



LAB 6 SALES OF A COMPANY



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Lab 6

Sales Of a Company

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Case situation:

You are a VP of sales and have responsibility for 41 stores. You have collected data from the stores on advertising costs, store size in square feet, % employee retention, customer satisfaction score, whether a promotion was run or not, and sales. You want to build a model that can predict sales based on these five variables.

Fit a best multiple linear regression model to predict the sales using the forward selection backward elimination procedure. Prepare a report based on the above questions with introduction, analysis, and conclusions.

Step1: Import dataset

```
library(readxl)
vps <- read_excel("C:/Users/mayur/Desktop/Mstat/Semesters/Tri-sem2/Regression/Dataset/vps.xlsx")
View(vps)
attach(vps)
```

Forward selection

Step2:

Fit a regression only with the constant term $y=b_0$

```
fitstart_1=lm(sales~1,data=vps)
fitstart_1

##
## Call:
## lm(formula = sales ~ 1, data = vps)
##
## Coefficients:
```

```
## (Intercept)
##          1210

summary(fitstart_1)

##
## Call:
## lm(formula = sales ~ 1, data = vps)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -1063.98  -310.98   -12.98    449.02   1298.02
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  1209.98      88.45    13.68  <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 566.3 on 40 degrees of freedom
```

Interpretation: 1210 is the intercept

Step3:forward procedure

```
fitall=lm(sales~.,data=vps)

fwd=step(fitstart_1,direction = "forward",scope=formula(fitall))

## Start:  AIC=520.8
## sales ~ 1
##
##              Df Sum of Sq      RSS      AIC
## + size         1   5737977  7091222  498.49
## + pro           1   5169224  7659975  501.66
## + cust_sat      1   5121575  7707624  501.91
## + Adv_cost      1   4385811  8443388  505.65
## <none>                          12829199  520.80
## + `%-emp_ret`   1       86968 12742231  522.52
## + store         1        1604 12827595  522.80
##
## Step:  AIC=498.49
## sales ~ size
##
##              Df Sum of Sq      RSS      AIC
## + pro         1   1729572  5361650  489.03
```

```

## + Adv_cost      1    1010282 6080940 494.19
## + cust_sat      1     786890 6304331 495.67
## + `%-emp_ret`   1     673165 6418057 496.40
## <none>                                7091222 498.49
## + store         1      24801 7066421 500.35
##
## Step:  AIC=489.03
## sales ~ size + pro
##
##           Df Sum of Sq    RSS    AIC
## + cust_sat  1    1678748 3682903 475.63
## + Adv_cost  1    1246351 4115299 480.18
## <none>                                5361650 489.03
## + `%-emp_ret` 1     138181 5223469 489.96
## + store      1      13876 5347775 490.92
##
## Step:  AIC=475.63
## sales ~ size + pro + cust_sat
##
##           Df Sum of Sq    RSS    AIC
## + Adv_cost  1     308276 3374626 474.05
## <none>                                3682903 475.63
## + `%-emp_ret` 1     136615 3546288 476.08
## + store      1      71008 3611894 476.83
##
## Step:  AIC=474.05
## sales ~ size + pro + cust_sat + Adv_cost
##
##           Df Sum of Sq    RSS    AIC
## + `%-emp_ret` 1     189767 3184859 473.67
## <none>                                3374626 474.05
## + store      1      27669 3346957 475.71
##
## Step:  AIC=473.67
## sales ~ size + pro + cust_sat + Adv_cost + `%-emp_ret`
##
##           Df Sum of Sq    RSS    AIC
## <none>                                3184859 473.67
## + store  1     11055 3173804 475.53

fwd

##
## Call:

```

```
## lm(formula = sales ~ size + pro + cust_sat + Adv_cost + `_%_emp_ret`,
##     data = vps)
##
## Coefficients:
## (Intercept)          size          pro      cust_sat      Adv_cost  `_%_emp_re
t`
## -1.762e+03    2.122e-02    5.208e+02    4.000e+01    4.751e+00    8.087e+
00
```

note: smaller AIC explains better about the variability, hence the appropriate model suggested according to forward selection is a regression between dependent variable as sales and regressors as size, promotion, customer satisfaction, advertisement cost and employment retention.

Step4: Fitting and significance of variable.

```
summary(fwd)

##
## Call:
## lm(formula = sales ~ size + pro + cust_sat + Adv_cost + `_%_emp_ret`,
##     data = vps)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -752.58  -78.54   33.32  165.38  560.34
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -1.762e+03  6.311e+02  -2.792 0.008432 **
## size         2.122e-02  2.052e-02   1.034 0.308304
## pro          5.208e+02  1.187e+02   4.386 0.000101 ***
## cust_sat     4.000e+01  1.446e+01   2.766 0.009005 **
## Adv_cost     4.751e+00  2.384e+00   1.993 0.054107 .
## `_%_emp_ret`  8.087e+00  5.600e+00   1.444 0.157602
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 301.7 on 35 degrees of freedom
## Multiple R-squared:  0.7517, Adjusted R-squared:  0.7163
## F-statistic: 21.2 on 5 and 35 DF, p-value: 1.052e-09

library(car)

## Loading required package: carData
```

```
vif(fwd)
```

```
##           size           pro    cust_sat    Adv_cost `_%_emp_ret`  
##    2.966729    1.579684    2.579197    1.819381    1.431279
```

here we observe that the significant variables at a 0.1 level of significance(for convenience) are promotion,customer satisfaction,advertisement cost. also all the variables do not have multicollinearity since $vif < 5$.

Step5: Choosing the model

```
fit1=lm(sales~pro+cust_sat+Adv_cost,data=vps)
```

```
fit1
```

```
##
```

```
## Call:
```

```
## lm(formula = sales ~ pro + cust_sat + Adv_cost, data = vps)
```

```
##
```

```
## Coefficients:
```

```
## (Intercept)           pro    cust_sat    Adv_cost  
##   -899.824       608.785       45.130        4.456
```

```
summary(fit1)
```

```
##
```

```
## Call:
```

```
## lm(formula = sales ~ pro + cust_sat + Adv_cost, data = vps)
```

```
##
```

```
## Residuals:
```

```
##      Min       1Q   Median       3Q      Max  
## -754.81 -126.44   -8.95   222.87   495.28
```

```
##
```

```
## Coefficients:
```

```
##              Estimate Std. Error t value Pr(>|t|)  
## (Intercept) -899.824    262.839  -3.423  0.001525 **  
## pro          608.785     96.399   6.315  2.35e-07 ***  
## cust_sat     45.130     11.991   3.764  0.000581 ***  
## Adv_cost      4.456      2.370   1.880  0.068007 .
```

```
## ---
```

```
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
##
```

```
## Residual standard error: 303 on 37 degrees of freedom
```

```
## Multiple R-squared:  0.7353, Adjusted R-squared:  0.7138
```

```
## F-statistic: 34.26 on 3 and 37 DF, p-value: 8.975e-11
```

here we observe that all the variables are significant. the adjusted R^2 $0.7138 > 0.5$ thus the model is significant. hence the model is $y = -899.82 + 608 * x_1 + 45.13 x_2 + 4.456 x_3 + e$ where y = sales x_1 = promotion x_2 = customer satisfaction x_3 = advertisement cost

Backward Selection:

```
fitall=lm(sales~.,data=vps)

bwd2=step(fitall,direction = "backward",scope=formula(fitall))

## Start:  AIC=475.53
## sales ~ store + Adv_cost + size + `%_emp_ret` + cust_sat + pro
##
##           Df Sum of Sq    RSS   AIC
## - store      1     11055 3184859 473.67
## - size       1      91525 3265330 474.70
## <none>                        3173804 475.53
## - `%_emp_ret` 1     173153 3346957 475.71
## - Adv_cost    1      322186 3495991 477.50
## - cust_sat    1       703122 3876927 481.74
## - pro         1     1761184 4934988 491.63
##
## Step:  AIC=473.67
## sales ~ Adv_cost + size + `%_emp_ret` + cust_sat + pro
##
##           Df Sum of Sq    RSS   AIC
## - size       1      97258 3282117 472.91
## <none>                        3184859 473.67
## - `%_emp_ret` 1     189767 3374626 474.05
## - Adv_cost    1      361429 3546288 476.08
## - cust_sat    1      696073 3880932 479.78
## - pro         1     1750531 4935390 489.63
##
## Step:  AIC=472.91
## sales ~ Adv_cost + `%_emp_ret` + cust_sat + pro
##
##           Df Sum of Sq    RSS   AIC
## - `%_emp_ret` 1     113860 3395978 472.31
## <none>                        3282117 472.91
## - Adv_cost    1      372946 3655063 475.32
## - cust_sat    1     1405913 4688030 485.52
## - pro         1     3362431 6644548 499.83
##
```

```
## Step: AIC=472.31
## sales ~ Adv_cost + cust_sat + pro
##
##           Df Sum of Sq    RSS   AIC
## <none>                 3395978 472.31
## - Adv_cost   1     324381 3720358 474.05
## - cust_sat   1    1300060 4696037 483.59
## - pro        1    3660523 7056501 500.29

bwd2

##
## Call:
## lm(formula = sales ~ Adv_cost + cust_sat + pro, data = vps)
##
## Coefficients:
## (Intercept)      Adv_cost      cust_sat          pro
##    -899.824         4.456        45.130        608.785
```

note: smaller AIC explains better about the variability, hence the appropriate model suggested according to backward selection is a regression between dependent variable as sales and regressors as size, promotion, customer satisfaction, advertisement cost.

```
fit1=lm(sales~pro+cust_sat+Adv_cost,data=vps)
fit1

##
## Call:
## lm(formula = sales ~ pro + cust_sat + Adv_cost, data = vps)
##
## Coefficients:
## (Intercept)          pro      cust_sat      Adv_cost
##    -899.824        608.785        45.130         4.456

summary(fit1)

##
## Call:
## lm(formula = sales ~ pro + cust_sat + Adv_cost, data = vps)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -754.81 -126.44   -8.95   222.87  495.28
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -899.824    262.839  -3.423  0.001525 **
```



```
## pro          608.785      96.399    6.315 2.35e-07 ***
## cust_sat      45.130      11.991    3.764 0.000581 ***
## Adv_cost       4.456       2.370    1.880 0.068007 .
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 303 on 37 degrees of freedom
## Multiple R-squared:  0.7353, Adjusted R-squared:  0.7138
## F-statistic: 34.26 on 3 and 37 DF,  p-value: 8.975e-11
```

Here we observe that all the variables are significant. the adjusted R^2 $0.7138 > 0.5$ thus the model is significant.

Hence the model is,

$$y = -899.82 + 608 * x_1 + 45.13 x_2 + 4.456 x_3 + e$$

where ,

y = sales x_1 = promotion x_2 = customer satisfaction x_3 = advertisement cost

Validating the Built Model

Multicollinearity

```
library(car)
vif(fit1)

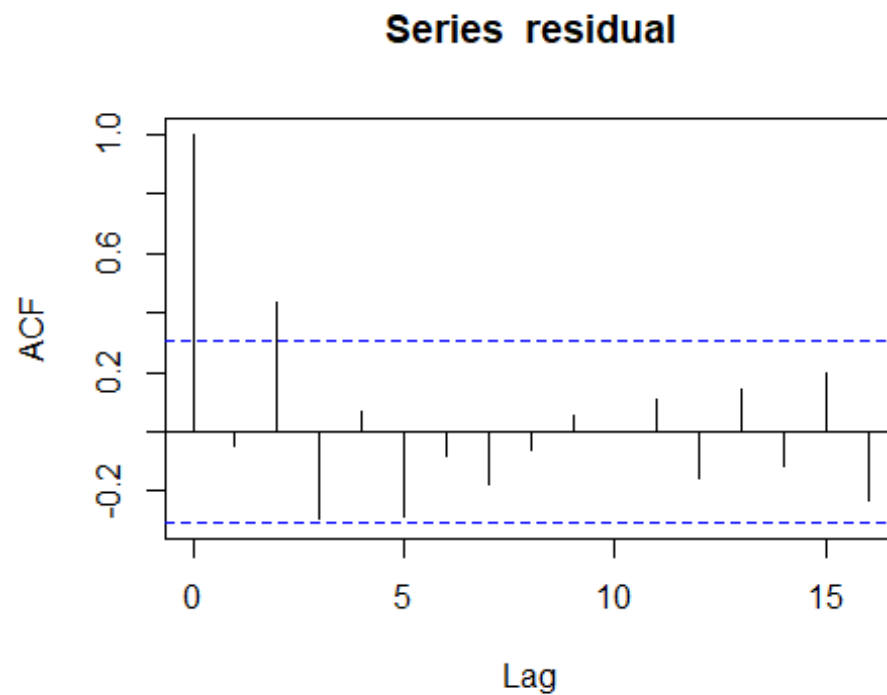
##          pro cust_sat Adv_cost
## 1.032233 1.757675 1.783104
```

Interpretation :

Here we observe that all the vif values are less than 5. thus there exist no multi-collinearity in the model.

Autocorrelation

```
residual=resid(fit1)
acf(residual)
```



Interpretation and Recommendation:

we observe there exist an auto-correlation in the model. thus, we need to include correction measures such as,

- 1) removing a few variables and refitting the model.
- 2) relax the assumptions by using transformation.
- 3) adopt nonlinear regression modeling