

| | | | | | | |
|-----|-------|-------|-------|-------|-------|-------|
| x | 10 | 20 | 30 | 40 | 50 | 60 |
| y | 1.105 | 1.808 | 2.614 | 3.604 | 4.857 | 6.451 |

3. The following data gives the marks obtained by 100 students in a subject in an examination using both Newton's forward and backward interpolation formulas, find the number of students who have scored 45 marks and above.

| | | | | | |
|-----------------|-------|-------|-------|-------|-------|
| Marks obtained: | 30-40 | 40-50 | 50-60 | 60-70 | 70-80 |
| No of students: | 25 | 35 | 22 | 11 | 7 |

[Hint: Rewrite the data in terms of x and y , where x denotes the lower boundary of marks and y the numbers of students who have secured marks x and above.]

4. Use both Newton's forward and backward interpolation formulas to find $\tan 17^\circ$ from the following data:

| | | | | | | |
|----------------|---|--------|--------|--------|--------|--------|
| x° | 0 | 4 | 8 | 12 | 16 | 20 |
| $\tan x^\circ$ | 0 | 0.0699 | 0.1405 | 0.2126 | 0.2167 | 0.3640 |

5. Use both Newton's forward and backward interpolation formulas to find the value of y when $x = 23.6$ from the following data:

| | | | | | | | |
|-----|-------|--------|--------|--------|--------|--------|--------|
| x | 19 | 20 | 21 | 22 | 23 | 24 | 25 |
| y | 91.00 | 100.25 | 110.00 | 120.25 | 131.00 | 142.25 | 154.00 |

6. Use both Newton's forward and backward interpolation formulas to find the number of students who have secured 75 or less marks from the following data:

| | | | | | |
|-----------------|-------|-------|-------|-------|-------|
| Mark range | 30-40 | 40-50 | 50-60 | 60-70 | 70-80 |
| No. of students | 31 | 42 | 51 | 35 | 31 |

7. Find $y(5)$, using both Newton's and backward interpolation formulas, if $y(10) = 35.3$, $y(15) = 32.4$, $y(20) = 29.2$, $y(25) = 26.1$, $y(30) = 23.2$ and $y(35) = 20.5$.
8. Find y at $x = 0.95$, using both Newton's forward and backward interpolations formulas, from the given table.

| | | | | | | |
|-----|-------|-------|-------|-------|-------|-------|
| x | 1.0 | 1.1 | 1.2 | 1.3 | 1.4 | 1.5 |
| y | 0.841 | 0.891 | 0.932 | 0.964 | 0.925 | 1.015 |

9. Find the value of y at $x = 0.47$ using Newton's forward and backward interpolations formulas from the given table.

| | | | | | |
|-----|--------|--------|--------|--------|--------|
| x | 0.50 | 0.55 | 0.60 | 0.65 | 0.70 |
| y | 0.1915 | 0.2088 | 0.2258 | 0.2422 | 0.2580 |

10. Find the value of y at $x = 6$, using both Newton's forward and backward interpolation formulas from the following table.

| | | | | | |
|-----|-------|-------|-------|-------|-------|
| x | 1 | 2 | 3 | 4 | 5 |
| y | 41.66 | 34.46 | 28.28 | 22.94 | 18.32 |

11. Find $e^{0.655}$, using both Newton's forward and backward interpolation formulas from the following table.

| | | | | | |
|-------|----------|----------|----------|----------|----------|
| x | 0.61 | 0.62 | 0.63 | 0.64 | 0.65 |
| e^x | 1.840431 | 1.858928 | 1.877610 | 1.896481 | 1.915541 |

4. Using the inverse Lagrange's interpolation, find the value of x when $y = 3$ from the following table

| | | | | |
|-----|----|----|----|-----|
| x | 36 | 54 | 72 | 144 |
| y | -2 | 1 | 2 | 4 |

5. Using Lagrange's interpolation formula find $f(x)$

| | | | | |
|--------|---|---|----|----|
| x | 0 | 1 | 4 | 5 |
| $f(x)$ | 4 | 3 | 24 | 39 |

6. Using Lagrange's interpolation formula find polynomial

| | | | | |
|-----|-----|---|---|----|
| x | 0 | 1 | 3 | 4 |
| y | -12 | 0 | 6 | 12 |

7. Find the polynomial using Lagrange's Interpolation

| | | | | |
|-----|---|---|----|----|
| x | 0 | 1 | 2 | 5 |
| y | 2 | 3 | 12 | 15 |

8. Find the polynomial using Lagrange's Interpolation

| | | | | | |
|--------|---|----|----|-----|-----|
| x | 0 | 2 | 3 | 4 | 7 |
| $f(x)$ | 4 | 26 | 58 | 112 | 466 |

9. Using Lagrange's Inverse interpolation find x at $y = 100$ from the given data.

| | | | | | |
|-----|---|----|----|-----|-----|
| x | 3 | 5 | 7 | 9 | 11 |
| y | 6 | 24 | 58 | 108 | 174 |

10. Using Lagrange's Inverse interpolation find x at $y = 85$ from the given data.

| | | | | |
|-----|------|------|------|------|
| x | 2 | 5 | 8 | 14 |
| y | 94.8 | 87.9 | 81.3 | 68.7 |

11. Using Lagrange's Inverse interpolation find polynomial.

| | | | | |
|--------|-----|-----|----|----|
| x | 30 | 34 | 38 | 42 |
| $f(x)$ | -30 | -13 | 3 | 18 |

12. Find polynomial using Lagrange's Interpolation.

| | | | | |
|--------|-----|-----|---|----|
| x | -1 | 0 | 3 | 4 |
| $f(x)$ | -38 | -12 | 6 | 12 |

13. Find the polynomial using Lagrange's Interpolation

| | | | | |
|--------|---|----|----|-----|
| x | 0 | 1 | 4 | 5 |
| $f(x)$ | 8 | 11 | 68 | 123 |

- 14.

| | | | | |
|--------|------|------|------|------|
| x | 1.2 | 2.0 | 2.5 | 3.0 |
| $f(x)$ | 1.36 | 0.58 | 0.34 | 0.20 |

Find $f(x)$ at $x = 1.6$

- 15.

| | | | | |
|--------|----|----|----|----|
| x | 25 | 30 | 40 | 50 |
| $f(x)$ | 26 | 34 | 42 | 47 |

Find $f(x)$ at $x = 25$