

11.2) The sequence of moves required to move 8 disks from source to destination using the above algorithm is given below.

My code is based on recursion where we first take the no. of disks as input from user and then solved it using 2 temporary pegs.

In this we first send  $(n-2)$  disks to a temporary peg and using the other 2 pegs send the 2 disks left to the destination and again hit the function where it sends remaining  $(n-2)$  disks to the destination.

Base case is when we either reach zero or one disk.

In case input = 8.

It first executes function call of taking 6 disks from  $T_1$  to  $T_2$  which again hits function call taking 4 disks from  $T_1$  to  $T_4$  again function call of 2 disks from  $T_1$  to  $T_2$  which in next function call of zero disks hits base case & returns then gets completed in opposite order moving 2 disks from  $T_1$  to  $T_2$ , then 4 disks from  $T_1$  to  $T_4$  then 6 to  $T_2$  & 8 to  $T_4$  completing the tower of hanoi.

The third peg was used for solving the 2 disks left behind.

Output of the code:-

>> Enter the number of disks : 8

>> The sequence of steps are:-

1.  $T_1 \rightarrow T_3$
2.  $T_1 \rightarrow T_2$
3.  $T_3 \rightarrow T_2$
4.  $T_1 \rightarrow T_3$
5.  $T_1 \rightarrow T_4$
6.  $T_3 \rightarrow T_4$
7.  $T_2 \rightarrow T_1$
8.  $T_2 \rightarrow T_4$
9.  $T_1 \rightarrow T_4$
10.  $T_1 \rightarrow T_3$
11.  $T_1 \rightarrow T_2$

12. T3 -> T2
13. T4 -> T1
14. T4 -> T3
15. T1 -> T3
16. T4 -> T1
17. T4 -> T2
18. T1 -> T2
19. T3 -> T4
20. T3 -> T2
21. T4 -> T2
22. T1 -> T3
23. T1 -> T4
24. T3 -> T4
25. T2 -> T1
26. T2 -> T4
27. T1 -> T4
28. T2 -> T1
29. T2 -> T3
30. T1 -> T3
31. T4 -> T2
32. T4 -> T3
33. T2 -> T3
34. T2 -> T1
35. T2 -> T4
36. T1 -> T4
37. T3 -> T2
38. T3 -> T1
39. T2 -> T1
40. T3 -> T2
41. T3 -> T4
42. T2 -> T4
43. T1 -> T3
44. T1 -> T4
45. T3 -> T4

H-3) The outcome from the typical towers of hanoi is given below.  
 Calculating time complexity of my code:  

$$T(n) = 2T(n-2) + c$$

↳ At 2 times  
function call for (n-2).

↳ for const. post operations

My code:

$$\begin{aligned}
 T(n) &= 2T(n-2) + C \\
 &= 2(2T(n-4) + C) + C \\
 &= 4T(n-4) + 3C \\
 &= 4(2T(n-6) + C) + 3C \\
 &= 8T(n-6) + 7C \\
 &\vdots \\
 &\quad n-2K=1 \Rightarrow K=\frac{n-1}{2} \\
 &= 2^K T(n-2K) + (2^K - 1)C \\
 &= 2^{\frac{n-1}{2}} T(1) + (2^{\frac{n-1}{2}} - 1)C \\
 &= 2^{\frac{n-1}{2}} + (2^{\frac{n-1}{2}} - 1)C - C \\
 &= 2^{\frac{n-1}{2}} (1+C) - C \\
 &\quad \downarrow \\
 &\boxed{T(n) = O(2^{n/2})} \quad \downarrow \leq 2^{n/2}(1+C)
 \end{aligned}$$

Time complexity of my code is smaller than that of typical one so it is better in regards of time

Typical Tower of Hanoi:

$$\begin{aligned}
 T(n) &= 2T(n-1) + C \\
 T(n) &= 4T(n-2) + 3C \\
 T(n) &= 8T(n-3) + 7C \\
 &\vdots \\
 &\quad n-K=1 \Rightarrow K=n-1 \\
 T_n &= 2^K T(n-K) + (2^K - 1)C \\
 &= 2^{n-1} T(1) + (2^{n-1} - 1)C \\
 &= \frac{2^n (1+C) - C}{2} \\
 &\quad \downarrow \quad K=n-1 \\
 &\boxed{T_n = O(2^n)} \quad \downarrow \leq 2^n (1+C)
 \end{aligned}$$

Typical Tower of Hanoi output with A as source rod and C as destination rod:-

Number of disks : 8

1. A → B
2. A → C
3. B → C
4. A → B
5. C → A
6. C → B
7. A → B
8. A → C
9. B → C
10. B → A
11. C → A
12. B → C
13. A → B
14. A → C
15. B → C
16. A → B
17. C → A
18. C → B
19. A → B
20. C → A

21.  $B \rightarrow C$
22.  $B \rightarrow A$
23.  $C \rightarrow A$
24.  $C \rightarrow B$
25.  $A \rightarrow B$
26.  $A \rightarrow C$
27.  $B \rightarrow C$
28.  $A \rightarrow B$
29.  $C \rightarrow A$
30.  $C \rightarrow B$
31.  $A \rightarrow B$
32.  $A \rightarrow C$
33.  $B \rightarrow C$
34.  $B \rightarrow A$
35.  $C \rightarrow A$
36.  $B \rightarrow C$
37.  $A \rightarrow B$
38.  $A \rightarrow C$
39.  $B \rightarrow C$
40.  $B \rightarrow A$
41.  $C \rightarrow A$
42.  $C \rightarrow B$
43.  $A \rightarrow B$
44.  $C \rightarrow A$
45.  $B \rightarrow C$
46.  $B \rightarrow A$
47.  $C \rightarrow A$
48.  $B \rightarrow C$
49.  $A \rightarrow B$
50.  $A \rightarrow C$
51.  $B \rightarrow C$
52.  $A \rightarrow B$
53.  $C \rightarrow A$
54.  $C \rightarrow B$
55.  $A \rightarrow B$
56.  $A \rightarrow C$
57.  $B \rightarrow C$
58.  $B \rightarrow A$
59.  $C \rightarrow A$
60.  $B \rightarrow C$
61.  $A \rightarrow B$
62.  $A \rightarrow C$
63.  $B \rightarrow C$
64.  $A \rightarrow B$
65.  $C \rightarrow A$
66.  $C \rightarrow B$
67.  $A \rightarrow B$
68.  $C \rightarrow A$

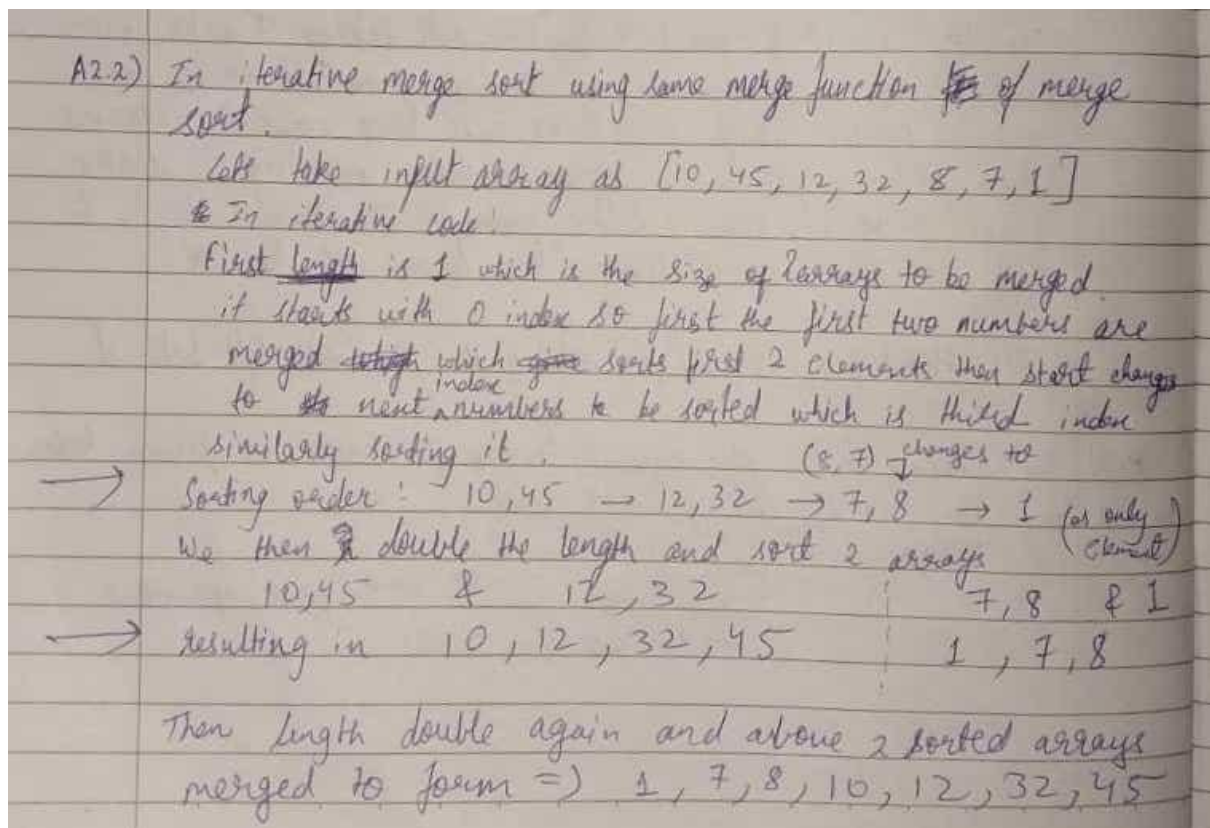
- 69.  $B \rightarrow C$
- 70.  $B \rightarrow A$
- 71.  $C \rightarrow A$
- 72.  $C \rightarrow B$
- 73.  $A \rightarrow B$
- 74.  $A \rightarrow C$
- 75.  $B \rightarrow C$
- 76.  $A \rightarrow B$
- 77.  $C \rightarrow A$
- 78.  $C \rightarrow B$
- 79.  $A \rightarrow B$
- 80.  $C \rightarrow A$
- 81.  $B \rightarrow C$
- 82.  $B \rightarrow A$
- 83.  $C \rightarrow A$
- 84.  $B \rightarrow C$
- 85.  $A \rightarrow B$
- 86.  $A \rightarrow C$
- 87.  $B \rightarrow C$
- 88.  $B \rightarrow A$
- 89.  $C \rightarrow A$
- 90.  $C \rightarrow B$
- 91.  $A \rightarrow B$
- 92.  $C \rightarrow A$
- 93.  $B \rightarrow C$
- 94.  $B \rightarrow A$
- 95.  $C \rightarrow A$
- 96.  $C \rightarrow B$
- 97.  $A \rightarrow B$
- 98.  $A \rightarrow C$
- 99.  $B \rightarrow C$
- 100.  $A \rightarrow B$
- 101.  $C \rightarrow A$
- 102.  $C \rightarrow B$
- 103.  $A \rightarrow B$
- 104.  $A \rightarrow C$
- 105.  $B \rightarrow C$
- 106.  $B \rightarrow A$
- 107.  $C \rightarrow A$
- 108.  $B \rightarrow C$
- 109.  $A \rightarrow B$
- 110.  $A \rightarrow C$
- 111.  $B \rightarrow C$
- 112.  $A \rightarrow B$
- 113.  $C \rightarrow A$
- 114.  $C \rightarrow B$
- 115.  $A \rightarrow B$
- 116.  $C \rightarrow A$

- 117.  $B \rightarrow C$
- 118.  $B \rightarrow A$
- 119.  $C \rightarrow A$
- 120.  $C \rightarrow B$
- 121.  $A \rightarrow B$
- 122.  $A \rightarrow C$
- 123.  $B \rightarrow C$
- 124.  $A \rightarrow B$
- 125.  $C \rightarrow A$
- 126.  $C \rightarrow B$
- 127.  $A \rightarrow B$
- 128.  $A \rightarrow C$
- 129.  $B \rightarrow C$
- 130.  $B \rightarrow A$
- 131.  $C \rightarrow A$
- 132.  $B \rightarrow C$
- 133.  $A \rightarrow B$
- 134.  $A \rightarrow C$
- 135.  $B \rightarrow C$
- 136.  $B \rightarrow A$
- 137.  $C \rightarrow A$
- 138.  $C \rightarrow B$
- 139.  $A \rightarrow B$
- 140.  $C \rightarrow A$
- 141.  $B \rightarrow C$
- 142.  $B \rightarrow A$
- 143.  $C \rightarrow A$
- 144.  $B \rightarrow C$
- 145.  $A \rightarrow B$
- 146.  $A \rightarrow C$
- 147.  $B \rightarrow C$
- 148.  $A \rightarrow B$
- 149.  $C \rightarrow A$
- 150.  $C \rightarrow B$
- 151.  $A \rightarrow B$
- 152.  $A \rightarrow C$
- 153.  $B \rightarrow C$
- 154.  $B \rightarrow A$
- 155.  $C \rightarrow A$
- 156.  $B \rightarrow C$
- 157.  $A \rightarrow B$
- 158.  $A \rightarrow C$
- 159.  $B \rightarrow C$
- 160.  $B \rightarrow A$
- 161.  $C \rightarrow A$
- 162.  $C \rightarrow B$
- 163.  $A \rightarrow B$
- 164.  $C \rightarrow A$

- 165.       $B \rightarrow C$
- 166.       $B \rightarrow A$
- 167.       $C \rightarrow A$
- 168.       $C \rightarrow B$
- 169.       $A \rightarrow B$
- 170.       $A \rightarrow C$
- 171.       $B \rightarrow C$
- 172.       $A \rightarrow B$
- 173.       $C \rightarrow A$
- 174.       $C \rightarrow B$
- 175.       $A \rightarrow B$
- 176.       $C \rightarrow A$
- 177.       $B \rightarrow C$
- 178.       $B \rightarrow A$
- 179.       $C \rightarrow A$
- 180.       $B \rightarrow C$
- 181.       $A \rightarrow B$
- 182.       $A \rightarrow C$
- 183.       $B \rightarrow C$
- 184.       $B \rightarrow A$
- 185.       $C \rightarrow A$
- 186.       $C \rightarrow B$
- 187.       $A \rightarrow B$
- 188.       $C \rightarrow A$
- 189.       $B \rightarrow C$
- 190.       $B \rightarrow A$
- 191.       $C \rightarrow A$
- 192.       $B \rightarrow C$
- 193.       $A \rightarrow B$
- 194.       $A \rightarrow C$
- 195.       $B \rightarrow C$
- 196.       $A \rightarrow B$
- 197.       $C \rightarrow A$
- 198.       $C \rightarrow B$
- 199.       $A \rightarrow B$
- 200.       $A \rightarrow C$
- 201.       $B \rightarrow C$
- 202.       $B \rightarrow A$
- 203.       $C \rightarrow A$
- 204.       $B \rightarrow C$
- 205.       $A \rightarrow B$
- 206.       $A \rightarrow C$
- 207.       $B \rightarrow C$
- 208.       $A \rightarrow B$
- 209.       $C \rightarrow A$
- 210.       $C \rightarrow B$
- 211.       $A \rightarrow B$
- 212.       $C \rightarrow A$

213.	$B \rightarrow C$
214.	$B \rightarrow A$
215.	$C \rightarrow A$
216.	$C \rightarrow B$
217.	$A \rightarrow B$
218.	$A \rightarrow C$
219.	$B \rightarrow C$
220.	$A \rightarrow B$
221.	$C \rightarrow A$
222.	$C \rightarrow B$
223.	$A \rightarrow B$
224.	$A \rightarrow C$
225.	$B \rightarrow C$
226.	$B \rightarrow A$
227.	$C \rightarrow A$
228.	$B \rightarrow C$
229.	$A \rightarrow B$
230.	$A \rightarrow C$
231.	$B \rightarrow C$
232.	$B \rightarrow A$
233.	$C \rightarrow A$
234.	$C \rightarrow B$
235.	$A \rightarrow B$
236.	$C \rightarrow A$
237.	$B \rightarrow C$
238.	$B \rightarrow A$
239.	$C \rightarrow A$
240.	$B \rightarrow C$
241.	$A \rightarrow B$
242.	$A \rightarrow C$
243.	$B \rightarrow C$
244.	$A \rightarrow B$
245.	$C \rightarrow A$
246.	$C \rightarrow B$
247.	$A \rightarrow B$
248.	$A \rightarrow C$
249.	$B \rightarrow C$
250.	$B \rightarrow A$
251.	$C \rightarrow A$
252.	$B \rightarrow C$
253.	$A \rightarrow B$
254.	$A \rightarrow C$
255.	$B \rightarrow C$





Output after sorting pair of elements:

Length 1 :-

10 45 12 32 8 7 1	sorted elements: 10,45 (no change right order)
10 45 12 32 8 7 1	sorted elements: 12,32 (no change right order)
10 45 12 32 7 8 1	sorted elements: 8,7 -> 7,8
10 45 12 32 7 8 1	sorted element: 1 (no change)

Length 2 :-

10 12 32 45 7 8 1	sorted elements: 10,45, 12, 32 -> 10,12,32, 45
10 12 32 45 1 7 8	sorted elements: 7, 8,1 -> 1,8,7

Length 4 :-

1 7 8 10 12 32 45	sorted whole list;
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A3) The sequence of elements are in the order given below.

<b>1</b>	<b>2</b>	<b>3</b>	<b>4</b> <sub>100</sub>	<b>5</b>	<b>6</b>
$n^{-1}$	$(\log(n))/n$	$n^{-1/2}$	$(2^2)$	$\log_{10} n$	$\log_2 n$
<b>7</b>	<b>8</b>	<b>9</b>	<b>10</b>	<b>11</b>	<b>12</b>
$2n$	$3n$	$n2^{100}$	$\log(n!)$	$n \log n$	$\binom{n}{2}$
<b>13</b>	<b>14</b>	<b>15</b>	<b>16</b>	<b>17</b>	<b>18</b>
$n^{64}$	$n^{65}$	$2.1^{\sqrt{n}}$	$2^n$	$2^{n+1}$	$n2^n$
<b>19</b>	<b>20</b>	<b>21</b>	<b>22</b>	<b>23</b>	<b>24</b>
$3^n$	$2^{2n}$	$4^n$	$n!$	$n^n$	$2^{2^n}$

Indexing done by black where below element is of index  $i$