



Temperature distribution in an element

$$T(\xi, \eta) = \begin{Bmatrix} (1-\xi)(1-\eta) \\ \xi(1-\eta) \\ \xi \cdot \eta \\ \eta(1-\xi) \end{Bmatrix}^T \begin{Bmatrix} T_0 \\ T_1 \\ T_2 \\ T_3 \end{Bmatrix}$$

$$\begin{Bmatrix} \frac{\partial x}{\partial \xi}(\eta) \\ \frac{\partial x}{\partial \eta}(\xi) \end{Bmatrix} = \begin{bmatrix} -(1-\eta) & (1-\eta) & \eta & -\eta \\ -(1-\xi) & -\xi & \xi & (1-\xi) \end{bmatrix} \begin{Bmatrix} x_0 \\ x_1 \\ x_2 \\ x_3 \end{Bmatrix}$$

$$\begin{Bmatrix} \frac{\partial y}{\partial \xi}(\eta) \\ \frac{\partial y}{\partial \eta}(\xi) \end{Bmatrix} = \begin{bmatrix} -(1-\eta) & (1-\eta) & \eta & -\eta \\ -(1-\xi) & -\xi & \xi & (1-\xi) \end{bmatrix} \begin{Bmatrix} y_0 \\ y_1 \\ y_2 \\ y_3 \end{Bmatrix}$$

Normal {n1} and {n2} to middle lines:

$$Q_{n_1}(\eta) = \frac{\lambda}{\sqrt{\left(\frac{\partial x}{\partial \xi}\right)^2 + \left(\frac{\partial y}{\partial \xi}\right)^2}} \frac{\partial T}{\partial \xi} = \frac{\lambda}{\sqrt{\left(\frac{\partial x}{\partial \xi}\right)^2 + \left(\frac{\partial y}{\partial \xi}\right)^2}} \begin{Bmatrix} -(1-\eta) \\ (1-\eta) \\ \eta \\ -\eta \end{Bmatrix}^T \begin{Bmatrix} T_0 \\ T_1 \\ T_2 \\ T_3 \end{Bmatrix}$$

$$Q_{n_2}(\xi) = \frac{\lambda}{\sqrt{\left(\frac{\partial x}{\partial \eta}\right)^2 + \left(\frac{\partial y}{\partial \eta}\right)^2}} \frac{\partial T}{\partial \eta} = \frac{\lambda}{\sqrt{\left(\frac{\partial x}{\partial \eta}\right)^2 + \left(\frac{\partial y}{\partial \eta}\right)^2}} \begin{Bmatrix} -(1-\xi) \\ -\xi \\ \xi \\ (1-\xi) \end{Bmatrix}^T \begin{Bmatrix} T_0 \\ T_1 \\ T_2 \\ T_3 \end{Bmatrix}$$

Length of middle lines:

$$l_1 = \frac{1}{2} \sqrt{(x_0 + x_1 - x_2 - x_3)^2 + (y_2 + y_3 - y_0 - y_1)^2}$$

$$l_2 = \frac{1}{2} \sqrt{(x_0 + x_3 - x_1 - x_2)^2 + (y_0 + y_3 - y_1 - y_2)^2}$$

$$S_0 = \frac{1}{16} (2x_1y_3 - 2x_3y_1 + (3x_0 - x_2)(y_1 - y_3) + (3y_0 - y_2)(x_3 - x_1))$$

$$S_1 = \frac{1}{16} (2x_2y_0 - 2x_0y_2 + (3x_1 - x_3)(y_2 - y_0) + (3y_1 - y_3)(x_0 - x_2))$$

$$S_2 = \frac{1}{16} (2x_3y_1 - 2x_1y_3 + (3x_2 - x_0)(y_3 - y_1) + (3y_2 - y_0)(x_1 - x_3))$$

$$S_3 = \frac{1}{16} (2x_0y_2 - 2x_2y_0 + (3x_3 - x_1)(y_0 - y_2) + (3y_3 - y_1)(x_2 - x_0))$$