HD28497(:,1)) ) *86400 );
```

```
[Tnew,Mnew] = Interp_spline(HD28497(:,1),HD28497(:,2));
```

```
Tnews = Tnew*86400; %convert time from days to seconds
```

```
dt = Tnews(2) - Tnews(1);
```

```
[fk,powerNor] = EnergySpec(HD28497(:,1),HD28497(:,2),dt);
```



```

N = length(HD28497(:,1));
F = nufft(HD28497(:,1),HD28497(:,2) )/N;
F0 = fftshift(F);

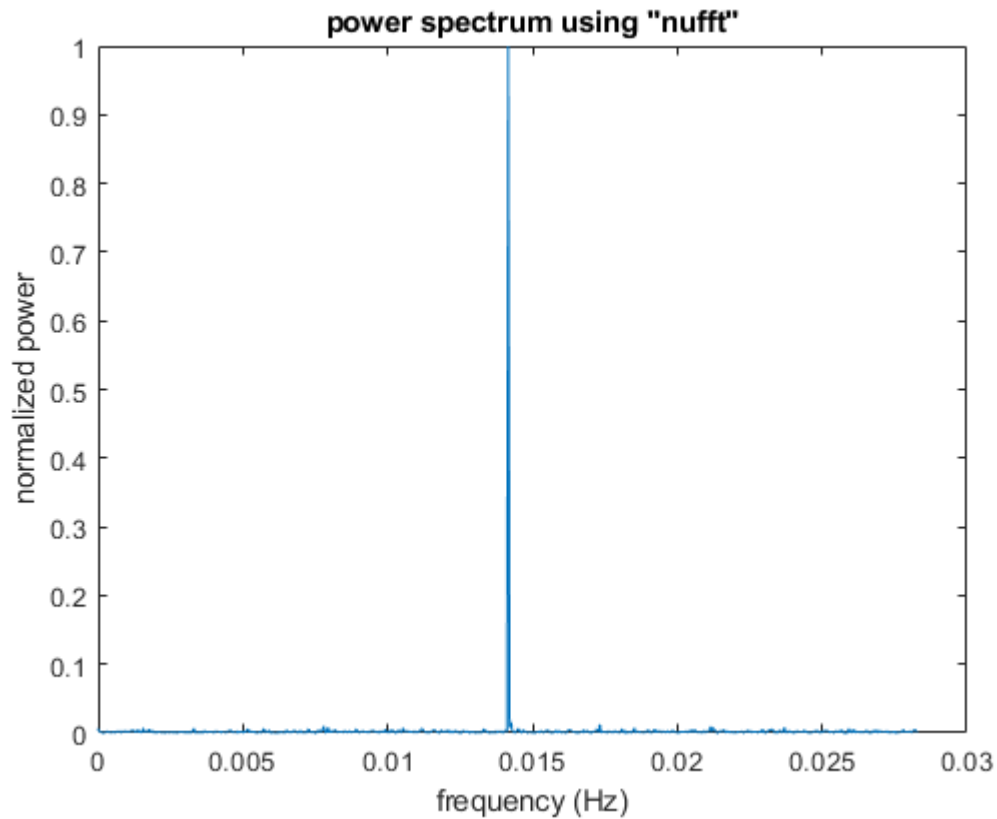
power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')

```



```
key_freq = 0.0141626
```

```
key_freq =  
0.0141626000000000
```

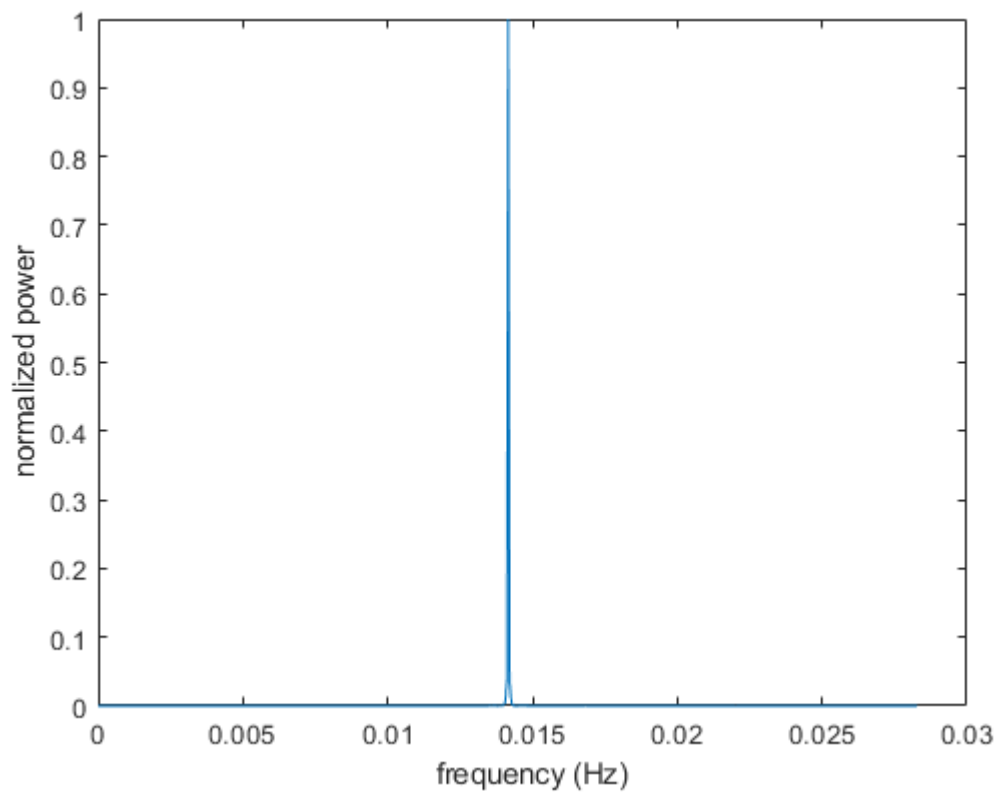
```
avg_freq =1/( mean( diff(HD28497(:,1)) ) *86400 )
```

```
avg_freq =  
0.028325177195336
```

```
avg_freq/key_freq
```

```
ans =  
1.999998389796817
```

```
%R  
avg_freq =1/( mean( diff(HD28497(:,3)) ) *86400 );  
  
[Tnew,Mnew] = Interp_spline(HD28497(:,3),HD28497(:,4));  
Tnews = Tnew*86400; %convert time from days to seconds  
dt = Tnews(2) - Tnews(1);  
[fk,powerNor] = EnergySpec(HD28497(:,3),HD28497(:,4),dt);
```



```

N = length(HD28497(:,3));
F = nufft(HD28497(:,3),HD28497(:,4) )/N;
F0 = fftshift(F);

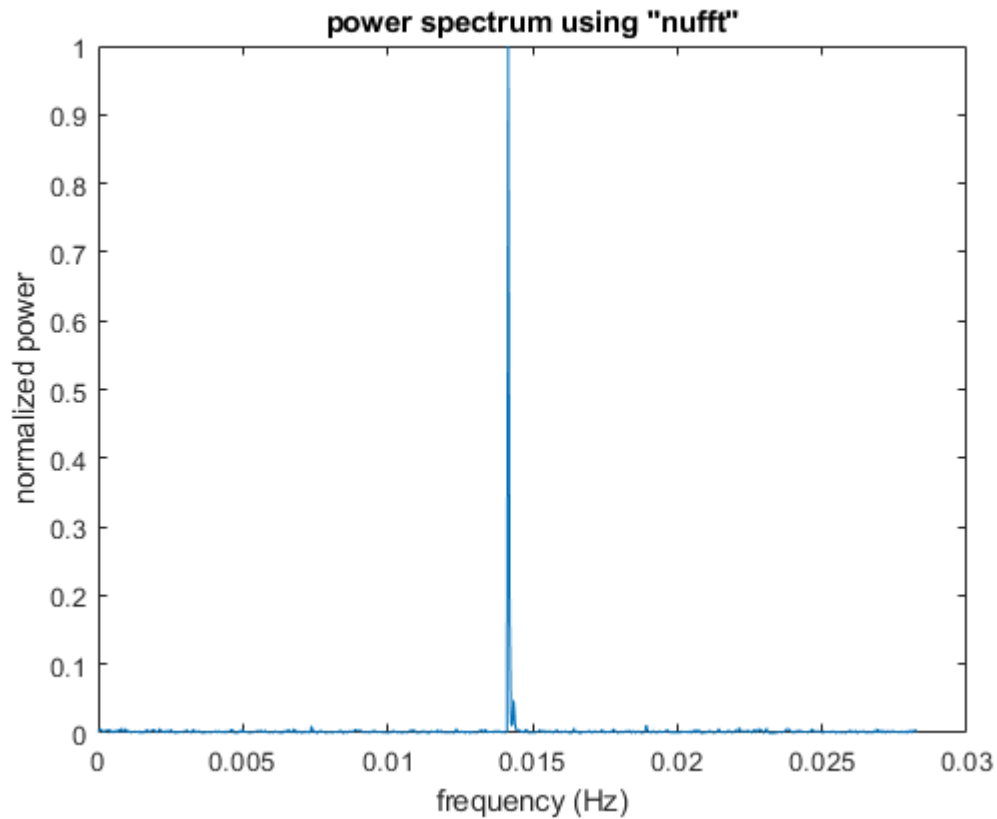
power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')

```



```
key_freq = 0.0141626
```

```
key_freq =  
0.014162600000000
```

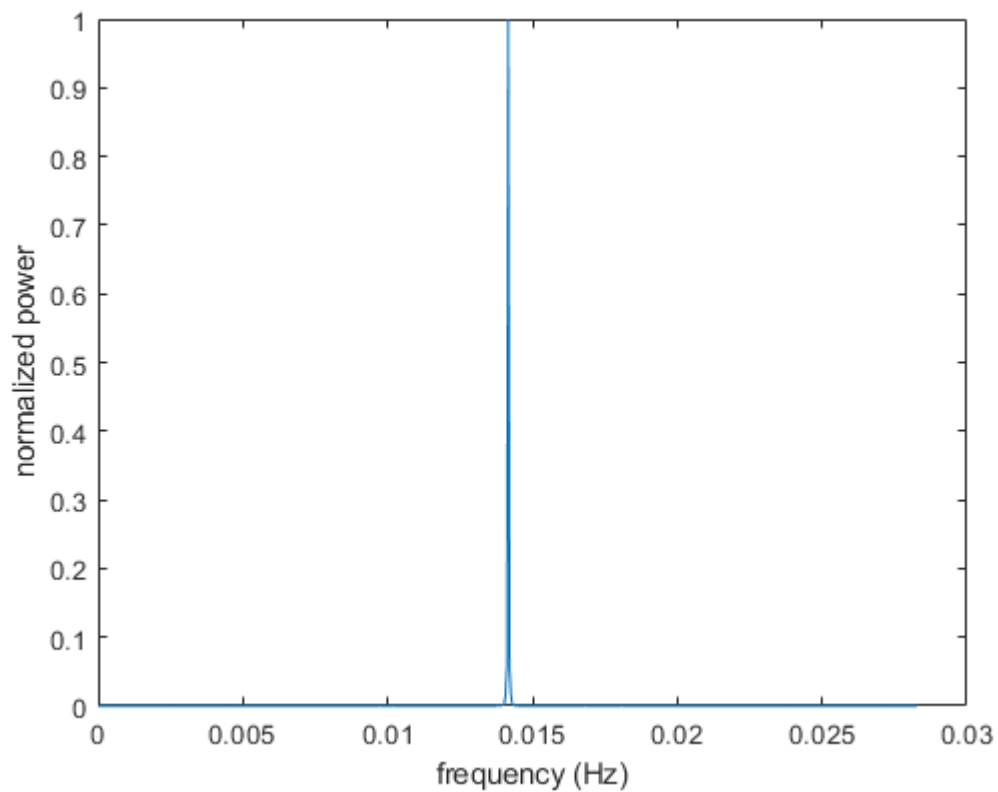
```
avg_freq = 1/( mean( diff(HD28497(:,3)) ) * 86400 )
```

```
avg_freq =  
0.028325177196178
```

```
avg_freq/key_freq
```

```
ans =  
1.99998389856271
```

```
%V  
avg_freq = 1/( mean( diff(HD28497(:,5)) ) * 86400 );  
  
[Tnew,Mnew] = Interp_spline(HD28497(:,5),HD28497(:,6));  
Tnews = Tnew*86400; %convert time from days to seconds  
dt = Tnews(2) - Tnews(1);  
[fk,powerNor] = EnergySpec(HD28497(:,5),HD28497(:,6),dt);
```



```

N = length(HD28497(:,5));
F = nufft(HD28497(:,5),HD28497(:,6) )/N;
F0 = fftshift(F);

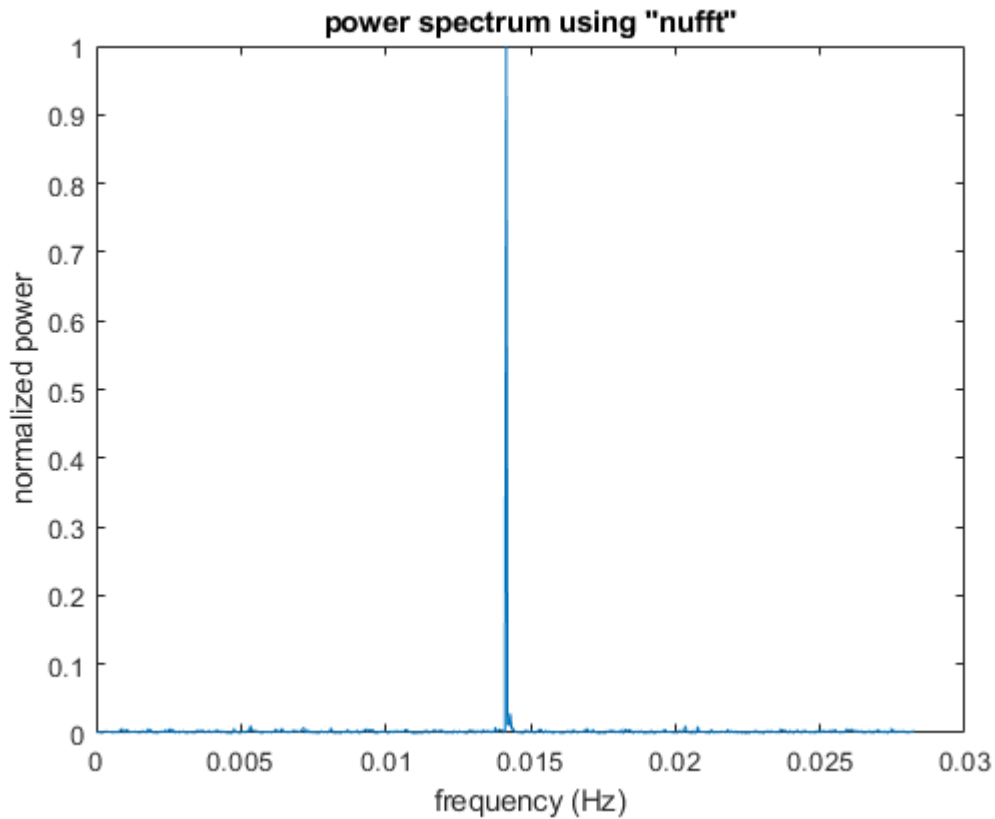
power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')

```



```
key_freq = 0.0141626
```

```
key_freq =  
0.014162600000000
```

```
avg_freq = 1/( mean( diff(HD28497(:,5)) ) * 86400 )
```

```
avg_freq =  
0.028325177195336
```

```
avg_freq/key_freq
```

```
ans =  
1.999998389796817
```

```
%HD152060
```

```
%R
```

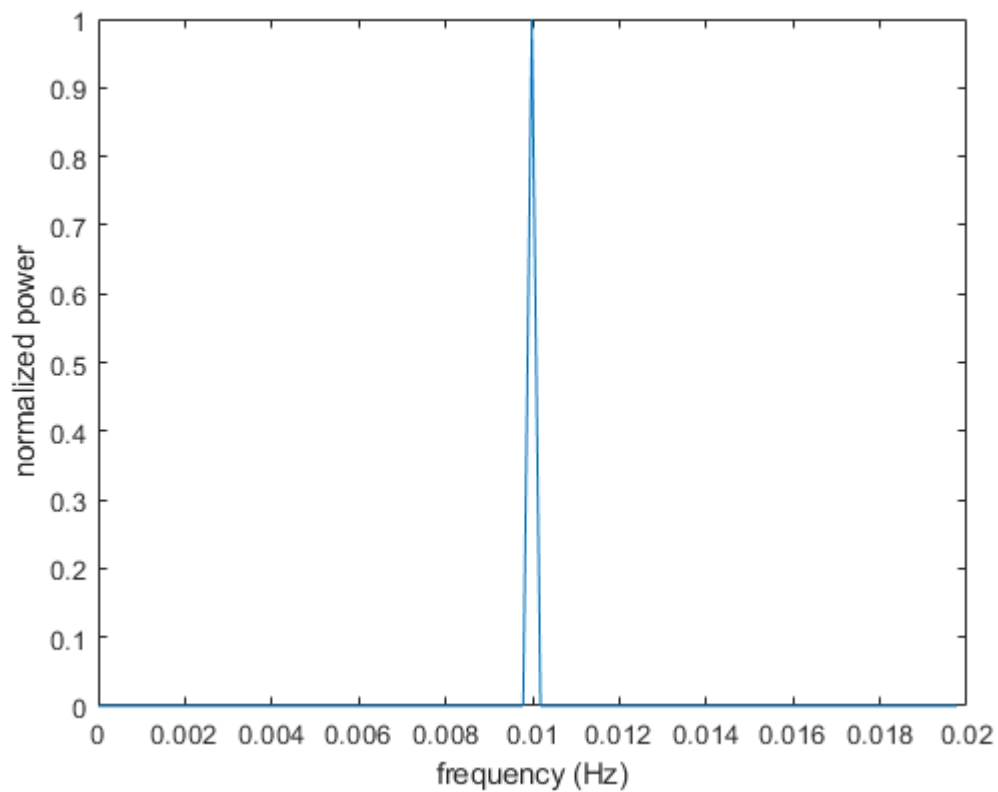
```
avg_freq = 1/( mean( diff(HD152060(:,1)) ) * 86400 );
```

```
[Tnew,Mnew] = Interp_spline(HD152060(:,1),HD152060(:,2));
```

```
Tnews = Tnew*86400; %convert time from days to seconds
```

```
dt = Tnews(2) - Tnews(1);
```

```
[fk,powerNor] = EnergySpec(HD152060(:,1),HD152060(:,2),dt);
```



```

N = length(HD152060(:,1));
F = nufft(HD152060(:,1),HD152060(:,2) )/N;
F0 = fftshift(F);

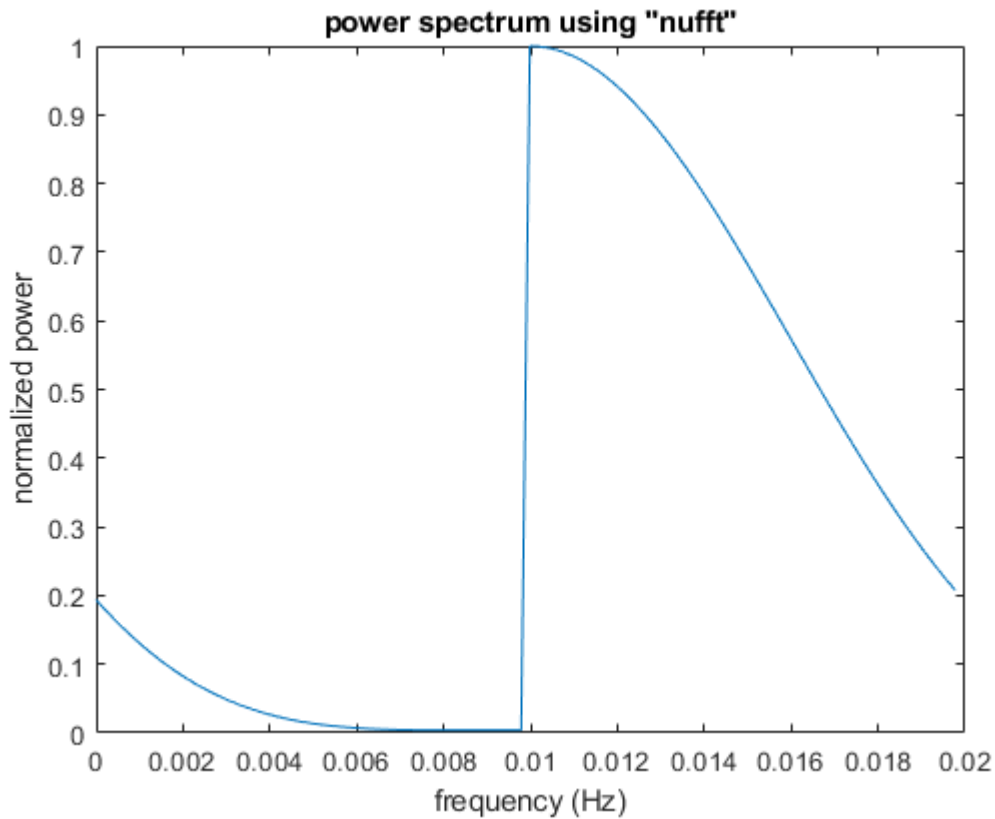
power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')

```

```
key_freq = 0.00998548
```

```
key_freq =  
0.009985480000000
```

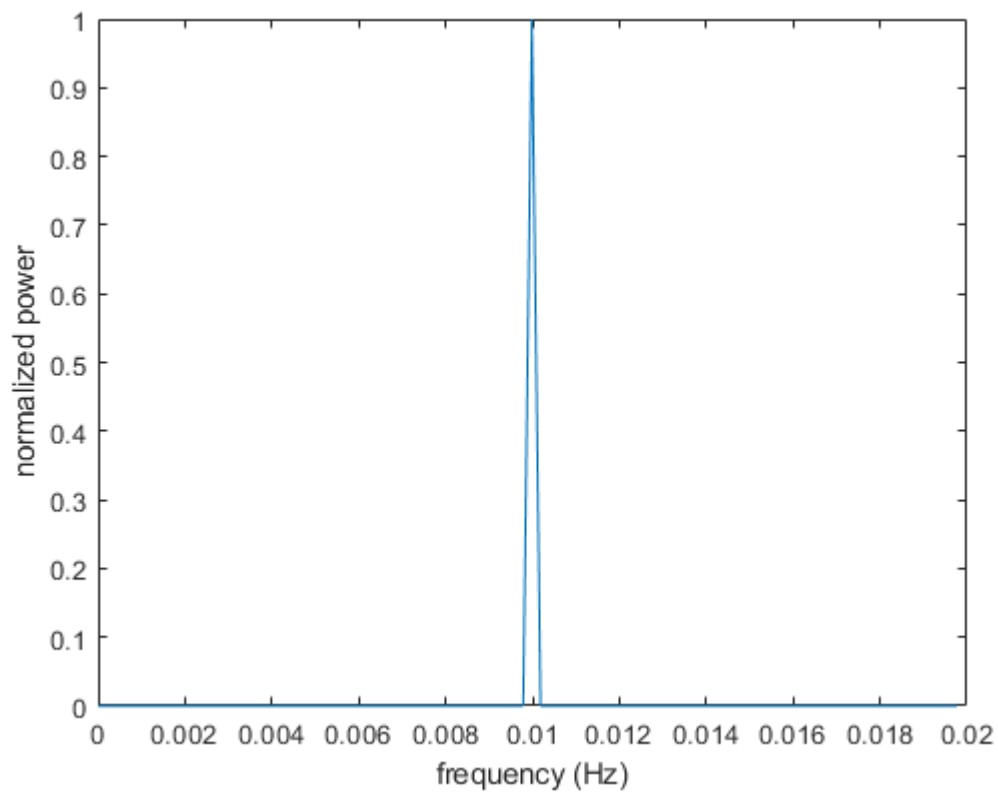
```
avg_freq =1/( mean( diff(HD152060(:,1)) ) *86400 )
```

```
avg_freq =  
0.019970951344655
```

```
avg_freq/key_freq
```

```
ans =  
1.999999133206939
```

```
%V  
avg_freq =1/( mean( diff(HD152060(:,3)) ) *86400 );  
  
[Tnew,Mnew] = Interp_spline(HD152060(:,3),HD152060(:,4));  
Tnews = Tnew*86400; %convert time from days to seconds  
dt = Tnews(2) - Tnews(1);  
[fk,powerNor] = EnergySpec(HD152060(:,3),HD152060(:,4),dt);
```



```

N = length(HD152060(:,3));
F = nufft(HD152060(:,3),HD152060(:,4) )/N;
F0 = fftshift(F);

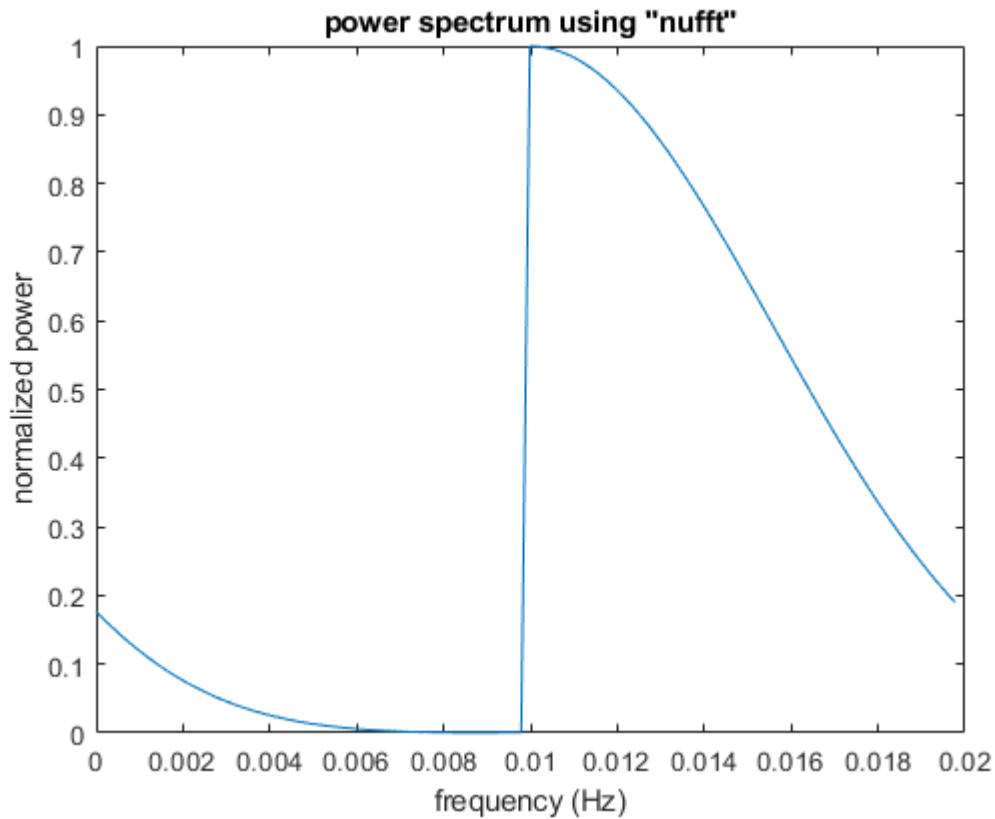
power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')

```



```
key_freq = 0.00998635
```

```
key_freq =  
0.009986350000000
```

```
avg_freq = 1/( mean( diff(HD152060(:,3)) ) * 86400 )
```

```
avg_freq =  
0.019972691882309
```

```
avg_freq/key_freq
```

```
ans =  
1.999999187121354
```

```
%HD209522
```

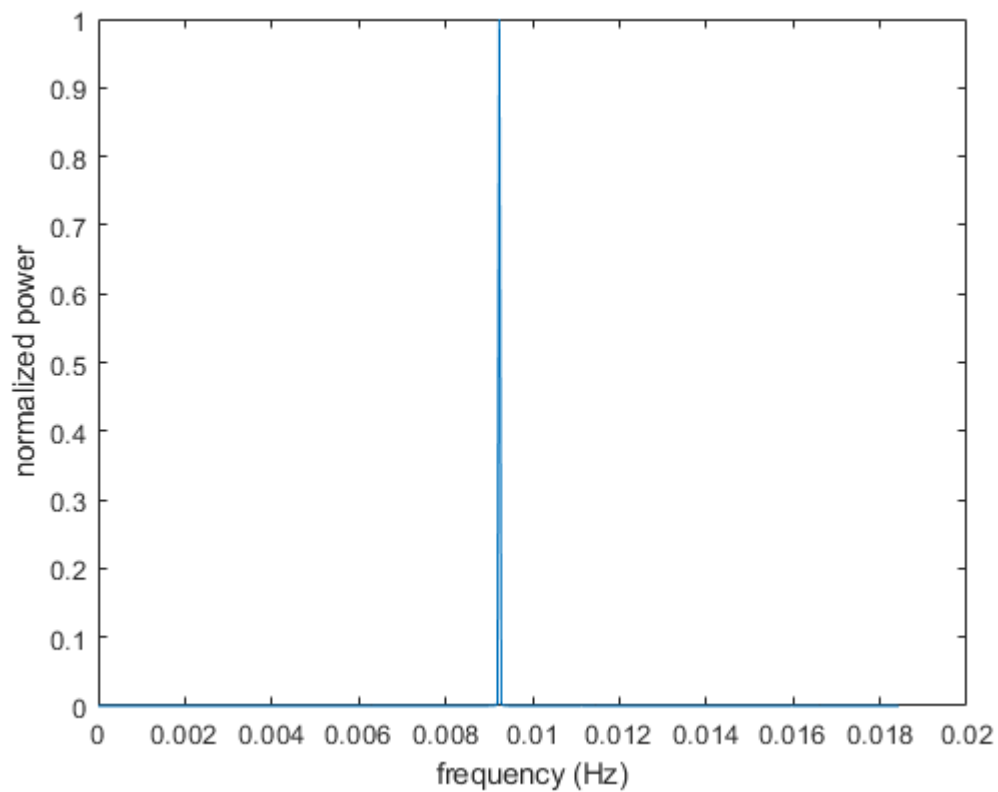
```
avg_freq = 1/( mean( diff(HD209522(:,1)) ) * 86400 );
```

```
[Tnew,Mnew] = Interp_spline(HD209522(:,1),HD209522(:,2));
```

```
Tnews = Tnew*86400; %convert time from days to seconds
```

```
dt = Tnews(2) - Tnews(1);
```

```
[fk,powerNor] = EnergySpec(HD209522(:,1),HD209522(:,2),dt);
```



```

N = length(HD209522(:,1));
F = nufft(HD209522(:,1),HD209522(:,2) )/N;
F0 = fftshift(F);

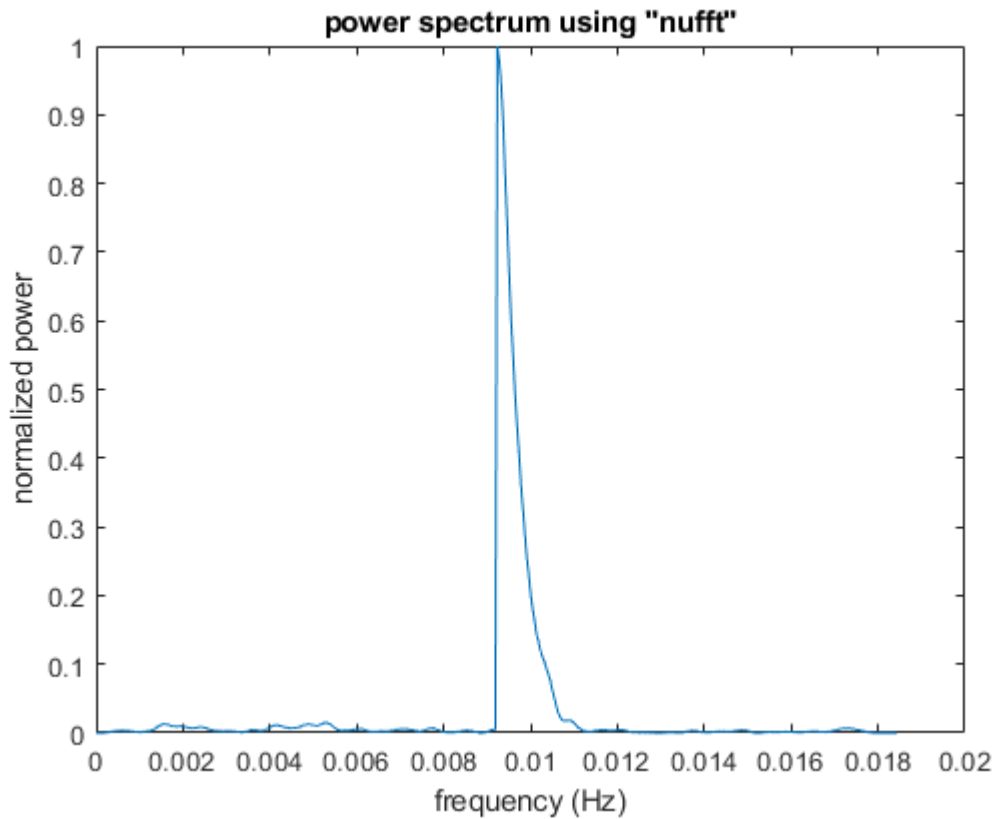
power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')

```



```
key_freq = 0.00923606
```

```
key_freq =  
0.009236060000000
```

```
avg_freq = 1/( mean( diff(HD209522(:,1)) ) * 86400 )
```

```
avg_freq =  
0.018472115837205
```

```
avg_freq/key_freq
```

```
ans =  
1.999999549288869
```

Interpolation Functions

There are two different linear interpolation functions - the first is without built-in functions and the other is built-in. The results from both functions are similar.

Other interpolation methods are displayed.

Custom functions

```
function [Tnew,Mnew] = Interp_Lin(T,M)  
%This is Joe's custom linear interpolation:  
%----
```

```

% --Sum all of the time differences between measurements--
n = numel(T);
sum = 0;
for l = 1:n-1
    sum = sum + abs(T(l+1) - T(l));
end

% --Find averaged time scale--
avg_dT = sum / (n-1);
Tnew = T(1):avg_dT:T(n);

% --Calculate Mnew values--
m = numel(Tnew);
Mnew = zeros(1,m);

Mnew(1) = M(1);
Mnew(m) = M(n);

for l = 2:m-1
    for k = 1:n
        if T(k) <= Tnew(l)
            if Tnew(l) <= T(k+1)
                Mnew(l) = (M(k+1) - M(k))./(T(k+1) - T(k)).*(Tnew(l)-T(k)) + M(k);
                %eq for a line. i.e. y = mx + b
            end
        end
    end
end
end

end

```

Various built-in Matlab Functions

```

function [Tnew,Mnew] = Interp_nearest(T,M)
%This uses the built-in function 'interp1' with method 'nearest'
%----

% --Sum all of the time differences between measurements--
n = numel(T);
sum = 0;
for l = 1:n-1
    sum = sum + abs(T(l+1) - T(l));
end

% --Find averaged time scale--
avg_dT = sum / (n-1);
Tnew = T(1):avg_dT:T(n);

% --Calculate Mnew values--
Mnew = interp1(T,M,Tnew,'nearest');
end

```

```

function [Tnew,Mnew] = Interp_linear(T,M)
%This uses the built-in function 'interp1' with method 'linear'
%----

% --Sum all of the time differences between measurements--
n = numel(T);
sum = 0;
for l = 1:n-1
    sum = sum + abs(T(l+1) - T(l));
end

% --Find averaged time scale--
avg_dT = sum / (n-1);
Tnew = T(1):avg_dT:T(n);

%--Calculate Mnew values--
Mnew = interp1(T,M,Tnew,'linear');
end

```

```

function [Tnew,Mnew] = Interp_spline(T,M)
%This uses the built-in function 'interp1' with method 'spline'
%----

% --Sum all of the time differences between measurements--
n = numel(T);
sum = 0;
for l = 1:n-1
    sum = sum + abs(T(l+1) - T(l));
end

% --Find averaged time scale--
avg_dT = sum / (n-1);
Tnew = T(1):avg_dT:T(n);

% --Calculate Mnew values--
Mnew = interp1(T,M,Tnew,'spline');
end

```

```

function [Tnew,Mnew] = Interp_polyfit(T,M)
%This uses the built-in function 'interp1' with method 'polyfit'
%----

% --Sum all of the time differences between measurements--
n = numel(T);
sum = 0;
for l = 1:n-1
    sum = sum + abs(T(l+1) - T(l));
end

```

```

% --Find averaged time scale--
avg_dT = sum / (n-1);
Tnew = T(1):avg_dT:T(n);

% --Calculate Mnew values--
n = numel(T);
p = polyfit(T,M,5);
Mnew = polyval(p,Tnew);
end

```

Joe's linear combo of non-linear functions function

```

function C = NLfit(F1,F2,F3,x,y)
%documentation: This program was developed from Gilat example 6-9

F1 = F1(x);
F2 = F2(x);
F3 = F3(x);

A(1,1) = sum(F1 .* F1);
A(1,2) = sum(F1 .* F2);
A(1,3) = sum(F1 .* F3);
A(2,2) = sum(F2 .* F2);
A(2,3) = sum(F2 .* F3);
A(3,3) = sum(F3 .* F3);

A(2,1) = A(1,2);    % A is symmetric
A(3,1) = A(1,3);
A(3,2) = A(2,3);

B(1,1) = sum(y .* F1);
B(2,1) = sum(y .* F2);
B(3,1) = sum(y .* F3);

%form is A*C=B, Therefore,

C = A\B;

end

```

Joe's power spectrum function

```

function [fk,powerNor] = EnergySpec(t,f,dt)
%this function is developed with refeernce to Gilat Program 7-4 and Example
%7-6

N = length(f);
F = fft(f)/N;
F0 = fftshift(F);

power = F0.*conj(F0)/N;

powerNor = power/max(power);

```



```
%Plot power Spectrum
fs = 1/dt;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')

end
```