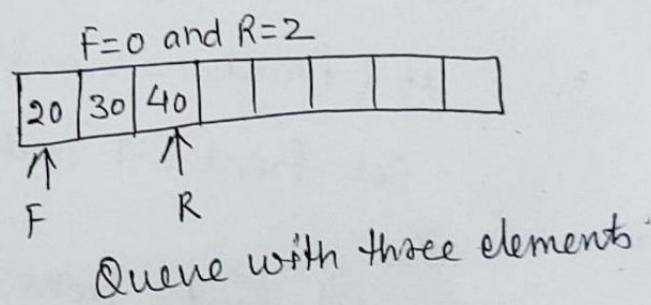
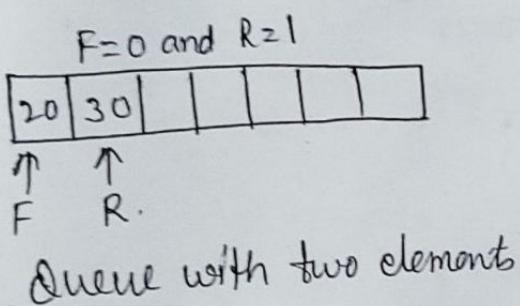
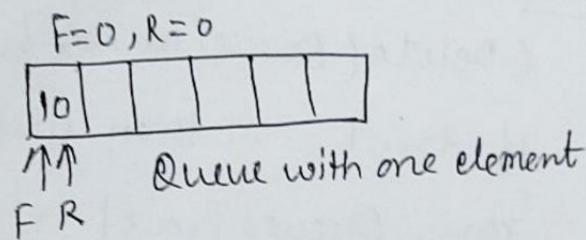
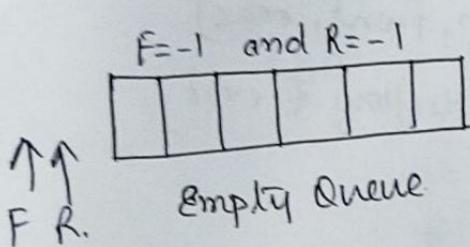


Queue → Queue is logically a first in first out types of list.

→ Queue is a non primitive linear data structure.

→ Queue is a homogeneous collection of elements in which new elements are added at one end called rear and existing elements are deleted from other end called the front.



Note- if $F == R$ then only one element is a Queue.

$$\text{No. of elements in a Queue} = R - F + 1$$

Implementation of Queue

- 1) Using array
- 2) using linked list

1) Using array → `QInsert(Queue[maxsize], ITEM, front, rear)`

Queue[maxsize] is the array, item is inserted or deleted in a Queue. front and rear is used for insertion deletion and insertion respectively.

⑤

1. if $\text{rear} == \text{maxsize}-1$ then write overflow and exit.
2. if $\text{rear} == -1$ then set $\text{rear} = 0$ and $\text{front} = 0$
else set $\text{rear} = \text{rear} + 1$
3. $\text{Queue}[\text{rear}] = \text{item}$
4. Exit

2) Deletion -

QDelete(Queue[maxsize], item, front, rear)

1. if $\text{front} == -1$ then write underflow & exit
2. $\text{item} = \text{Queue}[\text{front}]$
3. if ($\text{front} == \text{rear}$) then
Set $\text{front} = -1$ and $\text{rear} = -1$
else
set $\text{front} = \text{front} + 1$
4. Exit

3) Traversal -

Qtraverse(Queue[maxsize], front, rear)

1. if $\text{rear} == -1$ then write Queue is empty & exit.
2. ~~for~~ $i = \text{front}$
3. repeat step 4 & 5 until $i <= \text{rear}$
4. Display $\text{Queue}[i]$
5. $i = i + 1$
[END of Loop]
6. Exit

③

C function → Insertion

#define maxsize 30

int queue[maxsize], front=-1, rear=-1;

void insert()

{

int item;

~~if (front == (rear + 1) * maxsize)~~

~~if (rear == maxsize - 1) {~~

~~if (rear == maxsize - 1)~~
printf("Overflow");

else { exit(0); }

}

if (rear == -1)

{

front = 0;

rear = 0;

}

else

rear = (rear + 1); ~~maxsize~~;

printf("Enter item");

scanf("%d", &item);

queue[rear] = item;

}

}

```

void deletion()
{
    if (front == -1)
        printf("Underflow");
    else
    {
        if (front == rear)
        {
            front = -1;
            rear = -1;
        }
        else
            front = (front + 1); for i=front+1 to rear;
    }
}

```

```

void display()
{
    int i;
    if (rear == -1)
        printf("queue is empty");
    else
    {
        for (i = front; i <= rear; i++ i = (i + 1) % size)
            printf("%d", queue[i]);
    }
}

```

```

void main()
{
    insert();
    Insert();
    deletion();
    display();
}

```

2) Linked List Implementation

(6)

Algorithm →

Insert (Queue, front, rear, info, next, item, new)

1. new = AVAIL
2. if (new == NULL) write overflow & exit.
3. Info[new] = item
4. LINK[new] = NULL
5. if (front == NULL) then
 front = new and rear = new
6. else

~~rear → rear~~

LINK[rear] = new

Rear = new.
7. Exit

Deletion (Queue, front, rear, PTR, next, INFO)

1. if (front == NULL)
 write ~~over~~ underflow and exit
2. PTR = front
3. Display *INFO[PTR] is deleted
4. if (~~front~~ → LINK[front] == NULL) then
 front = NULL and rear = NULL & exit.
5. front = LINK[front]
6. free (PTR)
7. exit.

⑥

Traverse()

1. If (front == NULL) then make Queue's empty front

2. ptr = front

3. repeat step 4 & 5 till ptr != NULL

4. Display ptr->info

5. ptr = ptr->next

6. exit.

C function → ~~insert~~

void insert()

struct node,

{

int info;

struct node *next;

} *front = NULL, *rear = NULL;

void insert()

{

struct node *new;

new = (struct node *) malloc(sizeof(struct node));

If (new == NULL)

printf("Overflow");

else

{

printf("Enter item");

scanf("%d", &new->info);

new->next = NULL;

(7)

```

if (.front == NULL)
{
    front = new;
    rear = new;
}
else
{
    rear->next = new;
    rear = new;
}

```

void deletion()

```

{
    struct node *p;
    if (front == NULL)
        printf("Underflow");
    else
    {
        p = front;
        printf("%d is deleted", p->info);
        if (p->next == NULL) or if (front == rear)
            front = rear = NULL
        else
            front = front->next
            free(p);
    }
}

```

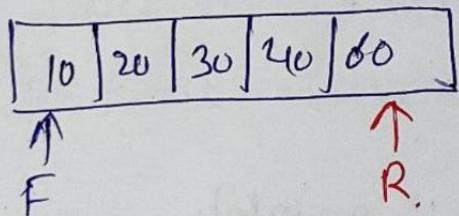
```

⑧ void traverse()
{
    struct node *p;
    int i;
    if( Rear == NULL)
        printf("Queue is empty");
    else
        for( f=front; p!=NULL; p=p->next)
            printf("%d", p->info);
}

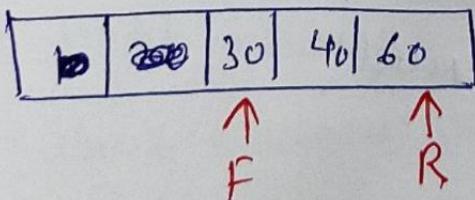
```

Limitation of ~~Circular~~ Queue -

Overflow condition
if ($\text{year} == \text{max_size} - 1$)



Deleted ~~the~~ Two items



In above $R = maxsize - 1$, so no item can be inserted even there is a space in Queue for two items.

Circular Queue

⑨

problem of simple queue can be solved by circular queue.

In a circular queue the insertion of new element is done at first location of Queue if the last location of the Queue is full.



Overflow condition (Array implementation)

If ($\text{front} = (\text{rear} + 1) \% \text{maxsize}$)
printf("Overflow");

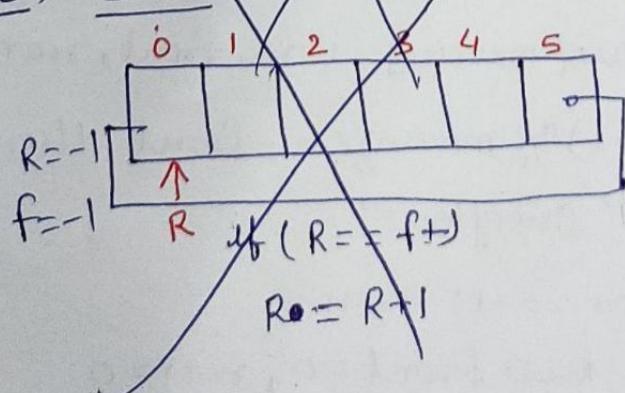
Underflow condition

$\text{front} = -1$ or $\text{rear} = -1$

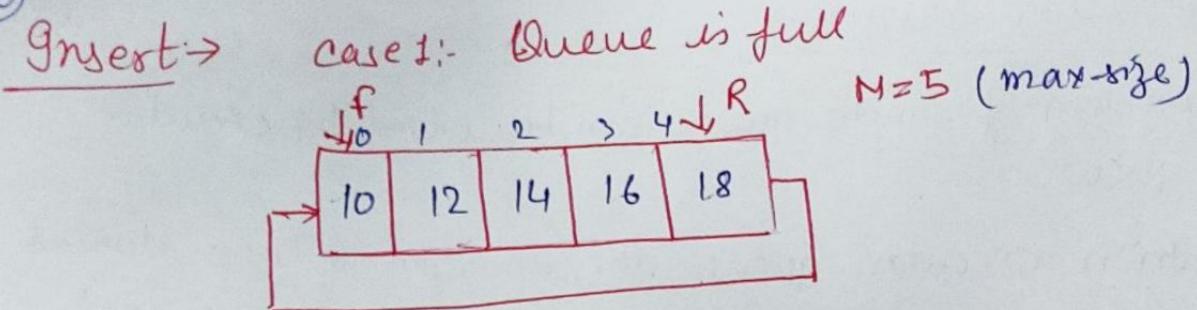
operations on circular Queue (Array implementation)

1) Insert →

concept → case 1 → Queue is empty

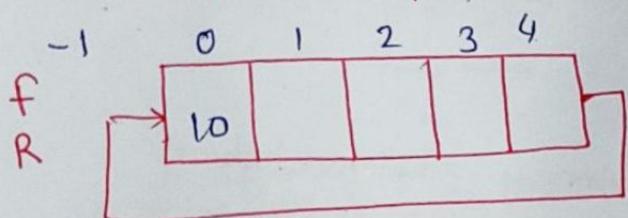


⑩



if $((R+1) \% \text{ maxsize} == \text{front})$
printf("Overflow")

Case 2:- Queue is empty



~~if ($R \neq -1$)~~ item = 10

if ($R == -1$)

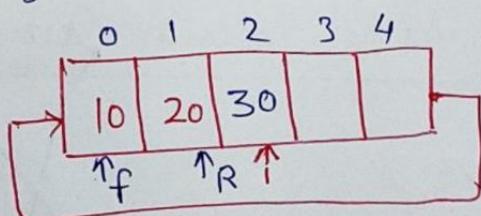
$f=R=0$

$cq[R] = \text{item}$

Case 3:- Queue is neither empty nor full

$R=(R+1) \% \text{ maxsize}$ item = 30

if $cq[R] = \text{item}$



Algorithm →

Qinsert (Queue[maxsize], item, front, rear)

1. if $(\text{rear}+1) \% \text{ maxsize} == \text{front}$ then
write "Overflow"

2. if ($\text{Rear} == -1$) then
Set ~~front~~ $\text{front}=0$, $\text{rear}=0$

else

Set $\text{rear} = (\text{rear}+1) \% \text{ maxsize}$

3. Queue[rear] = item
 4. Exit.

(11)

C function →

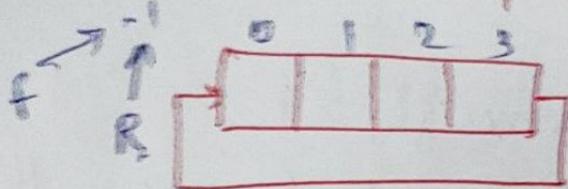
```
#define maxsize 30
int cq[maxsize], front=-1, rear=-1 //global declaration

void insert()
{
    int item;
    if ((rear+1)%maxsize == front)
    {
        printf("Overflow");
        exit(0);
    }
    if (rear == -1)
        front = rear = 0;
    else
        rear = (rear+1)%maxsize;
    printf("Enter item");
    scanf("%d", &item);
    cq[rear] = item;
}
```

2) Deletion →

(12)

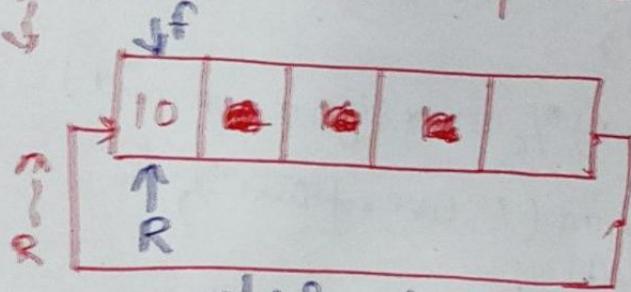
case 1:- Queue is empty



if (front == -1)

printf("Underflow");

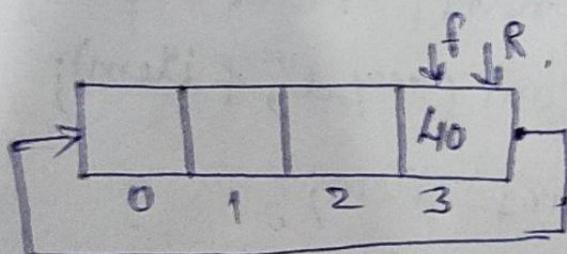
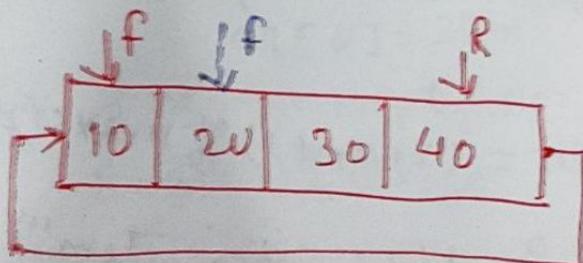
case 2: Queue has only one item



if (front == rear)

front = rear = -1

case 3: other wise



front = (front+1) % maxsize

Algorithm →

(13)

② Circular-Queue-delete()

1. if ($\text{front} == -1$) then
 write "Underflow" and exit.
2. $\text{item} = \text{Queue}[\text{front}]$
3. if ($\text{front} == \text{rear}$) then
 $\text{front} = \text{rear} = -1$
else
 $\text{front} = (\text{front} + 1) \% \text{maxSize}$
 [End of if]
4. write item "is deleted"
5. Exit.

C function →

```
void deletion()
{
    int item;
    if ( $\text{front} == -1$ ) then
    {
        printf("Underflow");
        exit(0);
    }
    item = cq[front];
    if ( $\text{front} == \text{rear}$ )
        front = rear = -1;
    else
        front = (front + 1) % maxSize;
    printf("old is deleted", item);
}
```

Traverse → concept →

(14)

C/C++

Case 1:- Queue is empty

If (front == -1)

printf("Queue is empty");

Case 2:- Queue is not empty

for (i = front; i != rear; i = (i + 1) % maxsize)

printf("%d", cq[i]);

printf("%d", cq[i]);

Algorithm →

Traverse()

1. if (front == -1)

 write "Queue is empty & exit.

2. ~~i = front~~ i = front

3. repeat step 4 & 5

~~until i > rear~~ until (i != rear)

4. write Queue[i]

5. i = (i + 1) mod maxsize

6. write Queue[i]

7. Exit

C function →

(15)

```

void traverse()
{
    if (front == -1)
    {
        printf("Queue is empty");
        exit(0);
    }

    for (i = front; i != rear; i = (i + 1) % maxsize)
        printf("%d", cq[i]);
        printf("%d", cq[i]);
}

```

Circular Queue (linked list implementation) →

struct node

{

int info;

struct node *next;

} *front=NULL, *rear=NULL;

↳ insertion → concept

case 1 → Over flow condition
 $\text{new} = \text{malloc}$)
if ($\text{new} == \text{NULL}$)
 printf("overflow");

Case 2 Queue is empty

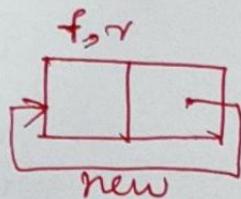
if (front == rear == NULL)

f, r = NULL
↓

front = new;

rear = new;

rear->next = front;

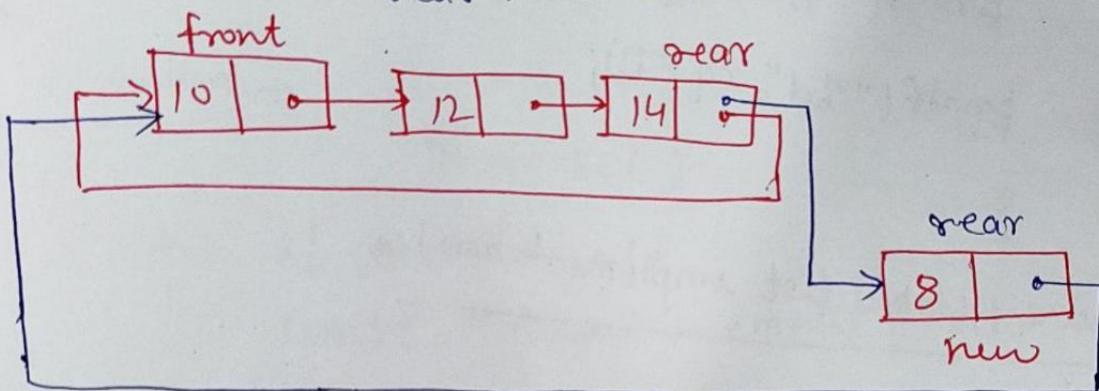


Case 3 -

rear->next = new

rear = new

rear->next = front



Algorithm → ginsert()

1. new = AVAIL
2. if (new == NULL)
 write "Overflow" & exit.
3. if (rear == NULL) then
 front = rear = new
 LINK[rear] = front
 else
 LINK[rear] = new
 rear = new
 LINK[rear] = front.
4. Exit.

C function →

(17)

```

void insert()
{
    struct node *new;
    new = (struct node *) malloc(sizeof(struct node));
    if (new == NULL)
    {
        printf("overflow");
        exit(0);
    }
    if (rear == NULL)
    {
        front = rear = new;
        rear->next = front;
    }
    else
    {
        rear->next = new;
        rear = new;
        rear->next = front;
    }
}

```

2) Deletion → concept-

\downarrow \downarrow
 f R
 NULL

case 1 → Queue is empty

if (front == NULL)

printf("underflow");

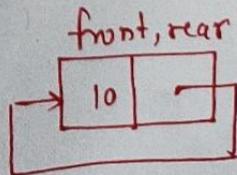
Case 2 → Queue contains only one node

if (front == rear)

{

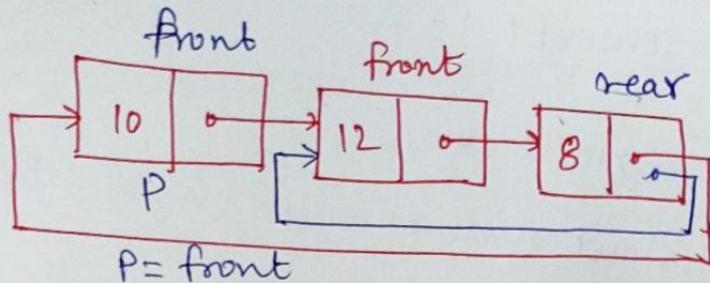
p = front

front = rear = NULL



case3 → Queue contains more than one node.

(18)



$P = \text{front}$

$\text{front} = \text{front} \rightarrow \text{next}$

$\text{rear} \rightarrow \text{next} = \text{front}$

$\text{free}(P)$

Algorithm →

$\text{deletion}()$

1. if ($\text{front} == \text{NULL}$) then
write "Queue is underflow" & exit.
 2. $P = \text{front}$
 3. if ($\text{front} == \text{rear}$) then
 $\text{front} = \text{rear} = \text{NULL}$
 $\text{free}(P)$
else
 $\text{front} = \text{front} \rightarrow \text{next}$
 $\text{rear} \rightarrow \text{next} = \text{front}$
 $\text{free}(P)$
 4. exit
- $\text{if } (\text{front} == \text{rear}) \text{ then}$
 $\text{front} = \text{rear} = \text{NULL}$
 $\text{free}(P)$
- else
 $\text{front} = \text{LINK}[\text{front}]$
 $\text{LINK}[\text{rear}] = \text{front}$
 $\text{free}(P)$
4. Exit.

C function →

```
void deletion()
{
    struct node *P;
    if (front == NULL)
    {
        printf("Queue is underflow");
        exit(0);
    }
}
```

(19)

```

P = front;
if (front == rear) then
{
    front = rear = NULL;
    free(P);
}
else
{
    front = front->next;
    rear->next = front;
    free(P);
}

```

3) Traverse or display:-

Concept →

Case 1:- Queue is empty

if (front == NULL)
printf("Queue is empty");

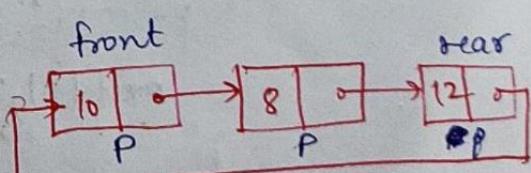
Case 2:- Queue is not empty

P = front;
do
{

printf("%d", p->info)

P = P->next;

} while (P != front) ~~while (P != front)~~



Algorithm

Q

Traverse()

1. if (front == NULL) then
 write " Queue is empty" & exit.
2. P = front
3. ~~do~~ write INFO[P]
4. P = LDNR[P]
5. while (P != front) repeat steps 5 & 6
6. write INFO[P]
6. P = LINK[P]
- [END of while]
7. Exit.

C function →

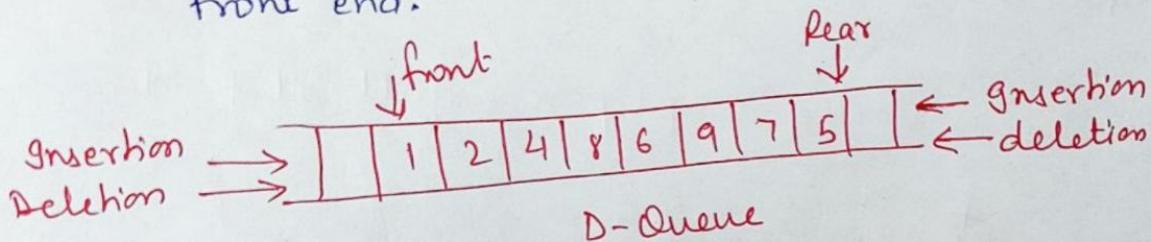
```
void traverse()
{
    struct node *p;
    if (front == NULL)
    {
        printf(" Queue is empty");
        exit(0);
    }
    p = front;
    do
    {
        printf("%d", p->info);
        p = p->next;
    } while (p != front);
}
```

3

Double ended Queue → (D-Queue)

(21)

In a D-Queue both insertion and deletion operations are performed at either end of the queue. i.e., we performed insertion and deletion from rear as well as front end.



Types of D-Queue

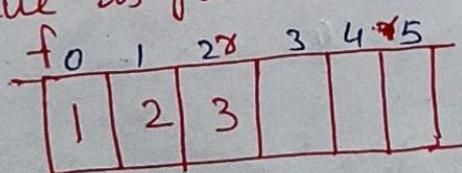
- i) Input restricted D Queue : Element can be added at only one end but we can delete the element from both end.
- ii) Output restricted D Queue : Element can be deleted only from one end but allow insertion at both ends.

Operations on D-Queue → (Array implementation)

(1) Insertion at front

Concept →

Case 1 → Queue is full at front



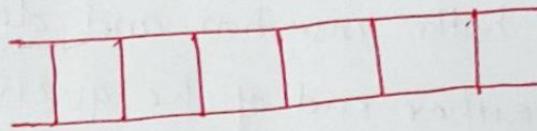
if (front == 0)

printf("overflow");

Case 2 → Queue is empty

(22)

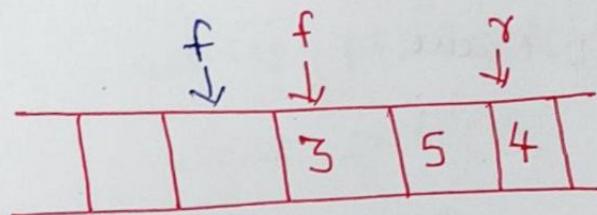
$$\begin{array}{l} f = -1 \\ r = -1 \end{array}$$



if (front == -1 or rear == -1)

front = rear = 0

case 3:- Queue is neither empty nor full at front



front = front - 1;

DQ[front] = item

Algorithm →

gnsert-at-front()

1. Read item

2. if (front == 0) then

 write "Overflow" & exit

3. if (front == -1)

 front = rear = 0

4. else

 front = front - 1

5. DQ[front] = item

6. Exit