Assignment 2: Verification

Maxwell Bo 43926871 April 12, 2017

1 Part A

Given

$$pre \triangleq D.len \geqslant max(\{A.len, B.len, C.len\})$$

 $\land sorted(A) \land sorted(B) \land sorted(C)$

and

$$post \triangleq D = A \cap B \cap C$$

$$\wedge r \in [0, D.len] \wedge i \in [0, A.len] \wedge j \in [0, B.len] \wedge k \in [0, C.len]$$

$$\wedge (i = A.len \vee j = B.len \vee k = C.len)$$

i, j, k, r, D : [pre, post]

 \sqsubseteq {Composition: middle predicate is inv} i, j, k, r, D : [pre, inv]; i, j, k, r, D : [inv, post]

. .

$$inv \triangleq D_{[0,r)} = A_{[0,i)} \cap B_{[0,j)} \cap C_{[0,k)}$$

$$\wedge r \in [0, D.len] \wedge i \in [0, A.len] \wedge j \in [0, B.len] \wedge k \in [0, C.len]$$

. .

$$\begin{array}{lll} \operatorname{inv}[i,j,k,r \backslash 0,0,0,0] & \equiv & D_{[0,0)} = A_{[0,0)} \, \cap \, B_{[0,0)} \, \cap \, C_{[0,0)} \\ & \wedge \, 0 \in [0,D.len] \, \wedge \, 0 \in [0,A.len] \, \wedge \, 0 \in [0,B.len] \, \wedge \, 0 \in [0,C.len] \\ & \equiv & \varnothing = (\varnothing \, \cap \, \varnothing \, \cap \, \varnothing) \, \wedge \, (\operatorname{true} \, \wedge \, \operatorname{true} \, \wedge \, \operatorname{true} \, \wedge \, \operatorname{true}) \\ & \equiv & \operatorname{true} \end{array}$$

 $\begin{array}{l} \cdots \\ inv \land \neg (i \neq A.len \ \lor \ j \neq B.len \ \lor \ k \neq C.len) \Rrightarrow post & \equiv inv \land (i = A.len \ \land \ j = B.len \ \land \ C.len) \Rrightarrow post \\ \\ \sqsubseteq & \{ \text{Repetition Rule} \} \\ & i,j,k,r := 0,0,0,0; \\ & \mathbf{do} \ (i \neq A.len \ \lor \ j \neq B.len \ \lor \ k \neq C.len) \rightarrow \\ & i,j,k,r,D : [inv \ \land \ (i \neq A.len \ \lor \ j \neq B.len \ \lor \ k \neq C.len), \ inv \ \land \ (0 \leqslant V < V_0)] \\ & \mathbf{od} \\ \end{array}$