

2.3-3

$$T(n) = \begin{cases} 2^n \cdot n - 2 \\ 2T(n/2) + n & n = 2^k, k > 1 \end{cases}$$

$$\begin{aligned} n > 2, \quad T(n) &= 2^k T(n/2^k) + kn \\ &= 2^{\lg n} T(1) + (\lg n)n \\ &= n + n \lg n \\ &= O(n \lg n) \end{aligned}$$

2.3-5

function binarySearch(array, l, r, elem)

if l == r == 0  
return false

else

$$\text{middle} = \frac{r-1}{2}$$

if array[middle] > elem

right = binarySearch(array, middle, r, elem)

if isNumber(right) return right

if array[left] < elem

left = binarySearch(array, l, middle, elem)

if isNumber(left) return left

for i in range(l, r)

if array[i] == elem

return i

return False

In the worst case, binary search will not find the element until the bottom of the search tree. In this case, runtime is  $O(h)$  where  $h$  is the height of the tree. Since  $h$  grows at  $\log_2 n$ , binary search's worst case is  $O(\log_2 n)$ .