Research Techniques Project

Milestone 1 (6 October)

Data Exploration of BD+55_441

For this milestone, BD+55_441 is displayed and explored in detail. The other sources are briefly imported in upcoming sections.

```
opts = detectImportOptions("BD+55_441.txt");
opts.DataLines = 3;
opts.VariableNames = {'B_time', 'B_flux', 'R_time', 'R_flux', 'V_time', 'V_flux'};
```

"time" is in the units of days and "flux" is "rel_flux_T1" from AstroImageJ outputs.

```
opts.VariableTypes = {'double','double','double','double','double','double','double'};
preview("BD+55_441.txt",opts)
```

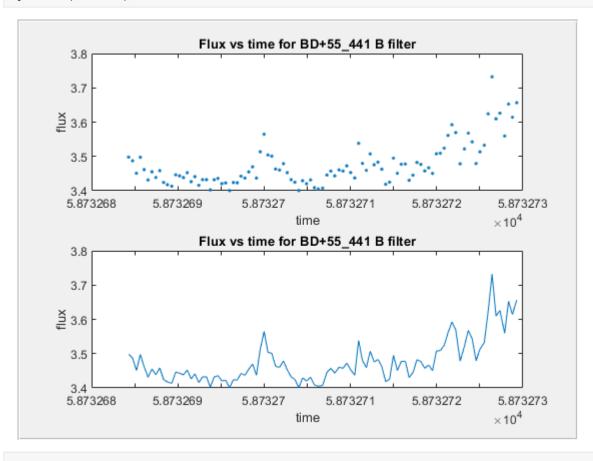
```
ans = 8 \times 6 table
           B time
                           B_flux
                                           R time
                                                           R flux
                                                                          V time
                                                                                          V flux
     5.873268430...
                        3.497996... 5.873268459...
                                                        1.961830... 5.873268445...
                                                                                        2.352058...
     5.873268430...
                        3.497996... 5.873268504...
                                                        1.942857... 5.873268490...
                                                                                        2.360458...
     5.873268475...
                        3.487289... 5.873268549...
                                                        1.947021... 5.873268535...
                                                                                        2.329957...
     5.873268520...
                        3.450942... 5.873268594...
                                                        1.930594... 5.873268580...
                                                                                        2.344889...
     5.873268565...
                        3.497567... 5.873268639...
                                                        1.942537... 5.873268625...
                                                                                        2.361048...
                                                        1.935141... 5.873268669...
     5.873268610...
                        3.461555... 5.873268684...
                                                                                        2.333341...
                                                        1.931290... 5.873268714...
                        3.431248... 5.873268729...
     5.873268655...
                                                                                        2.331904...
                                                        1.928260... 5.873268759...
     5.873268700...
                        3.455091... 5.873268774...
                                                                                        2.323782...
```

```
BD55_441 = readmatrix("BD+55_441.txt",opts);
whos BD55_441
```

```
Name Size Bytes Class Attributes
BD55 441 101x6 4848 double
```

```
hf_sub(1) = figure(1);
hp(1) = uipanel('Parent',hf_sub(1),'Position',[0 0 1 1]);
subplot(2,1,1,'Parent',hp(1));
plot(BD55_441(:,1),BD55_441(:,2),'.')
title('Flux vs time for BD+55\_441 B filter');
xlabel('time'),ylabel('flux');
subplot(2,1,2,'Parent',hp(1));
plot(BD55_441(:,1),BD55_441(:,2)),title('Flux vs time for BD+55\_441 B filter')
xlabel('time');
```

ylabel('flux');

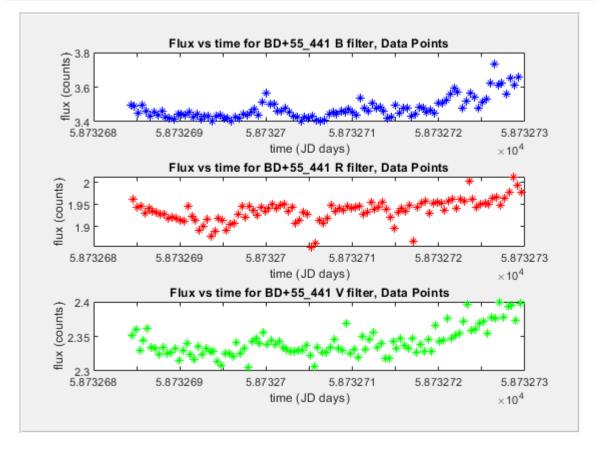


Noting the graph above - displayed in discrete points and as a line graph - there is some periodicity. There are peaks at 58732.70, 58732.711 and 58732.722.

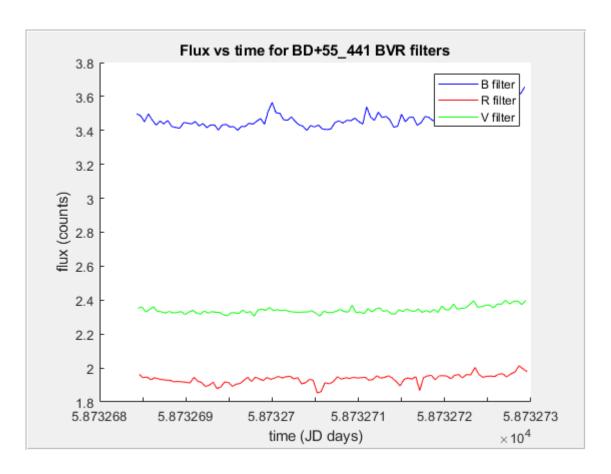
Periodicity between filters

```
hf_sub(2) = figure(2);
hp(2) = uipanel('Parent',hf_sub(2),'Position',[0 0 1 1]);
subplot(3,1,1,'Parent',hp(2));
% plotting in blue because B filter is blue light (~400-500 nm)
plot(BD55_441(:,1),BD55_441(:,2),'*b')
title('Flux vs time for BD+55\_441 B filter, Data Points');
xlabel('time (JD days)');
ylabel('flux (counts)');
```

```
subplot(3,1,2,'Parent',hp(2));
% plotting in red because R filter is red light (~550-800 nm)
plot(BD55_441(:,3),BD55_441(:,4),'*r');
title('Flux vs time for BD+55\_441 R filter, Data Points');
xlabel('time (JD days)');
ylabel('flux (counts)');
subplot(3,1,3,'Parent',hp(2));
% plotting green but V filter is visible light (~500-700 nm)
plot(BD55_441(:,5),BD55_441(:,6),'*g');
title('Flux vs time for BD+55\_441 V filter, Data Points');
xlabel('time (JD days)');
ylabel('flux (counts)');
```



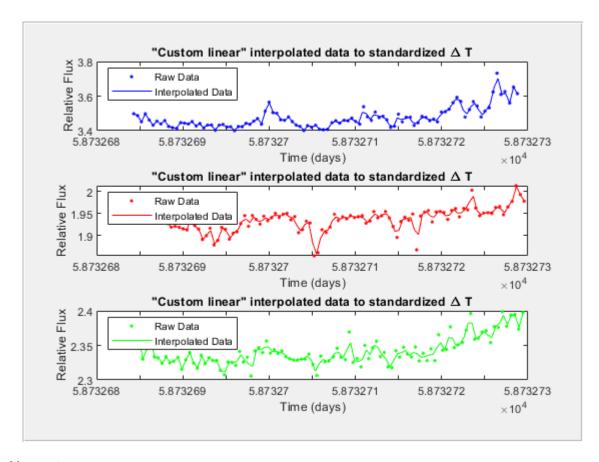
```
hf_sub(3) = figure(3);
hp(3) = uipanel('Parent',hf_sub(3),'Position',[0 0 1 1]);
subplot(1,1,1,'Parent',hp(3))
hold on
plot(BD55_441(:,1),BD55_441(:,2), 'b')
plot(BD55_441(:,3),BD55_441(:,4), 'r')
plot(BD55_441(:,5),BD55_441(:,6), 'g')
hold off
title('Flux vs time for BD+55\_441 BVR filters');
xlabel('time (JD days)');
legend('B filter', 'R filter', 'V filter');
ylabel('flux (counts)');
```



Interpolation investigation

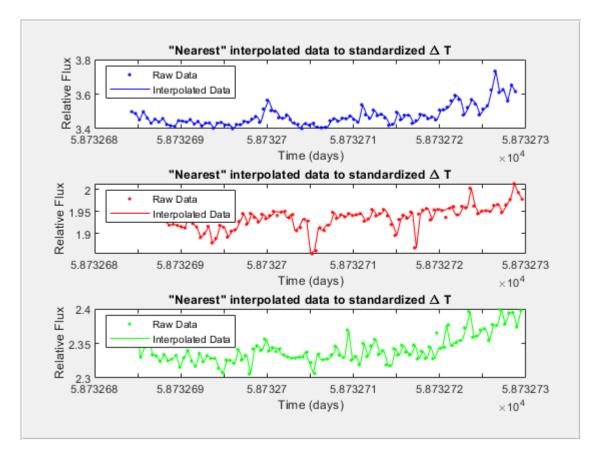
custom linear

```
hf sub(4) = figure(4);
hp(4) = uipanel('Parent', hf_sub(4), 'Position', [0 0 1 1]);
subplot(3,1,1,'Parent',hp(4));
[Tnew,Mnew] = Interp Lin(BD55 441(1:100,1),BD55 441(1:100,2));
plot(BD55_441(1:100,1),BD55_441(1:100,2),'.b',Tnew,Mnew,'b');
title('"Custom linear" interpolated data to standardized \Delta T');
legend('Raw Data','Interpolated Data','location','northwest');
xlabel('Time (days)');
ylabel('Relative Flux');
subplot(3,1,2,'Parent',hp(4));
[Tnew, Mnew] = Interp_Lin(BD55_441(1:100,3),BD55_441(1:100,4));
plot(BD55 441(1:100,3),BD55 441(1:100,4),'.r',Tnew,Mnew,'r');
title('"Custom linear" interpolated data to standardized \Delta T');
legend('Raw Data','Interpolated Data','location','northwest');
xlabel('Time (days)');
ylabel('Relative Flux');
subplot(3,1,3,'Parent',hp(4));
[Tnew,Mnew] = Interp Lin(BD55 441(1:100,5),BD55 441(1:100,6));
plot(BD55_441(1:100,5),BD55_441(1:100,6),'.g',Tnew,Mnew,'g');
title('"Custom linear" interpolated data to standardized \Delta T');
legend('Raw Data','Interpolated Data','location','northwest');
xlabel('Time (days)');
ylabel('Relative Flux');
```



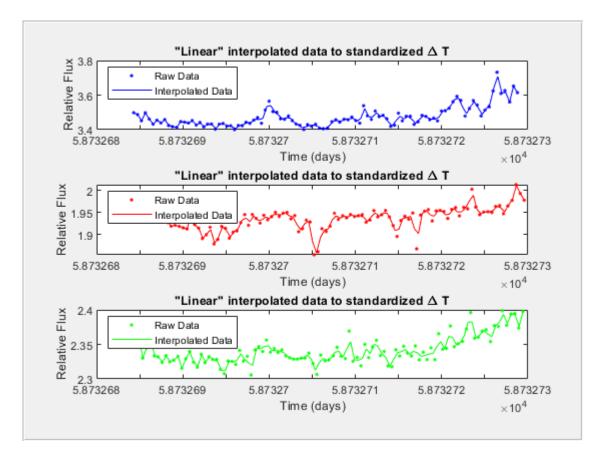
Nearest

```
hf sub(5) = figure(5);
hp(5) = uipanel('Parent', hf_sub(5), 'Position', [0 0 1 1]);
subplot(3,1,1,'Parent',hp(5));
[Tnew,Mnew] = Interp_nearest(BD55_441(2:100,1),BD55_441(2:100,2));
plot(BD55_441(1:100,1),BD55_441(1:100,2),'.b',Tnew,Mnew,'b');
title('"Nearest" interpolated data to standardized \Delta T');
legend('Raw Data','Interpolated Data','location','northwest');
xlabel('Time (days)');
ylabel('Relative Flux');
subplot(3,1,2,'Parent',hp(5));
[Tnew,Mnew] = Interp nearest(BD55 441(1:100,3),BD55 441(1:100,4));
plot(BD55_441(1:100,3),BD55_441(1:100,4),'.r',Tnew,Mnew,'r');
title('"Nearest" interpolated data to standardized \Delta T');
legend('Raw Data','Interpolated Data','location','northwest');
xlabel('Time (days)');
ylabel('Relative Flux');
subplot(3,1,3,'Parent',hp(5));
[Tnew,Mnew] = Interp nearest(BD55 441(1:100,5),BD55 441(1:100,6));
plot(BD55_441(1:100,5),BD55_441(1:100,6),'.g',Tnew,Mnew,'g');
title('"Nearest" interpolated data to standardized \Delta T');
legend('Raw Data','Interpolated Data','location','northwest');
xlabel('Time (days)');
ylabel('Relative Flux');
```



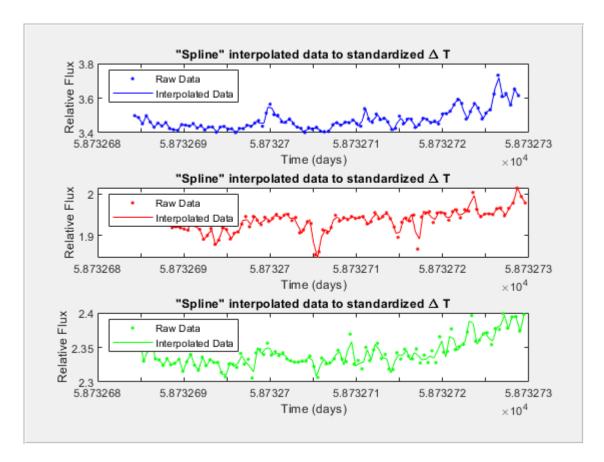
linear

```
hf sub(6) = figure(6);
hp(6) = uipanel('Parent', hf_sub(6), 'Position', [0 0 1 1]);
subplot(3,1,1,'Parent',hp(6));
[Tnew,Mnew] = Interp_linear(BD55_441(2:100,1),BD55_441(2:100,2));
plot(BD55_441(1:100,1),BD55_441(1:100,2),'.b',Tnew,Mnew,'b');
title('"Linear" interpolated data to standardized \Delta T');
legend('Raw Data','Interpolated Data','location','northwest');
xlabel('Time (days)');
ylabel('Relative Flux');
subplot(3,1,2,'Parent',hp(6));
[Tnew,Mnew] = Interp linear(BD55 441(1:100,3),BD55 441(1:100,4));
plot(BD55_441(1:100,3),BD55_441(1:100,4),'.r',Tnew,Mnew,'r');
title('"Linear" interpolated data to standardized \Delta T');
legend('Raw Data','Interpolated Data','location','northwest');
xlabel('Time (days)');
ylabel('Relative Flux');
subplot(3,1,3,'Parent',hp(6));
[Tnew,Mnew] = Interp linear(BD55 441(1:100,5),BD55 441(1:100,6));
plot(BD55_441(1:100,5),BD55_441(1:100,6),'.g',Tnew,Mnew,'g');
title('"Linear" interpolated data to standardized \Delta T');
legend('Raw Data','Interpolated Data','location','northwest');
xlabel('Time (days)');
ylabel('Relative Flux');
```



spline

```
hf sub(7) = figure(7);
hp(7) = uipanel('Parent', hf_sub(7), 'Position', [0 0 1 1]);
subplot(3,1,1,'Parent',hp(7));
[Tnew, Mnew] = Interp_spline(BD55_441(2:100,1),BD55_441(2:100,2));
plot(BD55_441(1:100,1),BD55_441(1:100,2),'.b',Tnew,Mnew,'b');
title('"Spline" interpolated data to standardized \Delta T');
legend('Raw Data','Interpolated Data','location','northwest');
xlabel('Time (days)');
ylabel('Relative Flux');
subplot(3,1,2,'Parent',hp(7));
[Tnew,Mnew] = Interp spline(BD55 441(1:100,3),BD55 441(1:100,4));
plot(BD55_441(1:100,3),BD55_441(1:100,4),'.r',Tnew,Mnew,'r');
title('"Spline" interpolated data to standardized \Delta T');
legend('Raw Data','Interpolated Data','location','northwest');
xlabel('Time (days)');
ylabel('Relative Flux');
subplot(3,1,3,'Parent',hp(7));
[Tnew,Mnew] = Interp spline(BD55 441(1:100,5),BD55 441(1:100,6));
plot(BD55_441(1:100,5),BD55_441(1:100,6),'.g',Tnew,Mnew,'g');
title('"Spline" interpolated data to standardized \Delta T');
legend('Raw Data','Interpolated Data','location','northwest');
xlabel('Time (days)');
ylabel('Relative Flux');
```



polyfit - needs to be conditioned appropriately.

```
hf_sub(8) = figure(8);
hp(8) = uipanel('Parent', hf_sub(8), 'Position', [0 0 1 1]);
subplot(3,1,1, 'Parent', hp(8));
[Tnew, Mnew] = Interp_polyfit(BD55_441(2:100,1), BD55_441(2:100,2));
```

Warning: Polynomial is badly conditioned. Add points with distinct X values, reduce the degree of the polynomial, or try centering and scaling as described in HELP POLYFIT.

```
plot(BD55_441(1:100,1),BD55_441(1:100,2),'.b',Tnew,Mnew,'b');
title('"Polyfit" interpolated data to standardized \Delta T');
legend('Raw Data','Interpolated Data','location','northwest');
xlabel('Time (days)');
ylabel('Relative Flux');
subplot(3,1,2,'Parent',hp(8));
[Tnew,Mnew] = Interp_polyfit(BD55_441(1:100,3),BD55_441(1:100,4));
```

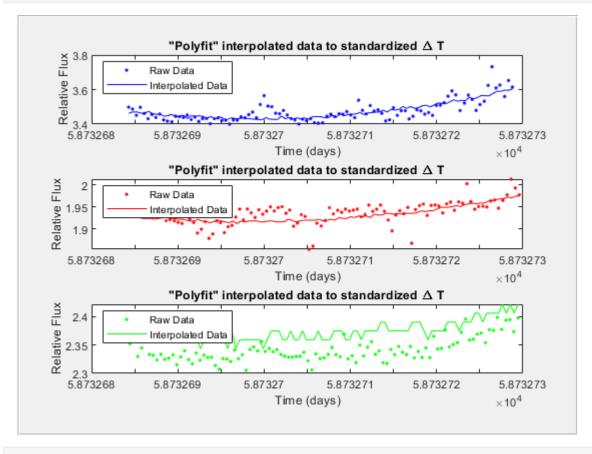
Warning: Polynomial is badly conditioned. Add points with distinct X values, reduce the degree of the polynomial, or try centering and scaling as described in HELP POLYFIT.

```
plot(BD55_441(1:100,3),BD55_441(1:100,4),'.r',Tnew,Mnew,'r');
title('"Polyfit" interpolated data to standardized \Delta T');
legend('Raw Data','Interpolated Data','location','northwest');
xlabel('Time (days)');
```

```
ylabel('Relative Flux');
subplot(3,1,3,'Parent',hp(8));
[Tnew,Mnew] = Interp_polyfit(BD55_441(1:100,5),BD55_441(1:100,6));
```

Warning: Polynomial is badly conditioned. Add points with distinct X values, reduce the degree of the polynomial, or try centering and scaling as described in HELP POLYFIT.

```
plot(BD55_441(1:100,5),BD55_441(1:100,6),'.g',Tnew,Mnew,'g');
title('"Polyfit" interpolated data to standardized \Delta T');
legend('Raw Data','Interpolated Data','location','northwest');
xlabel('Time (days)');
ylabel('Relative Flux');
```



Input all data

Text files:

```
%BD+48_1098
opts = detectImportOptions("BD+48_1098.txt");
opts.DataLines = 3;
opts.VariableNames = {'B_time','B_flux','R_time','R_flux','V_time','V_flux'};
opts.VariableTypes = {'double','double','double','double','double','double'};
BD48_1098 = rmmissing(readmatrix("BD+55_441.txt",opts)); %the matrix data of the text file
```

```
%preview("BD+48_1098.txt",opts)
whos BD48 1098
 Name
                 Size
                                Bytes Class
                                               Attributes
 BD48 1098
               100x6
                                4800
                                     double
%HD28497
opts = detectImportOptions("HD28497.txt");
opts.DataLines = 3;
opts.VariableNames = {'B_time', 'B_flux', 'R_time', 'R_flux', 'V_time', 'V_flux'};
opts.VariableTypes = {'double','double','double','double','double','double'};
HD28497 = rmmissing(readmatrix("HD28497.txt",opts)) %the matrix data of the text file
HD28497 = 600 \times 6
10^4 \times
  5.844163256000000
                    0.151884039400000
                                       5.844163279000000
                                                         0.047485834000000 . . .
  5.844163294000000
                                       5.844163317000000
                                                         0.047850097100000
                    0.157713255000000
  5.844163332000000
                    0.147648080800000
                                       5.844163355000000
                                                         0.050717498800000
  5.844163370000000
                    0.154105058200000
                                      5.844163393000001
                                                         0.048745268800000
  5.844163409000000
                    0.154416998300000
                                      5.844163431999999
                                                         0.046480291500000
  5.844163447000000
                    0.154034530100000
                                      5.844163470000000
                                                         0.052878906200000
  5.844163485000000
                    0.158524561400000
                                       5.844163508000000
                                                         0.050080829500000
  5.844163523000000
                   0.159731365000000
                                       5.844163546000000
                                                         0.053844298900000
  5.844163560999999
                   0.140623476800000
                                       5.844163584000000
                                                         0.050871022200000
  5.844163599000000 0.159835953000000
                                      5.844163622000000
                                                         0.053311599500000
%preview("HD28497.txt",opts)
whos HD28497
 Name
               Size
                              Bytes Class
                                             Attributes
 HD28497
             600x6
                              28800 double
%HD46131
opts = detectImportOptions("HD46131.txt");
opts.DataLines = 3;
opts.VariableNames = {'B_time', 'B_flux', 'R_time', 'R_flux', 'V_time', 'V_flux'};
opts.VariableTypes = {'double','double','double','double','double','double'};
HD46131 = rmmissing(readmatrix("HD46131.txt",opts)); %the matrix data of the text file
%preview("HD46131.txt",opts)
whos HD46131
 Name
               Size
                              Bytes Class
                                             Attributes
 HD46131
             250x6
                              12000 double
%HD88661
opts = detectImportOptions("HD88661.txt");
opts.DataLines = 3;
opts.VariableNames = {'B_time', 'B_flux', 'R_time', 'R_flux', 'V_time', 'V_flux'};
opts.VariableTypes = {'double','double','double','double','double','double'};
HD88661 = rmmissing(readmatrix("HD88661.txt",opts)); %the matrix data of the text file
%preview("HD88661.txt",opts)
whos HD88661
```

Name Size Bytes Class Attributes

HD88661 35x6 1680 double

```
%HD105521
opts = detectImportOptions("HD105521.txt");
opts.DataLines = 3;
opts.VariableNames = {'B_time','B_flux','R_time','R_flux','V_time','V_flux'};
opts.VariableTypes = {'double','double','double','double','double'};
HD105521 = rmmissing(readmatrix("HD105521.txt",opts)); %the matrix data of the text file %preview("HD105521.txt",opts)
whos HD105521
```

Name Size Bytes Class Attributes
HD105521 180x6 8640 double

```
%HD105521
opts = detectImportOptions("HD105521.txt");
opts.DataLines = 3;
opts.VariableNames = {'B_time','B_flux','R_time','R_flux','V_time','V_flux'};
opts.VariableTypes = {'double','double','double','double','double'};
HD105521 = rmmissing(readmatrix("HD105521.txt",opts)); %the matrix data of the text file %preview("HD105521.txt",opts)
whos HD105521
```

Name Size Bytes Class Attributes HD105521 180x6 8640 double

CSV files

```
%HD106306
%B filter
opts = detectImportOptions('HD106306_B.csv');
opts.DataLines = [2 Inf];
All_fields_available = opts.VariableNames;
opts.SelectedVariableNames = {'J_D_2400000', 'rel_flux_T1'};
%preview("HD106306 B.csv",opts)
HD106306_B = readmatrix("HD106306_B.csv",opts);
%R filter
opts = detectImportOptions('HD106306 R.csv');
opts.DataLines = [2 Inf];
All fields available = opts.VariableNames;
opts.SelectedVariableNames = {'J_D_2400000', 'rel_flux_T1'};
%preview("HD106306_R.csv",opts)
HD106306 R = readmatrix("HD106306 R.csv",opts);
%V filter
opts = detectImportOptions('HD106306_V.csv');
opts.DataLines = [2 Inf];
All_fields_available = opts.VariableNames;
opts.SelectedVariableNames = {'J_D_2400000','rel_flux_T1'};
%preview("HD106306_V.csv",opts)
HD106306_V = readmatrix("HD106306_V.csv",opts);
```

 $HD106306 = rmmissing([HD106306_B HD106306_R HD106306_V]);$ %the matrix data of the text file whos HD106306

Attributes

Bytes Class

```
HD106306
             100x6
                             4800
                                  double
%HD147302
%B_filter
opts = detectImportOptions('HD147302_B.csv');
opts.DataLines = [2 Inf];
All_fields_available = opts.VariableNames;
opts.SelectedVariableNames = {'J_D_2400000', 'rel_flux_T1'};
%preview("HD147302_B.csv",opts)
HD147302_B = readmatrix("HD147302_B.csv",opts);
%R filter
opts = detectImportOptions('HD147302_R.csv');
opts.DataLines = [2 Inf];
All fields_available = opts.VariableNames;
opts.SelectedVariableNames = {'J_D_2400000', 'rel_flux_T1'};
%preview("HD147302 R.csv",opts)
HD147302_R = readmatrix("HD147302_R.csv",opts);
%V filter
opts = detectImportOptions('HD147302_V.csv');
opts.DataLines = [2 Inf];
All fields available = opts.VariableNames;
opts.SelectedVariableNames = {'J_D_2400000', 'rel_flux_T1'};
%preview("HD147302 V.csv",opts)
HD147302 V = readmatrix("HD147302 V.csv",opts);
HD147302 = rmmissing([HD147302_B HD147302_R HD147302_V]); %the matrix data of the text file
whos HD147302
 Name
               Size
                            Bytes Class
                                           Attributes
 HD147302
             100x6
                             4800 double
```

HD152060 and HD209522 can't be described in the same form as the others.

Size

Name

```
%HD152060
%R_filter
opts = detectImportOptions('HD152060_R.csv');
opts.DataLines = [2 Inf];
All_fields_available = opts.VariableNames;
opts.SelectedVariableNames = {'J_D_2400000','rel_flux_T1'};
%preview("HD147302_R.csv",opts)
HD152060_R = readmatrix("HD152060_R.csv",opts);

%V_filter
opts = detectImportOptions('HD152060_V.csv');
opts.DataLines = [2 Inf];
All fields available = opts.VariableNames;
```

```
opts.SelectedVariableNames = {'J D 2400000','rel flux T1'};
%preview("HD147302_V.csv",opts)
HD152060_V = readmatrix("HD152060_V.csv",opts);
HD152060 = rmmissing([HD147302_R HD147302_V]); %the matrix data of the text file
whos HD152060
 Name
                                           Attributes
               Size
                             Bytes Class
 HD152060
             100x4
                             3200 double
%HD209522
%B filter
opts = detectImportOptions('HD209522_B.csv');
opts.DataLines = [2 Inf];
All_fields_available = opts.VariableNames;
opts.SelectedVariableNames = {'J_D_2400000', 'rel_flux_T1'};
%preview("HD147302 R.csv",opts)
HD209522 = readmatrix("HD209522_B.csv",opts);
%the matrix data of the text file
whos HD209522
                             Bytes Class
 Name
               Size
                                           Attributes
 HD209522
             408x2
                             6528 double
close all
            %closes all previous figures from milestone 1 so that the plots in milestone 2 and
```

Milestone 2 (13 October)

https://www.mathworks.com/help/matlab/ref/fft.html?searchHighlight=fft&s tid=srchtitle

This is the source for implementing Fourier Transform for a Noisy Signal from the MathWorks documentation

Using fft for HD28497

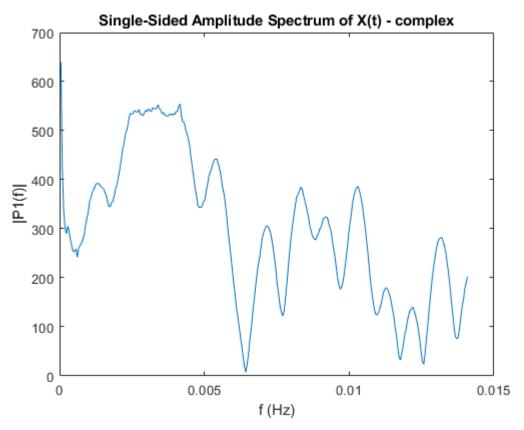
This star had the most data which made it ideal for performing a fourier transform. We chose linear interpolation for the purposes of this experiment at random. This is a feature to be explored later.

```
[Tnew,Mnew] = Interp_linear(HD28497(2:end,1),HD28497(2:end,2));
Tnew = Tnew*86400; %convert time from days to seconds
deltaT = Tnew(2)-Tnew(1);
Fs = 1/deltaT;
                         % Sampling frequency
                        % Sampling period
T = deltaT;
t = Tnew;
                         % Time vector
L = numel(Tnew);
                        % Length of signal
X = Mnew;
                        %signal with noise
%Fourier transformation
Y = fft(X);
P2complex = abs(Y/L); %real and imaginary parts together
%Bk
```

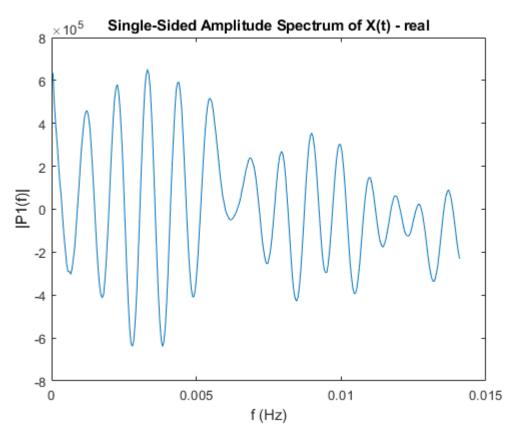
```
P2real = 2*real(Y);
P2imaginary = 2*imag(Y);
P1complex = P2complex(1:floor(L/2)+1);
P1complex(2:end-1) = 2*P1complex(2:end-1);

%Plot

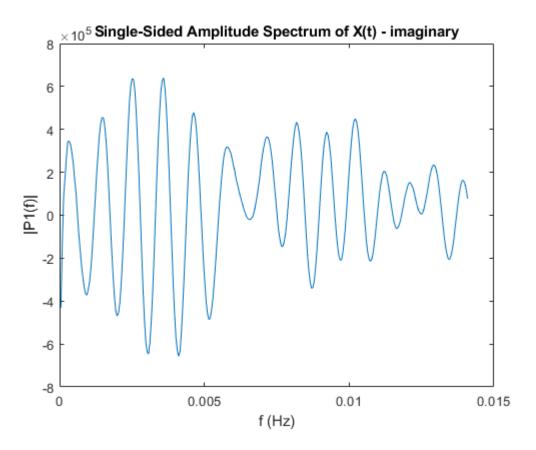
f = Fs*(0:(L/2))/L;
plot(f(2:end-1),P1complex(2:end-1))
title('Single-Sided Amplitude Spectrum of X(t) - complex')
xlabel('f (Hz)')
ylabel('|P1(f)|')
```



```
P1real = P2real(1:floor(L/2)+1);
P1real(2:end-1) = 2*P1real(2:end-1);
%plotting piece
f = Fs*(0:(L/2))/L;
plot(f(2:end-1),P1real(2:end-1))
title('Single-Sided Amplitude Spectrum of X(t) - real')
xlabel('f (Hz)')
ylabel('|P1(f)|')
```



```
Plimaginary = P2imaginary(1:floor(L/2)+1);
Plimaginary(2:end-1) = 2*Plimaginary(2:end-1);
%plotting piece
f = Fs*(0:(L/2))/L;
plot(f(2:end-1),Plimaginary(2:end-1))
title('Single-Sided Amplitude Spectrum of X(t) - imaginary')
xlabel('f (Hz)')
ylabel('|P1(f)|')
```

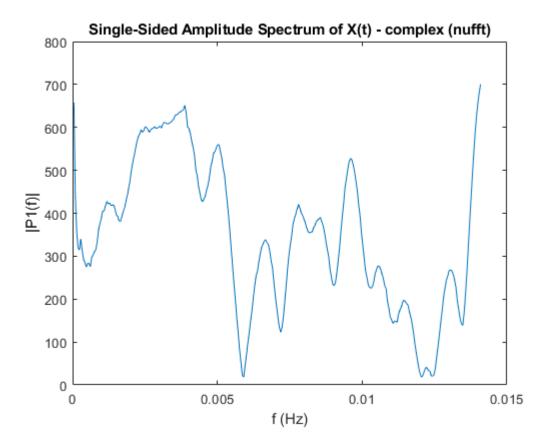


Using NUFFT - used the data without interpolation

Results for this one star using the complex combination was very similar to fft.

```
Tnew = HD28497(2:end,1);
Mnew = HD28497(2:end,2);
Tnew = Tnew*86400;
% --Find averaged time scale--
n = numel(Tnew);
sum = 0;
for l = 1:n-1
    sum = sum + abs(Tnew(1+1) - Tnew(1));
end
deltaT = sum / (n-1); %average time between points
Fs = 1/deltaT;
                         % Sampling frequency
T = deltaT;
                        % Sampling period
                         % Time vector
t = Tnew;
L = numel(Tnew);
                         % Length of signal
                        %signal with noise
X = Mnew;
%Fourier transformation
Y = nufft(X);
P2complex = abs(Y/L); %combination of real and imaginary
P2real = 2*real(Y);
P2imaginary = 2*imag(Y);
P1complex = P2complex(1:floor(L/2)+1);
P1complex(2:end-1) = 2*P1complex(2:end-1);
%plotting piece
f = Fs*(0:(L/2))/L;
```

```
plot(f(2:end-1),P1complex(2:end-1))
title('Single-Sided Amplitude Spectrum of X(t) - complex (nufft)')
xlabel('f (Hz)')
ylabel('|P1(f)|')
```



The investigation of the inverse fourier transform will be explored at a later date to complete milestone 2.

Milestone 3 (including previously unfinished parts of milestone 2)

Getting the Power Spectrum for HD28497

This star had the most data which made it ideal for performing a fourier transform. We chose linear interpolation for the purposes of this experiment at random. This is a feature to be explored late

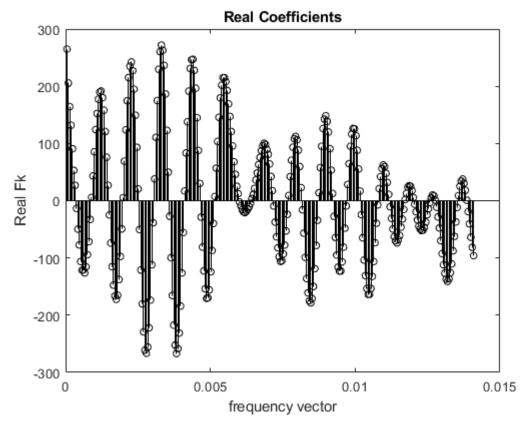
Documentation: We used a combination of the following sources to develop this:

- 1. https://www.mathworks.com/help/matlab/ref/fft.html?searchHighlight=fft&s_tid=srchtitle (This is the source for implementing Fourier Transform for a Noisy Signal from the MathWorks documentation)
- 2. Gilat, Example 7-6 (pg. 281)
- 3. Gilat, Example 7-8 (pg 287)

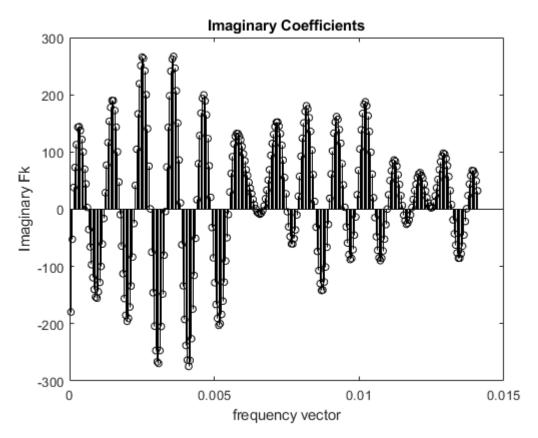
Bd+55 441 and HD 28497 have documented periodicity - citation pending

```
[Tnew,Mnew] = Interp_linear(HD28497(2:end,1),HD28497(2:end,2));
Tnew = Tnew*86400; %convert time from days to seconds
deltaT = Tnew(2)-Tnew(1);
```

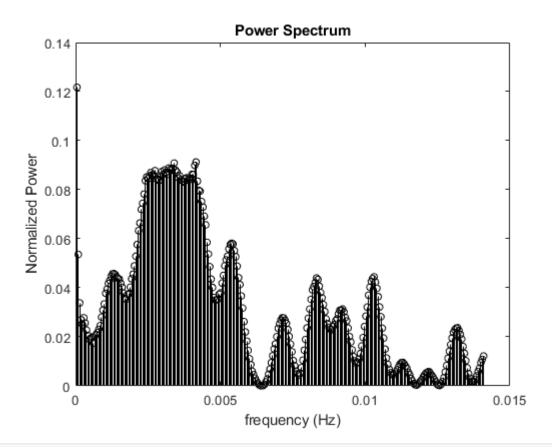
```
Fs = 1/deltaT;
                         % Sampling frequency
T = deltaT;
                        % Sampling period
t = Tnew-Tnew(1);
                                 % Time vector
L = numel(Tnew);
                        % Length of signal
X = Mnew;
                        %signal with noise
%Fourier transformation
                           %Based on Ex 7-6 Gilat
F = fft(X)/L;
                           %fourier transform devided by number of data points
power = F.*conj(F)/L;
powernorm = power/max(power);
                                %normalized power spectrum
                         %frequency vector Gilat 7-6
fk = (0:L-1)*(Fs/L);
stem(fk(2:floor(L/2)),real(F(2:floor(L/2))), 'ko','markersize',5)
                                                                              %Threw out first
xlabel('frequency vector')
ylabel('Real Fk')
title('Real Coefficients')
```

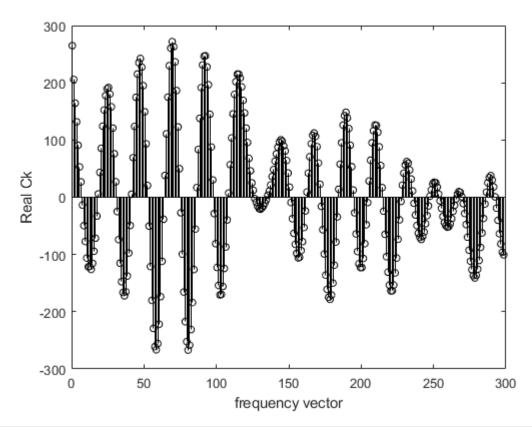


```
figure, stem(fk(2:floor(L/2)),imag(F(2:floor(L/2))),'ko','markersize',5)
xlabel('frequency vector')
ylabel('Imaginary Fk')
title('Imaginary Coefficients')
```

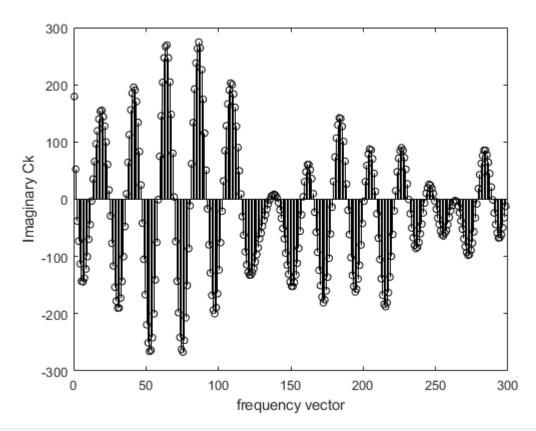


```
figure, stem(fk(2:floor(L/2)),powernorm(2:floor(L/2)),'ko','markersize',5)
xlabel('frequency (Hz)')
ylabel('Normalized Power')
title('Power Spectrum')
```

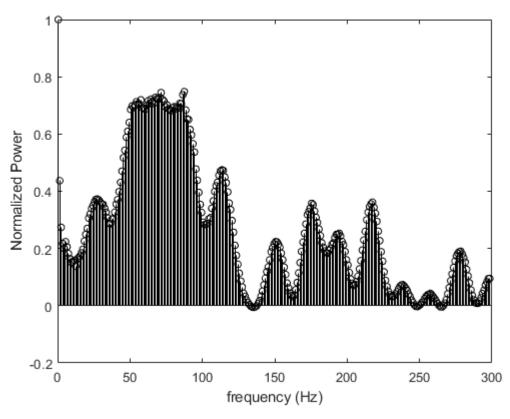




```
figure, stem(fk0(1:floor(L/2)),imag(C0(1:floor(L/2))),'ko','markersize',5)
xlabel('frequency vector')
ylabel('Imaginary Ck')
```



```
figure, stem(fk0(1:floor(L/2)),powernorm0(1:floor(L/2)),'ko','markersize',5)
xlabel('frequency (Hz)')
ylabel('Normalized Power')
```

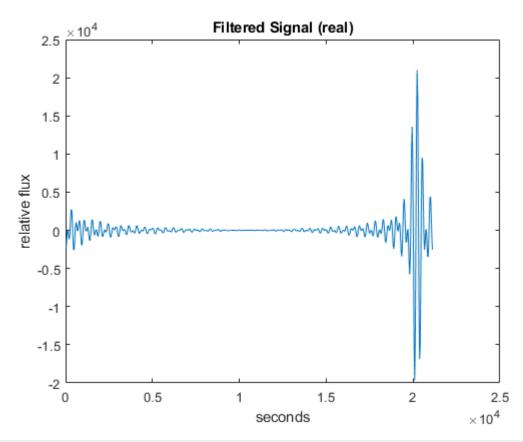


```
%Filtering out the noise Based on Gilat Example 7-8

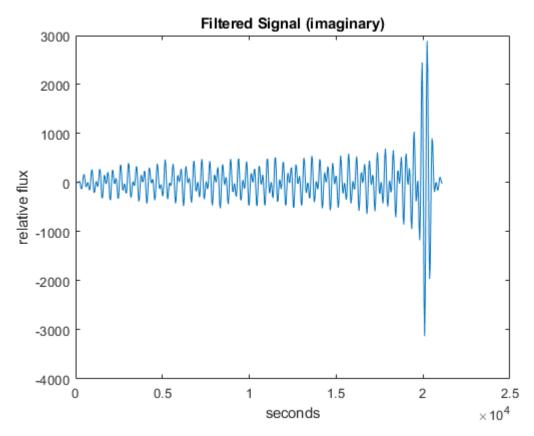
for k = 1:L-1
    if abs(fk0(k)) <= 50 || abs(fk0(k)) >= 90
        COflter(k) = 0+0i;

    else
        Coflter(k) = CO(k);
    end
end

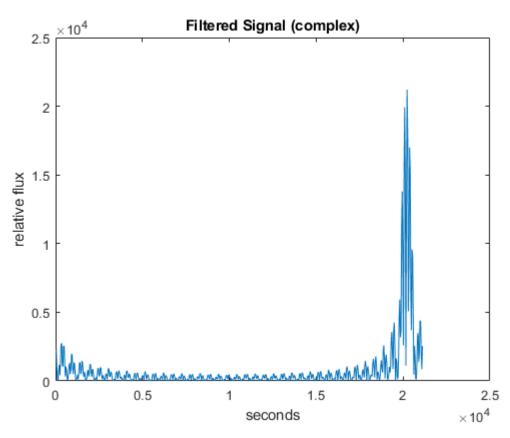
F0i = ifftshift(COflter) * L-1;
finv = ifft(F0i);
figure, plot(t(2:L),real(finv))
title('Filtered Signal (real)')
xlabel('seconds')
ylabel('relative flux')
```



```
F0i = ifftshift(C0flter) * L-1;
finv = ifft(F0i);
figure, plot(t(2:L),imag(finv))
title('Filtered Signal (imaginary)')
xlabel('seconds')
ylabel('relative flux')
```

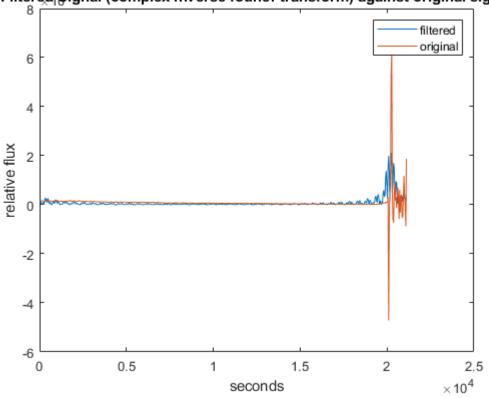


```
F0i = ifftshift(C0flter) * L-1;
finv = ifft(F0i);
figure, plot(t(2:L),abs(finv))
title('Filtered Signal (complex)')
xlabel('seconds')
ylabel('relative flux')
```



```
F0i = ifftshift(COflter) * L-1;
finv = ifft(F0i);
figure, plot(t(2:L),abs(finv),t(2:L),X(2:L))
legend('filtered','original')
title('Filtered Signal (complex inverse fourier transform) against original signal')
xlabel('seconds')
ylabel('relative flux')
```



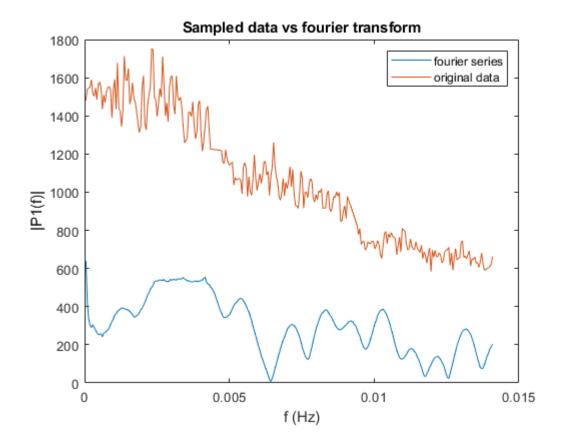


```
F =1./t(2:L);

%Fourier transformation
Y = fft(X);
P2complex = abs(Y/L); %real and imaginary parts together
P2real = 2*real(Y);
P2imaginary = 2*imag(Y);
P1complex = P2complex(1:floor(L/2)+1);
P1complex(2:end-1) = 2*P1complex(2:end-1);

%Plot

f = Fs*(0:(L/2))/L;
plot(f(2:end-1),P1complex(2:end-1),f(2:end-1),X(2:floor(1/2)))
title('Sampled data vs fourier transform')
xlabel('f (Hz)')
ylabel('|P1(f)|')
legend('fourier series','original data')
```

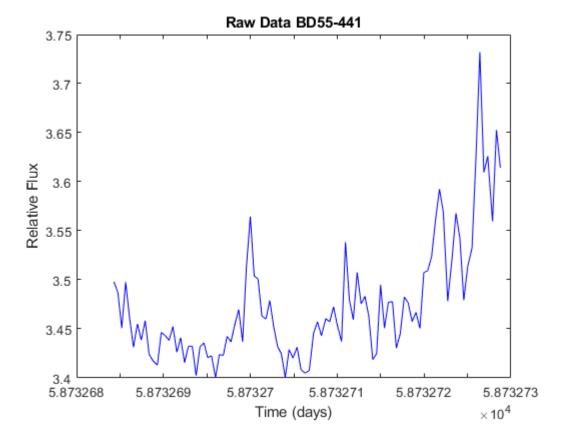


Milestone 4: Linear Combination of non-linear functions

BD55

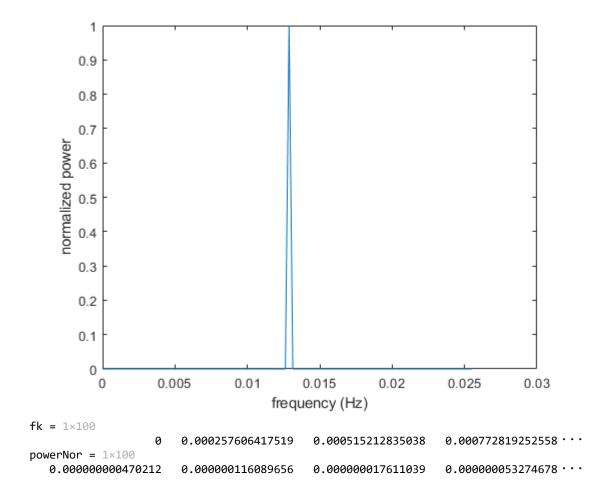
Plot the raw data

```
plot(BD55_441(1:100,1),BD55_441(1:100,2),'b');
title('Raw Data BD55-441');
xlabel('Time (days)');
ylabel('Relative Flux');
```



Use Linear Interpolation, then use a Fourier transform to attain the power spectrum

```
[Tnew,Mnew] = Interp_Lin(BD55_441(1:100,1),BD55_441(1:100,2));
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt)
```



Functions for linear combination:

(main frequency is 0.0129 HZ, or 1,115 per Day. Use this to choose my non-linear functions)

```
F1 =
     @(x) x./x;
     @(x) cos(2*pi*(1115)).*(x);
F2 =
     Q(x) \sin(2*pi*(1115)).*(x);
%call the NLfit function
c = NLfit(F1,F2,F3,BD55_441(1:100,1),BD55_441(1:100,2))
```

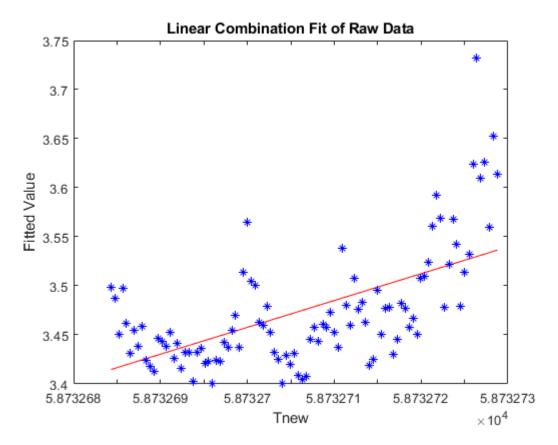
```
Warning: Matrix is close to singular or badly scaled. Results may be inaccurate. RCOND = 2.980448e-42.
c = 3 \times 1
10^{13} \times
  -0.000000016070897
```

0.000000000000894

3.724622381729035

```
%plot
```

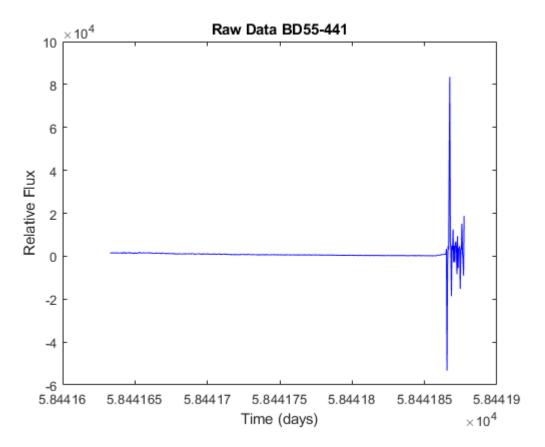
```
yfit = c(1).*F1(Tnew) + c(2).*F2(Tnew) + c(3).*F3(Tnew);
plot(Tnew,yfit,'r',BD55_441(1:100,1),BD55_441(1:100,2),'*b')
title('Linear Combination Fit of Raw Data')
xlabel('Tnew')
ylabel('Fitted Value')
```



HD28497

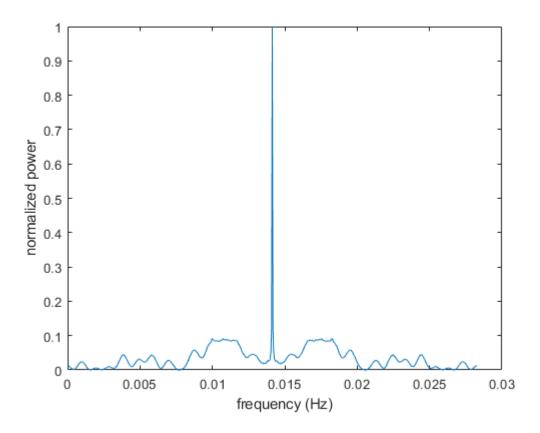
Plot the raw data

```
plot(HD28497(2:end,1),HD28497(2:end,2),'b');
title('Raw Data BD55-441');
xlabel('Time (days)');
ylabel('Relative Flux');
```



Use Linear Interpolation, then use a Fourier transform to attain the power spectrum

```
[Tnew,Mnew] = Interp_Lin(HD28497(2:end,1),HD28497(2:end,2));
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```



Functions for linear combination:

(main frequency at 0.0175 Hz or 1512 / day. use this for non-linear functions)

```
F1 = @(x) x./x;

F2 = @(x) cos(2*pi*(1512)).*(x);

F3 = @(x) sin(2*pi*(1512)).*(x);

%call the NLfit function

c = NLfit(F1,F2,F3,HD28497(2:end,1),HD28497(2:end,2))

Warning: Matrix is close to singular or badly scaled. Results may be inaccurate. RCOND = 1.465326e-41.

c = 3×1

10<sup>14</sup> x

0.00000000417432818

-0.0000000000006085

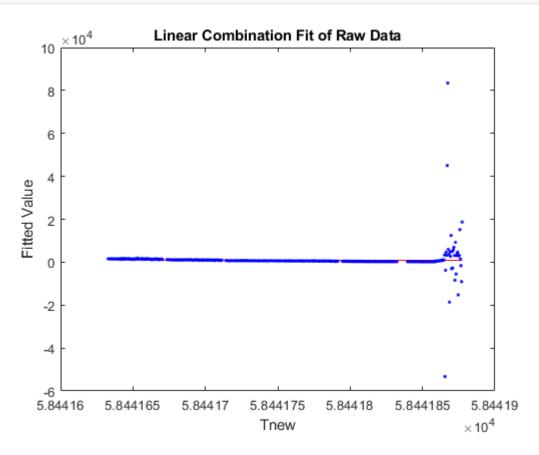
-7.488964229280974
```

```
%plot

yfit = c(1).*F1(Tnew) + c(2).*F2(Tnew) + c(3).*F3(Tnew);

plot(Tnew,yfit,'r',HD28497(2:end,1),HD28497(2:end,2),'.b')
```

```
title('Linear Combination Fit of Raw Data')
xlabel('Tnew')
ylabel('Fitted Value')
```



```
%This section should be run independently. This is a copy of what was %formerly titled Milestone 5v7

clearvars format long
```

Research Techniques Project Just Milestone 5

Input all data

Text files:

```
opts = detectImportOptions("BD+55_441.txt");
opts.DataLines = 3;
opts.VariableNames = {'B_time','B_flux','R_time','R_flux','V_time','V_flux'};
```

[&]quot;time" is in the units of days and "flux" is "rel_flux_T1" from AstroImageJ outputs.

```
opts.VariableTypes = {'double','double','double','double','double','double','double'};
preview("BD+55_441.txt",opts)
```

```
ans = 8 \times 6 table
```

	B_time	B_flux	R_time	R_flux	V_time	V_flux
1	5.873268430	3.497996	5.873268459	1.961830	5.873268445	2.352058
2	5.873268430	3.497996	5.873268504	1.942857	5.873268490	2.360458
3	5.873268475	3.487289	5.873268549	1.947021	5.873268535	2.329957
4	5.873268520	3.450942	5.873268594	1.930594	5.873268580	2.344889
5	5.873268565	3.497567	5.873268639	1.942537	5.873268625	2.361048
6	5.873268610	3.461555	5.873268684	1.935141	5.873268669	2.333341
7	5.873268655	3.431248	5.873268729	1.931290	5.873268714	2.331904
8	5.873268700	3.455091	5.873268774	1.928260	5.873268759	2.323782

```
BD55_441 = readmatrix("BD+55_441.txt",opts);
whos BD55_441
```

Name Size Bytes Class Attributes
BD55 441 101x6 4848 double

```
%BD+48_1098
opts = detectImportOptions("BD+48_1098.txt");
opts.DataLines = 3;
opts.VariableNames = {'B_time','B_flux','R_time','R_flux','V_time','V_flux'};
opts.VariableTypes = {'double','double','double','double','double','double'};
BD48_1098 = rmmissing(readmatrix("BD+55_441.txt",opts)); %the matrix data of the text file %preview("BD+48_1098.txt",opts)
whos BD48_1098
```

Name Size Bytes Class Attributes
BD48 1098 100x6 4800 double

```
%HD28497
opts = detectImportOptions("HD28497.txt");
opts.DataLines = 3;
opts.VariableNames = {'B_time','B_flux','R_time','R_flux','V_time','V_flux'};
opts.VariableTypes = {'double','double','double','double','double'};
HD28497 = rmmissing(readmatrix("HD28497.txt",opts)) %the matrix data of the text file
```

```
HD28497 = 600 \times 6
10<sup>4</sup> ×
                                                                 0.047485834000000 · · ·
   5.844163256000000
                       0.151884039400000
                                            5.844163279000000
   5.844163294000000
                       0.157713255000000
                                            5.844163317000000
                                                                 0.047850097100000
   5.844163332000000
                       0.147648080800000
                                            5.844163355000000
                                                                 0.050717498800000
   5.844163370000000
                       0.154105058200000
                                            5.844163393000001
                                                                 0.048745268800000
   5.844163409000000
                       0.154416998300000
                                            5.844163431999999
                                                                 0.046480291500000
   5.844163447000000
                       0.154034530100000
                                            5.844163470000000
                                                                 0.052878906200000
```

```
      5.844163485000000
      0.158524561400000
      5.844163508000000
      0.050080829500000

      5.844163523000000
      0.159731365000000
      5.844163546000000
      0.053844298900000

      5.844163560999999
      0.140623476800000
      5.844163584000000
      0.0508710222000000

      5.844163599000000
      5.844163622000000
      0.053311599500000
```

%preview("HD28497.txt",opts)
whos HD28497

Name Size Bytes Class Attributes

HD28497 600x6 28800 double

%HD46131 opts = detectImportOptions("HD46131.txt"); opts.DataLines = 3; opts.VariableNames = {'B_flux','B_time','R_time','R_flux','V_time','V_flux'}; opts.VariableTypes = {'double','double','double','double','double','double'}; HD46131 = rmmissing(readmatrix("HD46131.txt",opts)); %the matrix data of the text file preview("HD46131.txt",opts)

ans = 8×6 table

-						
	B_flux	B_time	R_time	R_flux	V_time	V_flux
1	80.30418	5.844670852	29.69434	5.844670891	43.24278	5.844670875
2	87.01571	5.844670916	29.50730	5.844670956	43.89599	5.844670939
3	86.15075	5.844670981	29.59417	5.844671021	43.11367	5.844671004
4	84.58512	5.844671046	29.01948	5.844671085	43.53672	5.844671069
5	82.72335	5.844671111	29.25732	5.844671150	44.34534	5.844671134
6	79.70069	5.844671175	30.09976	5.844671215	43.52612	5.844671199
7	84.42755	5.844671240	29.99023	5.844671280	42.63575	5.844671263
8	79.15342	5.844671305	29.78040	5.844671344	43.53322	5.844671329

whos HD46131

Name Size Bytes Class Attributes

HD46131 250x6 12000 double

```
%HD88661
opts = detectImportOptions("HD88661.txt");
opts.DataLines = 3;
opts.VariableNames = {'B_time','B_flux','R_time','R_flux','V_time','V_flux'};
opts.VariableTypes = {'double','double','double','double','double'};
HD88661 = rmmissing(readmatrix("HD88661.txt",opts)); %the matrix data of the text file %preview("HD88661.txt",opts)
whos HD88661
```

Name Size Bytes Class Attributes

HD88661 35x6 1680 double

```
%HD105521
opts = detectImportOptions("HD105521.txt");
opts.DataLines = 3;
opts.VariableNames = {'B_time','B_flux','R_time','R_flux','V_time','V_flux'};
opts.VariableTypes = {'double','double','double','double','double','double'};
HD105521 = rmmissing(readmatrix("HD105521.txt",opts)); %the matrix data of the text file %preview("HD105521.txt",opts)
whos HD105521
```

Name Size Bytes Class Attributes
HD105521 180x6 8640 double

```
%HD105521
opts = detectImportOptions("HD105521.txt");
opts.DataLines = 3;
opts.VariableNames = {'B_time','B_flux','R_time','R_flux','V_time','V_flux'};
opts.VariableTypes = {'double','double','double','double','double'};
HD105521 = rmmissing(readmatrix("HD105521.txt",opts)); %the matrix data of the text file %preview("HD105521.txt",opts)
whos HD105521
```

Name Size Bytes Class Attributes
HD105521 180x6 8640 double

```
%KIC_11924311
opts = detectImportOptions("KIC_11924311_Photometry.txt");
opts.DataLines = 3;
%opts.VariableNames = {'B_time','B_flux','R_time','R_flux','V_time','V_flux'};
opts.VariableNames = {'Time','Filter','Flux','error'};
opts.VariableTypes = {'double','char','double','double'};
KIC_11924311 = rmmissing(readtable("KIC_11924311_Photometry.txt",opts)); %the matrix data of the preview("KIC_11924311_Photometry.txt",opts)
```

ans = 8×4 table

	Time	Filter	Flux	error
1	5.79853734	'B'	0.68590	0.00300
2	5.79853742	'B'	0.68147	0.00299
3	5.79853758	'B'	0.69522	0.00301
4	5.79853766	'B'	0.69789	0.00303
5	5.79853775	'B'	0.69234	0.00300
6	5.79853783	'B'	0.70016	0.00303
7	5.79853791	'B'	0.69389	0.00299
8	5.79853799	'B'	0.70966	0.00305

```
filters = unique(KIC_11924311{:,2},'stable');
poscount = [1 0 0 0 0];
[n,~] = size(KIC_11924311);
KIC_11924311temp = table;
l = {0};
```

```
for count=1:4
    poscount(count+1)=poscount(count);
    while (char(filters(count))==char(KIC_11924311{poscount(count+1),2}) && poscount(count+1) =
        poscount(count+1) = poscount(count+1) + 1;
    end
    KIC = KIC_11924311(poscount(count):poscount(count+1)-1,:)
    KIC = KIC(1:348,:);
    KIC_11924311temp.J_D__240000 = KIC.Time;
    KIC_11924311temp.rel_flux_T1 = KIC.Flux;
    l{2*count-1} = sprintf('%s_time', char(filters(count)));
    l{2*count} = sprintf('%s_flux', char(filters(count)));
    KIC_11924311temp.Properties.VariableNames = 1;
end
```

 $KIC = 348 \times 4 \text{ table}$

	Time	Filter	Flux	error
1	5.79853734	'B'	0.68590	0.00300
2	5.79853742	'B'	0.68147	0.00299
3	5.79853758	'B'	0.69522	0.00301
4	5.79853766	'B'	0.69789	0.00303
5	5.79853775	'B'	0.69234	0.00300
6	5.79853783	'B'	0.70016	0.00303
7	5.79853791	'B'	0.69389	0.00299
8	5.79853799	'B'	0.70966	0.00305
9	5.79853807	'B'	0.70262	0.00302
10	5.79853815	'B'	0.70943	0.00305
11	5.79853823	'B'	0.71280	0.00305
12	5.79853831	'B'	0.71538	0.00306
13	5.79853840	'B'	0.71921	0.00314
14	5.79853848	'B'	0.72563	0.00327

 $KIC = 350 \times 4 \text{ table}$

	Time	Filter	Flux	error
1	5.79853728	'V'	0.72607	0.00284
2	5.79853736	'V'	0.72676	0.00284
3	5.79853744	'V'	0.72876	0.00283
4	5.79853752	'V'	0.73102	0.00284
5	5.79853760	'V'	0.73476	0.00285
6	5.79853769	'V'	0.74009	0.00287
7	5.79853777	'V'	0.74062	0.00285
8	5.79853785	'V'	0.74477	0.00287

	Time	Filter	Flux	error
9	5.79853793	'V'	0.74259	0.00285
10	5.79853801	'V'	0.74713	0.00287
11	5.79853809	'V'	0.74955	0.00288
12	5.79853817	'V'	0.75450	0.00289
13	5.79853826	'V'	0.76023	0.00291
14	5.79853834	'V'	0.76027	0.00292
	· :	1		

KIC = 350×4 table

	Time	Filter	Flux	error
1	5.79853729	'R'	0.74284	0.00304
2	5.79853737	'R'	0.74455	0.00306
3	5.79853746	'R'	0.75454	0.00309
4	5.79853754	'R'	0.75485	0.00307
5	5.79853762	'R'	0.75807	0.00307
6	5.79853770	'R'	0.76211	0.00308
7	5.79853778	'R'	0.76860	0.00311
8	5.79853787	'R'	0.77020	0.00313
9	5.79853795	'R'	0.76533	0.00309
10	5.79853803	'R'	0.76891	0.00309
11	5.79853811	'R'	0.76780	0.00309
12	5.79853819	'R'	0.77622	0.00313
13	5.79853827	'R'	0.78118	0.00314
14	5.79853835	'R'	0.78604	0.00316

 $KIC = 350 \times 4 \text{ table}$

	Time	Filter	Flux	error
1	5.79853731	'I'	0.76493	0.00514
2	5.79853739	'I'	0.78074	0.00526
3	5.79853747	'I'	0.77509	0.00512
4	5.79853755	'I'	0.77435	0.00518
5	5.79853763	'I'	0.78233	0.00519
6	5.79853772	'I'	0.78959	0.00518
7	5.79853780	'l'	0.78702	0.00513
8	5.79853788	'l'	0.78799	0.00519

	Time	Filter	Flux	error
9	5.79853796	'I'	0.79257	0.00515
10	5.79853805	'I'	0.79262	0.00514
11	5.79853813	'l'	0.79891	0.00518
12	5.79853821	'l'	0.80309	0.00517
13	5.79853829	'l'	0.81053	0.00517
14	5.79853837	'l'	0.80186	0.00522
	:	<u> </u>		

poscount

poscount = 1×5 1 349 699 1049 1399

```
KIC_11924311 = KIC_11924311temp;
whos KIC_11924311
```

Name Size Bytes Class Attributes
KIC 11924311 348x8 24799 table

CSV files

```
%HD106306
%B_filter
opts = detectImportOptions('HD106306_B.csv');
opts.DataLines = [2 Inf];
All_fields_available = opts.VariableNames;
opts.SelectedVariableNames = {'J_D_2400000', 'rel_flux_T1'};
%preview("HD106306_B.csv",opts)
HD106306_B = readmatrix("HD106306_B.csv",opts);
%R filter
opts = detectImportOptions('HD106306_R.csv');
opts.DataLines = [2 Inf];
All_fields_available = opts.VariableNames;
opts.SelectedVariableNames = {'J_D_2400000','rel_flux_T1'};
%preview("HD106306_R.csv",opts)
HD106306_R = readmatrix("HD106306_R.csv",opts);
%V filter
opts = detectImportOptions('HD106306_V.csv');
opts.DataLines = [2 Inf];
All_fields_available = opts.VariableNames;
opts.SelectedVariableNames = {'J_D_2400000','rel_flux_T1'};
%preview("HD106306_V.csv",opts)
HD106306_V = readmatrix("HD106306_V.csv",opts);
HD106306 = rmmissing([HD106306_B HD106306_R HD106306_V]); %the matrix data of the text file
whos HD106306
```

Name Size Bytes Class Attributes

4800

double

```
%HD147302
%B filter
opts = detectImportOptions('HD147302_B.csv');
opts.DataLines = [2 Inf];
All fields available = opts.VariableNames;
opts.SelectedVariableNames = {'J_D_2400000','rel_flux_T1'};
%preview("HD147302_B.csv",opts)
HD147302 B = readmatrix("HD147302 B.csv",opts);
%R_filter
opts = detectImportOptions('HD147302_R.csv');
opts.DataLines = [2 Inf];
All_fields_available = opts.VariableNames;
opts.SelectedVariableNames = {'J_D_2400000', 'rel_flux_T1'};
%preview("HD147302_R.csv",opts)
HD147302_R = readmatrix("HD147302_R.csv",opts);
%V filter
opts = detectImportOptions('HD147302_V.csv');
opts.DataLines = [2 Inf];
All fields available = opts.VariableNames;
opts.SelectedVariableNames = {'J_D_2400000', 'rel_flux_T1'};
%preview("HD147302_V.csv",opts)
HD147302_V = readmatrix("HD147302_V.csv",opts);
HD147302 = rmmissing([HD147302_B HD147302_R HD147302_V]); %the matrix data of the text file
whos HD147302
               Size
                                          Attributes
 Name
                            Bytes Class
```

Name Size Bytes Class Attributes
HD147302 100x6 4800 double

HD152060 and HD209522 can't be described in the same form as the others. Will investigate

HD46131

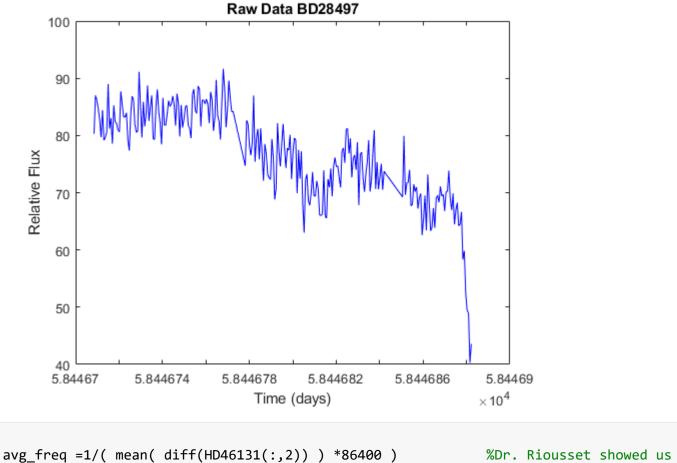
Plot the raw data

HD106306

100x6

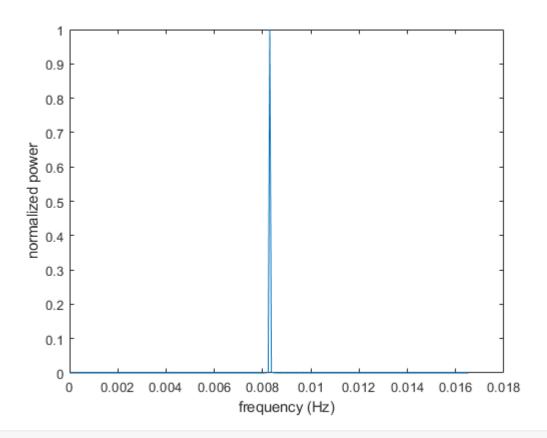
```
plot(HD46131(:,2),HD46131(:,1),'b');
title('Raw Data BD28497');
```

```
xlabel('Time (days)');
ylabel('Relative Flux');
```



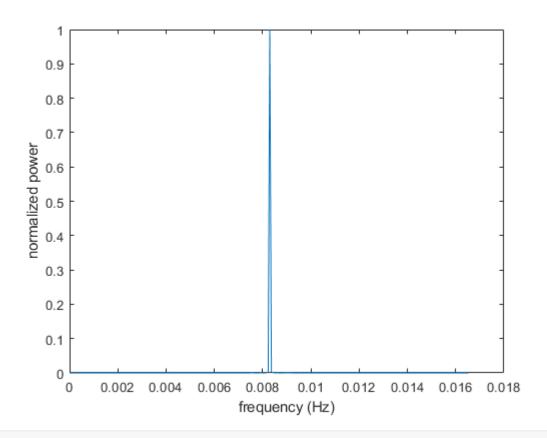
Use Linear Interpolation, then use a Fourier transform to attain the power spectrum

```
[Tnew,Mnew] = Interp_Lin(HD46131(:,2),HD46131(:,1));
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```



Use Spline Interpolation, then use a Fourier transform to attain the power spectrum

```
[Tnew,Mnew] = Interp_spline(HD46131(:,2),HD46131(:,1));
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```



Try non-uniform built in function "nufft"

```
N = length(HD46131(:,2));
F = nufft( HD46131(:,2),HD46131(:,1) )/N;
F0 = fftshift(F);

power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')
```

```
power spectrum using "nufft"
     1
   0.9
   0.8
   0.7
normalized power
   0.6
   0.5
   0.4
   0.3
   0.2
   0.1
     0
      0
            0.002 0.004
                            0.006
                                    0.008
                                            0.01
                                                    0.012 0.014 0.016 0.018
                                   frequency (Hz)
```

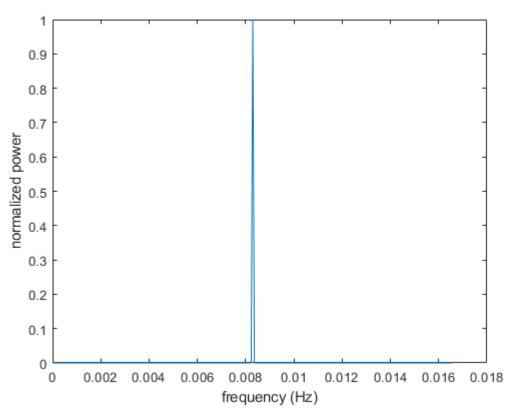
```
key_freq = 0.008296;
avg_freq =1/( mean( diff(HD46131(:,2)) ) *86400 )
```

avg_freq =
 0.016592460385689

avg_freq/key_freq

ans =

```
%R
[Tnew,Mnew] = Interp_spline(HD46131(:,4),HD46131(:,3));
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```



```
avg_freq =1/( mean( diff(HD46131(:,4)) ) *86400 );
N = length(HD46131(:,4));
F = nufft( HD46131(:,4), HD46131(:,3) )/N;
F0 = fftshift(F);
power = F0.*conj(F0)/N;
N = length(HD46131(:,4));
F = nufft( HD46131(:,4), HD46131(:,3) )/N;
F0 = fftshift(F);
power = F0.*conj(F0)/N;
powerNor = power/max(power);
%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);
plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')
```

```
power spectrum using "nufft"
     1
   0.9
   0.8
   0.7
normalized power
   0.6
   0.5
   0.4
   0.3
   0.2
   0.1
     0
      0
            0.002 0.004
                           0.006
                                   0.008
                                           0.01
                                                    0.012 0.014 0.016 0.018
                                   frequency (Hz)
```

```
key_freq = 0.00829623;
avg_freq =1/( mean( diff(HD46131(:,4)) ) *86400 )
```

avg_freq =
 0.016592460386384

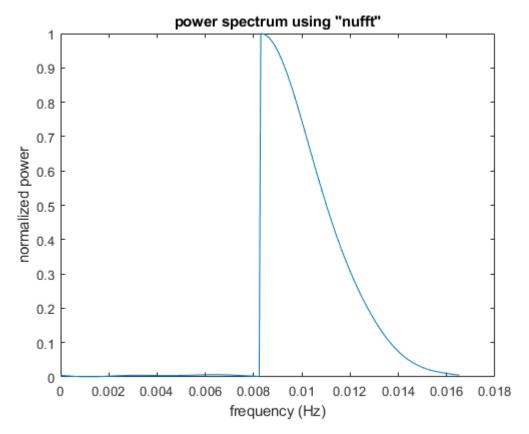
avg_freq/key_freq

ans =

```
powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')
```



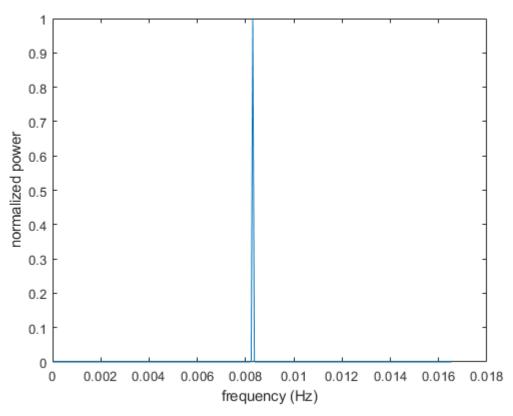
```
key_freq = 0.008296;
avg_freq =1/( mean( diff(HD46131(:,4)) ) *86400 )
```

avg_freq =
 0.016592460386384

avg_freq/key_freq

ans =

```
%v
[Tnew,Mnew] = Interp_spline(HD46131(:,6),HD46131(:,5));
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```



```
avg_freq =1/( mean( diff(HD46131(:,6)) ) *86400 );
N = length(HD46131(:,6));
F = nufft( HD46131(:,6), HD46131(:,5) )/N;
F0 = fftshift(F);
power = F0.*conj(F0)/N;
N = length(HD46131(:,6));
F = nufft( HD46131(:,6), HD46131(:,5) )/N;
F0 = fftshift(F);
power = F0.*conj(F0)/N;
powerNor = power/max(power);
%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);
plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')
```

```
power spectrum using "nufft"
     1
   0.9
   0.8
   0.7
normalized power
   0.6
   0.5
   0.4
   0.3
   0.2
   0.1
     0
      0
            0.002 0.004
                           0.006
                                   0.008
                                           0.01
                                                   0.012 0.014 0.016 0.018
                                  frequency (Hz)
```

```
key_freq = 0.00829623;
avg_freq =1/( mean( diff(HD46131(:,6)) ) *86400 )
```

avg_freq =
 0.016592460385689

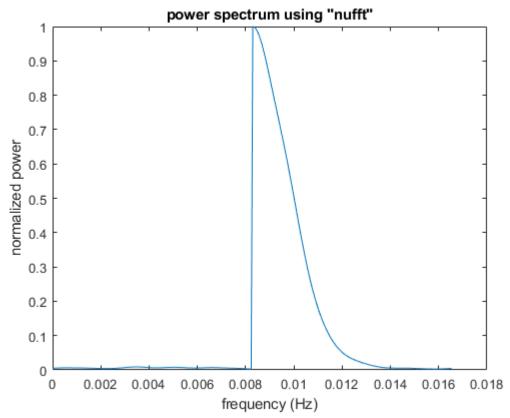
avg_freq/key_freq

ans =

```
powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')
```



```
key_freq = 0.008296;
avg_freq =1/( mean( diff(HD46131(:,4)) ) *86400 )

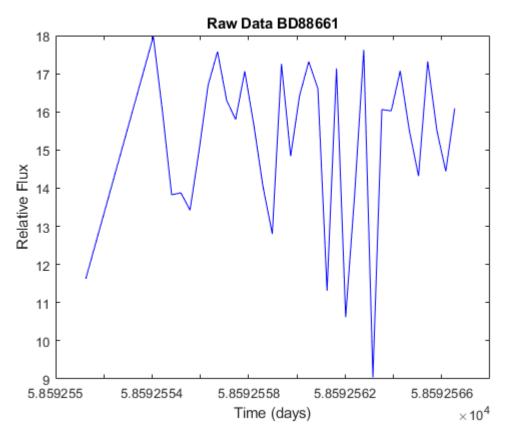
avg_freq =
   0.016592460386384

avg_freq/key_freq
ans =
```

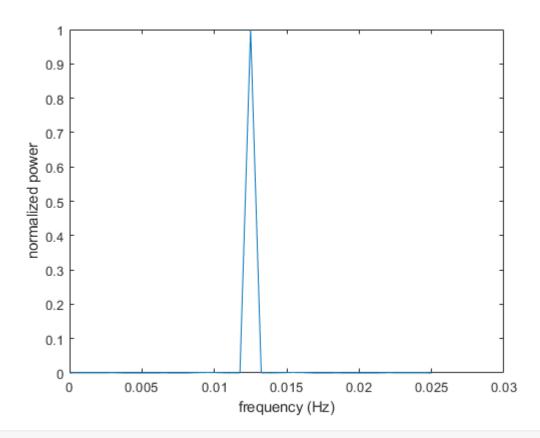
HD88661

Plot the raw data

```
plot(HD88661(:,2),HD88661(:,1),'b');
title('Raw Data BD88661');
xlabel('Time (days)');
ylabel('Relative Flux');
```

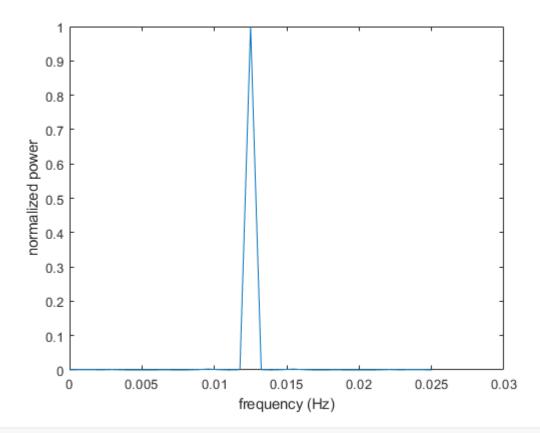


```
%B
avg_freq =1/( mean( diff(HD88661(:,2)) ) *86400 );
[Tnew,Mnew] = Interp_Lin(HD88661(:,2),HD88661(:,1));
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```



Use Spline Interpolation, then use a Fourier transform to attain the power spectrum

```
[Tnew,Mnew] = Interp_spline(HD88661(:,2),HD88661(:,1));
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```



Try non-uniform built in function "nufft"

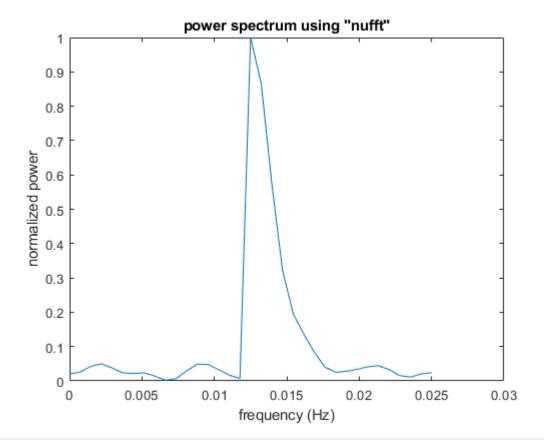
```
N = length(HD88661(:,2));
F = nufft( HD88661(:,2),HD88661(:,1) )/N;
F0 = fftshift(F);

power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')
```



```
key_freq = 0.0125008
```

key_freq =
 0.012500800000000

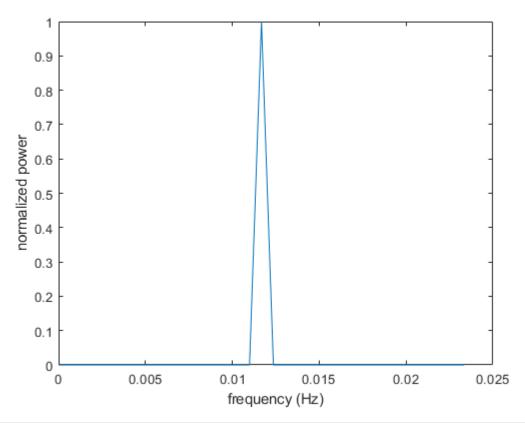
```
avg_freq =1/( mean( diff(HD88661(:,2)) ) *86400 )
```

avg_freq =
 0.025736986163581

avg_freq/key_freq

ans = 2.058827128150297

```
%R
avg_freq =1/( mean( diff(HD88661(:,4)) ) *86400 );
[Tnew,Mnew] = Interp_Lin(HD88661(:,4),HD88661(:,3));
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```



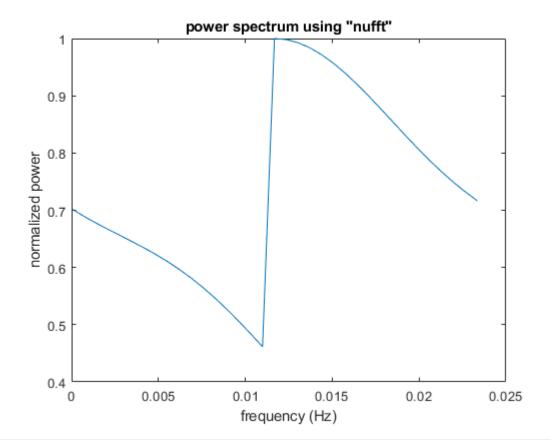
```
N = length(HD88661(:,4));
F = nufft( HD88661(:,4),HD88661(:,3) )/N;
F0 = fftshift(F);

power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')
```



```
key_freq = 0.0116761
```

key_freq =
 0.011676100000000

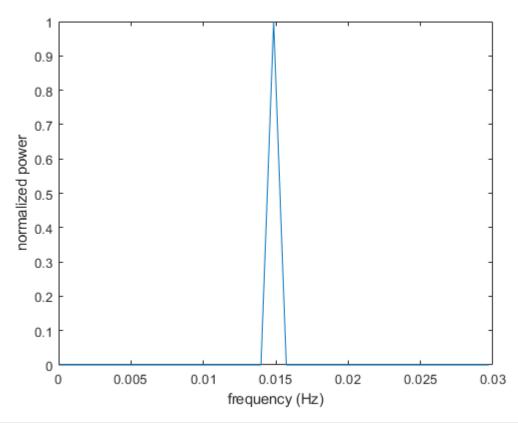
```
avg_freq =1/( mean( diff(HD88661(:,4)) ) *86400 )
```

avg_freq =
 0.024039005400274

avg_freq/key_freq

ans =

```
%V
avg_freq =1/( mean( diff(HD88661(:,6)) ) *86400 );
[Tnew,Mnew] = Interp_Lin(HD88661(:,6),HD88661(:,5));
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```



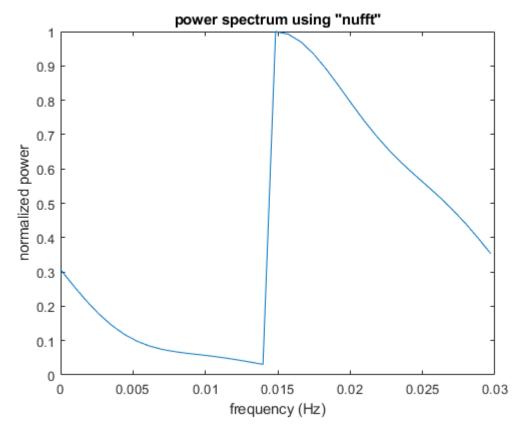
```
N = length(HD88661(:,6));
F = nufft( HD88661(:,6), HD88661(:,5) )/N;
F0 = fftshift(F);

power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')
```



```
key_freq = 0.0148514;
avg_freq =1/( mean( diff(HD88661(:,6)) ) *86400 )

avg_freq =
   0.030576419468500
```

c (1 c

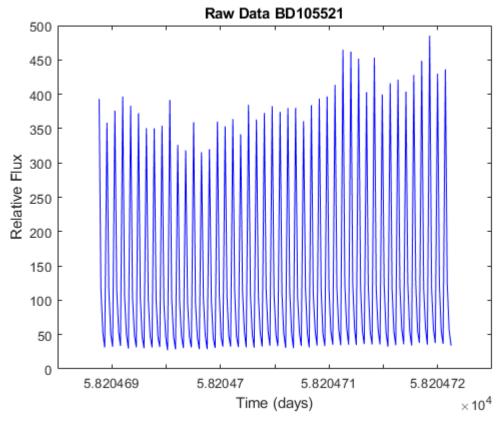
avg_freq/key_freq

ans = 2.058824048136881

HD105521

Plot the raw data

```
plot(HD105521(:,1),HD105521(:,2),'b');
title('Raw Data BD105521');
xlabel('Time (days)');
ylabel('Relative Flux');
```

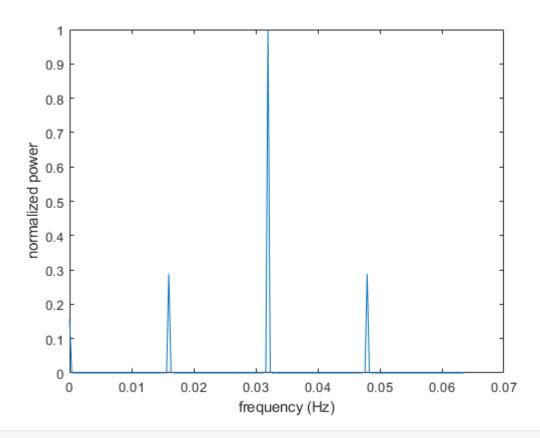


```
%B
avg_freq =1/( mean( diff(HD105521(:,1)) ) *86400 )
```

avg_freq =
 0.063943187006892

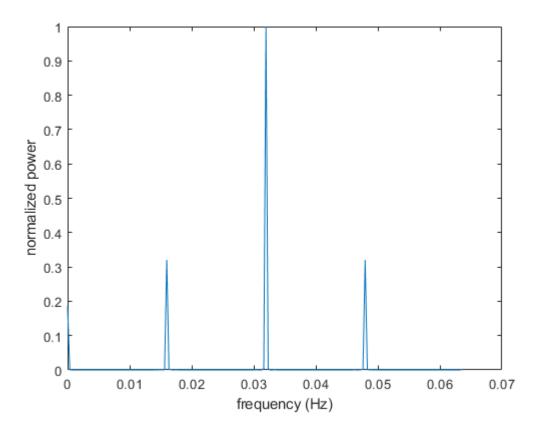
Use Linear Interpolation, then use a Fourier transform to attain the power spectrum

```
[Tnew,Mnew] = Interp_Lin(HD105521(:,1),HD105521(:,2));
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```



Use Spline Interpolation, then use a Fourier transform to attain the power spectrum

```
[Tnew,Mnew] = Interp_spline(HD105521(:,1),HD105521(:,2));
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```



Try non-uniform built in function "nufft"

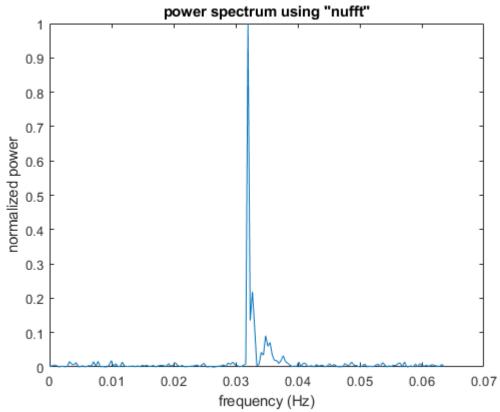
```
N = length(HD105521(:,1));
F = nufft( HD105521(:,1),HD105521(:,2) )/N;
F0 = fftshift(F);

power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')
```



```
key_freq = 0.0319716

key_freq =
    0.031971600000000

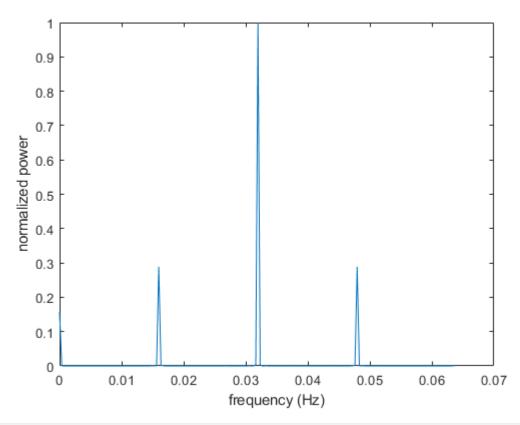
avg_freq =1/( mean( diff(HD105521(:,1)) ) *86400 )

avg_freq =
    0.063943187006892
```

```
avg_freq/key_freq
```

ans = 1.999999593604684

```
%R
avg_freq =1/( mean( diff(HD105521(:,3)) ) *86400 );
[Tnew,Mnew] = Interp_Lin(HD105521(:,3),HD105521(:,4));
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```



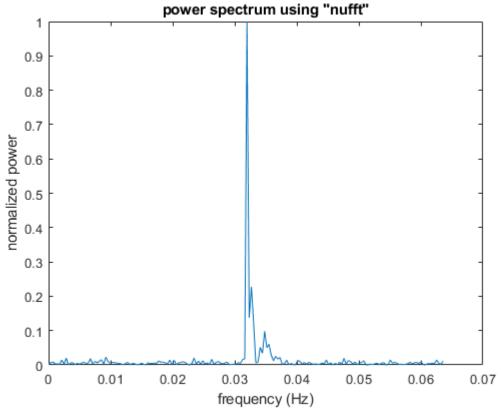
```
N = length(HD105521(:,3));
F = nufft( HD105521(:,3), HD105521(:,4) )/N;
F0 = fftshift(F);

power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')
```

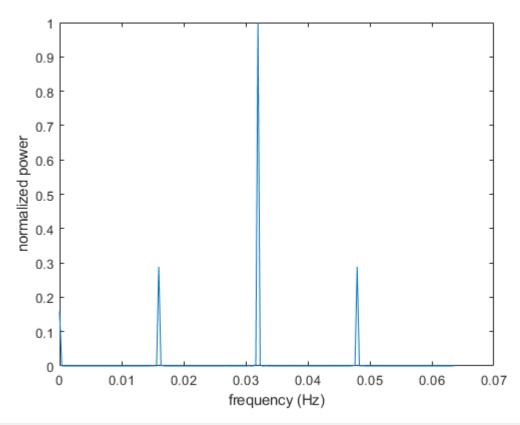


avg_freq =
 0.063943187006892

```
avg_freq/key_freq
```

ans =

```
%V
avg_freq =1/( mean( diff(HD105521(:,5)) ) *86400 );
[Tnew,Mnew] = Interp_Lin(HD105521(:,5),HD105521(:,6));
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```



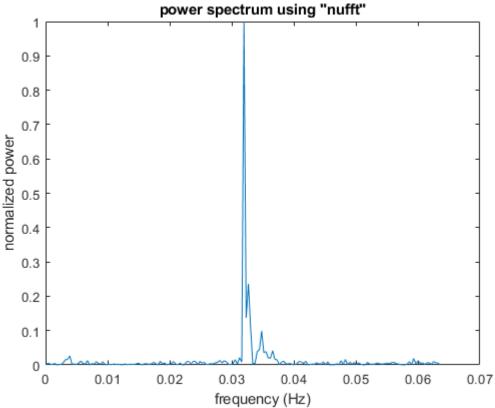
```
N = length(HD105521(:,5));
F = nufft( HD105521(:,5), HD105521(:,6) )/N;
F0 = fftshift(F);

power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')
```



```
key_freq = 0.0319716

key_freq = 0.031971600000000

avg_freq =1/( mean( diff(HD105521(:,5)) ) *86400 )

avg_freq = 0.063943187006892

avg_freq/key_freq

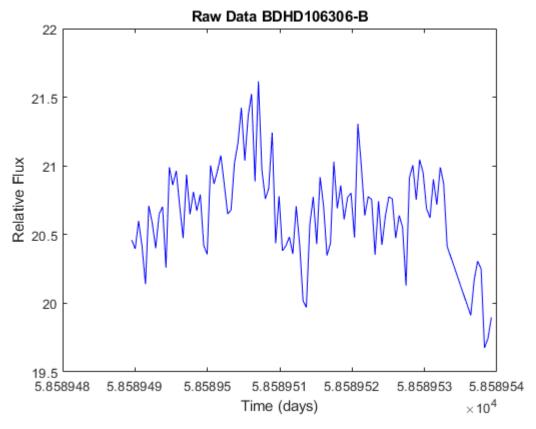
ans =
```

HD106306 B

1.999999593604684

Plot the raw data

```
plot(HD106306_B(:,1),HD106306_B(:,2),'b');
title('Raw Data BDHD106306-B');
xlabel('Time (days)');
ylabel('Relative Flux');
```

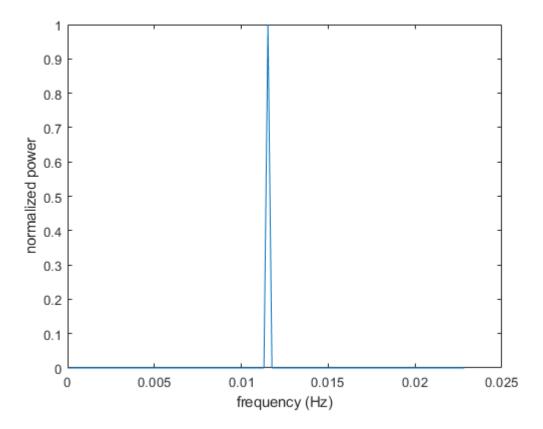


```
avg_freq =1/( mean( diff(HD106306_B(:,1)) ) *86400 )
```

avg_freq =
 0.023064278044436

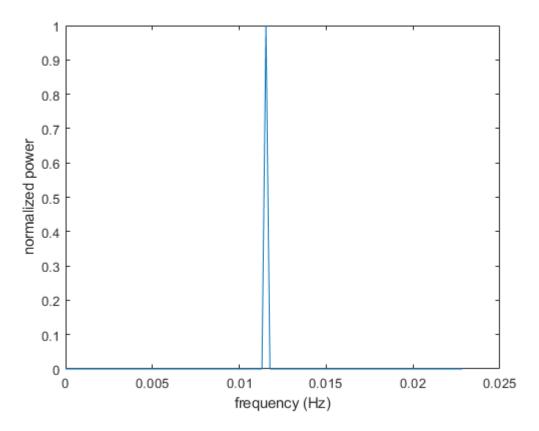
Use Linear Interpolation, then use a Fourier transform to attain the power spectrum

```
[Tnew,Mnew] = Interp_Lin(HD106306_B(:,1),HD106306_B(:,2));
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```



Use Spline Interpolation, then use a Fourier transform to attain the power spectrum

```
[Tnew,Mnew] = Interp_spline(HD106306_B(:,1),HD106306_B(:,2));
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```



Try non-uniform built in function "nufft"

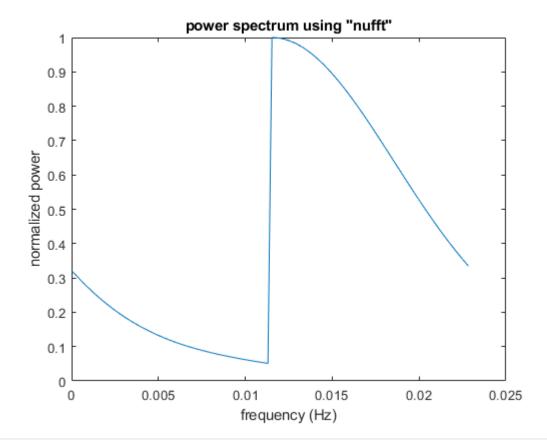
```
N = length(HD106306_B(:,1));
F = nufft( HD106306_B(:,1),HD106306_B(:,2) )/N;
F0 = fftshift(F);

power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')
```



```
key_freq = 0.0115321
```

key_freq =
 0.011532100000000

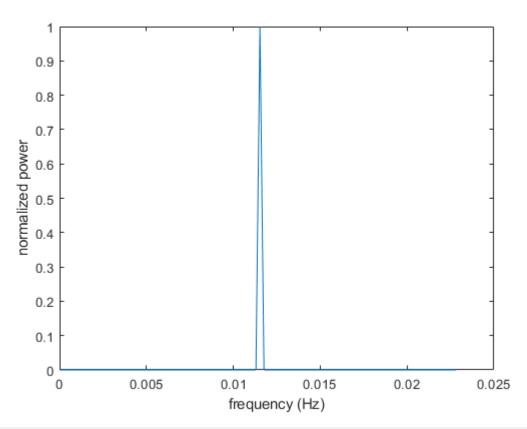
```
avg_freq =1/( mean( diff(HD106306_B(:,1)) ) *86400 )
```

avg_freq =
 0.023064278044436

avg_freq/key_freq

ans =

```
%R
avg_freq =1/( mean( diff(HD106306_R(:,1)) ) *86400 );
[Tnew,Mnew] = Interp_Lin(HD106306_R(:,1),HD106306_R(:,2));
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```



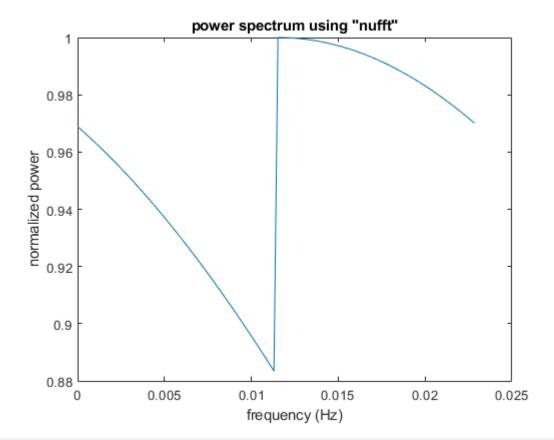
```
N = length(HD106306_R(:,1));
F = nufft( HD106306_R(:,1),HD106306_R(:,2) )/N;
F0 = fftshift(F);

power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')
```



```
key_freq = 0.0115326
```

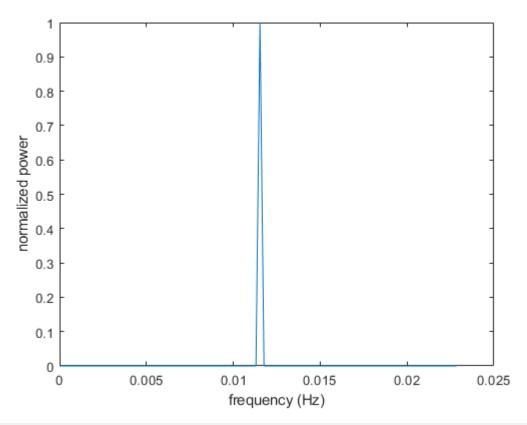
```
avg_freq =1/( mean( diff(HD106306_R(:,1)) ) *86400 )
```

avg_freq =
 0.023065206595740

avg_freq/key_freq

ans =

```
%V
avg_freq =1/( mean( diff(HD106306_V(:,1)) ) *86400 );
[Tnew,Mnew] = Interp_Lin(HD106306_V(:,1),HD106306_V(:,2));
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```



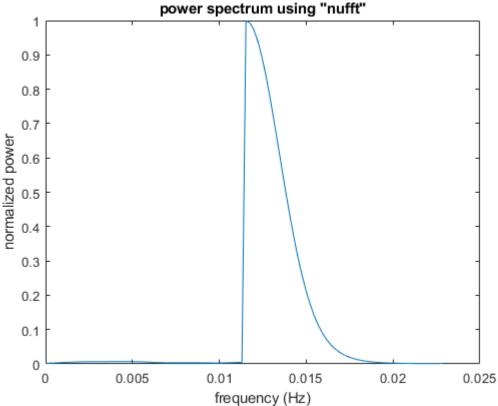
```
N = length(HD106306_V(:,1));
F = nufft( HD106306_V(:,1),HD106306_V(:,2) )/N;
F0 = fftshift(F);

power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

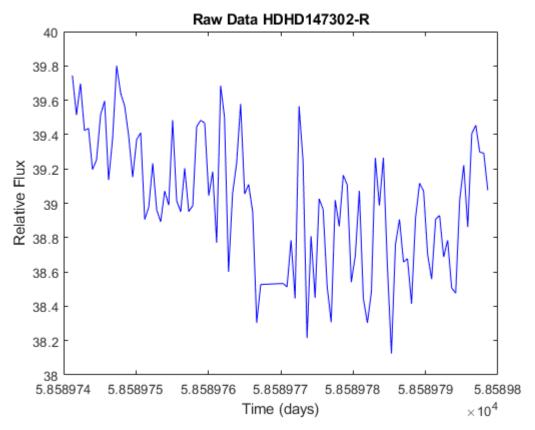
plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')
```



HD147302_R

Plot the raw data

```
plot(HD147302_R(:,1),HD147302_R(:,2),'b');
title('Raw Data HDHD147302-R');
xlabel('Time (days)');
ylabel('Relative Flux');
```

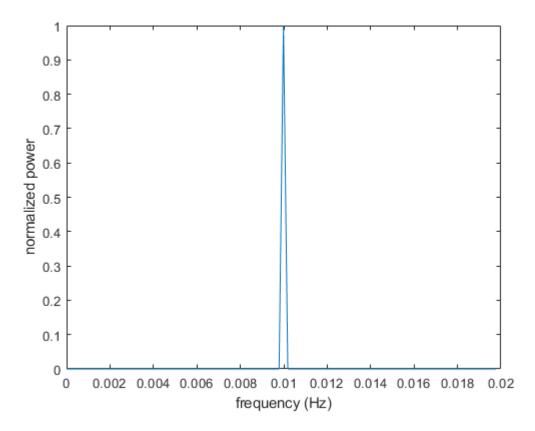


```
avg_freq =1/( mean( diff(HD147302_R(:,1)) ) *86400 )
```

avg_freq =
 0.019970951344655

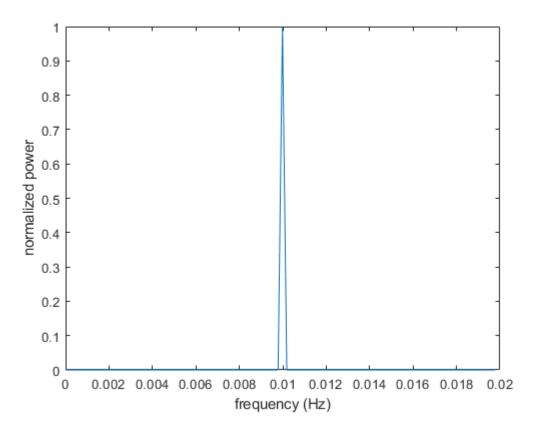
Use Linear Interpolation, then use a Fourier transform to attain the power spectrum

```
[Tnew,Mnew] = Interp_Lin(HD147302_R(:,1),HD147302_R(:,2));
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```



Use Spline Interpolation, then use a Fourier transform to attain the power spectrum

```
[Tnew,Mnew] = Interp_spline(HD147302_R(:,1),HD147302_R(:,2));
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```



Try non-uniform built in function "nufft"

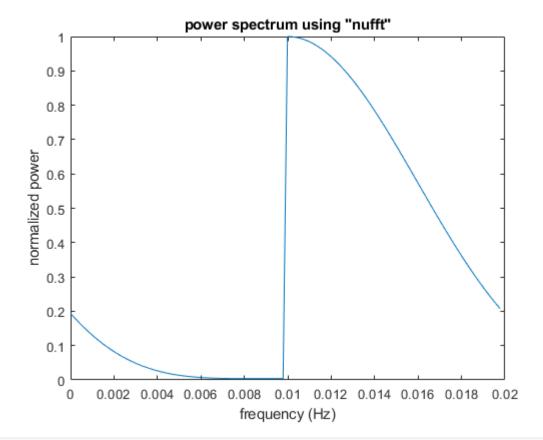
```
N = length(HD147302_R(:,1));
F = nufft( HD147302_R(:,1),HD147302_R(:,2) )/N;
F0 = fftshift(F);

power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')
```



[Tnew,Mnew] = Interp_Lin(HD147302_V(:,1),HD147302_V(:,2));
Tnews = Tnew*86400; %convert time from days to seconds

dt = Tnews(2) - Tnews(1);

[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);

```
key_freq = 0.00998548

key_freq = 0.009985480000000

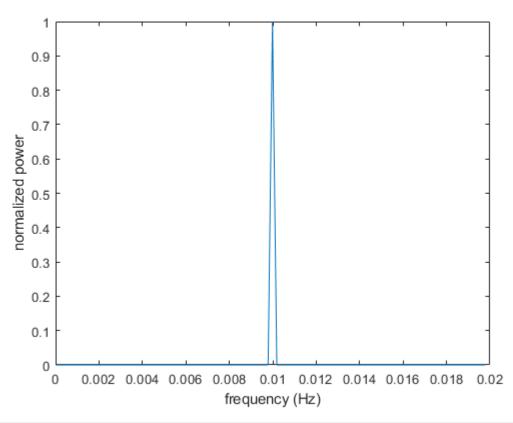
avg_freq =1/( mean( diff(HD147302_R(:,1)) ) *86400 )

avg_freq = 0.019970951344655

avg_freq/key_freq

ans = 1.999999133206939

%V
avg_freq =1/( mean( diff(HD147302_V(:,1)) ) *86400 );
```



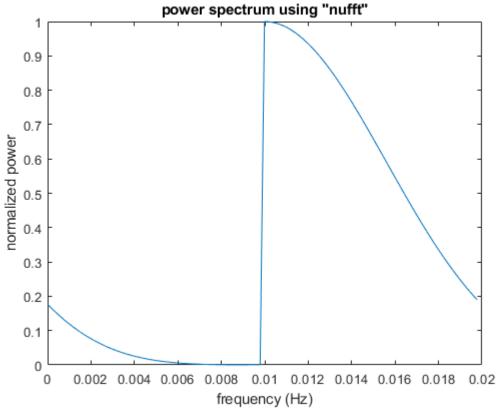
```
N = length(HD147302_V(:,1));
F = nufft( HD147302_V(:,1),HD147302_V(:,2) )/N;
F0 = fftshift(F);

power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')
```



```
key_freq = 0.00998635

key_freq = 0.009986350000000

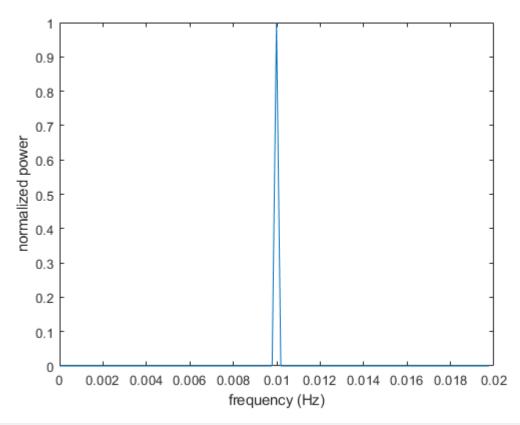
avg_freq =1/( mean( diff(HD147302_V(:,1)) ) *86400 )

avg_freq = 0.019972691882309

avg_freq/key_freq
```

```
ans = 1.999999187121354
```

```
%B
avg_freq =1/( mean( diff(HD147302_B(:,1)) ) *86400 );
[Tnew,Mnew] = Interp_Lin(HD147302_B(:,1),HD147302_B(:,2));
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```



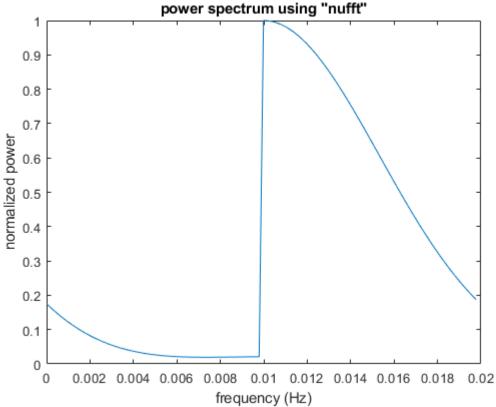
```
N = length(HD147302_B(:,1));
F = nufft( HD147302_B(:,1),HD147302_B(:,2) )/N;
F0 = fftshift(F);

power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')
```



```
key_freq = 0.00998669

key_freq = 0.00998669000000

avg_freq =1/( mean( diff(HD147302_B(:,1)) ) *86400 )

avg_freq = 0.019973388183336

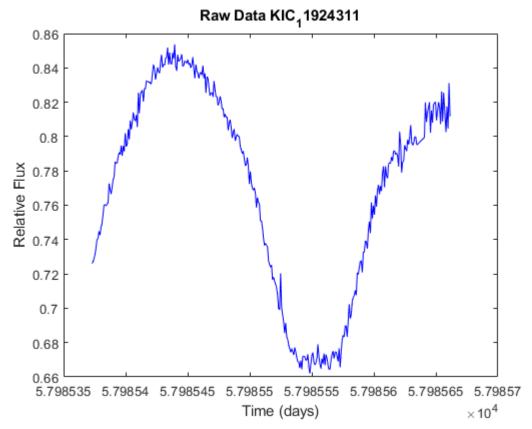
avg_freq/key_freq

ans = 2.000000819424234
```

KIC_11924311

Plot the raw data

```
plot(KIC_11924311.V_time,KIC_11924311.V_flux,'b');
title('Raw Data KIC_11924311');
xlabel('Time (days)');
ylabel('Relative Flux');
```

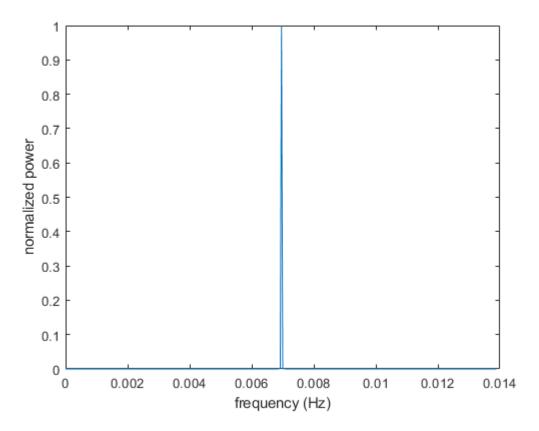


```
avg_freq =1/( mean( diff(KIC_11924311.V_time) ) *86400 )
```

avg_freq =
 0.013917606486280

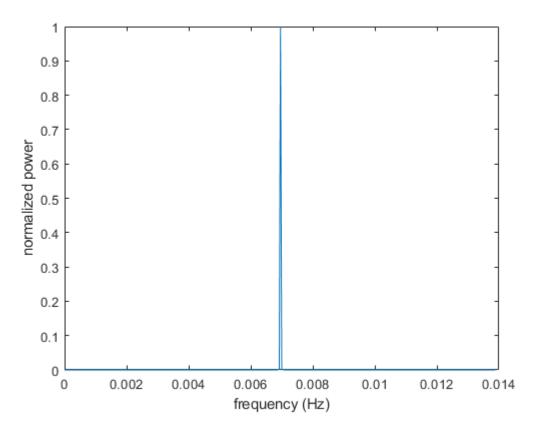
Use Linear Interpolation, then use a Fourier transform to attain the power spectrum

```
[Tnew,Mnew] = Interp_Lin(KIC_11924311.V_time,KIC_11924311.V_flux);
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```



Use Spline Interpolation, then use a Fourier transform to attain the power spectrum

```
[Tnew,Mnew] = Interp_spline(KIC_11924311.V_time,KIC_11924311.V_flux);
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(Tnews,Mnew,dt);
```



Try non-uniform built in function "nufft"

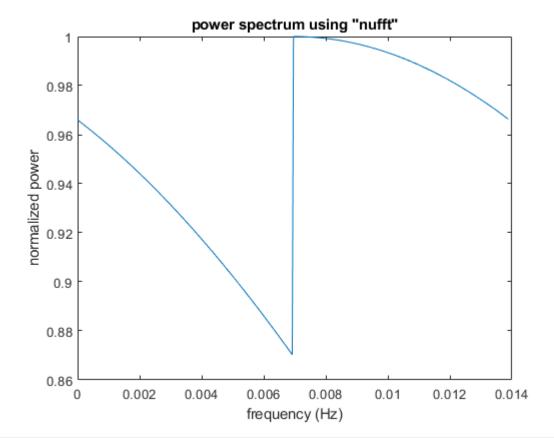
```
N = length(KIC_11924311.V_time);
F = nufft( KIC_11924311.V_time,KIC_11924311.V_flux )/N;
F0 = fftshift(F);

power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')
```



```
key_freq = 0.0069588
```

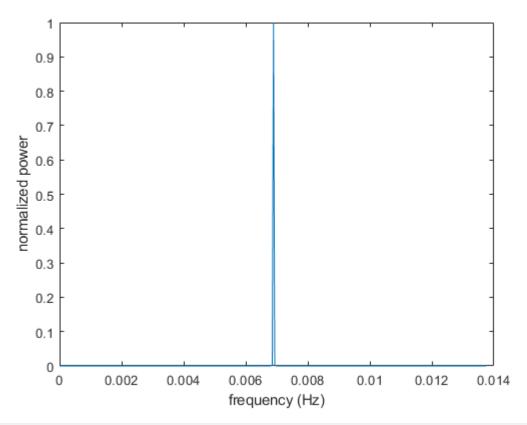
```
avg_freq =1/( mean( diff(KIC_11924311.V_time) ) *86400 )
```

avg_freq =
 0.013917606486280

avg_freq/key_freq

ans =

```
%B
avg_freq =1/( mean( diff(KIC_11924311.B_time) ) *86400 );
[Tnew,Mnew] = Interp_spline(KIC_11924311.B_time,KIC_11924311.B_flux);
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(KIC_11924311.B_time,KIC_11924311.B_flux,dt);
```



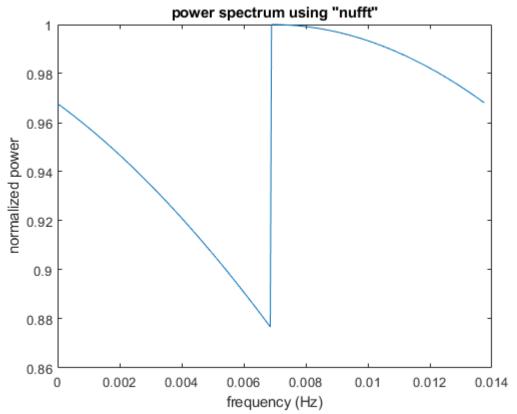
```
N = length(KIC_11924311.B_time);
F = nufft( KIC_11924311.B_time,KIC_11924311.B_flux )/N;
F0 = fftshift(F);

power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')
```



```
key_freq = 0.00689501

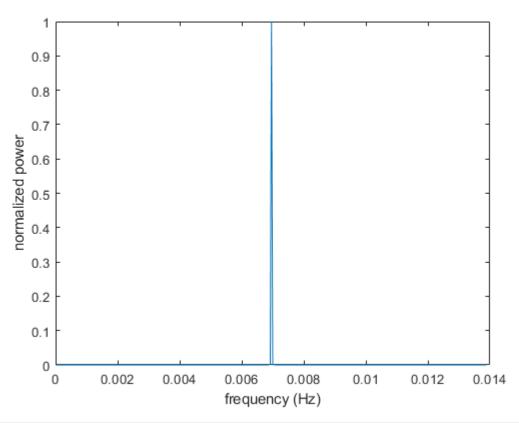
key_freq = 0.006895010000000

avg_freq =1/( mean( diff(KIC_11924311.B_time) ) *86400 )

avg_freq = 0.013790014090173

avg_freq/key_freq
ans =
```

```
%R
avg_freq =1/( mean( diff(KIC_11924311.R_time) ) *86400 );
[Tnew,Mnew] = Interp_spline(KIC_11924311.R_time,KIC_11924311.R_flux);
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(KIC_11924311.R_time,KIC_11924311.R_flux,dt);
```



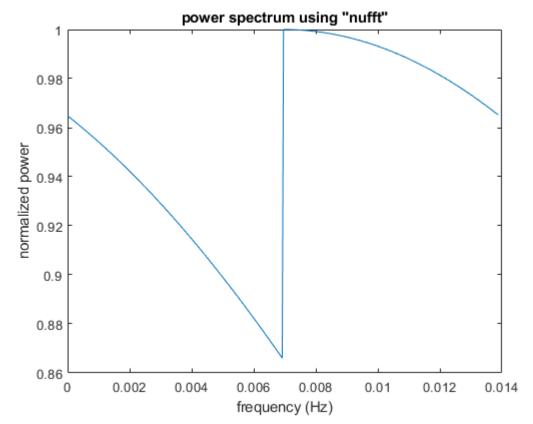
```
N = length(KIC_11924311.R_time);
F = nufft( KIC_11924311.R_time,KIC_11924311.R_flux )/N;
F0 = fftshift(F);

power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')
```



```
key_freq = 0.0069588

key_freq =
   0.006958800000000
```

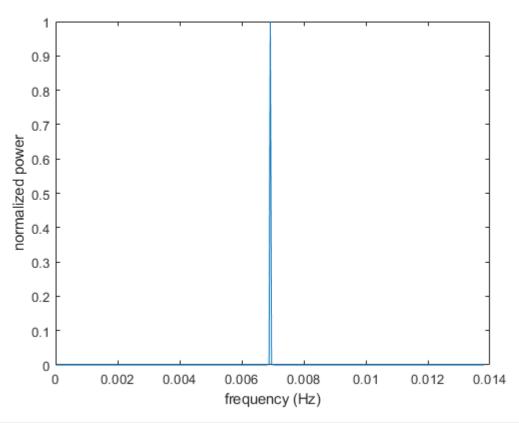
```
avg_freq =1/( mean( diff(KIC_11924311.R_time) ) *86400 )
```

avg_freq =
 0.013917606486280

avg_freq/key_freq

ans = 2.000000932097445

```
%I
avg_freq =1/( mean( diff(KIC_11924311.I_time) ) *86400 );
[Tnew,Mnew] = Interp_spline(KIC_11924311.I_time,KIC_11924311.I_flux);
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(KIC_11924311.I_time,KIC_11924311.I_flux,dt);
```



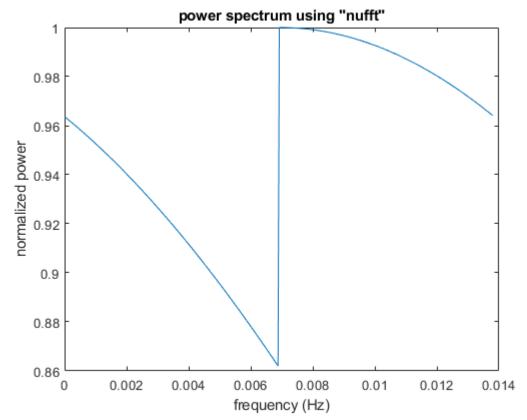
```
N = length(KIC_11924311.I_time);
F = nufft( KIC_11924311.I_time,KIC_11924311.I_flux )/N;
F0 = fftshift(F);

power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')
```



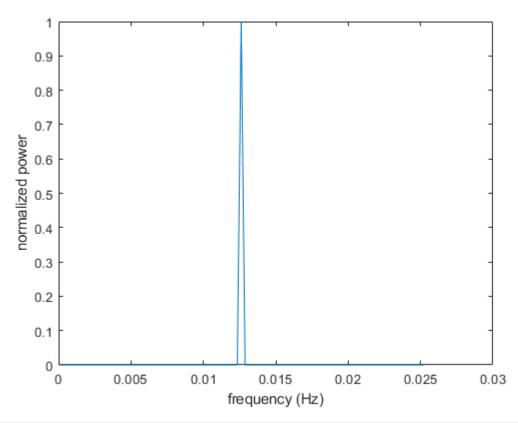
avg_freq =
 0.013839433851694

avg_freq/key_freq

ans = 1.999999111480495

```
%BD48_1098
BD48_1098 = BD48_1098(2:end,:);
%B
avg_freq =1/( mean( diff(BD48_1098(:,1)) ) *86400 );

[Tnew,Mnew] = Interp_spline(BD48_1098(:,1),BD48_1098(:,2));
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(BD48_1098(:,1),BD48_1098(:,2),dt);
```



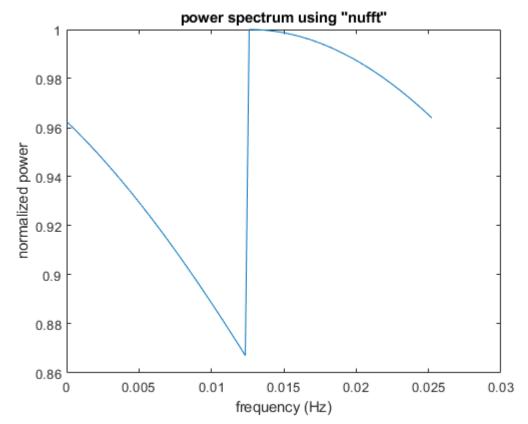
```
N = length(BD48_1098(:,1));
F = nufft(BD48_1098(:,1),BD48_1098(:,2))/N;
F0 = fftshift(F);

power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')
```

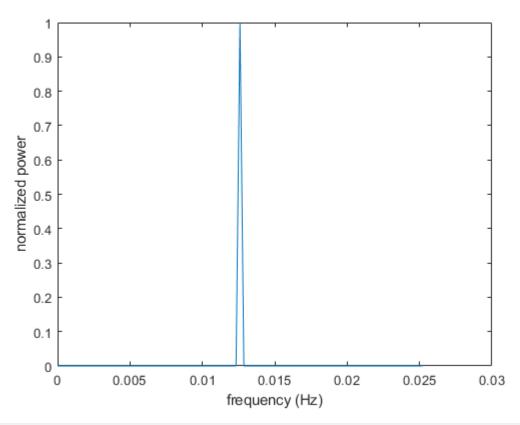


avg_freq = 0.025491165955887

avg_freq/key_freq

ans = 1.999307133795079

```
%R
avg_freq =1/( mean( diff(BD48_1098(:,3)) ) *86400 );
[Tnew,Mnew] = Interp_spline(BD48_1098(:,3),BD48_1098(:,4));
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(BD48_1098(:,3),BD48_1098(:,4),dt);
```



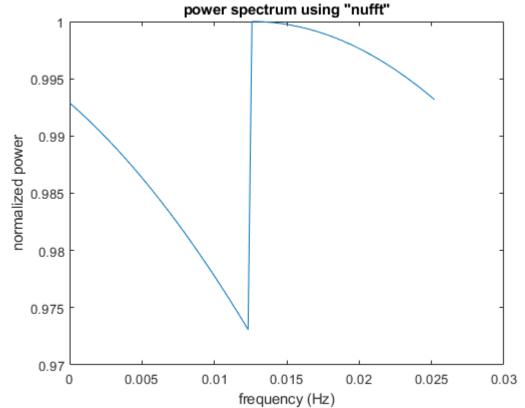
```
N = length(BD48_1098(:,3));
F = nufft(BD48_1098(:,3),BD48_1098(:,4) )/N;
F0 = fftshift(F);

power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

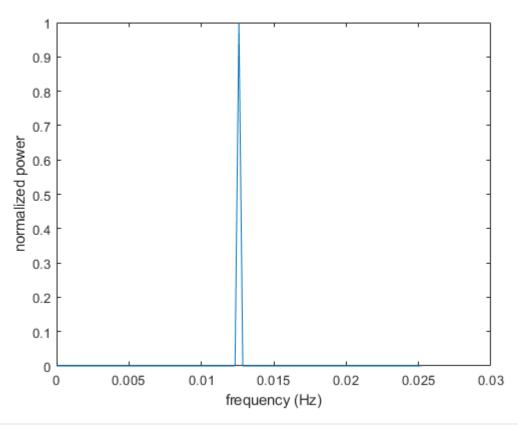
plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')
```



```
avg_freq/key_freq
```

ans = 2.021270473264992

```
%V
avg_freq =1/( mean( diff(BD48_1098(:,5)) ) *86400 );
[Tnew,Mnew] = Interp_spline(BD48_1098(:,5),BD48_1098(:,6));
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(BD48_1098(:,5),BD48_1098(:,6),dt);
```



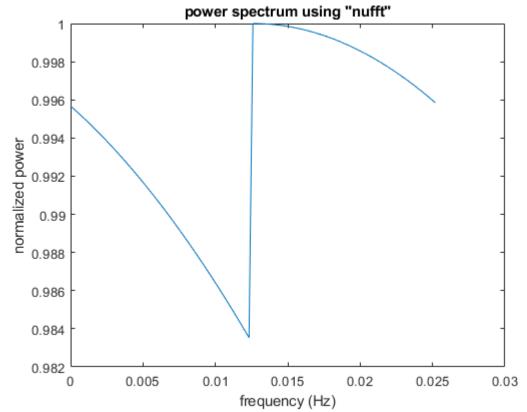
```
N = length(BD48_1098(:,5));
F = nufft(BD48_1098(:,5),BD48_1098(:,6) )/N;
F0 = fftshift(F);

power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')
```



```
key_freq = 0.0127234

key_freq =
    0.012723400000000

avg_freq =1/( mean( diff(BD48_1098(:,5)) ) *86400 )

avg_freq =
    0.025455380510899
```

```
avg_freq/key_freq
```

ans = 2.000674388205868

```
%BD5_441
BD55_441 = BD55_441(2:end-1,:);
%V
avg_freq =1/( mean( diff(BD55_441(:,5)) ) *86400 );

[Tnew,Mnew] = Interp_spline(BD55_441(:,5),BD55_441(:,6));
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(BD55_441(:,5),BD55_441(:,6),dt);
```

```
1
    0.9
    0.8
   0.7
normalized power
    0.6
    0.5
   0.4
    0.3
   0.2
    0.1
     0
       0
                  0.005
                                 0.01
                                              0.015
                                                             0.02
                                                                          0.025
                                                                                        0.03
                                        frequency (Hz)
```

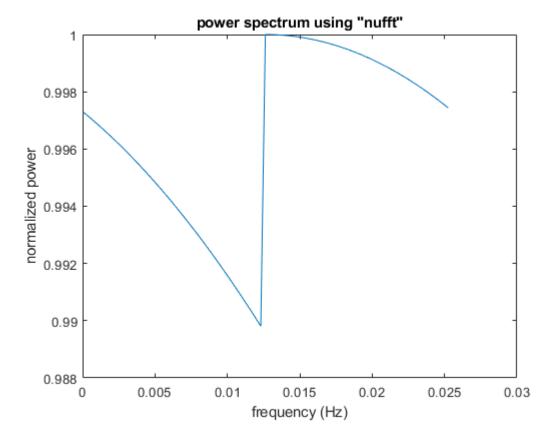
```
N = length(BD55_441(:,5));
F = nufft(BD55_441(:,5),BD55_441(:,6))/N;
F0 = fftshift(F);

power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')
```



```
key_freq = 0.0127232
```

```
avg_freq =1/( mean( diff(BD55_441(:,5)) ) *86400 )
```

avg_freq =
 0.025563940526795

avg_freq/key_freq

ans =

```
%B
avg_freq =1/( mean( diff(BD55_441(:,1)) ) *86400 );

[Tnew,Mnew] = Interp_spline(BD55_441(:,1),BD55_441(:,2));
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(BD55_441(:,1),BD55_441(:,2),dt);
```

```
1
   0.9
   0.8
   0.7
normalized power
   0.6
   0.5
   0.4
   0.3
   0.2
   0.1
     0
       0
                  0.005
                                 0.01
                                              0.015
                                                            0.02
                                                                          0.025
                                                                                        0.03
                                        frequency (Hz)
```

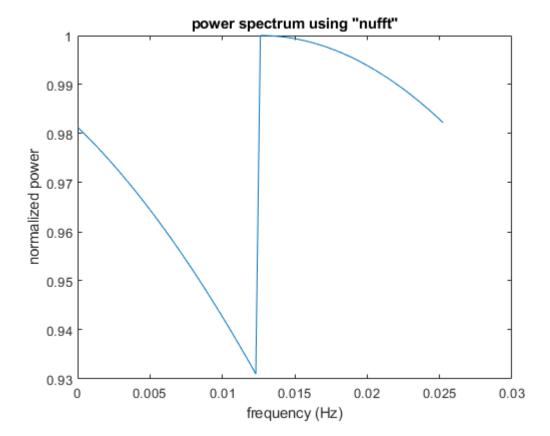
```
N = length(BD55_441(:,1));
F = nufft(BD55_441(:,1),BD55_441(:,2))/N;
F0 = fftshift(F);

power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')
```



```
key_freq = 0.0127699
```

```
avg_freq =1/( mean( diff(BD55_441(:,1)) ) *86400 )
```

avg_freq =
 0.025563940526795

avg_freq/key_freq

ans =

```
%R
avg_freq =1/( mean( diff(BD55_441(:,3)) ) *86400 );

[Tnew,Mnew] = Interp_spline(BD55_441(:,3),BD55_441(:,4));
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(BD55_441(:,3),BD55_441(:,4),dt);
```

```
1
   0.9
   0.8
   0.7
normalized power
   0.6
   0.5
   0.4
   0.3
   0.2
   0.1
     0
       0
                  0.005
                                 0.01
                                              0.015
                                                            0.02
                                                                          0.025
                                                                                        0.03
                                        frequency (Hz)
```

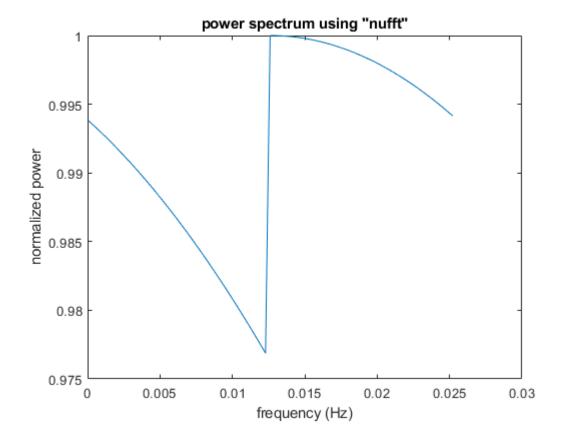
```
N = length(BD55_441(:,3));
F = nufft(BD55_441(:,3),BD55_441(:,4))/N;
F0 = fftshift(F);

power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')
```



```
key_freq = 0.0127829
```

```
avg_freq =1/( mean( diff(BD55_441(:,3)) ) *86400 )
```

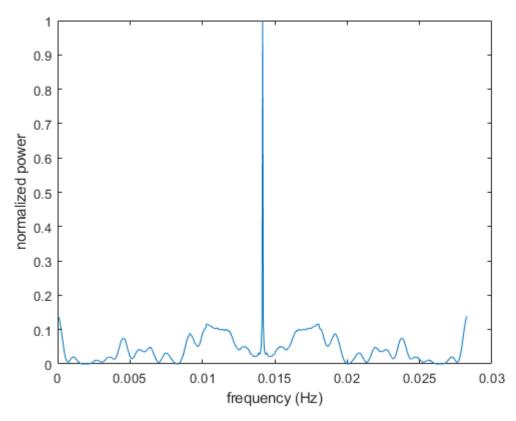
avg_freq =
 0.025528699366024

avg_freq/key_freq

ans = 1.997097635593180

```
%HD28497
%B
avg_freq =1/( mean( diff(HD28497(:,1)) ) *86400 );

[Tnew,Mnew] = Interp_spline(HD28497(:,1),HD28497(:,2));
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(HD28497(:,1),HD28497(:,2),dt);
```



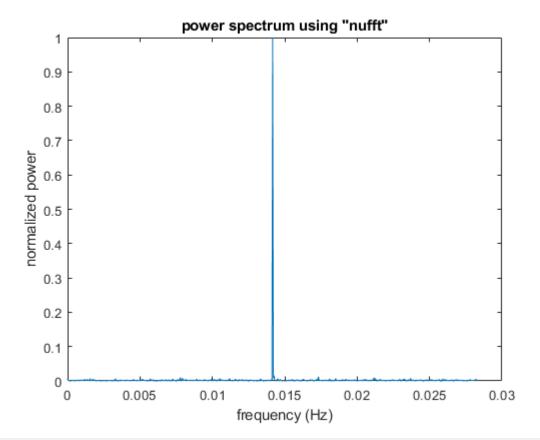
```
N = length(HD28497(:,1));
F = nufft(HD28497(:,1), HD28497(:,2) )/N;
F0 = fftshift(F);

power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')
```



```
key_freq = 0.0141626

key_freq = 0.014162600000000

avg_freq =1/( mean( diff(HD28497(:,1)) ) *86400 )

avg_freq = 0.028325177195336

avg_freq/key_freq

ans = 1.999998389796817

%R
```

```
%R
avg_freq =1/( mean( diff(HD28497(:,3)) ) *86400 );

[Tnew,Mnew] = Interp_spline(HD28497(:,3),HD28497(:,4));
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(HD28497(:,3),HD28497(:,4),dt);
```

```
1
   0.9
   0.8
   0.7
normalized power
   0.6
   0.5
   0.4
   0.3
   0.2
   0.1
     0
       0
                  0.005
                                 0.01
                                              0.015
                                                            0.02
                                                                          0.025
                                                                                        0.03
                                        frequency (Hz)
```

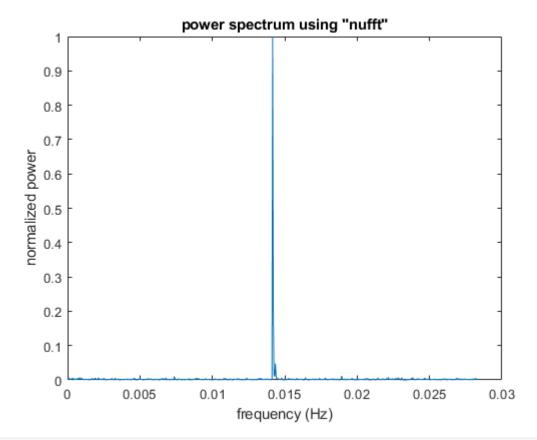
```
N = length(HD28497(:,3));
F = nufft(HD28497(:,3), HD28497(:,4) )/N;
F0 = fftshift(F);

power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')
```



```
key_freq = 0.0141626

key_freq = 0.0141626000000000

avg_freq =1/( mean( diff(HD28497(:,3)) ) *86400 )

avg_freq = 0.028325177196178

avg_freq/key_freq

ans = 1.999998389856271

%V
```

```
%V
avg_freq =1/( mean( diff(HD28497(:,5)) ) *86400 );

[Tnew,Mnew] = Interp_spline(HD28497(:,5),HD28497(:,6));
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(HD28497(:,5),HD28497(:,6),dt);
```

```
1
   0.9
   0.8
   0.7
normalized power
   0.6
   0.5
   0.4
   0.3
   0.2
   0.1
     0
       0
                  0.005
                                 0.01
                                              0.015
                                                            0.02
                                                                         0.025
                                                                                        0.03
                                        frequency (Hz)
```

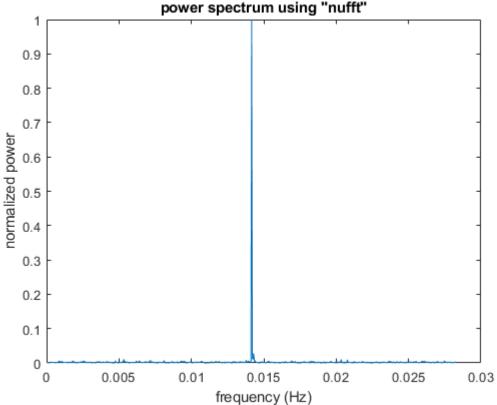
```
N = length(HD28497(:,5));
F = nufft(HD28497(:,5),HD28497(:,6) )/N;
F0 = fftshift(F);

power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')
```



```
key_freq = 0.0141626

key_freq = 0.014162600000000

avg_freq =1/( mean( diff(HD28497(:,5)) ) *86400 )

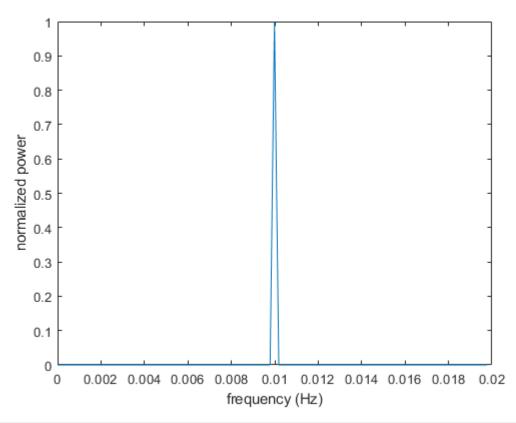
avg_freq = 0.028325177195336

avg_freq/key_freq
```

```
ans = 1.999998389796817
```

```
%HD152060
%R
avg_freq =1/( mean( diff(HD152060(:,1)) ) *86400 );

[Tnew,Mnew] = Interp_spline(HD152060(:,1),HD152060(:,2));
Tnews = Tnew*86400; %convert time from days to seconds
dt = Tnews(2) - Tnews(1);
[fk,powerNor] = EnergySpec(HD152060(:,1),HD152060(:,2),dt);
```



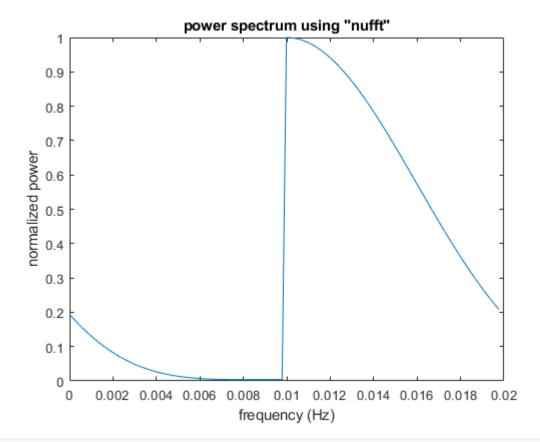
```
N = length(HD152060(:,1));
F = nufft(HD152060(:,1),HD152060(:,2))/N;
F0 = fftshift(F);

power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')
```



dt = Tnews(2) - Tnews(1);

[fk,powerNor] = EnergySpec(HD152060(:,3),HD152060(:,4),dt);

```
key_freq = 0.00998548

key_freq = 0.009985480000000

avg_freq =1/( mean( diff(HD152060(:,1)) ) *86400 )

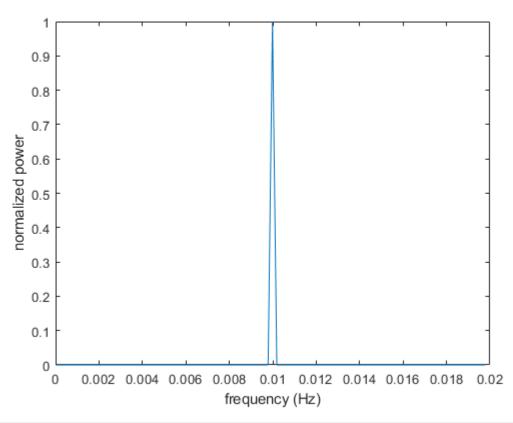
avg_freq = 0.019970951344655

avg_freq/key_freq

ans = 1.999999133206939

%V
avg_freq =1/( mean( diff(HD152060(:,3)) ) *86400 );

[Tnew,Mnew] = Interp_spline(HD152060(:,3),HD152060(:,4));
Tnews = Tnew*86400; %convert time from days to seconds
```



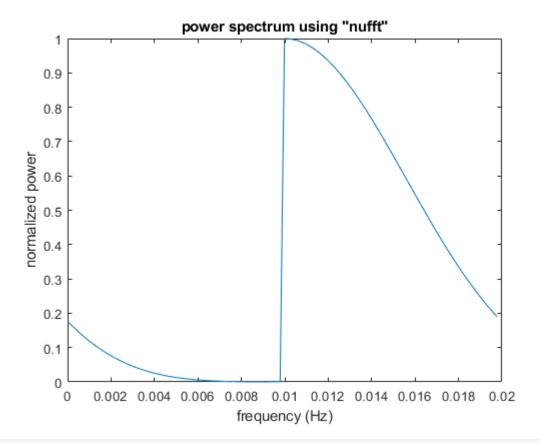
```
N = length(HD152060(:,3));
F = nufft(HD152060(:,3),HD152060(:,4) )/N;
F0 = fftshift(F);

power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')
```



[Tnew,Mnew] = Interp_spline(HD209522(:,1),HD209522(:,2));
Tnews = Tnew*86400; %convert time from days to seconds

[fk,powerNor] = EnergySpec(HD209522(:,1),HD209522(:,2),dt);

dt = Tnews(2) - Tnews(1);

```
key_freq = 0.00998635

key_freq = 0.009986350000000

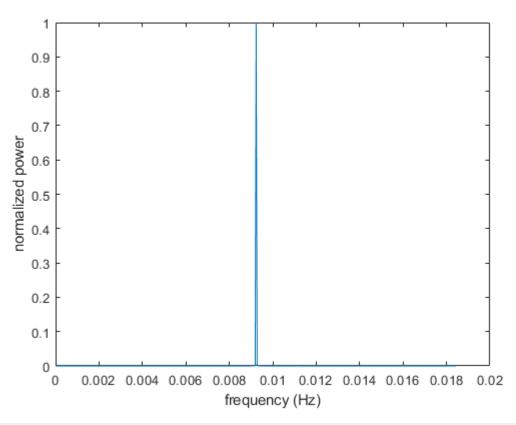
avg_freq =1/( mean( diff(HD152060(:,3)) ) *86400 )

avg_freq = 0.019972691882309

avg_freq/key_freq

ans = 1.999999187121354

%HD209522
avg_freq =1/( mean( diff(HD209522(:,1)) ) *86400 );
```



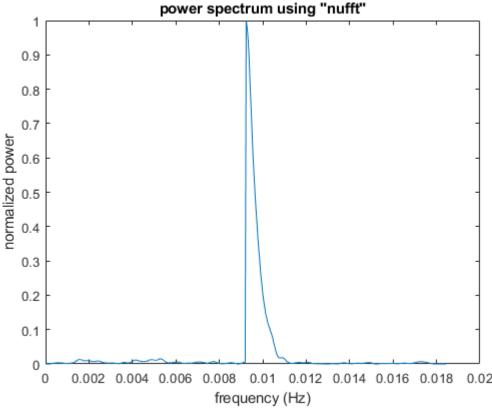
```
N = length(HD209522(:,1));
F = nufft(HD209522(:,1),HD209522(:,2))/N;
F0 = fftshift(F);

power = F0.*conj(F0)/N;

powerNor = power/max(power);

%Plot power Spectrum
fs = avg_freq;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
title('power spectrum using "nufft"')
```



```
key_freq = 0.00923606

key_freq = 0.009236060000000

avg_freq =1/( mean( diff(HD209522(:,1)) ) *86400 )

avg_freq = 0.018472115837205

avg_freq/key_freq

ans = 1.999999549288869
```

Interpolation Functions

There are two different linear interpolation functions - the first is without built-in functions and the other is built-in. The results from both functions are similar.

Other interpolation methods are displayed.

Custom functions

```
function [Tnew,Mnew] = Interp_Lin(T,M)
%This is Joe's custom linear interpolation:
%----
```

```
% --Sum all of the time differences between measurements--
n = numel(T);
sum = 0;
for 1 = 1:n-1
    sum = sum + abs(T(1+1) - T(1));
end
% --Find averaged time scale--
avg_dT = sum / (n-1);
Tnew = T(1):avg_dT:T(n);
% --Calculate Mnew values--
m = numel(Tnew);
Mnew = zeros(1,m);
Mnew(1) = M(1);
Mnew(m) = M(n);
for 1 = 2:m-1
    for k = 1:n
        if T(k) \leftarrow Tnew(1)
            if Tnew(1) <= T(k+1)
                Mnew(1) = (M(k+1) - M(k))./(T(k+1) - T(k)).*(Tnew(1)-T(k)) + M(k);
                %eq for a line. i.e. y = mx + b
            end
        end
    end
end
end
```

Various built-in Matlab Functions

```
function [Tnew,Mnew] = Interp_nearest(T,M)
%This uses the built-in function 'interp1' with method 'nearest'
%----

% --Sum all of the time differences between measurements--
n = numel(T);
sum = 0;
for l = 1:n-1
    sum = sum + abs(T(l+1) - T(l));
end

% --Find averaged time scale--
avg_dT = sum / (n-1);
Tnew = T(1):avg_dT:T(n);

% --Calculate Mnew values--
Mnew = interp1(T,M,Tnew,'nearest');
end
```

```
function [Tnew,Mnew] = Interp_linear(T,M)
%This uses the built-in function 'interp1' with method 'linear'
%----
% --Sum all of the time differences between measurements--
n = numel(T);
sum = 0;
for l = 1:n-1
    sum = sum + abs(T(l+1) - T(l));
end
% --Find averaged time scale--
avg_dT = sum / (n-1);
Tnew = T(1):avg_dT:T(n);
%--Calculate Mnew values--
Mnew = interp1(T,M,Tnew,'linear');
end
```

```
function [Tnew,Mnew] = Interp_spline(T,M)
%This uses the built-in function 'interp1' with method 'spline'
%----

% --Sum all of the time differences between measurements--
n = numel(T);
sum = 0;
for l = 1:n-1
    sum = sum + abs(T(l+1) - T(l));
end

% --Find averaged time scale--
avg_dT = sum / (n-1);
Tnew = T(1):avg_dT:T(n);

% --Calculate Mnew values--
Mnew = interp1(T,M,Tnew,'spline');
end
```

```
function [Tnew,Mnew] = Interp_polyfit(T,M)
%This uses the built-in function 'interp1' with method 'polyfit'
%----
% --Sum all of the time differences between measurements--
n = numel(T);
sum = 0;
for l = 1:n-1
    sum = sum + abs(T(l+1) - T(l));
end
```

```
% --Find averaged time scale--
avg_dT = sum / (n-1);
Tnew = T(1):avg_dT:T(n);

% --Calculate Mnew values--
n = numel(T);
p = polyfit(T,M,5);
Mnew = polyval(p,Tnew);
end
```

Joe's linear combo of non-linear functions function

```
function C = NLfit(F1,F2,F3,x,y)
%documentation: This program was developed from Gilat example 6-9
F1 = F1(x);
F2 = F2(x);
F3 = F3(x);
A(1,1) = sum(F1 .* F1);
A(1,2) = sum(F1 .* F2);
A(1,3) = sum(F1 .* F3);
A(2,2) = sum(F2 .* F2);
A(2,3) = sum(F2 .* F3);
A(3,3) = sum(F3 .* F3);
A(2,1) = A(1,2);
                  % A is symmetric
A(3,1) = A(1,3);
A(3,2) = A(2,3);
B(1,1) = sum(y .* F1);
B(2,1) = sum(y .* F2);
B(3,1) = sum(y .* F3);
%form is A*C=B, Therefore,
C = A \setminus B;
end
```

Joe's power spectrum function

```
function [fk,powerNor] = EnergySpec(t,f,dt)
%this function is developed with reference to Gilat Program 7-4 and Example
%7-6

N = length(f);
F = fft(f)/N;
F0 = fftshift(F);

power = F0.*conj(F0)/N;

powerNor = power/max(power);
```

```
%Plot power Spectrum
fs = 1/dt;
fk = (0:N-1)*(fs/N);

plot(fk, powerNor)
xlabel('frequency (Hz)')
ylabel('normalized power')
end
```