

所有倒过来解释为二进制数时不被5整除的串的集合

$h$  是  $\{0, 1, 2\}$  到  $\{a, b\}$  同态,  $h(0) = a, h(1) = ab, h(2) = ba$

(i)  $h(0120) = aabbaa$

② 如果  $L$  是语言  $L(0^*1^*2)$ ,  $h(L) = a(ab)^*ba$

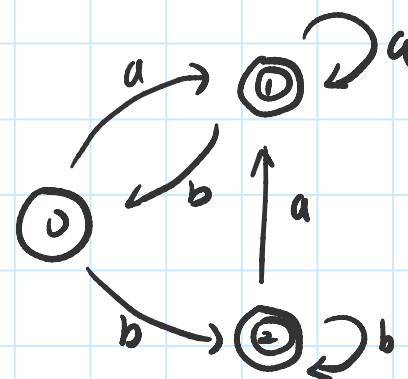
③  $L = \{a b a b a\}$ ,  $h^{-1}(L) = \{110, 102, 022\}$

$$\underbrace{a \ b \ a \ b \ a}_1 \quad \underbrace{a \ b \ a \ b \ a}_1 \quad \underbrace{a}_0$$

$$\underbrace{a}_0 \quad \underbrace{b \ a \ b \ a}_2 \quad \underbrace{a}_2$$

# 自测题

|                   | 0                                    | 1   |
|-------------------|--------------------------------------|---|
| $\rightarrow q_0$ | $r(q_0, 0) = \delta'(q_0, ab) = q_0$ | $r(q_0, 1) = \delta'(q_0, ba) = q_1 \xrightarrow{\text{start}}$ |
| $q_1$             | $r(q_1, 0) = \delta'(q_1, ab) = q_0$ | $r(q_1, 1) = \delta'(q_1, ba) = q_1$                            |
| $q_2$             | $r(q_2, 0) = \delta'(q_2, ab) = q_1$ | $r(q_2, 1) = \delta'(q_2, ba) = q_2$                            |



1. 考虑任意  $n \geq 1$ , 取  $w = 0^n 1^n$

任取  $x, y, z$  使  $w = xyz$  且  $y \neq \varepsilon$  且  $|xy| \leq n$

若  $k=0$ , 则有  $xy^kz = xz \notin L$  (0 的个数不是 1 的两倍)

2.  $w = 1^n 0^{n+1}$ ,  $w = xyz$  且  $y \neq \varepsilon$  且  $|xy| \leq n$

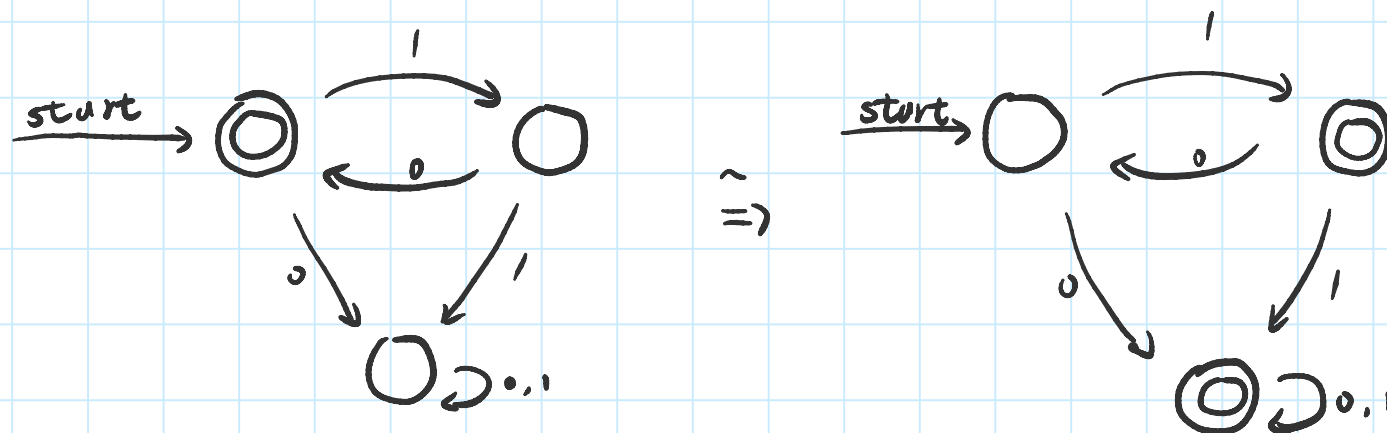
$k=2$   $xy^kz \notin L$

3. 1)  $E = \varepsilon + (a+b)(ba)^*$

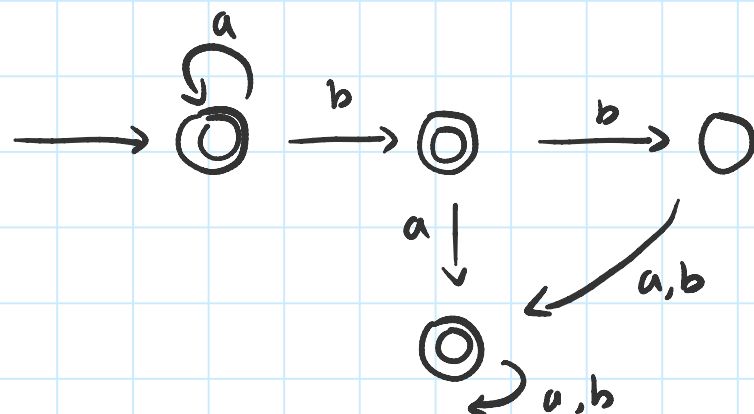
$\Rightarrow E^R = \varepsilon + (ab)^*(a+b)$

$$2) h(E) = \varepsilon + (\varepsilon + 10)(10)^* = (10)^*$$

3)

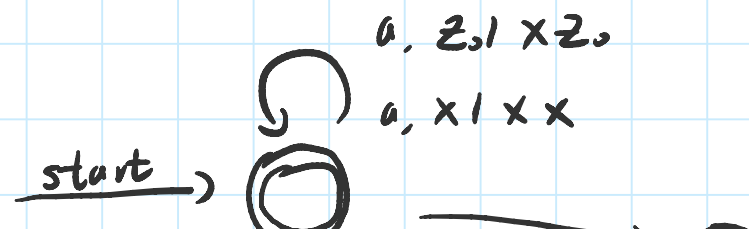


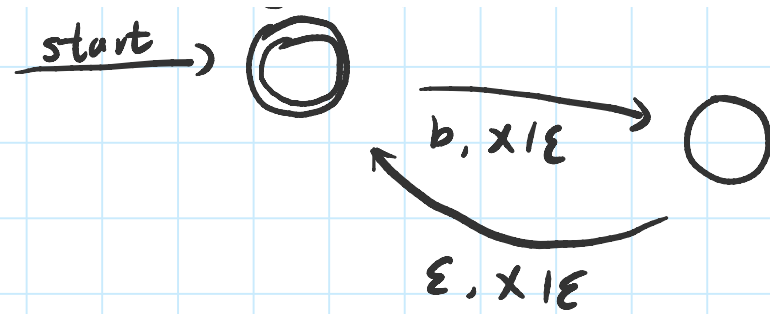
6.



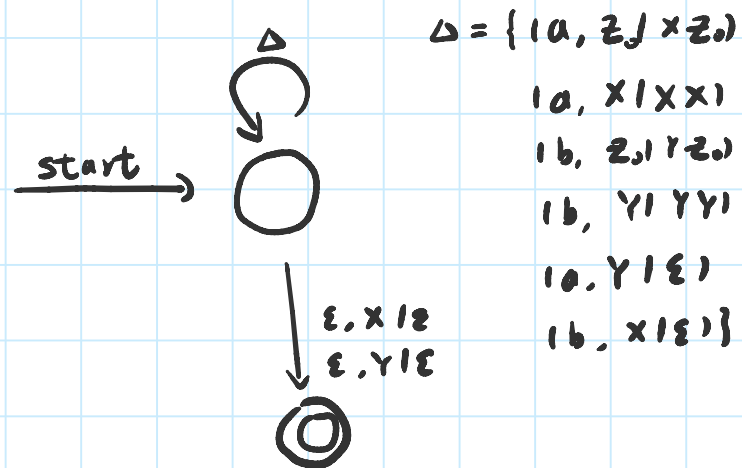
自测题

1)





2)



3)

