

## Operating System:

### Teaching Schedule:

#### I. Introduction and Background

#### II. Process Management

- CPU Scheduling
- Synchronization

- Concurrent Programming
- Deadlocks
- Threads

#### III. Memory Management

- RAM Chip Implementation

- Loading, Linking and Address Binding

#### Techniques

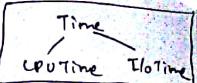
- Paging
- Multi level paging
- Inverted paging
- Segmentation
- Segmented paging
- Virtual Memory

#### IV. File Systems

### Textbooks:

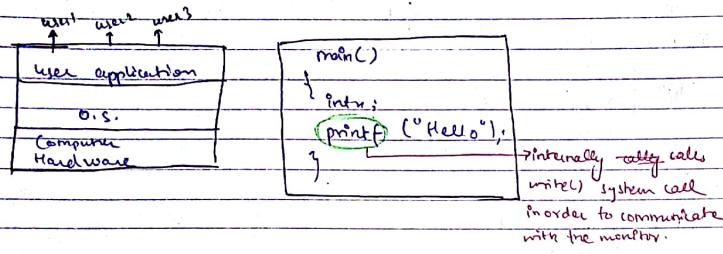
1. O.S. by Galvin
2. Modern O.S. by A.S. Tenenbaum
3. O.S. by W. Stallings

Faculty ⇒ Balakrishna



## # Introduction and Background:

→ Operating System is an interface between user and computer hardware.

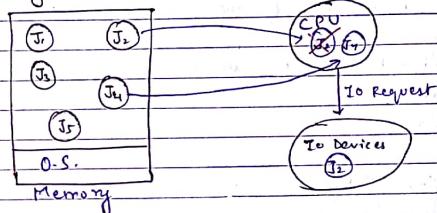


- If the job is completed completely, then only another job will be scheduled onto the CPU.
- Increased CPU utilization.
- Decreased throughput of the system.

\* Throughput: No. of jobs completed for unit time is known as throughput of the system.

E.g. IBM OS/2.

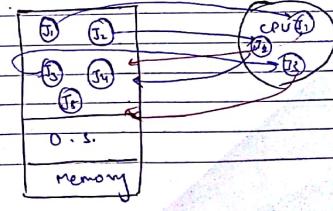
## (2) Multi Programming O.S. :



- If the job is leaving the CPU to perform I/O operation, then another job which is ready for execution will be scheduled on to the CPU.
- Increased CPU utilization.
- Increased throughput of the system.

E.g. Windows, UNIX, LINUX

## (3) Multitasking O.S. :



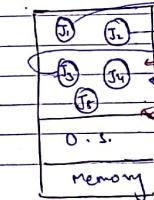
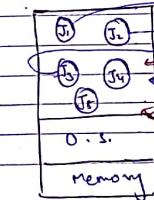
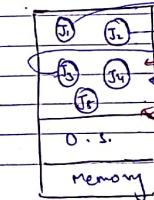
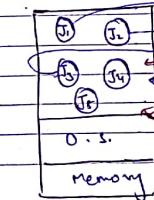
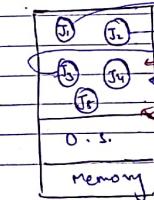
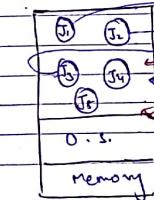
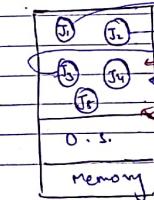
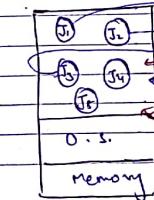
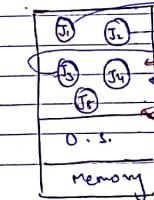
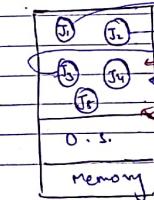
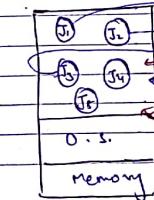
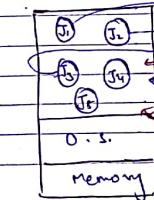
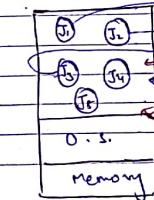
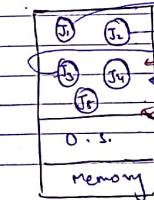
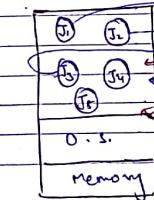
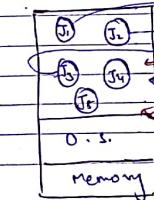
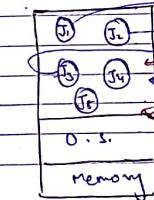
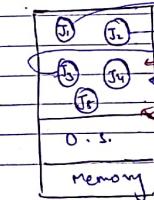
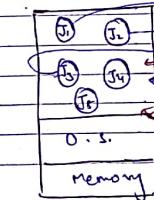
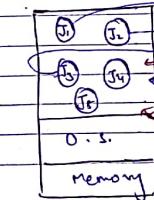
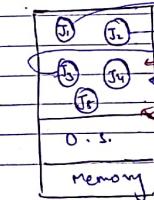
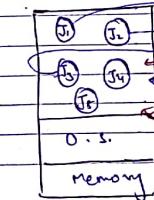
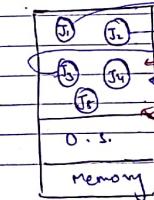
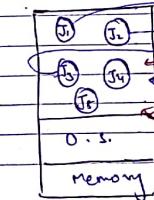
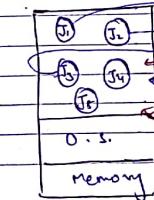
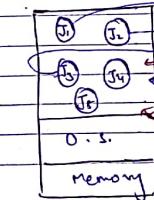
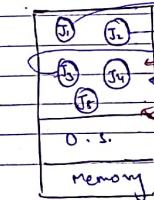
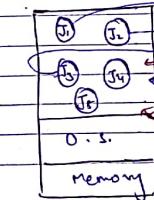
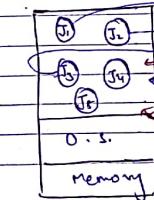
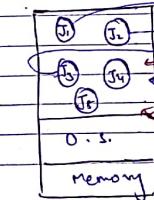
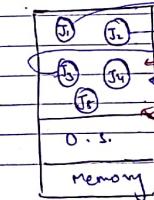
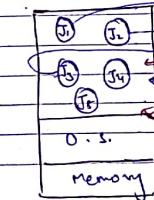
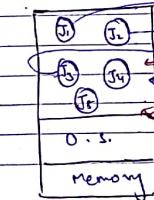
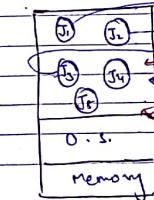
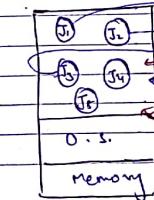
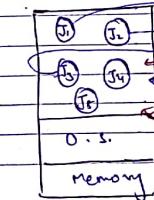
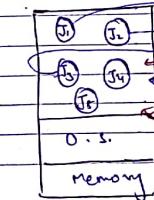
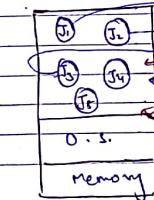
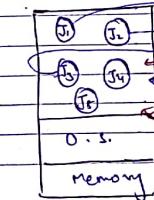
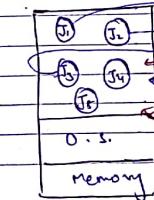
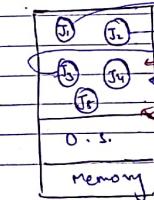
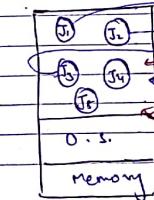
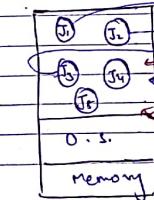
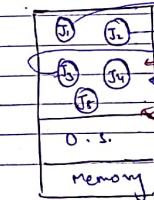
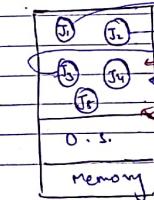
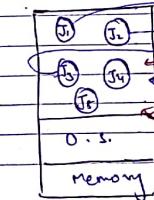
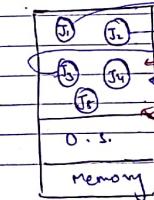
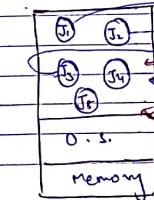
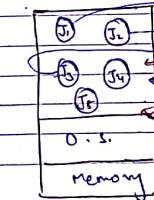
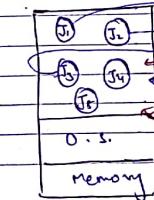
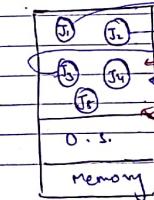
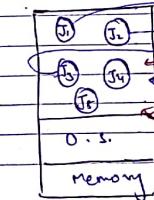
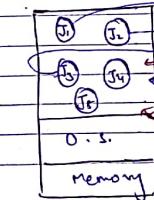
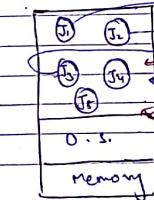
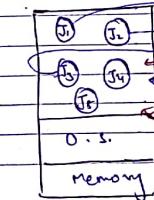
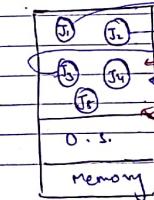
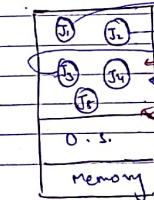
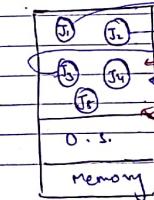
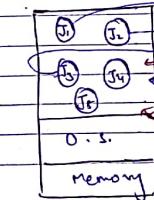
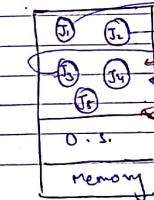
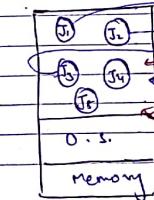
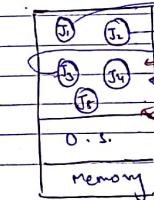
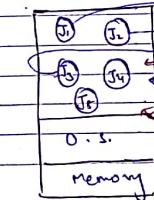
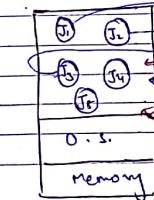
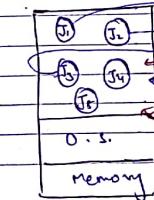
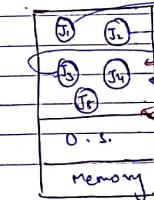
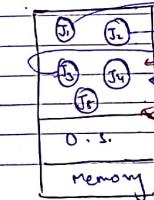
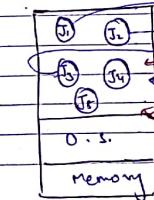
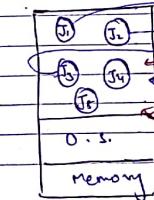
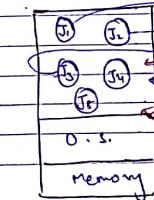
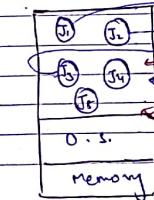
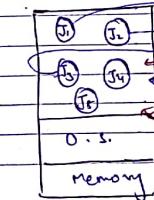
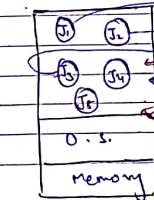
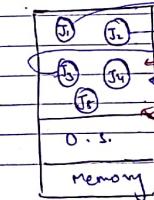
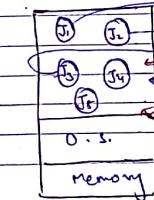
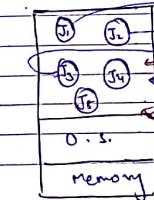
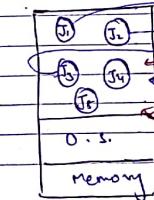
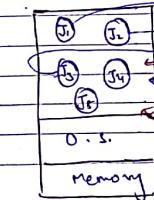
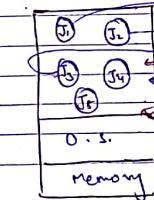
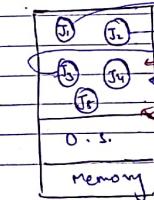
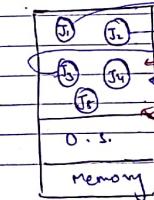
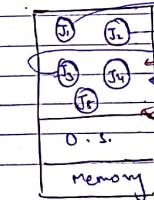
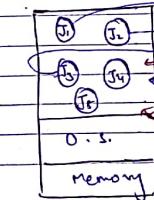
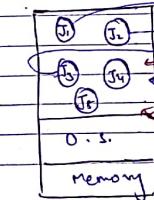
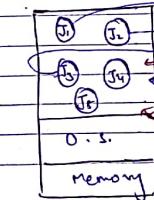
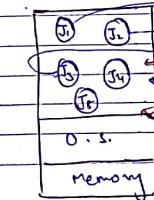
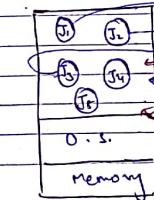
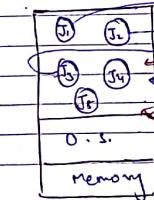
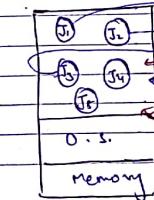
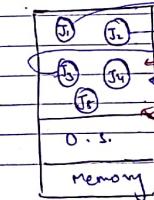
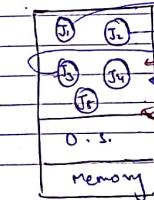
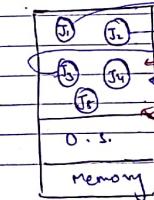
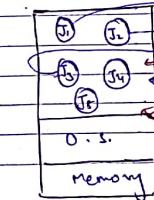
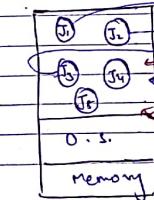
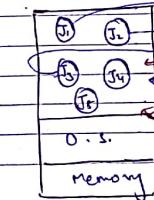
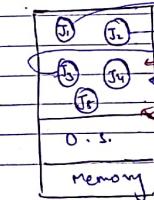
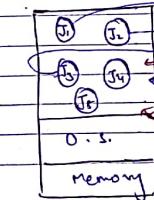
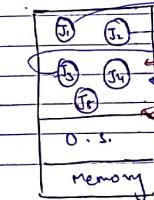
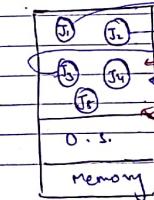
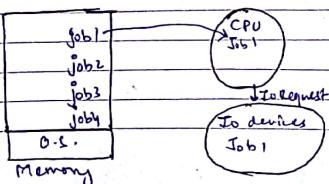
## \* Goals of O.S.:

→ The primary goal is convenience (Easy to use)

→ The secondary goal is efficiency.

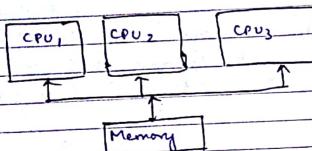
## \* Types of O.S.:

### (1) The Batch O.S.:



→ Multitasking is an extension of multiprogramming O.S.  
 → The jobs will be executed in the time sharing mode.

#### (4) Multiprocessor O.S.:



(i) Increased throughput of the system.

(ii) Reliability:

↳ Fault tolerant systems

(iii) Economical

E.g. UNIX.

#### (5) Real Time O.S.:

→ The systems which are strict deadly time bound.

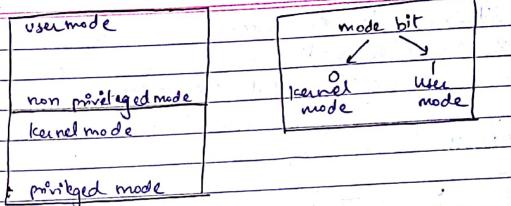
→ Categorised as: Hard RTOS and Soft RTOS

↳ E.g. Satellite systems,  
Missile system

↳ E.g. Banking sector

Eg. Vx Works, RTOS.

#### Dual mode Operation:



→ In the hardware level, instructions are executed in the 2 different modes:

- ① User mode / non-privileged mode
  - ② Kernel mode / privileged mode / System mode / Supervisory mode
- The dual mode operation is used in order to provide protection and security from "evil user".
- It is purely the decision of the O.S. in which particular mode, the instruction has to be executed.
- Generally, the privileged instructions are executed in the kernel mode and non-privileged instructions executed in the user mode.
- The mode bit is used to identify, in which particular mode, the current instruction is executing.
- In the boot time, system always starts in kernel mode.
- The O.S. always runs in kernel mode.

#### NOTE

→ Mode switching takes very less time compared to the process switching.

#### \* Privileged instructions:

- ① I/O operation
- ② Context switching
- ③ Disabling interrupts
- ④ Changing the memory map
- ⑤ Clearing the memory map.

⑥ Set the time of clock.

### \* Non Privileged Instructions:

- ① Reading the status of the processor.
- ② Reading the time of clock.
- ③ Sending the final print output to the printer.

### # Layered Approach:

Process Mgmt.	L <sub>1</sub>	→ The design and implementation of the O.S. will be done in multiple layers.
Memory Mgmt.	L <sub>2</sub>	
File Mgmt.	L <sub>3</sub>	
Device Mgmt.	L <sub>4</sub>	→ The main advantage of layered approach is modularity, abstraction and debugging.
Protection & Security	L <sub>5</sub>	O.S.

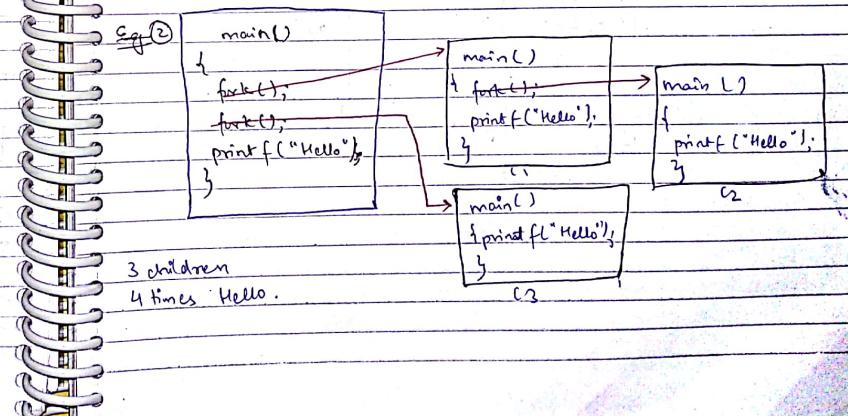
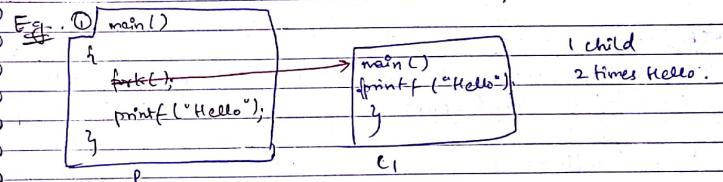
→ It means that if any specific layer is updated, then, it will not have any affect or impact on other layers.

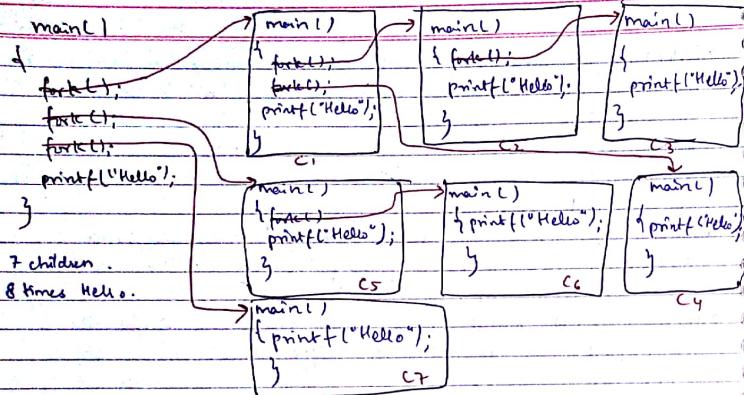
### # FORK() SYSTEM CALL IMPLEMENTATION

```
main()
{
    int pid;
    pid = fork();
    if (pid < 0)
        printf("child process creation failed.");
    else if (pid == 0)
        {
            printf("child process");
        }
    else
        {
            printf("parent process");
        }
}
```



- fork() is a system call used to create the child process.
- fork() returns negative value if the child process creation is unsuccessful.
- fork() returns value '0' to the newly created child process.
- fork() returns positive value to the parent process (i.e., process id of child process).
- When the child process is created by using fork() system call, the new memory location will be allocated to the child process.
- The child and parent process will have same virtual address but physical addresses will be different.





Program is passive & static.

## # PROCESS MANAGEMENT

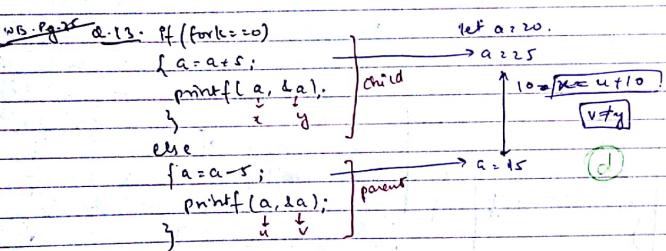
### \* Process Concepts:

Def: The program under execution is called process.

- ① It should reside in the main memory.
- ② It is occupied the CPU to execute the instructions.
- ③ Active and dynamic

→ Process will have various attributes.

- ① Process id
  - ② Process state
  - ③ Priority
  - ④ Program counter
  - ⑤ General Purpose Registers
  - ⑥ List of open files
  - ⑦ List of open devices
  - ⑧ Protection information
- Context  
Switched  
PCB



(i) Process id: It is the unique identification number which is assigned by the O.S. at the time of process creation.

(ii) Process State: contains current state information of a process where it is residing.

(iii) Priority: It is a parameter which is assigned by the O.S. at the time of process creation.

(iv) Program Counter: contains the address of the next instruction to be executed.

- All the attributes of the process is called as context of the process.
- The context of the process will be stored in the process PCB (Process Control Block).

#### \* PCB:

Pid	P-S
P.C.	Memory
G.R.	L.O.F
L.O.D	Anterium Info

- Every process will have its own PCB.
- PCBs of the processes will be stored in the main memory.
- PCBs of the processes will be implemented by using double linked list.

#### # States of a Process:

- (1) New
- (2) Ready
- (3) Run
- (4) Wait or Block
- (5) Termination or Completion
- (6) Suspend Ready
- (7) Suspend Block or Suspend wait

#### # Operations :

- (1) Creation
- (2) Scheduling
- (3) Dispatching
- (4) Execution
- (5) Killing or Termination
- (6) Suspend/Resuming
- (7) Resuming

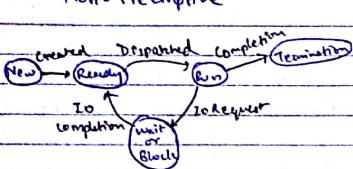
#### # Process State Diagram:

- Initially Process will be in the new state, it means the process is under creation or process is being created.
- In the Ready state, there will be multiple number of processes, and one of the process will be selected and that will be dispatched onto the running state.
- In the Running state, process has occupied the CPU, and executing the instructions of the process and performing CPU time.
- In the Running state, there will be only one process at any point of time.
- If the running process requires IO operation, it will be moved out to wait/blocked state.
- In the wait state also there will be multiple number of processes, it means multiple processes will perform IO operation simultaneously.
- When the process is in the ready, running and block states, it is residing in the main memory.
- If the resources are not sufficient to manage the processes in the ready state, then some of the processes will be suspended and they will be moved on to suspend ready state.
- When the process is in the suspend ready, then it is residing in the secondary memory [Backing state].

#### \* Operations:

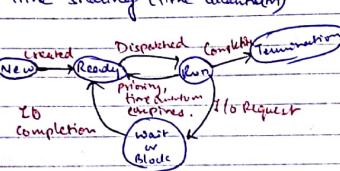
## # Multiprogramming:

Non-preemptive



Pre-emptive  
(or)  
Multi-tasking  
(or)

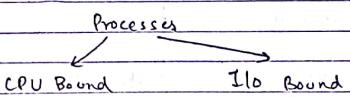
Time sharing (Time Quantum)



## # Degree of Multiprogramming:

→ The number of processes present in the main memory at any point of time is called as degree of multiprogramming.

→ Processes are categorised as follows:



\* CPU Bound Processes: Processes which require more amount of CPU time are called as CPU bound processes.

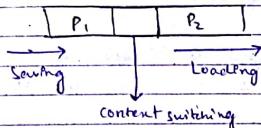
→ These processes will spend more time in the running state.

\* I/O Bound Processes: The processes which require more amount of I/O time are called as I/O bound processes.

→ These processes will spend more time in the wait/block state.

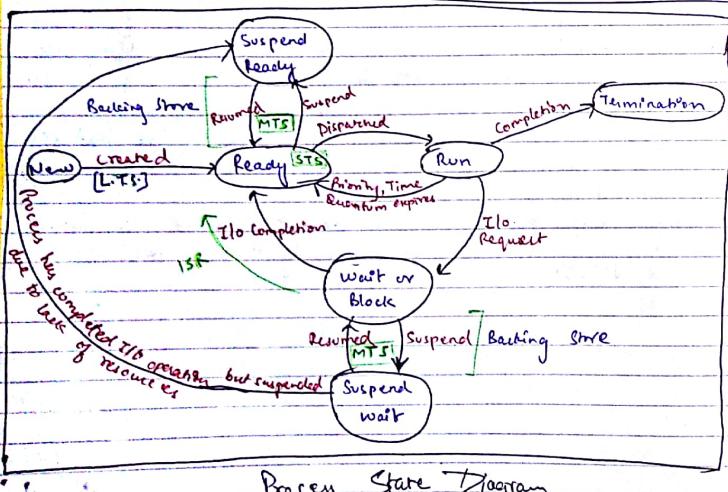
→ Each and every time, when a process is moving from one state to other state, the context of the process will change.

## \* Context Switching:



→ Saving the context of one process and loading the context of another process is called as context switching.

→ If the context of the process is more, then context switching time will also increase, which is undesirable.



**NOTE**  
→ If the context switching is disabled, then the process is not allowed for preemption.

→ Context Switching time is considered as a overhead for the system.

**NOTE**  
→ In some special cases, if there is only one process, still it is called as context switching.  
E.g. Round robin scheduling with 1 process.

→ In the O.S., there are 3 different schedulers:

(1) Long Term Scheduler (L.T.S) (or) Job Scheduler:

→ LTS is responsible of creating and bringing the new processes into the system.

(2) Short Term Scheduler (S.T.S) (or) CPU Scheduler:

→ STS is responsible of selecting one of the process in the ready state for scheduling onto the running state.

(3) Mid Term Scheduler (M.T.S) (or) Medium Term Scheduler:

→ MTS is responsible of suspending and resuming the processes.

→ The job done by mid term scheduler is called as swapping.

**Dispatcher:** Dispatcher is responsible of loading the selected job on to the CPU.

→ It is also responsible of performing context switching.

\* The LTS should select good combination of both CPU bound and IO bound processes in order to get good throughput for the system.

⇒ Long Term Scheduler controls degree of multiprogramming.

Q. Consider a system which has "n" CPU processors. Then, what

is the minimum and maximum no. of processes that may present in the Ready, Running and Block states.

	min	max
Ready	0	Any
Run	0	n
Block	0	Any

depends on max degree of multiprogramming of the system

→ Process is having various different times.

(1) Arrival Time: The time when the process is arrived into ready state.

(2) Burst Time: The time required by the process for its execution.

(3) Completion Time [C.T.]: The time when the process is completing its total execution.

(4) Turn around time [T.A.T.]: The time difference between completion time and arrival time. to call this

$$T.A.T. = C.T. - A.T.$$

(5) Waiting Time [W.T.]: The time difference between T.A.T. and B.T.

$$W.T. = T.A.T. - B.T.$$

(6) Response Time [R.T.]: The time difference between first response and arrival time.

## CPU SCHEDULING:

- Where : Ready State  
 Who : Short Term Scheduler  
 When :  
 (i) Run  $\rightarrow$  Termination  
 Run  $\rightarrow$  Wait  
 Run  $\rightarrow$  Ready  
 (ii) Wait  $\rightarrow$  Ready  
 (iii) New  $\rightarrow$  Ready

Goal : ① To maximize the CPU utilization and throughput of the system.

② To minimize the average T.A.T., avg W.T. & R.T. of the processes.

## FCFS [First Come First Serve] :

Criteria : Arrival Time

Mode : Non-preemptive

Q.	P.No	A.T	B.T	P <sub>1</sub> P <sub>2</sub> P <sub>3</sub> P <sub>4</sub> P <sub>5</sub>				
				Gantt Chart				
1	0	3		P <sub>1</sub>	P <sub>2</sub>	P <sub>3</sub>	P <sub>4</sub>	P <sub>5</sub>
2	1	2		↑	3	5	11	15
3	2	6		P <sub>2</sub>	P <sub>3</sub>	P <sub>4</sub>	P <sub>5</sub>	
4	3	4		P <sub>4</sub>	P <sub>5</sub>	P <sub>5</sub>		
5	4	5						

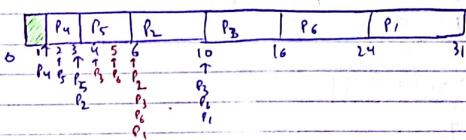
$$\text{Avg TAT} = \frac{3+4+12+16}{5} = 8.8 \text{ sec}$$

$$\text{Avg WT} = \frac{0+2+6+9}{5} = 4.8 \text{ sec}$$

$$\text{Avg TAT} = 8.8$$

$$\text{Avg WT} = 4.8$$

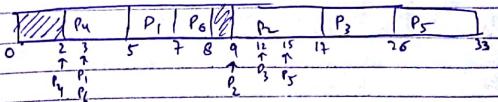
Q.	P.No	A.T.	B.T.	T.A.T.	W.T	Ang..
1	6	7	25	18		TAT = @11.5
2	3	4	7	3		WT = 6.5
3	4	6	12	6		
4	1	2	2	0		
5	2	3	4	1		
6	5	8	19	11		
			69	39		



### NOTE

If the arrival times of the processes are matching, then schedule the process which has lowest process id.

Q.	P.No	A.T	B.T	TAT	WT
1	3	2	4	2	Ag TAT = 8.67
2	9	8	8	0	Ag WT = 3.67
3	12	9	14	5	
4	2	3	3	0	
5	15	7	18	11	
6	3	1	5	4	
			52	22	



S.	P.N.	AT	BT	CY	TAT	WT
1	1	0	20	20	20	0
2	2	1	21	20	19	1
3	3	2	1	22	20	19

$$\text{Avg WT} = \frac{38}{3} = 12.67$$

S.	P.N.	AT	BT	TAT	WT
1	1	0	1	1	0
2	2	1	1	1	0
3	3	2	20	20	0

S.	P.N.	AT	BT	TAT	WT
1	1	0	1	1	0
2	2	1	1	1	0
3	3	2	20	20	0

\* Convo Effect: In FCFS, if the first process is having CPU bound process and followed by many I/O bound processes, then it will have major effect on average waiting time of the processes.  
This effect is called as Convoy Effect.

### # Shortest Job First (SJF)

Criteria : Burst Time

Mode : Non Preemptive SJF

S.	P.N.	AT	BT	TAT	WT
1	1	7	7	7	0
2	2	12	3	12	9
3	3	18	2	18	6
4	4	18	4	18	40
5	5	18	5	18	13
6	6	18	1	18	2

S.	P.N.	AT	BT	TAT	WT
1	1	8	9	8	0
2	2	9	11	9	2
3	3	11	13	11	2
4	4	13	18	13	5
5	5	18	18	18	0
6	6	18	23	18	5

### NOTE

→ If the burst times of the processes are matching then schedule the process which has lowest A.T.

S.	P.N.	AT	BT	TAT	WT
1	1	2	30	20	90
2	2	3	20	62	42
3	3	15	15	15	0
4	4	16	22	16	12
5	5	27	87	27	60
6	6	19	39	19	20

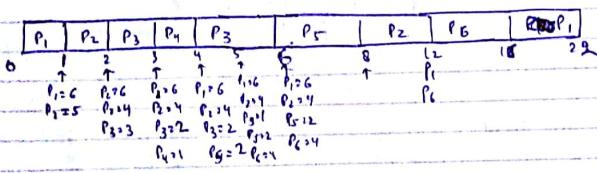
S.	P.N.	AT	BT	TAT	WT
1	P3	0	23	23	0
2	P4	23	16	39	16
3	P5	39	26	65	26
4	P6	65	45	110	45
5	P1	110	92	202	92

### Shortest Remaining Time First (SRTF):

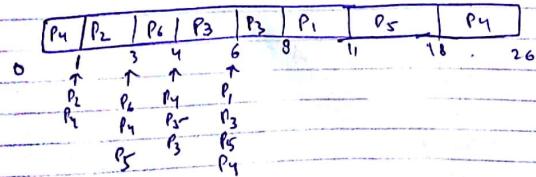
Criteria: Burst Time

Mode: Pre-emptive

Q.	P.No.	A.T.	B.T.	TAT	WT
1	1	0	1	18.22	
2	1	5	11	6	
3	2	3	4	1	
4	3	1	1	0	
5	4	2	4	2	
6	5	4	11	7	



Q.	P.No.	A.T.	B.T.	TAT	WT
1	1	6	3	5	2
2	1	7	2	9	2
3	2	0	4	4	4
4	3	1	4	5	1
5	4	2	15	17	2
6	5	1	8	9	1



Q.	P.No.	AT	BT	TAT	WT
1	6	2	4	2	
2	4	5	10	5	
3	5	3	3	0	
4	1	12	38	26	
5	3	7	17	10	
6	2	9	26	17	

$$\text{Avg TAT} = \frac{98}{6} = 16.33$$

$$\text{Avg WT} = \frac{60}{6} = 10$$

Q.	P4	P6	P5	P2	P3	P1	P1	P2	P5	P6	P4
0	1	2	3	4	5	6	8	10	14	20	28

2016

Q.	P.No.	AT	BT	TAT	WT
1	0	10	20	10	
2	3	6	7	1	
3	7	1	1	0	
4	8	3	5	2	

$$\text{Avg TAT} = 3 \times 4 = 12$$

$$\text{Avg WT} = 13/4 = 3.25$$

P1	P1	P1	P2	P2	P2	P3	P2	P4	P1
0	1	2	3	4	5	6	7	8	10

Q.	P.No.	AT	BT	TAT	WT
1	0	20			
2	15	25	40	15	
3	30	10			
4	45	15			

P1	P1	P2	P3	P2	P2
0	15	20	30	40	45

Total W.T. of P2 using SRTF?

A	C	B	C
2	8	10	4
0.75	8.25	10.75	4.12

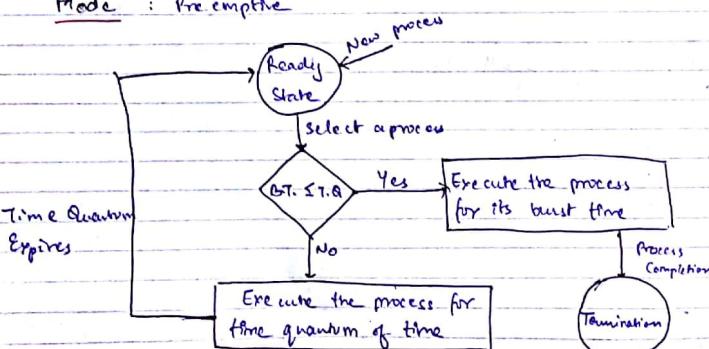
Q. Consider 3 processes A, B, C to be scheduled as per the SJF algorithm. The process 'A' is known to be scheduled first and when 'A' has been running for '7' units of time, process 'C' has arrived. The process 'C' has run for 1 unit of time, then the process 'B' has arrived and completed running in '2' units of time. Then, what could be the minm burst times of processes 'A' & 'C'?

- (1) 11 and 3
- (2) 11 and 4
- (3) 12 and 3
- (4) 12 and 4

$$\begin{aligned} A &\rightarrow 12 \quad A \rightarrow 7 + 5 = 12 \\ C &\rightarrow 4 \quad C \rightarrow 1 + 3 = 4 \\ B &\rightarrow 2 \end{aligned}$$

### # Round Robin Scheduling:

Criteria : Time Quantum, Arr. Arrival Time  
Mode : Pre-emptive



TQ=2

P.No.	A.T.	B.T.	TAT	W.T.	R.T.
1	0	4	8	4	0
2	1	5	17	16	7
3	2	2	4	2	2
4	3	1	6	5	5
5	4	6	17	11	5
6	6	3	13	10	7

Ready Queue: P1, P2, P3, P4, P5, P6, P7, P8, P9, P10, P11

P1	P2	P3	P4	P5	P6	P7	P8	P9	P10	P11
0	2	4	6	8	9	10	12	13	15	17

TQ=3

P.No.	A.T.	B.T.	TAT	W.T.	L.T.	Mg
1	5	5	27	22	10	$TA_1 = 128/6 = 21.33$
2	4	6	23	17	5	$WT_2 = 96/6 = 16$
3	3	7	30	23	3	$LT_3 = 32/6 = 5.33$
4	1	9	29	20	0	$GT_4 = 96/6 = 16$
5	2	2	4	2	2	XO
6	6	3	15	12	12	XO

Ready Queue: P4, P5, P3, P1, P6, P7, P2, P4, P5

P1	P5	P3	P2	P4	P6	P3	P2	P4	P1	P5
0	1	4	6	9	12	15	18	21	24	27

Ready Queue: P1, P6, P3, P2, P4, P5, P1, P4, P1, P2

P4	P5	P3	P2	P1	P6	P3	P2	P4	P1	P5
0	1	4	6	9	12	15	18	21	24	27

TQ = 2

Q. P.No.	AT	BT	TAT	WT	RT
1	2	4	15	11	2
2	4	1	7	6	6
3	0	5	18	13	0
4	5	2	10	8	8
5	3	3	16	13	5
6	1	6	20	14	1

$$\text{Avg. } \frac{\text{WT}}{\text{BT}} = \frac{86}{6} = 14.33$$

$$WT = \frac{65}{6} = 10.83$$

$$RT = \frac{22}{6} = 3.67$$



Ready Queue: P1, P2, P3, P4, P5, P6

No. of	P3	P6	P1	P3	P5	P1	P6	P4	P1	P3	P5	P6
0 2 4 6 8 10 11 13 15 17 18 19 21												

Context switching

#### NOTE

→ In the Round Robin, if the time quantum is less, then the no. of context switches will increase and response time will be less.

→ If the time quantum is large, then, the number of context switches will decrease and response time will be more.

→ If the time quantum is greater than all the burst time, then Round Robin behaves similar to FCFS scheduling.

#### WB. Pg 82

Q.31. P.No.	AT	BT	P.CFS & P.R.P.Q		
P1	0	5	$\infty$		
P2	1	7		$\infty$	
P3	3	4			$\infty$

TR. P1 P2 P3 P4 P5 P6 P7 P8 P9 P10 P11

Round Robin:	P1	P2	P3	P4	P5	P6	P7
	0	2	4	6	8	10	11

Q. Consider a system which has 4 processes, P1, P2, P3 & P4, all arriving in the ready queue in the same order at time 0. The BT requirement of these processes are 4, 1, 3, 1. Then what is the completion time of process P1, assuming RR scheduling with  $TQ = 1$ ?

P. AT BT

1 0 4

2 0 1

3 0 3

4 0 1

CY q. P1 = 9

④ 7 ④ 9

④ 8 ④ 10

8 1 X2 P3 P4 P1 P2

P1	P2	P3	P4	P1	P3	P1	P3	P2
0	1	2	3	4	5	6	7	8

Q. Consider 'n' processes sharing the CPU in RR scheduling. The context switching time is 's' units, then what will be the time quantum "q" such that, the no. of context switches are reduced, but at the same time each process is guaranteed to get  $q$  units of job at the CPU after every 't' seconds of time?

$$(a) q = \frac{t - ns}{n+1}$$

$$(c) q = \frac{t - ns}{n-1}$$

$$(b) q = t + ns$$

$$(d) q = \frac{t + ns}{n+1}$$

AT assume 0 if not given  
BT assume  $\infty$  if not given

P1	P2	P3	P4	P5	P1
0	2	4	6	8	10

t = 10 q = 2 ns = 10/2 = 5

q = 10 - 5 = 5

t = q(n-1) + ns

$$t - ns = q$$

$$t = q(n-1) + ns$$

$$q = t - ns$$

$$n-1$$

P1	P2	P3	P4	P5	P1	P2	P1
5	4	5	4	5	4	3	2

t = 10 - 5 = 5

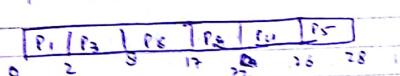
t - ns = q

### # Longer Job First:

(Criteria : Burst Time)

Mode : Non Preemptive

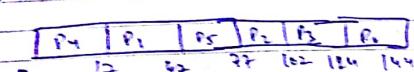
Q.	P.No.	AT	BT	TAT	WT	Avg
1	0	2	2	2	0	$TAT = 83/6 = 14.67$
2	1	5	21	16	11	$WT = 69/6 = 10$
3	2	6	6	0		
4	3	4	23	19		
5	4	2	24	22		
6	5	9	12	3		



### NOTE

If the burst time of the processes are matching then schedule the process which has the lowest arrival time

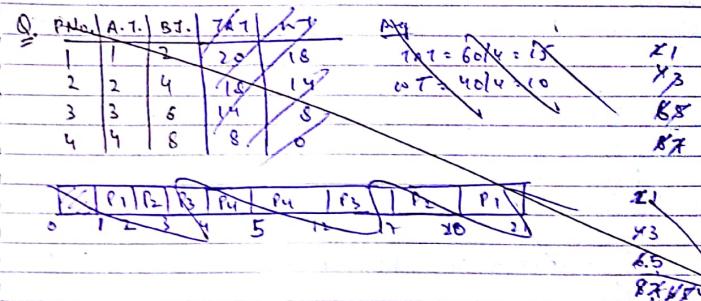
Q.	P.No.	AT	BT	TAT	WT	Avg
1	10	20	30	30	0	$TAT = 43/6 = 7.17$
2	15	25	87	82	62	$WT = 281/6 = 47.83$
3	23	22	101	79		
4	0	12	12	0		
5	20	30	57	27		
6	5	20	132	112		



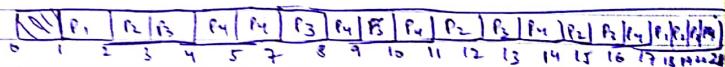
### Longest Remaining Time First (LRTF)

(Criteria : Burst Time)

Mode : Preemptive

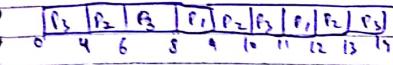


Q.	P.No.	AT	BT	TAT	WT	Avg
1	1	1	2	13	15	$TAT = 68/4 = 17$
2	2	2	4	17	13	$WT = 48/4 = 12$
3	3	3	6	17	11	
4	4	4	8	17	9	

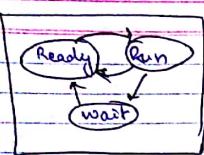


Q.	P.No.	AT	BT	TAT	WT	Avg
1	0	2	12			
2	0	4	13			
3	0	8	14			

Avg TAT using LRTF



### Life Cycle



① CPU	✓
② I/O	✓
③ CPU, I/O	✓
④ CPU, I/O, CPU	✓
⑤ I/O, CPU, I/O	✓
⑥ CPU, CPU, I/O	X

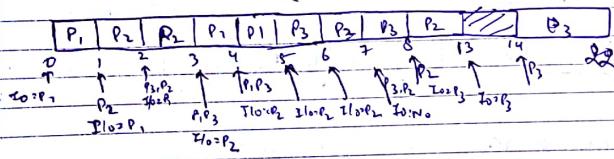
CT?  
Using SRTF?

P.No.	AT	Execution Time			CT
		I/O Time	CPU Time	I/O Time	
1	0	4	14	2	20
2	0	8	28	4	50
3	0	12	42	6	94

Q.	P.No.	AT	Execution Time			C.T.
			CPU Time	I/O Time	CPU Time	
1	1	0	10	20	20	5
2	1	20	4	14	50	13
3	2	30	6	8	22	

What is completion time of processes P<sub>1</sub>, P<sub>2</sub>, P<sub>3</sub> using SRTF algo?

- NOTE**
- ① Process first spends CPU Time followed by I/O Time and followed by CPU Time again.
  - ② I/O of the processes can be overlapped as much as possible.



G.T.

P<sub>1</sub>  
P<sub>2</sub>  
P<sub>3</sub>

(a) 18, 46, 88
(b) 18, 46, 94
(c) 20, 50, 94
(d) 18, 50, 94

Q. No.	Execution Time			
	P <sub>1</sub>	P <sub>2</sub>	P <sub>3</sub>	
1	4	18	46	
2	10	14	50	
3	12	21	3	

0 ↑	P <sub>1</sub>	P <sub>2</sub>	P <sub>3</sub>	
↓ P <sub>1</sub>	P <sub>2</sub>	P <sub>3</sub>	T <sub>10:P<sub>2</sub></sub>	T <sub>10:N<sub>0</sub></sub>
T <sub>10:P<sub>1</sub></sub>	P <sub>2</sub>	P <sub>3</sub>	T <sub>10:P<sub>2</sub></sub>	T <sub>10:N<sub>0</sub></sub>
T <sub>10:P<sub>2</sub></sub>	P <sub>3</sub>	T <sub>10:P<sub>3</sub></sub>	T <sub>10:P<sub>2</sub></sub>	T <sub>10:N<sub>0</sub></sub>

CPU Idle time =  $\frac{5}{22} \times 100 = 10.638\%$

P <sub>1</sub>	0	CPU	I/O	23	25
P <sub>2</sub>	20	4		CPU	I/O
P <sub>3</sub>	20	6		CPU	I/O

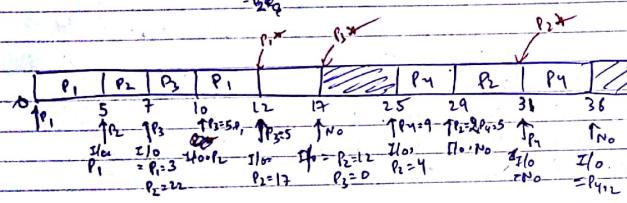
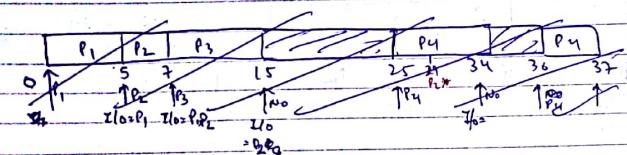
P.No.	AT.	Execution Time			CT?
		CPU time	Tat time	Wt time	
1	0	5 <sub>0</sub>	5 <sub>3</sub>	2	P <sub>2</sub>
2	3	2 <sub>0</sub>	2 <sub>2</sub>	2	P <sub>3</sub>
3	7	8 <sub>0</sub>	0	0	P <sub>4</sub>
4	25	9	2	1	39



P <sub>1</sub>	P <sub>3</sub>	P <sub>5</sub>	P <sub>6</sub>	P <sub>4</sub>	P <sub>2</sub>
0	2	6	12	19	29
P <sub>2</sub>					
P <sub>3</sub>					
P <sub>4</sub>					
P <sub>5</sub>					
P <sub>6</sub>					

NOTE

If the priorities of the processes are matching then schedule the process which has lowest arrival time.



S.	Priority	P.No	AT	B.T	Tat	WT	Mng
4	P <sub>1</sub>	4	6	21	15	0	TAT = 70/6 = 13
5	P <sub>2</sub>	6	9	9	0	0	WT = 52/6 = 8.66
6	P <sub>3</sub>	3	4	16	12	0	
6	P <sub>4</sub>	2	2	4	2	0	
1	P <sub>5</sub>	1	3	3	0	0	
3	P <sub>6</sub>	2	25	23	0	0	

### # Priority Based Scheduling:

Criteria : Priority

Mode : Non Preemptive .

Eq.	Priority	P.No.	A.T.	B.T.	TAT	WT	Ans	
							TAT	WT
	2	P <sub>1</sub>	0	2	2	0	$TAT = \frac{P1+B1}{2} = 2$	
	1	P <sub>2</sub>	1	3	26	23	WT = 23	
	3	P <sub>3</sub>	2	6	8	2		
	4	P <sub>4</sub>	3	5	21	16		
High ← 6	P <sub>5</sub>	4	4	3	4	0		
5	P <sub>6</sub>	5	7	14	7	0		

P <sub>5</sub>	P <sub>4</sub>	P <sub>2</sub>	P <sub>3</sub>	P <sub>1</sub>	P <sub>6</sub>
0	1	4	6	19	25
P <sub>4</sub>					
P <sub>6</sub>					
P <sub>3</sub>					
P <sub>1</sub>					
P <sub>2</sub>					

## # Preemptive Priority:

Criteria : Priority

Mode : Preemptive

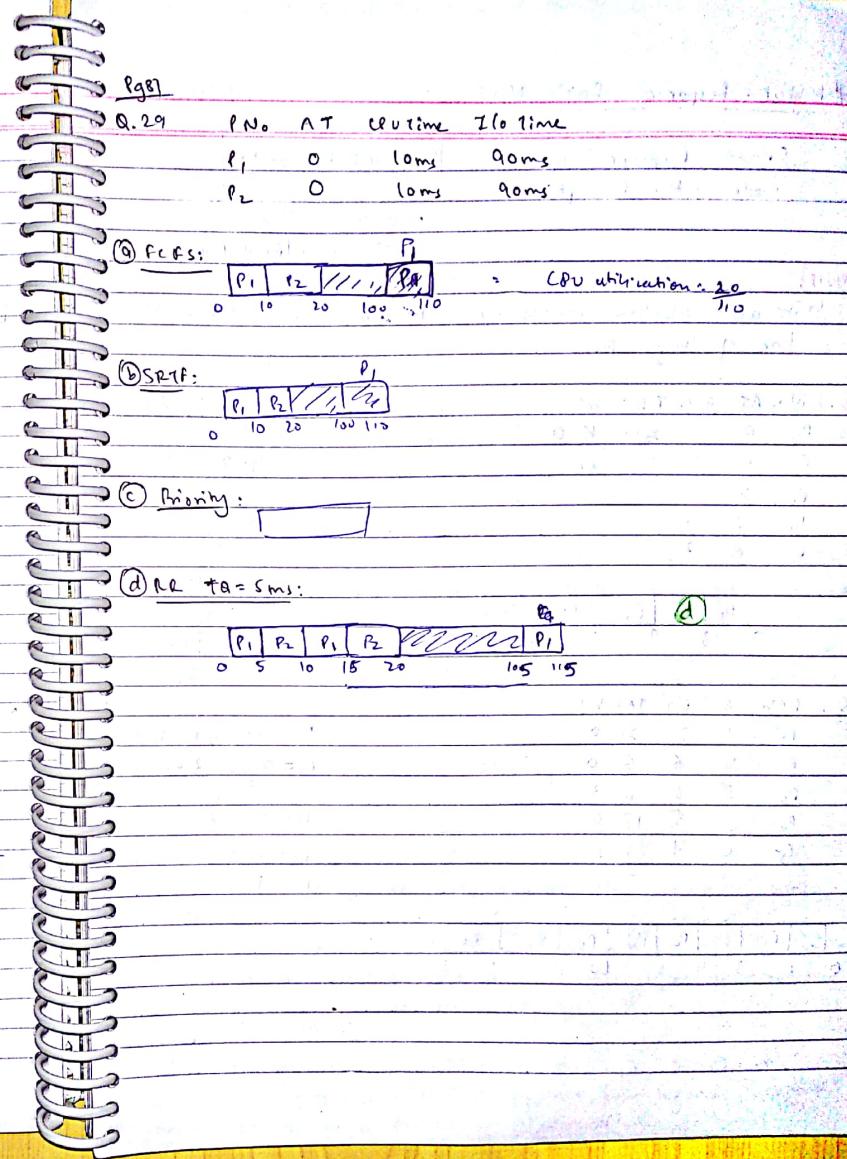
Q.	P.No	A <sub>T</sub>	B <sub>T</sub>	Priority	TAT	WT
	P <sub>1</sub>	0	4	2	27	23
	P <sub>2</sub>	1	5	3	23	18
	P <sub>3</sub>	1	6	4	18	12
	P <sub>4</sub>	2	2	5	12	10
	P <sub>5</sub>	2	3	6	10	7
	P <sub>6</sub>	3	7	7 ← high	7	0

P <sub>1</sub>	P <sub>3</sub>	P <sub>6</sub>	P <sub>4</sub>	P <sub>5</sub>	P <sub>2</sub>	P <sub>1</sub>
0	1	2	3	10	12	14

Q.	P.No	A <sub>T</sub>	B <sub>T</sub>	Priority	TAT	WT
	P <sub>1</sub>	1	8	2	44	36
	P <sub>2</sub>	2	6	3	30	24
	P <sub>3</sub>	3	9	5	24	15
	P <sub>4</sub>	0	7	2	32	20
	P <sub>5</sub>	4	8	6	35	25
	P <sub>6</sub>	5	7	7 high	7	0

P <sub>1</sub>	P <sub>4</sub>	P <sub>2</sub>	P <sub>3</sub>	P <sub>5</sub>	P <sub>6</sub>	P <sub>5</sub>	P <sub>3</sub>	P <sub>2</sub>	P <sub>4</sub>	P <sub>1</sub>
0	2	3	4	5	12	19	27	32	37	45

W3 Pg 87  
Q. 29. P<sub>1</sub> & 10ms 90ms  
P<sub>2</sub> 10ms 90ms



## Highest Response Ratio Next

Criterion: Response Ratio  
Mode : Non Pre-emptive

$$\text{Response Ratio} = \frac{W_t + S}{S}$$

$W_t$  → Waiting Time

$S$  → Service/Burst Time

### NOTE

→ The above algorithm favours the shorter jobs and limits the waiting time of longer jobs.

Q. P.No. AT BT TAT WT

P<sub>1</sub> 0 3 20 17 0

P<sub>2</sub> 2 6 10 12

P<sub>3</sub> 4 4

P<sub>4</sub> 6 5

P<sub>5</sub> 8 2

P <sub>1</sub>	P <sub>2</sub>	P <sub>3</sub>	P <sub>4</sub>	P <sub>5</sub>
0	3	9	13	15 20

$$P_3 = \frac{5+4}{4} = 2.25$$

$$P_4 = \frac{3+5}{5} = 1.6$$

$$P_5 = \frac{3}{5} = 0.6$$

$$P_4 = \frac{7+5}{5} = 2.4$$

$$P_5 = \frac{5+3}{2} = 3.5$$

Q. P.No. AT BT TAT WT

P<sub>1</sub> 1 2 2 0

P<sub>2</sub> 4 6 6 0

P<sub>3</sub> 5 3 6 3

P<sub>4</sub> 6 5 13 8

P<sub>5</sub> 8 1 3 2

P <sub>1</sub>	P <sub>2</sub>	P <sub>3</sub>	P <sub>4</sub>	P <sub>5</sub>
0	1	3	4	8 10 11 14 19

$$P_3 = \frac{2+5+1}{3} = 3, P_3 = 0 + 3 = 3$$

$$P_4 = \frac{5+3}{3} = 2.67$$

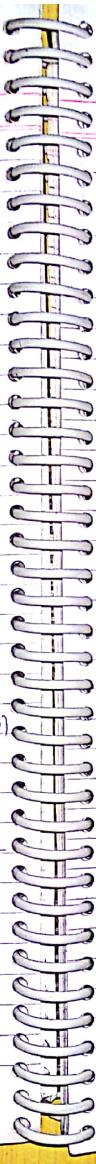
$$P_5 = \frac{9}{5} = 1.8$$

$$P_5 = \frac{2+3}{2} = 2.5$$

$$P_3 = \frac{4}{3} = 1.33$$

$$P_4 = \frac{6+3}{3} = 3$$

$$P_5 = \frac{5+5}{5} = 2$$



## # Multi Level Queue Scheduling:

R.Q.1 →

R.Q.2 →

R.Q.3 →

R.Q.4 →

→ Depending on the priority of the process in which particular ready queue, the process has to be placed will be decided.  
→ The high priority processes will be placed in the top level ready queue and the low priority processes will be placed in the bottom level ready queue.

→ Only after the completion of all the processes from the top level ready queue, the further level ready queue processes will be scheduled.

→ If this is the strategy followed, then the processes which are placed in the bottom level ready queue will suffer from starvation.

\* Starvation: The indefinite waiting of a process is called as starvation.

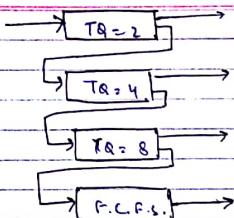
### NOTE

→ To avoid the problem of starvation, the concept of ageing will be used.

\* Ageing: If the waiting time of a process increases, then the priority of the process will be increased.

→ If the age of a process increases by increasing the priority, the processes will definitely get a strong chance to execute and the starvation problem will be avoided.

### # Multi Level Feed Back Queue (MLF.Q)

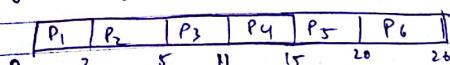


→ In the above algorithm, every process will definitely get a chance to execute for some amount of time, but still there may be a possibility for the process to go into starvation.

P.T. = 20 B.T. = 40		
	Queue Remaining B.T.	TQ
0	1 38	2 Queue = 5
20	2 31	7
31	3 19	12
19	4 2	17
2	5 0	22

Q. P.No   A.T.   B.T.		
1 0 2		Throughput = $\frac{26}{6} = 4.33$
2 1 3		
3 2 6		
4 3 4		
5 4 5		
6 5 6		

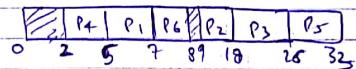
Throughput using FCFS scheduling?



$$\text{* Throughput: } = \frac{\# \text{ of processes}}{\text{Max (C.T.)} - \text{min (A.T.)}}$$

Q. P.No	A.T.	B.T.
1	3	2
2	9	9
3	12	8
4	2	3
5	15	7
6	3	1

$$\text{Throughput} = \frac{6}{33-2} = \frac{6}{31} = 0.193$$



\*\*

Algorithm

1. FCFS
2. NP  $\rightarrow$  SJF
3. SJF
4. RR
5. NP  $\rightarrow$  LRTF
6. LRTF
7. NP  $\rightarrow$  Priority
8. Pre  $\rightarrow$  Priority
9. HRRN
10. MLQ.S.
11. MLF.B.Q

Starvation

NO

YES  $\rightarrow$  New shorter processes will finish & leave nothing

YES  $\rightarrow$  Thus, nothing never gets full

NO

YES  $\rightarrow$  New longer processes don't leave anything

NO  $\rightarrow$  New longer processes don't leave anything

YES  $\rightarrow$  Quantum is finite

YES

NO

$\rightarrow$  RR:  $WTS \uparrow$

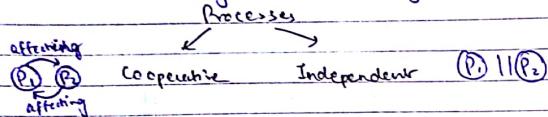
YES  $\rightarrow$  Quantum is constant

YES

\* Majority of the O.S. practically implement Round Robin scheduling

## # Synchronization: (Terenbaum)

→ Processes are categorized into 2 types.



→ The execution of one process affects or affected by other process, then, those processes are said to be cooperative processes; otherwise, they are said to be independent processes.

## \* Understanding Synchronization:

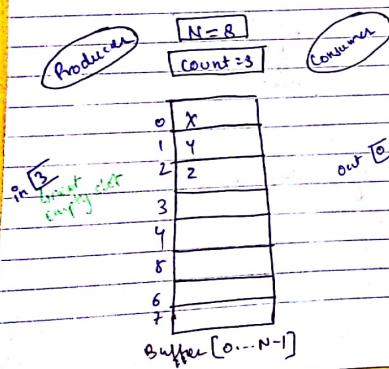
(1) The problem arises NOT having synchronization between the processes.

(2) The conditions to be followed to achieve synchronization.

(3) The solutions [Wrong and Right]

STEPS: Problems arising due to NOT having synchronization between the processes.

## \* THE PRODUCER-CONSUMER PROBLEM:



```
int count = 0;  
void producer(void)
```

```
{  
    int temp;  
    while (TRUE)
```

```
        produce-item(item p);  
        while (count == N);  
        Buffer[in] = item p;  
        in = (in + 1) % N;  
        count = count + 1;
```

check if buffer is full.  
if the condition is true, it will keep looping until condition becomes false.

- I. load Rp, m[count]  
II. INCR Rp  
III. store m[count], Rp

```
void consumer(void)
```

```
{  
    int item c;  
    while (TRUE)
```

```
        while (count == 0);  
        item c = Buffer[out];  
        out = (out + 1) % N;  
        count = count - 1;  
        process-item(item c);
```

- I. load Rc, m[count]  
II. DECR Rc  
III. store m[count], Rc

- in is a variable used by the producer to identify the next empty slot in the buffer.
- out is a variable used by the consumer to identify from where it has to consume the items.
- count is a variable used by producer and consumer to identify the number of items present in the buffer at any point of time.

## \* Shared Resources:

- (1) Count variable
  - (2) Buffer.

\* Two conditions to be followed:

- ① when the buffer is full, producer is not allowed to produce the item into buffer.
  - ② when the buffer is empty, consumer is not allowed to consume the item from the buffer.

## \* Universal Assumption:

→ The running process can get pre-empted at any point of time after completion of the current instruction.

## # Analysis:

Item A: 'A'  
Item C: 'X'

$$\begin{array}{ll}
 P \rightarrow I & R_P \boxed{B[4]} \\
 P \rightarrow II & \\
 C \rightarrow I & \\
 C \rightarrow II & R_C \boxed{B[2]} \\
 C \rightarrow III & \\
 P \rightarrow IV &
 \end{array}$$

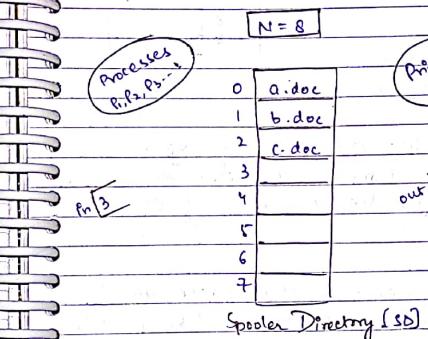
$$\begin{array}{l} \text{count} = \emptyset \neq 4 \\ \text{in} = \emptyset 4 \\ \text{out} = \emptyset 1 \end{array}$$

0
1 Y
2 Z
3 A
4
5
6
7

### First Problem:

- ① Inconsistency: The processes are not properly synchronised while sharing the common variable "count".  
 Hence, it is leading to the problem of inconsistency.

## \* Printer Spooler Daemon:



respective  
process  
register

Enter file :

- I. load R<sup>i</sup> m[in]
- II. Show SD[R<sup>i</sup>], "F-N"
- III. INCR R<sup>i</sup> filename
- IV. Store m[in], R<sup>i</sup>

- `in` is a variable used by all the processes to identify the next empty slot in the spooler directory.
- `out` is a variable used by the printer to identify from where it has to print the document.

## \*Shared Resources:

- ① Spooler Directory (SD)
  - ② "in" variable.

\* Analysis: R.Q | P<sub>1</sub> | P<sub>2</sub>

$$\begin{array}{ll}
 P_1 \rightarrow I & R_1 \boxed{\cancel{X^4}} \\
 P_1 \rightarrow II & \\
 P_1 \rightarrow III & \hline \\
 P_2 \rightarrow I & R_2 \boxed{\cancel{X^4}} \quad [3] \\
 P_2 \rightarrow II &
 \end{array}$$

### Second Problem:

② Loss of Data: The processes are not properly synchronized while sharing the common variable "in", hence, it is leading to the problem of loss of data.

	list of data
0	a.doc
1	b.doc
2	c.doc
3	xyz.doc pqr.doc
4	
5	
6	
7	s.d.

### NOTE

→ To avoid the RACE condition only one process should be allowed into critical section at any point of time.

25/09/2019 : STEP-2

# The Conditions To Be Followed To Achieve Synchronisation:

① Mutual Exclusion: No 2 processes may be simultaneously present inside the critical section at any point of time.

→ Only one process is allowed into critical section at any point of time.

② Progress: No process running outside the critical section should block the other interested process from entering into the critical section when critical section is free.

→ If there is only one process trying to enter into critical section, then it should be definitely allowed into critical section.

→ If two or more processes are trying to enter into critical section, then one process should be definitely allowed into critical section.

③ Bounded Waiting: No process should have to wait forever to enter into critical section.

→ There should be a bound on getting chance to enter into critical section.

→ Some process is indefinitely waiting to enter into critical section because critical section is always busy by some other processes. This situation should not arise.

→ If the bounded waiting is not satisfied, then, it is possible for starvation to occur.

### Third Problem:

③ Deadlock: If the processes are not properly synchronized, while sharing the common variables or common resources, then, it is also for the occurrence of deadlock.

### # Definitions:

① Critical Section: The portion of program text, where shared variables or shared resources will be placed.  
E.g. count = count + 1, (or) count = count - 1.

② Non-critical Section: The portion of program text where the independent code of the processes will be placed.  
E.g. in = (int) mod N;

③ Race Condition: The final value of any variable depends on execution sequence of the processes. This type of condition is called as RACE condition.

E.g.-	count = 4	Count = 2
P → I		C → I
P → II		C → II
C → I	P → I	
C → II	P → II	
C → III	P → III	
P → III		C → III

④ No assumptions related to hardware and processor speed.  
→ Architectural neutral.

### Step 3. The Solutions:

#### I. Software Type:

- (a) Lock variables
- (b) Strict alternation or Dekker's algorithm
- (c) Peterson's Algorithm

#### II. Hardware Type:

- (a) TSL, Instruction Set  
→ Test and set Lock

#### III. O.S. Type:

- (a) Counting Semaphore
- (b) Binary Semaphore

#### IV. Programming Language Compiler Support Types:

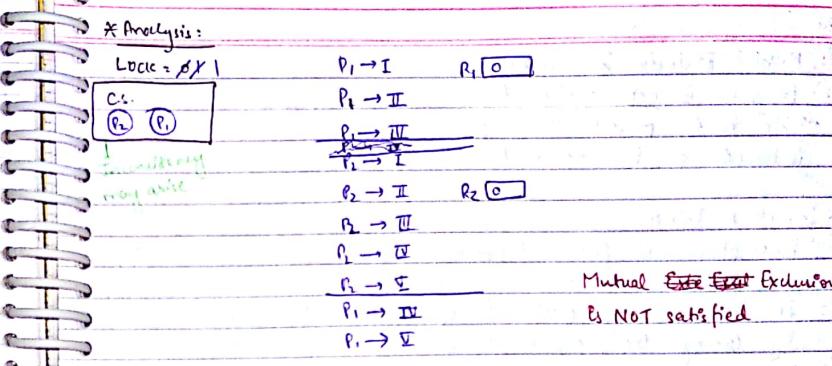
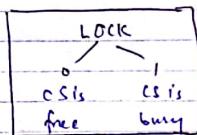
- (a) Monitors

### I. SOFTWARE TYPE SOLUTIONS:

#### ① Lock Variables:

Entry Section: *lock + unlock*

- I. Load R0 m[lock]
- II. CMP R0, #0
- III. JNZ to Step I
- IV. Store m[lock], #1
- V. [C-S]
- VI. Store m[lock], #0

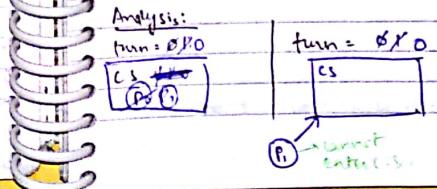
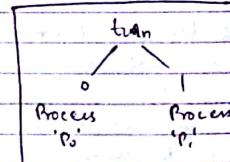


\* We have proved that both the processes are entering into critical section at the same time, hence, mutual exclusion is not satisfied and solution is bound to be incorrect.

#### ② Strict Alternation or Dekker's Algorithm:

(process takes "turn" to enter into C-S.)

Process 'P0' code	Process 'P1' code
<pre> while (true) {     Non-(SC);     while (turn != 0);     C-S;     turn = 1; }   </pre>	<pre> while (true) {     Non-(SC);     while (turn != 1);     C-S;     turn = 0; }   </pre>



- ① Mutual Exclusion is satisfied
- ② Progress is not satisfied  
→ We have proved that progress is not satisfied and solution is bound to be incorrect.

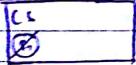
#### \* Important Points:

- ① Preemption is just a temporary stop and process will come back and continue the remaining execution.
- ② If there is any possibility of a solution becoming wrong by taking the pre-emption, then, consider the pre-emption.
- ③ If any solution is having deadlock, then, the progress is not satisfied.

W.B.Pg.90-

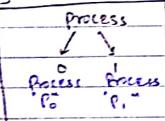
D.15.  $S_1 = P_1$   $S_2 = 1$

- ② Mutual exclusion but not progress



#### C) Peterson's Algorithm: [2 process solution]

```
#define N 2
#define TRUE 1
#define FALSE 0
int turn;
int interested[N];
void Enter-Region (int process)
{
    1. int other;
    2. other = 1 - process;
    3. interested[process] = TRUE;
    4. turn = process;
    5. while (turn == process & interested[other] == TRUE);
}
```



\* If current turn right from assume CS to other.

C.S.

void Enter-Region (int process)

{ Interested [process] = FALSE;

Initially:

interested [0] = FALSE; TRUE

interested [1] = FALSE; TRUE

# Analysis 1:

Initially:

interested [0] = FALSE; TRUE

interested [1] = FALSE; TRUE

turn =  $\neq 1$

Process P <sub>0</sub>	Process P <sub>1</sub>
Other=1	Other=0



# Analysis 2:

interested [0] = FALSE; TRUE

interested [1] = FALSE; TRUE

turn = process & interested [other] = TRUE

1 T 1 ①

0 T 0 ②

T X

turn = X 0

Process P <sub>0</sub>	Process P <sub>1</sub>
Other=1	Other=0



① Mutual Exclusion is satisfied.

② Progress is satisfied

③ Bounded waiting is satisfied.

→ We have proved that all the 3 conditions are satisfied in the above algorithm.  
The solution is bound to be correct and it is properly providing synchronization to the processes to access common critical section.

Q. Assume that both the processes  $P_0$  and  $P_1$  are trying to enter into critical section at the same time. Then, which process will enter into critical section first.

Q. The process which executes statement 2 first:



## Steps :-

$P_0 \rightarrow -3$  then  $P_1 \rightarrow 3$

8-3

$$P_1 \rightarrow 4 \quad \text{then} \quad P_0 \rightarrow 4$$

• 100 •

## II. HARDWARE TYPE SOLUTIONS

## TSL INSTRUCTION SET [Test and Set Lock]

$\Rightarrow$  TSL Register flag: copies the current value of flag into register and stores the value '1' into flag  
In a single atomic cycle without any preemption.

### Entry Section:

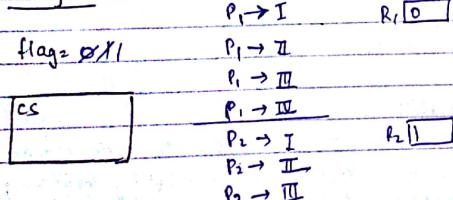
- I. TSL R<sub>i</sub>, m[flag]
  - II. CMP R<sub>i</sub>, #0
  - III. JNZ to step ①

IV: Store in [flag], #0

### Analysis:

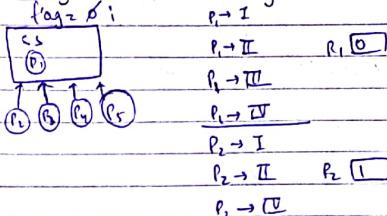


① Mutual Exclusion is satisfied.



- ① Mutual Exclusion is satisfied.
  - ② Progress is satisfied.
  - ③ Round robin waiting is NOT satisfied

## Analysis: (Bounded Waiting)



Round Robin:  
 $(q_j = p_i x, 0 \rightarrow B.W. \text{ not satisfied})$

$$P_{\text{Q}} = P_1 P_2 P_3 P_4 P_5 P_6 P_7 P_8$$

$$PQ = P_1 P_2 P_3 P_4 P_5 P_6 P_7 P_8$$

**NOTE**

↳ If some process is in the critical section, then all the other processes which are trying to enter critical section will be regularly checking I, II, III instructions.

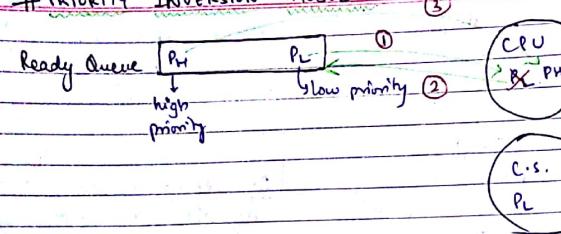
→ These processes are busy in checking these instructions and waiting to enter into critical section. This is called as busy waiting and these processes are wasting the CPU cycles [time].

→ Busy waiting is also called as spin lock.

→ To avoid busy waiting, semaphore will be used.

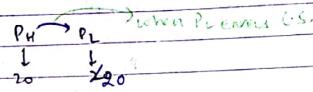
<u>Solution</u>	<u>Mutual Exclusion</u>	<u>Progress</u>	<u>Bounded waiting</u>
① Lock Variable	X	✓	X
② Strict Alteration (or) Dekker's algorithm	✓	X	✓
③ Peterson's Algorithm	✓	✓	✓
④ TSL instruction set	✓	✓	X

### # PRIORITY INVERSION PROBLEM:



Solution:

#### ④ Priority Inheritance



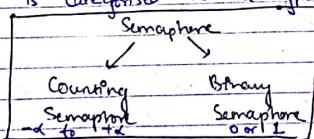
- If a lower priority process is executing the critical section and a higher priority process arrives into the CPU.
- the low priority process inherits the priority of the higher priority process.
- Thus, the process which arrives first executes the critical section first, i.e.,  $P_2'$ .

26/09/2017:

### III OPERATING SYSTEM TYPE SOLUTIONS:

#### 1. Semaphore:

- Semaphore is an integer variable used by various processes in a mutual exclusive manner to achieve synchronization.
- Improper usage of semaphore will also give wrong results.
- Semaphore is categorised into 2 types:



- The two different operations will be performed on the semaphore variable by the processes.
- ① Down(); or wait(); or p();
- ② Up(); or signal(); or v(); or Release();

#### # Counting Semaphore:

##### Down (Semaphore s)

```

s.value = s.value - 1;
if (s.value < 0)
    {
        Block the process and
        place its PCB in the
        suspended list();
    }
}

```

(In my case, the process is  
not suspended.)

##### Up (Semaphore s)

```

s.value = s.value + 1;
if (s.value >= 0)
    {
        Select a process from
        the suspended list
        and wakeup();
    }
}

```

- After performing down operation, if the process is getting suspended, then, it is called as unsuccessful down operation.
- If it is unsuccessful down operation, then process will not continue further execution.
- After performing down operation if the process is not getting suspended, then, it is called as successful down operation.
- If it is successful down operation, then only process will continue further execution in the code.
- The positive value of the counting semaphore represents the number of successful down operations we can perform.
- The down operation on the counting semaphore is successful only if the initial value of the semaphore is  $s > 1$ .

$$s > 1$$

→ There is no unsuccessful up operation and up operation is always successful.

→ The process performing up operation will definitely continue further execution.

Q. Consider a system where initial value of the counting semaphore is  $s = +17$ , then, various semaphore operations like  $23P, 18V, 16P, 14V, 1P$  are performed. Then what is the final value of the counting semaphore.

$$+17 \rightarrow 23P = -6$$

$$+18 \rightarrow -6 \rightarrow 18V = 12$$

④ 7    ⑤ 8    ⑥ 9    ⑦ 10

⑧ 12    ⑨ 14    ⑩ 16

⑪ 18    ⑫ 20    ⑬ 23

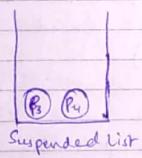
⑭ 16    ⑮ 14    ⑯ 12

⑰ 10    ⑱ 8    ⑲ 6

⑳ 6    ㉑ 4    ㉒ 2

㉓ 2    ㉔ 0    ㉕ -2

P <sub>1</sub>	P <sub>2</sub>	P <sub>3</sub>	P <sub>4</sub>
P	P	P	P
✓	✓	X	X



#### NOTE

→ The negative value of the counting semaphore indicates the number of processes blocked. [In the suspended list]

Q. Consider a counting semaphore variable 's'. The various semaphore operations like  $10P, 12V$  are performed during execution. Then what is the largest initial value of 's' so that 1 process will be blocked.

$$+10 \rightarrow 10P = -10 \rightarrow x - 10 + 12 = -1 \rightarrow x = 11$$

$$\boxed{x = 11} \rightarrow \boxed{11}$$

#### # Binary Semaphore:

Down (Semaphore s)

{ If (s.value == 1)  
s.value = 0;

else

{ Block the process and  
place its PCB in the  
suspended list L;

}

Up (Semaphore s)

{ If (Suspended List L) is empty  
s.value = 1;

else

{ Select a process from the  
suspended list and wakeup();

}

→ After performing down operation, if the process is getting suspended, then, it is called as unsuccessful down operation.  
→ If it is unsuccessful down operation, then, the process will not continue further execution.  
→ After performing down operation, if the process is not getting suspended, then, it is called as successful down operation.

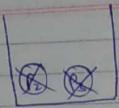
→ If it is successful down operation, then only process will continue further execution.

→ Down operation on the binary semaphore will be successful, only if the initial value of the semaphore is 1. [s=1]

→ There is no unsuccessful up operation and up operation is always successful.

→ The process performing up operation will definitely continue further execution.

$S = X_1, D_1, X_1$	$P_1$	$S_1$	$P_2$	$D_2$	$P_3$	$D_3$	$P_4$	$D_4$	$P_5$	$D_5$	$P_6$	$D_6$
	P	D	P	D	V	V	V	V	V	V	V	V
V	X	X	V	V	V	V	V	V	V	V	V	V



W.B Page 1

Q. 22: Mutex = 1 ; 9 p( ), 1 v( ), 6 p( ), 8 v( ), 3 p( ), 2 v( )

{ }

Mutex = ~~X, X, X~~ 0



NOTE

- ↳ Applicable for both Counting and binary semaphore.
- 1. ⇒ Every semaphore variable will have its own suspended list.
- 2. ⇒ The down and up operations are atomic.
- 3. ⇒ If more than one process is in the suspended list, then, every time, when we perform one up operation, one process will wake up from the suspended list and this will be based on FCFS.
- 4. ⇒ If two or more processes are in the suspended list and there is no other process to wake up these processes, then those processes are said to be involved in the deadlock.

- Q. Each process  $P_i; i=1 \text{ to } 10$  executes the following code:
- ```

while (true)
{
    p(mutex);
    [processes]
    v(mutex);
}

```
- Process  $P_{10}$  executes this code.

What can be the maximum no. of processes that may be present inside the critical section at any point of time?

[NOTE] Initial value of binary semaphore mutex = 1.

- (a) 2    (b) 3    (c) 9    (d) 10    (e) 1

\* Analysis:

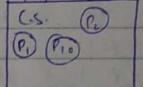
mutex = ~~X, X, X, X, X, X, X, X, X, X~~ 1    If  $P_{10}$  after every process it makes the value of mutex = 1.



∴ So, all process are able to enter C.S.

Q.  $\frac{P_{10}}{\text{mutex} = 0}$  while (true)  
{ v(mutex);  
[CS];  
p(mutex); }

mutex ≠ 0



• Maximum 3 processes can enter C.S.

Q.  $\frac{P_1-P_9}{\text{mutex} = 0}$  while (true)  
{ p(mutex);  
[CS];  
v(mutex); }

$\frac{P_{10}}{\text{mutex} = 10}$  while (true)  
{ p(mutex);  
[CS];  
v(mutex); }



- MF satisfied
- Progress satisfied
- Round robin wait satisfied

- (a) 2    (b) 3    (c) 9    (d) 10    (e) 1

2003

Q. Consider two concurrent processes 'P' and 'Q' executing their respective codes:

|                  |                  |
|------------------|------------------|
| Process 'P' code | Process 'Q' code |
| while(true)      | while(true)      |
| {                | {                |
| W: P(T)   P(S)   | W: P(S)          |
| print('0');      | print('1');      |
| print('0');      | print('1');      |
| X: V(S)          | Z: V(T)          |
| }                | }                |

What should be the binary semaphore operations on w, x, y, z respectively and what initial values of binary semaphores 'S' and 'T' should be taken in order to get print always as:  
0011001100... .

- (A) W = P(T), X = V(T), Y = P(S), Z = V(S); S = T = 1;
- (B) W = P(T), X = V(LT), Y = P(S), Z = V(S); S = 1; T = 0;
- (C) W = P(LT), X = V(S), Y = P(S), Z = V(T); S = T = 1;
- (D) W = P(T), X = V(S), Y = P(S), Z = V(T), S = 0, T = 1;

$$S = \cancel{1} \cancel{0} \times 0$$

$$T = \cancel{1} \cancel{0} 1$$

Q. Which of the following will ensure that the output string never contains a substring of the form  $0^n0$  or  $1^n1$ , where n is odd?

- (A) W = P(S), X = V(S), Y = P(T), Z = V(T), S = T = 1
- (B) W = P(S), X = V(T), Y = P(T), Z = V(S), S = T = 1
- (C) W = P(S), X = V(S), Y = P(S), Z = V(S), S = 1
- (D) W = V(S), X = V(T), Y = P(S), Z = P(T), S = T = 1

$$S = \cancel{1} \cancel{0} 1$$

$$011110 \checkmark$$

|                                                                    | $S_x = P(x)   V(x)$                                        | $t_1$                                   | $P_c$                                              |
|--------------------------------------------------------------------|------------------------------------------------------------|-----------------------------------------|----------------------------------------------------|
| 0.17.                                                              | $S_y = P(y)   V(y)$                                        | while true do {                         | while true do {                                    |
|                                                                    | $L_1 : P(s_0)   P(s_1)   P(s_2)$                           | $L_1 : P(s_0)   P(s_1)   P(s_2)$        | $L_2 : P(s_0)   P(s_1)   P(s_2)   P(s_3)$          |
|                                                                    | $L_2 : P(s_0)   P(s_2)   P(s_3)   P(y)$                    | $L_2 : P(s_0)   P(s_2)   P(s_3)   P(y)$ | $L_3 : P(s_0)   P(s_1)   P(s_2)   P(s_3)   P(s_4)$ |
|                                                                    | $x = x + 1;$                                               | $y = y + 1;$                            | $x = y - 1;$                                       |
|                                                                    | $y = y - 1;$                                               | $v(s_2);$                               | $v(s_4);$                                          |
|                                                                    | $v(s_1);$                                                  | $v(s_3);$                               | $v(s_x);$                                          |
|                                                                    |                                                            | }                                       | }                                                  |
| * Both processes should not be in suspended state at the same time |                                                            |                                         |                                                    |
|                                                                    | $S_0 = x \cancel{x} x \cancel{x} 1 \rightarrow x 1$        | (a)                                     | 000                                                |
|                                                                    | $S_1 = \cancel{x} \cancel{x} \cancel{y} 0 \rightarrow x 0$ | (b)                                     |                                                    |
|                                                                    | $S_2 = \cancel{x} x \cancel{y} 0 \rightarrow x 0$          |                                         |                                                    |
| Analysis:                                                          |                                                            |                                         |                                                    |
| Case 1:                                                            |                                                            |                                         |                                                    |
| $S_0 \rightarrow P_1 \rightarrow P_2 \rightarrow P_0$              |                                                            |                                         |                                                    |
| $S_1 = \cancel{x} \cancel{x} \cancel{y} 0$                         |                                                            |                                         |                                                    |
| $S_2 = \cancel{x} x \cancel{y} 1$ 000                              |                                                            |                                         |                                                    |
| Case 2:                                                            |                                                            |                                         |                                                    |
| $S_0 \rightarrow P_1 \rightarrow P_2 \rightarrow P_0$              |                                                            |                                         |                                                    |
| $S_1 = x \cancel{x} \cancel{y} 0$                                  |                                                            |                                         |                                                    |
| $S_2 = \cancel{x} \cancel{x} 1$ 00                                 |                                                            |                                         |                                                    |
| $S_3 = \cancel{x} x \cancel{y} 1$                                  |                                                            |                                         |                                                    |
| At least twice<br>(process wake up)                                |                                                            |                                         |                                                    |
| Case 3:                                                            |                                                            |                                         |                                                    |

WB  
Chap 3

Q.1.  $T_B = Q$

$$C.S. = T$$

I/O = R

$$\text{Efficiency} = \frac{\text{Useful time spent by CPU}}{\text{Total time spent by CPU}} = \frac{Q}{Q+T+R}$$

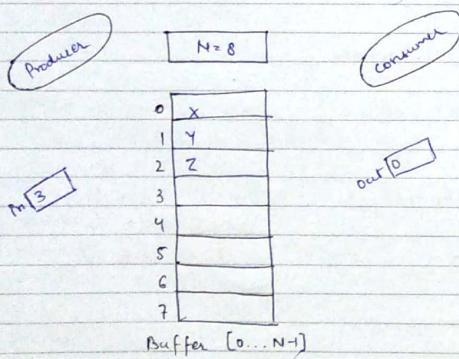
$\frac{Q}{Q+T+R} \rightarrow I/O \text{ is unpredictable}$   
 $\therefore \text{ignore it}$

- \* I/O
- ① I/O may occur alone
  - ② I/O may occur alongwith CPU
  - ③ Multiple I/Os may occur simultaneously.

27/09/2017

# Classical Problems of IPC:  
↳ Inter Process Communication.

I. Producer - Consumer with Semaphores:



Semaphore mutex = 1;

Semaphore Empty = N;

Semaphore Full = 0;

void producer (void)

{

int Item p;  
while (true)

{

produce\_item (item p)

down (Empty);

down (mutex);

Buffer [in] = item p;

in = (in + 1) mod N;

up (mutex);

up (Full);

y

}

void consumer (void)

{

int Item c;  
while (true)  
{  
down (Full);  
down (mutex);  
Item C = Buffer [out];  
out = (out + 1) mod N;  
up (mutex);  
up (Empty);  
process\_item (item C);  
}

- Mutex is a binary semaphore used by producer and consumer to access the buffer in a mutual exclusive manner.
- Empty is a counting semaphore variable representing the number of slots empty in the buffer at any point of time.
- Full is a counting semaphore variable representing the number of slots full in the buffer at any point of time.

Analysis:

mutex = 1 or 0 or 1

Empty = 8 X 8 X 5

Full = 8 X 8 X 3

8 8 8 5

Item p = X, B

Item C = X, Y

| in | out |
|----|-----|
| 1  |     |
| 2  | Z   |
| 3  | A   |
| 4  | B   |
| 5  | C   |
| 6  | D   |
| 7  | E   |

Q. What happens if we interchange down(empty), down(mutex) in the producer code.

- ④ No problem, the solution still works correct.
- ⑤ Both producer and consumer will access the buffer at the same time.
- ⑥ Some of the items produced by the producer will be lost.
- ⑦ It is possible for deadlock.

+ Buffer is full

mutex = 0

empty = 1

full = 2

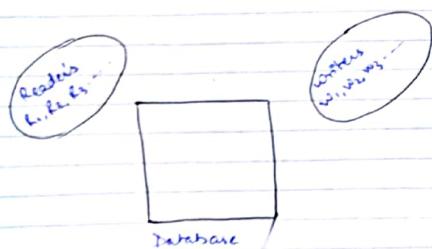
Q. What happens if we interchange up(mutex), up(full) in the producer code? [Same options as above]

- ⑧ mutex = 1
- ⑨ No problem, the solution still works correct.

Empty = 0

full = 2

## # READERS-WRITERS PROBLEM:



```
int rc = 0;  
Semaphore mutex = 1;  
Semaphore db = 1;  
void Reader(void)  
{  
    while (true)  
    {  
        down(mutex);  
        rc++;  
        if (rc == 1) down(db);  
        up(mutex);  
        D.B.  
        down(mutex);  
        rc--;  
        if (rc == 0) up(db);  
        up(mutex);  
    }  
}  
void writer(void)  
{  
    while (true)  
    {  
        down(db);  
        D.B.  
        up(db);  
    }  
}
```

# 4 conditions to be followed:

- ① R → W X
- ② R → R ✓
- ③ W → R X
- ④ W → W X

→ rc is the reader's count, represents the number of readers present in the database at any point of time.

→ mutex is a binary semaphore used by the readers in a mutual exclusive manner.

→ db is a binary semaphore used by readers and writers in a mutual exclusive manner.

Analysis(1):

rc = 0 X 2  
mutex = X X X 0  
db = X 0



Analysis(2):

rc = 0 1  
mutex = 1  
db = 1 0



Q. What happens if we interchange down(mutex), rc = rc + 1 in the reader's code?

④ No problem, the solution still works correctly.

⑤ multiple readers are NOT allowed into database at the same time.

⑥ Both reader and writer will enter into database at the same time.

⑦ It is possible for deadlock.

rc = 0 1  
mutex = X 0  
db = X 0



rc = 0 X 2  
mutex = X X 0  
db = X 0 X 0

Q. What happens if we interchange "if" condition and "up(mutex)" in the reader's code? (same options as above)

rc = 0 1

✓ Both reader and writer will enter into database at the same time.

mutex = X 0 1

db = 1

Q. What happens if we interchange "down(mutex)", "rc = rc - 1" in the reader's code?

rc = 0 X 1  
mutex = X X 1  
db = X 0

✓ It is possible for deadlock  
rc = 0 X 0 1  
mutex = X X 0  
db = X 0

WB Page 91

Q. 19. (1): down(mutex);

if (w==1)

{

up(mutex);

goto L1;

}

else

{ R=R+1;

up(mutex);

}

DB

down(mutex);

R=R-1;

up(mutex);

}

R = 0 X 1 X 0 1

w = 1 X 0 1

mutex = X X X 0 X 0 1

Q. 20. (d)

Q. 2: down (mutex),

if (w==1 or R>1)

{

up(mutex);

goto L2;

}

w=1;

up(mutex);

DB

down(mutex);

w=0;

up(mutex);

}

① up(mutex), up(mutex), w=1 or R>1

② R = 0 X 1 X 0 1

w = 1 X 0 1

mutex = X X X 0 X 0 1

③ R = 0 X 1 X 0 1

w = 0 X 0 1

mutex = X X X 0 X 0 1

④ R = 0 X 1 X 0 1

w = 1 X 0 1

mutex = X X X 0 X 0 1

⑤ R = 0 X 1 X 0 1

w = 0 X 0 1

mutex = X X X 0 X 0 1

⑥ R = 0 X 1 X 0 1

w = 1 X 0 1

mutex = X X X 0 X 0 1

⑦ R = 0 X 1 X 0 1

w = 0 X 0 1

mutex = X X X 0 X 0 1

⑧ R = 0 X 1 X 0 1

w = 1 X 0 1

mutex = X X X 0 X 0 1

⑨ R = 0 X 1 X 0 1

w = 0 X 0 1

mutex = X X X 0 X 0 1

⑩ R = 0 X 1 X 0 1

w = 1 X 0 1

mutex = X X X 0 X 0 1

⑪ R = 0 X 1 X 0 1

w = 0 X 0 1

mutex = X X X 0 X 0 1

⑫ R = 0 X 1 X 0 1

w = 1 X 0 1

mutex = X X X 0 X 0 1

⑬ R = 0 X 1 X 0 1

w = 0 X 0 1

mutex = X X X 0 X 0 1

⑭ R = 0 X 1 X 0 1

w = 1 X 0 1

mutex = X X X 0 X 0 1

⑮ R = 0 X 1 X 0 1

w = 0 X 0 1

mutex = X X X 0 X 0 1

⑯ R = 0 X 1 X 0 1

w = 1 X 0 1

mutex = X X X 0 X 0 1

⑰ R = 0 X 1 X 0 1

w = 0 X 0 1

mutex = X X X 0 X 0 1

⑱ R = 0 X 1 X 0 1

w = 1 X 0 1

mutex = X X X 0 X 0 1

⑲ R = 0 X 1 X 0 1

w = 0 X 0 1

mutex = X X X 0 X 0 1

⑳ R = 0 X 1 X 0 1

w = 1 X 0 1

mutex = X X X 0 X 0 1

㉑ R = 0 X 1 X 0 1

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w = 1 X 0 1

mutex = X X X 0 X 0 1

㉓ R = 0 X 1 X 0 1

w = 0 X 0 1

mutex = X X X 0 X 0 1

㉔ R = 0 X 1 X 0 1

w = 1 X 0 1

mutex = X X X 0 X 0 1

㉕ R = 0 X 1 X 0 1

w = 0 X 0 1

mutex = X X X 0 X 0 1

㉖ R = 0 X 1 X 0 1

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㉟ R = 0 X 1 X 0 1

w = 0 X 0 1

mutex = X X X 0 X 0 1

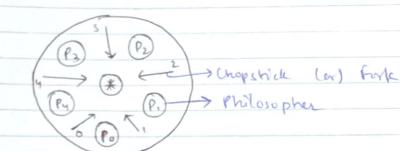
㉟ R = 0 X 1 X 0 1

w = 1 X 0 1

mutex = X X X

## #DINING PHILOSOPHERS:

$N = 5$



void philosopher (int i) // philosopher number

{

thinking();

take-fork(); // take left fork

take-fork((i+1)%N); // take right fork

eat();

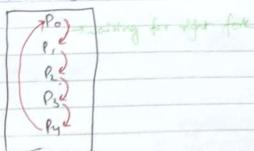
put-fork(i); // put left fork back

put-fork((i+1)%N); // put right fork back

}

}

→ If all the philosophers are hungry at the same time, then everybody will take their left fork first and when they try to attempt to take the right fork, nobody will get the right fork and all the philosophers will wait on each other and that leads to deadlock.



#define N

#define THINKING 0

#define HUNGRY 1

#define EATING 2 // left philosopher

#define LEFT (i+N-1)%N

#define RIGHT (i+1)%N // right philosopher

Semaphore mutex=1;

Semaphore S[N]; // all S[i]'s are

initialised to 0

int state[N]; // an array to keep track of everyone's state

void philosopher (int i)

// philosopher number

{

Thinking();

take-forks(i);

eat();

put-forks(i);

}

take-forks (int i)

{

down(mutex);

state[i] = HUNGRY;

test(i);

up(mutex);

down(S[i]);

}

put-forks (int i)

{

down(mutex);

state[i] = THINKING;

test(LEFT);

test(RIGHT);

up(mutex);

void test (int i)

{

if (state[i] == HUNGRY &

state[LEFT] != EATING &

state[RIGHT] != EATING)

{

State[i] = EATING;

up(S[i]);

}

- mutex is a binary semaphore used by the philosophers in a mutual exclusive manner.
- $S[0..N]$  is an array of binary semaphore, initially all are assigned to 0.
- State[N] is an integer array used to keep track of every philosopher's state. Initially, all the philosophers will be in the THINKING state.

Analysis:

$$\text{mutex} = 1001$$

$$P_0 = T$$

$$S[0] = 0$$

$$P_1 = T$$

$$S[1] = 0$$

$$P_2 = F \times E$$

$$S[2] = 0 \times 0$$

$$P_3 = T$$

$$S[3] = 0$$

$$P_4 = T$$

$$S[4] = 0$$

Q. Assume that  $P_1$  and  $P_3$  are in the eating state then the philosopher  $P_2$  is also trying to go into eating state, then which statement in the above code is controlling the philosopher?

- (A) down(mutex);
- (B) if condition
- (C) test condition
- (D) down(S[2]);

$$P_0 = T$$

$$S[0] = 0$$

$$P_1 = F$$

$$S[1] = 0 \times 0$$

$$P_2 = T$$

$$S[2] = 0$$

$$P_3 = F$$

$$S[3] = 0 \times 0$$

$$P_4 = T$$

$$S[4] = 0$$

$$\text{mutex} = 1$$

- Q. What happens if we interchange up(mutex), down(S[i]) in the take\_forces() function.
- (A) No problem, solution still works correct.
  - (B) More than 2 philosophers can go into eating state at the same time.
  - (C) Possible for deadlock.
  - (D) None of the above.

$$\text{mutex} = 1001$$

$$P_0 = T$$

$$P_1 = F \times E$$

$$P_2 = T$$

$$P_3 = F \times E$$

$$P_4 = T$$

$$S[0] = 0$$

$$S[1] = 0 \times 0$$

$$S[2] = 0$$

$$S[3] = 0$$

$$S[4] = 0$$

$(P_3 \quad P_4)$   
mutex

Q. 28/09/2017

Q. Let  $p[0] \dots p[4]$  be the processes and  $m[0] \dots m[4]$  be the binary semaphore mutexes all initialized to '1'. Each process  $'p_i'$  executes the following code:

|                         |                              |
|-------------------------|------------------------------|
| wait (m[2])             | $m[0] = 1 \times 0 \times 0$ |
| wait (m[(i+1) mod 4])   | $m[1] = 1 \times 0 \times 0$ |
| [C.S.]                  | $m[2] = + 1$                 |
| signal (m[1])           | $m[3] = 1 \times 0 \times 1$ |
| signal (m[(i+1) mod 4]) | $m[4] = 0 \times 1 \times 0$ |

Consider the following statements:

I. M.E. is satisfied.

II. M.E. is NOT satisfied.

III. It is possible for deadlock.

IV. Which of the following are TRUE?

(A) only I

(B) only II

(C) only I, II

(D) only II, III.

Q. Consider the following code used by the processes to access the common C.S.:

```
Shared boolean lock = FALSE;  
boolean key;  
do  
    key = TRUE;  
    while (key == TRUE)  
        swap(lock, key);  
    [C.S.]  
    lock = FALSE;  
} while (TRUE);
```

swap function atomically swaps two variables by using call by reference.

Consider the following statements:

I. M.F. is satisfied.

II. M.F. is NOT satisfied

III. It is possible for deadlock.

Which of the above are TRUE?

(A) only I

(B) only I, III

(C) only II

(D) only II, IV.

lock : FALSE ! F  
P<sub>1</sub> > key : TRUE ! F  
P<sub>2</sub> > key : FALSE !  
P<sub>3</sub> > key : T

lock : FALSE ! T  
P<sub>1</sub> | P<sub>2</sub> | P<sub>3</sub>  
key : T F | key : T

#### IV. PROGRAMMING LANGUAGE (COMPILER SUPPORT TYPE):

##### Monitors:

- Monitors is programming language compiler support type of solution to achieve synchronization.
- Monitors is collection of variables, own condition variables and procedures combined together in a special kind of module or package.
- The processes running outside the monitor cannot directly access the internal variables of the monitor but however, they can call procedures of the monitor.
- Monitors has an important property that only one process can be active inside the monitor at any point of time.

# Syntax: *Monitor* Example

```
variables;  
condition variables;  
procedure P1  
{  
}  
procedure P2  
{  
}
```

##### # Condition Variables:

###### Condition n, y;

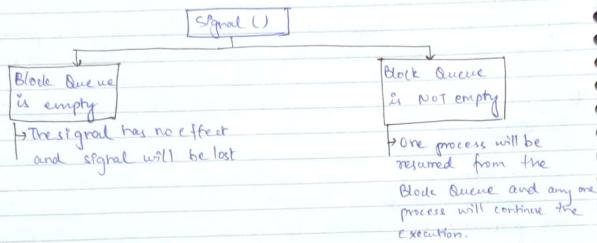
The two different operations will be performed on the condition variables of the monitor.

① wait();  
② signal();

wait():  $n.wait();$  (or)  $wait(n);$

→ The process performing wait() operation on any condition variable will be suspended and suspended process will be placed in the Block Queue of respective condition variable.

signal():  $n.signal();$  (or)  $signal(n);$



# Producer Consumer with monitors:

| Producer          | $N=8$ | Consumer |
|-------------------|-------|----------|
| 0                 | X     |          |
| 1                 | Y     |          |
| 2                 | Z     |          |
| 3                 |       |          |
| 4                 |       |          |
| 5                 |       |          |
| 6                 |       |          |
| 7                 |       |          |
| Buffer[0 ... N-1] |       |          |

### Monitor producer - consumer

```
int count = 0;
condition Empty, Full;
procedure Enter-Item,
{
    if (count == N) wait (full);
    enter (item);
    count = count + 1;
    if (count == 1) signal (empty);
}
```

```
procedure Remove-item
{
    if (count == 0) wait (empty);
    Remove (item);
    count = count - 1;
    if (count == N-1) signal (full);
}
```

### procedure producer

```
{ int item p;
while (TRUE)
    produce-item (item p);
    producer-consumer.Enter-item;
}
```

### procedure consumer

```
{ int item c;
while (TRUE)
    produces-consumer.Remove-item;
    process-item (item c);
}
```

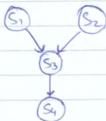
## NOTE

Even though we are using count variable, there will not be any inconsistency w.r.t. while updating the count variable because inside the monitor, only one process can be active at any point of time.

## # CONCURRENT PROGRAMMING:

S1:  $a = b + c$ ; Read set = {b, c, e, f, a, d, g, i};  
S2:  $d = e * f$ ;  
S3:  $g = a / d$ ; Write set = {a, d, g, h};  
S4:  $h = g * i$ ;

## Precedence Graph:



→ Any 2 statements "S<sub>i</sub>" and "S<sub>j</sub>" can be executed concurrently or parallelly if they are following the below conditions.

- ①  $R(S^o) \cap W(S^o) = \emptyset$
  - ②  $W(S^p) \cap R(S^o) = \emptyset$
  - ③  $W(S^p) \cap W(S^o) = \emptyset$

[NOT]

**NOTE** ↴ The real concurrent programming is possible only on the multi-processor system.

Concurrent: [3 meanings]:

→ They can execute concurrently or parallelly.

→ They don't have any dependency.

→ Anyone can start first.\*

→ The concurrent programming will be written by using:

|                             |            |
|-----------------------------|------------|
| par begin - par end<br>(or) | parallel   |
| co-begin - co-end           | concurrent |

```
begin  
    s1;  
    s2;  
    s3 i  
end
```

par begin  
S<sub>1</sub> ; S<sub>2</sub> ; S<sub>3</sub> ;  
par end

En

```

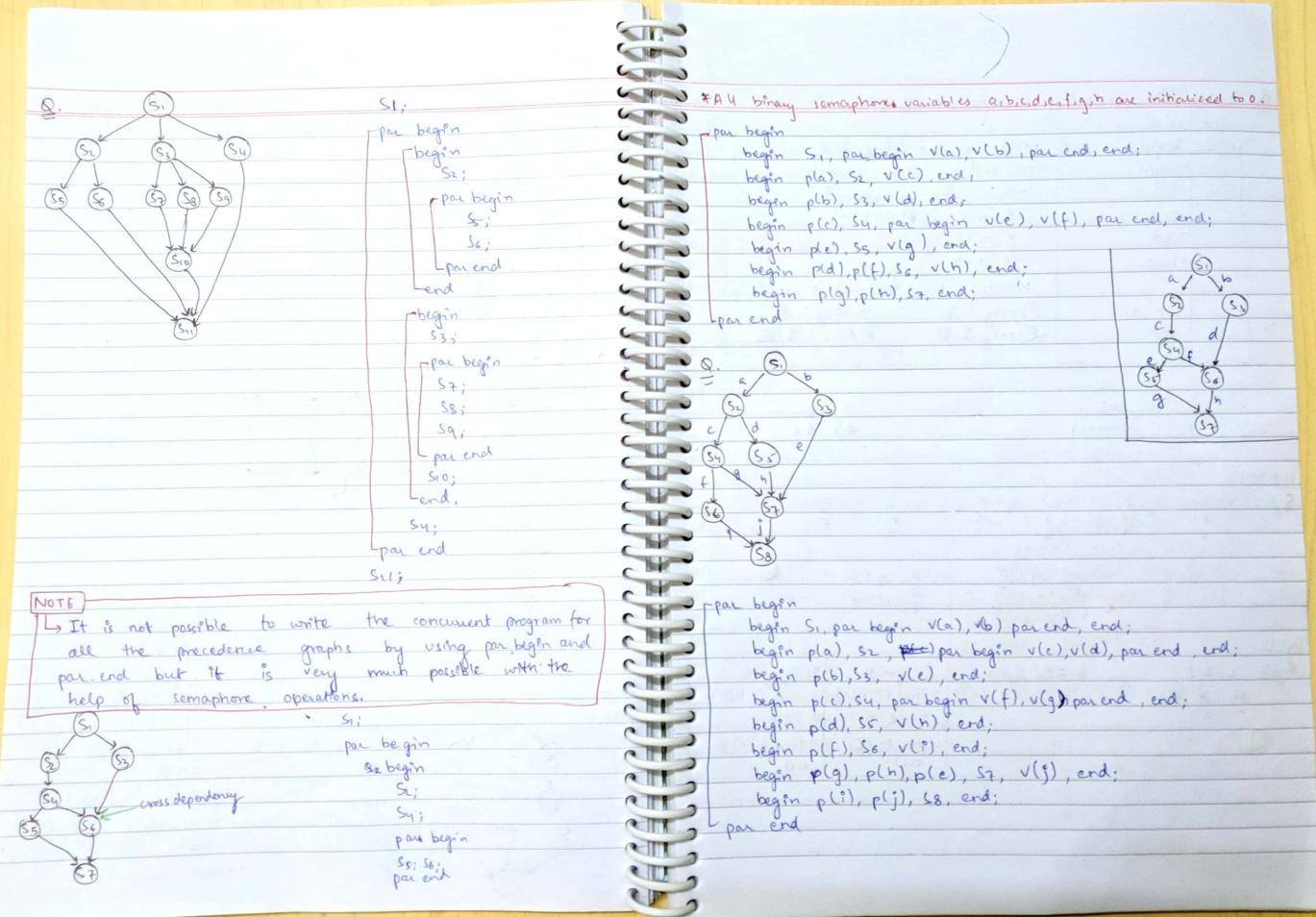
graph TD
    S0((S0)) --> S1((S1))
    S0 --> S2((S2))
    S1 --> S3((S3))
    S1 --> S4((S4))
    S3 --> S5((S5))
    S4 --> S5
    S5 --> S6((S6))
    S6 --> S0
  
```

begv  
S4;  
S5;  
end  
S6;  
S7;  
par end.  
S8;

```

graph TD
    S1((S1)) --> S2((S2))
    S1((S1)) --> S3((S3))
    S2((S2)) --> S4((S4))
    S3((S3)) --> S4((S4))
    S3((S3)) --> S5((S5))
    S4((S4)) --> S6((S6))
    S5((S5)) --> S6((S6))
    S6((S6)) --> S7((S7))
  
```

```
begin
  S1;
  par begin
    begin
      S2;
      S4;
    par begin
      S5;
      S6;
    par end
  end
  S3;
  par end
  S7;
end
```



Q. Consider the following concurrent program:

```
int x = 0, y = 0;
par begin
begin
x = 1;
y = y + x;
end
begin
y = 2;
z = x + 3;
end
par end
```

What can be the final values of 'x' and 'y' after completion of above concurrent program?

- I. x = 1, y = 2
  - II. x = 1, y = 3
  - III. x = 4, y = 6
- Which of the following above are possible?
- Ⓐ only I, II
  - Ⓑ only I, III
  - Ⓒ Only II, III
  - Ⓓ All I, II, III

$$\begin{array}{l} x=1 \\ y=0+1=1 \end{array}$$

$$\begin{array}{l} x=2 \\ y=0+3=3 \end{array}$$

$$\begin{array}{ll} x & y \\ 4 & 3 \\ 1 & 6 \end{array}$$

$$\text{Q.8. } \begin{array}{cccccc} x=\emptyset & y=\emptyset & z=\emptyset & y=\emptyset & z=\emptyset & y=\emptyset \\ x & x & x & x & x & x \\ 6 & 4 & 6 & 10 & 6 & 5 \end{array}$$

$$\begin{array}{cccccc} x=\emptyset & y=\emptyset & z=\emptyset & y=\emptyset & z=\emptyset & y=\emptyset \\ x & x & x & x & x & x \\ 6 & 4 & 6 & 4 & 8 & 5 \end{array}$$

Pg 92:

$$\text{Q.25. } \begin{array}{ll} x=\emptyset+2 & S=2XX+2 \\ x & x \\ * & * \end{array}$$

$$S=2XX+2$$

|                                        |                                        |
|----------------------------------------|----------------------------------------|
| $p_1(x), x$                            | $y, z_{P_1}(s)$                        |
| I. Load R <sub>1</sub> , M[x]          | I. Load R <sub>1</sub> , M[x]          |
| II. INCR R <sub>1</sub>                | II. DECR R <sub>1</sub>                |
| III. Store M[x], R <sub>1</sub> ; V(s) | III. Store M[x], R <sub>1</sub> ; V(s) |

(d)

S22

$x = \emptyset \rightarrow x \rightarrow x \neq x + 2$

Analysis:

W → I      R<sub>1</sub> [P1]

W → II

Y → I

Y → II      R<sub>1</sub> [P2]

Y → III

Z → I

Z → II      R<sub>2</sub> [Z = 4]

Z → III

W → III

X → I      R<sub>2</sub> [X = 2]

X → II

X → III

| W                               | X | Y                               | Z |
|---------------------------------|---|---------------------------------|---|
| I. Load R <sub>1</sub> , M[x]   |   | I. Load R <sub>1</sub> , M[x]   |   |
| II. INCR R <sub>1</sub>         |   | II. DECR R <sub>1</sub> (by 2)  |   |
| III. Store M[x], R <sub>1</sub> |   | III. Store M[x], R <sub>1</sub> |   |

Q. Consider the following concurrent program:

int count = 0;

void tally()

{

int i;

for (i = 1; i <= 5; i++)

count = count + 1;

}

y

main()

{

par begin

tally() → P<sub>1</sub>

tally() → P<sub>2</sub>

par end

}

y

what can be the minimum final value of count after completion of both tally() functions:

[NOTE] count = count + 1, will execute in 3 instructions like load, incr & store.

I. Load R<sub>0</sub>, M[count]

II. INCR R<sub>0</sub>

III. Store M[count], R<sub>0</sub>

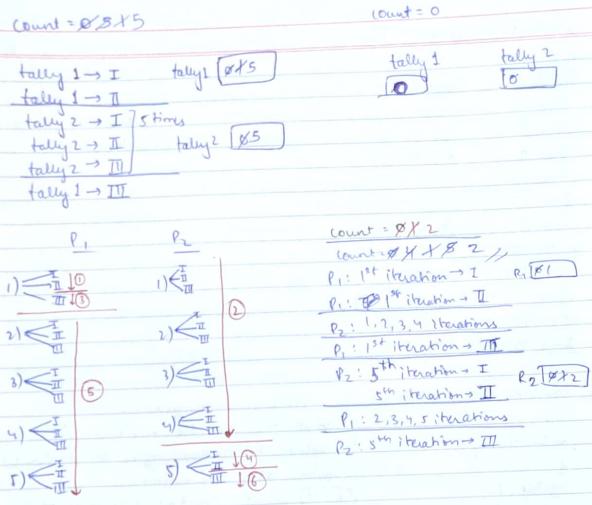
Ⓐ 1 Ⓑ 2 Ⓒ 3 Ⓓ 4 Ⓔ 5

count = ~~5~~ 0

tally 1

tally 2

0/1



# DEADLOCKS:

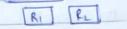
→ Two or more processes are waiting on some event to happen, which never happens, then those processes are said to be involved in the deadlock.

\* Basics of deadlocks:

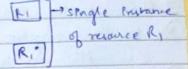
\* Processes



\* Resources



\* Resources with instances



\* Requesting Edge:

P<sub>1</sub> → Process P<sub>1</sub> is requesting for one instance of resource R<sub>1</sub>

P<sub>2</sub> → Process P<sub>2</sub> is requesting for 2 instances of resources R<sub>2</sub>

\* Allocation Edge:

P<sub>1</sub> → 1 instance of resource R<sub>1</sub> allocated to process P<sub>1</sub>

R<sub>2</sub> → 2 instances of resources R<sub>2</sub> allocated to process P<sub>2</sub>

NOTE

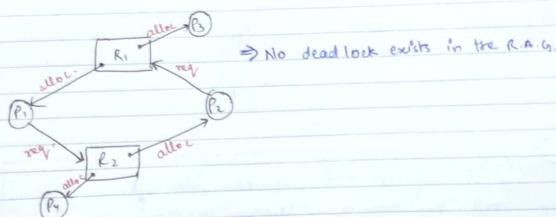
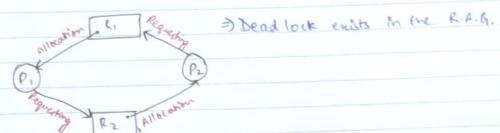
→ The resource request and resource allocation will be represented by resource allocation graph.

Resource Allocation Graph (R.A.G):  $G(V, E)$

processes, requesting  
resources

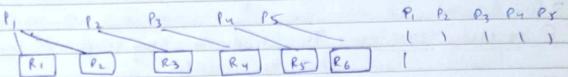
Allocation,

- \* The Resource Request / Release lifecycle:
- ① The process will make a request for the resource.
- ② O.S. clearly validates request of the process.
- ③ If the request made by the process is valid, then the O.S. will check for the availability of resource.
- ④ If the resource is freely available, then, it will be allocated to the process, otherwise, process has to wait.
- ⑤ If all the resources required for the execution are allocated, then, the process will go into execution.
- ⑥ Once the execution of the process is completed, then, the process will release all the resources.



Q.1. Consider a system which has ' $n$ ' processes and  $\frac{n}{2}$  tape drives and each process requires 2 tape drives, then to complete their execution. Then what is the maximum value of ' $n$ ' which ensures deadlock free execution.

④ 2      ⑤ 3      ⑥ 4      ⑦ 5



Q.2. Consider a system, which has 3 processes and each process requires 2 resources to complete their execution. Then what is the minimum no. of resources required to ensure deadlock free environment.

④ 2      ⑤ 3      ⑥ 4      ⑦ 5

Q.3. Consider a system, which has ' $n$ ' processes and 6 resources. Each process requires 3 resources to complete their execution. Then, what is the maxm value of ' $n$ ', which ensures deadlock free execution.

④ 2      ⑤ 3      ⑥ 4      ⑦ 5

Q.4. Consider a system, which has 3 processes  $P_1$ ,  $P_2$  &  $P_3$ . The peak demand of each process is 5, 9, 13 respectively for the resource  $R$ . Then what is the minm number of resources required to ensure deadlock free execution.

④ 22      ⑤ 23      ⑥ 24      ⑦ 25

$$P_1, P_2, P_3 \Rightarrow 5 + 9 + 13 = 27$$

WB Pg 98

Q. 23. P<sub>1</sub>, P<sub>2</sub>, P<sub>3</sub>, P<sub>4</sub> 20 resources.

|   |   |   |   |
|---|---|---|---|
| 4 | 3 | 7 | 9 |
| 3 | 2 | 6 | 8 |

→ In deadlock, we will use 4 conditions:

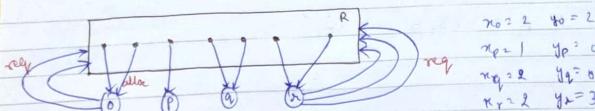
- ① necessary condition: The deadlock may be possible or may not be possible.  
 ② sufficient condition: The deadlock never be possible.  
 → The least upper bound which satisfies the condition is called as sufficient condition.

WB Pg 97

Q. 13. n resources      | P<sub>1</sub> = P<sub>n</sub>       $\sum_{i=1}^n S_i = m$       P = 4      m = 20  
 n processes      | S<sub>1</sub>      m = 17  
 Demand of P<sub>i</sub> → S<sub>i</sub>

|                          |                                         |                                                                                        |
|--------------------------|-----------------------------------------|----------------------------------------------------------------------------------------|
| (a) $\forall i, S_i < m$ | (b) $\forall i, S_i < n \times$         | (c) $\sum_{i=1}^n S_i = m$                                                             |
| $m = 10$                 | $P_1 = 9$<br>$P_2 = 9$<br>$P_{100} = 9$ | $\sum_{i=1}^n S_i = m - 1$<br>$\sum_{i=1}^n S_i = m - 1$<br>$\sum_{i=1}^n S_i < m - 1$ |

Q. 96.  
 Q. 10. n processes  
 $P_i \rightarrow R_j$  for R<sub>j</sub> is given  
 $P_i \rightarrow x_i$   
 $R_j \rightarrow y_j$



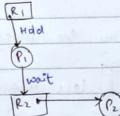
### # CONCEPTS OF DEADLOCKS.

- ① Deadlock Characteristics
- ② Deadlock Prevention
- ③ Deadlock Avoidance \*
- ④ Deadlock Detection
- ⑤ Deadlock Recovery

### \* Deadlock Characteristics:

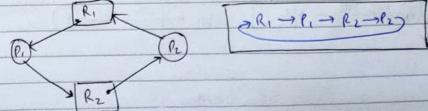
- ① Mutual Exclusion: The resource has to be allocated to only one process or it is freely available.
- There should be a one to one relationship between the resource and the process.

- ② Hold and Wait: The process is holding the resource and waiting on some other resource simultaneously.



- ③ No Preemption: The resource has to be "voluntarily" released by the process after completion of the execution.
- It is not allowed to forcefully preempt the resource from the process.

- ④ Circular Wait: The processes are circularly waiting on each other for the resources.



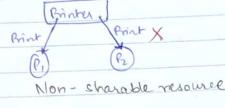
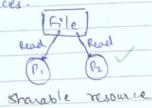
By disatisfying any of the 4 conditions we can prevent deadlock:

[NOTE]

If all the 4 conditions are existing simultaneously in the system, then, definitely, there exists a deadlock.

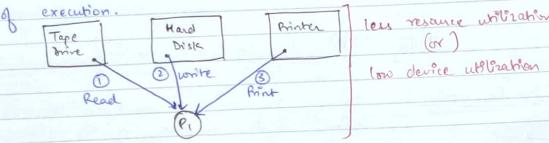
### \* Deadlock Prevention:

① Mutual Exclusion: It is not possible to disatisfy mutual exclusion always because of sharable and non-sharable resources.

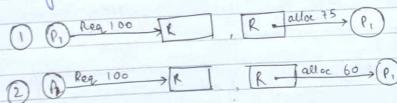


### ② Hold & Wait:

(1) Allocate all the resources required by the process before start of execution.



(ii) The process should release all the existing resources before making the new request.



Starvation

### ③ No Preemption:

The process 'P1' is requesting for resource 'R1'.

If the Resource R1 is free, then, it will be allocated to process P1.

The resource R1 is not free, and it is allocated to some other process P2.

If the process P2 is in execution, then the process P1 has to wait.

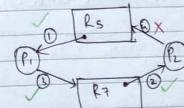
If the process P2 is NOT in execution & it is waiting on some other resource R2.  
→ Preempt Resource R2 from process P2 and allocate it to process P1.

### ④ Circular Wait:

→ The resources will be assigned with the unique numerical numbers.

→ The process can request for the resource only in the increasing (or decreasing) order of enumeration (numbering).

Increasing order: P1 → R2 | P1 → R3 | P1 → R4



| Total available          | Resources = A, B, C |
|--------------------------|---------------------|
| A B C<br>4 2 3<br>10 5 7 |                     |

Processes = P<sub>0</sub>, P<sub>1</sub>, P<sub>2</sub>, P<sub>3</sub>

#### Deadlock avoidance:

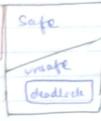
→ Deadlock avoidance is implemented by using Banker's algorithm.

| Max Need               | Current allocation |                |                | Current available |                |                | Remaining need |                  |                |                |                |                |  |
|------------------------|--------------------|----------------|----------------|-------------------|----------------|----------------|----------------|------------------|----------------|----------------|----------------|----------------|--|
|                        | P <sub>0</sub>     | P <sub>1</sub> | P <sub>2</sub> | P <sub>0</sub>    | P <sub>1</sub> | P <sub>2</sub> | P <sub>0</sub> | P <sub>1</sub>   | P <sub>2</sub> | P <sub>0</sub> | P <sub>1</sub> | P <sub>2</sub> |  |
| P <sub>0</sub> → 7 3 3 | 0 1 0              |                |                | 3 3 2             |                |                | 7 4 3          | → P <sub>0</sub> |                |                |                |                |  |
| P <sub>1</sub> → 3 2 2 | 2 0 0              |                |                | 5 3 2             |                |                | 1 2 2          | → P <sub>1</sub> |                |                |                |                |  |
| P <sub>2</sub> → 9 0 2 | 3 0 2              |                |                | 7 4 3             |                |                | 6 0 0          | → P <sub>2</sub> |                |                |                |                |  |
| P <sub>3</sub> → 2 2 2 | 2 1 1              |                |                | 7 5 3             |                |                | 0 1 1          | → P <sub>3</sub> |                |                |                |                |  |
| P <sub>4</sub> → 4 3 3 | 0 0 2              |                |                | 10 5 5            |                |                | 4 3 1          | → P <sub>4</sub> |                |                |                |                |  |
|                        | 3 2 5              |                |                | 10 5 7            |                |                |                |                  |                |                |                |                |  |

$$\text{Remaining} = \text{Max Need} - \text{Current allocation}$$

$$\text{Need} = \text{Max Need} - \text{Current allocation}$$

Safe sequence: The order in which we satisfy the remaining need of all the processes.



→ If we can satisfy remaining need of all the processes with the current available resources, then, the system is said to be in the safe state, otherwise system is said to be in the unsafe state.

→ If the system is in the unsafe state, then, it is possible for the deadlock.

→ Safe sequence may not be unique, there may be multiple safe sequences.

→ The deadlock avoidance is less restrictive than deadlock prevention.

→ The unsafe state purely depends on the behaviour of the processes.

| P <sub>0</sub> → 3 3 2 → | P <sub>1</sub> → 5 3 2 → | P <sub>2</sub> → 2 2 2 → |
|--------------------------|--------------------------|--------------------------|
| 2 0 0<br>5 2 2           | 2 1 1<br>2 4 3           | 2 2 2<br>2 5 3           |

→ Each & every time when the process is requesting for any resource, the banker's algorithm will be implemented to identify whether the system is in the safe state or unsafe state.

→ If the system is in the safe state, then, the request of the process will be granted and if the system is in the unsafe state then, the request of the process will be denied and the deadlock will be avoided.

Ques 2:

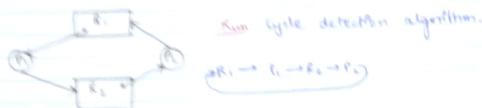
| Max                    | Allocated              | Available              | Remaining              |
|------------------------|------------------------|------------------------|------------------------|
| P <sub>0</sub> : 4 0 2 | P <sub>0</sub> : ABC   | P <sub>0</sub> : ABC   | P <sub>0</sub> : ABC   |
| P <sub>1</sub> : 6 5 4 | P <sub>1</sub> : 0 3 4 | P <sub>1</sub> : 4 3 1 | P <sub>1</sub> : 6 2 0 |
| P <sub>2</sub> : 3 4 2 | P <sub>2</sub> : 2 1 2 |                        | P <sub>2</sub> : 1 3 0 |
| P <sub>3</sub> : 1 0 4 | P <sub>3</sub> : 0 0 2 |                        | P <sub>3</sub> : 1 0 2 |
| P <sub>4</sub> : 3 2 5 | P <sub>4</sub> : 1 2 1 |                        | P <sub>4</sub> : 2 0 4 |

②

| P <sub>1</sub> → 4 3 1                                                     | P <sub>0</sub> → 6 4 3       | P <sub>2</sub> → 1 8 3 | P <sub>1</sub>         |
|----------------------------------------------------------------------------|------------------------------|------------------------|------------------------|
| 4 2 1 2<br>6 4 3                                                           | 1 0 3 4<br>6 7 7             | 6 3 9<br>3 9 9         | P <sub>1</sub> : 8     |
|                                                                            |                              |                        | P <sub>1</sub> : 6 4 3 |
| P <sub>2</sub> → 6 4 3                                                     | P <sub>2</sub> → 6 0 0 6 4 3 | P <sub>0</sub> → 6 4 5 | P <sub>0</sub> → 2 6 4 |
|                                                                            | 6 0 0 6 4 3<br>6 4 5         | 6 3 4<br>6 7 9         | P <sub>0</sub> → 2 6 4 |
|                                                                            |                              |                        | P <sub>2</sub> → 2 6 4 |
| P <sub>1</sub> : 6 4 3<br>P <sub>2</sub> : 6 4 3<br>P <sub>3</sub> : 1 8 3 |                              | 6 3 4<br>6 7 9         | P <sub>2</sub> → 2 6 4 |
|                                                                            |                              |                        | P <sub>2</sub> → 2 6 4 |
|                                                                            |                              |                        | P <sub>2</sub> → 2 6 4 |

## ~~Digraph Detection~~

① The advantage of single instance type



→ If all the resources are of single instance type, then cycle in the R.A.F. is necessary and sufficient condition for occurring of deadlock.

→ If all the resources are of NOT single instance type, the cycle in the RAB is just a necessary condition but not sufficient condition for the occurrence of deadlock.

② Resources are of multiple instance type.

| Current<br>Allocation  | Current<br>Available | Remaining<br>Need      | → what happens if the<br>process P <sub>2</sub> is requesting for<br>additional resources (P <sub>2</sub> , 0, 0, 1) |
|------------------------|----------------------|------------------------|----------------------------------------------------------------------------------------------------------------------|
| A B C                  | A B C                | A B C                  |                                                                                                                      |
| P <sub>0</sub> → 0 1 0 | → 0 0 0              | 0 0 0 → P <sub>0</sub> |                                                                                                                      |
| P <sub>1</sub> → 2 0 0 | ✗ 0 1 0              | 2 0 2 → P <sub>1</sub> |                                                                                                                      |
| P <sub>2</sub> → 3 0 3 | ✗ 3 1 3              | 0 0 0 → P <sub>2</sub> | P <sub>2</sub> → (0, 0, 1)<br>0 0 0 (old)<br>+ 0 0 1 (new)<br>0 0 1 (what)                                           |
| P <sub>3</sub> → 2 1 1 | → 5 1 3              | 1 0 0 → P <sub>3</sub> |                                                                                                                      |
| P <sub>4</sub> → 0 0 2 | → 7 2 4              | 0 0 2 → P <sub>4</sub> |                                                                                                                      |
|                        | 7 2 6                |                        |                                                                                                                      |

| Current alloc. | Current avail. | Remaining need. |             |
|----------------|----------------|-----------------|-------------|
| P1 → 0 1 0     | → 0 0 0        | 0 0 0           | P2 → unsafe |
| P1 → 2 0 0     | 0 1 0          | 2 0 2           |             |
| P2 → 2 0 3     |                | 0 0 1           |             |
| P2 → 2 1 1     |                | 1 0 0           |             |
| P2 → 0 0 2     |                | 0 0 2           |             |

## \* DEADLOCK RECOVERY:

## ① Killing the process:

- (a) Kill all the processes which are involved in the deadlock.
  - (b) Kill one after the other.

→ low priority processes

→ % of process completion

→ Number of resources, the process is holding.  $P_1$   $P_2$  Total

→ Number of resources the process is requesting.

→ Number of ~~remover~~, the process is going

② Resource Preemption: The resources will be preempted from the processes which are involved in the deadlock and the preempted resources will be allocated to some other process, so that, there may be a possibility of recovering the system from deadlock.

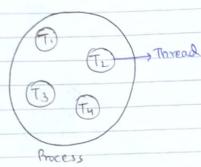
→ If the above condition is followed, then, there may be a possibility for the process to go into starvation.

③ Ostrich Algorithm: Ignore the deadlock.

### THREADS :

→ The light weight process.

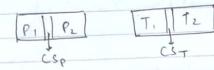
- No. of instructions will be less
- Context will be less



### # Advantages of Threads:

- ① Responsiveness: If the process is divided into multiple threads, then if one thread has completed its execution, then, the output will be responded immediately.  
• This response will be faster compared to the response of the process.

### ② Faster Context switches:



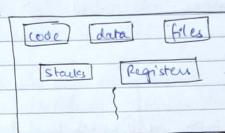
CSP <> CST

- The context switching time, b/w the threads will be very less compared to the context switching time between the processes because threads will have less context compared to processes.

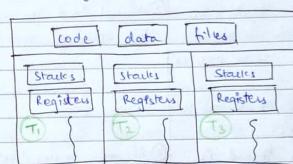
### ③ Effective utilization of multiprocessor system:

- If the process is divided into multiple threads, then, different threads can be scheduled onto different processors, so, that process execution will be faster.

### ④ Resource Sharing:



Single Threaded Process



Multi-threaded process.

- The resources [like code, data {global variables} and heap], files and memory will be shared among all the threads within the process but the stacks and registers cannot be shared and every thread will have its own stacks and registers.

- ⑤ Enhanced throughput of the system: If the process is divided into multiple threads and if we consider one thread as one job, then, number of jobs completed per unit time will increase and throughput of the system will be enhanced.

- ⑥ Economical: Implementation of threads does not require any cost and there are various programming language APIs which support implementation of threads.

E.g. JAVA API.

→ The threads are further categorized into 2 types:

- ① User level threads
- ② Kernel level threads.

#### User Level Threads

- ① User level threads are implemented by user / programmer.
- ② O.S. doesn't know about user level threads and it views user level thread as a process only.  
It means O.S. cannot recognize user level threads.
- ③ If one user level thread is performing (#) blocking system call, then, the entire process will go into block state.
- ④ User level threads are designed as dependent threads.
- ⑤ Implementation of user level threads is easy.
- ⑥ User level threads will have less context.
- ⑦ No hardware support required for the user level threads.

#### Kernel Level Threads

- ① Kernel level threads are implemented by the O.S.
- ② Kernel level threads are recognized by operating system.
- ③ If one kernel level thread is performing blocking system call, another thread will continue the execution.
- ④ Kernel level threads are designed as independent threads.
- ⑤ Implementation of kernel level threads is complicated.
- ⑥ Kernel level threads will have more context.
- ⑦ Scheduling requires hardware support.

#### NOTE

↳ Only scheduling is used in threads.

I/O Operation: I/O of the processes is categorised into 2 types:

- ① Synchronous I/O
- ② Asynchronous I/O

\* Synchronous I/O: In synchronous I/O, the process performing I/O operation, will be placed in the block state till the I/O operation is completed.

→ Once I/O operation is completed and, an Interrupt Service Routine (ISR) will be initiated, which brings the process from block state to ready state.

\* Asynchronous I/O: In asynchronous I/O, while initiating I/O request, the handler function will be registered.

→ The process is not placed in the block state and it continues to execute remaining code after initiating I/O request.

→ Once, the I/O operation is completed, the signal mechanism will be used to notify the process that the data is available and registered handler function will be asynchronously invoked.

Main mem  
Addressing mem  
Physical address  
Path

# MEMORY MANAGEMENT [William Stallings]  
\* functionality: Allocating and de allocating the memory to the processes.

\* Goal: The efficient utilization of memory by minimizing the internal and external fragmentation.

→ Memory will be represented in 2 different ways:

- ① Byte addressable E.g. 512 KB
- ② Word addressable E.g. 512 KW

$$\begin{array}{ll}
 2^2 = 4 & 2^8 = 256 \\
 2^3 = 8 & 2^9 = 512 \\
 2^4 = 16 & 2^{10} = 1024 \approx 1K \\
 2^5 = 32 & 2^{11} = 1M \\
 2^6 = 64 & 2^{12} = 1G \\
 2^7 = 128 & 2^{13} = 1T
 \end{array}$$

|   | ↑ 16 bits | Capacity of memory = No. of words * word size |
|---|-----------|-----------------------------------------------|
| 0 | 000       | = 8 words * 16 bits                           |
| 1 | 001       | = 8 * 2B                                      |
| 2 | 010       |                                               |
| 3 | 011       | = 16 Bytes.                                   |
| 4 | 100       |                                               |
| 5 | 101       |                                               |
| 6 | 110       |                                               |
| 7 | 111       |                                               |

Memory

Q. Consider a system which has 512 MWords and each words is having size of 128 bits, then what is the capacity of the memory in Bytes:  
 $512 \times 2^{30} \Rightarrow 2^{38} \Rightarrow 8 \text{ GB}$

Q. Consider a system which has 256 Gwords and each word is having 64 Bytes. Then what is the capacity of the memory in Bytes?  
 $2^{30} \times 2^6 = 2^{36} \times 2^{10} \Rightarrow 16 \text{ TB}$

Q. Consider a system where 32 binary bits are used to represent all the words of the mem and each word is having size of 32 bits, then what is the capacity of the mem in Bytes?  
 $2^{32} \times 2^3 = 2^{35} \Rightarrow 16 \text{ GB}$

### RAM Chip Implementation:

RAM Chip Size = 128 B

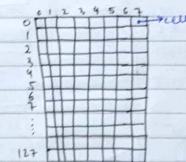
Organize the main memory capacity of 16 KB.

Q1. # of Ram chips required?

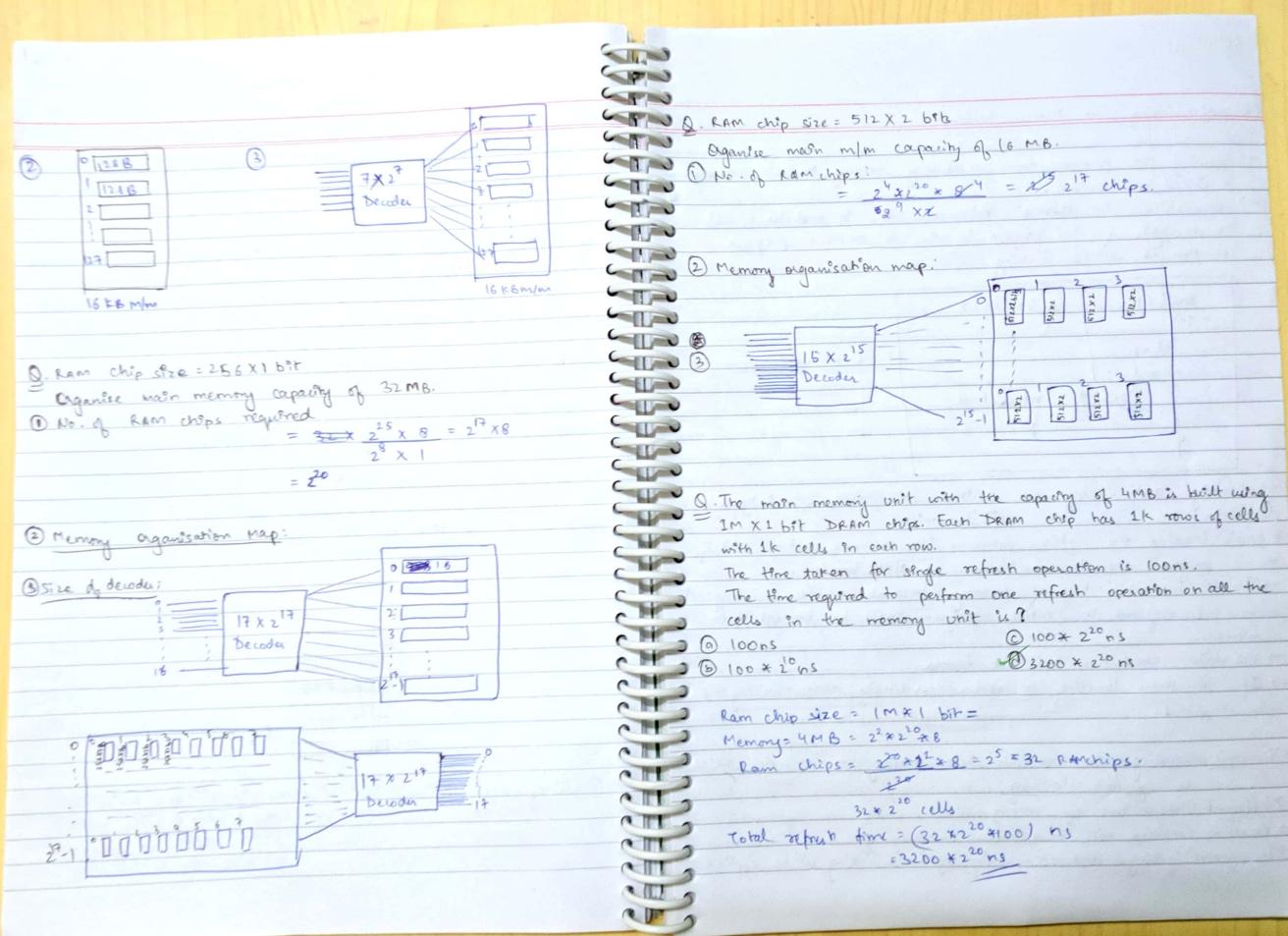
Q2. Draw the memory organisation map?

Q3. What is the size of the decoder required?

RAM chip size = 128 B



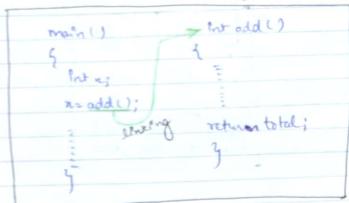
Q1. No. of Ram chips required =  $\frac{16 \text{ KB}}{128 \text{ B}} = \frac{2^{14} \text{ B}}{2^7 \text{ B}} = 2^7 = 128$



## 3. Loadings

### # Loading, Linking and Address Binding:

- Bringing the program from secondary memory to main memory is called as loading.
- Establishing the linking between all the modules or all the functions of the program in order to continue program execution is called linking.



→ Loading and linking are further categorized into 2 types:

① Static

② Dynamic

\* Static: Loading the entire program into memory before start of program execution is known as static loading.

→ Inefficient utilization of memory because whether it is required or not required, the entire program will be brought into memory.

→ Program execution will be faster.

→ If the static loading is used, accordingly, static linking will be applied.

\* Dynamic: Loading the program into memory on demand is called as dynamic loading.

→ Efficient utilization of memory.

→ Program execution will be slower.

→ If dynamic loading is used, accordingly, dynamic linking will be applied.

### # Address Binding:

→ Association of program instructions and data, to the actual physical memory locations is called as address binding.

→ Address binding is categorised into

3 types:

① Compile Time A.B.

② Load Time A.B.

③ Execution Time/Dynamic A.B.

|                      |    |
|----------------------|----|
| program's            | 1  |
| $I_1 \rightarrow 10$ | 2  |
| $I_2 \rightarrow 20$ | 3  |
| $I_3 \rightarrow 30$ | 4  |
| $I_4 \rightarrow 40$ | 5  |
|                      | 6  |
|                      | PI |

PC = 10, 20, 30, 40

Memory

### \* Compile Time Address Binding:

→ If the compiler is responsible of performing address binding, then it is called as compile time A.B.

→ This type of address binding will be done, before loading the program into memory.

→ Compiler requires to interact with the O.S. memory manager to perform compile time A.B.

### \* Load Time Address Binding:

→ This type of address binding will be done after loading the program into memory.

→ This type of address binding will be done by O.S. memory manager, i.e., loader.

### \* Execution Time/Dynamic Address Binding:

→ The address binding will be postponed even after loading the program into memory.

→ The program will keep on changing the locations in the memory till the time of program execution.

→ This type of address binding will be done by the processor at the time of program execution.

#### NOTE

↳ Majority of the O.S.s practically implement dynamic loading, dynamic linking and dynamic address binding.  
E.g. Windows, UNIX, Linux

#### # Memory Management Techniques:

##### Contiguous

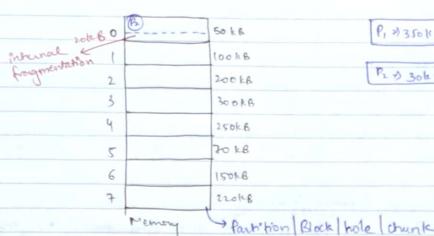
- Fixed partition scheme
- Variable partition scheme

##### Non-Contiguous

- Paging
- Multi-level paging
- Inverted paging
- Segmentation
- Segmented Paging

#### # CONTIGUOUS:

##### \* Fixed Partition Scheme:



- In the fixed partition scheme, memory will be divided into fixed number of partitions.
- fixed means, the number of partitions are fixed in the memory.
- In every partition, only one process will be accommodated.
- Degree of multiprogramming is restricted by no. of partitions in the memory.

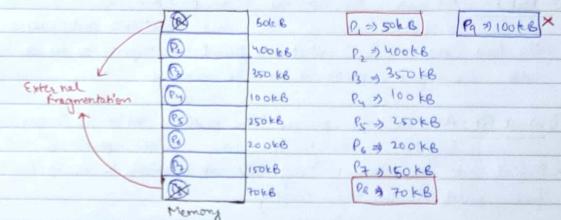
→ Maximum size of the process is restricted by maximum size of the partition.

→ Every partition is associated with the Unit Registers Limit Registers.

↳ Lower Unit: contains starting address of the partition.

↳ Upper Unit: contains ending address of the partition.

##### \* Variable Partition Scheme:



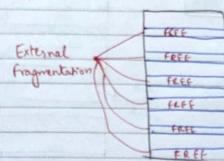
→ In the variable partition scheme, initially memory will be single continuous free block.

→ Whenever a process requires memory, accordingly, partition will be made in the memory.

→ If the smaller process requests keep on coming, then, the larger partitions will be made into smaller partitions.

→ To avoid the problem of external fragmentation, the following techniques are used:

- ① Compaction: Moving all the processes towards the top or towards the bottom to make free available memory in a single contiguous place.



→ Compaction is undesirable to implement because it interrupts all the running processes in the memory.

② Implementing non-contiguous memory management techniques:

# Partition Allocation Methods:

① First fit: Allocate the process in a partition which is first sufficient partition from top of the memory.

② Best fit: Allocate the process in a partition which is smallest sufficient among the free available partitions.

To find out the smallest sufficient, it requires to search all the free partitions in the memory.

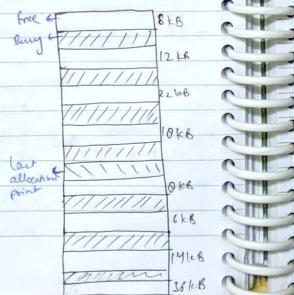
③ Worst fit: Allocate the process in a partition which is largest sufficient among the free available partitions.

To find out the largest sufficient, it requires to search all the free partitions in the memory.

④ Next fit: Next fit also works like first fit but it will search for first sufficient partition from last allocation point.

Q. Consider the following memory map:

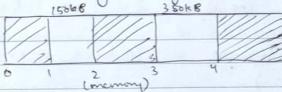
First fit → [22 kB]  
Best fit → [18 kB]  
Worst fit → [26 kB]  
Next fit → [26 kB]



Q. How many successive requests of 6 kB will be satisfied by using first fit, assuming variable partition scheme.

- Ⓐ 17 Ⓑ 18 Ⓒ 19 Ⓓ 20 Ⓔ 21

Q. Consider the following memory map:



The request from the processes are 300 kB, 25 kB, 125 kB, 50 kB respectively.

The above requests could be satisfied with? (Assume variable partition scheme is used).

- Ⓐ Both fit but NOT first fit  
Ⓑ First fit but NOT best fit  
Ⓒ Both first and best fit  
Ⓓ Neither first fit NOR best fit

### # Non-Contiguous Memory Management Technique:

\* Paging:

- (a) Logical Address Space (L.A.S.) or Virtual Address Space (V.A.S.)
  - ↳ Represented in the form of words or bytes. E.g. 512kB or 512B
- (b) Logical Address (L.A.) or Virtual Address (V.A.)
  - ↳ Represented in the form of bits. E.g. 19 bits, 32 bits
- (c) Physical Address Space (P.A.S.)
  - ↳ Represented in the form of words/bytes. E.g. 32kB or 32B
- (d) Physical Address (P.A.)
  - ↳ Represented in the form of bits. E.g. 15 bits

|                                                                                 |                                                                                       |                                                                    |                    |
|---------------------------------------------------------------------------------|---------------------------------------------------------------------------------------|--------------------------------------------------------------------|--------------------|
| E.g. ① L.A. = 20 bits<br>L.A.S. = $2^{20}$<br>= $2^8 \times 2^{12}$<br>= 256 MB | ② L.A.S. = 32 kB<br>L.A. = 15 bits<br>D.A.S. = $2^{12} \times 2^{12}$<br>= 4096 Bytes | ③ P.A. = 46 bits<br>D.A. = 15 bits<br>P.A.S. = $2^{46}$<br>= 64 TB | ④ P.A.S. = 12.8 GB |
|---------------------------------------------------------------------------------|---------------------------------------------------------------------------------------|--------------------------------------------------------------------|--------------------|

→ The technique of mapping CPU generated logical address to physical address is called as paging.

→ Paging is implemented in the hardware level.

→ If the logical address is the same as physical address, then no hardware support of paging is required.

① L.A. = 13 bits; No. of frames = 4

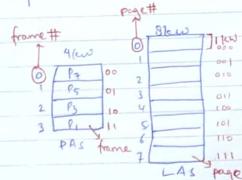
$$L.A.S. = 8 kB$$

$$PA = 12 bits$$

$$PAS = 4 kB$$

$$\text{Page size} = 1 kB$$

$$\text{No. of pages} = 8 = 8 \text{ pages}$$



→ Logical address space will be divided into equal size pages.

$$\text{No. of pages} = \frac{\text{L.A.S.}}{\text{Page size}}$$

→ Physical address space will be divided into equal size frames.

→ Page size will always be same as frame size.  $\boxed{\text{Page size} = \text{frame size}}$

$$\boxed{\text{No. of frames} = \frac{\text{P.A.S.}}{\text{frame size}}}$$

→ Some of the pages of L.A.S. will be brought into P.A.S.

→ Whenever the paging is applied, the page table has to be maintained.

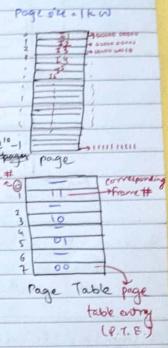
→ No. of entries in the page table is the same as number of pages in the L.A.S.

$$\boxed{\text{No. of P.T.E.} = \text{No. of pages in L.A.S.}}$$

→ Page table is also called as Address Translation Table.

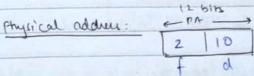
→ Page table entry definitely contains frame numbers.

→ Frame number is also called as Translation bit.



$P = \text{No. of bits required to represent pages of L.A.S. or page number}$   
 $d = \text{No. of bits required to represent page size or word no. of the page}$

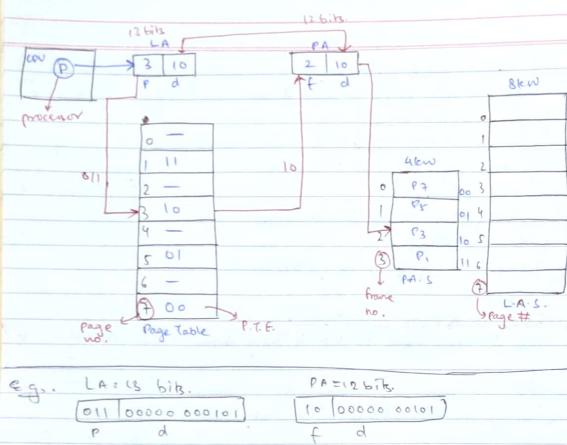
or page offset.



$f = \text{No. of bits required to represent frames of P.A.S. or frame number}$   
 $d = \text{No. of bits required to represent frame size or word no. of the frame}$

or frame offset

Windows Page Size = 4KB



- # Important Points:**
- Whenever the process is created, paging will be applied on the process and page table will be created and base address of the page table will be stored in the PCB.
  - Paging is with respect to every process and every process will have its own page table.
  - Page tables of the processes will be stored in the main memory.
  - There is no external fragmentation in paging.
  - Internal fragmentation exists in the last page and internal fragmentation is considered as  $\frac{P}{2}$ , where "P" is the page size.
  - Maintaining the page table is considered as overhead for the system.

#### NOTE:

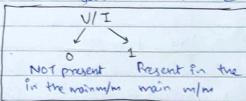
- Page table entry definitely contains frame number but sometimes along with a frame number, it may also contain additional bits like:
- Valid / Invalid bit or present bit
  - Dirty bit / Modified bit
  - Reference bit
  - Page protection bits or permission bits.

#### \* P.T.E.

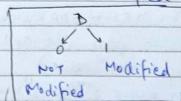
| F.No. | V/I | D | R | P.P. |
|-------|-----|---|---|------|
|       |     |   |   |      |

- Page Protection / Permission bits  
 → Reference bit  
 → Dirty / Modified bit  
 → Valid / Invalid / Present bit  
 → Frame No. / Translation bit

- # Valid / Invalid or Present bit: This bit is used to identify whether the page is currently available or not available in the main memory.



- # Dirty bit or Modified bit: used to identify whether the page is modified or not modified by the processor.



*(no. of reference bits is just fixed  
because for availability)*

# Reference bits: These bits are used to identify how many times, page is referred by the processor as part of the execution.

# Page Protection/permission bits: These bits are used for the protection and security from unauthorised access.

Q1. Consider a system which has logical address = 27 bits, and P.A. = 21 bits and page size is 4KB. Memory is word addressable. Then, calculate no. of pages and no. of frames.

$$LAS = 2^{27}$$

$$PA = 2^{21}$$

$$\text{No. of pages} = \frac{2^{27}}{2^{21}} = 2^6 = 64$$

$$PA = 2^{21}$$

$$\text{No. of frames} = \frac{2^{27}}{2^{21}} = 2^6 = 64$$

Q2. Consider a system which has no. of pages as 8K and page size = 16KB and mem. is word addressable. P.A. = 22 bits. Then calculate logical address and no. of frames.

$$PA = 2^{22}$$

$$\text{No. of frames} = \frac{2^{22}}{2^{14}} = 2^8 = 256$$

$$LAS = 8 \times 2^{10} + 16 \times 2^{10} = 2^{27}$$

$$LA = 27 \text{ bits.}$$

Q3. Consider a system which has LAS = 17.8MW, PA = 24 bits, PMS divided into 8K frames, then, what is the page size and how many pages in the LAS? (memory is word addressable)

$$LA = 17.8MW, PA = 2^{24}W, \text{frame size } \leq 2^{19} \leq 2^{11} \text{ words} = 2K W$$

$$\text{No. of pages} = 12 = 64$$

④ Consider a system, L.A. = 32 bits; PMS = 64MB; Memory is byte addressable and page size = 4KB. Then, what is approximate size of page table in bytes.

$$LAS = 2^{32}$$

$$PA = 2^{28}$$

$$\text{No. of pages} = 2^{28}$$

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2marks  
GATE 2016

Q. Consider a system which has logical address of 40 bits and page size 16 kB and memory byte addressable.

PTE size = 48 bits. Then what is page table size

in MB?

$$LAS = 2^{10} B$$

$$\text{No. of pages} = \frac{2^{40}}{2^{10}} = 2^{26}$$

$$\text{Page table size} = 6 \times 2^{26} = 354 \times 2^{10} = 354 \text{ MB}$$

GATE 2015 2-marks

Q. Consider a system which has page size = 8 kB and PA = 32 bits and memory is byte addressable and page table size = 24 MB. P.T.E. contains a valid bit, a dirty bit, 3 permission bits and translation bits. What is the logical address supported by the system in bits.

$$PAS = 2^{32} B$$

$$\text{Page size} = 2^{13}$$

$$\text{No. of frames} = 2^9 \text{ frames} = 19 \text{ translation bits.}$$

$$\text{PTE size} = 24 \text{ bits} = 3B$$

$$\# \text{ PTE} = \frac{2^{24}}{2^3} = 8M \Rightarrow \text{No. of pages} = 2^{23}$$

$$LAS = 2^{23} + 2^{13} = 2^{26}$$

$$LA = 2^{32} \text{ bits.}$$

Q. Consider a system which has LAS = PAS = 5 bytes. Page size = P bytes. PTE size = 8 bytes. Then, what is the optimal value of page size by minimizing the memory overhead by maintaining page table size and internal fragmentation in the paging [memory is byte addressable].

$$\textcircled{a} \quad P \leq 8$$

$$\textcircled{b} \quad P \geq 8$$

$$\textcircled{c} \quad p \leq 5$$

$$\textcircled{d} \quad p = \sqrt{256}$$

$$LAS = S \text{ bytes} \quad \text{Page table size} = \frac{S}{P}$$

$$PAS = s \text{ bytes}$$

$$\text{Page size} = P \text{ bytes}$$

$$\text{No. of pages} = \frac{S}{P}$$

$$\text{PTE size} = 8 \text{ bytes}$$

$$\text{No. of frames} = \frac{S}{P}$$

$$\text{PTE size} = \frac{S}{P} \times 8$$

Memory overhead = Page Table size + Internal fragmentation in paging

$$= \frac{S}{P} + \frac{P}{2}$$

$$\therefore d \left( \frac{S}{P} + \frac{P}{2} \right) = 0 \Rightarrow -\frac{S}{P} + \frac{1}{2} = 0$$

$$\therefore \frac{S}{P} = \frac{1}{2} \quad \boxed{P = 512}$$

#### # Performance of Paging:

→ Main memory access time = m

Page tables are stored in the main memory.

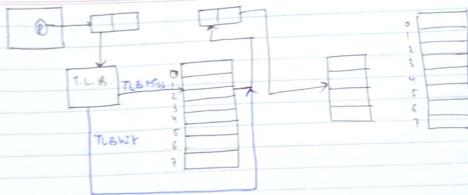
Then, the formula for effective memory access time = 2m

→ The translation lookaside buffer (TLB) is added to improve the performance of paging.

→ TLB is a hardware device, which is implemented by using associative registers.

→ TLB access time will be very less compared to main memory access time.

→ TLB contains frequently referred page numbers and corresponding frame numbers.



$\Rightarrow$  TLB access time = C

$$\text{TLB hit ratio} = x$$

Then, the formula for effective memory access time

$$E.M.A.T. = x(c+m) + (1-x)\cancel{c} (c+2m)$$

Q Consider a system which has main memory access time = 10 ns and TLB access time = 20 ns ; TLB hit ratio is 95%. Then what is the E.M.A.T with TLB and upto TLB.

vol o TLB

$$EMAT = 2 \times 100 \approx 200 \text{ ns}$$

with TIB

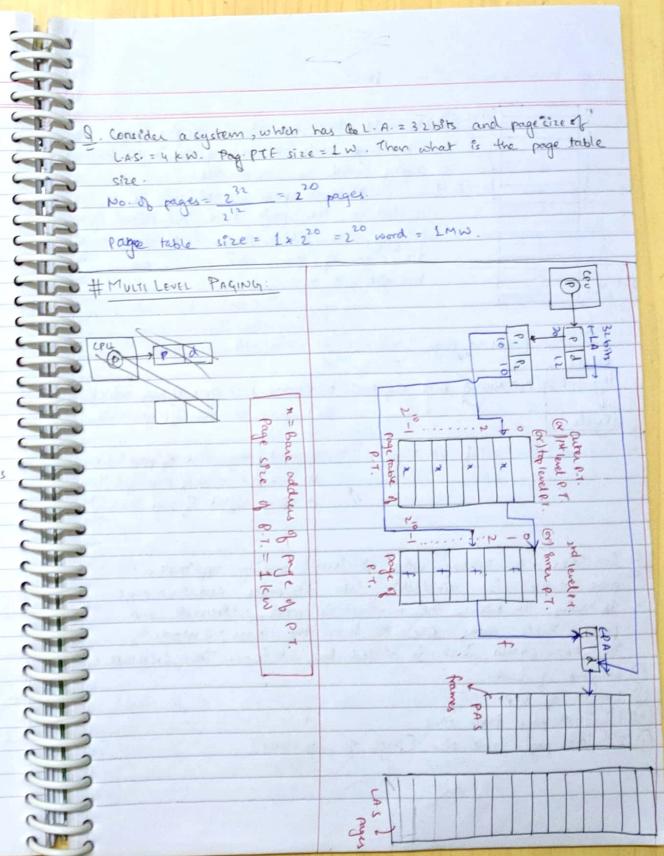
$$EMAT = 0.95 * (20) + (0.05) * (220) \\ = 114 + 11 = 125 \text{ ns},$$

Q. How much hit ratio is required to reduce EMAT from 300ns into TLB, to 250 ns with T-LB. The TLB access time = 60ns.

Mean access time = 150 n

四百三

$$150n = 110 \Rightarrow n = \frac{11}{15} = 0.7333 = 73.33\%$$



$$\text{Page table size} = 2^{20} w = 1 \text{ MW}$$



① To avoid the overhead of bringing large size page table into memory, the multi-level paging will be implemented.

② In multi-level paging, paging will be applied on the page table and instead of bringing the entire page table into memory, the pages of page table will be brought into memory.

$$\text{No. of pages on page table} = \frac{2^{20} w}{2^{10} w} = 2^{10} = 1 \text{ K}$$



P<sub>1</sub> = No. of bits required to represent pages of page table  
(or) page number of page table

P<sub>2</sub> = No. of bits required to represent page size of page table  
(or) word number of page of P.T.  
(or) page offset of page table.

Q Consider a system using 2-level paging applicable. The page table is divided into 16K pages and each page is having 4K entries. The memory is word addressable and page table entry size in both the levels = 2 words.

The PAG = 64MW, which is divided in 16K frames. Then calculate:

① Length of L.A.

② Length of P.A.

③ 1st level page table size

④ 2nd level page table size [page of page table]

$$\text{No. of pages of page table} = \frac{2^{20}}{2^10} = 2^11 \text{ pages}$$

$$\text{Size of page of P.T.} = 4 \text{ K} = 2^{12}$$

$$\text{P.T. size} = 2^W$$

$$\text{PMS} = 2^{21} w$$

$$\# frames = 2^M$$

$$\text{frame size} = \frac{2^{10}}{2^{11}} = 2^12 w$$

$$① \text{Length of L.A.} = 35 \text{ bits}$$

$$② \text{Length of P.A.} = 26 \text{ bits}$$

$$③ 1^{\text{st}} \text{ level page table size} = 2^{11} \times 2 = 2^{12} w = 4 \text{ K w}$$

$$④ 2^{\text{nd}} \text{ level page table size} = 2^{12} \times 2 = 8 \text{ K w}$$

Q Consider a system with 2-level paging applicable. The page table is divided into 8K pages and each page is having 16K entries. Memory is page addressable. P.T.E size = 31 bits. In both the levels. The PAG = 128 MB, which is divided into 4KB frames. Then calculate:

① Length of L.A.

② Length of P.A.

③ 1st level P.T. size

④ 2nd level P.T. size [page of P.T.]

$$① \boxed{27-48/12} \quad \text{PAG} = 128 \text{ MB} \quad \text{frame size} = 2^12 w = 2^{12} B$$

$$\# \text{frames} = \frac{2^{27}}{2^{12}} = 2^15$$

$$\text{Length of L.A.} = 42 \text{ bits } 39 \text{ bits}$$

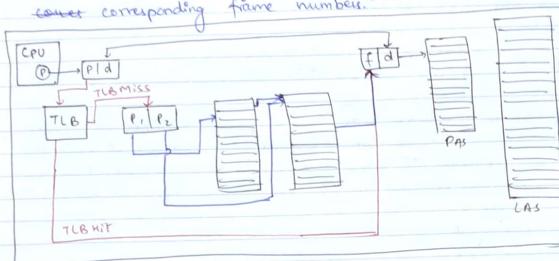
$$② \text{Length of P.A.} = 27 \text{ bits}$$

$$③ 1^{\text{st}} \text{ level P.T. size} = \frac{1}{2} \times 2^{13} = 2^{15} B = 32 \text{ KB}$$

$$④ 2^{\text{nd}} \text{ level P.T. size} = \frac{1}{2} \times 2^{14} = 2^{16} B = 64 \text{ KB}$$

### # Performance of 2-level Paging:

- ⇒ Main memory access time = 'm'  
 The page tables are stored in the main memory.  
 Then, the formula for effective memory access time =  $3m$
- ⇒ The T.L.B. is added to improve the performance of paging.  
 T.L.B. contains frequently referred page numbers and  
 their corresponding frame numbers.



- ⇒ TLB access time = 'c' and TLB hit ratio = 'x'.  
 Then, the formula for Effective Memory Access Time :

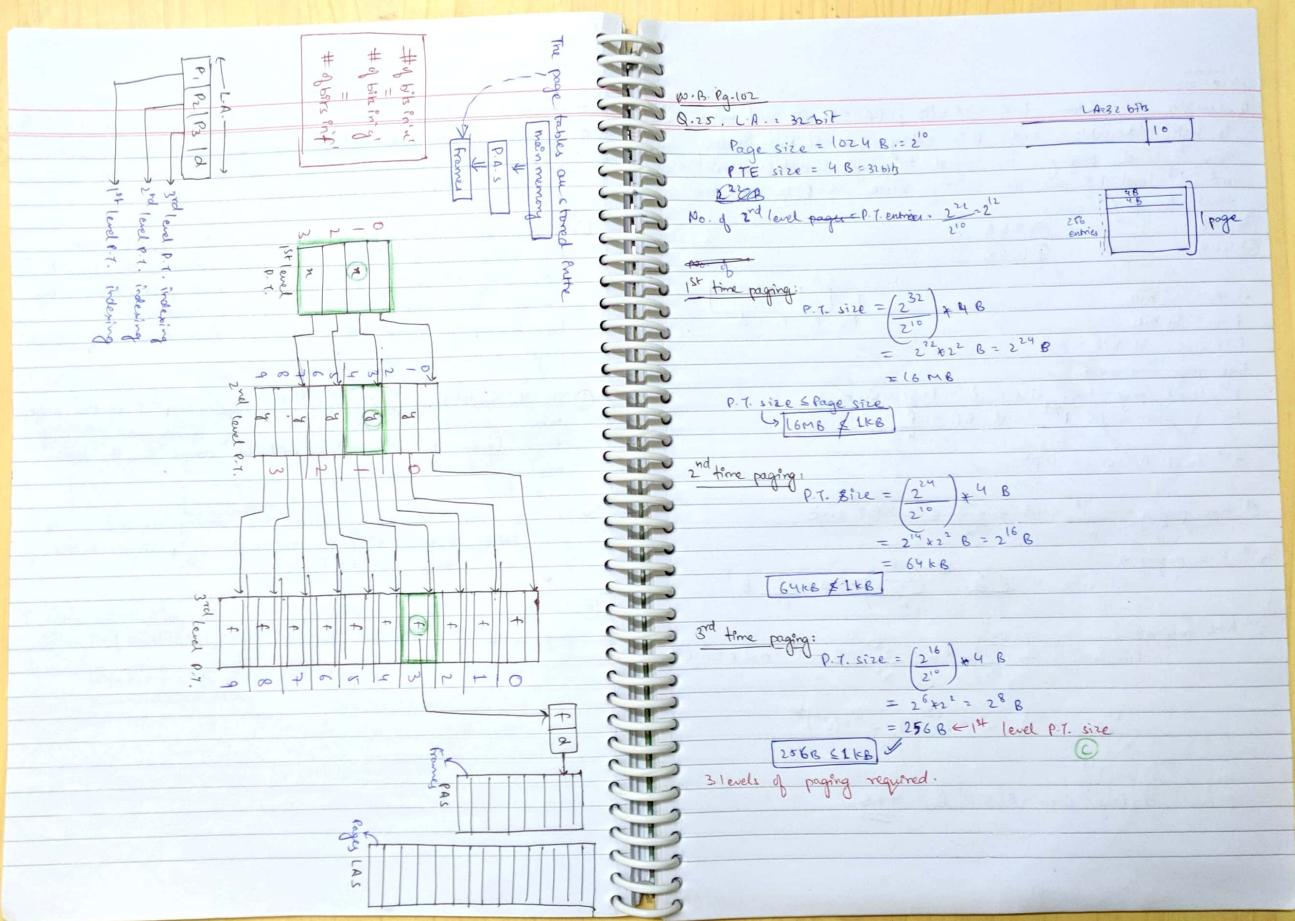
$$EMAT = x(c+m) + ((1-x)(c+3m))$$

$$EMAT = x(c+m) + ((1-x)(c+(n+1)*m))$$

↓  
n-level paging

### # Important Points:

- ① In the multi level paging when the paging applied on the page tables, the last page table which we get is called as First level page table.
- ② In the multi level paging, when the paging applied on the page tables, the first level page table entry contains base address of 2<sup>nd</sup> level page table, 2<sup>nd</sup> level page table entry contains base address of 3<sup>rd</sup> level page table and so on. The final page table's entry contains frame number of actual page.
- ③ In the multi level paging, when the paging applied on the page tables, whatever may be the levels of paging, all the page tables [page of page table] will be stored in the main memory.
- ④ In the multi level paging, when the paging applied on the page tables, whatever may be the levels of paging, all the page table entries contain frame number.
- ⑤ If the page size is not mentioned in the problem, generally, page size will be same in all the places [levels].



Q.25, Pg.102

Q.25, L.A. = 32-bit

$$\text{Page size} = 1024 \text{ B} = 2^{10}$$

$$\text{PTE size} = 4 \text{ B} = 31 \text{ bits}$$

2<sup>32</sup>B

$$\text{No. of } 2^{\text{14}} \text{ level pages} = \text{P.T. entries} \cdot \frac{2^{24}}{2^{10}}$$

LA=32 bit

| 10 |

256 entries

1 page

1<sup>st</sup> time paging:

$$\begin{aligned} \text{P.T. size} &= \left(\frac{2^{32}}{2^{10}}\right) \times 4 \text{ B} \\ &= 2^{12} \times 2^2 \text{ B} = 2^{14} \text{ B} \\ &= 16 \text{ MB} \end{aligned}$$

P.T. size > Page size  
↳ 16MB > 1KB

2<sup>nd</sup> time paging:

$$\begin{aligned} \text{P.T. size} &= \left(\frac{2^{14}}{2^{10}}\right) \times 4 \text{ B} \\ &= 2^4 \times 2^2 \text{ B} = 2^{10} \text{ B} \\ &= 64 \text{ KB} \end{aligned}$$

64KB > 1KB

3<sup>rd</sup> time paging:

$$\begin{aligned} \text{P.T. size} &= \left(\frac{2^4}{2^{10}}\right) \times 4 \text{ B} \\ &= 2^0 \times 2^2 \text{ B} = 2^2 \text{ B} \\ &= 256 \text{ B} < 1^{\text{st}} \text{ level P.T. size} \end{aligned}$$

256B < 1KB

3 levels of paging required.

Ques no. 103

Q. Consider a system, L.A. = 46 bits; P.A. = 32 bits and main memory is byte addressable and P.T. entry size = 32 bits. The O.S. uses 3 level paging for logical to physical address translation and 1st level P.T. size is exactly same as page size. Then what is page size.

(A) 2 kB  
(B) 4 kB

(C) 8 kB  
(D) 16 kB

$$L.A. = 46 \text{ bits}$$

$$P.A. = 32 \text{ bits}$$

$$P.T. \text{ size} = 32 \text{ bits} = 4 \text{ B}$$

1st page size = ~~4 B~~

1st level page table size =  $P = \text{Page size}$

No. of entries in 1st level P.T. =  $\frac{P}{4}$

2nd level P.T. size =  $\frac{P^2}{4}$

$$2^{\text{nd}} \text{ time paging} = 2^{46} \times 4 \text{ B} = \frac{2^{48}}{n} \text{ B} \Rightarrow P.T. \text{ size}$$

$$2^{\text{nd}} \text{ time paging} \Rightarrow P.T. \text{ size} = \frac{2^{48}}{n} \times \left( \frac{2^{32}}{n} \right) \times 4 \text{ B} = \frac{2^{50}}{n^2} \text{ B}$$

3rd time paging

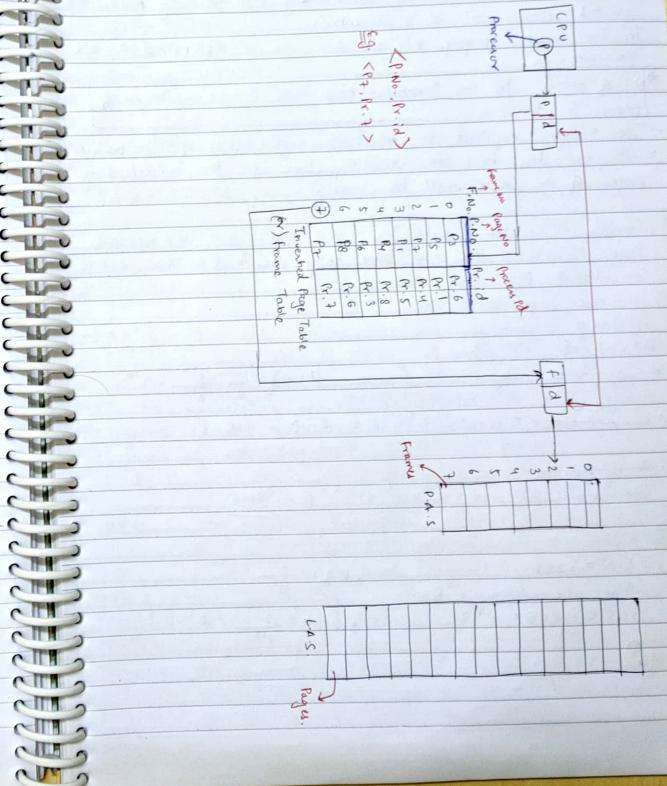
$$P.T. \text{ size} = \frac{2^{50}}{n^2} \times 4 \text{ B} = \frac{2^{52}}{n^3} \text{ B} \leftarrow 1^{\text{st}} \text{ level P.T. size}$$

$$\frac{2^{52}}{n^3} = n \Rightarrow n^4 = 2^{52} \Rightarrow n^4 = (2^3)^{17}$$

$$n = 2^{13}$$

$$\therefore \text{Page size} \times B = 2^{13} \text{ B} = 8 \text{ kB}$$

### # Inverted Paging



⇒ To avoid the overhead of maintaining P.T. for every process, the inverted paging will be implemented.

In the inverted paging, only one P.T. will be maintained for all the processes.

No. of entries in the inverted page table is same as the no. of frames in the P.A.S.

→ The memory required to maintain page tables of the processes will be less but the searching time for the corresponding page of a process will be more.

Q. Consider a system which has L.A. = 34 bits and P.A. = 20 bits. Page size = 16KB. The page table entry size is 8B. Then calculate

① Conventional Page table size.

② Inverted page table size.

$$P.A.S = 2^{29} B$$

$$\text{No. of frames} = \frac{2^{34}}{2^{14}} = 2^{15} \text{ frames. } | \text{No. of pages} = \frac{2^{34}}{2^{11}} = 2^{20}$$

$$\text{Inverted conventional P.T. size} = 2^{15} \times 8 = 2^{18} B = 256 kB$$

① No. of pages =

$$\text{Conventional P.T. size} = 2^{10} \times 2^3 = 2^{13} B = 8 MB$$

Ques:

$$L.A. = 32 bits$$

$$\text{Page size} = 4 KB = 2^{12} B$$

$$P.A.S = 128 KB = 2^{17} B$$

$$\text{No. of frames} = \frac{2^{17}}{2^{12}} = 2^5$$

④

W.B.

Page 100

Q. 5. Page size = 4 KB

L.A. = 32 bits

P.A. = 30 bits

Overhead bits = 12

$$\text{No. of frames} = \frac{2^{30}}{2^{12}} = 2^{18} \text{ frames.}$$

$$\text{No. of pages} = \frac{2^{12}}{2^{12}} = 2^{20} \text{ pages. } \rightarrow 20 \text{ bits}$$

→ bits to represent page no.

$$\text{⑧ Inverted PTE size} = 20 + 12 = 32 bits$$

$$= 4 B$$

$$\text{Inverted P.T. size} = 2^{18} \times 4 = 2^{20} B$$

# Segmentation

→ Paging does not follow user's view of memory allocation.

→ To achieve user's view of memory allocation, the segmentation will be implemented.

→ In the segmentation, L.A.s will be divided into various segments.

→ Segments of L.A.s will vary in the size.

→ Segments of L.A.s will be brought into P.A.S.

S = No. of bits required to represent segments of L.A.S.

(or) segment number

d = No. of bits required to represent segment size (or)

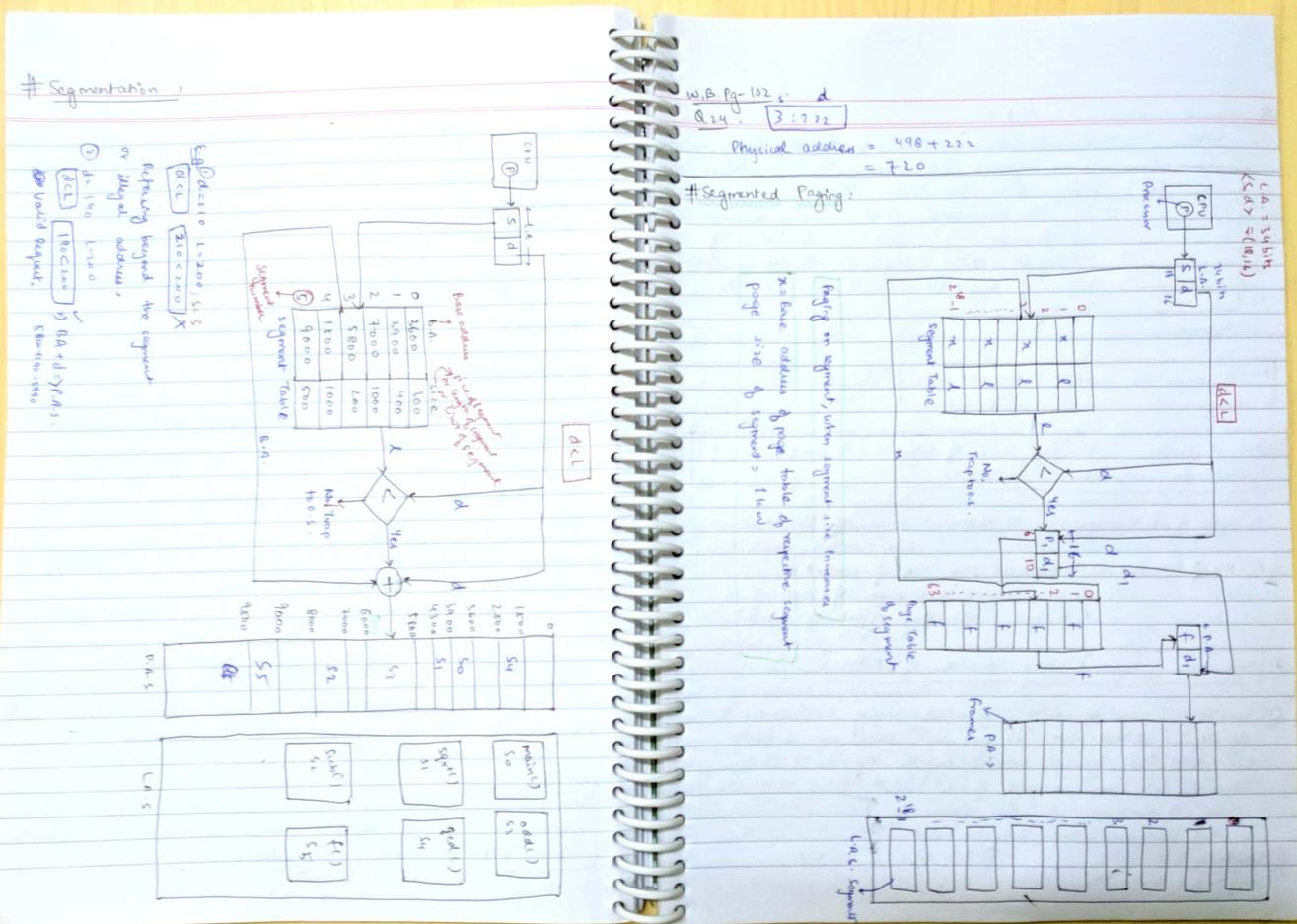
word number of the segment (or)

segment offset.

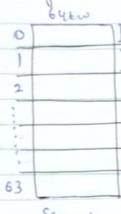
⇒ No. of entries in the segment table is same as number of segments in the L.A.S.

NOTE

Variable size segments are brought from L.A.S. to P.A.S., so, it is behaving similar to variable partition scheme. Hence, segmentation still suffers from external fragmentation.



# Segment size =  $2^{16} W = 64 \text{ kW}$



→ To avoid the overhead of bringing large size segment into memory, the segmented paging will be implemented.  
→ In the segmented paging, paging will be applied on the segment and instead of bringing the entire segment into memory, the pages of segment will be brought into memory.

$$\text{No. of pages on segment} = \frac{\text{segment size}}{\text{page size}} = \frac{64 \text{ kW}}{1 \text{ kW}} = 64$$

⇒ No. of entries in the page table of segment is same as no. of pages on segment.

$$P_1 = \text{No. of bits required to represent pages of segment (or)} \\ \text{page number of segment}$$

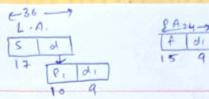
$$d_1 = \text{No. of bits required to represent page size of segment (or)} \\ \text{word no. of page of segment or} \\ \text{page offset of segment.}$$

\* Page size of segment = frame size of P.A.S.

Q) Consider a system using segmented paging architecture. The segment is divided into 1k pages and each page is having 512 entries. The segment number requires 17 bits to represent all the segments of L.A.S. and frame no requires 15 bits to represent all the frames of P.A.S. & memory is word addressable and P.T. size = 2<sup>13</sup>W. Then calculate.

① Length of L.A.

② P.T. size of segment.



$$\text{Page size} = 512 \text{ W} = 2^9 \text{ W}$$

$$\text{No. of pages} = 2^{10}$$

$$\text{No. of segments} = 2^{17}$$

$$\text{Segment size} = 2^{10} + 2^9 = 2^{19} \text{ W}$$

$$\text{No. of frames} = 2^{15}$$

$$\textcircled{1} \text{ Length of L.A.} = \text{segment size} \times \text{No. of segments} \\ = 2^{19} \times 2^{17} = 2^{36}$$

$$= 36 \text{ bits}$$

$$\textcircled{2} \text{ Length of P.A.} = \text{No. of frames} \times \text{No. of frame bits} + \text{No. of segm. page size bits} \\ = 15 + 9 = 24 \text{ bits.}$$

$$\textcircled{3} \text{ P.T. size of segment} \Rightarrow \text{PT entries} \# \times \text{PTE size}$$

$$= 2^{10} \times 2$$

$$= 2^{11} = 2 \text{ kW}$$

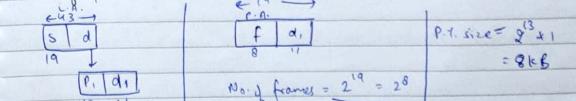
Q. Consider a system using segmented paging architecture. The segment is divided into 8K pages and each page is having 2K entries. The segment number requires 19 bits to represent all the segments of L.A.S. Memory is Byte addressable and P.A.S = 512kB. P.T. size = 8 bits. Then calculate:

$$\textcircled{1} \text{ Length of L.A.} = 43 \text{ bits}$$

$$\textcircled{2} \text{ Length of P.A.} = 19 \text{ bits}$$

$$\textcircled{3} \text{ Page Table size of segment} = 8 \text{ kB}$$

$$\textcircled{4} \text{ No. of frames in the P.A.S} = 2^8 = 256 \text{ frames.}$$

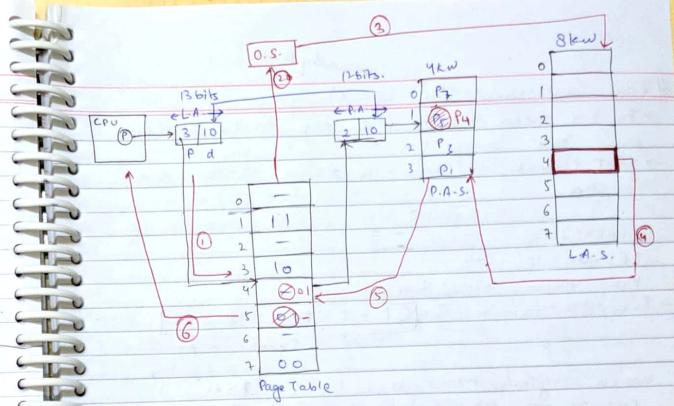


$$\text{P.T. size} = 2^{13} + 1$$

$$= 8 \text{ kB}$$

$$\text{No. of frames} = \frac{2^{19}}{2^{11}} = 2^8$$

WB Pg102  
 L.A. 16  
 3 13  
 P1 d1  
 P.T. size = 2<sup>8</sup>  
 P.S. = 2<sup>16</sup> B  
 No. of segments = 2<sup>3</sup>  
 Page size = x  
 No. of pages = 2<sup>13</sup>  
 P.T. size =  $2^{13} \times 2$   
 $x$   
 $= 2^{14}$   
 $x$   
 P.T. size = x  
 $2^{14} = x^2 \Rightarrow (2^7)^2 = x^2 \Rightarrow x = 2^7$   
 $= 128 B$



# Virtual Memory:

- Virtual memory gives an illusion to the programmer that the programs larger size than actual physical memory can be executed.
- Virtual memory will be implemented by using demand paging or demand segmentation.

# Demand Paging:

- Loading the page into memory on demand [whenever page fault occurs] is called as demand paging.

Step ①: CPU is trying to refer the page in the main memory but the page is currently not available [This is called as page fault].

Step ②: Program execution will stop and signal will be sent to the OS, regarding the page fault.

Step ③: OS will search for the required page in the L.A.S.

Step ④: Required page will be brought from L.A.S. to P.A.S.  
The page replacement algorithms will be used for the decision making of selecting the page for the replacement.

Step ⑤: Respective page table entry will be updated accordingly.

Step ⑥: Signal will be sent to the CPU to continue program execution and the CPU will access the required page in the main memory and continue program execution.

# Page fault service time (PFST) <sup>periodically in ms</sup>  
 → The time taken to service the page fault is called as page fault service time (PFST).  
 → PFST includes the time to perform all the above 6 steps.

$$PFST = 3$$

$$PF \text{ rate} = 1P$$

Main Memory access time =  $m$   
 Then the formula for  $EMAT = PA S + (1-P) \times m$

Consider a system  $MMAT = 25 \text{ ms}$ ,  $PageFST = 7.5 \text{ ms}$   
 $Page HIT \text{ rate} = 75\%$ . Then what is the EMAT?  
 $TFRate = 0.25$   
 $EMAT = 0.25 \times 17.5 + 0.75 \times 25$   
 $= 13.8 \text{ ms}$

WB Page

Q.20.  $PFrame = \frac{1}{K}$   $PFST = i+j$   $MMAT = ?$

$$EMAT = \frac{1}{K} \times (i+j) + \frac{(K-i)}{K} \times \frac{i+j}{K} + \frac{K-i}{K}$$

$$\Rightarrow \frac{P+i}{K} * P + \frac{i}{K}$$

for k instructions  $\frac{1}{K}$

WB Paging

Q.21.  $PFST = 10 \text{ ms}$   $MMAT = 20 \text{ ms}$

$$PF \text{ rate} = \frac{1}{100}$$

$$EMAT = \frac{1}{100} \times 10 + \frac{99}{100} \times 20 \times 10^{-3}$$

$$= 10 \text{ ms} + 19.8 \text{ ms} = 30 \text{ ms}$$

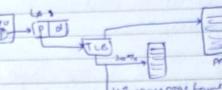
WB Pg106

Q.12.  $PFST = 8 \text{ ms}$   $PFST_m = 20 \text{ ms}$   $MMAT = 1 \text{ ms}$   
 Modified : 20%  
 $EMAT = 2 \text{ ms}$

$EMAT = \frac{8}{100} P [0.7 \times 20 + 0.3 \times 8] + (1-P) [1]$

$$2 = P [14 + 2.4] + 1 - P$$

$$2 = 14P + 2.4 + 1 - P \Rightarrow 15.4P = 1$$

$$P = \frac{1}{15.4} = 0.064$$


pg107

Q.21.  $PFST = 200 \text{ ms}$   $MMAT = 10 \text{ ms}$   
 $TLB \text{ HIT ratio} = 0.5$

$$EMAT = 0.5 \times (10) + 0.5 \times (200) + 0.5 \times (20)$$

$$= 8 + 100 + 10$$

$$= 0.8(10) + 0.2 \times 0.1(200) + 0.2 \times 0.9(10)$$

$$= 8 + 13.8 \text{ ms}$$

$EMAT = 0.4 \times (8 + 10) + 0.2 (8 + 0.1 \times 200 + 0.9 \times (10))$

$$= 13.8 \text{ ms}$$

### # Page Replacement Algorithms:

Reference strings: 7, 0, 1, 2, 0, 3, 0, 4, 2, 3, 0, 3, 2, 1, 2, 0, 1, 7, 0, 1  
 Page numbers referred in the L.A.

#### (Note)

↳ No. of frames allocated to the process is decided by instruction set architecture.

### # FIFO (First In First Out):

# of frames = 4

|   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| 7 | 0 | 1 | 2 | 0 | 3 | 0 | 4 | 2 | 3 | 0 | 3 | 2 | 1 | 2 | 0 | 1 | 7 | 0 | 1 |
| 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | / | 7 | 7 | 7 |
| 7 | 7 | 7 | X | 8 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 |
| F | F | F | F | F | F | F | F | F | F | F | F | F | F | F | F | F | F | F | F |

= 10 faults

### # 3 frames:

|   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| 7 | 0 | 1 | 2 | 0 | 3 | 0 | 4 | 2 | 3 | 0 | 3 | 2 | 1 | 2 | 0 | 1 | 7 | 0 | 1 |
| 1 | 1 | 1 | X | 0 | 0 | 0 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 |
| 7 | 7 | X | 2 | 2 | X | 4 | 4 | X | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| F | F | F | F | F | F | F | F | F | F | F | F | F | F | F | F | F | F | F | F |

= 15 faults

R.S. → 1, 1, 3, 4, 1, 2, 5, 1, 2, 3, 4, 5

|   |   |   |   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 1 | 2 | 5 | 1 | 2 | 3 | 4 | 5 |
| 3 | 3 | 3 | 2 | 2 | 2 | 2 | 4 | 4 | 4 | 4 | 4 |
| 2 | 2 | 2 | 1 | 1 | 1 | 1 | 3 | 3 | 3 | 3 | 3 |
| 1 | 1 | 1 | 4 | 4 | 4 | 5 | 5 | 5 | 5 | 5 | 5 |
| F | F | F | F | F | F | F | F | F | F | F | F |

F F F F F F F F F F = 9 faults.

### 4 frames

|   |   |   |   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 1 | 2 | 5 | 1 | 2 | 3 | 4 | 5 |
| 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 |
| 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 1 | 1 | 1 | 1 |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |

c. f. = 10 faults.

### \* Belady's Anomaly:

→ By increasing no. of frames to the process, no. of page faults should decrease but instead, they are increasing.  
 This problem is called as Belady's Anomaly.

### # Optimal Page Replacement:

→ In the event of page fault replaces the page which is not used for longer duration of time in future.

|          |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
|----------|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| 4 frames | 7 | 0 | 1 | 2 | 0 | 3 | 0 | 4 | 2 | 3 | 0 | 3 | 2 | 1 | 2 | 0 | 1 | 7 | 0 |
|          | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | X | 7 |
|          | 1 | 1 | 1 | 1 | X | 9 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 |
|          | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
|          | 7 | 7 | 7 | X | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | A | 1 | 1 | 1 |
|          | F | F | F | F | F | F | F | F | F | F | F | F | F | F | F | F | F | F | F |

8 faults =

use LRU

### 3 frames:

|          |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
|----------|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| 3 frames | 7 | 0 | 1 | 2 | 0 | 3 | 0 | 4 | 2 | 3 | 0 | 3 | 2 | 1 | 2 | 0 | 1 | 7 | 0 |
|          | 1 | 1 | 1 | X | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 |
|          | 0 | 0 | 0 | 0 | 0 | X | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 |
|          | 7 | 7 | X | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 |
|          | F | F | F | F | F | F | F | F | F | F | F | F | F | F | F | F | F | F | F |

9 faults =

# LRU Recently Used (LRU) Page replacement:  
 → In the event of page fault, we replace the page which is least recently used.

3 frames

|   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| 7 | 0 | 1 | 2 | 0 | 3 | 0 | 4 | 2 | 3 | 0 | 3 | 2 | 1 | 2 | 0 | 1 | 7 | 0 | 1 |
|   | 1 | 1 | X | 3 | 3 | X | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 7 | 7 | 2 |
|   | 0 | 3 | 0 | 0 | 0 | 0 | 0 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 0 | 0 | 0 |
|   | 2 | 7 | 7 | 2 | 2 | 2 | 2 | X | 4 | 4 | 4 | 0 | 0 | 0 | 1 | 1 | 1 | 1 | 1 |

F F F F F F F F F F F F = 12 faults

4 frames

|   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| 7 | 0 | 1 | 2 | 0 | 3 | 0 | 4 | 2 | 3 | 0 | 3 | 2 | 1 | 2 | 0 | 1 | 7 | 0 | 1 |
|   | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 |
|   | 1 | 1 | 1 | 1 | X | 4 | 4 | 4 | 4 | 4 | X | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
|   | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |

F F F F F F F F F F F F = 8 faults

# MRU Most Recently Used (MRU) Page replacement:

→ In the event of page fault, replace the page which is most recently used.

4 frames

|   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| 7 | 0 | 1 | 2 | 0 | 3 | 0 | 4 | 2 | 3 | 0 | 3 | 2 | 1 | 2 | 0 | 1 | 7 | 0 | 1 |
|   | 2 | 2 | 2 | 2 | 2 | X | 8 | X | 3 | 2 | 2 | X | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
|   | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
|   | 0 | 0 | 0 | X | X | 8 | 0 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 |

F F F F F F F F F F F F = 12 faults

3 frames

|   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| 7 | 0 | 1 | 2 | 0 | 3 | 0 | 4 | 2 | 3 | 0 | 3 | 2 | 1 | 2 | 0 | 1 | 7 | 0 | 1 |
|   | X | 2 | 2 | 2 | 2 | X | 3 | 8 | X | X | X | X | X | X | X | X | 1 | 1 | 1 |
|   | 0 | 0 | 0 | X | 8 | 0 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 |
|   | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 |

F F F F F F F F F F F F = 16 faults

WB Pg 107

| Record no. | Page no. | Page 4                                   |
|------------|----------|------------------------------------------|
| 0-99       | 0        | X X X X X = 7 faults. @                  |
| 100-199    | 1        |                                          |
| 200-299    | 2        | R.S. → 1, 2, 4, 5, 1, 2, 3               |
| 300-399    | 3        | L.R.S. does not contain same page twice. |
| 400-499    | 4        |                                          |
| 500-599    | 5        |                                          |

needed to write again

NOTE

① R.S. str never contains continuous same page.  
 Eg 1, 2, 3, 4, 9, 3, 2, 1 (X)

1, 2, 3, 4, 3, 2, 1 ✓

② If there is only one frame allocated to the process, then every page referred will be a page fault.

WB Pg 106

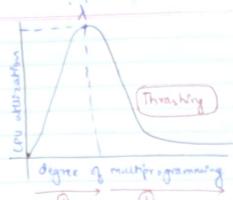
B12. (Q.m, n)

minimum page faults = m (unique pages)

maximum page faults = n (total pages referred)

L.T.S : long term scheduler.

Threshing:



Free Frames = 400

No. of processes = 100

Each process 'P' gets  $\approx 4$  frames.

② If No. of processes = 400

Each process 'P' gets = 1 frame

→ In the initial, degree of multiprogramming upto the point of 'X', the CPU utilization is very high and system resources are utilized perfectly.

→ If we further increase the degree of multiprogramming, the CPU utilization will drastically fall down and the system will spend more time only in the page replacement and the time taken to complete the execution of the process increases.

This situation in the system is called as Threshing.

# Causes of Threshing:

- ① High degree of multiprogramming
- ② Lack of frames

# Recovery of Threshing:

① Don't allow the system to go into threshing and instruct the L.T.S. not to bring the processes into the memory after the point of 'X'.

② If the system is already in threshing, then instruct the mid term scheduler to suspend some of the processes, so that we can recover the system from threshing.

Q Consider the system & with the following parameters:

CPU utilization = 10% Paging disk = 90%

Then which of the following factors will improve the CPU utilization?

- ① Install bigger disk NO
- ② Install faster CPU NO
- ③ Increase degree of multiprogramming NO
- ④ Decrease degree of multiprogramming YES
- ⑤ Install more main memory \* YES
- ⑥ Decrease page size NO (Assume frame size is constant)
- ⑦ Increase page size LIKELY YES

Paging disk = Time spent on page replacement

02/07/2017

### # File Systems:

→ File : collection of logically related entities (records). File will have various attributes.

#### Attributes:

- ① Name
- ② Type
- ③ Size
- ④ Location
- ⑤ Creation date
- ⑥ Last modified date
- ⑦ Permissions
- ⑧ Owner
- ⑨ Password

→ All the attributes of the file, is called as File context.  
→ File context will be stored in the File Control Block (FCB).  
→ Every file will have its own FCB.

#### # Types:

- ① .doc
- ② .txt
- ③ .dll
- ④ .exe
- ⑤ .obj
- ⑥ .class
- ⑦ .bat
- ⑧ .pdf
- ⑨ .png
- ⑩ .apt
- ⑪ .xls | .xlsx
- ⑫ .c | .cpp | .java | .html | .php | .smil | ...
- ⑬ .mp3 | .mp4
- ⑭ .avi | .mkv | .flv
- ⑮ .bmp

→ Various operations will be performed on files:

#### Operations:

- ① Create
- ② Open
- ③ Write
- ④ Read
- ⑤ Edit
- ⑥ Delete
- ⑦ Close
- ⑧ Save
- ⑨ Copy
- ⑩ Paste
- ⑪ Cut
- ⑫ Undo
- ⑬ Redo
- ⑭ Send
- ⑮ Print
- ⑯ Rename
- ⑰ Save as

### # Access Methods:

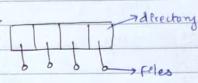
- ① Sequential Access

- ② Random Access

→ For better classification of files, files will be stored in the directory.

### # Directory Structure:

- ① Single level directory:

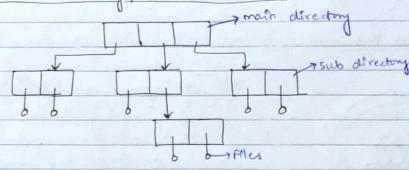


→ Implementation of the directory structure is easy/simple.

→ Two files cannot have the same name.

→ Searching time for the specific file will be more.

- ② Multi level directory / Hierarchical / Tree :



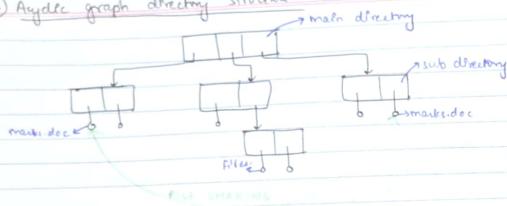
→ Implementation is difficult.

→ Better classification of the files as per the criteria.

→ Searching time for the specific file will be less.

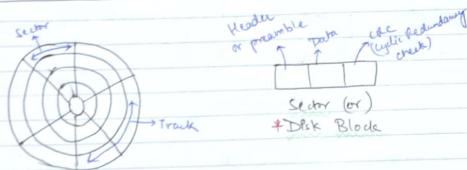
→ If the same file exists in two different directories, then if one file is updated, the other file has to be updated accordingly. Otherwise, there will be inconsistency.

### ③ Andile graph directory structure:



- ⇒ The implementation of the directory structure is difficult.
- ⇒ Better classification of the files as per the criteria.
- ⇒ The searching time for files will be less.
- ⇒ If the same file exists in two different directories, then, if one file is updated, then other file will be updated automatically by using file sharing concept.

### # Disk Structure:



Q. Consider a disk which has 16 platters, each platter is having 2 surfaces. Each surface is divided into 1 k tracks. Track is divided in 512 sectors and each sector can store 2 kB data. Then calculate:

- ① Capacity of the disk
- ② How many bits are required to identify specific sector of a disk.

$$\text{① Capacity} = (2^4 \times 2^{10} \times 2^9 \times 2^{11}) \text{ B}$$

$$= 32.9 \text{ GB}$$

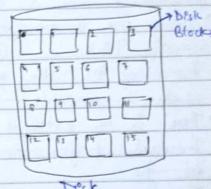
$$\text{② Bits for sector} = 4 + 1 + 10 + 9$$

$$= 24 \text{ bits}$$

### # Disk space allocation methods:

#### \* Contiguous Allocation:

| File    | Starting D.B.A. | Size | Disk Block address |
|---------|-----------------|------|--------------------|
| abc.doc | 2               | 4    | disk blocks.       |
| xyz.doc | 9               | 5    |                    |



→ In contiguous allocation, whenever a file is created, the disk blocks will be allocated in a continuous manner.

→ Every file is associated with two parameters:

#### ① Starting D.B.A.

#### ② Size

→ Increasing the file size may not be possible always.

→ It is suffering from external fragmentation.

→ Internal fragmentation may exist in the last disk block of the file.

→ It supports both sequential and random access of the file.

→ Starting D.B.A. + offset ⇒ Random access.

Eg.  $9+4=13$  ⇒ Offset value for this blocks

### # Linked Allocation [Non Contiguous]:

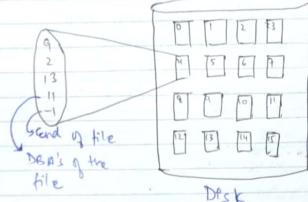
| File    | Starting DBA | Ending DBA |
|---------|--------------|------------|
| abc.doc | 2            | 1          |
| xyz.doc | 9            | 10         |



- In the linked allocation, disk blocks will be allocated in a non-contiguous manner.
- Every file is associated with 2 parameters:
  - ① Starting DBA
  - ② Ending DBA
- Increasing the file size is always possible if the free disk block is available.
- There is no external fragmentation.
- Internal fragmentation may exist in the last disk block of the file.
- There is overhead of maintaining the pointer in every disk block.
- If the pointer of any disk block is lost, file will be truncated.
- It supports only sequential access of the file.

### # Indexed Allocation

| File    | I-Node |
|---------|--------|
| abc.doc | 4      |



- In indexed allocation, every file is associated with its own index node.

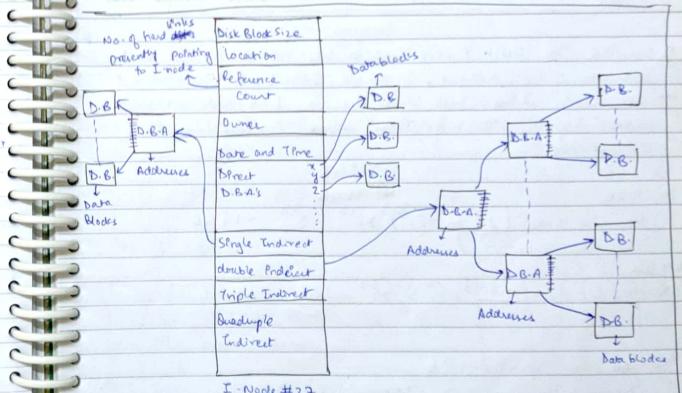
→ Index node contains all the disk block addresses (DBAs) of the file.

→ There is no outer external fragmentation, but internal fragmentation may exist in the last disk block.

→ If the file is very very large, then, one disk block may not be sufficient to store all the disk block addresses.

→ If the file is very very small, then, it is waste of using entire one disk block, just to store the addresses.

### # UNIX-I-NODE Implementations:



$$\text{Total size of the file} = \left[ \# \text{ of Direct DBAs} + \frac{(\text{DB size})}{\text{DBA}} + \frac{(\text{DB size})^2}{\text{DBA}} + \frac{(\text{DB size})^3}{\text{DBA}} + \dots \right] \times \frac{\text{DB size}}{\text{DB size}}$$

| File    | I-NODE |
|---------|--------|
| abc.doc | 27     |

# of single indirect DBAs      # of double indirect DBAs      # of triple indirect DBAs

- Unix follows I-node way of implementation. In order to allocate the disk space to the files.
- Every file is associated with its own I-node.
- Depending on the size of the file, file will be stored in one particular place, maybe in the direct disk block addresses, or maybe in the single indirect or maybe in the double indirect or maybe in the triple indirect and so on.

DB block size = # of DBAs, one disk block can contain DBA

Q. Consider the UNIX I-node which has 10 direct disk block addresses, 1 single indirect, 1 double indirect, 1 triple indirect disk block address. Disk block size is 1 KB and disk block address requires 32 bits. Then what is maximum file size possible.

$$\begin{array}{ll} \textcircled{a} 24B & \textcircled{c} 84B \\ \textcircled{b} 44B & \textcircled{d} 164B \\ \text{Max file size} = \left(\frac{2^{10}}{2^2}\right)^3 \times \left(\frac{10}{2^3}\right) \times \left(\frac{1}{2^1}\right) \times \left(\frac{1}{2^3}\right) \times \left(\frac{1}{2^1}\right) = 2^{30} = 16GB \end{array}$$

WIB pg 114  
 $\text{Q8. Max file size} = \left(\frac{2^9}{2^2}\right)^3 \times 2^9 = 2^{30} = 1GB$

$\frac{1024B}{1KB} = 1024B = 2^{10}B$   
 $\frac{1024}{128} = 128 \Rightarrow \frac{1024}{128} = \text{DB size} \Rightarrow 2^3 = \text{DBA size}$   
 $\text{Max file size} = \left(\frac{\text{DB size}}{\text{DBA}}\right)^3 \times \text{DB size} = \left(\frac{2^{10}}{2^3}\right)^3 \times 2^{10} = 2^{31} \Rightarrow 24B$

WIB pg 113

Q. 7. DB size = 1 KB  $\Rightarrow 2^{10}B$

Max file size =  $4TB = 2^{42}B$

$$\left(\frac{\text{DB size}}{\text{DBA}}\right)^4 \times \text{DB size} = 2^{42} \Rightarrow \left(\frac{\text{DB}}{\text{DBA}}\right)^4 = 2^{32}$$

$$\text{DB} (2^8)^4 = \left(\frac{\text{DB size}}{\text{DBA}}\right)^4$$

$$2^8 = 3 \text{ DB size} \Rightarrow \frac{f}{2^2} \text{ DBA} = 4 \text{ Bytes} = 32 \text{ bits}$$

#### # Disk Free Space Management:

size of disk = 20 MB

Disk block size = 1 KB

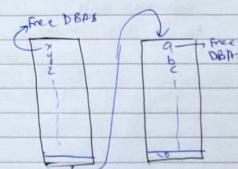
DBA = 16 bits

# of disk blocks available on the given disk =  $\frac{\text{size of disk}}{\text{disk block size}}$

$$= \frac{20MB}{1KB} = \frac{20 \times 2^{20}}{2^{10}} = 20K$$

#### ① Free List approach:

In the free list approach, some disk blocks are used just to store the free disk block addresses.

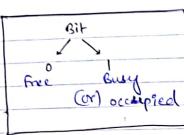


② # of DBAs possible to store in one disk block =  $\frac{\text{DB size}}{\text{DBA}} = \frac{1KB}{2^3} = 512$

For 20K  $\Rightarrow \frac{2^9 \times 2^2}{2^3} = 20 \times 2^{10} = 40$  disk blocks.

② Bit Map Approach:

|          |
|----------|
| 10110100 |
| 01001010 |
| 10001011 |
| 10101001 |
| 01011010 |



Free disk blocks:

1, 4, 6, 7, 8, 10, 11, ...

Busy disk blocks:

0, 2, 3, 5, 9, 12, ...

Bit map

In bitmap approach, every disk block will be mapped with one binary bit.

① To make map 20k disk blocks, we need 20k bits.

$$\textcircled{2} \quad 20k \text{ bits} = \frac{20k \text{ bits}}{1 \text{ bit}} = 2^5 = 3 \text{ disk blocks}$$

Q. 17. Hard disk = 40 MB

$$40 \times 2^{20} \text{ B}$$

$$DBA = 38$$

$$\text{No. of disk blocks} = \frac{40 \times 2^{20}}{2^{11}} = 2^2 \times 2^9 \times 10 = 20 \text{ k}$$

Bits = 20k bits

$$\text{No. of disk blocks to store bit map} = \frac{20 \text{ k}}{2^8} = 10 \text{ k}$$

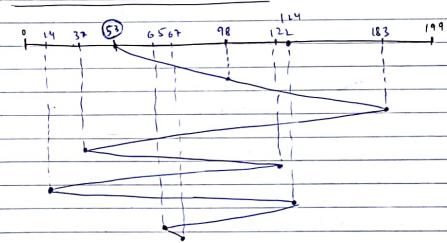
# Disk Scheduling:

Track Requests: 98, 183, 37, 122, 14, 124, 365, 67



Goal: To minimize the average seek time of disk.

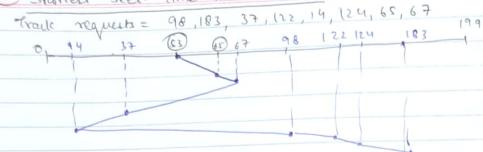
① First Come First Serve (FCFS):



\* Total track movements made by I/O header (Seek Time):

$$\begin{aligned} &= (48-53) + (183-98) + (83-37) + (122-14) + (124-14) + (124-67) \\ &\quad + (67-53) \\ &= 45 + 85 + 146 + 85 + 108 + 110 + 59 + 2 \\ &= 130 + 220 + 231 + 59 = 290 + 110 + 130 = 640. \end{aligned}$$

② Shortest seek time first (SSTF): Nearest track next

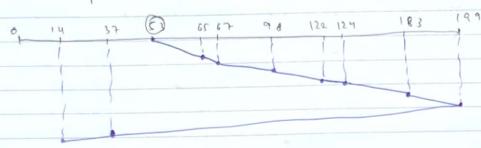


$$= 236$$

$$= 12 + 2 + 30 + 23 + 84 + 24 + 2 + 59$$

③ SCAN scheduling / Elevator :

Disk requests: 98, 183, 37, 122, 14, 124, 65, 67

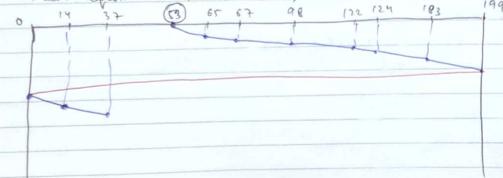


$$= 12 + 2 + 31 + 24 + 2 + 59 + 16 + 162 + 23$$

$$= 90 + \cancel{40} + 201 = 331$$

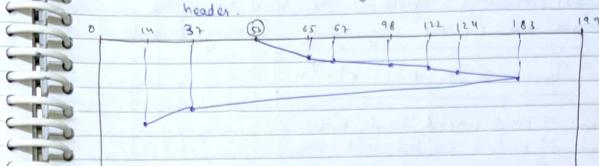
④ C-SCAN (Circular SCAN):

Disk requests: 98, 183, 37, 122, 14, 124, 65, 67



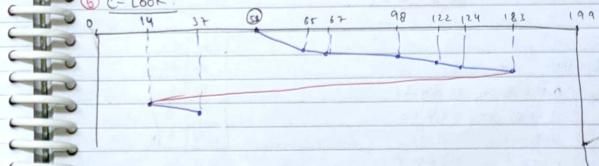
$$= 146 + 37 + 199 = 382$$

⑤ LOOK : look for last pending request in the direction of r/w header.



$$= 130 + 146 + 23 = 299$$

⑥ C-LOOK:



$$= 130 + 23 + 169 = 322$$

## CPU SCHEDULING

NOTE

In SJF scheduling algorithm, the burst time of the processes are expected by using following formula.

$$T_{n+1} = \alpha \cdot T_n + (1-\alpha) \cdot T_m$$

$T_{n+1}$  → Next expected burst time  
 $T_n$  → previous expected burst time  
 $T_m$  → previous actual burst time.

' $\alpha$ ' is a parameter which controls relative weight of recent and past history.

$$0.6 < \alpha < 1$$

WB Pg 82

Q.32.  $T_1 = 10$      $\alpha = 0.5$   
 $T_2 = 0.5 \times T_1 + 0.5 \times T_1$   
 $= 0.5 \times 10 + 0.5 \times 10$   
 $= 7.5$

$$T_3 = 0.5 \times 8 + 0.5 \times 7.5$$

$$= 4 + 3.75$$

$$= 7.75$$

$$T_4 = 0.5 \times 3 + 0.5 \times 7.75$$

$$= 1.5 + 3.875$$

$$= 5.375$$

$$T_5 = 0.5 \times 5 + 0.5 \times 5.375$$

$$= 2.5 + 2.6875$$

$$= 5.1875$$

④

| Frm | Blk |
|-----|-----|
| P1  | 5   |
| P2  | 0   |
| P3  | 3   |
| P4  | 5   |

Q.32  
 $x = 1$   
 $T_2 = T_1$        $T_5 = T_4$   
 $T_3 = T_2$        $\frac{T_5 - T_4}{T_2 - T_1} = 5$   
 $T_4 = T_3$

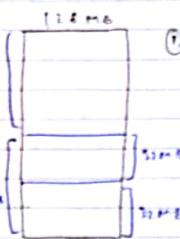
WB page 92

Q.34. (b)  $n=21, k=12$

Pg 9 R12, R10

Pg 9 R10, R12

# BUDDY SYSTEM:



Initial

After

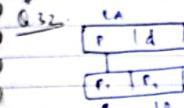
Memory

- In the buddy system, initially memory will be single continuous free block.
- whenever the request by the process arrives, memory will be divided into 2 half blocks.
- If the request by the process is too small, then the lower block of the memory is further divided into two half blocks again.
- In the buddy system, memory will be allocated from lower blocks to higher blocks.

WB Pg 102

Q.32. PA = 36 bits      No. of frames =  $2^{14}$   
 $\text{Page size} = 4KB$        $4KB = 2^{12}$   
 $2^{14} \times 2^{12} = 2^{26}$

Q.33



$$\begin{aligned} &\text{L1 level PT size} + \text{L2 level PT size} \\ &= 2^9 \times 2 + 2^{10} \times 4 \\ &= 16 + 4096 \\ &= 5120 \end{aligned}$$