

	0°	30°	45°	60°	90°	120°	135°	150°	180°	225°	240°
\sin	0	$1/2$	$1/\sqrt{2}$	$\sqrt{3}/2$	1	$\sqrt{3}/2$	$1/2$	$1/\sqrt{2}$	0	-1	0
\cos	1	$\sqrt{3}/2$	$1/\sqrt{2}$	$1/2$	0	$-1/2$	$-1/\sqrt{2}$	$-\sqrt{3}/2$	-1	0	1
\tan	0	$1/\sqrt{3}$	1	$\sqrt{3}$	∞	$-\sqrt{3}$	-1	$-1/\sqrt{3}$	0	$-\infty$	0

$$1) \int x^n dx = \frac{x^{n+1}}{n+1} + C$$

$$2) \int \frac{1}{x^n} dx = \frac{-1}{(n-1)x^{n-1}} + C$$

$$3) \int \frac{1}{x} dx = \log|x| + C$$

$$4) \int e^x dx = e^x + C$$

$$5) \int a^x dx = \frac{a^x}{\log a} + C$$

$$6) \int \sin x dx = -\cos x + C$$

$$7) \int \cos x dx = \sin x + C$$

$$8) \int \tan x dx = \log|\sec x| + C$$

$$9) \int \cot x dx = \log|\sin x| + C$$

$$10) \int \sec x dx = \log|\sec x + \tan x| + C$$

$$11) \int \csc x dx = \log|\csc x - \cot x| + C$$

$$12) \int \sec^2 x dx = \tan x + C$$

$$13) \int \csc^2 x dx = -\cot x + C$$

$$14) \int \sec x \tan x dx = \sec x + C$$

$$15) \int \csc x \cot x dx = -\csc x + C$$

$$16) \int (f(x) \pm g(x)) dx = \int f(x) dx \pm \int g(x) dx$$

$$17) \int k f(x) dx = k \int f(x) dx$$

$$18) \int k dx = kx + C$$

$$19) \frac{1}{\text{co-efficient of } x}$$

$$20) \int \frac{f'(x)}{f(x)} dx = \log|f(x)| + C$$

$$21) \int \frac{f'(x)}{\sqrt{f(x)}} dx = 2\sqrt{f(x)} + C$$

$$22) \int [f(x)]^n f'(x) dx = \frac{[f(x)]^{n+1}}{n+1} + C$$

$$23) \sin^2 x = \frac{1 - \cos 2x}{2}$$

$$24) \cos^2 x = \frac{1 + \cos 2x}{2}$$

$$25) \int \frac{1}{a^2 - x^2} dx = \frac{1}{2a} \log \left| \frac{a+x}{a-x} \right| + C$$

$$26) \int \frac{1}{x^2 - a^2} dx = \frac{1}{2a} \log \left| \frac{x-a}{x+a} \right| + C$$

$$27) \int \frac{1}{a^2 + x^2} dx = \frac{1}{a} \tan^{-1} \left(\frac{x}{a} \right) + C$$

$$28) a^2 + x^2 \rightarrow x = a \tan \theta$$

$$29) \int \frac{1}{\sqrt{a^2 - x^2}} dx = \sin^{-1} \left(\frac{x}{a} \right) + C$$

$$30) a^2 - x^2 \rightarrow x = a \sin \theta$$

$$31) x^2 - a^2 \rightarrow x = a \sec \theta$$

$$32) \int \frac{1}{\sqrt{a^2 + x^2}} dx = \log|x + \sqrt{a^2 + x^2}| + C$$

$$33) \int \frac{1}{\sqrt{x^2 - a^2}} dx = \log|x + \sqrt{x^2 - a^2}| + C$$

$$34) \int \sqrt{a^2 - x^2} dx = \frac{x}{2} \sqrt{a^2 - x^2} + \frac{a^2}{2} \sin^{-1} \left(\frac{x}{a} \right) + C$$

$$35) \int \sqrt{x^2 + a^2} dx = \frac{x}{2} \sqrt{x^2 + a^2} + \frac{a^2}{2} \log|x + \sqrt{x^2 + a^2}| + C$$

$$36) \int \sqrt{x^2 - a^2} dx = \frac{x}{2} \sqrt{x^2 - a^2} - \frac{a^2}{2} \log|x + \sqrt{x^2 - a^2}| + C$$

$$37) \int I \Pi dx = I \int \Pi dx - \int (I' \Pi) dx$$

$$38) \int \frac{P(x)}{(x+a)(x+b)(x+c)} dx = \frac{A}{x+a} + \frac{B}{x+b} + \frac{C}{x+c}$$

$$39) \frac{\text{Dividend}}{\text{Divisor}} = Q + \frac{\text{remainder}}{\text{Divisor}}$$

$$40) \int e^x [f(x) + f'(x)] dx = e^x f(x) + C$$

$$41) \int f(x) dx = 0 \quad 42) \int_a^b f(x) dx = \int_a^b f(t) dt$$

$$43) \int_a^b f(x) dx = - \int_b^a f(x) dx \quad 44) \int_a^b f(x) dx = \int_a^c f(x) dx + \int_c^b f(x) dx$$

$$45) \int_a^b f(x) dx = \int_a^b f(a+b-x) dx \quad 46) \int_a^b f(x) dx = \int_a^b f(a-x) dx$$

$$47) \int_0^{2a} f(x) dx = \begin{cases} 2 \int_0^a f(x) dx, & f(2a-x) = f(x) \\ 0, & f(2a-x) = -f(x) \end{cases}$$

$$48) \int_{-a}^a f(x) dx = \begin{cases} 2 \int_0^a f(x) dx, & \text{when } f(x) \text{ is even } f(-x) = f(x) \\ 0, & \text{when } f(x) \text{ is odd } f(-x) = -f(x) \end{cases}$$

$$\rightarrow \sin \theta = \frac{\text{opp}}{\text{hyp}} \quad \cos \theta = \frac{\text{adj}}{\text{hyp}} \quad \tan \theta = \frac{\text{opp}}{\text{adj}}$$

$$\csc \theta = \frac{\text{hyp}}{\text{opp}} \quad \sec \theta = \frac{\text{hyp}}{\text{adj}} \quad \cot \theta = \frac{\text{adj}}{\text{opp}}$$

$$\rightarrow \sin \theta \times \csc \theta = 1$$

$$\sin \theta = \frac{1}{\csc \theta} \quad \csc \theta = \frac{1}{\sin \theta}$$

$$\cos \theta \times \sec \theta = 1$$

$$\cos \theta = \frac{1}{\sec \theta} \quad \sec \theta = \frac{1}{\cos \theta}$$

$$\tan \theta \times \cot \theta = 1$$

$$\tan \theta = \frac{1}{\cot \theta} \quad \cot \theta = \frac{1}{\tan \theta}$$

$$\rightarrow \sin^2 \theta + \cos^2 \theta = 1$$

$$\sec^2 \theta - \tan^2 \theta = 1$$

$$\sin^2 \theta = 1 - \cos^2 \theta$$

$$\sec^2 \theta = 1 + \tan^2 \theta$$

$$\sin \theta = \sqrt{1 - \cos^2 \theta}$$

$$\sec \theta = \sqrt{1 + \tan^2 \theta}$$

$$\cos^2 \theta = 1 - \sin^2 \theta$$

$$\tan^2 \theta = \sec^2 \theta - 1$$

$$\cos \theta = \sqrt{1 - \sin^2 \theta}$$

$$\tan \theta = \sqrt{\sec^2 \theta - 1}$$

$$\csc^2 \theta - \cot^2 \theta = 1$$

$$\csc^2 \theta = 1 + \cot^2 \theta$$

$$\csc \theta = \sqrt{1 + \cot^2 \theta}$$

$$\cot^2 \theta = \csc^2 \theta - 1$$

$$\cot \theta = \sqrt{\csc^2 \theta - 1}$$

$$\rightarrow \sin 2x = 2 \sin x \cdot \cos x = \frac{2 \tan x}{1 + \tan^2 x}$$

$$\cos 2x = \cos^2 x - \sin^2 x = 2 \cos^2 x - 1 = 1 - 2 \sin^2 x = \frac{1 - \tan^2 x}{1 + \tan^2 x}$$

$$\tan 2x = \frac{2 \tan x}{1 - \tan^2 x}$$

$$\sin 3x = 3 \sin x - 4 \sin^3 x$$

$$\cos 3x = 4 \cos^3 x - 3 \cos x$$

$$\tan 3x = \frac{3 \tan x - \tan^3 x}{1 - 3 \tan^2 x}$$

$$1 + \cos 2x = 2 \cos^2 x = \frac{1 + \cos 2x}{2}$$

$$1 - \cos 2x = 2 \sin^2 x = \frac{1 - \cos 2x}{2}$$

$$\rightarrow \sin x = 2 \sin \frac{x}{2} \cdot \cos \frac{x}{2} = \frac{2 \tan \frac{x}{2}}{1 + \tan^2 \frac{x}{2}}$$

$$\cos x = \cos^2 \frac{x}{2} - \sin^2 \frac{x}{2} = 2 \cos^2 \frac{x}{2} - 1 = 1 - 2 \sin^2 \frac{x}{2} = \frac{1 - \tan^2 \frac{x}{2}}{1 + \tan^2 \frac{x}{2}}$$

$$\tan x = \frac{2 \tan \frac{x}{2}}{1 - \tan^2 \frac{x}{2}}$$

$$1 + \cos x = 2 \cos^2 \frac{x}{2} \Rightarrow \cos^2 \frac{x}{2} = \frac{1 + \cos x}{2}$$

$$1 - \cos x = 2 \sin^2 \frac{x}{2} \Rightarrow \sin^2 \frac{x}{2} = \frac{1 - \cos x}{2}$$

$$\rightarrow \sin(x+y) = \sin x \cos y + \cos x \sin y$$

$$\sin(x-y) = \sin x \cos y - \cos x \sin y$$

$$\cos(x+y) = \cos x \cos y - \sin x \sin y$$

$$\cos(x-y) = \cos x \cos y + \sin x \sin y$$

$$\tan(x+y) = \frac{\tan x + \tan y}{1 - \tan x \tan y} \quad \tan(x-y) = \frac{\tan x - \tan y}{1 + \tan x \tan y}$$

$$\rightarrow \sin A \cdot \cos B = \frac{1}{2} [\sin(A+B) + \sin(A-B)]$$

$$\cos A \cdot \sin B = \frac{1}{2} [\sin(A+B) - \sin(A-B)]$$

$$\cos A \cdot \cos B = \frac{1}{2} [\cos(A+B) + \cos(A-B)]$$

$$\sin A \cdot \sin B = \frac{1}{2} [\cos(A-B) - \cos(A+B)]$$

$$\rightarrow \sin C + \sin D = 2 \sin \left[\frac{C+D}{2} \right] \cos \left[\frac{C-D}{2} \right]$$

$$\sin C - \sin D = 2 \cos \left[\frac{C+D}{2} \right] \sin \left[\frac{C-D}{2} \right]$$

$$\cos C + \cos D = 2 \cos \left[\frac{C+D}{2} \right] \cos \left[\frac{C-D}{2} \right]$$

$$\cos C - \cos D = -2 \sin \left[\frac{C+D}{2} \right] \sin \left[\frac{C-D}{2} \right]$$

$$\rightarrow \frac{\sin \theta}{\cos \theta} = \tan \theta \quad \frac{\cos \theta}{\sin \theta} = \cot \theta$$

$$\rightarrow \frac{d}{dx} \sin^{-1} x = \frac{1}{\sqrt{1-x^2}} \quad \frac{d}{dx} \cos^{-1} x = \frac{-1}{\sqrt{1-x^2}}$$

$$\frac{d}{dx} \tan^{-1} x = \frac{1}{1+x^2} \quad \frac{d}{dx} \cot^{-1} x = \frac{-1}{1+x^2}$$

$$\frac{d}{dx} \sec^{-1} x = \frac{1}{x\sqrt{x^2-1}} \quad \frac{d}{dx} \csc^{-1} x = \frac{-1}{x\sqrt{x^2-1}}$$

$$\begin{aligned} \rightarrow \int x^n dx &= \frac{x^{n+1}}{n+1} + c & \rightarrow \sin 2x &= 2 \sin x \cos x = \frac{2 \tan x}{1 + \tan^2 x} \\ \rightarrow \int \frac{1}{x^n} dx &= \frac{-1}{(n-1)x^{n-1}} + c & \rightarrow \cos 2x &= \cos^2 x - \sin^2 x = 2 \cos^2 x - 1 = 1 - 2 \sin^2 x = \frac{1 - \tan^2 x}{1 + \tan^2 x} \\ \rightarrow \int \frac{1}{x} dx &= \log|x| + c & \rightarrow \tan 2x &= \frac{2 \tan x}{1 - \tan^2 x} \\ \rightarrow \int e^x dx &= e^x + c & \rightarrow \sin 3x &= 3 \sin x - 4 \sin^3 x \\ \rightarrow \int a^x dx &= \frac{a^x}{\log a} + c & \rightarrow \cos 3x &= 4 \cos^3 x - 3 \cos x \\ \rightarrow \int \sin x dx &= -\cos x + c & \rightarrow \tan 3x &= \frac{3 \tan x - \tan^3 x}{1 - 3 \tan^2 x} \\ \rightarrow \int \cos x dx &= \sin x + c & \rightarrow 1 + \cos 2x &= 2 \cos^2 x = \frac{1 + \cos 2x}{2} \rightarrow 1 - \cos 2x = 2 \sin^2 x = \frac{1 - \cos 2x}{2} \end{aligned}$$

$$\begin{aligned} \rightarrow \int \tan x dx &= \log|\sec x| + c \\ \rightarrow \int \cot x dx &= \log|\sin x| + c \\ \rightarrow \int \sec x dx &= \log|\sec x + \tan x| + c \\ \rightarrow \int \csc x dx &= \log|\csc x - \cot x| + c \end{aligned}$$

$$\begin{aligned} \rightarrow \int \sec^2 x dx &= \tan x + c \\ \rightarrow \int \csc^2 x dx &= -\cot x + c \\ \rightarrow \int \sec x \tan x dx &= \sec x + c \\ \rightarrow \int \csc x \cot x dx &= -\csc x + c \\ \rightarrow \int (f(x) \pm g(x)) dx &= \int f(x) dx \pm \int g(x) dx \\ \rightarrow \int k f(x) dx &= k \int f(x) dx \\ \rightarrow \int k dx &= kx + c \end{aligned}$$

$$\begin{aligned} \rightarrow \frac{d}{dx} x^n &= nx^{n-1} & \rightarrow \frac{d}{dx} \cos x &= -\sin x & \rightarrow \frac{d}{dx} a^x &= a^x \log a & \rightarrow \sin^2 \theta + \cos^2 \theta &= 1 \\ \rightarrow \frac{d}{dx} x &= 1 & \rightarrow \frac{d}{dx} \tan x &= \sec^2 x & \rightarrow \frac{d}{dx} \sqrt{x} &= \frac{1}{2\sqrt{x}} & \rightarrow \sec^2 \theta - \tan^2 \theta &= 1 \\ \rightarrow \frac{d}{dx} (\text{constant}) &= 0 & \rightarrow \frac{d}{dx} \cot x &= -\csc^2 x & \rightarrow \frac{d}{dx} UV &= UV' + VU' & \rightarrow \csc^2 \theta - \cot^2 \theta &= 1 \\ \rightarrow \frac{d}{dx} \frac{1}{x^n} &= \frac{-n}{x^{n+1}} & \rightarrow \frac{d}{dx} \sec x &= \sec x \tan x & \rightarrow \frac{d}{dx} \left(\frac{U}{V} \right) &= \frac{VU' - UV'}{V^2} \\ \rightarrow \frac{d}{dx} \frac{1}{x} &= \frac{-1}{x^2} & \rightarrow \frac{d}{dx} \csc x &= -\csc x \cot x & \rightarrow \sin \theta \times \csc \theta &= 1 \\ \rightarrow \frac{d}{dx} f(x) &= k \frac{d}{dx} f(x) & \rightarrow \frac{d}{dx} e^x &= e^x & \rightarrow \cos \theta \times \sec \theta &= 1 \\ \rightarrow \frac{d}{dx} \sin x &= \cos x & \rightarrow \frac{d}{dx} \log x &= \frac{1}{x} & \rightarrow \tan \theta \times \cot \theta &= 1 \end{aligned}$$