

$$C = E_1 \cap E_2$$

$$D = E_1 \cap E_2$$

$$P(X) = C + D$$

Properties  
Associate  
Distribution

### \* Random Variables \*

- Discrete Random Variable

- Continuous Random Variable

- Expectation of Random Variable

- Variance of a random Variable

- Jointly distributed Random Variables

- Combinations and Functions of

- Random variables.

For each point of a Sample Space, we assign a number and define a function on the Sample Space. This function is random variable.

A numerical value to each outcome of a particular experiment

Ex 1: Machine Breakdowns.

- Sample Space:  $S = \{\text{electrical, mechanical, misuse}\}$

- Each of these failures may be associated with a repair cost.

- State Space: {50, 200, 350}

- Cost is a random variable 50, 200 and 350

a pair of fair dice are tossed or let the random variable denote the sum of points

$$S = \{(1,1), (1,2), (2,3), (1,4), (1,5), (1,6)$$

$$(2,1), (2,2)$$

$$(3,1), (3,2), (3,3), (3,4), (3,5), (3,6)$$

$$(4,1), (4,2), (4,3), (4,4), (4,5), (4,6)$$

$$(5,1), (5,2), (5,3), (5,4), (5,5), (5,6)$$

$$(6,1), (6,2), (6,3), (6,4), (6,5), (6,6)\}$$

Possible Sums

$$X = \{2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12\}$$

$$\frac{1}{36}, \frac{2}{36}, \frac{3}{36}, \frac{4}{36}, \frac{5}{36}, \frac{6}{36}, \frac{7}{36}, \frac{8}{36}, \frac{9}{36}, \frac{10}{36}, \frac{11}{36}, \frac{12}{36}$$

A random variable which takes on finite number of values is a discrete random variable and one which takes on non countably infinite number of values is called as continuous random variable.

### \* Probability Mass Function

- A set of probability value

- $p_i$  assigned to each of the values taken by discrete random variable  $X$

- $0 \leq p_i$  and  $\sum_i p_i = 1$

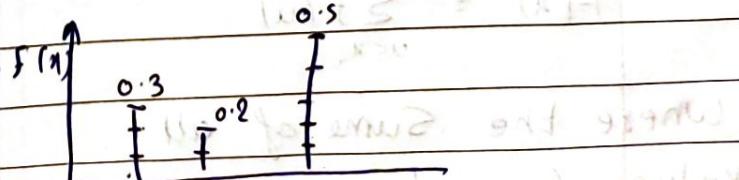
- Probability:  $P(X=x_i) = p_i$

$$P(\text{cost} = 50) = 0.3$$

$$P(\text{cost} = 200) = 0.2$$

$$P(\text{cost} = 350) = 0.5$$

$$0.3 + 0.2 + 0.5 = 1$$



Let  $X$  be a discrete random variable and suppose that possible values which it can assume are given by  $x_1, x_2, \dots, x_m$  arranged in increasing order of magnitude. Suppose some values are also associated with probabilities given by.

$$P(X = x_k) = f(x_k).$$

In general the probability function  $f(x) \geq 0$

- $\sum f(x) = 1$ .

(Probability Function).

### \* Cumulative Distribution Function

$$F(x) = P(X \leq x).$$

$$F(x) = \sum_{y \leq x} P(X = y).$$

CDF for a random variable  $X$

is defined as -

$$P(X \leq x) = F(x),$$

where  $x$  is any real number  $-\infty < x < \infty$

The distribution function can be obtained from distribution function by noting.

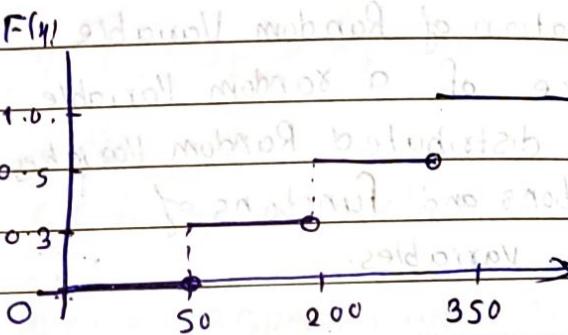
$$F(u) = \sum_{u \leq x} f(u)$$

Where the sum of all values of  $u$  for which  $u \leq x$  and the probability function can

be obtained from distribution function if only finite number of values  $x_1, x_2, \dots, x_m$

then the distribution function is given by

$$F(x) = \begin{cases} 0 & -\infty < x < x_1 \\ f(x_1) & x_1 \leq x < x_2 \\ f(x_1 + x_2) & x_2 \leq x < x_3 \\ f(x_1 + x_2 + \dots) & x_n \leq x < \infty \end{cases}$$



A pair of dice thrown  $X$  denotes Sum of no

Find CDF

Construct graph for the distribution

$$f(x) = \begin{cases} 0 & -\infty < x < 2 \\ 1/36 & 2 \leq x < 3 \\ 2/36 & 3 \leq x < 4 \\ 3/36 & 4 \leq x < 5 \\ 4/36 & 5 \leq x < 6 \\ 5/36 & 6 \leq x < 7 \\ 6/36 & 7 \leq x < 8 \\ 5/36 & 8 \leq x < 9 \\ 4/36 & 9 \leq x < 10 \\ 3/36 & 10 \leq x < 11 \\ 2/36 & 11 \leq x < 12 \\ 1/36 & 12 \leq x < \infty \end{cases}$$

We define the probability  
 $x$  lies between  $a$  &  $b$  as  
 $p(a < x < b) = \int_a^b f(x) dx.$

which satisfies this properties  
 is called probability function  
 or probability distribution for  
 CRV  $x$  or probal desity  
 function.

$$f(x) = \begin{cases} Cx^2 & 0 < x < 3 \\ 0 & \text{otherwise} \end{cases}$$

Compute  $P(1 < x < 2)$ .

$$\begin{aligned} P(1 < x < 2) &= \int_1^2 Cx^2 dx \\ &= \left[ \frac{Cx^3}{3} \right]_1^2 = \frac{7C}{3}. \end{aligned}$$

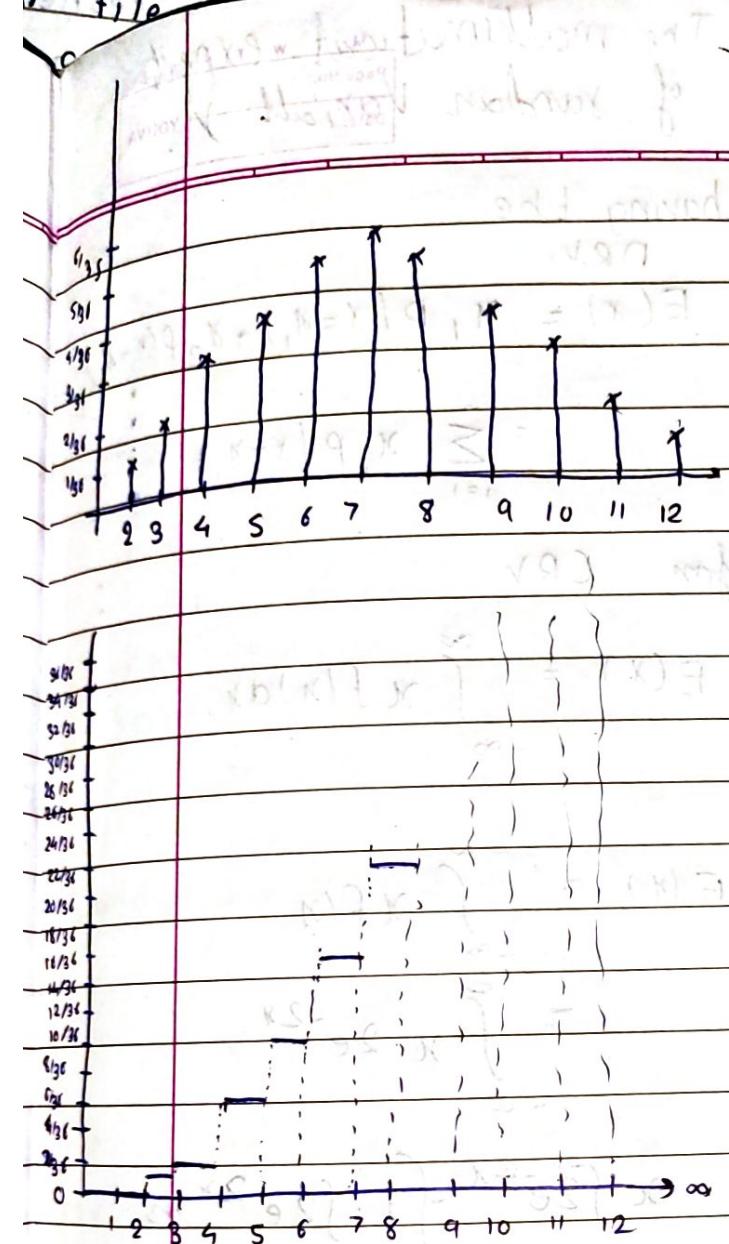
$$\int_{-\infty}^{\infty} f(x) dx = \int_{-\infty}^0 f(x) dx + \int_0^3 f(x) dx + \int_3^{\infty} f(x) dx$$

$$= \left[ \frac{Cx^3}{3} \right]_0^3 = 1$$

$$= C \times 27 = 1$$

$$C = \frac{1}{27}$$

$$P(1 < x < 2) = \frac{7}{27}$$



If  $x$  is a CRV

and prob  $x$  takes any  
 one particular value generally  
 0. So we cannot define a  
 probability function as the  
 same way as discrete  
 random variable.

Lies between two diff  
 Values A and B

The properties.

$$f(x) \geq 0$$

$$\int_{-\infty}^{\infty} f(x) dx = 1.$$

Suppose that the random variable  $X$  is the diameter

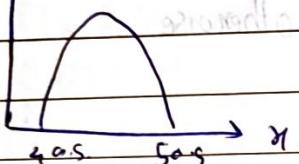
of a randomly chosen cylinder manufactured by the company.

$$f(x) = 1.5 - 6(x - 50.2)^2$$

for  $49.5 \leq x \leq 50.2$

$= 0$  otherwise.

$f(x)$ .



$$\int_{49.5}^{50.2} (1.5 - 6(x - 50.2)^2) dx$$

$$= [1.5x - 2(x - 50.2)^3] \Big|_{49.5}^{50.2}$$

$$= 1.0$$

$\Rightarrow$  It is valid PDF.

\* CDF for CRV.

$$F(x) = P(X \leq x) = \int_{-\infty}^x f(y) dy$$

\* A CRV.  $X$  has probability density function  $f(x)$  given by

$$f(x) = \begin{cases} 2e^{-2x} & x > 0 \\ 0 & x \leq 0. \end{cases}$$

find  $E(X)$ ,  $E(X^2)$

The mathematical expectation  
of random Variable

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having the DR.V.

$$E(X) = x_1 P(X=x_1) + x_2 P(X=x_2)$$

$$= \sum_{i=1}^n x_i P(X=x_i)$$

for CRV.

$$E(X) = \int_{-\infty}^{\infty} x f(x) dx.$$

$$E(X) = \int_{-\infty}^{\infty} x f(x) dx$$

$$= \int_{-\infty}^{\infty} x \cdot 2e^{-2x} dx$$

$$= x \cdot \int 2e^{-2x} dx - \int 1 \cdot \int 2e^{-2x} dx dx$$

$$= \frac{x \cdot 2e^{-2x}}{-2} - \int 1 \cdot \frac{2e^{-2x}}{-2} dx$$

$$= \left[ -xe^{-2x} + \frac{e^{-2x}}{-2} \right]_0^\infty$$

When the probabilities are equal

$$E(X) = \frac{x_1 + x_2 + \dots + x_n}{n}$$

$$E(CX) = C \cdot E(X)$$

$$E(X+Y) = E(X) + E(Y)$$

$$E(XY) = E(X) E(Y)$$

$$\text{Var}(X) = E[(X-\mu)^2]$$

$$\sigma^2 = E[(X-\mu)^2]$$

KAIST  
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for DRV:

$$\sigma^2 = \int_{-\infty}^{\infty} (x-\mu)^2 f(x) dx$$

$$\sigma^2 = E[X - \bar{x}]^2$$

for CRV

$$\sigma^2 = \int_{-\infty}^{\infty} (x-\mu)^2 f(x) dx$$

$$\text{Var}(cx) = c^2 \text{Var}(x)$$

$$\text{Var}(x+y) = \text{Var}(x) + \text{Var}(y)$$

Standardize a Random Variable

$$x^* = \frac{x-\mu}{\sigma}$$

The expected diameter of a metal cylinder

$$E(X) = \int_{-50}^{50} x (1.5 - 6(x-50)^2) dx$$

$$\text{let } y = x - 50$$

$$E(X) = \int_{-50}^{50} (y+50) (1.5 - 6y^2) dy$$

$$= \int_{-50}^{50} (-5y^3 - 300y^2 + 15y + 75) dy$$

$$= -3y^4/4 - 100y^3 + 15y^2 +$$

$$- 50$$

$$\begin{cases} 50 \\ 0 \\ 50 \end{cases}$$

$$E(X) = \int_{-\infty}^{\infty} xf(x) dx$$

$$= \int_{-\infty}^{\infty} x f(x) dx + \int_{-\infty}^{\infty} xf(x) dx$$

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$$\int_{-\infty}^{\infty} x^2 2e^{-2x}$$

$$= x^2 \int_{-\infty}^{\infty} 2e^{-2x} dx - \int_{-\infty}^{\infty} 2x \int_{-\infty}^{\infty} 2e^{-2x} dx$$

$$= x^2 \left[ \frac{2e^{-2x}}{-2} \right] - \left( 2x \left[ \frac{2e^{-2x}}{-2} \right] \right)$$

$$= -x^2 [e^{-2x}] - \int x 2e^{-2x} dx$$

$$= \left[ -x^2 [e^{-2x}] \right]_0^\infty + \frac{1}{2}$$

$$= \frac{1}{2}$$

A Pair of fair dice find Variance & Std deviation of sum.

$$f(x) = \begin{cases} x=2 & 1/36 \\ x=3 & 2/36 \\ x=4 & 3/36 \\ x=5 & 4/36 \\ x=6 & 5/36 \\ x=7 & 6/36 \\ x=8 & 5/36 \\ x=9 & 4/36 \\ x=10 & 3/36 \\ x=11 & 2/36 \\ x=12 & 1/36 \end{cases}$$

$$2 \times \frac{1}{36} + 3 \times \frac{1}{36} + 4 \times \frac{1}{36} + 5 \times \frac{1}{36} + \dots$$

$$2 + 6 + 12 + 20 + 30 + 42 + 40 + 30 + \dots + 12 + 36/36 =$$

$$\frac{252}{36} = \frac{126}{18} = \frac{63}{9} = \frac{21}{3}$$

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$$= 1 - \left[ \frac{1}{2} \right]$$

$$= \frac{1}{2}$$

If  $X = CRV$

Pdf.

$$f(x) = \begin{cases} 2(2x-x^2) & 0 < x < 2 \\ 0 & \text{otherwise.} \end{cases}$$

find  $\alpha$

$$\text{P}(\alpha > 1)$$

$$\int_{-\infty}^{\infty} f(x) dx = \int_{-\infty}^0 f(x) + \int_0^2 f(x) + \int_2^{\infty} f(x) dx$$

$$= \int_0^2 \alpha(2x-x^2) dx = 1$$

$$= \int_0^2 2\alpha x - \alpha x^2 dx$$

$$= \left[ \frac{2\alpha x^2}{2} - \frac{\alpha x^3}{3} \right]_0^2 = 1.$$

$$= 4\alpha - 8\alpha = 1.$$

$$= 12\alpha - 8\alpha = 3$$

$$= 4\alpha = 3$$

$$\boxed{\alpha = \frac{3}{4}}$$

$$\text{P}(\alpha > 1) = \int_{-\infty}^{\infty} f(x) dx,$$

$$= \int_1^2 f(x) dx + \int_2^{\infty} f(x) dx.$$

$$= \left[ \frac{3}{4}x^2 - \frac{x^3}{3} \right]_1^2$$

Q If  $X = CRV$ .

Pdf

$$f(x) = \begin{cases} kx^2 & -3 < x < 3 \\ 0 & \text{otherwise.} \end{cases}$$

Find  $k$

$$\text{P}(1 \leq x \leq 2)$$

$$\text{P}(x > 1)$$

$$\text{P}(x \leq 2)$$

$$\int_{-3}^3 kx^2 dx = 1$$

$$\left[ \frac{kx^3}{3} \right]_{-3}^3 = 1.$$

$$9k - [-9k] = 1.$$

$$18k = 1$$

$$\boxed{k = 1/18}$$

$\text{P}(1 \leq x \leq 2)$

$$= \int_1^2 \frac{1}{18} x^2 dx = \left[ \frac{x^3}{3 \times 18} \right]_1^2$$

Joint Distribution

If  $X$  and  $Y$  are two discrete random variable we define the joint probability distribution of  $X$  &  $Y$  by.

$$P(X=x, Y=y) = f(x, y)$$

where  $f(x, y) \geq 0$

$$\text{2. } \sum_{x,y} f(x, y) = 1.$$

$X = x_j$  is obtained by adding all entries in the rows corresponding to  $X_j$  is given by.

$$P(X=x_j) = f(x_j) = \sum_{k=1}^n f(x_j, y_k)$$

$y$	$y_1, y_2, \dots, y_n$
$x_1$	$f(x_1, y_1), f(x_1, y_2), \dots, f(x_1, y_n)$
$x_2$	$f(x_2, y_1), f(x_2, y_2), \dots, f(x_2, y_n)$
$x_3$	$f(x_3, y_1), f(x_3, y_2), \dots, f(x_3, y_n)$
$x_4$	$f(x_4, y_1), f(x_4, y_2), \dots, f(x_4, y_n)$
$\vdots$	$\vdots$
$x_n$	$f(x_n, y_1), f(x_n, y_2), \dots, f(x_n, y_n)$

$$F(x, y) = P(X \leq x, Y \leq y)$$

$$= \sum_{u \leq x} \sum_{v \leq y} f(u, v)$$

$$\Rightarrow f(x, y) \geq 0$$

$$\int_{-\infty}^{\infty} \int_{-\infty}^{\infty} f(x, y) dx dy$$

Graphically  $f(x, y)$  represents a surface called probability surface and volume bounded by this surface on  $X-Y$  is equal to 1.

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And the probability that  $X$  lies  $a < x < b$  &  $c < y < d$ .

$$P(a < X < b, c < Y < d) = \int_a^b \int_c^d f(x, y) dx dy.$$

\* Suppose  $X$  and  $Y$  discrete R.V. and the events  $X=x, Y=y$  are independent events for all  $X \in \mathcal{X}$  the we say that R.V are independent random variables.

$$P(X=x, Y=y) = P(X=x) P(Y=y)$$

if for all  $x$  and  $y$ , the joint probability function  $F(x, y)$  can be expressed as product of function of  $x$  alone and function of  $y$  alone.

$X$  and  $Y$  are independent however if  $F(x, y)$  cannot be represented then Capital  $X$  and  $Y$  are dependent.

If  $X$  &  $Y$  are CRV

we say that they are independent random variables

then we say that  $X$  &  $Y$  are independent events

$$P(X \leq x, Y \leq y) = P(X \leq x)$$

$$(d > r > p) \rightarrow P(Y \leq y) F_2$$

$$\xrightarrow{x} \quad \xrightarrow{y}$$

\* Change of Random Variable.

Given the probability distribution

of one or more R.V.s if we are interested in finding

distribution of other R.V.s

which depend on them

In some specified manner.

The procedures for obtaining this distributions are.

### 1. Discrete R.V.

Let  $X$  be the D.R.V.

whose probability function is  $f(x)$ .

Suppose that D.R.V.  $U$  is defined in terms of  $x$ .

$$U = \phi(X),$$

where each value of  $X$

corresponds to one

and only one variable

of  $U$ , and conversely

so that

$$X = \psi(U)$$

Then the probability function.

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$$g(u) = f[\psi(u)]$$

Let  $X$  and  $Y$  be the DRV having joint prob function

Suppose that two D.R.V.  $U$  &  $V$ .

$$U = \phi(X, Y)$$

$$V = \psi(X, Y)$$

$$g(u) = f[\psi(u)]$$

$$X = \psi_1(U, V)$$

$$Y = \psi_2(U, V).$$

Then the joint prob func of  $U$  &  $V$  is given as

$$g(u, v) = f[\psi_1(u, v), \psi_2(v)]$$

### 2. Continuous R.V.

Let  $X$  be a CRV.

with Prob den fun

let  $u = \phi(x)$  where

$$x = \psi(u)$$

then the pdf of  $U$  is given by

$$g(u) |du| = f(x) |dx|$$

or

$$g(u) = f(x) / \left| \frac{dx}{du} \right| = f[\psi(u)] [\psi'(u)]$$

The density fun of sum  
of two CRV  $X$  &  $Y$

$$P(Y=y | X=x) = \frac{f(x,y)}{f_1(x)}$$

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$U = X+Y$  having the joint  
density function

$f(x,y)$  given by

$$g(u) = \int_{-\infty}^{\infty} f(x, u-x) dx$$

When  $X$  &  $Y$  are independent  
random variables

$$f(x,y) = f_1(x) f_2(y).$$

$$g(u) = \int_{-\infty}^{\infty} f_1(x) f_2(u-x) dx.$$

which is called as  
convolution of  $f_1$  and  $f_2$   
written as  $f_1 * f_2$ .

Rules :

$$f_1 * f_2 = f_2 * f_1$$

$$f_1(f_2 * f_3) = (f_1 * f_2) * f_3$$

Commutative

Distr., bin.

Associativity

where  $f(x,y)$  is joint prob. fun.

$f_1(x)$  = marginal prob func. of  $X$ .

$f(Y|X)$  is the conditional  
probability function.

$$\text{Similarly } f(X|Y) = \frac{f(X,Y)}{f_2(Y)}$$

\* For CRV.

$$f_1 * f_2 = \frac{f_1(x)}{f_2(y)}$$

$x - x - x - x - x -$

\* Binomial & Poisson Distribution

pmf of a binomial random  
variable  $X$  depends on two  
parameters  $n$  and  $p$ , we  
denote the pmf by  
 $b(x; n, p)$ .

$$b(x; n, p) = \binom{n}{x} p^x (1-p)^{n-x}, x=0, 1, n.$$

$$\sigma_x = \sqrt{npq}$$

$$np(1-p)$$

$$E(X) = np$$

If  $Y$  is purchase is made by  
credit card and  $X$  is the  
no amount taken randomly  
Selected purchase.

\* Conditional Distribution.  
If  $X$  &  $Y$  are D.R.V. and  
we are having events  $A$   
and  $B$  as

$$A : (X=x)$$

$$B : (Y=y)$$

then the eq.  $P(B|A)$

$$= P(A \cap B)$$

$$P(A)$$

The binomial R.V with parameter P and N with the prob mass function

$$f(x) = \binom{n}{x} p^x q^{n-x}$$

to find the prob mass funct

we have to find the prob of x success

in n independent trials.

On 5 question MCQ test

there are 5 possible ans of

which 1 is correct. If a

student guesses randomly

& independently what is

the probability that she

's correct only on

two questions

$$f(2) = \binom{5}{2} \left(\frac{1}{5}\right)^2 \left(\frac{4}{5}\right)^3$$

$$= \frac{5!}{3!2!} \times \frac{1}{25} \times \frac{4^3}{25 \times 5}$$

$$= \frac{5 \times 4 \times 3}{25^2 \times 5} = 0.1024$$

$$P(X) = \binom{4}{1} \left(\frac{1}{2}\right)^1$$

$$= \frac{4}{2^4}$$

$$= \frac{1}{2^4}$$

$$= \frac{1}{16}$$

$$\frac{1}{16}$$

$$P(Y) = \left[ \binom{4}{1} \left(\frac{1}{2}\right) + \binom{4}{2} \left(\frac{1}{2}\right)^2 + \binom{4}{3} \left(\frac{1}{2}\right)^3 + \binom{4}{4} \left(\frac{1}{2}\right)^4 \right]$$

$$= \frac{4}{1} \times \frac{4}{2} \times \frac{4}{3}$$

$$= \frac{1}{1} \times \frac{2}{2} \times \frac{3}{3} \times \frac{2}{2} \times \frac{1}{1}$$

$$= \frac{4 \times 3 \times 2}{2^4}$$

$$= \boxed{\frac{7}{8}}$$

Out of 2000 families

with 4 children

how many would you expect

1) 2 boy

3) 1 or 2 girls

Q Find the prob that in a family of 4 children there will be atleast 1 boy

2) Atleast 1 boy & 1 girl

X = At least 1 boy

Y = At least 1 boy & At least 1 girl.

Q Tell if this binomial  
Shuffle a deck of cards

given that 2% of the fuses  
the manufacturer by firm

are defect ~ find Probability

1) box containing 200 fuses  
had atleast 1 defect

2) No defective fuse.

$$P(X=x) = \frac{e^{-\lambda} \lambda^x}{x!}$$

200  
1 defective.  
1000  
20 defective  
200

Poisson

$$\lambda = np$$

$$= 200 \times 0.002$$

$$\lambda = 4 \leftarrow$$

$$P(X=0) = \frac{e^{-\lambda} \lambda^0}{0!}$$

$$= e^{-4}$$

$$0.018$$

$$0.9816$$

In a certain factory there  
are manufacturing blades  
there is a small chance  
of be 0.002 the blade to  
be defect. The blades  
are supplied in packets of  
10 using poisson distribution  
as well as binomial dist  
find the approximate no of  
packets containing no  
1) defective blade.  
2) One defect in  
In a Consignment of  
10,000 packets

No of blades in Consignment  
=  $10,000 \times 10$

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$$= 10,000$$

$$= np$$

$$= 1,00,000 \times 0.002$$

If a bank receives on  
the average 6 bad cheques  
per day. Find the probability  
that it will receive 4 bad  
cheques on any day

A Web Server receives on average  
of 1,000 queries per day  
How much excess capacity  
should it build into be  
95% Sure that it can  
meet the demand.

The mean weight of 500  
male students at a certain  
college is 75

Assuming that the weights  
are normally distributed  
find the between 60 and  
78 kg (How many students)

and more than 92 kg.

$$\rightarrow \mu = 75$$

$$n = 500$$

$$\sigma = 7$$

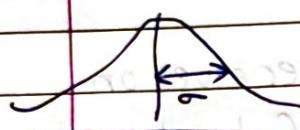
$$= \frac{1}{\sqrt{2\pi}} e^{-\frac{(x-\mu)^2}{2\sigma^2}}$$

Normal pdfs have two parameters  $\mu$  &  $\sigma$ .

$\mu$  Controls location



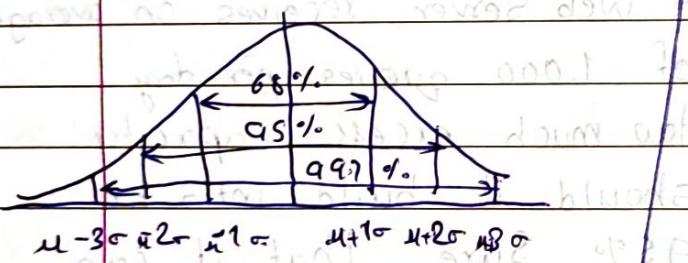
$\sigma$  Controls spread



68% of AUC with  $\pm 1\sigma$

95%  $\pm 2\sigma$

99.7%  $\pm 3\sigma$



Wechsler adult intelligence

Scores: Normally

$$\mu = 100, \sigma = 15$$

$$X \sim N(100, 15)$$

$$\mu \pm \sigma$$

$$= 100 \pm 15$$

$$= 80 \text{ to } 115$$

68% of Score,

As curve is Symmetrical

total AUC is exactly 1.

$$Z = \frac{X - \mu}{\sigma}$$

Z Score

Q What percentage of gestation  
are less than 40 weeks?

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Q 500 boys preques  
conting

→ below 60 & 78.

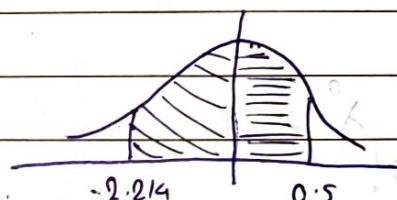
$$Z = \frac{X - \mu}{\sigma}$$

Calculate  $Z_1, Z_2$

$$\frac{59.5 - 75}{7}$$

$$\frac{78.5 - 75}{7}$$

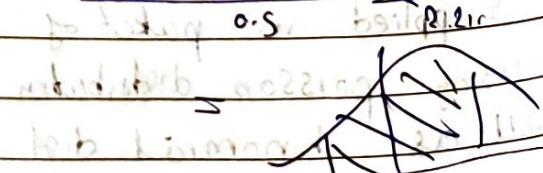
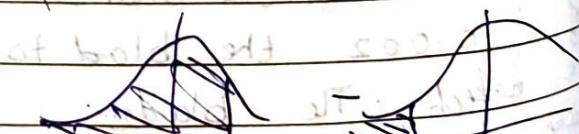
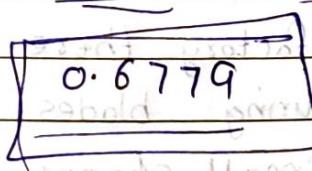
$$Z_1 = -2.214, Z_2 = 0.5$$



find Area under Curve.

$$0.0136$$

$$0.6915$$

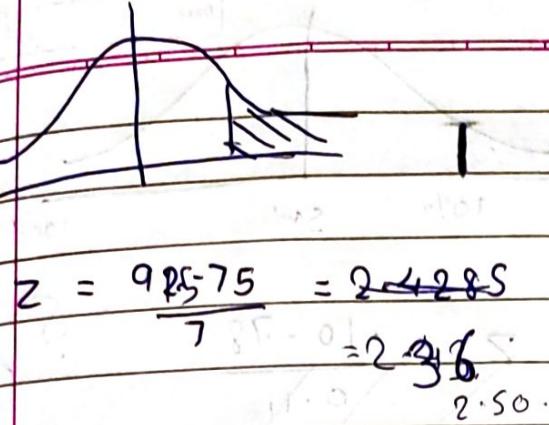


$$0.6779 \times 500$$

$$= 339 \text{ Students}$$

$\geq 92$

above 92



$$Z = \frac{92.5 - 75}{7} = \frac{2.5 - 2.5}{7} = 2.5$$

$\Rightarrow 1 - \text{below } 92.$

$$= 1 - 0.9909$$

$$= 0.0091$$

$$\text{or } \frac{92.5 - 75}{7} = 2.5$$

$$1 - 0.9938$$

$$= 100 \cdot 0.0062 \times 500$$

$$= 3$$

Find the prob of getting 3 & 6 heads in 10 tosses of fair coin by using binomial distribution and the normal approximation to the binomial distribution

$$\lambda = np$$

$$= 10$$

$$20.0$$

$$20.0$$

In a simultaneous inspection of 10 units. The prob of getting

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defective unit & not defective are equal. Find prob of getting atleast 7 non defective units and atleast 8 non defective units.

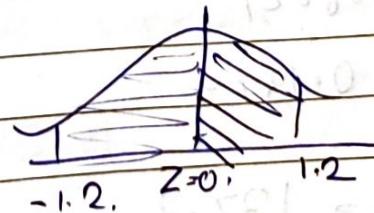
The mean inside diameter of a sample of 200 washers produced by a machine is 0.502 inches.

$$S.D = 0.005$$

0.496 to 0.508 inches. Consider defect as determine the %age of defective washers produced assuming the diameters are normally distributed.

$$Z_1 = \frac{0.496 - 0.502}{0.005} = -1.2$$

$$Z_2 = \frac{0.508 - 0.502}{0.005} = 1.2$$



$$0.8849$$

$$- 0.5000$$

$$0.3849$$

$$0.3449 \times 2$$

$$= 0.7678$$

$$= 77\%$$

The marks of by 1000 students are normally distributed with mean 78 % and S.D. 11 %

Determine How many Students got marks

above 90 %

What are the highest Score by the lowest 10% of the Students.

Find the limits of 90% marks.

$$\mu = 0.78$$

$$\sigma = 0.11$$

$$N = 1000$$

$$P(X > 90) = \frac{0.90 - 0.78}{0.11}$$

$$= \frac{0.12}{0.11} = 1.09$$

$$= 0.8621$$

$$1 - 0.8621$$

$$= 0.1379$$

$$\text{No of Students} = 137.9$$

$$\approx 138$$

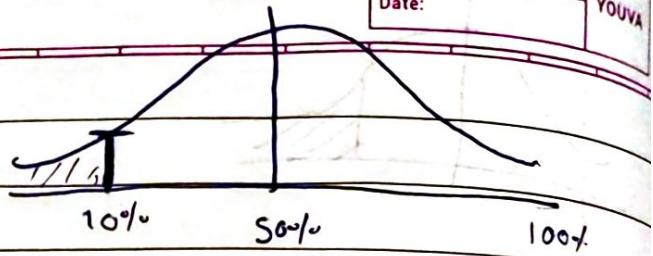
$$= 0.0920$$

Q. Highest of lowest 10%.

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YOUVA



$$Z_1 = \frac{10 - 78}{0.11} = -6.18$$

$$P(X < X_1) = 10\% = 0.1$$

$$P(Z < Z_1) = 0.1$$

$$A(Z_1) + A(Z < Z_1) = 0.5$$

$$= 0.5 - 0.1$$

$$= 0.4$$

$$-1.28 = x - 0.78$$

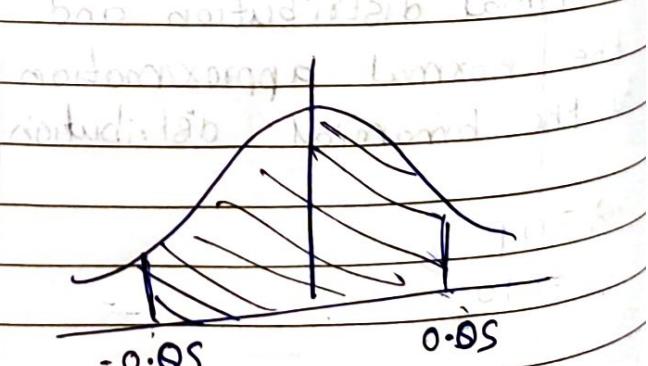
$$x = 0.50 - 0.11 = 0.39$$

$$x = 0.11x - 1.28 + 0.78$$

$$= x = 0.63 \times 100$$

$$= 63.92$$

$$= 64\%$$



$$-2 \times 0.5 =$$

$$0.05 - 0.78$$

In a normal distribution  
7% of the items < 3s

89% of items are under 6s  
determine mean and  
variance of the  
distribution

Prob  
bayer  
Ind even  
Random Var.

Descri  
Con

Joint

Change of  
Pd ravn

Condif dist

Binom

Norm

Poisn

Relationship  
betw Norm

Norm & Poisson.

0.9382.

Poisson distribution is given  
as  $X \sim P(\lambda)$

$$P(Y=x) = \frac{\lambda^x e^{-\lambda}}{x!}, x=0,1,2,\dots$$

A Poisson dist arises when  
the events being counted  
are independently such that  
the probability that two or  
more events occur simultaneously

Given length of material  
accidents on a particular  
part of road in a given  
time or telephone calls  
made to a call centre  
in one day.  
and the key parameter in  
fitting the  
is the mean value.

2% of the fuses,.....  
200 fuses has atleast 1 defect.

$$\begin{aligned}\lambda &= np \\ &= 200 \times 0.002 \\ &= 4\end{aligned}$$

20% of items from a factory are  
defective find the prob that in a  
sample of 5 chosen at random  
none defective item is chosen.

1. One is defective
3.  $P(1 < X < 4)$

$$P(X=0)$$

pls by  
Murray Spiegel  
Schaum Series.

1,2,4