

# Package ‘mixingsimulation’

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**Type** Package

**Title** Microbiological Risk Assessment of Powder Mixing Process by Simulation Results

**Version** 0.0.1

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**URL** <https://github.com/Mayooran1987/mixingsimulation>

**BugReports** <https://github.com/Mayooran1987/mixingsimulation/issues>

**Description** This package develops to study microbiological risk assessment of mixing primary samples in the powdered products using simulation results.

**License** GPL (>= 2)

**Encoding** UTF-8

**LazyData** true

**Imports** ggplot2, ggthemes, gridExtra, magrittr, purrr, reshape2, stats

**Suggests** testthat

**RoxygenNote** 7.2.3

**Depends** R (>= 4.0)

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**Language** en-US

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compare_alphas	<i>Graphical display to investigate the impact of concentration parameter values in the Dirichlet distribution.</i>
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### Description

This function provides a graphical display to investigate the impact of concentration parameter values in the Dirichlet distribution.

### Usage

```
compare_alphas(n, alpha)
```

### Arguments

n	number of weights which is generated from Dirichlet distribution
alpha	concentration parameter is given in vector form; each element represents each group.

### Details

We assumed that the concentration parameters are identical in all weights, it means that  $\alpha = [\alpha, \alpha, \dots, \alpha]$ . The probability mass function of the weights is given by:

$$f(w_1, w_2, \dots, w_n; \alpha) = \frac{\Gamma(n\alpha)}{\Gamma(\alpha)^n} \prod_{i=1}^n w_i^{\alpha-1}$$

where  $\alpha = [\alpha, \alpha, \dots, \alpha]$  is the vector of concentration parameter, and  $w_i$  is the stochastic weights which sum to one.

### Value

graphical display of different concentration parameters of Dirichlet distribution

### Examples

```
n <- 10000
alpha <- c(5, 10, 20)
compare_alphas(n, alpha)
```

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compare_mixing_1	<i>Graphical comparison of mixing plans based on the estimated detection probability at each revolution.</i>
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### Description

This function provides a graphical display to compare mixing plans based on the estimated detection probability at each revolution of the mixing process.

**Usage**

```
compare_mixing_1(mu, sigma, alpha_in, k, l, r, distribution, UDL, n_sim)
```

**Arguments**

mu	the average number of CFUs ( $\mu$ ) in the mixed sample, which is in a logarithmic scale if we use a Lognormal / Poisson lognormal distribution
sigma	the standard deviation of the colony-forming units (CFUs) in the mixed sample on the logarithmic scale (default value 0.8)
alpha_in	concentration parameter at the initial stage
k	number of small portions / primary samples
l	number of revolutions / stages
r	the rate of the concentration parameter changes at each mixing stage
distribution	what suitable distribution type we have employed for simulation such as "Poisson-Type A" or "Poisson-Type B" or "Lognormal-Type A" or "Lognormal-Type B" or "Poisson lognormal-Type A" or "Poisson lognormal-Type B"
UDL	the upper decision limit, which depends on the type of microorganisms and testing regulations.
n_sim	number of simulations

**Value**

graphical display of estimated detection probability at each revolution in the mixing.

**References**

- Nauta, M.J., 2005. Microbiological risk assessment models for partitioning and mixing during food handling. *International Journal of Food Microbiology* 100, 311-322.

**See Also**

[sim\\_single\\_pd\\_stages](#)

**Examples**

```
mu <- 100
sigma <- 0.8
alpha_in <- 0.01
k <- c(10,30,60)
l <- 2500
r <- 0.01
distribution <- "Poisson lognormal-Type B"
UDL <- 0
n_sim <- 2000
compare_mixing_1(mu,sigma , alpha_in, k, l, r, distribution, UDL, n_sim)
```

---

compare_mixing_2	<i>Graphical comparison of mixing plans based on estimated probability of detection at the end of the mixing with different revolutions</i>
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---

### Description

This function provides a graphical display to compare mixing plans using a different number of revolutions based on the estimated probability of detection at the end of mixing.

### Usage

```
compare_mixing_2(
  mulower,
  muupper,
  sigma,
  alpha_in,
  k,
  l,
  r,
  distribution,
  UDL,
  n_sim
)
```

### Arguments

mulower	the lower value of the mean concentration ( $\mu$ ) for use in the graphical display's x-axis.
muupper	the upper value of the mean concentration ( $\mu$ ) for use in the graphical display's x-axis.
sigma	the standard deviation of the colony-forming units (CFUs) in the mixed sample on the logarithmic scale (default value 0.8)
alpha_in	concentration parameter at the initial stage
k	number of small portions / primary samples
l	number of revolutions / stages
r	the rate of the concentration parameter changes at each mixing stage
distribution	what suitable distribution type we have employed for simulation such as "Poisson-Type A" or "Poisson-Type B" or "Lognormal-Type A" or "Lognormal-Type B" or "Poisson lognormal-Type A" or "Poisson lognormal-Type B"
UDL	the upper decision limit, which depends on the type of microorganisms and testing regulations.
n_sim	number of simulations

### Value

graphical display compares mixing plans using a different number of revolutions based on the estimated probability of detection at the end of the mixing.

## References

- Nauta, M.J., 2005. Microbiological risk assessment models for partitioning and mixing during food handling. *International Journal of Food Microbiology* 100, 311-322.

## See Also

[sim\\_single\\_pd\\_stages](#)

## Examples

```
mulower <- 0.1
muupper <- 200
sigma <- 0.8
alpha_in <- 0.01
k <- 30
l <- c(500,5000)
r <- 0.01
distribution <- "Poisson lognormal-Type B"
UDL <- 0
n_sim <- 2000
compare_mixing_2(mulower, muupper, sigma , alpha_in, k, l, r, distribution, UDL, n_sim)
```

---

compare\_mixing\_3

*Graphical comparison of mixing plans based on cumulative distribution of expected total CFUs in the mixing process.*

---

## Description

This function provides a graphical display to compare mixing plans based on the cumulative distribution of expected total CFUs in the mixing process using different mixing parameters, such as type of distribution and number of primary samples.

## Usage

```
compare_mixing_3(mu, sigma, alpha_in, k, l, r, distribution, n_sim)
```

## Arguments

mu	the average number of CFUs ( $\mu$ ) in the mixed sample, which is in a logarithmic scale if we use a Lognormal / Poisson lognormal distribution
sigma	the standard deviation of the colony-forming units in the mixed sample on the logarithmic scale (default value 0.8)
alpha_in	concentration parameter at the initial stage
k	number of small portions / primary samples
l	number of revolutions / stages
r	the rate of the concentration parameter changes at each mixing stage
distribution	what suitable distribution type we have employed for simulation such as "Poisson-Type A" or "Poisson-Type B" or "Lognormal-Type A" or "Lognormal-Type B" or "Poisson lognormal-Type A" or "Poisson lognormal-Type B"
n_sim	number of simulations

## Details

Let  $N'$  be the number of CFUs in the mixed sample, which is produced by the mixing of  $k$  primary samples and  $N' = \sum N_i$  and let  $N_i$  be the number of CFUs in the  $i^{th}$  primary sample; where  $i = 1, 2, \dots, k$ .

For this package development, we have employed the notations 'Type-A' and 'Type-B' to indicate the type of distributions, which are applied in the previous literature as 'fair' and 'beta', respectively; see [Nauta \(2005\)](#).

Following [Nauta \(2005\)](#), the contribution weight of contamination by each primary sample can be defined by the random variable  $w_i$ , which is possible to be followed by either uniform distribution with parameter  $1/k$  or the joint distribution of  $w_1, w_2, \dots, w_k$  follows a Dirichlet distribution with concentration parameter  $\alpha$ . From the previous literature, a Dirichlet distribution can be formulated by beta or gamma algorithms, which have revealed the same results; see [Nauta \(2005\)](#).

This function is developed based on the beta algorithm and the following steps formulate it.

$$w_i = x_i \prod_{j=1}^{i-1} 1 - x_j \quad \forall i = 2, 3, \dots, k, \quad w_1 = x_1$$

;

where  $x_i$  follows  $Beta(\alpha, \alpha(k - i))$  and also  $\sum w_i$  must be equal to one.

- Case 1 (Poisson-Type A):  $N_i$  follows  $Poisson(\mu/k)$
- Case 2 (Poisson-Type B):  $N_i$  follows  $Poisson(\mu w_i)$
- Case 3 (Lognormal-Type A):  $N_i$  follows  $Binomial(M_i, 1/k)$ ; where  $M_i$  follows  $Lognormal(\mu, \sigma)$
- Case 4 (Lognormal-Type B):  $N_i$  follows  $Binomial(M_i, w_i)$ ; where  $M_i$  follows  $Lognormal(\mu, \sigma)$
- Case 5 (Poisson lognormal-Type A):  $N_i$  follows  $Binomial(M_i, 1/k)$ ; where  $M_i$  follows  $Poissonlognormal(\mu, \sigma)$
- Case 6 (Poisson lognormal-Type B):  $N_i$  follows  $Binomial(M_i, w_i)$ ; where  $M_i$  follows  $Poissonlognormal(\mu, \sigma)$

The powder-mixing process can be defined as breaking clusters stage-by-stage. Usually, it occurs systematically in the standard powder mixtures. For this package development, we assume that mixing parameters also systematically change with a fixed rate at each stage of the mixing. The mixing parameter can be defined as revolutions instead of the mixing stage in general. Due to the lack of theoretical results for the dependent random variable sum's distribution, we have chosen simulation techniques for this modelling.

Let  $l$  be the number of stages or revolutions of the mixture, and we also assumed a fixed concentration parameter value at the initial phase of the mixing process. Based on the literature in this area, the concentration parameter can be assumed to increase at every stage of the mixing, which is possible to do systematically.

Therefore, this function exhibits the graphical display with different quantities of primary sample mixing as a large unit.

## Value

Graphical comparison between different mixing schemes.

## References

- Nauta, M.J., 2005. Microbiological risk assessment models for partitioning and mixing during food handling. *International Journal of Food Microbiology* 100, 311-322.

**See Also**

[sim\\_single](#), [sim\\_single\\_stages](#), [sim\\_multiple\\_stages](#)

**Examples**

```
mu <- 100
sigma <- 0.8
alpha_in <- 0.01
k <- c(10,30,60)
r <- 0.01
distribution <- c("Poisson lognormal-Type B", "Poisson lognormal-Type B", "Poisson lognormal-Type B")
n_sim <- 2000
plot1 <- compare_mixing_3(mu, sigma, alpha_in, k, l = 250, r, distribution, n_sim) +
  ggplot2::theme(legend.text = ggplot2::element_text(size = 7.5),
    legend.title = ggplot2::element_text(size = 7.5),
    legend.key.size = ggplot2::unit(4, 'mm'))
#+ ggplot2::xlim(0,300)
plot2 <- compare_mixing_3(mu, sigma, alpha_in, k, l = 500, r, distribution, n_sim) +
  ggplot2::theme(legend.title = ggplot2::element_text(size = 7.5),
    legend.key.size = ggplot2::unit(4, 'mm'))
plot3 <- compare_mixing_3(mu, sigma, alpha_in, k, l = 5000, r, distribution, n_sim) +
  ggplot2::theme(legend.text = ggplot2::element_text(size = 7.5),
    legend.title = ggplot2::element_text(size = 7.5),
    legend.key.size = ggplot2::unit(4, 'mm'))
plot4 <- compare_mixing_3(mu, sigma, alpha_in, k, l = 25000, r, distribution, n_sim) +
  ggplot2::theme(legend.text = ggplot2::element_text(size = 7.5),
    legend.title = ggplot2::element_text(size = 7.5),
    legend.key.size = ggplot2::unit(4, 'mm'))
gridExtra::grid.arrange(plot1, plot2, plot3, plot4, ncol = 2, nrow = 2)
```

---

sim\_meanvar

*Mean and variance of the expected number of CFUs in the single mixing stage.*

---

**Description**

This function provides the mean and variance of the expected number of CFUs in the single mixing stage.

**Usage**

```
sim_meanvar(mu, sigma, alpha, k, distribution, n_sim)
```

**Arguments**

mu	the average number of CFUs ( $\mu$ ) in the mixed sample, which is in a logarithmic scale if we use a Lognormal / Poisson lognormal distribution
sigma	the standard deviation of the colony-forming units in the mixed sample on the logarithmic scale (default value 0.8)
alpha	concentration parameter
k	number of small portions / primary samples

distribution	what suitable distribution type we have employed for simulation such as "Poisson-Type A" or "Poisson-Type B" or "Lognormal-Type A" or "Lognormal-Type B" or "Poisson lognormal-Type A" or "Poisson lognormal-Type B"
n_sim	number of simulations

### Details

Let  $N'$  be the number of colony-forming units in the mixed sample which is produced by mixing of  $k$  primary samples and  $N' = \sum N_i$ . This function produces a graphical display of the mean and variance changes at each mixing stage. It is helpful to identify the optimal number of revolutions of the mixture, which is a point of mixing that initiates Poisson-like homogeneity.

### Value

Mean and variance changes in the single mixing stage.

### Examples

```
mu <- 100
sigma <- 0.8
alpha <- 0.1
k <- 30
distribution <- "Poisson lognormal-Type B"
n_sim <- 2000
sim_meanvar(mu, sigma, alpha, k, distribution, n_sim)
```

---

sim_meanvar_stages	<i>Mean and variance of the expected number of CFUs at each mixing stage.</i>
--------------------	---

---

### Description

This function provides the mean and variance of the expected number of CFUs at each mixing stage.

### Usage

```
sim_meanvar_stages(mu, sigma, alpha_in, k, l, r, distribution, n_sim)
```

### Arguments

mu	the average number of CFUs ( $\mu$ ) in the mixed sample, which is in a logarithmic scale if we use a Lognormal / Poisson lognormal distribution
sigma	the standard deviation of the colony-forming units in the mixed sample on the logarithmic scale (default value 0.8)
alpha_in	concentration parameter at the initial stage
k	number of small portions / primary samples
l	number of revolutions / stages
r	the rate of the concentration parameter changes at each mixing stage
distribution	what suitable distribution type we have employed for simulation such as "Poisson-Type A" or "Poisson-Type B" or "Lognormal-Type A" or "Lognormal-Type B" or "Poisson lognormal-Type A" or "Poisson lognormal-Type B"
n_sim	number of simulations



## Details

Let  $N'$  be the number of colony-forming units in the mixed sample which is produced by mixing of  $k$  primary samples and  $N' = \sum N_i$ . This function produces a graphical display of the mean and variance changes at each mixing stage. It is helpful to identify the optimal number of revolutions of the mixture, which is a point of mixing that initiates Poisson-like homogeneity.

## Value

Mean and variance changes at each mixing stage.

## Examples

```
mu <- 100
sigma <- 0.8
alpha_in <- 0.01
k <- 30
l <- 2500
r <- 0.01
distribution <- "Poisson lognormal-Type B"
n_sim <- 2000
result1 <- sim_meanvar_stages(mu, sigma, alpha_in, k, l, r, distribution, n_sim)
melten.Prob <- reshape2::melt(result1, id = "Revolutions",
  variable.name = "summary", value.name = "Value")
plot_example <- ggplot2::ggplot(melten.Prob, ggplot2::aes(x = Revolutions,
  y = Value, group = summary, colour = summary)) +
  ggplot2::geom_line(ggplot2::aes(x = Revolutions, y = Value)) +
  ggplot2::ylab(expression("No. of colony forming units")) +
  ggplot2::theme_classic() + ggplot2::xlab(expression("No. of revolutions")) +
  ggplot2::theme(plot.title = ggplot2::element_text(hjust = 0.5),
  legend.position = c(0.75, 0.25), legend.title = ggplot2::element_blank()) +
  ggthemes::scale_colour_colorblind()
plot_example
```

---

sim_multiple	<i>The expected total number of colony-forming units in the mixed sample in the multiple mixing schemes at the single stage of the mixing process.</i>
--------------	--

---

## Description

This function calculates the resulting expected total number of colony-forming units in the mixed sample in the multiple mixing plans at the single stage of the mixing process.

## Usage

```
sim_multiple(mu, sigma, alpha, k, distribution, summary, n_sim)
```

## Arguments

mu	the average number of CFUs ( $\mu$ ) in the mixed sample, which is in a logarithmic scale if we use a Lognormal / Poisson lognormal distribution
sigma	the standard deviation of the colony-forming units in the mixed sample on the logarithmic scale (default value 0.8)

alpha	concentration parameter
k	number of small portions / primary samples
distribution	what suitable distribution type we have employed for simulation such as "Poisson-Type A" or "Poisson-Type B" or "Lognormal-Type A" or "Lognormal-Type B" or "Poisson lognormal-Type A" or "Poisson lognormal-Type B"
summary	if we need to get all simulated $N'$ , use summary = 2; otherwise, if we use summary = 1, the function provides the mean value of the simulated $N'$ .
n_sim	number of simulations

### Details

Let  $N'$  be the number of colony-forming units in the mixed sample which is produced by contribution of  $k$  primary samples mixing and  $N' = \sum N_i$ . This function provides the simulated resulting of the expected total number of colony-forming units in the mixed sample in the multiple mixing plans at the single stage of the mixing process. To more details, please refer the details section of [compare\\_mixing\\_3](#).

### Value

total number of colony forming units in the multiple mixing scheme

### References

- Nauta, M.J., 2005. Microbiological risk assessment models for partitioning and mixing during food handling. *International Journal of Food Microbiology* 100, 311-322.

### See Also

[sim\\_single](#), [compare\\_mixing\\_3](#)

### Examples

```
set.seed(1350)
mu <- 100
sigma <- 0.8
alpha <- c(0.1,5)
k <- c(30,30)
distribution <- "Poisson lognormal-Type B"
n_sim <- 2000
f_spri <- function(alpha, distribution) {
  sprintf("mixing plan (alpha = %.1f, %s)", alpha, distribution)
}
sim.sum3 <- sim_multiple(mu, sigma, alpha, k, distribution, summary = 2, n_sim)
result <- data.frame(1:n_sim, sim.sum3)
colnames(result) <- c("n_sim", f_spri(alpha, distribution))
melten.Prob <- reshape2::melt(result, id = "n_sim", variable.name = "mixing_scheme",
                             value.name = "Total_CFU")

plot_example <-
ggplot2::ggplot(melten.Prob, ggplot2::aes(Total_CFU, group = mixing_scheme, colour = mixing_scheme))+
ggplot2::geom_line(stat="density", ggplot2::aes(x = Total_CFU))+
ggplot2::ylab(expression("pmf"))+
ggplot2::theme_classic()+ ggplot2::xlab(expression("Total number of CFU in the mixed sample"))+
ggplot2::theme(plot.title = ggplot2::element_text(hjust = 0.5), legend.position = c(0.75,0.75))+
ggthemes::scale_colour_colorblind()
plot_example
```

---

sim_multiple_stages	<i>The expected total number of CFUs in the mixed sample in the multiple mixing schemes at each stage of the mixing process.</i>
---------------------	--

---

### Description

This function calculates the resulting expected total number of CFUs in the mixed sample in the multiple mixing plans at each stage of the mixing process.

### Usage

```
sim_multiple_stages(mu, sigma, alpha_in, k, l, r, distribution, n_sim)
```

### Arguments

mu	the average number of CFUs ( $\mu$ ) in the mixed sample, which is in a logarithmic scale if we use a Lognormal / Poisson lognormal distribution
sigma	the standard deviation of the colony-forming units in the mixed sample on the logarithmic scale (default value 0.8)
alpha_in	concentration parameter at the initial stage
k	number of small portions / primary samples
l	number of revolutions / stages
r	the rate of the concentration parameter changes at each mixing stage
distribution	what suitable distribution type we have employed for simulation such as "Poisson-Type A" or "Poisson-Type B" or "Lognormal-Type A" or "Lognormal-Type B" or "Poisson lognormal-Type A" or "Poisson lognormal-Type B"
n_sim	number of simulations

### Details

Let  $N'$  be the number of CFUs in the mixed sample, which is produced by the mixing of  $k$  primary samples and  $N' = \sum N_i$  and let  $N_i$  be the number of CFUs. For this package development, we have employed the notations 'Type-A' and 'Type-B' to indicate the type of distributions, which are applied in the previous literature as 'fair' and 'beta', respectively; see [Nauta \(2005\)](#).

This package will consider stage-by-stage the mixing process and assumes systematically breaking clusters at every stage of the mixing. Therefore, it can be assumed the concentration parameter also systematically changes with the concentration of the contribution.

### Value

The expected total number of CFUs in each revolution / stage.

### References

- Nauta, M.J., 2005. Microbiological risk assessment models for partitioning and mixing during food handling. International Journal of Food Microbiology 100, [311-322](#).

### See Also

[sim\\_single](#)

### Examples

```
mu <- 100
sigma <- 0.8
alpha_in <- 0.01
k <- c(30,75)
l <- 2500
rate <- 0.01
distribution <- c("Poisson lognormal-Type B","Poisson lognormal-Type B")
n_sim <- 2000
colMeans(sim_multiple_stages(mu, sigma, alpha_in, k, l, rate, distribution, n_sim))
```

---

sim_single	<i>The generated number of colony-forming units in the mixed sample by the simulation results in the single mixing plan with a single stage of the mixing.</i>
------------	--

---

### Description

This function calculates the resulting generated number of colony forming units in the mixed sample in the single mixing plan with single stage of the mixing.

### Usage

```
sim_single(mu, sigma, alpha, k, distribution, summary, n_sim)
```

### Arguments

mu	the average number of CFUs ( $\mu$ ) in the mixed sample, which is in a logarithmic scale if we use a Lognormal / Poisson lognormal distribution
sigma	the standard deviation of the colony-forming units in the mixed sample on the logarithmic scale (default value 0.8)
alpha	concentration parameter
k	number of small portions / primary samples
distribution	what suitable distribution type we have employed for simulation such as "Poisson-Type A" or "Poisson-Type B" or "Lognormal-Type A" or "Lognormal-Type B" or "Poisson lognormal-Type A" or "Poisson lognormal-Type B"
summary	if we need to get all simulated $N'$ , use summary = 2; otherwise, if we use summary = 1, the function provides the mean value of the simulated $N'$ .
n_sim	number of simulations

### Details

Let  $N'$  be the number of colony-forming units in the mixed sample which is produced by mixing of  $k$  primary samples and  $N' = \sum N_i$ . To more details, please refer the details section of [compare\\_mixing\\_3](#).

### Value

total number of colony forming units in the single mixing plan

## References

- Nauta, M.J., 2005. Microbiological risk assessment models for partitioning and mixing during food handling. International Journal of Food Microbiology 100, [311-322](#).

## See Also

[compare\\_mixing\\_3](#)

## Examples

```
mu <- 100
sigma <- 0.8
alpha <- 0.1
k <- 30
n_sim <- 20000
sim_single(mu, sigma, alpha, k, distribution = "Poisson lognormal-Type B", summary = 1, n_sim)
```

---

sim_single_pd	<i>The estimated value of detection probability at a single stage (or revolution) of the mixing process.</i>
---------------	--

---

## Description

This function gives a probability of detection at a single stage (or revolution) of the mixing process.

## Usage

```
sim_single_pd(mu, sigma, alpha, k, distribution, UDL, n_sim)
```

## Arguments

mu	the average number of CFUs ( $\mu$ ) in the mixed sample, which is in a logarithmic scale if we use a Lognormal / Poisson lognormal distribution
sigma	the standard deviation of the colony-forming units in the mixed sample on the logarithmic scale (default value 0.8)
alpha	concentration parameter
k	number of small portions / primary samples
distribution	what suitable distribution type we have employed for simulation such as "Poisson-Type A" or "Poisson-Type B" or "Lognormal-Type A" or "Lognormal-Type B" or "Poisson lognormal-Type A" or "Poisson lognormal-Type B"
UDL	the upper decision limit, which depends on the type of microorganisms and testing regulations.
n_sim	number of simulations

## Details

Let  $N'$  be the number of CFUs in the mixed sample, which is produced by the contribution of  $k$  primary samples mixing,  $N' = \sum N_i$  and let  $l$  be the number of stages in the mixing process. This function provides the probability of detection at each stage of the mixing process. The probability of detection can be determined by how many primary samples contain CFUs greater than UDL out of the number of primary samples engaged at each mixing stage.

Therefore, the probability of detection ( $p_d$ ) can be estimated from following formula,

$$p_d = \frac{\text{Number of primary samples which contain CFUs greater than UDL}}{\text{Number of primary samples}};$$

where the upper decision limit (UDL) depends on microorganisms and testing regulations. For example, UDL should be equal to 0 for testing Salmonella in milk powder sample if we consider 25g primary sample.

## Value

The probability of detection at each stage of the mixing process.

## References

- Nauta, M.J., 2005. Microbiological risk assessment models for partitioning and mixing during food handling. International Journal of Food Microbiology 100, 311-322.

## See Also

[sim\\_single\\_stages](#)

## Examples

```
mu <- 100
sigma <- 0.8
alpha <- 0.1
k <- 30
distribution <- "Poisson lognormal-Type B"
UDL <- 0
n_sim <- 2000
sim_single_pd(mu, sigma, alpha, k, distribution, UDL, n_sim)
```

---

sim\_single\_pd\_end\_stages

*The estimated value of detection probability at end of stage (or revolution) of the mixing process.*

---

## Description

This function gives a probability of detection at end of stage (or revolution) of the mixing process.

**Usage**

```
sim_single_pd_end_stages(
  mu,
  sigma,
  alpha_in,
  k,
  l,
  r,
  distribution,
  UDL,
  n_sim
)
```

**Arguments**

mu	the average number of CFUs ( $\mu$ ) in the mixed sample, which is in a logarithmic scale if we use a Lognormal / Poisson lognormal distribution
sigma	the standard deviation of the colony-forming units in the mixed sample on the logarithmic scale (default value 0.8)
alpha_in	concentration parameter at the initial stage
k	number of small portions / primary samples
l	number of revolutions /stages
r	the rate of the concentration parameter changes at each mixing stage
distribution	what suitable distribution type we have employed for simulation such as "Poisson-Type A" or "Poisson-Type B" or "Lognormal-Type A" or "Lognormal-Type B" or "Poisson lognormal-Type A" or "Poisson lognormal-Type B"
UDL	the upper decision limit, which depends on the type of microorganisms and testing regulations.
n_sim	number of simulations

**Details**

Let  $N'$  be the number of CFUs in the mixed sample, which is produced by the contribution of  $k$  primary samples mixing,  $N' = \sum N_i$  and let  $l$  be the number of stages in the mixing process. This function provides probability of detection at each stage of the mixing process. At each stage (or revolution), the probability of detection ( $p_d$ ) can be estimated by using function [sim\\_single\\_pd](#).

**Value**

The probability of detection at end of stage of the mixing process.

**References**

- Nauta, M.J., 2005. Microbiological risk assessment models for partitioning and mixing during food handling. International Journal of Food Microbiology 100, 311-322.

**See Also**

[sim\\_single\\_pd\\_stages](#)

**Examples**

```

mu <- 100
sigma <- 0.8
alpha_in <- 0.01
k <- 30
l <- 25000
r <- 0.01
distribution <- "Poisson lognormal-Type B"
UDL <- 0
n_sim <- 2000
sim_single_pd_end_stages(mu, sigma , alpha_in, k, l, r, distribution, UDL, n_sim)

```

---

sim_single_pd_stages	<i>The estimated value of detection probability at each stage (or revolution) of the mixing process.</i>
----------------------	--

---

**Description**

This function gives a probability of detection at each stage (or revolution) of the mixing process.

**Usage**

```
sim_single_pd_stages(mu, sigma, alpha_in, k, l, r, distribution, UDL, n_sim)
```

**Arguments**

mu	the average number of CFUs ( $\mu$ ) in the mixed sample, which is in a logarithmic scale if we use a Lognormal / Poisson lognormal distribution
sigma	the standard deviation of the colony-forming units in the mixed sample on the logarithmic scale (default value 0.8)
alpha_in	concentration parameter at the initial stage
k	number of small portions / primary samples
l	number of revolutions /stages
r	the rate of the concentration parameter changes at each mixing stage
distribution	what suitable distribution type we have employed for simulation such as "Poisson-Type A" or "Poisson-Type B" or "Lognormal-Type A" or "Lognormal-Type B" or "Poisson lognormal-Type A" or "Poisson lognormal-Type B"
UDL	the upper decision limit, which depends on the type of microorganisms and testing regulations.
n_sim	number of simulations

**Details**

Let  $N'$  be the number of CFUs in the mixed sample, which is produced by the contribution of  $k$  primary samples mixing,  $N' = \sum N_i$  and let  $l$  be the number of stages in the mixing process. This function provides probability of detection at each stage of the mixing process. At each stage (or revolution), the probability of detection ( $p_d$ ) can be estimated by using function [sim\\_single\\_pd](#).



**Value**

The probability of detection at each stage of the mixing process.

**References**

- Nauta, M.J., 2005. Microbiological risk assessment models for partitioning and mixing during food handling. *International Journal of Food Microbiology* 100, 311-322.

**See Also**

[sim\\_single\\_stages](#)

**Examples**

```
mu <- 100
sigma <- 0.8
alpha_in <- 0.01
k <- 30
l <- 25000
r <- 0.01
distribution <- "Poisson lognormal-Type B"
UDL <- 0
n_sim <- 2000
stages <- c(1:l)
Prob_df <-
data.frame(stages,sim_single_pd_stages(mu,sigma,alpha_in,k,l,r,distribution,UDL,n_sim))
colnames(Prob_df) <- c("no.revolutions","prob.detection")
plot_example <- ggplot2::ggplot(Prob_df) +
  ggplot2::geom_line(ggplot2::aes(x = stages, y = prob.detection)) +
  #ggplot2::stat_smooth(geom = "smooth", method = "gam", mapping = ggplot2::aes(x = no.revolutions,
  #y = prob.detection), se = FALSE, n = 1000) +
  ggplot2::ylab(expression("Prob. detection" ~~ (P[d[l]]))) +
  ggplot2::theme_classic() + ggplot2::xlab(expression("No. of revolutions")) +
  ggplot2::theme(plot.title = ggplot2::element_text(hjust = 0.5), legend.position = c(0.75,0.25)) +
  #ggplot2::ggtitle(label = f_spr(n_sim))+
  ggthemes::scale_colour_colorblind()
print(plot_example)
```

---

sim\_single\_stages

*The total number of colony-forming units in the mixed sample by the simulation results in the single mixing plan with l number of stages.*

---

**Description**

This function gives a simulated number of CFUs after each stage of the mixing process.

**Usage**

```
sim_single_stages(mu, sigma, alpha_in, k, l, r, distribution, n_sim)
```

**Arguments**

mu	the average number of CFUs ( $\mu$ ) in the mixed sample, which is in a logarithmic scale if we use a Lognormal / Poisson lognormal distribution
sigma	the standard deviation of the colony-forming units in the mixed sample on the logarithmic scale (default value 0.8)
alpha_in	concentration parameter at the initial stage
k	number of small portions / primary samples
l	number of revolutions / stages
r	the rate of the concentration parameter changes at each mixing stage
distribution	what suitable distribution type we have employed for simulation such as "Poisson-Type A" or "Poisson-Type B" or "Lognormal-Type A" or "Lognormal-Type B" or "Poisson lognormal-Type A" or "Poisson lognormal-Type B"
n_sim	number of simulations

**Details**

Let  $N'$  be the number of colony-forming units in the mixed sample which is produced by contribution of  $k$  primary samples mixing,  $N' = \sum N_i$  and  $l$  be the number of stages in the mixing process. This function provides simulated number of CFUs after each stages of the mixing process. To more details, please refer the details section of [compare\\_mixing\\_3](#).

**Value**

average number of colony forming units in the single mixing plan with  $l$  number of stages.

**References**

- Nauta, M.J., 2005. Microbiological risk assessment models for partitioning and mixing during food handling. International Journal of Food Microbiology 100, [311-322](#).

**See Also**

[sim\\_single](#)

**Examples**

```
mu <- 100
sigma <- 0.8
alpha_in <- 0.01
k <- 30
l <- 25000
r <- 0.01
distribution <- "Poisson lognormal-Type B"
n_sim <- 2000
stages <- c(1:l)
Prob_df <-
data.frame(stages, sim_single_stages(mu, sigma, alpha_in, k, l, r, distribution, n_sim))
colnames(Prob_df) <- c("no.revolutions", "CFU")
plot_sim_single_stages <- ggplot2::ggplot(Prob_df, ggplot2::aes(x = no.revolutions, y = CFU)) +
ggplot2::geom_line() +
# tidyquant::geom_ma(ma_fun = SMA, n = 50, linetype = 1, colour = "red") +
ggplot2::xlab(expression("Number of revolutions")) +
```

```
ggplot2::ylab(expression("Expected total number of CFUs")) +  
ggplot2::theme_classic() +  
ggplot2::theme(plot.title = ggplot2::element_text(hjust = 0.5)) +  
ggthemes::scale_colour_colorblind()  
print(plot_sim_single_stages)
```

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