Assignment 2: Verification

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1 Part A

Given

$$pre \triangleq D.len \geqslant max(\{A.len, B.len, C.len\})$$

 $\land sorted(A) \land sorted(B) \land sorted(C)$

and

$$post \triangleq D = A \cap B \cap C$$

$$\triangleq D_{[0,D.len)} = A_{[0,A.len)} \cap B_{[0,B.len)} \cap C_{[0,C.len)}$$

 $\sqsubseteq \quad \{ \text{Composition: middle predicate is } \textit{inv} \}$

$$i, j, k, r, D : [pre, inv]; i, j, k, r, D : [inv, post]$$

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$$inv \triangleq D_{[0,r)} = A_{[0,i)} \cap B_{[0,j)} \cap C_{[0,k)}$$

$$\wedge r \in [0, D.len] \wedge i \in [0, A.len] \wedge j \in [0, B.len] \wedge k \in [0, C.len]$$

. .

$$\begin{array}{lll} inv[i,j,k,r\backslash 0,0,0,0] & \equiv & D_{[0,0)} = A_{[0,0)} \, \cap \, B_{[0,0)} \, \cap \, C_{[0,0)} \\ & \wedge \, 0 \in [0,D.len] \, \wedge \, 0 \in [0,A.len] \, \wedge \, 0 \in [0,B.len] \, \wedge \, 0 \in [0,C.len] \\ & \equiv & \varnothing = (\varnothing \, \cap \, \varnothing \, \cap \, \varnothing) \, \wedge \, (\text{true } \wedge \, \text{true } \wedge \, \text{true}) \\ & \equiv & \varnothing = \varnothing \, \wedge \, \text{true} \\ & \equiv & \text{true} \end{array}$$

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$$inv \land \neg (i \neq A.len \lor j \neq B.len \lor k \neq C.len) \Rrightarrow post \equiv inv \land (i = A.len \land j = B.len \land k = C.len) \Rrightarrow post \equiv TODO$$

$$((a \land b) \Rrightarrow (a \land c)) \equiv (b \Rrightarrow c)$$

$$\sqsubseteq \text{ {Repetition Rule } \atop i,j,k,r:=0,0,0,0; \\ \textbf{do } (i \neq A.len \lor j \neq B.len \lor k \neq C.len) \rightarrow \atop i,j,k,r,D:[inv \land (i \neq A.len \lor j \neq B.len \lor k \neq C.len), inv \land (0 \leqslant V < V_0)]$$

$$\textbf{od}$$

$$V \triangleq (A.len - i) + (B.len - j) + (C.len - k)$$

 $\triangleq (A.len + B.len + C.len) - (i + j + k)$