## Tutorial-03

1. Let 
$$\times$$
 be the weights of frying chicken  $\times NN(500, 100^{2})$  pdf of Normal distribution of  $(x < 650)$   $(x < 650)$   $(x < 650)$   $(x < 650 < 500)$   $(x < 650 < 500)$ 

b) 
$$P(x < 345)$$
  
=  $P(x - \mu < 345 - 500)$   
=  $P(z < 0.0669)$  or  $1 - P(z < 1.55)$   
= 0.0606

c) 
$$P(480 \angle \times \angle 710)$$
  
=  $P(480-500 \angle Z \angle 710-500)$ 

= 0.9332

$$P(-0.2 \angle Z \angle 2.1)$$
=  $1 - [P(Z \angle -0.2) + P(Z \angle 2.1)]$ 
=  $1 - [P(Z \angle -0.2) + P(Z \angle -2.1)]$ 

d) 
$$P(\times > 590)$$
  
=  $P(\times - \mu > 590 - 500)$   
=  $P(\times > 0.9)$  =  $1 - P(\times < 0.9)$  0.9  
=  $P(\times < -0.9)$  =  $0.1841$ 

$$= P(x-\mu < 142-125)$$

$$= P(x-\mu > \frac{108-125}{10})$$

$$= 1 - 0.0446 = 0.9554$$

$$Z = 1.175$$

$$Z = x - \mu$$

88%.

c) 
$$P(\times \angle \times) = 0.36$$
  
 $P(Z \angle Z) = 0.36$   
 $Z = -0.36$   
 $x = \mu + 6z$ 

$$= 125 + 1018 \times -0.36$$

$$= 121.4$$

$$= P(x-\mu < 100-125)$$

$$P(x_1 \angle \times \angle x_2) = 0.95$$

$$2 = \mu + 62$$

$$= 125 + 10(1.96)$$

$$= 144.6$$

3) Let 
$$\times$$
 be the annual rainfall.  $\times N(40, 5^2)$ 

$$= P(X-\mu > \frac{36-40}{5})$$

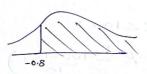
$$= P(z > -0.8)$$

$$= P(x-\mu < \frac{38-40}{5}) + P(x-\mu > \frac{50-40}{5})$$

$$= P(Z \angle -0.4) + P(Z > 2)$$

$$= 0.3674$$

$$= P(x-\mu > \frac{308-268}{15})$$





b) 
$$P(\times \angle x_{1}) = 0.04$$
  
 $P(\angle z) = 0.04$   
 $z = -1.75$   
 $\alpha_{1} = \mu + \delta z$ 

$$= 268 + 15(-1.75)$$

$$= 241.75$$

$$= P\left(\frac{60-70}{4} \angle Z \angle \frac{80-70}{4}\right)$$

c) 
$$5.D = \sqrt{n} = \frac{4}{\sqrt{9}} = 1.333$$

$$P(68.5 \angle X \angle 71.75)$$

$$= P(68.5 \angle X \angle 71.75)$$

$$= P(\frac{68.5 - 70}{4\sqrt{q}} \angle Z \angle \frac{71.75 - 70}{4\sqrt{q}})$$

$$= P(-1.125 \angle Z \angle 1.3125)$$

$$= 1 - [P(Z \angle -1.13) + P(Z \angle -1.31)] -1.731$$

P(
$$\overline{x}_{1} \angle \overline{x} \angle \overline{x}_{2}$$
) = 0.95  
P( $-1.96 \angle Z \angle 1.96$ ) = 0.95  
 $\overline{x}_{1} = \mu_{\overline{x}} + \delta_{\overline{x}} Z$   
=  $70 + 1.33(-1.96)$ 

= 67.39

$$P(z < z_1) = 0.025.$$
 $z_1 = -1.96$ 
 $\overline{z}_2 = \mu_{\overline{z}} + \delta_{\overline{x}} Z$ 
 $= 70 + 1.33(1.96)$ 
 $= 72.61$ 

Db)

Let X be the daily cost of photo copies.

P (mean daily cost for 25 days < 11.85)

XNH (
$$\mu = 200 \times 0.05$$
,  $\sigma^2 = 50^2 \times 0.05$ ).

N( $\mu = 12.5$ ,  $\sigma^2 = 125$ )

N( $\mu = 12.5$ ,  $\sigma^2 = 125$ )

N( $\mu = 12.5$ ,  $\sigma^2 = 5$ )

P (X < 11.85) = P( $\overline{X} - 12.5$  < 11.85 + 12.5)

= P( $\overline{Z} < -0.05$ )

= 0.3859

Let x be the net weights of boxes filled from the machine × NN(16,0.32)

$$= P(x-\mu > \frac{15-16}{0.3})$$

$$= 1 - P(z \angle -3.33)$$

$$= 1 - 0.0005$$

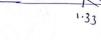
$$= P(\frac{x-\mu}{8} > \frac{16.5-16}{0.3})$$

$$= 1 - 0.9525$$

$$= 0.0475$$

$$= P\left(\frac{x-\mu}{6} > \frac{16.4-16}{0.3}\right)$$





$$6 = \sqrt{npq}$$

$$= \sqrt{400\times0.92\times0.8}$$

$$= 8$$

mp 75, ng 75.

We can use normal approximation

$$P(\times \leq 90) = P(\times \leq 90.5)$$

$$P(\times \leq 90) = P(\times \leq 90.5)$$

$$= P(\times - \mu \leq 90.5 - 80)$$

$$= P(\times \leq 1.31)$$

$$= 0.9049$$

The sample event is not unlikely assuming the claimed percentage of 20%, hence the daim is not unreasonable.

$$= P\left(\frac{x-\mu}{\sqrt[6]{n}} > \frac{16\cdot 3 - 16}{\frac{0\cdot 3}{\sqrt{32}}}\right)$$

$$= P(\overline{X} - \mu) \geq \frac{15.8 - 16}{0.3}$$

np=45>5 & nq>5 So we can use normal approximation.

 $P(X > 57) \stackrel{\triangle}{=} P(X > 56.5)$  By a continuity correction is needed as the response are binary & the counts have a Binomial distinuith n = 100, p = 0.45.

$$\mu = np$$
=  $100 \times 0.45$ 
 $= 45$ 
 $6 = \sqrt{npq}$ 
=  $\sqrt{100 \times 0.45 \times 0.55}$ 
=  $4.9749$ 

P(X>57) = P(X>56.5)

$$= P\left(\frac{X-45}{4.9749} > \frac{56.5-45}{4.9749}\right)$$

a) 
$$6x = \frac{6}{\sqrt{n}} = \frac{1.6}{\sqrt{16}} = 0.4$$

b) 
$$P(\overline{x} > 12.3)$$
  
=  $P(\overline{x} - 11.5) > \frac{12.3 - 11.5}{0.4}$ 

P(
$$\overline{z}$$
,  $\angle \overline{x}$   $\angle \overline{z}$ <sub>2</sub>)=0.68  
P( $\overline{z}$ ,  $\angle \overline{z}$   $\angle \overline{z}$ <sub>2</sub>)=0.68

$$z = \frac{7z - \mu_{x}}{\sigma_{x}}$$
 $p(z \angle z_{1}) = 0.16$ 
 $p(z \angle z_{2}) = 0.84$ 
 $z_{1} = -1.0$ 
 $z_{2} = 1$ 

$$\overline{z}'_{1} = \mu_{x} + z_{6x}$$

$$= 11.5 + (-1)^{\circ}.4$$

$$= 11.1$$

$$z_{2} = 1$$

$$\overline{x}_{2} = \mu_{x} + 26x$$

$$= 11.5 + 1(0.4)$$

$$= 11.9$$

standard deviation = 
$$\sqrt{np(1-p)}$$
  
=  $\sqrt{1500 \times 0.7 \times 0.3}$   
= 17.7482

b) 
$$np > 5$$
,  $nq > 5$   
50, we can use normal approximation  $\times N N (1050, 17.7482)$   
 $P(\times > 1000) = P(\underline{\times - \mu}) = \frac{1000 - 1050}{17.7482}$   
 $= P(\times > 999.5)$ 
 $= P(\times > 999.5)$ 

$$=1-0.0022$$
)  
 $=0.9978$ 

• c) 
$$P(x > 1200) = P(x-\mu > \frac{1200.51050}{17.7482})$$
  
•  $P(x > 1200.5)$   
=  $P(z > \frac{8.4797}{8.4516})$ 

1 1 61

$$mean = 1700 \times 0.7$$
  
= 1190

$$S \cdot D = \sqrt{1700 \times 0.7 \times 0.3}$$

$$P(\times > 1200) = P(\times - \mu > \frac{1200.51190}{18.8944})$$

$$= P(\times > 1200.5) = P(\times > 0.5557)$$

$$= 1 - P(\times < > 0.5293)$$

$$= 0.2877$$

$$f_{x}(x) = \lambda e^{\lambda x}$$
 $\lambda = \frac{1}{2} = 0.2/y_{eq}$ 

$$P(T < 1/2) = \int_{0}^{1/2} 0.2e^{-0.2.x} dx$$

$$= -e^{-0.2x} \int_{1/2}^{1/2} dx$$

$$= -e^{-0.2x} \int_{1/2}^{1/2} + 1$$

$$= -0.7919 + 1 = 0.2081$$

Let X be the lifetime of a particular fan

$$P(X > 10000) = P(X > 10000)$$

$$= -e^{\lambda_{X}} | (0,000) = P(X = 0.0003 \times 10,000)$$

$$= -e^{\lambda_{X}} | (0,000) = P(X = 0.0003 \times 10,000)$$

$$= -e^{3}$$

$$= 0.04978$$

$$= 0.0498$$

$$\lambda = 0.00035$$

$$P(\times > 10,000) = \int_{0,000}^{\infty} \lambda e^{-\lambda x} dx$$

$$= -e^{-\lambda x} \Big|_{0,000}^{\infty}$$

$$= 0 + e^{0.00035 \times 10,000}$$

$$= e^{3.5}$$

$$= 0.030197$$

$$= 0.0302$$

It will fewer fans compare with early a one

mean = 8
$$\begin{array}{c}
\lambda = 8 \\
\lambda = \frac{1}{8} = 0.125 \\
\times n = xp(\frac{1}{8}) \\
f_{x(n)} = \lambda e^{\lambda x} \times 70
\end{array}$$

$$\begin{array}{c}
A \\
p(x < 5) = \int \lambda e^{\lambda x} dx \\
= -e^{\frac{1}{8} \cdot 5} = 0.4647
\end{array}$$

b) 
$$P(T>t) = \int_{t}^{\infty} 0.125 e^{-0.125t} dt$$

$$= -e^{-0.125t} |_{t}^{\infty}$$

$$= e^{-0.125t}$$

$$= e^$$