

# Meet in the Middle

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You are given an array of  $n$  numbers. In how many ways can you choose a subset of the numbers with sum  $x$ ?

$$1 \leq n \leq 40$$

Divide into two part then brute force and then use set to find if sum exists or not

## String problem

You are given two string  $S$  and  $T$  of length  $N$ . Figure out if we can get string  $T$  starting from string  $S$  and applying 4 substring reverse algorithms

Apply two substring reverse on  $s$  and add to set and the apply two on  $t$  and add to set

```
for(int l1=0;l1<n;l1++){
    for(int r1=l1;r1<n;r1++){
        for(int l2=0;l2<n;l2++){
            for(int r2=l2;r2<n;r2++){
                string temp=s;
                reverse(temp.begin()+l1,temp.begin()+r1+1);
                reverse(temp.begin()+l2,temp.begin()+r2+1);
                add to set
            }
        }
    }
}
```

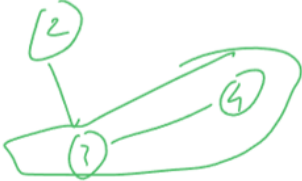
## Graph problem

Find minimum vertex cover when  $n \leq 30$  and  $m \leq 40$

```

// graph: 1 1 0 0 0 0
// vertexCover: 0 1 0 0 0 0
bool check(int graph, int vertexCover, int edges[][2], int M) {
    for (int i = 1; i <= M; i++) {
        int a = edges[i][0];
        int b = edges[i][1];
        if (((graph >> a) & 1) == 0 or ((graph >> b) & 1) == 0) {
            // this edge doesn't lie in graph
            continue;
        }
        if (((vertexCover >> a) & 1) == 0 && ((vertexCover >> b) & 1) == 0) {
            // no edge vertex lies in vertex cover
            return false;
        }
    }
    return true;
}

```



```

int solve(int edges[][2], int N, int M) {
    unacademy le9;
    int leftSize = N / 2;
    int rightSize = N - leftSize;

    vector<int> adj[N + 5];
    for (int i = 1; i <= M; i++) {
        adj[edges[i][0]].push_back(edges[i][1]);
        adj[edges[i][1]].push_back(edges[i][0]);
    }

    int dp[(1 << leftSize) + 5];

    for (int graph = 0; graph < (1 << leftSize); graph++) {
        int minVertexCover = inf;

        if (check(graph, 0, edges, M))
            minVertexCover = 0;

        for (int vertexCover = graph; vertexCover > 0;
             vertexCover = (vertexCover - 1) & graph) {
            if (check(graph, vertexCover, edges, M)) {
                minVertexCover = min(minVertexCover, countSetBits(vertexCover));
            }
        }
        dp[graph] = minVertexCover;
    }

    int res = inf;
    for (int vertexCover = 0; vertexCover < (1 << rightSize); vertexCover++) {
        int graph = (1 << rightSize) - 1;
        if (!check(graph << leftSize, vertexCover, edges, M))
            continue;

        int rightVertexCover = countSetBits(vertexCover);
        int remGraph = graph ^ vertexCover;

        int leftVerticesToTake = 0;

        for (int remVertex = 0; remVertex < rightSize; remVertex++) {
            if ((remGraph >> remVertex) & 1) {
                int actualVertex = remVertex + leftSize;
                for (int leftVertex : adj[actualVertex]) {
                    if (leftVertex < leftSize)
                        leftVerticesToTake |= (1 << leftVertex);
                }
            }
        }

        int leftVertexCover = countSetBits(leftVerticesToTake) +
                               dp[(1 << leftSize) - 1 ^ leftVerticesToTake];
        res = min(res, leftVertexCover + rightVertexCover);
    }
    return res;
}

```