

## UNIT-3 (CPU SCHEDULING)

CPU SCHEDULING:- CPU Scheduling is a process of determining which process will own CPU for execution while another process is on hold.

### PURPOSE OF SCHEDULING ALGORITHM:-

- (1) maximum CPU utilization
- (2) fair-allocation of CPU
- (3) maximum throughput
- (4) minimum waiting time

### TYPES OF CPU SCHEDULING ALGORITHM:-

- (1) Preemptive Algorithm
- (2) Non Preemptive

#### PREEMPTIVE ALGORITHM

- (1) Shortest Remaining time first (SRTF) (SJF)  
Shortest Job first.
- (2) Round Robin (RR) scheduling
- (3) Priority Scheduling

#### NON-PREEMPTIVE SCHEDULING ALGORITHM:-

- (1) First come first serve (FCFS)
- (2) Shortest Job first (SJF)
- (3) Priority scheduling.
- (4) multilevel queue
- (5) Highest Response Ratio Next (HRRN)

## PERFORMANCE CRITERIA FOR CPU SCHEDULING

- (1) Arrival time (A.T)
- (2) Burst time (B.T)
- (3) Completion time (C.T)
- (4) Turn around time (T.A.T)
- (5) Waiting time (W.T)
- (6) Response time

ARRIVAL TIME (A.T):- The time at which the process enters into the ready queue is called arrival time.

BURST TIME (B.T):- The amount of time required by the CPU to execute the process is called burst time. This does not include waiting time.

COMPLETION TIME:- The time at which the process completes its execution is called completion time (C.T).

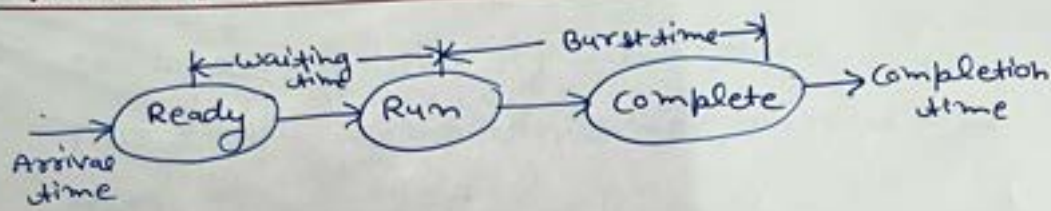
TURN-AROUND TIME:- The amount of time spent by the process from its arrival to its completion is called turn-around time (T.A.T)

WAITING TIME:- The amount of time for which the process waits for the CPU to be assigned is called waiting time (W.T).



RESPONSE TIME :- Response time is the time spent when the process is in the ready queue and gets the CPU the first time.

VARIOUS TIME RELATED TO THE PROCESS:-



NON-PREEMPTIVE ALGORITHM:-

(1) FIRST COME FIRST SERVE (FCFS) Scheduling Algorithm:-

Ex1 Consider the following process

Process	Burst time
P <sub>1</sub>	7
P <sub>2</sub>	5
P <sub>3</sub>	6
P <sub>4</sub>	3

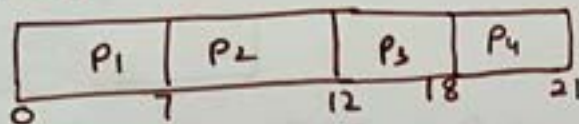
what is the average waiting time and turn around time for these process with FCFS Scheduling.

Sol →

Process	Burst time	Arrival time
P <sub>1</sub>	7	0
P <sub>2</sub>	5	0
P <sub>3</sub>	6	0
P <sub>4</sub>	3	0

Criteria ⇒  
Arrival time  
mode ⇒ non-Preemptive

Step-1:  
Gantt chart / Bar chart



turn around time of all Process.

T.A.T (P<sub>1</sub>) = Completion time - Arrival time

$$(T.A.T) P_1 = 7 - 0$$

$$(T.A.T) P_1 = 7$$

$$(T.A.T) P_2 = CT - A.T$$

$$(T.A.T) P_2 = 12 - 0$$

$$(T.A.T) P_2 = 12$$

$$(T.A.T) P_3 = CT - AT$$

$$(T.A.T) P_3 = 18 - 0$$

$$(T.A.T) P_3 = 18$$

$$(T.A.T) P_4 = CT - A.T$$

$$(T.A.T) P_4 = 21 - 0$$

$$(T.A.T) P_4 = 21$$

$$\begin{aligned} \text{Average turn around time (T.A.T)} &= \frac{P_1 + P_2 + P_3 + P_4}{4} \\ &= \frac{7 + 12 + 18 + 21}{4} \\ &= \frac{58}{4} \Rightarrow 14.5 \text{ unit} \end{aligned}$$



(5)

Waiting time = Turnaround time - Burst time

$$W.T(P_1) = 7 - 7$$

$$W.T(P_1) = 0$$

$$W.T(P_2) = T.A.T - B.T$$

$$W.T(P_2) = 12 - 5$$

$$W.T(P_2) = 7$$

$$W.T(P_3) = T.A.T - B.T$$

$$W.T(P_3) = 18 - 6$$

$$W.T(P_3) = 12$$

$$W.T(P_4) = T.A.T - B.T$$

$$W.T(P_4) = 21 - 3$$

$$W.T(P_4) = 18$$

$$\text{Average waiting time} = \frac{P_1 + P_2 + P_3 + P_4}{4}$$

$$= \frac{0 + 7 + 12 + 18}{4}$$

$$= \frac{37}{4}$$

$$= 9.25 \text{ units}$$

$$\text{Average waiting time} = 9.25 \text{ units. Avg}$$

(6)

example-2 Consider the following process

Process	Burst time
P <sub>1</sub>	2
P <sub>2</sub>	5
P <sub>3</sub>	3
P <sub>4</sub>	9
P <sub>5</sub>	4

What is the average waiting time and turn around time for these process with FCFS scheduling.  
(Do your self)

FIRST COME FIRST SERVE (FCFS) :-

Criteria  $\Rightarrow$  Arrival time

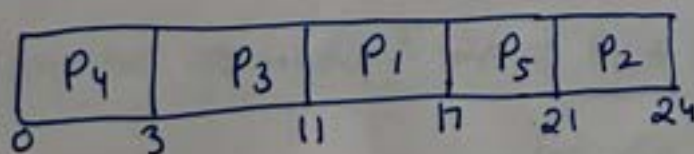
mode  $\Rightarrow$  Non-Preemptive

Process	Average time	Burst time
P <sub>1</sub>	2	6
P <sub>2</sub>	5	3
P <sub>3</sub>	1	8
P <sub>4</sub>	0	3
P <sub>5</sub>	4	4

calculate average waiting time.

Gantt Chart / Bar chart :-

Step-1



⑦

turn around time of  $P_i$  = Completion Time - Arrival time

$$T.A.T(P_1) = CT - AT$$

$$T.A.T(P_1) = 17 - 2$$

$$T.A.T(P_1) = 15$$

$$T.A.T(P_2) = CT - AT$$

$$T.A.T(P_2) = 24 - 5$$

$$T.A.T(P_2) = 19$$

$$T.A.T(P_3) = CT - AT$$

$$T.A.T(P_3) = 11 - 1$$

$$T.A.T(P_3) = 10$$

$$T.A.T(P_4) = CT - AT$$

$$T.A.T(P_4) = 3 - 0$$

$$T.A.T(P_4) = 3$$

$$T.A.T(P_5) = CT - AT$$

$$T.A.T(P_5) = 21 - 4$$

$$T.A.T(P_5) = 17$$

$$\text{Average turn around time} = \frac{P_1 + P_2 + P_3 + P_4 + P_5}{5}$$

$$= \frac{15 + 19 + 10 + 3 + 17}{5}$$

$$= \frac{54}{5} = 10.8 \text{ units}$$



(8)

waiting time = Turned around time - Burst time

$$W.T(P_1) = T.A.T - B.T$$

$$W.T(P_1) = 15 - 6$$

$$W.T(P_1) = 9$$

$$W.T(P_2) = T.A.T - B.T$$

$$W.T(P_2) = 19 - 3$$

$$W.T(P_2) = 16$$

$$W.T(P_3) = T.A.T - B.T$$

$$W.T(P_3) = 10 - 8$$

$$W.T(P_3) = 2$$

$$W.T(P_4) = T.A.T - B.T$$

$$W.T(P_4) = 3 - 3$$

$$W.T(P_4) = 0$$

$$W.T(P_5) = T.A.T - B.T$$

$$W.T(P_5) = 17 - 4$$

$$W.T(P_5) = 13$$

$$\begin{aligned} \text{Average waiting time} &= \frac{P_1 + P_2 + P_3 + P_4 + P_5}{5} \\ &= \frac{9 + 16 + 2 + 0 + 13}{5} \\ &= \frac{40}{5} = 8 \text{ units} \underline{\underline{Ans}} \end{aligned}$$



(9)

## SHORTEST JOB FIRST (SJF) NON PREEMPTIVE SCHEDULING ALGORITHM

Process	Arrival time	Burst time
P <sub>1</sub>	2	6
P <sub>2</sub>	5	2
P <sub>3</sub>	1	8
P <sub>4</sub>	0	3
P <sub>5</sub>	4	4

Criteria  $\Rightarrow$  Burst-time  
mode  $\Rightarrow$  Non-Preemptive

Calculate Avg waiting time and avg turn around time.

Grant chart:-

$P_4$	$P_1$	$P_2$	$P_5$	$P_3$	
0	3	9	11	15	23

Turn around time of = Completion time - Arrival time

$$T.A.T \text{ of } P_1 = CT - A.T$$

$$T.A.T(P_1) = 9 - 2$$

$$T.A.T(P_1) = 7$$

$$T.A.T \text{ of } P_2 = CT - A.T$$

$$T.A.T \text{ of } (P_2) = 11 - 5$$

$$T.A.T(P_2) = 6$$

Turn around time of  $P_3 = CT - AT$

$$T.A.T(P_3) = 23 - 1$$

$$T.A.T(P_3) = 22$$

$$T.A.T(P_4) = CT - AT$$

$$T.A.T(P_4) = 0 - 0$$

$$T.A.T(P_4) = 0$$

$$T.A.T(P_5) = CT - AT$$

$$T.A.T(P_5) = 15 - 4$$

$$T.A.T(P_5) = 11$$

$$\text{Average turn Around time} = \frac{P_1 + P_2 + P_3 + P_4 + P_5}{5}$$

$$= \frac{7 + 6 + 22 + 3 + 11}{5}$$

$$= \frac{13 + 25 + 11}{5}$$

$$= \frac{38 + 11}{5}$$

$$= \frac{49}{5}$$

$$= 9.8 \text{ units}$$



(11)

Waiting time = Turnaround time - Burst time

$$W.T(P_1) = T.A.T - B.T$$

$$W.T(P_1) = 7 - 6$$

$$\boxed{W.T(P_1) = 1}$$

$$W.T(P_2) = T.A.T - B.T$$

$$W.T(P_2) = 6 - 2$$

$$\boxed{W.T(P_2) = 4}$$

$$W.T(P_3) = T.A.T - B.T$$

$$W.T(P_3) = 22 - 8$$

$$\boxed{W.T(P_3) = 14}$$

$$W.T(P_4) = T.A.T - B.T$$

$$W.T(P_4) = 3 - 3$$

$$\boxed{W.T(P_4) = 0}$$

$$W.T(P_5) = T.A.T - B.T$$

$$W.T(P_5) = 11 - 4$$

$$\boxed{W.T(P_5) = 7}$$

$$\text{Average waiting time} = \frac{P_1 + P_2 + P_3 + P_4 + P_5}{5}$$

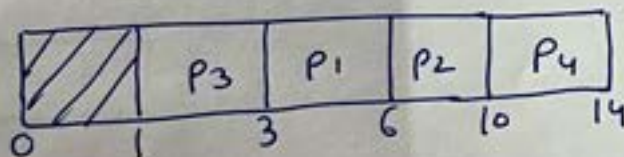
$$= \frac{1 + 4 + 14 + 0 + 7}{5}$$

$$= \frac{26}{5} = 5.2 \text{ units. } \underline{\underline{\text{Ans}}}$$

(2)

SHORTEST JOB FIRST (SJF) NON PREEMPTIVE:-Ex Calculate the Average Turn around time and Average waiting time.

Process	Arrival time	Burst time
P <sub>1</sub>	1	3
P <sub>2</sub>	2	4
P <sub>3</sub>	1	2
P <sub>4</sub>	4	1

Criteria  $\Rightarrow$  Burst-time  
mode  $\Rightarrow$  No PreemptiveStep 1:Gantt Chart:

Turn around time = Completion time  
— Arrival time

Completion time P<sub>1</sub> = 6C.T P<sub>2</sub> = 10C.T P<sub>3</sub> = 3C.T P<sub>4</sub> = 14T.A.T (P<sub>1</sub>) = C.T - A.TT.A.T (P<sub>1</sub>) = 6 - 1

T.A.T (P<sub>1</sub>) = 5



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$$T.A.T(P_2) = CT - AT$$

$$T.A.T(P_2) = 10 - 2$$

$$\boxed{T.A.T(P_2) = 8}$$

$$T.A.T(P_3) = CT - AT$$

$$T.A.T(P_3) = 3 - 1$$

$$\boxed{T.A.T(P_3) = 2}$$

$$T.A.T(P_4) = CT - AT$$

$$T.A.T(P_4) = 14 - 4$$

$$\boxed{T.A.T(P_4) = 10}$$

$$\text{Average turn around time} = \frac{P_1 + P_2 + P_3 + P_4}{4}$$

$$= \frac{5 + 8 + 2 + 10}{4}$$

$$= \frac{25}{4}$$

$$= 6.25 \text{ units.}$$

Waiting time = turnaround time - Burst time

$$W.T(P_1) = T.A.T - B.T$$

$$W.T(P_1) = 5 - 3$$

$$\boxed{W.T(P_1) = 2}$$

waiting time of  $P_2$  = Turn around time -  
Burst time

$$W.T(P_2) = T.A.T - B.T$$

$$W.T(P_2) = 8 - 4$$

$$W.T(P_2) = 4$$

$$W.T(P_3) = T.A.T - B.T$$

$$W.T(P_3) = 2 - 2$$

$$W.T(P_3) = 0$$

$$W.T(P_4) = T.A.T - B.T$$

$$W.T(P_4) = 10 - 1$$

$$W.T(P_4) = 9$$

$$\text{Average waiting time} = \frac{P_1 + P_2 + P_3 + P_4}{4}$$

$$= \frac{2 + 4 + 0 + 9}{4}$$

$$= \frac{15}{4}$$

$$= 3.75 \text{ Avg}$$

SJF (Shortest Job First) :-

In this algorithm allocates CPU Based on CPU Burst time.



⇒ Process with the smallest burst time will be allocated to the CPU first.

⇒ if two Process is Having the same Burst-time then FCFS (first come - first serve) is follow.

⇒ It also called Shortest - next CPU Burst - algorithm.

PRIORITY SCHEDULING (NON-PREEMPTIVE)

Higher the No - Higher the Priority. Calculate the average W.T & Avg

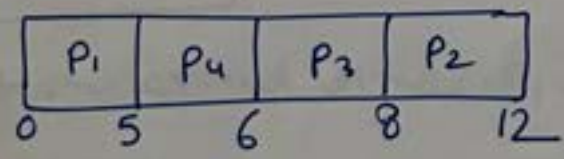
Priority	Process	Arrival time	Burst time
1	P <sub>1</sub>	0	5
2	P <sub>2</sub>	1	4
3	P <sub>3</sub>	2	2
→ 4 (H)	P <sub>4</sub>	4	1

+ AT?

Criteria ⇒ Priority  
mode ⇒ Non-Pre-emptive

Step 1:

Gantt Chart:



Average waiting turnaround time

= Completion time - Arrival time

P<sub>1</sub> completion time = 5

P<sub>2</sub> (C.T) = 12

P<sub>3</sub> (C.T) = 8

P<sub>4</sub> (C.T) = 6

Turnaround time = completion time - Arrival time

$$T.A.T(P_1) = C.T - A.T$$

$$T.A.T(P_1) = 5 - 0$$

$$T.A.T(P_1) = 5$$

$$T.A.T(P_2) = C.T - A.T$$

$$T.A.T(P_2) = 12 - 1$$

$$T.A.T(P_2) = 11$$

$$T.A.T(P_3) = C.T - A.T$$

$$T.A.T(P_3) = 8 - 2$$

$$T.A.T(P_3) = 6$$

$$T.A.T(P_4) = C.T - A.T$$

$$T.A.T(P_4) = 6 - 4$$

$$T.A.T(P_4) = 2$$

Average turn-around time =  $\frac{P_1 + P_2 + P_3 + P_4}{4}$

$$= \frac{5 + 11 + 6 + 2}{4}$$

$$= \frac{24}{4}$$

$$= 6$$

units.



(17)

Waiting time = turn around time - Burst time

$$W.T(P_1) = T.A.T - B.T$$

$$W.T(P_1) = 5 - 5$$

$$W.T(P_1) = 0$$

$$W.T(P_2) = T.A.T - B.T$$

$$W.T(P_2) = 11 - 4$$

$$W.T(P_2) = 7$$

$$W.T(P_3) = T.A.T - B.T$$

$$W.T(P_3) = 6 - 2$$

$$W.T(P_3) = 4$$

$$W.T(P_4) = T.A.T - B.T$$

$$W.T(P_4) = 2 - 1$$

$$W.T(P_4) = 1$$

$$\text{Average Waiting time} = \frac{P_1 + P_2 + P_3 + P_4}{4}$$

$$= \frac{0 + 7 + 4 + 1}{4}$$

$$= \frac{12}{4}$$

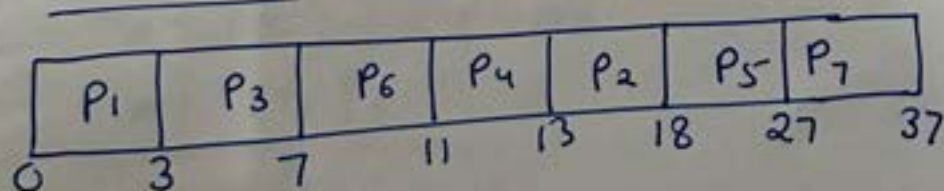
$$= 3 \text{ units Avg}$$

Ex2 calculate the Average turn around time and waiting time given Lesser the Number Highest Priority.

Process	Priority	Arrival time	Burst time
P <sub>1</sub>	→ 2 (H)	0	3
P <sub>2</sub>	6	2	5
P <sub>3</sub>	3	1	4
P <sub>4</sub>	5	4	2
P <sub>5</sub>	7	6	9
P <sub>6</sub>	4	5	4
P <sub>7</sub>	→ 10 (L)	7	10

Step 1:

Gantt chart:



Completion time of

$$P_1 (C.T) = 3$$

$$P_2 (C.T) = 18$$

$$P_3 (C.T) = 7$$

$$P_4 (C.T) = 13$$

$$P_5 (C.T) = 27$$

$$P_6 (C.T) = 11$$

$$P_7 (C.T) = 37$$



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Turn around time = completion time - Arrival time

$$T.A.T(P_1) = C.T - A.T$$

$$T.A.T(P_1) = 3 - 0$$

$$T.A.T(P_1) = 3$$

$$T.A.T(P_2) = C.T - A.T$$

$$T.A.T(P_2) = 18 - 2$$

$$T.A.T(P_2) = 16$$

$$T.A.T(P_3) = C.T - A.T$$

$$T.A.T(P_3) = 7 - 1$$

$$T.A.T(P_3) = 6$$

$$T.A.T(P_4) = C.T - A.T$$

$$T.A.T(P_4) = 13 - 4$$

$$T.A.T(P_4) = 9$$

$$T.A.T(P_5) = C.T - A.T$$

$$T.A.T(P_5) = 27 - 6$$

$$T.A.T(P_5) = 21$$

$$T.A.T(P_6) = C.T - A.T$$

$$T.A.T(P_6) = 11 - 5$$

$$T.A.T(P_6) = 6$$

$$T.A.T(P_7) = C.T - A.T$$

$$T.A.T(P_7) = 37 - 7$$

$$T.A.T(P_7) = 30$$

(20)

$$\begin{aligned}
 \text{Average turn around time} &= \frac{P_1 + P_2 + P_3 + P_4 + P_5 + P_6 + P_7}{7} \\
 &= \frac{3 + 16 + 6 + 9 + 21 + 6 + 30}{7} \\
 &= \frac{25 + 30 + 36}{7} \\
 &= \frac{45 + 36}{7} \\
 &= \frac{81}{7} \\
 &= 11.5 \text{ units}
 \end{aligned}$$

Average waiting time = Turnaround time - Burst time

$$WT(P_1) = T.A.T - B.T$$

$$WT(P_1) = 3 - 3$$

$$\boxed{WT(P_1) = 0}$$

$$WT(P_2) = T.A.T - B.T$$

$$WT(P_2) = 16 - 5$$

$$\boxed{WT(P_2) = 11}$$

$$WT(P_3) = T.A.T - B.T$$

$$WT(P_3) = 6 - 4$$

$$\boxed{WT(P_3) = 2}$$



Waiting time of  $P_1 = T \cdot A \cdot T - B \cdot T$

$$W.T(P_1) = 9 - 2$$

$$\boxed{W.T(P_1) = 7}$$

$$W.T(P_5) = T \cdot A \cdot T - B \cdot T$$

$$W.T(P_5) = 21 - 9$$

$$\boxed{W.T(P_5) = 12}$$

$$W.T(P_6) = T \cdot A \cdot T - B \cdot T$$

$$W.T(P_6) = 6 - 4$$

$$\boxed{W.T(P_6) = 2}$$

$$W.T(P_7) = T \cdot A \cdot T - B \cdot T$$

$$W.T(P_7) = 30 - 10$$

$$\boxed{W.T(P_7) = 20}$$

$$\text{Average waiting time} = \frac{P_1 + P_2 + P_3 + P_4 + P_5 + P_6 + P_7}{7}$$

$$= \frac{0 + 11 + 2 + 7 + 12 + 2 + 20}{7}$$

$$= \frac{20 + 34}{7}$$

$$= \frac{54}{7}$$

$$= 7.714285714 \text{ units Avg}$$

## ROUND-ROBIN SCHEDULING:-

⇒ Round - Robin scheduling algorithm is a Preemptive algorithm. CPU selects the Process from the ready queue. To implement RR Scheduling, ready queue is maintained as a FIFO queue (first in first out) of the Processes. New Processes are added to the tail of the ready queue.

The CPU Scheduler picks the first Process from the ready queue through the system.

if the time quantum is very short, then short Processes will move through the system relatively quickly. It increases the processing overhead involved in handling the clock interrupt and performing the scheduling and dispatch function.

Ex Let us consider the set of Processes with Burst time in milliseconds. All the Processes are arrived at time 0, we can draw the Gantt chart calculate W.T and so on.

Process	Burst time

criteria ⇒ time quantum  
mode ⇒ Preemptive



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Ex Round-Robin Preemptive Algorithm:-

time quantum = 2 units

calculate average TAT & avg w.T

Process	Arrival time	Burst time	Completion time	TAT	w.T
P <sub>1</sub>	0	8	7	7	4
P <sub>2</sub>	1	6	19	18	12
P <sub>3</sub>	2	2	6	4	2
P <sub>4</sub>	3	2	9	5	4
P <sub>5</sub>	4	5	22	18	13
P <sub>6</sub>	5	4	21	15	11

Ready Queue  $\Rightarrow$ 

P <sub>1</sub>	P <sub>2</sub>	P <sub>3</sub>	P <sub>4</sub>	P <sub>5</sub>	P <sub>6</sub>	P <sub>5</sub>	P <sub>2</sub>	P <sub>6</sub>	P <sub>5</sub>
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Grant Chart  $\Rightarrow$ 

P <sub>1</sub>	P <sub>2</sub>	P <sub>3</sub>	P <sub>1</sub>	P <sub>4</sub>	P <sub>5</sub>	P <sub>2</sub>	P <sub>6</sub>	P <sub>5</sub>	P <sub>2</sub>	P <sub>6</sub>	P <sub>5</sub>
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0 2 4 6 7 9 11 13 15 17 19 21 22

Completion time of P<sub>1</sub> = 7

P<sub>2</sub> = 19

P<sub>3</sub> = 6

P<sub>4</sub> = 9

P<sub>5</sub> = 22

P<sub>6</sub> = 21

Turn around time = Completion time - Arrival time

$$T.A.T \text{ of } (P_1) = 7 - 0$$

$$T.A.T (P_1) = 7$$

$$T.A.T \text{ of } (P_2) = C.T - A.T$$

$$T.A.T (P_2) = 19 - 1$$

$$T.A.T (P_2) = 18$$

$$T.A.T (P_3) = C.T - A.T$$

$$T.A.T (P_3) = 6 - 2$$

$$T.A.T (P_3) = 4$$

$$T.A.T (P_4) = C.T - A.T$$

$$T.A.T (P_4) = 9 - 3$$

$$T.A.T (P_4) = 6$$

$$T.A.T (P_5) = C.T - A.T$$

$$T.A.T (P_5) = 22 - 4$$

$$T.A.T (P_5) = 18$$

$$T.A.T (P_6) = C.T - A.T$$

$$T.A.T (P_6) = 21 - 5$$

$$T.A.T (P_6) = 16$$



(25)

$$\text{Average w turn around time} = \frac{P_1 + P_2 + P_3 + P_4 + P_5 + P_6}{6}$$

$$= \frac{7 + 18 + 4 + 6 + 18 + 16}{6}$$

$$= \frac{25 + 10 + 34}{6}$$

$$= \frac{25 + 44}{6}$$

$$= \frac{69}{6}$$

$$= 11.5 \text{ units.}$$

$$\text{Waiting time} = \text{Turnaround time} - \text{Burst time}$$

$$W.T(P_1) = T.A.T - B.T$$

$$W.T(P_1) = 7 - 3$$

$$W.T(P_1) = 4$$

$$W.T(P_2) = T.A.T - B.T$$

$$W.T(P_2) = 18 - 6$$

$$W.T(P_2) = 12$$

$$W.T(P_3) = T.A.T - B.T$$

$$W.T(P_3) = 4 - 2$$

$$W.T(P_3) = 2$$

$$W.T(P_4) = T.A.T - B.T$$

$$W.T(P_4) = 18 - 5$$

$$W.T(P_4) = 13$$

$$W.T(P_4) = 2$$

$$W.T(P_5) = T.A.T - B.T$$

$$W.T(P_5) = 18 - 5$$

$$= 13$$

$$W.T(P_6) = T.A.T - B.T$$

$$W.T(P_6) = 15 - 4$$

$$W.T(P_6) = 11$$

$$\text{Average waiting time} = \frac{P_1 + P_2 + P_3 + P_4 + P_5 + P_6}{6}$$

$$= \frac{4 + 12 + 2 + 4 + 14 + 11}{6}$$

$$= \frac{47}{6}$$

$$= 7.8 \text{ units Avg}$$

Round Robin Algorithm:-

if CPU scheduling policy is RR mode - preemptive with the time-quantum = 2 units calculate the average waiting time and average turn around time.



Process	Arrival time	B.T	C.T	T.A.T	W.T	R.T
P <sub>1</sub>	0	5/3/0	13	13	8	0
P <sub>2</sub>	1	2/1/0	12	11	8	2
P <sub>3</sub>	2	1/0	5	3	2	4
P <sub>4</sub>	3	2/0	9	6	4	7
P <sub>5</sub>	4	3/1/0	14	10	7	9

Ready queue:-

P <sub>1</sub>	P <sub>2</sub>	P <sub>3</sub>	P <sub>1</sub>	P <sub>4</sub>	P <sub>5</sub>	P <sub>2</sub>	P <sub>1</sub>	P <sub>5</sub>	
----------------	----------------	----------------	----------------	----------------	----------------	----------------	----------------	----------------	--

Grant Chart  $\Rightarrow$

P <sub>1</sub>	P <sub>2</sub>	P <sub>3</sub>	P <sub>1</sub>	P <sub>4</sub>	P <sub>5</sub>	P <sub>2</sub>	P <sub>1</sub>	P <sub>5</sub>	
0	2	4	5	7	9	11	12	13	14

Completion time of P<sub>1</sub> = 13

$$C.T (P_2) = 12$$

$$C.T (P_3) = 5$$

$$C.T (P_4) = 9$$

$$C.T (P_5) = 14$$

Turn around time = Completion time - Arrival time

$$T.A.T (P_1) = C.T - A.T$$

$$T.A.T (P_1) = 13 - 0$$

$$T.A.T (P_1) = 13$$

$$T.A.T(P_2) = C.T - A.T$$

$$T.A.T(P_2) = 12 - 1$$

$$\boxed{T.A.T(P_2) = 11}$$

$$T.A.T(P_3) = C.T - A.T$$

$$T.A.T(P_3) = 5 - 2$$

$$\boxed{T.A.T(P_3) = 3}$$

$$T.A.T(P_4) = C.T - A.T$$

$$T.A.T(P_4) = 9 - 3$$

$$\boxed{T.A.T(P_4) = 6}$$

$$T.A.T(P_5) = C.T - A.T$$

$$T.A.T(P_5) = 14 - 4$$

$$\boxed{T.A.T(P_5) = 10}$$

$$\text{Average Turn around time} = \frac{P_1 + P_2 + P_3 + P_4 + P_5}{5}$$

$$= \frac{13 + 11 + 3 + 6 + 10}{5}$$

$$= \frac{42}{5}$$

$$= 8.4 \text{ units } \underline{\underline{A.T}}$$



A waiting time = Turn around time - Burst time

$$W.T \text{ of } (P_1) = T.A.T - B.T$$

$$W.T (P_1) = 13 - 5$$

$$W.T (P_1) = 8$$

$$W.T \text{ of } (P_2) = T.A.T - B.T$$

$$W.T \text{ of } (P_2) = 11 - 3$$

$$W.T (P_2) = 8$$

$$W.T (P_3) = T.A.T - B.T$$

$$W.T (P_3) = 3 - 1$$

$$W.T (P_3) = 2$$

$$W.T \text{ of } (P_4) = T.A.T - B.T$$

$$W.T \text{ of } (P_4) = 6 - 2$$

$$W.T \text{ of } (P_4) = 4$$

$$W.T \text{ of } (P_5) = T.A.T - B.T$$

$$W.T (P_5) = 10 - 3$$

$$W.T (P_5) = 7$$

$$\Rightarrow \text{Average waiting time} = \frac{P_1 + P_2 + P_3 + P_4 + P_5}{5}$$

$$= \frac{8 + 8 + 2 + 4 + 7}{5}$$

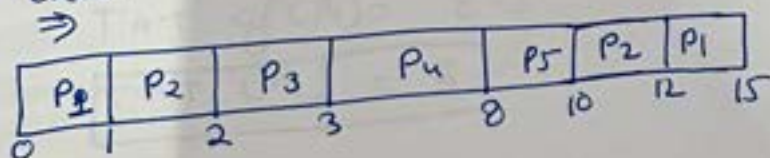
$$= \frac{29}{5} = 5.8 \text{ units Ag}$$

# PRIORITY SCHEDULING (Preemptive)

Ex. Consider the set of 5 Processes whose arrival time and burst time are given below: if the CPU Scheduling Policy is Preemptive Priority. Calculate the average waiting time. (Higher Priority number represents higher priority).

Process	Arrival time	BURST TIME	Priority
P <sub>1</sub>	0	43	2
P <sub>2</sub>	1	20	3
P <sub>3</sub>	2	10	4
P <sub>4</sub>	3	54	5 ← (H)
P <sub>5</sub>	4	21	5

Gantt Chart  
⇒



Ready Queue:

P <sub>1</sub>	P <sub>2</sub>	P <sub>3</sub>	P <sub>4</sub>
----------------	----------------	----------------	----------------

$$P_1 = 0 +$$

Completion time of P<sub>1</sub> = 15

C.T of P<sub>2</sub> = 12

C.T of P<sub>3</sub> = 3

C.T of P<sub>4</sub> = 8



(3)

turn around time = completion time - arrival time

$$\text{T.A.T of } P_1 = \text{C.T} - \text{A.T} \\ = 15 - 0$$

$$\boxed{\text{T.A.T } (P_1) = 15}$$

$$\text{T.A.T of } P_2 = \text{C.T} - \text{A.T}$$

$$\text{T.A.T } (P_2) = 12 - 1$$

$$\boxed{\text{T.A.T } (P_2) = 11}$$

$$\text{T.A.T of } P_3 = \text{C.T} - \text{A.T}$$

$$\text{T.A.T of } (P_3) = 8 - 2$$

$$\boxed{\text{T.A.T } (P_3) = 6}$$

$$\text{T.A.T of } (P_4) = \text{C.T} - \text{A.T}$$

$$\text{T.A.T of } (P_4) = 8 - 3$$

$$\boxed{\text{T.A.T } (P_4) = 5}$$

$$\text{T.A.T of } (P_5) = \text{C.T} - \text{A.T}$$

$$\text{T.A.T } (P_5) = 10 - 4$$

$$\boxed{\text{T.A.T } (P_5) = 6}$$

waiting time = turnaround time - Burst time

$$WT \text{ of } (P_1) = TAT - B.T$$

$$WT (P_1) = 15 - 4$$

$$WT (P_1) = 11$$

$$WT \text{ of } (P_2) = TAT - B.T$$

$$WT (P_2) = 11 - 2$$

$$WT (P_2) = 9$$

$$WT \text{ of } (P_3) = TAT - B.T$$

$$WT (P_3) = 8 - 2$$

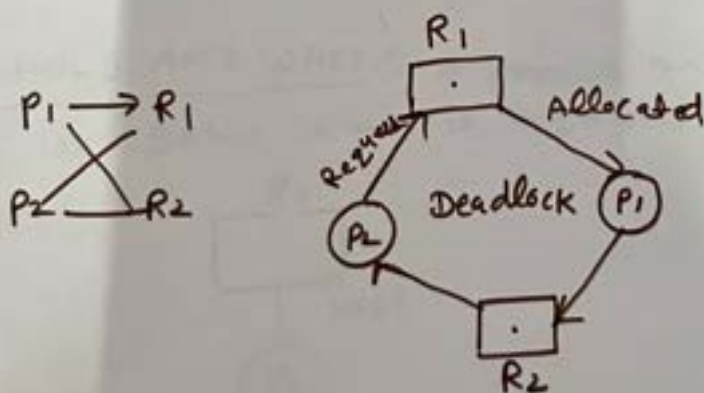
$$WT (P_3) =$$





DEADLOCK :- A Deadlock is a Situation where a group of Processes are permanently blocked as a result of each Process having acquired a subset of the resources needed for its completion and waiting for release of the remaining resource held by others in the same group.

Deadlock is a state between two or more Resources in which they are completing for each other Resources for completing their task, and no one is Ready to leave Resources, that means waiting for that which cannot occur.



### DEADLOCK CHARACTERIZATION!

In a deadlock Processes never finish executing and system resources are tied-up preventing other jobs from starting.

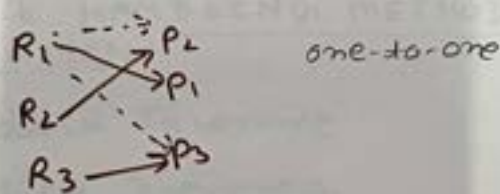
### NECESSARY CONDITIONS FOR DEADLOCK!

Deadlock can arise if four conditions hold

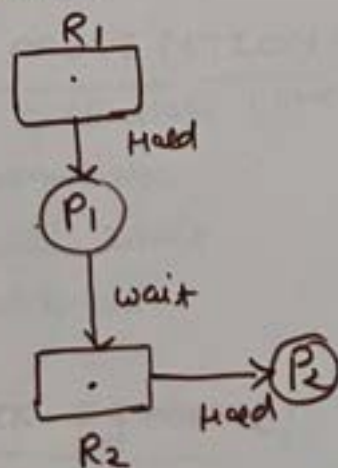
- (1) mutual exclusion
- (2) Hold and wait
- (3) No-Preemption
- (4) Circular wait

### (1) MUTUAL EXCLUSION:

only one process may use a resource at a time. Once a process has been allocated a particular resource, it has exclusive use of the resource. No other process can use a resource while it is allocated to a process.



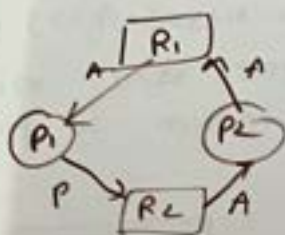
(2) HOLD AND WAIT: A process may hold a resource at the same time it requests another one.



(3) NO PRE-EMPTION: No Resource can be forcibly removed from a process holding it. Resources can be released only one by the explicit action of the process, rather than by the action of an external authority.



(4) CIRCULAR WAIT! All the Processes must be waiting for the resource in a cyclic manner.



DEADLOCK HANDLING METHOD AND DEADLOCK PREVENTION!

- ⇒ Deadlock Ignorance
- ⇒ Deadlock Prevention
- ⇒ Deadlock avoidance (Banker's Algo)
- ⇒ Deadlock detection and recovery. (RAG)

DEADLOCK PREVENTION!

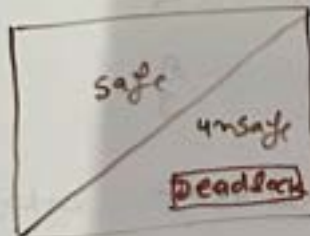
- (1) Mutual Exclusion (Share resource)
- (2) No Preemption
- (3) Hold and wait
- (4) Circular wait.

(1) Deadlock Ignorance! - we ignore the problem as if it does not exist.

(2) Deadlock Prevention!

## DEADLOCK AVOIDANCE:-

- (i) Safe State:- A state is safe if the system can allocate Resource upto its maximum in some sequence (safe sequence) and still Avoid Dead lock. Safe sequence may not be unique there may be multiple safe sequence.



### Safety Algorithm:

- (i)  $work = Available$   
 $finish = false$
- (ii) Find an 'i' such that  
 $Finish[i] = false$  and  
 $Need_i \leq work$   
if no such i, go to step 4
- (iii)  $Finish[i] = true$   
 $work = work + Allocation_i$
- (iv) if  $Finish[i] = true$  for all i,  
then the system is safe.



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→ A state is said to be safe if it is not deadlocked and there is some scheduling order in which every process can run to completion even if they suddenly request their maximum number of resource immediately.

ex	Process	Allocated	maximum
	A	3	9
	B	2	4
	C	2	7

total resources are 10

7 resources already allocated

so there are three resources free

$$\text{Free Resource} = 10 - 7 \\ = 3$$

A need 6 resources more to complete it

$$\text{Need} = \text{maximum} - \text{Allocation} \\ = 9 - 3 \\ = 6$$

$$\text{B need} = 4 - 2$$

$$= 2 \text{ Resources}$$

$$\text{C need} = 7 - 2 = 5 \text{ resources more to complete}$$

Process	Allocate	max	
A	3	9	$9-3=6$
B	2	4	$4-2=2$
C	2	7	$7-2=5$

Free Resource = 3

Process	Allocd	max	
A	3	9	$9-3=6$
B	<del>2</del>	<del>4</del>	-
C	2	7	$7-2=5$

Free Resource = 5

Process	Allocated	max	
A	3	9	$9-3=6$
B	0	-	-
C	0	-	-

free resource = 7

Process	Allocated	max	
A	0	-	-
B	0	-	-
C	0	-	-

free = 1



(39)

Safe Sequence

$\langle B, C, A \rangle$

### BANKER'S ALGORITHM:-

⇒ The Banker's algorithm is the best known of the avoidance strategies. The strategy is modelled after the leading policies employed in banking system. The resource-allocation graph algorithm is suitable to a resource allocation system with single instances of each resource type.

⇒ Banker's Algorithm is suitable to a resource allocation system with multiple instances of each resource type. Algorithm makes decisions on granting a resource based on whether or not granting the request will put the system into an unsafe state.

⇒ Several data structure must be maintained to implement the Banker's algorithm. Let  $n$  be the number of processes in the system and  $m$  be the number of resource types. We need the following data-structure.

- (1) Available
- (2) max
- (3) Allocation
- (4) Need.



(40)

(1) Available:- A vector of length  $m$  indicates the number of available resources of each type. if available  $[j] = k$  there are  $k$  instances of resource type  $R_j$  available.

2) max:- An  $n \times m$  matrix defines the maximum demand of each process. if  $\text{max}[i, j] = t$  then process  $P_i$  may request at most  $t$  instances of resource type  $R_j$ .

(3) Allocation:- An  $n \times m$  matrix defines the number of resources of each type currently allocated to each process. if allocation  $[i, j] = k$ , then process  $P_i$  is currently allocated  $k$  instances of resource type  $R_j$ .

(4) Need:- An  $n \times m$  matrix indicates the remaining resource need of each process. if need  $[i, j] = k$ , then process  $P_i$  may need  $k$  more instances of resource type  $R_j$  to complete its task.  $\text{Need}[i, j] = \text{max}[i, j] - \text{Allocation}[i, j]$

### ALGORITHM:-

Bankers Algorithm is the combination of Safety Algorithm and the resource request Algorithm.



(41)

Step 1: Initialize work = available

finish[i] = false for  $i = 0, 1, 2, 3, \dots, n-1$

Step 2:

check the availability

Need[i]  $\leq$  work go to Step 3

else finish[i] = false if i does  
not exist go  
to Step 4

Step 3: work = work + Allocation[i]

finish[i] = true then go to Step 2

~~else finish[i] = false if i~~

Step 4: if finish[i] = true for all

System is safe state

Need = Maximum -  
Allocation

Example:

Consider a system that contains five processes  $P_1, P_2, P_3, P_4, P_5$ , and three types A, B & C. A has 10, B has 5 and C has 7 instances.

(42)

Process	Allocation			maximum			Available			Need		
	A	B	C	A	B	C	A	B	C	A	B	C
P <sub>1</sub>	0	1	0	7	5	3	3	3	2	7	4	3
P <sub>2</sub>	2	0	0	3	2	2				1	2	2
P <sub>3</sub>	3	0	2	9	0	2				6	0	0
P <sub>4</sub>	2	1	1	2	1	1				0	0	0
P <sub>5</sub>	0	0	2	4	3	3				4	3	1

Step 1:

Available work = 3 3 2

 $Need_1 \leq work$  $7\ 4\ 3 \leq 3\ 3\ 2$  P<sub>1</sub> is not executed. $Need_2 \leq work$  $1\ 2\ 2 \leq 3\ 3\ 2$  P<sub>2</sub> is executedwork = work + Allocation of P<sub>2</sub>

work = 3 3 2 + 2 0 0

work = 5 3 2

 $Need_3 \leq work$  $6\ 0\ 0 \leq 5\ 3\ 2$  false P<sub>3</sub> waiting $Need_4 \leq work$  $0\ 0\ 0 \leq 5\ 3\ 2$  done P<sub>4</sub> executed.



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$$\begin{aligned}\text{New work} &= \text{work} + \text{Allocation of } P_4 \\ &= 532 + 211 \\ &= 743\end{aligned}$$

$$\text{Need}_5 \leq \text{work}$$

$$431 \leq 743 \text{ true } P_5 \text{ executed.}$$

$$\text{Need}_1 \leq \text{work}$$

$$743 \leq 745 \text{ true.}$$

$$\text{work} = \text{work} + \text{Allocation of } P_1$$

$$\begin{aligned}\text{work} &= 745 + 010 \\ &= 755\end{aligned}$$

$$\text{Need}_3 \leq \text{work}$$

$$600 \leq 755 \text{ true } P_3 \text{ is executed}$$

$$\text{new work} = \text{work} + \text{Allocation of } P_3$$

$$\begin{aligned}\text{new work} &= 755 + 302 \\ &= 1057\end{aligned}$$

Safe Sequence

$$\langle P_2, P_4, P_5, P_1, P_3 \rangle \text{ Ans}$$

Ex2

Process	Allocation A B C D	maximum A B C D	Available A B C D	Need A B C D
P <sub>0</sub>	0 0 1 2	0 0 1 2	1 5 2 0	0 0 0 0
P <sub>1</sub>	1 0 0 0	1 7 5 0	1 5 3 2	0 7 5 0
P <sub>2</sub>	1 3 5 4	2 3 5 6	2 8 8 6	1 0 0 2
P <sub>3</sub>	0 6 3 2	0 6 5 2	2 14 11 8	0 0 2 0
P <sub>4</sub>	0 0 1 4	0 6 5 6	2 14 12 12	0 6 4 2
			3 14 12 12	

Do you get?

<P<sub>0</sub>, P<sub>2</sub>, P<sub>3</sub>, P<sub>4</sub>, P<sub>1</sub>>RESOURCES ALLOCATION GRAPH:-

○ ⇒ Process

□ ⇒ Resource

□.. ⇒ Number of Instances

⇒ Request and Allocated arrow like