

12.1-2

The binary-search-tree property guarantees that for any parent node, all nodes in the left subtree will be \leq the parent and all nodes in the right subtree will be \geq the parent. The min-heap property guarantees that for every parent node, both of its children will be \geq the parent. While the binary-search-tree invariant guarantees that a tree always remain sorted left to right, the min-heap invariant only mandates that each ancestry chain remain sorted against itself; not taking into account other ancestry chains on different parts of the tree. Min-heaps cannot be traversed in $O(n)$ time because, unlike BSTs, they are not globally sorted. In order to sort the heap, one must run an algorithm that recursively:

- 1) moves the last node to the top spot
- 2) percolates the new top node down until it resides in a sorted position

Since step 1 takes $O(n)$ time and step 2 takes $O(\log n)$ time, heapsort is $O(n \log n)$ and thus cannot match the BST's $O(n)$ performance.