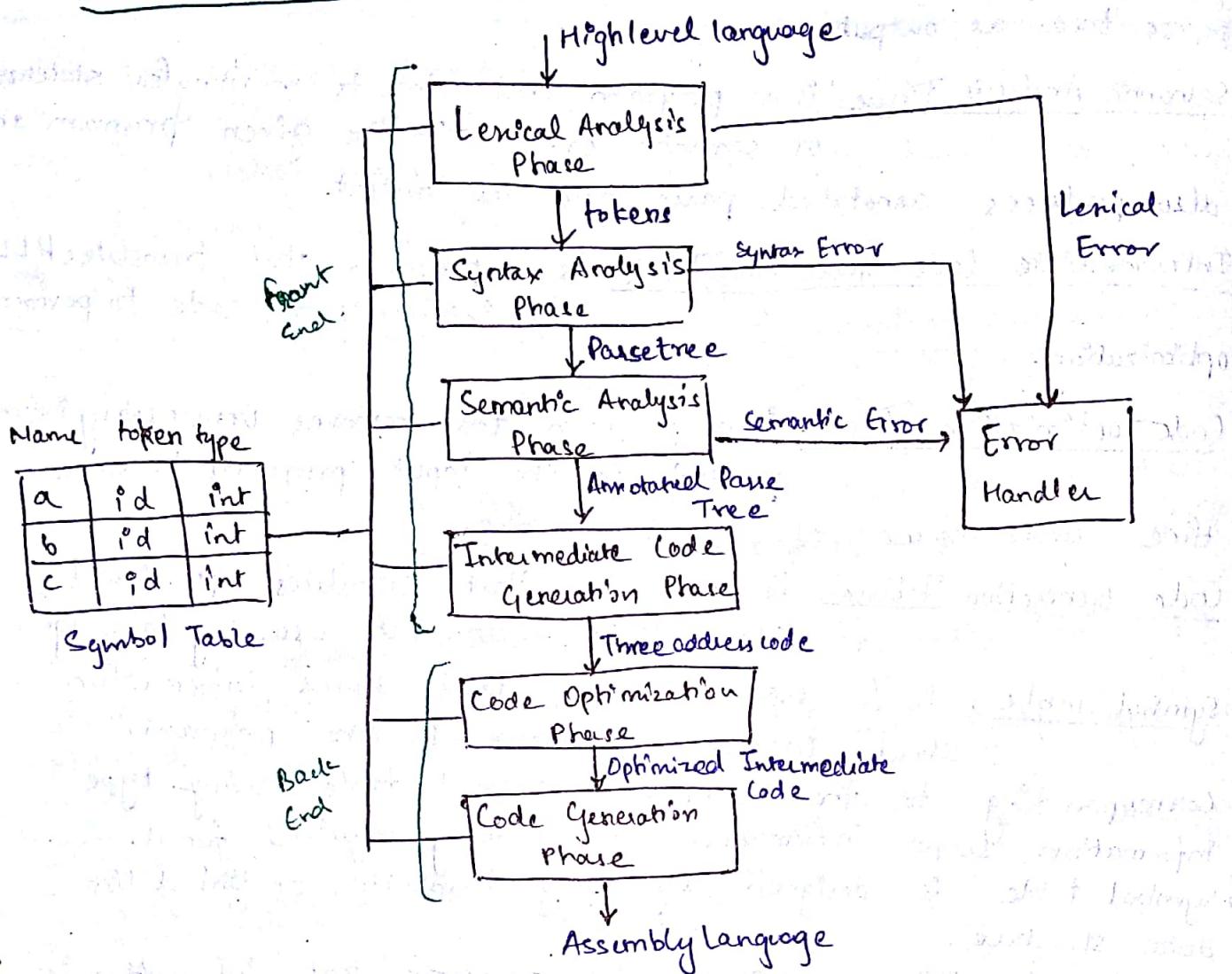


02/08/2017

COMPILER DESIGN



→ Lexical Analysis 10%

→ Parsing 60%

→ Syntax Directed Translation] 30%

→ Intermediate Code Generation

Compiler:

Compiler is a program that translates a program written in one language into an equivalent program of any language and also detects errors present in the program.

Errors detected by compiler are classified into:

- ① Lexical Errors
- ② Syntax Errors
- ③ Semantic Errors

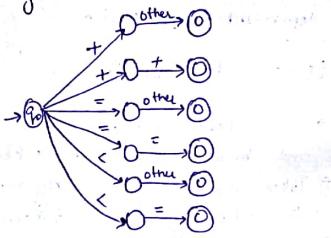
Lexical Analysis Phase: It is a program that detects lexical errors present in the HLL program and also produces tokens as output.

- # Syntax Analysis Phase: is a program that detects syntax errors present in the HLL program and also produces parse tree as output.
- # Semantic Analysis Phase: is a program that detects meaningless statements or semantic errors in the given program and also produces annotated parse tree as output.
- # Intermediate Code Generation Phase: is a program that translates HLL into intermediate code to perform optimization.
- # Code Optimization Phase: is a program that removes unnecessary information present in the input program to save time and space of target machine.
- # Code Generation Phase: is a program that translates optimized intermediate code into assembly language.
- # Symbol Table: is a data structure that stores information about identifiers present in the program corresponding to the identifier symbol table having type information, scope information and memory required for it.
- Symbol table is designed by using hashtable or linked list data structure.
- # Error Handler: If any phase detects error, that information is sent to error handler and compilation process is continued.
- Error handler having information about lexical errors, syntax errors and semantic errors.
- NOTE: Lexical analysis is designed by using reg. expression & F.A. technique.
- Syntax analysis is designed by using PDA and CFG formal methods.
 - Semantic analysis & Intermediate code designed by using CSG or SDT.
- # Front End: The phases of compiler which are depending on source language and independent of the target machine.
- front end phases include lexical analysis, syntax analysis, semantic analysis, intermediate code generation and machine independent optimization.
- # Back End: The phases of compiler which are completely dependent on target machine and independent on the source language.
- Backend phases include code generation phase and machine dependent optimization.
- # LEXICAL ANALYSIS PHASE:
- Lexical analysis reads HLL program character by character and breaks them into tokens.
 - Token describes the category of the input.
 - There are tokens in programming language:
 - ① Keyword
 - ② Identifier
 - ③ Constants
 - ④ Operator
 - ⑤ Punctuations
- * Lexeme: Sequence of characters in the source program that completely matches with rules of a token known as lexeme.
- If any sequence of characters is not a valid lexeme, then lexical error is produced.
- Lexical analysis is designed by using F.A. and regular expressions.
- NOTE:
- Detection of tokens, identifier and keyword is by using following regular expression and F.A.:
-
- ```

graph LR
 Start[I.D.] --> W((W))
 W -- d --> I((I))
 W -- other --> f((f))
 I --> other
 f --> other
 other --> returnId[return id]

```
- If any sequence of characters matching with identifier automaton then search operation is performed with keyword table.
- If search is success keyword token will be written returned otherwise identifier token will be returned.
- Lexical analyser cannot detect syntax and semantic errors.
- For the following "C" program statements, no lexical errors will be detected:
- ① int i; float f;
  - ② int i; float f;
  - ③ if (a < b) {
  - ④ abc(); x(c);

→ The following is a F.A. corresponding to token operator.



→ If any sequence of characters by which F.A. reaches final state, then token operator is produced.

→ If operator automata reaches final state with other symbol, then other symbol is excluded from token sequence.

→ The following is the F.A. and reg. exp. for token constant:

Constant:  $R_E = (\text{digit})^*$

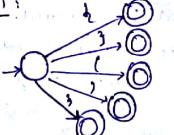
Int constant:  $\rightarrow \text{digit} \rightarrow \text{digit} \rightarrow \dots \rightarrow \text{other}$

Real constant:  $(\text{digit})^+ \cdot (\text{digit})^+$

String constant:  $\rightarrow \text{anyting} \rightarrow "$

Character constant:  $\rightarrow \text{anyting} \rightarrow ' \rightarrow '$

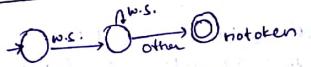
Punctuation symbol:



Comment/Line:

$\rightarrow \text{anyting} \rightarrow '*' \rightarrow '*' \rightarrow \text{no token}$

white space:  $ws = \backslash b + \backslash t + \backslash n$



→ Lexical analyser removes all white spaces present in the program.

→ If any sequence of characters matches with w.s. automata, no token will be returned, so that, w.s. is removed.

→ Lexical analyser eliminates all comment lines present in the program.

→ If any sequence of characters matches with comment line automata, no token will be returned.

Q. Identify the no. of tokens produced by following programs.

① main() (21)  $\{ \text{int } x, y; \text{ if } (x > b) \{ \text{if } (a > b) \{ \text{return } a; \text{ else } b; \} \} \}$

② main() (22)  $\{ \text{print } f ("welcome"); \} \}$

Q. Which of the following program results has lexical error?

① main() { No error

$\{ \text{int } a, b; \text{ if } (a > b) \{ \text{int } c = a + b; \text{ else } d = b + c; \} \}$

③ main() { i. No error

$\{ \text{int } a, b; \text{ char } c = "Hello"; \text{ if } (a > b + c) \{ \text{int } d = a + b + c; \} \}$

④ main() { i. No error

$\{ \text{int } a, b; \text{ if } (a > b + c) \{ \text{int } d = a + b + c; \} \}$

No error

</

- Symbol table is constructed in the lexical analyser, whenever identifier token is produced.
- In the symbol table, lexical value and token information is inserted and type of the identifier is filled during semantic analysis phase.
- Hence, lexical analyser constructs symbol table partially but not completely.

| lex | token | type |
|-----|-------|------|
| a   | id    | -    |
| b   | id    | -    |
| c   | id    | -    |

- Syntax of programming languages are represented by CFG.
- Parsing algos. are deterministically designed by using D-PDA.
- Only unambiguous grammars are used to design parser.

#### # Bottom Up Parsing:

- Bottom Up Parser constructs the parse tree, starts from the given string and proceeds towards starting symbol.
- Bottom Up Parser uses rightmost derivation in reverse order.
- Handle detection is major problem for bottom up parser.
- \* Handle: is a part or substring in the sentential form that is completely matching with the R.H.S. part of grammar production and its replacement by non-terminal leads to starting symbol. [Every matching thing is not a handle.]

Q. How many no. of handles are detected by bottom up parser for the following input string and grammar:

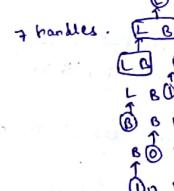
$$\begin{array}{l} \textcircled{1} \quad E \rightarrow EFT \mid T \\ \quad \quad T \rightarrow TX \mid F \\ \quad \quad X \rightarrow a \end{array}$$

$$\begin{array}{l} a + \textcircled{1} \\ a + (\textcircled{1} \times P) \\ a + (\textcircled{1} \times F) \\ a + \textcircled{1} \times F \\ a + a \times \textcircled{1} \\ a + a \times a \end{array}$$

8 handles.

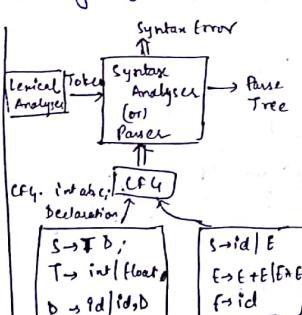
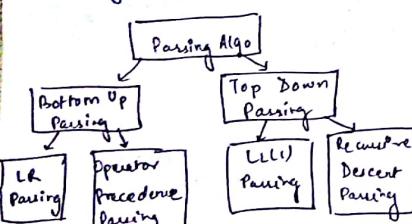
$$\begin{array}{l} \textcircled{2} \quad S \rightarrow L \\ \quad L \rightarrow LB \mid B \\ \quad B \rightarrow 0 \mid 1 \end{array}$$

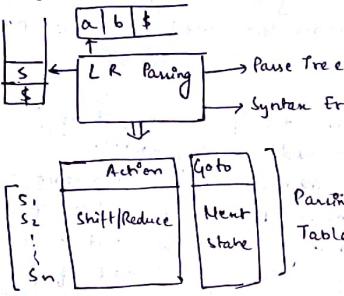
101



7 handles.

- # Syntax Analyser or Parser: is a program that takes tokens and CFG as input and verifies tokens are member of CFG or not.
- If tokens are member, parse tree is produced as output, otherwise syntax error is generated.
- To design parser, two algorithms exist, known as bottom up parsing algorithm and top down parsing algorithm.





→ LR parser is shift reduce parser because parsing is done with the help of the following 4 actions:

- ① Shift Action: Moving input symbols from input buffer to stack is known as shift action.
  - ② Reduce Action: Whenever a handle is detected in the stack, it is replaced by corresponding L.H.S. non-terminal known as reduce action.
  - ③ Accept Action: If the lookahead symbol points to "\$" (dollar) & stack contains the starting symbol, accept action is

④ Error Action:  
# LR Parsing Algorithm:

- Working based on LR Parsing table.
  - LR Parsing table is designed by using DFA.
  - Parsing table is divided into 2 parts: ① Action Part ② Goto Part
  - Action part contains all possible actions information (shift, reduce, accept and error).
  - Goto part of the table contains information regarding next state of the DFA.
  - All the tokens for which syntax analysis is performed, are taken in the input buffer along with " $\$$ " as end marker.
  - A stack is used in LR parser to identify handles.
  - Let ' $s$ ' is state of the DFA / table present in the top of the stack

and "a" is the lookahead symbol.

→ Parser takes decision regarding which action to perform from the parsing table as follows;

- If table action  $[S, a]$  (Son a) is Accept, then  
and input is valid. [No syntax error]  $[S, a] = \text{Accept}$
  - If table action  $[S, a] = \text{Blank}$ , then, there is a syntax error in  
the input and return it to error handler.
  - If action  $[S, a] = \text{shift } j$ , then "a" is pushed into the stack and  
then "j" is pushed into top of the stack and lookahead symbol is  
incremented.
  - If table action  $[S, a] = \text{reduce } A \rightarrow B$ , then:  
    - $\text{pop } 2x|B|$  (pop 2 times the length of B symbols from stack).
    - $\text{push } A$  into stack
    - $\text{push } G_0(t_k, A)$  into top of stack, where " $k$ " is previous DFA state in

→ The time complexity of LR parsing algorithm is  $O(n^3)$ , where the length of input.

- Q. How many shift actions and reduce actions are taken by LR parser to parse the input "ab" by using the following grammar and parsing table.

## Ques & Sol:

### LR Parsing:

Q. How many shift actions and reduce actions taken by LR parser to parse the input "fd+id x id" by using following grammar: and LR parsing table?

- ①  $E \rightarrow E + E$
- ②  $E \rightarrow E * E$
- ③  $E \rightarrow id$

|       | Id    | +     | x      | * |
|-------|-------|-------|--------|---|
| $S_L$ |       |       |        |   |
| $I_0$ |       |       |        |   |
| $I_1$ | $S_3$ | $S_4$ | accept |   |
| $I_2$ | $T_1$ | $T_3$ | $R_3$  |   |
| $I_3$ | $S_2$ |       |        |   |
| $I_4$ | $S_2$ |       |        |   |
| $I_5$ | $T_1$ | $S_4$ | $R_1$  |   |
| $I_6$ | $T_1$ | $T_2$ | $R_2$  |   |

| E |
|---|
| 1 |
| 5 |
| 6 |

- ①  $\$ | 0 | id | 2$
- ②  $\$ | 0 | id | 2$
- ③ pop 2 & length
- ④  $\$ | 0 | E | 1$
- ⑤  $\$ | 0 | E | 1 | + | 3 | id | 2$
- ⑥  $\$ | 0 | E | 1 | + | 3 | id | 2 \Rightarrow E | 5$
- ⑦  $\$ | 0 | E | 1 | + | 3 | E | 5 | * | 4$
- ⑧  $\$ | 0 | E | 1 | + | 3 | E | 5 | x | 4 | id | 2$
- ⑨  $\$ | 0 | E | 1 | + | 3 | E | 5 | x | 4 | id | 2 \Rightarrow E | 6$
- ⑩  $\$ | 0 | E | 1 | + | 3 | E | 5$
- ⑪  $\$ | 0 | E | 1$

Accept: shift = 5 Reduce = 5

### # LR - Parsing Table Construction:

→ To construct LR parsing table, 4 methods exist, known as:

- ① LR(0)
- ② CLR(1)
- ③ CRL(1)
- ④ LALR(1)

### ① LR(0) Parsing Table Construction:

→ To construct LR(0) parsing table for the given grammar:

- ① Construct augmented grammar
- ② calculated LR(0) items set, by using closure function and goto function.
- ③ Construct LR(0) items DFA
- ④ Construct LR(0) parsing table from DFA.

\* Augmented Grammar: means adding a new production  $S' \rightarrow S$  for the original grammar known as augmented grammar.

→ Advantage of constructing augmented grammar is to get accept action in the parsing table.

→ Whenever parser tries to perform reduce action by using augmented production then accept action is called.

\* LR(0) Item: Any context free grammar production having (.) dot on the RHS part at some position, is called LR(0) item.

→ The LR(0) Item  $A \rightarrow X_1 Y_2$  means " $X_1$ " is there in the stack and parser has to see "2".

→ In any LR(0) item, the LHS part of the (.) dot is present in the stack and RHS part is ready to come into the stack.

→ In any LR(0) item, if (.) dot is at rightmost end, then, reduce action is performed.

→ Corresponding to given grammar, total no. of LR(0) items are calculated by using closure() and goto() functions.

→ The task of closure() is, in any LR(0) item, if (.) is followed by non-terminal exists on the RHS part, then closure() adds that non-terminal production and places puts (.) dot in the first place on the RHS part.

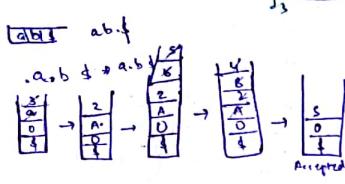
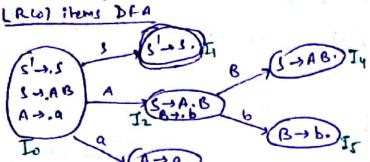
$$\begin{array}{|c|} \hline S \rightarrow A \cdot B \\ \hline B \rightarrow a \\ \hline \end{array} \quad \begin{array}{|c|} \hline S \rightarrow \cdot A B \\ \hline A \rightarrow a \\ \hline \end{array}$$

→ The task of goto() is, if more (.) dot are present ahead towards right side.

→ Construct LR(0) parsing table for the following grammar.

Q. Construct LR(0) parsing table for the following grammar:

$S \rightarrow A B$   
 $A \rightarrow a$   
 $B \rightarrow b$



Action

| a  | b  | \$ |
|----|----|----|
| I0 | S3 |    |
| I1 |    |    |
| I2 | S5 |    |
| I3 | T2 | T2 |
| I4 | T1 | T1 |
| I5 | T3 | T3 |

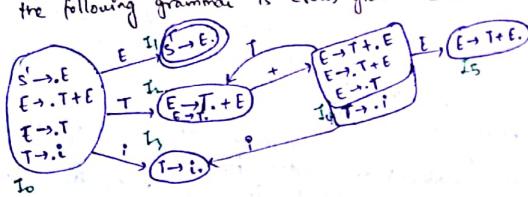
Goto

| S  | A | B |
|----|---|---|
| I1 | 2 |   |
| I2 |   | 4 |
| I3 |   |   |
| I4 |   |   |
| I5 |   |   |

(NOTE) Any grammar, LR(0) parsing table contains multiple actions in the same box, That grammar is not LR(0) grammar, otherwise, it is LR(0) grammar.

Q. Check whether the following grammar is LR(0) grammar or not.

①  $E \rightarrow T+E$   
 ②  $E \rightarrow T$   
 ③  $T \rightarrow i$



Action

| +  | i              | \$             |
|----|----------------|----------------|
| I0 | S3             |                |
| I1 |                |                |
| I2 | $\frac{S3}{i}$ | $\frac{T2}{i}$ |
| I3 | T3             | T3             |
| I4 | S3             |                |
| I5 | T1             | T1             |

Goto

| E  | T |
|----|---|
| I1 | 2 |
| I2 | 3 |
| I3 | 5 |
| I4 | 2 |

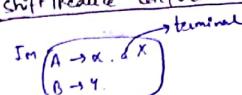
Not LR(0) grammar.

(NOTE)

→ If LR(0) items DFA having either shift/reduce conflict state or reduce-reduce conflict state, then, the given grammar is not LR(0) grammar.

→ The following are the conflict states in LR(0) items DFA:

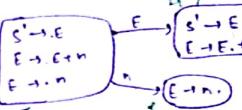
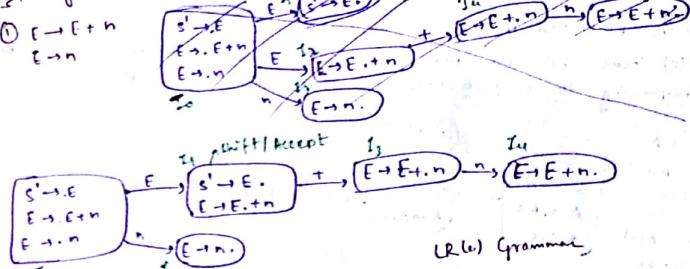
Shift/Reduce Conflict State



Reduce/Reduce Conflict State



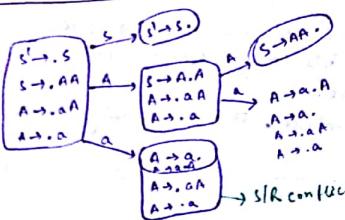
Q. Verify which of the following grammars are LR(0) grammars:



LR(0) Grammar

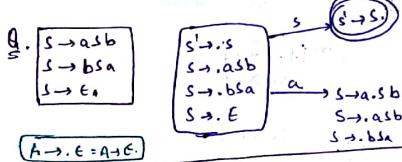
②  $S \rightarrow AA$   
 $A \rightarrow AA$   
 $A \rightarrow a$

Not LR(0)  
 grammar.



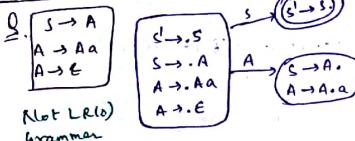
Ambiguous

**NOTE** All ambiguous grammars are not LR(0) grammars.  
 → Any ambiguous grammar, LR(0) parsing table contains either S/R conflict or R/R conflict.  
 → All LR(0) grammars are unambiguous grammars, but all unambiguous grammars need not be LR(0).



**NOTE F** The LR(0) item  $[A \xrightarrow{\cdot} E = A \rightarrow E_0]$ .

→ LR(0) items DFA does not contain  $\epsilon$ -transitions. Hence, the LR(0) items corresponding to  $\epsilon$ -productions are reduced in the initial state.



#### # Drawback of LR(0):

→ In LR(0) parsing table, reduce actions are placed without considering lookahead symbol. This may lead to unnecessary reduce actions in the parsing table.

→ To avoid this drawback, SLR(1) parsing tables are used in LR parser.

#### # first():

→ first() of a non-terminal is set of terminals existing first place of RHS part of grammar production.

→ first() of string abc → first(abc) = {a}

→ If the production is of the form:  
 $A \rightarrow a \star b^k$  then  $\text{first}(A) = \{a\}$

- ③ If any production is of the form:  $A \rightarrow B \alpha$ , where B does not produce  $\epsilon$ , directly or indirectly, then  $\text{first}(A) = \text{first}(B)$ .
- ④ If any production is of the form:  $A \rightarrow B \alpha$ , B produces  $\epsilon$  directly or indirectly, then:
- $$\text{first}(A) = \{ \text{first}(B) - \{ \epsilon \} \cup \text{first}(\alpha) \}$$

Q. Calculate first() of each non-terminal, for the following grammar productions.

①  $E \rightarrow TE'$   
 $E' \rightarrow +TE' | \epsilon$   
 $T \rightarrow FT'$   
 $T' \rightarrow *FT' | \epsilon$   
 $F \rightarrow (E) | a$

|    |          |
|----|----------|
| E  | {(a, y)} |
| E' | {+, E'}  |
| T  | {*, T'}  |
| T' | {*, E'}  |
| F  | {(, a)}  |

②  $S \rightarrow AB$   
 $A \rightarrow a|b$   
 $B \rightarrow c|d$

|   |           |
|---|-----------|
| S | {a, b, E} |
| A | {a, b}    |
| B | {c, d}    |

③  $S \rightarrow AB$   
 $A \rightarrow a|b$   
 $B \rightarrow d$

|   |           |
|---|-----------|
| S | {a, b, E} |
| A | {a, b}    |
| B | {d}       |

④  $S \rightarrow AB$   
 $A \rightarrow a|b|c$   
 $B \rightarrow d|e|f$

|   |                       |
|---|-----------------------|
| S | {a, b, c, d, e, f, E} |
| A | {a, b, c}             |
| B | {d, e, f}             |

⑤  $S \rightarrow ACB | Cb | Ba$   
 $A \rightarrow d|bC$   
 $B \rightarrow g|E$   
 $C \rightarrow h|t$

|   |                    |
|---|--------------------|
| S | {d, g, h, b, a, E} |
| A | {d, g, h, E}       |
| B | {g, E}             |
| C | {h, t}             |

⑥  $S \rightarrow aABA | bBA | aE$   
 $A \rightarrow S$   
 $B \rightarrow S$

|   |           |
|---|-----------|
| S | {a, b, E} |
| A | {a, b, E} |
| B | {a, b, E} |

Scanned by CamScanner

### # Follow(1) set:

→ Follow(1) of a non-terminal is set of terminals, which appears immediately after RHS part of [after] that non-terminal in some sentential form.

(1) Follow of starting symbol of the grammar is \$.

$$\text{Follow}(S) = \{\$ \}$$

(2) Any production is of the form:  $A \rightarrow \alpha BX ; \text{Follow}(B) = \text{First}(X)$

(3)  $F \rightarrow \alpha B ; \text{Follow}(B) = \text{Follow}(A)$

(4)  $A \rightarrow \alpha BX ; X \rightarrow E$  .  $\text{Follow}(B) = \{\text{First}(X) - E\} \cup \text{Follow}(A)$

NOTE: follow set doesn't contain E.

Q. Calculate follow(1) of each non-terminal, for the following grammar:

$$① S \rightarrow AaAb | BbBa \\ A \rightarrow \epsilon \\ B \rightarrow \epsilon$$

|   |        |
|---|--------|
| S | \$, #  |
| A | {a, b} |
| B | {b, a} |

$$② E \rightarrow TE' \\ E' \rightarrow +E'E' \\ T \rightarrow FT' \\ T' \rightarrow xFT' | E \\ F \rightarrow (E) | a$$

|    |           |
|----|-----------|
| E  | {+, #}    |
| E' | {+, #}    |
| T  | {+, #}    |
| T' | {+, #}    |
| F  | {x, +, #} |

$$③ S \rightarrow E + Ts's' | a \\ S' \rightarrow es | e \\ E \rightarrow b$$

|    |        |
|----|--------|
| S  | \$, e  |
| S' | {e, s} |
| E  | {t}    |

$$④ S \rightarrow aAbA | bBba | \epsilon \\ A \rightarrow s \\ B \rightarrow s$$

|   |        |
|---|--------|
| S | \$, b  |
| A | {b, #} |
| B | {b}    |

$$⑤ S \rightarrow L = R \\ S \rightarrow R \\ L \rightarrow R \\ L \rightarrow id \\ R \rightarrow L$$

|   |        |
|---|--------|
| S | \$, #  |
| L | {=, #} |
| R | {#, =} |

Q. find first & follow?

|   | First     | Follow     |
|---|-----------|------------|
| S | {a, b, E} | {\$, b, a} |
| A | {a, b, E} | {b, a}     |
| B | {a, b, E} | {a, b, a}  |

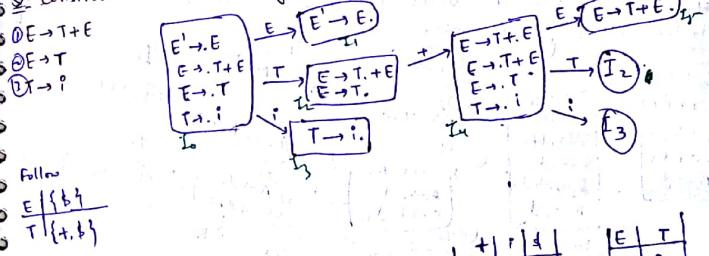
### # Simple LR(1) [SLR(0)]

\* Comparison between LR(0) and SLR(1) parsing tables:

- ① No. of states are same in both tables.
- ② No. of shift actions are same in both tables.
- ③ No. of goto table entries are same in both tables.
- ④ No. of reduce actions may be different in both tables.
- ⑤ No. of error actions may be different in both tables.
- ⑥ To construct LR(0) and SLR(1) parsing tables, LR(0) items automata (DFA) is used.

NOTE: In SLR(1) parsing table, reduce actions are placed as based on L.H.S. non-terminal's follow(1) set values.

Q. Construct SLR(1) parsing table for the following grammar:



|    | +  | 1  | 2 | E   | T |
|----|----|----|---|-----|---|
| I0 |    |    |   | S3  |   |
| I1 |    |    |   | and |   |
| I2 | S4 | T2 |   |     |   |
| I3 | T3 | T3 |   |     |   |
| I4 | S3 |    |   |     |   |
| I5 | T1 |    |   |     |   |

NOTE: Any grammar, SLR(1) parsing table contains either SR conflict or RR conflict, then that grammar is not SLR(1) grammar. Otherwise, SLR(1) grammar.

→ The following are conflict states corresponding to SLR(1) parser.

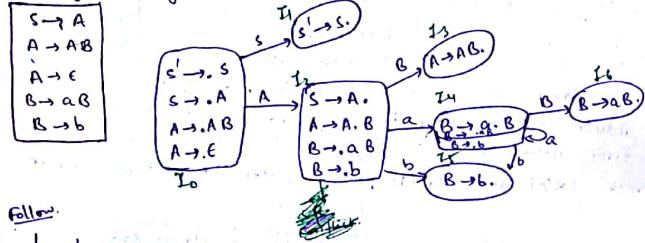
SR conflict:  $A \rightarrow d, aB$  (produces terminal in follow(B))

RR conflict:  $A \rightarrow d, a$  (produces terminal in follow(B))

If  $a \in \text{follow}(B)$

$\text{Follow}(A) \cap \text{Follow}(B) \neq \emptyset$

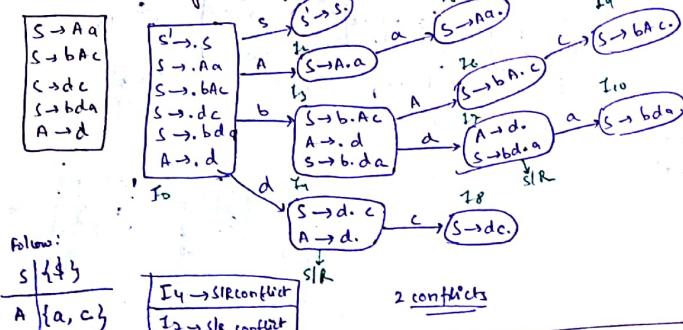
Q. Verify following grammars are SLR(1) grammars or not.



## Follow.

|   |                |              |
|---|----------------|--------------|
| S | $\{f, \$\}$    | No conflict. |
| A | $\{a, b, \$\}$ |              |
| B | $\{a, b, \$\}$ |              |

Q. How many conflict states exist in CLR(1) parser corresponding to the following grammar.

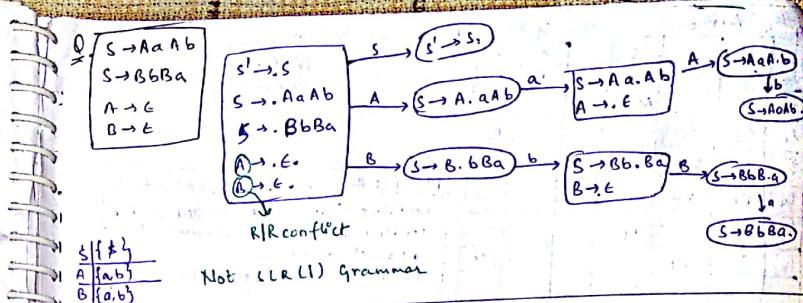


**NOTE** → All LR(0) grammars are SLR(1) grammars, but all SLR(1) grammars need not be LR(0) grammars.

All ambiguous grammars are not SLR(1) grammar

→ Any ambiguous grammar, SLR(1) parsing table contains either S/R or N/A conflict

conflict or RLR conflict. All such grammars are unambiguous grammars.



→ # Drawbacks of SLR(1):

→ In SRL(1) passing, reduce actions are placed, based on follow() set values.

- follow() set may result more number of entries.
- hence, parsing table contains unnecessary reduce actions.
- To place reduce actions properly, LALR(1) parsing tables are used.

- # CLR(1) Canonical LR(1) and Lookahead LR(1) (LALR(1)) :
- To construct CLR(1) and LALR(1) tables, LR(1) items DFA is

$\Rightarrow$  LEL(1) item is nothing but any LR(0) item associated with lookahead.  
 $\Rightarrow$  construct LEL(1) parsing table for the following grammar.

Q. Construct CLR(1) parser of given grammar or not.  
 Q. Verify given grammar is CLR(1) grammar or not.  
 Q. Construct LALR(1) parsing table for the following grammars.

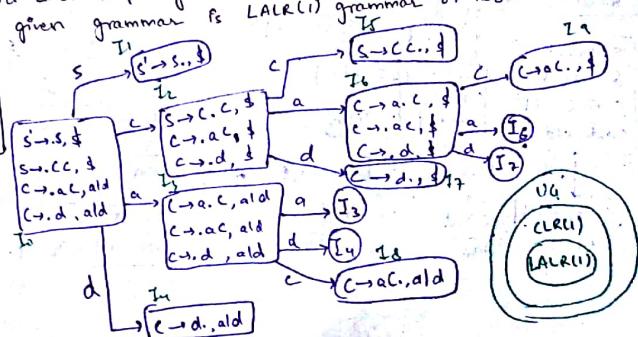
D. Construct LALR(1) parsing table

E. Verify given grammar is LALR(1) grammar or not.

```

graph LR
 S((S)) -- "c" --> C((C))
 S -- "a" --> T((T))
 T -- "c" --> C
 T -- "a" --> S
 C -- "c" --> S
 C -- "a" --> T
 C -- "a" --> C
 C -- "c" --> C
 I0((I_0)) -- "a" --> C

```



|                | Action         | a              | d              | t | l | w |
|----------------|----------------|----------------|----------------|---|---|---|
| T <sub>0</sub> | c <sub>3</sub> | c <sub>4</sub> |                |   |   |   |
| T <sub>1</sub> | c <sub>8</sub> |                | S <sub>7</sub> |   |   |   |
| T <sub>2</sub> |                | S <sub>4</sub> |                |   |   |   |
| T <sub>3</sub> | S <sub>1</sub> | S <sub>4</sub> |                |   |   |   |
| T <sub>4</sub> | r <sub>3</sub> | r <sub>3</sub> |                |   |   |   |
| T <sub>5</sub> |                |                | r <sub>1</sub> |   |   |   |
| T <sub>6</sub> | S <sub>6</sub> | S <sub>7</sub> |                |   |   |   |
| T <sub>7</sub> |                |                | r <sub>1</sub> |   |   |   |
| T <sub>8</sub> | r <sub>2</sub> | r <sub>2</sub> |                |   |   |   |
| T <sub>9</sub> |                |                | r <sub>1</sub> |   |   |   |

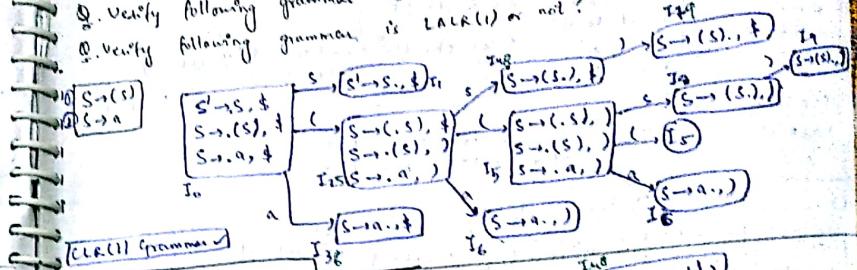
NOTE: Any grammar CLR(1) table contains either LR conflict or LR conflict, then that grammar is not CLR(1) grammar.  
Otherwise CLR(1) grammar.

- ① S → ε
- ② C → ac
- ③ C → ad

|                | Action | a | d | t | l | w |
|----------------|--------|---|---|---|---|---|
| T <sub>0</sub> |        |   |   |   |   |   |
| T <sub>1</sub> |        |   |   |   |   |   |
| T <sub>2</sub> |        |   |   |   |   |   |
| T <sub>3</sub> |        |   |   |   |   |   |
| T <sub>4</sub> |        |   |   |   |   |   |
| T <sub>5</sub> |        |   |   |   |   |   |
| T <sub>6</sub> |        |   |   |   |   |   |
| T <sub>7</sub> |        |   |   |   |   |   |
| T <sub>8</sub> |        |   |   |   |   |   |
| T <sub>9</sub> |        |   |   |   |   |   |

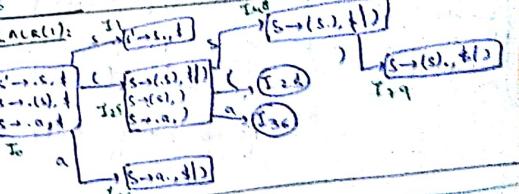
NOTE: Any grammar LALR(1) table contains LR or RL conflict, if it is not LALR(1), otherwise it is LALR(1).

- Q. Verify following grammar is CLR(1) or not?  
Q. Verify following grammar is LALR(1) or not?



CLR(1) grammar

|                | Action         | a              | d | t | l | w |
|----------------|----------------|----------------|---|---|---|---|
| T <sub>0</sub> | S <sub>3</sub> | S <sub>4</sub> |   |   |   |   |
| T <sub>1</sub> |                |                |   |   |   |   |
| T <sub>2</sub> | S <sub>6</sub> | S <sub>5</sub> |   |   |   |   |
| T <sub>3</sub> |                |                |   |   |   |   |
| T <sub>4</sub> | S <sub>6</sub> | S <sub>7</sub> |   |   |   |   |
| T <sub>5</sub> |                |                |   |   |   |   |
| T <sub>6</sub> | S <sub>6</sub> | S <sub>8</sub> |   |   |   |   |
| T <sub>7</sub> |                |                |   |   |   |   |
| T <sub>8</sub> |                |                |   |   |   |   |
| T <sub>9</sub> |                |                |   |   |   |   |



|                | Action         | a              | d | t | l | w |
|----------------|----------------|----------------|---|---|---|---|
| T <sub>0</sub> | S <sub>3</sub> | S <sub>4</sub> |   |   |   |   |
| T <sub>1</sub> |                |                |   |   |   |   |
| T <sub>2</sub> | S <sub>6</sub> | S <sub>5</sub> |   |   |   |   |
| T <sub>3</sub> |                |                |   |   |   |   |
| T <sub>4</sub> | S <sub>6</sub> | S <sub>7</sub> |   |   |   |   |
| T <sub>5</sub> |                |                |   |   |   |   |
| T <sub>6</sub> | S <sub>6</sub> | S <sub>8</sub> |   |   |   |   |
| T <sub>7</sub> |                |                |   |   |   |   |
| T <sub>8</sub> |                |                |   |   |   |   |
| T <sub>9</sub> |                |                |   |   |   |   |

No. of States in Parsing Table

LALR(1), CLR(1), LALR(1) & CLR(1)

No. of conflict states in LALR following are the conflict states in LALR items DFA corresponding to CLR(1) and LALR(1) parsing tables.

SL Conflict  
A → N, B, t, f, l  
B → X, t, f, l

HL Conflict  
(f, l) (t, f, l)

Ant x, SL  
B = Y(t, f, l)

Q. Verify the following grammar is CLR(1) grammar or not,  
LALR(1) grammar or not.

$$\begin{array}{l} S \rightarrow AaAb \\ S \rightarrow BbBa \\ A \rightarrow e \\ B \rightarrow e. \end{array}$$

CLR(1) ✓  
LALR(1) ✓

$$\begin{array}{l} S' \rightarrow S, \$ \\ S \rightarrow AaAb, \$ \\ S \rightarrow BbBa, \$ \\ A \rightarrow e, a \\ B \rightarrow e., b \end{array}$$

$$\begin{array}{l} S \rightarrow S, \$ \\ A \xrightarrow{I_1} S \rightarrow AaAb, \$ \\ B \xrightarrow{I_2} S \rightarrow BbBa, \$ \\ \xrightarrow{I_3} S \rightarrow B.bBa, \$ \\ \xrightarrow{I_4} S \rightarrow Bb.Ba, \$ \\ B \xrightarrow{I_5} S \rightarrow Bb.Ba, \$ \\ B \xrightarrow{I_6} S \rightarrow B.BB.a, \$ \\ \xrightarrow{I_7} S \rightarrow Bb.BB.a, \$ \\ B \xrightarrow{I_8} S \rightarrow Bb.BB.a, \$ \\ B \xrightarrow{I_9} S \rightarrow Bb.BB.a, \$ \end{array}$$

No. of states: LR(1) = 10 | SLR(1) = 10 X | LALR(1) = 10 | CLR(1) = 10 X | LR(0) = 10 X

→ Any ambiguous grammar is not CLR(1) and not LALR(1) because ambiguous grammar parsing table having conflicts.

Q. Verify the following grammar is CLR(1) grammar or not, LALR(1)

$$\begin{array}{l} S \rightarrow Aa \\ S \rightarrow bAC \\ S \rightarrow BC \\ S \rightarrow bBA \\ A \rightarrow d \\ B \rightarrow d \end{array}$$

I<sub>0</sub>

$$\begin{array}{l} S' \rightarrow S, \$ \\ S \rightarrow Aa, \$ \\ S \rightarrow bAC, \$ \\ S \rightarrow BC, \$ \\ S \rightarrow bBA, \$ \\ A \rightarrow d, a \\ B \rightarrow d, c \end{array}$$

$$\begin{array}{l} S \rightarrow S, \$ \\ A \xrightarrow{I_1} S \rightarrow Aa, \$ \\ B \xrightarrow{I_2} S \rightarrow bAC, \$ \\ B \xrightarrow{I_3} S \rightarrow BC, \$ \\ B \xrightarrow{I_4} S \rightarrow bBA, \$ \\ A \xrightarrow{I_5} S \rightarrow bAC, \$ \\ A \xrightarrow{I_6} S \rightarrow BC, \$ \\ A \xrightarrow{I_7} S \rightarrow bBA, \$ \\ B \xrightarrow{I_8} S \rightarrow bAC, \$ \\ B \xrightarrow{I_9} S \rightarrow BC, \$ \\ B \xrightarrow{I_{10}} S \rightarrow bBA, \$ \end{array}$$

$$\begin{array}{l} A \rightarrow d, a \\ B \rightarrow d, c \\ B \xrightarrow{I_{11}} A \rightarrow d, a \\ B \xrightarrow{I_{12}} A \rightarrow d, c \\ B \xrightarrow{I_{13}} A \rightarrow d, a \\ B \xrightarrow{I_{14}} A \rightarrow d, c \end{array}$$

LR(0) ✓  
LALR(1) X

CLR(1) ✓  
LALR(1) X

I<sub>1</sub>

Conflict:

$$\begin{array}{l} A \rightarrow \alpha, \{\beta\} \\ B \rightarrow \beta, \{\alpha\} \end{array}$$

$$\begin{array}{l} A \rightarrow \alpha, \{\beta\} \\ B \rightarrow \beta, \{\alpha\} \end{array}$$

$$\begin{array}{l} A \rightarrow \alpha, \{\beta, \gamma\} \\ B \rightarrow \beta, \{\alpha, \gamma\} \end{array}$$

→ LALR(1)  
R/R conflict

# States.

CLR(1) → 13  
LALR(1) → 12  
SLR(1) → 12  
LR(0) → 12

H.W. Find the number of states of LR(0), SLR(1), CLR(1), LALR(1) parsing tables.

Verify the given grammar is LR(0), SLR(1), CLR(1), LALR(1) or not?

$$\begin{array}{l} S \rightarrow A \\ A \rightarrow AB \\ A \rightarrow E \\ B \rightarrow aB \\ B \rightarrow b \end{array}$$

$$\begin{array}{l} S \rightarrow S, \$ \\ S \rightarrow A, \$ \\ A \rightarrow AB, \$ \\ A \rightarrow E, \$ \\ B \rightarrow aB, \$ \\ B \rightarrow b, \$ \\ A \xrightarrow{I_1} S \rightarrow A, \$ \\ A \xrightarrow{I_2} S \rightarrow AB, \$ \\ A \xrightarrow{I_3} S \rightarrow E, \$ \\ B \xrightarrow{I_4} S \rightarrow aB, \$ \\ B \xrightarrow{I_5} S \rightarrow b, \$ \\ B \xrightarrow{I_6} S \rightarrow aB, \$ \\ B \xrightarrow{I_7} S \rightarrow b, \$ \\ B \xrightarrow{I_8} S \rightarrow aB, \$ \\ B \xrightarrow{I_9} S \rightarrow b, \$ \\ B \xrightarrow{I_{10}} S \rightarrow aB, \$ \\ B \xrightarrow{I_{11}} S \rightarrow b, \$ \end{array}$$

No Conflict

CLR(1) ✓

LALR(1) ✓

LR(0) X

SLR(1) ✓

# States

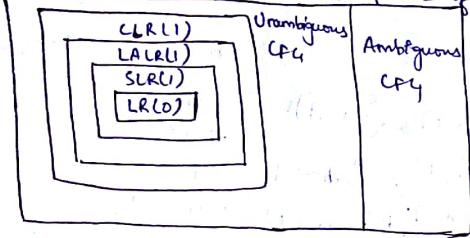
7

7

7

7

\*Power of a parser: No. of grammars suitable for particular parser is known as power of that parser.



Ambiguous CFG

Ambiguous CFT

[LR(0)] CSLR(1) CLAR(1) CLK(1)

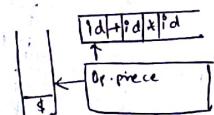
To perform reduce action, pop the symbols from stack, such that the terminal on top of stack has less precedence over most recently popped out terminal.

The time complexity of operator precedence parsing alg. is  $O(n)$ , where 'n' is the length of input.

The size of operator precedence parsing table is  $(T+1)^L$

Q: How many shift and reduce actions are taken by O.P. parser to parse the input "Id + id \* Id" by using the following grammar and parsing table.

$E \rightarrow E + E$   
 $E \rightarrow E * E$   
 $E \rightarrow id$



Stack      Input      Action

① \$      < . id + id \* id \$      shift

② \$ id      > + id id \$      reduce

③ \$ E      < . id \* id \$      shift

④ \$ E E      > . id \* id \$      reduce shift

⑤ \$ E E + id      > . id \$      reduce

⑥ \$ E E + id      < . id \$      shift

⑦ \$ E E + id \* id      < . id \$      shift

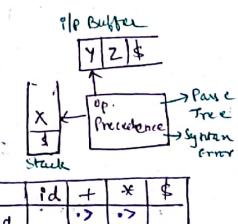
⑧ \$ E E + id \* id      > . id \$      reduce

⑨ \$ E E + id \* id      > . \$      reduce

⑩ \$ E E + id      > . \$      reduce

⑪ \$ E E + id      - \$      accept

|      |   |   |        |
|------|---|---|--------|
| id   | + | * | \$     |
| id   | > | > | >      |
| + <  | > | < | .      |
| * <  | > | > | .      |
| \$ < | < | < | accept |



|    | id | + | * | \$     |
|----|----|---|---|--------|
| id | >  | > | > |        |
| +  | <  | > | > |        |
| *  | >  | < | = |        |
| \$ | >  |   |   | accept |

Op. precedence Table.

To perform reduce action, pop symbols from stack, such that the terminal on top of stack has lesser precedence over

| <u>state</u>                                | <u>input</u> | <u>action</u>         |
|---------------------------------------------|--------------|-----------------------|
| ① <u>\$</u>                                 | <            | id × id + id \$ shift |
| ③ <u>\$ id</u>                              | >            | id + id \$ reduce     |
| ② <u>\$ E</u>                               | <            | id + id \$ S          |
| ④ <u>\$ E   *</u>                           | <            | id + id \$ S          |
| ⑤ <u>\$ E   * id</u><br><small>(q5)</small> | ->           | + id \$ R             |
| ⑥ <u>\$ E   * E</u>                         | >            | + id \$ R             |
| ⑦ <u>\$ E</u>                               | <            | + id \$ S             |
| ⑧ <u>E E   +</u>                            | <            | id \$ S               |
| ⑨ <u>E E   + id</u>                         | >            | + id \$ R             |
| ⑩ <u>E E   + E</u>                          | ->           | + id \$ R             |
| ⑪ <u>E E</u>                                | <            | accept                |

# Construction of Operator Precedence Parsing table: • table construction is

- Operator precedence parsing table construction is different for ambiguous grammars and unambiguous grammars.
  - If the grammar is unambiguous, then, to get precedences of operators parse tree method is used.
  - If the grammar is ambiguous, general programming language or general mathematical precedences are inserted in the table.

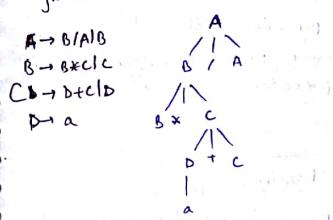
**NOTE**

- If any operator grammar contains both left recursion and right recursion, then, it is ambiguous.
- In any operator grammar, either left recursion or right recursion, but not both and different precedence operators present at different non-terminals, then it is unambiguous.

~~big~~ Non-~~assoc~~ Precedence grammar:

- A CFG is said to be operator precedence grammar if it is operator grammar and at most one precedence relation exists between every pair of terminals.
  - In operator precedence parsing table, '\$' is lesser precedence over all other operators.
  - Identifier is having higher precedence over all other operators.

Q. Construct operator precedence parsing table for the following grammar.



|    | a | + | * | / | \$      |
|----|---|---|---|---|---------|
| a  | > | > | > | > | >       |
| +  | < | < | > | > | >       |
| *  | < | < | > | > | >       |
| /  | < | < | < | < | >       |
| \$ | < | < | < | < | accept. |

$A \rightarrow AXA \mid a \mid t \mid \$$  Construct op. prec. parsing table for the following ambiguous grammar.

$\rightarrow$  left associative  
 $\neq \rightarrow$  " "

use general  
precedence associative  
rules

|    |   |              |              |        |
|----|---|--------------|--------------|--------|
|    | a | +            | *            | \$     |
| a  | . | >            | >            | >      |
| +  | < | ( $\gamma$ ) | <            | >      |
| x  | < | >            | ( $\gamma$ ) | >      |
| \$ | < | <            | L-           | accept |

Q Which of the following is true about precedence and associativity of operators from the following grammar. A

$A \rightarrow B \sqcup A \sqcap B$   
 $B \rightarrow B \& C \sqcup C$   
 $C \rightarrow D @ C \sqcap D$   
 $D \rightarrow E - D \sqcap E$   
 $E \rightarrow a$

- X(2) '@' is lesser precedence than '^' and '-'

X(3) Both '^' and '@' are left associative

(4) '-' operator is higher precedence than '^'; '@' and '-' operator is right associative.

X(5) All operators present in grammar are right associative

```

graph TD
 A --- B
 A --- C
 B --- D
 B --- E
 E --- F

```

Q. Consider the following grammar: which is true?

- X → X ⊕ Y | Y
- Y → Z \* Y | z
- Z → a

X @ Both “⊕” and “\*” are left associative  
 X @ Both “⊕” and “\*” are right associative  
 @ “⊕” is left associative & “\*” is right associative

x ① None of these

Q. Consider the following grammar which of the following is true:

$$\begin{array}{l} E \rightarrow E * F \mid F + E \mid F \\ F \rightarrow F - F \mid id \end{array}$$

- ① "\*" is higher precedence than "+"
- ② "-" is higher precedence than "\*"
- ③ "+" and "-" have same precedence
- ④ "F" is higher precedence than "id"



### # Drawbacks of Operator Precedence Parsing:

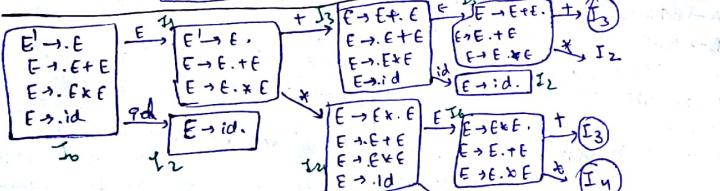
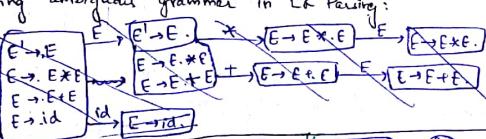
- The power of operator precedence parser is very less compared to LR parser [suitable only for operator precedence grammars].
- Hence, LR parser is powerful compared to operator precedence parser in bottom up parsing.

Q5/03/2017:

### # Handling Ambiguous Grammar in LR Parsing:

Q. Handle following ambiguous grammar in LR Parsing:

- ①  $E \rightarrow E + E$
- ②  $E \rightarrow E * E$
- ③  $E \rightarrow id$



| id                            | +                                                           | *              | \$             |
|-------------------------------|-------------------------------------------------------------|----------------|----------------|
| I <sub>0</sub> S <sub>2</sub> |                                                             |                |                |
| I <sub>1</sub>                | S <sub>3</sub> S <sub>4</sub>                               |                |                |
| I <sub>2</sub>                | T <sub>3</sub> T <sub>3</sub>                               | T <sub>3</sub> |                |
| I <sub>3</sub> S <sub>2</sub> |                                                             |                |                |
| I <sub>4</sub> S <sub>2</sub> |                                                             |                |                |
| I <sub>5</sub>                | S <sub>1</sub> S <sub>2</sub> T <sub>1</sub>                |                | T <sub>1</sub> |
| I <sub>6</sub>                | S <sub>1</sub> S <sub>2</sub> T <sub>2</sub> T <sub>2</sub> |                | T <sub>2</sub> |

| E              | I |
|----------------|---|
| E { +, *, \$ } |   |
| 5              |   |
| 6              |   |

(Case 1): The SLR conflict at I<sub>0</sub> state on "+" is resolved by giving priority for shift action over reduce action in order to make "+" as higher precedence than "\*".

(Case 2): The SLR conflict at I<sub>5</sub> state on "+" is resolved by giving priority for reduce action over shift action in order to make "+" as left associative.

(Case 3): The SLR conflict at I<sub>6</sub> state on "+" is resolved by giving priority for reduce action over shift action in order to make "+" as higher precedence than "\*".

(Case 4): The SLR conflict at I<sub>6</sub> state on "\*" is resolved by giving priority for reduce action over shift action in order to make "\*" as left associative.

→ All expression grammar's conflicts in the parsing table are resolved based on precedence and associativity of operators.

→ To design lexical analyser, there exists a tool, known as LEX tool.

→ To design parser (LR), there exists a tool known as YACC [Yet another compiler compiler].

→ SLR conflict:

→ For general ambiguous grammars SLR conflict is resolved by giving priority for shift action over reduce action.

→ If parsing is success for shift action, then shift action is suitable in the parsing table. Otherwise, reduce action is suitable in the parsing table.

→ RLR Conflict:

→ For general ambiguous grammars, RLR conflict in the parsing table is resolved by giving priority for first reduce action over second reduce action.

→ If the parsing is success for first action, then first reduce action is suitable in the parsing table otherwise, second reduce action is suitable.

→ The LR parser generator tool (YACC) also resolves the conflicts in the same manners.

Q. Consider the following expression grammar and it is fed to a YACC tool. Then which of the following is true about the action of YACC tool for the given grammar [precedence and associativities of operators are not known to YACC tool].

① It detects recursion and eliminates recursion.

② It detects RLR conflict and resolves the conflict by giving priority for first reduce action over second reduce action.

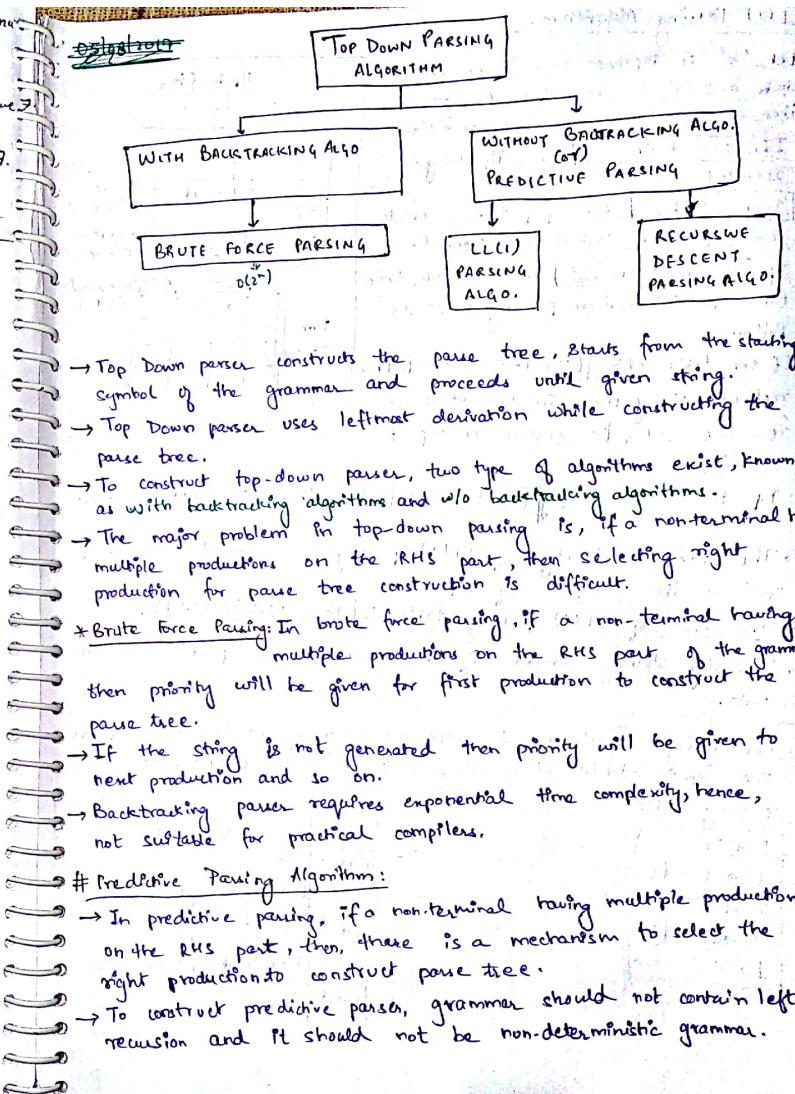
③ It detects SLR conflicts and resolves the conflict by giving priority for shift action over reduce action.

④ It detects SLR conflict and resolves the conflict by giving priority for reduce action over shift action.

$$\begin{array}{l} E \rightarrow E + F \\ E \rightarrow E * C \\ E \rightarrow id \end{array}$$

Scanned by CamScanner

- ② If the conflicts are resolved in the above manner what precedence and associativity rules parser will realize? What is the value of the expression "3x2+1"?
- ③ Both operators are equal precedence, left associative and expression value 7.
- ④ Both operators equal precedence, right associative, expression value 9.
- ⑤ " $*$ " is higher precedence than "+", both operators left associative, expression value 7.
- ⑥ "+" is higher precedence than " $*$ ", both are left associative, expression value 9.



### #LL(1) Parsing Algorithm:

→ Let "x" is topmost symbol on the stack and "a" is the lookahead symbol, then parser takes decisions as follows:

- ① If  $[x=a \neq \$]$  [Accept], then input string is accepted.
- ②  $x=a \neq \$$  [Pop x], then pop "x" from stack and increment lookahead symbol.
- ③ If  $x$  is nonterminal in the stack, then take decision from parsing table as follows:
  - If the table entry  $[x, a] = X \rightarrow uvw$ , then replace  $X$  by  $uvw$  in the stack in reverse order  $E^*$  appears on top of stack].
  - ④ If the table entry  $[x, a] = \text{blank}$ , then there is a syntax error.

→ The time complexity of LL(1) parsing algorithm is  $O(n)$ , where "n" is the length of input.

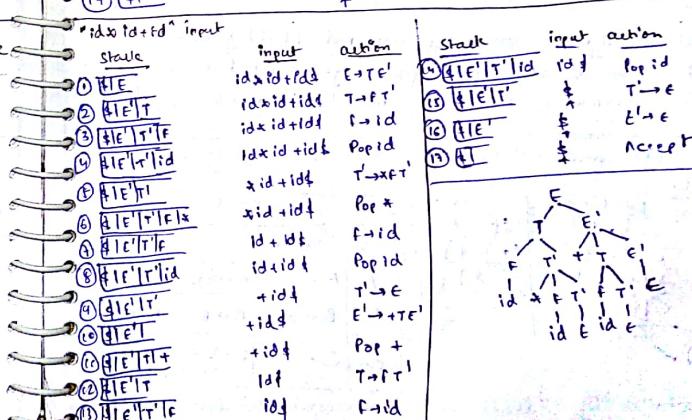
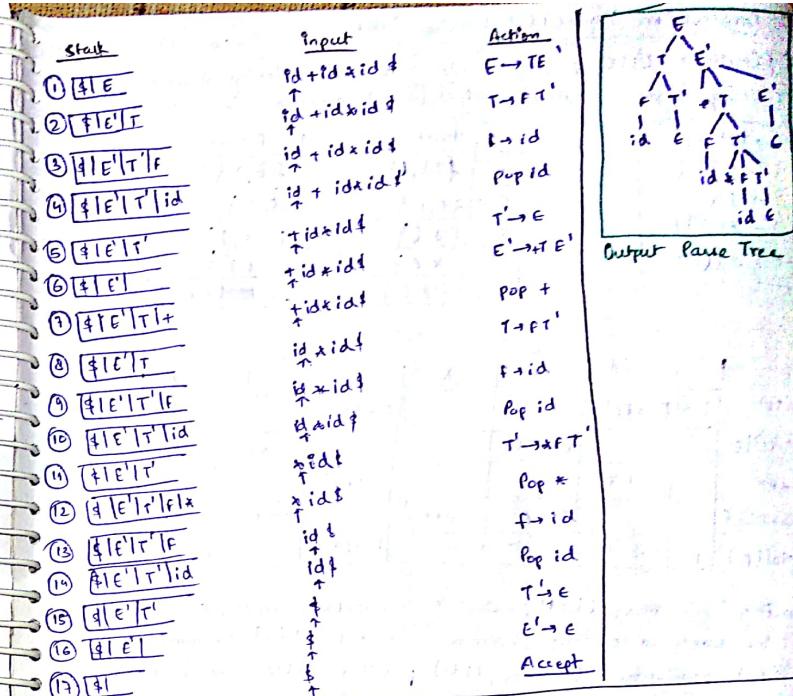
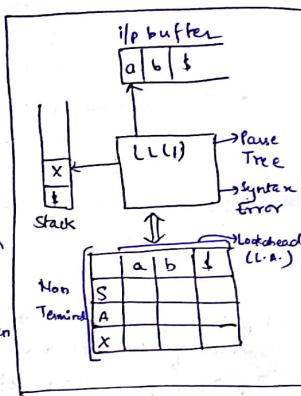
→ The size of LL(1) parsing table is  $(N \cdot d \cdot N.T.) \times (T+1)$ .

→ Initially starting symbol of the grammar is pushed onto the stack.

Q. How many total no. of steps are taken by LL(1) parser to parse the input "id + id \* id" by using following grammar and LL(1) parsing table.

$$\begin{array}{l} E \rightarrow TE' \\ E' \rightarrow +TE'E \\ T \rightarrow FT' \\ F \rightarrow id \\ T' \rightarrow FT' \\ F \rightarrow id \end{array}$$

|    | id                     | +                    | x                  | \$ |
|----|------------------------|----------------------|--------------------|----|
| E  | $E \rightarrow TE'$    |                      |                    |    |
| E' | $E' \rightarrow +TE'E$ |                      |                    |    |
| T  | $T \rightarrow FT'$    |                      |                    |    |
| T' | $T' \rightarrow E$     | $T' \rightarrow FT'$ | $T' \rightarrow E$ |    |
| F  | $f \rightarrow id$     |                      |                    |    |



## # Construction of LL(1) Parsing Table:

- Q1. Construct LL(1) parsing table for the following grammar.  
2. Verify given grammar is LL(1) grammar or not.

$E \rightarrow TE'$   
 $E' \rightarrow +TE' | G$   
 $T \rightarrow FT'$   
 $T \rightarrow *FT' | E'$   
 $F \rightarrow id | (E)$

|      | first   | follow                   |
|------|---------|--------------------------|
| $E$  | {id, (} | {+, \$)}                 |
| $E'$ | {+, E}  | {+, \$)}                 |
| $T$  | {id, (} | {+, \$, )}               |
| $T'$ | {x, E}  | {+, t, )}                |
| $F$  | {id, (} | {x, <del>+, t, )</del> } |

|                          | id   | +                   | *                    | (                    | )                  | \$                 |
|--------------------------|------|---------------------|----------------------|----------------------|--------------------|--------------------|
| $E \rightarrow TE'$      | $E$  | $E \rightarrow TE'$ |                      | $E \rightarrow TE'$  |                    |                    |
| $E' \rightarrow TE'E'$   | $E'$ |                     | $E' \rightarrow TE'$ |                      | $E' \rightarrow E$ | $E' \rightarrow E$ |
| $T \rightarrow FT'$      | $T$  | $T \rightarrow FT'$ |                      | $T \rightarrow FT'$  |                    |                    |
| $T' \rightarrow *FT'(t)$ | $T'$ |                     | $T \rightarrow E$    | $T' \rightarrow FT'$ | $T' \rightarrow E$ | $T' \rightarrow E$ |
| $F \rightarrow id(E)$    | $F$  | $F \rightarrow id$  |                      | $F \rightarrow (E)$  |                    |                    |

- Any grammar, LL(1) parsing table contains multiple productions in the same box, that grammar is not LL(1) grammar.
- All ambiguous grammars, LL(1) parsing table contains multiple productions.
- Hence, all ambiguous grammars are not LL(1) grammars.
- All, LL(1) grammars are unambiguous grammars, but all unambiguous grammars need not be LL(1) grammars.

- Q2. Construct LL(1) parsing table and also verify given grammar is LL(1) or not.

$S \rightarrow aABC$   
 $A \rightarrow a1bb$   
 $B \rightarrow a1tE$   
 $C \rightarrow b1tE$

|     | first  | follow     |
|-----|--------|------------|
| $S$ | {a}    | {1, \$}    |
| $A$ | {a, b} | {a, b, \$} |
| $B$ | {a, t} | {b, \$}    |
| $C$ | {b, t} | {1, \$}    |

LL(1) ✓

|     | a                    | b                  | t                  |
|-----|----------------------|--------------------|--------------------|
| $S$ | $S \rightarrow aABC$ |                    |                    |
| $A$ | $A \rightarrow a$    | $A \rightarrow bb$ |                    |
| $B$ | $B \rightarrow a$    | $B \rightarrow tE$ | $B \rightarrow tE$ |
| $C$ | $C \rightarrow b$    | $C \rightarrow tE$ | $C \rightarrow tE$ |

②  $S \rightarrow aAbB | bAaB | tC$   
 $A \rightarrow S$   
 $B \rightarrow S$

|     | first     | follow      |
|-----|-----------|-------------|
| $S$ | {a, b, t} | {t, b, a, } |
| $A$ | {a, b, t} | {b, a, }    |
| $B$ | {a, b, t} | {t, b, a, } |

Not LL(1)

|     | a                    | b                    | \$                 |
|-----|----------------------|----------------------|--------------------|
| $S$ | $S \rightarrow aAbB$ | $S \rightarrow bAaB$ | $S \rightarrow tC$ |
| $A$ | $A \rightarrow S$    | $A \rightarrow S$    |                    |
| $B$ | $B \rightarrow S$    | $B \rightarrow S$    |                    |

③  $S \rightarrow PEts's'a$   
 $S' \rightarrow es'tE$   
 $E \rightarrow b$

|      | first     | follow  |
|------|-----------|---------|
| $S$  | {t, a, t} | {es, t} |
| $S'$ | {e, t}    | {t, e}  |
| $E$  | {b}       | {t}     |

|      | i                   | t                   | e                  | a                 | b                 | \$                |
|------|---------------------|---------------------|--------------------|-------------------|-------------------|-------------------|
| $S$  | $S \rightarrow iet$ |                     |                    | $s \rightarrow a$ |                   | $d \rightarrow c$ |
| $S'$ | $S' \rightarrow i$  | $S' \rightarrow es$ | $S' \rightarrow e$ |                   |                   |                   |
| $E$  |                     |                     |                    |                   | $E \rightarrow b$ |                   |

④  $S \rightarrow AaAb | BbBa$  LL(1) ✓

|     | a      | b      |
|-----|--------|--------|
| $S$ | {a, b} | {t, }  |
| $A$ | {b}    | {a, t} |
| $B$ | {t}    | {a, b} |

|     | a                    | b                    | \$ |
|-----|----------------------|----------------------|----|
| $S$ | $S \rightarrow aAbB$ | $S \rightarrow bBba$ |    |
| $A$ | $A \rightarrow a$    | $A \rightarrow a$    |    |
| $B$ | $B \rightarrow b$    | $B \rightarrow b$    |    |

## # LL(1) Grammar Detection:

- ① A single production grammar is always LL(1) grammar.
- ② Any grammar is of the form  $A \rightarrow a_1a_2 \dots a_n$ , then if  $first(a_1), first(a_2), \dots$  and so on  $first(a_n)$  are pairwise disjoint, then the grammar is LL(1), otherwise not LL(1).
- ③ Any grammar is of the form  $A \rightarrow \alpha | \epsilon$ , then  $first(\alpha) \cap follow(A)$  equal to  $\emptyset$ , then it is LL(1).  
 $first(\alpha) \cap follow(A) = \emptyset$
- ④ Left recursive grammars are not LL(1), but elimination of left recursion may result LL(1) grammars.
- ⑤ Non-Deterministic grammars are not LL(1) but left factoring of ND grammar may result into LL(1) grammar.

Q: Which of the following grammars are LL(1).

- ①  $S \rightarrow aSb \mid bSa \mid c$
- ④  $S \rightarrow aS^k t$
- ②  $S \rightarrow aSb \mid bSa \mid t \mid X$
- ⑤  $S \rightarrow Sa \mid bSb \mid X$
- ③  $S \rightarrow aS \mid bSb \mid X$

$$\begin{array}{c} S \xrightarrow{*} a \\ \downarrow \quad b \\ S \xrightarrow{*} b \\ S \xrightarrow{*} a \end{array} \quad ] \text{LL}(1)$$

\*Non-deterministic grammar: If a grammar having multiple productions on the RHS pair where each production having some common prefix, that grammar is non-deterministic grammar.

E.g. Q:  $S \rightarrow aeb$

$$\begin{array}{l} S \xrightarrow{*} a \\ S \xrightarrow{*} ab \end{array}$$

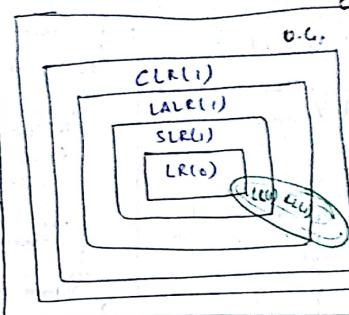
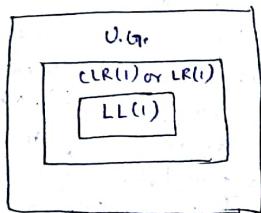
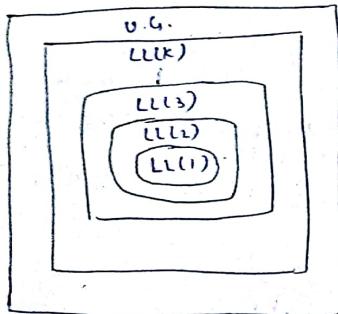
$$\begin{array}{l} S \xrightarrow{*} aetsletsesla \\ S \xrightarrow{*} aets'la \\ S \xrightarrow{*} eal \\ E \xrightarrow{*} b \end{array}$$

# Left factoring  
# Eliminating left factoring  
# does not remove ambiguity

Q: Which of the following is sufficient to convert an arbitrary CFG into LL(1) grammar.

- ① Elimination of left recursion alone.
- ② Factoring the grammar alone.
- ③ Both (a) and (b).
- ④ None of these.

NOTE: It is undecidable to convert every CFG into LL(1) grammar.



Q: Ambiguous.

L  $\rightarrow$  left to right scanning of input.  
L  $\rightarrow$  leftmost derivation  
(k)  $\rightarrow$  Lookahead of length k

LR(1) = LR(k)

Q: Consider the following grammars: Given grammar is:

$S \rightarrow aSb \mid bSa$ .

① LL(1) and LR(1)

② LR(1) but not LL(1)

③ Neither LL(1) nor LR(1)

④ LL(1) but not LR(1)

Scanned by CamScanner

## # RECURSIVE DESCENT PARSING:

$E \rightarrow \text{num } T$   
 $T \rightarrow * \text{num } T \mid \epsilon$

|                                |                                                                                                                                                                                                         |
|--------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <pre>Main() {     E(); }</pre> | <pre>Procedure E() {     if (lookahead == num)         {Match();          T();          }     else         error();     if (lookahead == *)         print("Success");     else         error(); }</pre> |
|--------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|

|                                                                                                                                                                                                                                              |
|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <pre>Procedure T() {     if (lookahead == *)         {Match();          if (lookahead == num)              {Match();               T();               }          else              error();          }     else         return null; }</pre> |
|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|

Match()

```
{lookahead = nextToken;
}
error()
{print("syntax error");
}
```

- The power of recursive descent parser is less compared to LL(1) parser.
- Recursive Descent parser not using predictive parsing tables. Hence, for large class of grammars, parser may fall into back tracking.
- Hence, LL(1) parser is used in top-down parsing to construct without backtracking parser.

## # SEMANTIC ANALYSIS PHASE:

→ The following are some of the semantic errors, parser cannot detect:

① Using a variable without declaration.

② Declaration of same variable multiple times in the same scope.

③ Expression statements which are not type compatible.

④ Scope violation statements.

⑤ Mismatch of formal and actual parameters.

⑥ Type mismatches in formal and actual parameters.

→ To construct semantic analysis phase, CGs can be used. Hence, semantic analysis phase is also called as context sensitive analysis phase.

→ Content sensitive grammars are difficult to implement. Hence, another form of CGs, known as attribute grammars are used to design semantic analysis phase.

→ Attribute grammar is a CFG where each grammar symbol is associated with a set of attribute values, where attribute can be a type information or scope information of a variable.

→ To compute attribute information of grammar symbols, semantic rules are attached to grammar productions.

## # Syntax Directed Translation (SDT):

→ SDT is a mechanism where each CFG production is associated with set of semantic rules.

→ Semantic rules are nothing but rules to compute attribute information in the annotated parse tree.

\* Annotated Parse Tree: It is a parse tree, where each grammar symbol is decorated with set of attribute information.

→ To construct semantic analysis phase and intermediate code generation phase, SDT is constructed for the requirement.

→ Hence, semantic errors are detected, complete symbol is constructed and intermediate code is generated by constructing SDTs.

### #Steps to construct SDT:

- ① Construct the parse tree.
  - ② Construct annotated parse tree.
  - ③ Compute attribute information in the annotated parse tree.
  - ④ Generalized rules of attribute combination in the annotated parse tree, attached to grammar production as semantic rules.

Q Construct the SDT, to detect semantic error in the expression statement of a language having int and boolean datatypes. Where type is attribute that computes type information at every grammar symbol. Then write semantic rules by using following grammar productions:

Diagram illustrating the derivation of E-type from E<sub>i</sub> type rules:

```

graph TD
 E[E] -- "E → Ei + Ej" --> Ei[Ei]
 E -- "E → Ei * Ej" --> Ej[Ej]
 E -- "E → (Ei)" --> Ei_in_parentheses["(Ei)"]
 E -- "E → num" --> num["num"]
 E -- "E → true" --> true["true"]
 E -- "E → false" --> false["false"]

 Ei -- "if (Ei.type == Ej.type) Ei.type = int" --> Ei_int["Ei.type = int"]
 Ei -- "else \"semantic error\";" --> semantic_error["\"semantic error\""]

 Ej -- "if (Ej.type == Ei.type) Ej.type = bool" --> Ej_bool["Ej.type = bool"]
 Ej -- "else \"semantic error\";" --> semantic_error

 Ei_in_parentheses -- "if (Ei.type == Ei.type) Ei.type = bool" --> Ei_in_parentheses_bool["Ei.type = bool"]
 Ei_in_parentheses -- "else \"semantic error\";" --> semantic_error

 num -- "E.type = Ei.type" --> num_Ei_type["E.type = Ei.type"]
 true -- "E.type = num.type" --> true_num_type["E.type = num.type"]
 false -- "E.type = bool" --> false_bool["E.type = bool"]

 Ei_int -- "int E.type" --> Ei_int_int["E.type = int"]
 Ej_bool -- "int E.type" --> Ej_bool_int["E.type = int"]
 Ei_in_parentheses_bool -- "int E.type" --> Ei_in_parentheses_int["E.type = int"]
 num_Ei_type -- "int E.type" --> num_Ei_type_int["E.type = int"]
 true_num_type -- "int E.type" --> true_num_type_int["E.type = int"]
 false_bool -- "int E.type" --> false_bool_int["E.type = int"]

 Ei_int_int -- "int E.type" --> Ei_int_int_int["E.type = int"]
 Ej_bool_int -- "int E.type" --> Ej_bool_int_int["E.type = int"]
 Ei_in_parentheses_int -- "int E.type" --> Ei_in_parentheses_int_int["E.type = int"]
 num_Ei_type_int -- "int E.type" --> num_Ei_type_int_int["E.type = int"]
 true_num_type_int -- "int E.type" --> true_num_type_int_int["E.type = int"]
 false_bool_int -- "int E.type" --> false_bool_int_int["E.type = int"]

 Ei_int_int_int -- "int E.type" --> Ei_int_int_int_int["E.type = int"]
 Ej_bool_int_int -- "int E.type" --> Ej_bool_int_int_int["E.type = int"]
 Ei_in_parentheses_int_int -- "int E.type" --> Ei_in_parentheses_int_int_int["E.type = int"]
 num_Ei_type_int_int -- "int E.type" --> num_Ei_type_int_int_int["E.type = int"]
 true_num_type_int_int -- "int E.type" --> true_num_type_int_int_int["E.type = int"]
 false_bool_int_int -- "int E.type" --> false_bool_int_int_int["E.type = int"]

```

→ SDTs are carried out along with parser.

- Whenever parser is performing parsing by using grammar productions, the semantic rules associated with grammar productions also executed, hence, verifies semantic features of the language.
- SDIs can be given to Top-down or bottom-up parser.

→ SDTs can be given to Top-down or bottom-up parser.

LSDT for checking expressions not type compatible: 06 or 11

$E \rightarrow id \quad \{E.type = id.type\}$

Q. Construct the SBT that would calculate total no. of reductions taken by a S/R parser, where "red" is attribute that gives no. of reductions at every place and the root value "E.red" would be reductions value.

give total no. of reductions value.  
Write semantic rules by using following grammar productions.

$E \rightarrow E + T \quad \{ F.\text{real} = (E.\text{real} + T.\text{real}) + 1 \}$   
 $E \rightarrow T \quad \{ E = T.\text{real} + 1 \}$   
 $T \rightarrow T * F \quad \{ T.\text{real} = (F.\text{real} + T.\text{real}) + 1 \}$   
 $T \rightarrow F \quad \{ T.\text{real} = F.\text{real} + 1 \}$   
 $F.\text{real} \neq F.\text{real} + 1$

Q Construct the SDT that would compute total height of the parse tree, where height is attribute and the root left value E.height would give total height of the parse tree. Write semantic rules for the following grammar productions: if ( $E_1$ , height), T, height) then  $E_1 \leftarrow E_1 . ht + 1$

$E \rightarrow [ + T ] \quad \{ E.height = (E.height + T.height) + 1 \}$   
 $E \rightarrow T \quad \{ E.height = T.height + 1 \}$   
 $T \rightarrow T * F \quad \{ T.height = (T.height, F.height) + 1 \}$   
 $T \rightarrow F \quad \{ T.height = F.height + 1 \}$   
 $F \rightarrow id \quad \{ F.height = 1 \}$

Q. Construct the SDT that would count total no. of 1's present in the given binary string, where count is attribute and S. count given total no. of 1's value. Write semantic rules for the following grammar productions.

```

S → L { S.Count = L.Count }

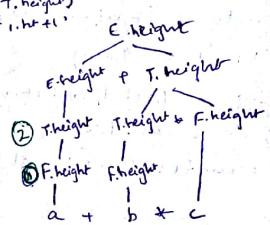
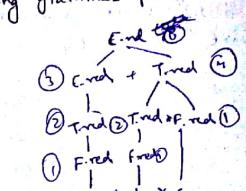
L → LB { L.Count = L.Count + B.Count }

L → B { L.Count = B.Count }

B → 1 { B.Count = 1 }

B → 0 { B.Count = 0 }

```



Q. Construct the SDT that would give total no. of balanced parenthesis information, where "count" is attribute and the root value "S.count" would give the total no. of balanced parenthesis information.

Write semantic rules for the following grammar productions.

$$S \rightarrow S \{ S.\text{count} = S_1.\text{count} + 1 \}$$

$$S \rightarrow \epsilon \{ S.\text{count} = 0 \}$$



GATE

Q. Consider the following SDT and compute root value "E.val" for the expression  $2\#3 \& 5\#6 \& 4$ .

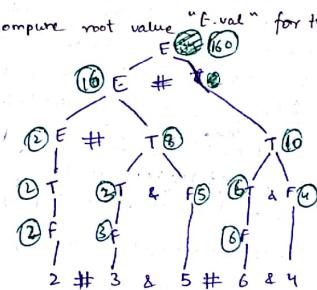
$$E \rightarrow E_1 \# T \{ E.\text{val} = E_1.\text{val} + T.\text{val} \}$$

$$E \rightarrow T \{ E.\text{val} = T.\text{val} \}$$

$$T \rightarrow T_1 \& F \{ T.\text{val} = T_1.\text{val} + F.\text{val} \}$$

$$T \rightarrow F \{ T.\text{val} = F.\text{val} \}$$

$$F \rightarrow \text{num} \{ F.\text{val} = \text{num}.\text{val} \}$$



Q.  $F \rightarrow L \{ F.v = L.v \}$

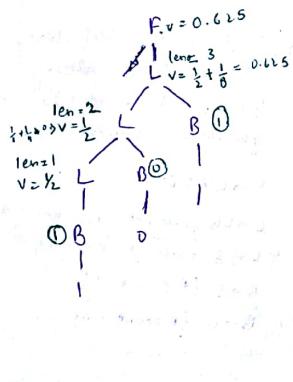
$$L \rightarrow L_1 B \{ L.\text{len} = L_1.\text{len} + 1 \}$$

$$L.v = L_1.v + 2^{-L.\text{len}} * B.v$$

$$L \rightarrow B \{ L.\text{len}=1 \}$$

$$B \rightarrow D \{ B.v = D \}$$

$$B \rightarrow I \{ B.v=1 \}$$



Q. Consider the following SDT:

$$S \rightarrow x W \{ \text{print}(1) \}$$

$$S \rightarrow y \{ \text{print}(2) \}$$

$$W \rightarrow z \{ \text{print}(3) \}$$

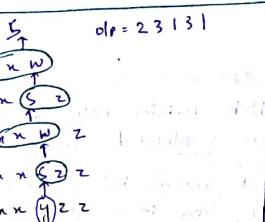
① This SDT is carried out along with SLR parser, then what o/p it will produce for the input "xxxyyz".

② If this SDT is carried out along with LL(1) parser, then what o/p it will produce for the input "xxxyyz".

NOTE

- If the SDT is carried out along with bottom up parser corresponding to every reduce action, the semantic rule associated with the production is executed.
- If the SDT is carried out along with a top down parser, then semantic rules are executed while traversing the parse tree depth first search (left to right manner), in which whenever a non-terminal visited 2 times, the semantic rule corresponding to that non-terminal production is executed.

$\text{o/p} = 23131$



NOTE

If the SDT is carried out along top down parser or bottom up parser, the output is same for the given same input.

Q.  $S \rightarrow aA \{ \text{print}(1) \}$

$S \rightarrow a \{ \text{print}(2) \}$

$A \rightarrow bB \{ \text{print}(3) \}$

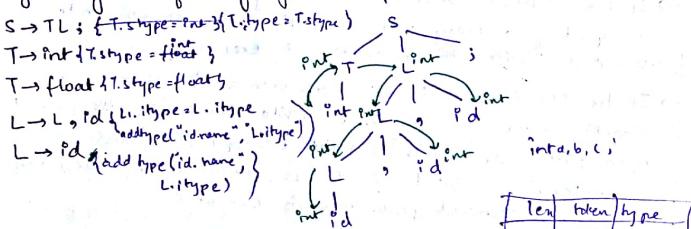
"aab"  $\rightarrow$  o/p?



# Synthesized attribute: If the attribute value at a node is computed from its children, then it is known as synthesized attribute.

# Inherited attribute: If the attributed value at a node is computed either from parent or from left siblings, then it is known as inherited attribute.

Q. Construct the SDT to fill type information in the symbol table by using the following grammar productions.

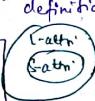


**NOTE**  
Any syntax directed definition which contains only synthesized attributes, then it is called as s-attributed definition.

Any syntax directed definition that contains both synthesized attributes and inherited attributes, then it is called as L-attributed definition.

All s-attributed definitions are L-attributed definitions, but all L-attributed definitions need not be s-attributed definitions.

Grammar productions:

$$\begin{aligned} S &\rightarrow 2AC \quad \{ x = A.x \} \quad I \\ S &\rightarrow 3ABMC \quad \{ M.x = Ax + B.x \} \quad I \\ C &\rightarrow Y \quad \{ C.x = x \} \quad S \\ M &\rightarrow E \quad \{ M.x = 0 \} \\ B &\rightarrow E \quad \{ B.x = E \} \\ A &\rightarrow E \quad \{ A.x = E \} \end{aligned}$$


→ There are two types of formalisms exist to construct semantic analysis phase and intermediate code generation phase. They are:

① Syntax Directed Definition (SDD)

② Syntax Directed Translation Scheme (Translation Scheme)

→ In SDD, all the semantic rules corresponding to synthesized attributes and inherited attributes are placed at right most end of grammar production.

→ In SDT, semantic rules may not be placed in proper places, hence attribute values may not be available in the attribute computation time.

→ To avoid this drawback, translation schemes can be constructed.

→ In translation scheme, all the semantic rules corresponding to synthesized attributes and inherited attributes are placed in proper places.

→ Hence, every attribute value is available in the attribute completion-time computation time.

→ In translation scheme, all the semantic rules corresponding to synthesized attribute are placed at right most end of grammar productions.

→ In translation scheme, all the semantic rules corresponding to inherited attributes of a non-terminal is placed before that non-terminal and after the depending variable.

→ All SDTs having only synthesized attributes are known as Post fix SBT, because all semantic rules are placed at right most end.

**NOTE**

→ Translation scheme is a SDT, in which semantic rules may be embedded within grammar production symbols of RHS part of the production.

Q. Convert the following SDD into SDT (translation scheme).

Grammar productions:

$$\begin{aligned} S &\rightarrow TL; \quad \{ L.iType = T.iType \} \\ T &\rightarrow \text{int} \quad \{ T.type = \text{int} \} \\ T &\rightarrow \text{float} \quad \{ T.type = \text{float} \} \\ L &\rightarrow L, Pd \quad \{ L.iType = L.iType \} \\ L &\rightarrow Pd \quad \{ \text{addtype}(\text{id.name"}, L.iType) \} \\ L &\rightarrow Pd \quad \{ \text{addtype}(\text{id.name"}, L.iType) \} \end{aligned}$$

→ L-id [addtype ("id.name", L.iType)]

SDT:

$$S \rightarrow T \{ L.i.type = T.i.type \} L ;$$

$$T \rightarrow \text{int } \{ T.i.type = \text{Int} \}$$

$$T \rightarrow \text{float } \{ T.i.type = \text{Float} \}$$

$$L \rightarrow L.i.type = L.i.type \{ L.i.type = \text{id} \{ \text{addtype} \{ "id.name", L.i.type \} \} \}$$

$$L \rightarrow \text{id } \{ \text{addtype} \{ "id.name", L.i.type \} \}$$

### # Translation scheme with top-down parsing:

- If the translation scheme is carried out along with a top-down parser, then semantic rules are executed by traversing the tree: BFS (left to right manner).
- Corresponding to translation scheme, an edge is provided for semantic rule also in the annotated parse tree.
- If the translation scheme is carried out with top-down parser then left recursion should be eliminated from it.

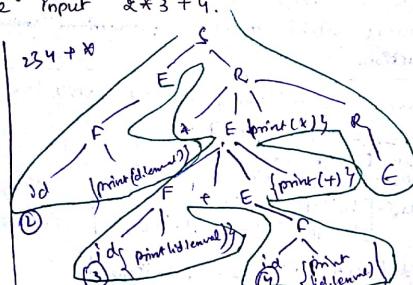
### Q. Eliminate left recursion from the following translation scheme.

$$\begin{array}{l} E \rightarrow E + T \{ \text{print}(+) \} \\ E \rightarrow T \{ \text{print}(+) \} E' \\ T \rightarrow T * F \{ \text{print}(*) \} \\ T \rightarrow F \\ F \rightarrow \text{id } \{ \text{print}(id. lexical) \} \end{array}$$

$$\begin{array}{l} E \rightarrow E + T \{ \text{print}(+) \} | T \\ E \rightarrow T \{ \text{print}(+) \} E' | E \\ T \rightarrow T * F \{ \text{print}(*) \} | T' \\ T \rightarrow F \\ F \rightarrow \text{id } \{ \text{print}(id. lexical) \} \end{array}$$

Q. Consider the following translation scheme and what output it will produce for the input  $*3+4$ .

$$\begin{array}{l} S \rightarrow ER \\ R \rightarrow xE \{ \text{print}(x) \} R \\ R \rightarrow \epsilon \\ E \rightarrow F + E \{ \text{print}(+) \} \\ E \rightarrow F \\ F \rightarrow (s) \\ F \rightarrow id \{ \text{print}(id. lexical) \} \end{array}$$



Q. S → TR

$$R \rightarrow + T \{ \text{print}(+) \} R$$

$$R \rightarrow E$$

$$T \rightarrow \text{num } \{ \text{print}(\text{num. lexical}) \}$$

95 + 2 +

### # Translation Scheme with bottom up parsing:

- If the translation scheme is carried out along with bottom up parser, handles cannot be detected because of semantic rules preceding within grammar symbols.
- Hence, translation scheme is converted as follows to carry out bottom up parsing:
- Translation scheme middle semantic rules are replaced by new non-terminals which produce " $\epsilon$ " to carry out bottom up parsing.

### Q. Convert the following translation scheme suitable for bottom up parser.

$$E \rightarrow E + T \{ \text{print}(+) \} | T$$

$$\boxed{\begin{array}{l} E \rightarrow TE' \\ E' \rightarrow + T \{ \text{print}(+) \} F' | \epsilon \\ T \rightarrow FT' \\ T' \rightarrow * F \{ \text{print}(*) \} T' | \epsilon \\ F \rightarrow PD \{ \text{print}(id. lexical) \} \end{array}}$$

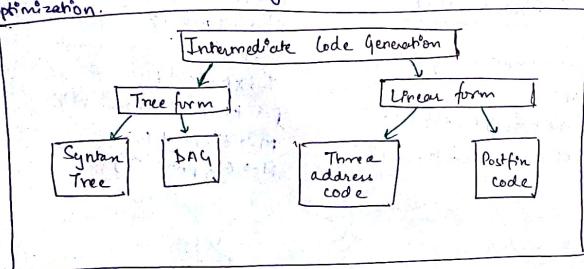
$$\begin{array}{l} E \rightarrow TE' \\ E' \rightarrow + T ME' | \epsilon \\ T \rightarrow FT' \\ T' \rightarrow * FNNT' | \epsilon \\ M \rightarrow PD \{ \text{print}(id. lexical) \} \\ N \rightarrow E \{ \text{print}(x) \} \end{array}$$

### NOTE

- SOT is used only to detect static semantic errors.
- Cannot be used for dynamic semantic errors checking.
- To identify dynamic semantic errors additional program code should be inserted.
- If all the type errors are detected by compiler at compile time only, then, that language is known as statically typed language.
- If the type errors of the program, even detected at runtime, then that language is known as dynamically typed language.
- A language in which no type checking is done, then that language is known as untyped language.  
E.g. machine language.

## # Intermediate Code Generation Phase

- Intermediate code is a type of code, which is easily produced from HLL and easily translated into LLL.
- The following are different forms of intermediate code.
- The advantage of generating intermediate code is to perform optimization.



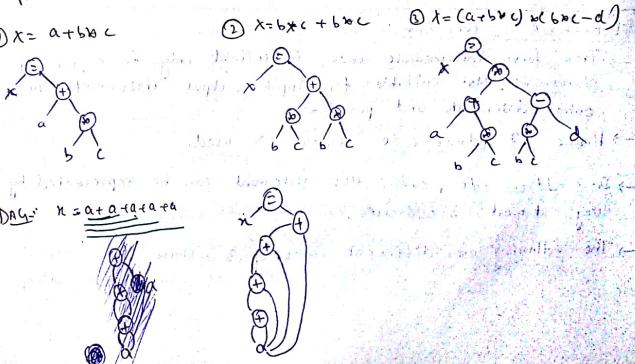
|                         | S.T. | DAG | TAC | Pcode |
|-------------------------|------|-----|-----|-------|
| ① Declaration statement | X    | X   | X   | X     |
| ② If, else, statement   | X    | X   | ✓   | X     |
| ③ Expression            | ✓    | ✓   | ✓   | ✓     |
| ④ Flow control          | X    | X   | ✓   | X     |
| ⑤ Function/procedures   | X    | X   | ✓   | X     |

### # Syntax Tree:

- Syntax tree is optimized form of the parse tree.
- Syntax tree is constructed for expression statements.
- Syntax tree represents order of evaluation of expressions.
- Syntax tree corresponding to the expression contains all operands at leaf nodes and all operators are at root positions.
- Syntax tree is optimized form of the parse tree.

### # Directed Acyclic Graph (DAG):

- DAG is a syntax tree in which common subexpressions are eliminated.
- For expression statement, if DAG is constructed, then automatically performs an optimization known as common subexpression elimination.



Q. Construct the SDT to construct syntax tree from the expression statements by using following grammar production, where "mknnode" is a function that creates root nodes.

Node is attribute that gives syntax tree at every place.

Write semantic rules for the given grammar productions.

$$S \rightarrow id = E \{ mknnode(id.name, "=", E.node) \}$$

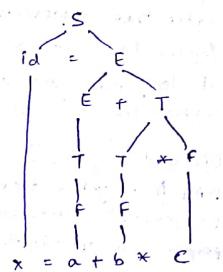
$$E \rightarrow E + T \{ E.node = mknnode(E.node, "+", T.node) \}$$

$$E \rightarrow P T \{ E.node = T.node \}$$

$$T \rightarrow T * F \{ T.node = mknnode(T.node, "*", F.node) \}$$

$$T \rightarrow F \{ T.node = F.node \}$$

$$F \rightarrow id \{ F.node = id.name \}$$



#### # Drawback of Tree form:

→ Tree form intermediate code is suitable only for expression statements. Not suitable for input output statements, flow control statements and procedures.

→ Hence, 3 address code format is used.

→ In 3 address code, every HLL statement can be represented by using at most 3 addresses.

→ The following are different forms of 3 address code:

$$\begin{array}{l} ① X = Y \\ ② X = op Y \\ ③ X = Y \end{array}$$

Expressions

$$\begin{array}{l} ④ X[i] = Y \\ X = Y[i] \end{array}$$

Arrays

⑤ goto L ] Unconditional Jump

⑥ if a > b goto L1 ] Conditional Jump  
goto L2

#### ⑦ Procedure / Function

p( P1, P2, ..., Pn )

Param P1  
Param P2  
:  
Param Pn  
Call name, #args

#### Three Address Code

# Three address code for expression statements:

$$\begin{array}{lll} ① X = a + b * c & ② X = (a * b) + (c * d) & ③ X = (a + b) + (c * (c - d)) \end{array}$$

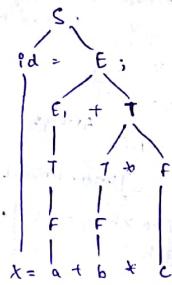
$$\begin{array}{lll} t_1 = b * c & t_1 = a * b & t_1 = a * b \\ t_2 = a + t_1 & t_2 = b * d & t_2 = c - d \\ x = t_2 & t_3 = a * b & t_3 = e + t_2 \\ & t_4 = t_1 + t_3 & t_4 = e + t_3 \\ & t_5 = t_1 + t_4 & x = t_5 \end{array}$$

Q. Construct the SDT to generate 3 address code for expression statements. Where "newtemp()" that generates 3 address code a new temporary variable on every function call.

gen() is a function, that produces 3 address code, where place is attribute that gives 3 address code at every place.

Write semantic rules by using the following grammar productions.

$E \rightarrow E + T$   $\left[ t = \text{newtemp}(); \text{gen}(t = E.\text{place} + T.\text{place}) \right]$   
 $E \rightarrow T$   $\left[ E.\text{place} = t \right]$   
 $T \rightarrow T * F$   $\left[ t = \text{newtemp}(); \text{gen}(t = T.\text{place} * F.\text{place}) \right]$   
 $T \rightarrow F$   $\left[ T.\text{place} = F.\text{place} \right]$   
 $F \rightarrow \text{id}$   $\left[ F.\text{place} = \text{id.name} \right]$



### # 3-Address code for arrays:

#### 1-D array

$$A[i] = \text{base} + (i - \text{low}) * w$$

#### 2-D array

$$A[i, j] = (i * n_2 + j) * w + \text{base} = (\text{low}_1 * n_2 + \text{low}_2) * w$$

#### n-D array

$$A[i_1, i_2, \dots, i_n] = (((i_1 * n_2 + i_2) * n_3 + i_3) \dots) * n_k + i_k)$$

$$+ \text{base} - ((((\text{low}_1 * n_2) + \text{low}_2) * n_3 + \text{low}_3) \dots) * n_k + \text{low}_k) * w$$

### Q. Construct the 3 address code for following expression:

$X = A[i, j]$ , where size of array is  $A[10][20]$ ,  
size of each word is 4 bytes  
and  $\text{low}_1 = \text{low}_2 = 1$ .

$$A[i, j] = i * 20 + j * 4 + \text{base} - (1 * 20 + 1) * 4$$

|                          |                |
|--------------------------|----------------|
| $t_1 = i * 20$           | $t_2 = A[t_1]$ |
| $t_2 = t_1 + j$          | $X = t_2$      |
| $t_3 = t_2 * 4$          |                |
| $t_4 = \text{base} - 84$ |                |
| $t_5 = t_3 + t_4$        |                |

### # Three AC for flow control statements:

$\text{Pf}(a > b)$ ,  $\left[ \begin{array}{l} t_1 = a + c \\ t_2 = b + c \\ \text{if } a > b \text{ goto L1} \\ \text{else } x = t_1 + t_2 \text{ goto LAST} \end{array} \right]$   
 $L1: t_1 = b + c$   
 $x = t_1$   
 $\text{LAST: } g$

$\text{Q. } \text{for } (i=1; i<10; i++)$   
 $i = y + a * b;$   
 $\{$   
 $i = 1;$

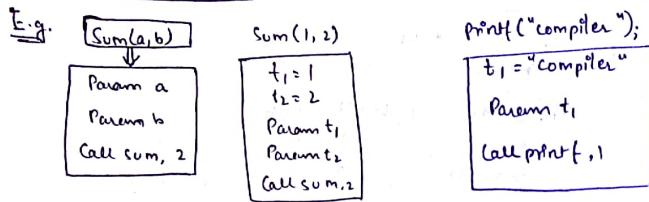
$L1: \text{if } i < 10 \text{ goto L2}$   
 $\text{else } x = a * b$   
 $i = i + 1$   
 $L2: i = y + t_1$   
 $x = t_2$

$L1: t_1 = a * b$   
 $i = i + 1$   
 $L2: i = t_3$   
 $t_3 = i + 1$   
 $i = t_3$   
 $\text{goto L0}$

### Q. How many temporary variables required.

$\text{for } (i=1; i<100; i++)$   
 $\{ x = (y + z) * (a + b * c);$   
 $i = 1;$   
 $L0: \text{if } i < 100 \text{ goto L1}$   
 $\text{else goto L2}$   
 $L1: t_1 = y + z$   
 $t_2 = b * c$   
 $t_3 = a + t_2$   
 $t_4 = t_1 * t_3$   
 $x = t_4$   
 $t_5 = i + 1, \text{ goto L0}$   
 $L2: \dots$

### # 3AC for functions:



```

if (a>b) {r1} ((c>d) and (e>f))
 {
 x=a+b;
 r2
 }
else
 P = Q + R;
 r3
 L1: if (a>b) goto L7
 L2: goto L3
 L3: if (c>d) goto L5
 L4: goto L10
 L5: if (e>f) goto L7
 L6: goto L10
 L7: t1 = a+b;
 L8: x = t1
 L9: goto L12
 L10: t1 = Q + R;
 L11: P += t1
 L12: r4

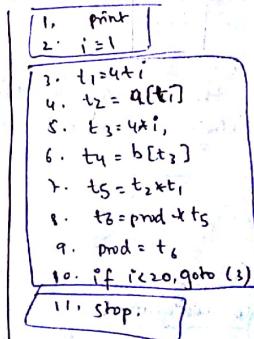
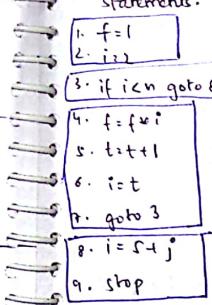
```

⑥ Back Patching: While generating 3 address code for flow control statements, initially code is generated and target labels information filled later, known as backpatching.

### # Basic Block Construction:

- Basic block is a sequence of 3 AC instructions which is having single entry and single exit property.
- Basic blocks are constructed by using leader statements.
- The following are leader statements for the given 3 address code
- ① First statement is always leader.
- ② The target of conditional or unconditional goto is a leader.
- ③ The statement immediately followed by conditional or unconditional goto is a leader.
- ④ One leader statement to until next leader statement, one basic block is constructed.
- Control flow graph is constructed, for all basic blocks which represents the flow of execution among the statements of 3 address code.

Q. Construct basic blocks for the following 3 address code statements.



- The generated 3 address code is stored in array with 4 fields known as quadruple.
- In quadruple representation space is allocated for temporary variables also in the result field.
- Hence, compiler may insert its value in the symbol table along with variables of the program.
- To avoid this drawback triples representation is used.
- In triples notation, expression value is stored in memory locations and accessing of it from memory locations is done whenever required.

→ Triple :

| op | opr1 | opr2 |
|----|------|------|
| *  | b    | c    |
| +  | a    | (10) |
| =  | x    | (14) |

→ Quadruple

| result         | op | opr1           | opr2           |
|----------------|----|----------------|----------------|
| t <sub>1</sub> | *  | b              | c              |
| t <sub>2</sub> | +  | a              | t <sub>1</sub> |
| x              | =  | t <sub>2</sub> | --             |

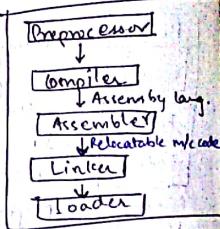
Q. Consider the following 3 address code and which of the following is static single assignment form of the given code?

$$\begin{aligned} p &= a - b \\ q &= p \times c \\ p &= u \times v \\ q &= p + q \end{aligned}$$

Static single assignment : In this, every expression is assigned to a new variable.

- ① P<sub>1</sub> = a - b      ② P<sub>3</sub> = a - b      ③ P<sub>1</sub> = a - b      ④ None  
 Q<sub>1</sub> = P<sub>1</sub> \* C      Q<sub>4</sub> = P<sub>3</sub> \* C      Q<sub>1</sub> = P<sub>3</sub> \* C  
 P<sub>1</sub> = U \* V      P<sub>4</sub> = U \* V      P<sub>3</sub> = U \* V  
 Q<sub>1</sub> = P<sub>1</sub> + Q<sub>4</sub>      Q<sub>5</sub> = P<sub>4</sub> + Q<sub>3</sub>      Q<sub>1</sub> = P<sub>4</sub> + Q<sub>3</sub>

- \* Interpreter : Interpreter is a language processor that takes HLL program and produces output of it by performing line by line execution.
- \* Preprocessor : is a translator that executes some of the HLL statements present in the program.  
The task done by preprocessor is file inclusion and macro evaluation.
- \* Assembler : is a program that translates assembly language into relocatable machine code.
- \* Relocatable machine code : is not executable code.  
After performing linking, then, the code is placed in absolute addresses in memory.
- \* Linker : is a program, that makes different modules of the program into single module.
- \* Loader : is a program, that loads the program into main memory from secondary memory.
- \* Pass : One complete scan of the source program is known as one pass.  
A phase can be part of the pass.



#### Chapter 2. 15. Visible Prefix:

| Stack | input  | action |
|-------|--------|--------|
| ① t   | a b \$ | S      |
| a     | b \$   | R      |
| A     | b \$   | S      |
| A b   | \$     | R      |
| A B   | \$     | R      |
| A B S | \$     | Accept |

→ Set of prefixes of right sentential form that appear on left part of the handle ; the viable prefix.

→ Viable prefixes are nothing but stack content of S/R parser.

# Runtime Environment:

|       |
|-------|
| Heap  |
| Stack |
| Data  |
| Code  |

→ Compiler uses 2 techniques while allocating m/m for generated code, i.e., static and dynamic allocation.

→ In static allocation strategy, compiler takes decision regarding runtime memory by looking at program text only.

→ By using static allocation strategy, recursive programs cannot be executed and so, dynamic data structures cannot be created.

→ Dynamic storage allocation: In this strategy, operating system allocates some memory to execute the program.

Compiler divides runtime memory into code area, data area, stack area, heap area.

Compiler allocates space for fixed code at code area.

The space for global variables is allocated at compile time in data area.

Whenever a function is called, activation record is pushed into the stack.

The space for local variables of a function are kept in activation record.

If the func<sup>n</sup> returns its value, then activation record is popped out from the stack.

→ If space is allocated in stack m/m, then, memory management is completely automated.

→ If we want to maintain any value throughout the program, that is not kept in stack space. Hence, space for that value is given in heap area.

→ Memory management is completely manual in heap area.

→ Additional programs like garbage collection is required to free heap memory.

#### # Practice:

T.O.C:

- DFA to language (20 questions)
- Minimization of DFA (15)
- Language to DFA (40)
- F.A. to reg. ex. (15)
- Reg. ex to F.A. (25)
- Lang. to reg. ex / Reg. ex to lang. (30)
- Reg. grammar to reg. ex. & reg. ex to reg. grammar (20)
- Reg. lang. detection (40)
- Ambiguity of grammar (20)
- Language to PDA & PPA to lang. (25)
- CFL detection (with reg. & DCFL) (30)
- T.M. to language (20)
- Recursive, R.P., not R.F. detection from T.M. (20)
- Undecidability Table

# Compiler: (10 to 20 questions)

- No. of tokens
- Lexical error detection
- Detection of the grammar (LR(0), SLR, CLR, LALR, LLL, operator precedence)
- SDF construction (including translation)
- SDF output file scheme
- Construction of DAG with no. of edges and nodes.

- 3 address code for expression statements with temporary variables
- Construction of basic blocks.