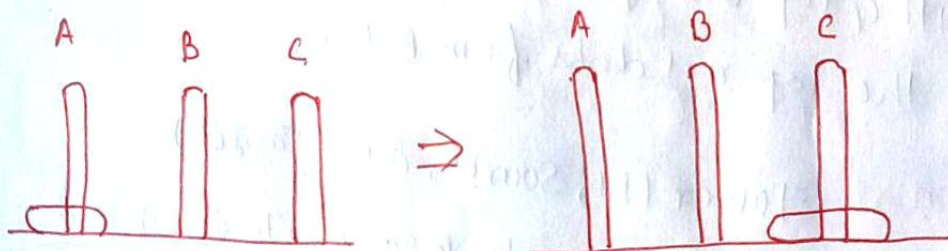


Tower of Hanoi Problem - In this problem, there are  $n$  disks of different sizes and there are three rods A, B and C. All the  $n$  disks are placed on rod A in such a way that a larger disk is always below a smaller disk. The other two rods are initially empty. The aim is to move the  $n$  disks to the rod C using rod B as a temporary storage.

The rules for the movement of disks are as follows:

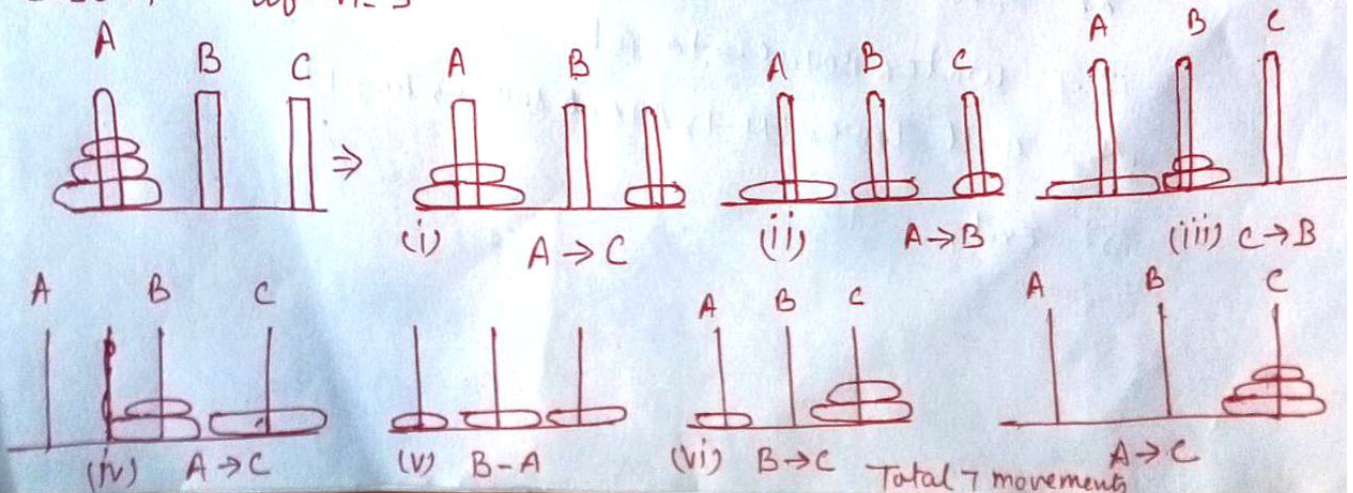
- Only one disk move at a time.
- A larger disk must never be stacked above a smaller one.
- Only the top disk on any rod may be moved to any other rod.

Case 1:- if  $n=1$



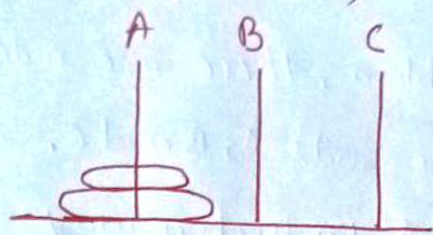
$A \rightarrow C$  Total 1 movement

Case 2:- If  $n=3$

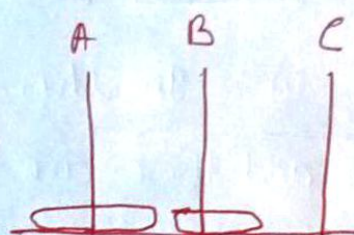




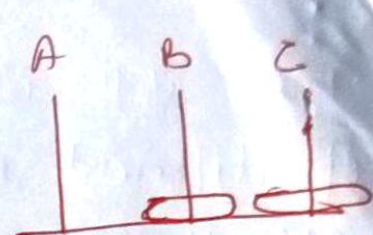
iii) If  $(n=2)$



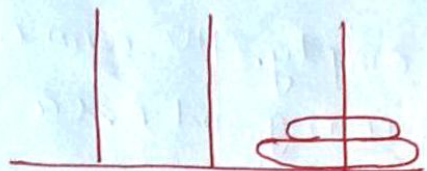
$\Rightarrow$



$A \rightarrow B$   
(i)



$A \rightarrow C$   
(ii)



(iii)  $B \rightarrow C$

Total 3 movements

so if there are  $n$  disk then total movement needed  $= 2^n - 1$

We use recursion to solve tower of hanoi problem.

The solution to tower of Hanoi for  $n > 1$  disks may be reduced to the following sub problems.

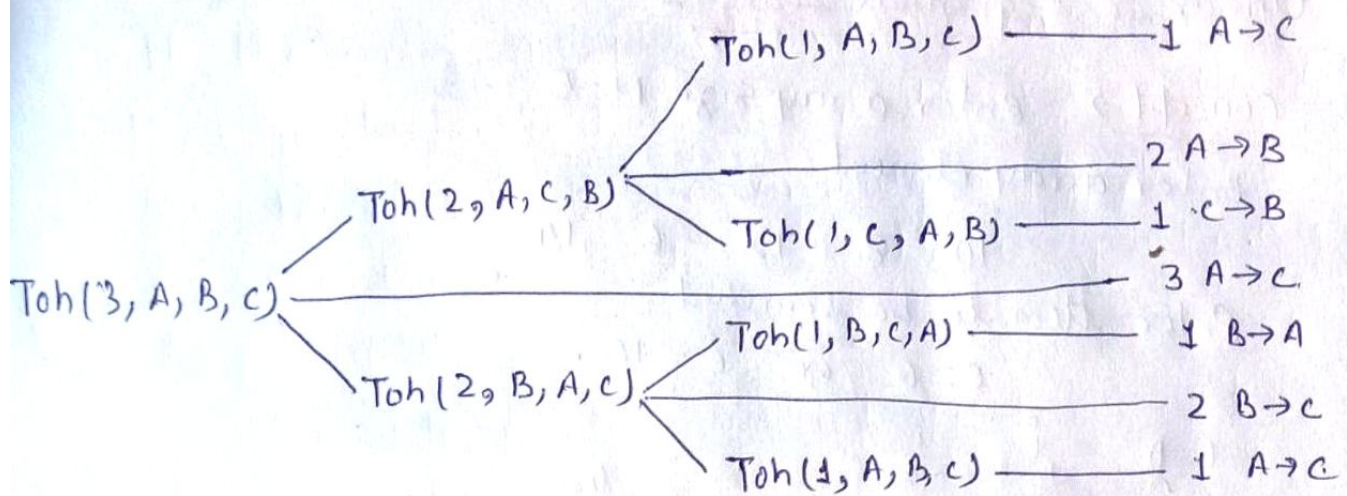
- (i) move the top  $n-1$  disks from A to B
- ii) move the top disk from A to C
- iii) move the top  $n-1$  disks from B to C

Algorithm  $\rightarrow$  Tower ( $M$ , Source, Aux, Target)

1. If  $M=1$  then write  $\text{Source} \rightarrow \text{Target}$  & Exit
2. Call Tower( $M-1$ , source, Target, Aux)
3. write  $\text{source} \rightarrow \text{target}$
4. Call Tower( $M-1$ , Aux, Source, Target)
5. Exit.



Example →  $Toh(3, A, B, C)$



C program →

```

void toh(int N, char S, char A, char T)
{
    if (N > 0)
    {
        toh(N-1, S, T, A);
        printf("move %d disk from %c to %c", N, S, T);
        toh(N-1, A, S, T);
    }
}

int main()
{
    char S = 'A', aux = 'B', T = 'C';
    int n;
    printf("Enter no. of disk");
    scanf("%d", &n);
    toh(n, S, A, T);
}
  
```