

Assignment 3

Question 1

① characteristic table

| P | N | Q_{t+1} | |
|---|---|-----------|------------|
| 0 | 0 | 0 | clear to 0 |
| 0 | 1 | Q_t | no change |
| 1 | 0 | Q_t' | complement |
| 1 | 1 | 1 | set to 1 |

③ excitation table

| Q_t | Q_{t+1} | P | N |
|-------|-----------|---|---|
| 0 | 0 | 0 | X |
| 0 | 1 | 1 | X |
| 1 | 0 | X | 0 |
| 1 | 1 | X | 1 |

② truth table

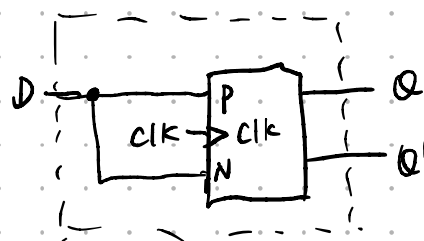
| P | N | Q_t | Q_{t+1} |
|---|---|-------|-----------|
| 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 0 |
| 0 | 1 | 0 | 0 |
| 0 | 1 | 1 | 1 |
| 1 | 0 | 0 | 1 |
| 1 | 0 | 1 | 0 |
| 1 | 1 | 0 | 1 |
| 1 | 1 | 1 | 1 |

④ PN flip flop \rightarrow D flip flop

| Present | Input | Next | pnFF Input | |
|---------|-------|-----------|------------|---|
| Q_t | X | Q_{t+1} | P | N |
| 0 | 0 | 0 | 0 | X |
| 0 | 1 | 1 | 1 | X |
| 1 | 0 | 0 | X | 0 |
| 1 | 1 | 1 | X | 1 |

Karnaugh map

| PN \ Q_t | Q_t | |
|------------|-------|---|
| | 0 | 1 |
| 0 0 | 0 | 0 |
| 0 1 | 0 | 1 |
| 1 1 | 1 | 1 |
| 1 0 | 1 | 0 |



D-Flip Flop

| Q_t | D | Q_{t+1} |
|-------|---|-----------|
| 0 | 0 | 0 |
| 0 | 1 | 1 |
| 1 | 0 | 0 |
| 1 | 1 | 1 |

| D | Q_{t+1} |
|---|-----------|
| 0 | 0 |
| 1 | 1 |

characteristic equation: $Q_{t+1} = Q_t N + Q_t' P$

Question 2

$$JKFF: Q_{t+1} = JQ_t' + K'Q_t$$

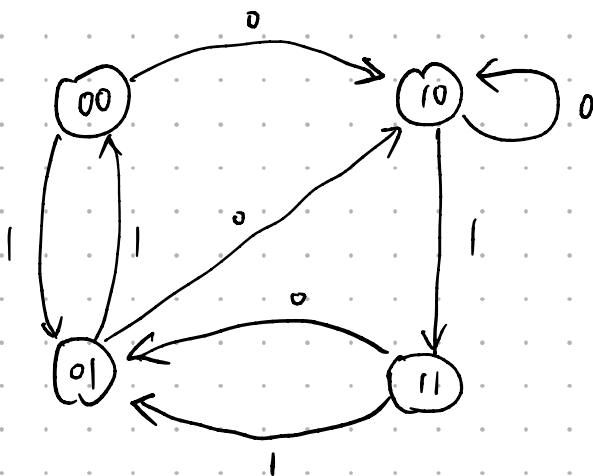
$$A(t+1) = J_A A' + K_A' A = x'A' + B'A$$

$$B(t+1) = J_B B' + K_B' B = xB' + AB$$

$$\begin{cases} A(t+1) = x'A'(t) + B'(t)A(t) \\ B(t+1) = xB'(t) + A(t)B(t) \end{cases}$$

| present | | Next | | | |
|---------|---|------|---|-----|---|
| | | x=0 | | x=1 | |
| A | B | A | B | A | B |
| 0 | 0 | 1 | 0 | 0 | 1 |
| 0 | 1 | 1 | 0 | 0 | 0 |
| 1 | 0 | 1 | 0 | 1 | 1 |
| 1 | 1 | 0 | 1 | 0 | 1 |

state diagram



Question 3

② state table

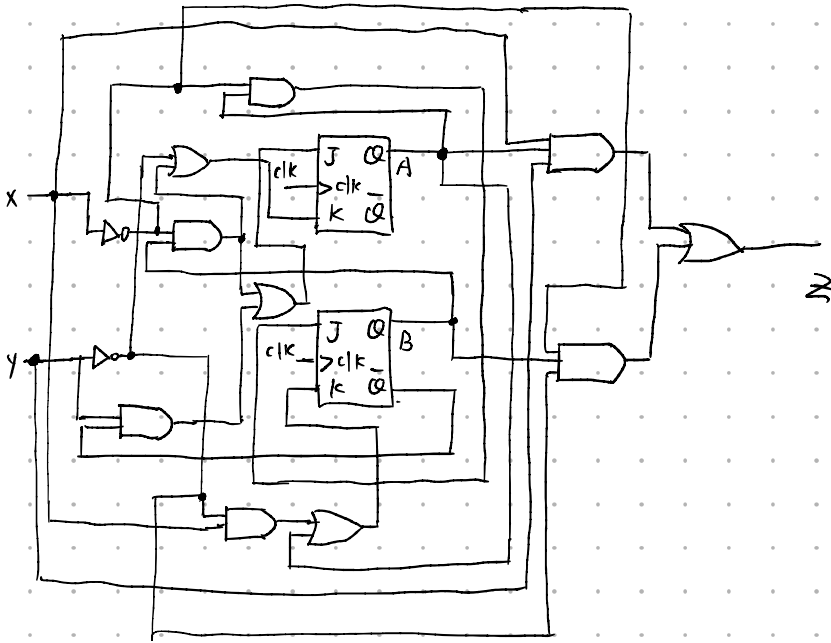
如果写成行格式

$$JKFF: Q_{t+1} = JQ_t' + K'Q_t$$

$$\begin{cases} J_A = Bx' + B'y \\ K_A = Bx' + y' \end{cases} \begin{cases} J_B = Ax' \\ K_B = A + xy' \end{cases}$$

$$Z = Axy + Bx'y'$$

logic diagram:



| Present | Next | | | | Output | | | |
|---------|----------|----------|----------|----------|----------|----------|----------|----------|
| | x=0, y=0 | x=0, y=1 | x=1, y=0 | x=1, y=1 | x=0, y=0 | x=0, y=1 | x=1, y=0 | x=1, y=1 |
| A B | A B | A B | A B | A B | z | z | z | z |
| 0 0 | 0 0 | 1 0 | 0 0 | 1 0 | 0 | 0 | 0 | 0 |
| 0 1 | 1 1 | 1 1 | 0 0 | 0 1 | 1 | 0 | 0 | 0 |
| 1 0 | 0 1 | 1 1 | 0 0 | 1 0 | 0 | 0 | 0 | 1 |
| 1 1 | 0 0 | 0 0 | 0 0 | 1 0 | 1 | 0 | 0 | 1 |

| Present | | Input | | Next | | Output |
|---------|---|-------|---|------|---|--------|
| A | B | x | y | A | B | z |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 1 | 1 | 0 | 0 |
| 0 | 0 | 1 | 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 1 | 1 | 0 | 0 |
| 0 | 1 | 0 | 0 | 1 | 1 | 1 |
| 0 | 1 | 0 | 1 | 1 | 1 | 0 |
| 0 | 1 | 1 | 0 | 0 | 0 | 0 |
| 0 | 1 | 1 | 1 | 0 | 0 | 0 |
| 1 | 0 | 0 | 0 | 0 | 1 | 0 |
| 1 | 0 | 0 | 1 | 1 | 1 | 0 |
| 1 | 0 | 1 | 0 | 0 | 0 | 0 |
| 1 | 0 | 1 | 1 | 0 | 0 | 1 |
| 1 | 1 | 0 | 0 | 0 | 0 | 1 |
| 1 | 1 | 0 | 1 | 0 | 0 | 0 |
| 1 | 1 | 1 | 0 | 0 | 0 | 0 |
| 1 | 1 | 1 | 1 | 1 | 0 | 1 |

③ karnaugh map for A_{t+1}

| A _t B _t \ xy | 00 | 01 | 11 | 10 |
|------------------------------------|----|----|----|----|
| 00 | 0 | 1 | 1 | 0 |
| 01 | 1 | 1 | 0 | 0 |
| 11 | 0 | 0 | 1 | 0 |
| 10 | 0 | 1 | 1 | 0 |

$$A(t+1) = B(t)y + A(t)xy + A'(t)B(t)x'$$

state equation for A and B

$$\begin{cases} A(t+1) = B(t)y + A(t)xy + A'(t)B(t)x' \\ B(t+1) = A'(t)B(t)x' + A'(t)B(t)y + A(t)B'(t)x' \end{cases}$$

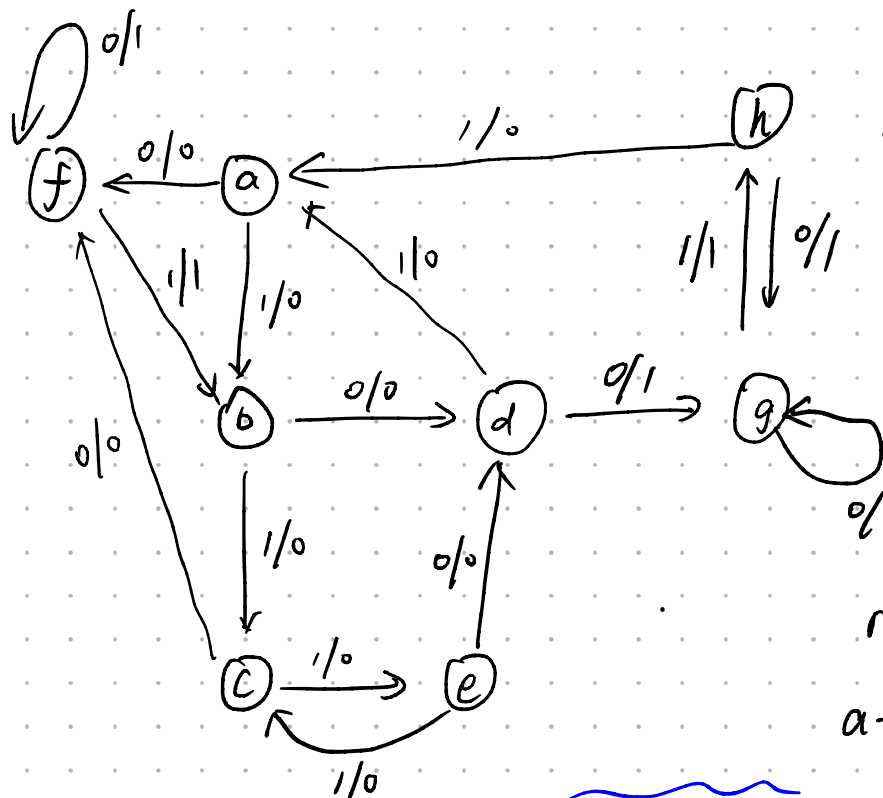
karnaugh map for B_{t+1}

| A _t B _t \ xy | 00 | 01 | 11 | 10 |
|------------------------------------|----|----|----|----|
| 00 | 0 | 0 | 0 | 0 |
| 01 | 1 | 1 | 1 | 0 |
| 11 | 0 | 0 | 0 | 0 |
| 10 | 1 | 1 | 0 | 0 |

$$B(t+1) = A'(t)B(t)x' + A'(t)B(t)y + A(t)B'(t)x'$$

Question 4

① state diagram



④ 0/0/00/0111

original table:

$$a \xrightarrow{0} f \xrightarrow{1} b \xrightarrow{0} d \xrightarrow{0} a \xrightarrow{0} f \xrightarrow{1} f$$
$$\begin{array}{ccccccccc} \xrightarrow{1} & b & \xrightarrow{0} & d & \xrightarrow{1} & a & \xrightarrow{1} & b & \xrightarrow{1} & c \\ & 1 & & 0 & & 0 & & 0 & & 0 \end{array}$$

Output \rightarrow 01000110000

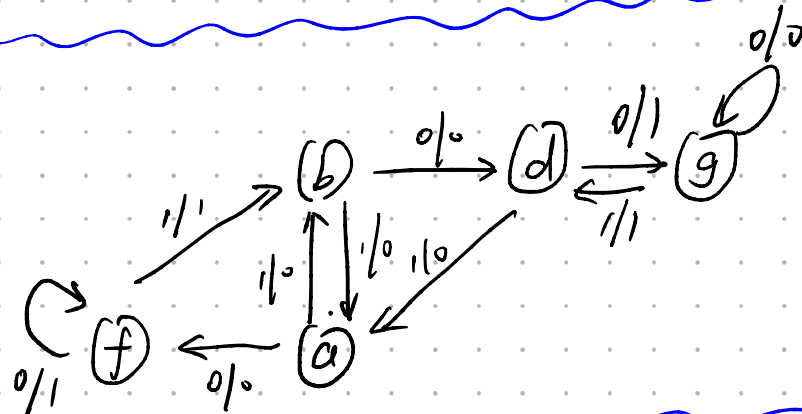
reduced table.

[illegible]

②

| present | Next State | | Output | |
|---------|------------|-----|--------|-----|
| | x=0 | x=1 | x=0 | x=1 |
| a | f | b | 0 | 0 |
| b | d | a | 0 | 0 |
| d | g | a | 1 | 0 |
| f | f | b | 1 | 1 |
| g | g | d | 0 | 1 |

Output → 01000110000



Question 5

| Present | | Input | Output | | Input for TFF | |
|---------|---|-------|--------|----|----------------|----------------|
| A | B | x | A' | B' | T _A | T _B |
| 0 | 0 | 0 | 0 | 1 | 0 | 1 |
| 0 | 0 | 1 | 0 | 0 | 0 | 0 |
| 0 | 1 | 0 | 1 | 1 | 1 | 0 |
| 0 | 1 | 1 | 1 | 0 | 1 | 1 |
| 1 | 0 | 0 | 1 | 1 | 0 | 1 |
| 1 | 0 | 1 | 1 | 0 | 0 | 0 |
| 1 | 1 | 0 | 0 | 0 | 1 | 1 |
| 1 | 1 | 1 | 1 | 1 | 0 | 0 |

| AB \ x | 0 | 1 |
|--------|---|---|
| 00 | 0 | 0 |
| 01 | 1 | 1 |
| 11 | 1 | 0 |
| 10 | 0 | 0 |

$$T_A = A'B + Bx'$$

| AB \ x | 0 | 1 |
|--------|---|---|
| 00 | 1 | 0 |
| 01 | 0 | 1 |
| 11 | 1 | 0 |
| 10 | 1 | 0 |

$$T_B = A'Bx + B'x' + Ax'$$

Input Equation

$$\begin{cases} T_A = A'B + Bx' \\ T_B = A'Bx + B'x' + Ax' \end{cases}$$